# **Symbol Tables**

► API

- ▶ sequential search
- binary search
- ▶ applications
- ▶ challenges

### Symbol tables

### Key-value pair abstraction.

- Insert a value with specified key.
- Given a key, search for the corresponding value.

### Ex. DNS lookup.

- Insert URL with specified IP address.
- Given URL, find corresponding IP address.

URL	IP address
www.cs.princeton.edu	128.112.136.11
www.princeton.edu	128.112.128.15
www.yale.edu	130.132.143.21
www.harvard.edu	128.103.060.55
www.simpsons.com	209.052.165.60
1	
key	value

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### Symbol table applications

application	purpose of search	key	value	
dictionary	look up word	word	definition	
book index	find relevant pages	term	list of page numbers	
file share	find song to download	name of song	computer ID	
financial account	process transactions	account number	transaction details	
web search	find relevant web pages	keyword	list of page names	
compiler	find properties of variables	variable name	value and type	
routing table	route Internet packets	destination	best route	
DNS	find IP address given URL	URL	IP address	
reverse DNS	find URL given IP address	IP address	URL	
genomics	find markers	DNA string	known positions	
file system	find file on disk	filename	location on disk	

### Symbol table API

Associative array abstraction. Associate one value with each key.

public	1		
	*ST()	create a symbol table	
void	<pre>put(Key key, Value val)</pre>	put key-value pair into the table	<pre>a[key] = val;</pre>
Value	get(Key key)	return value paired with key	← a[key]
boolean	contains (Key key)	is there a value paired with key?	
void	remove(Key key)	remove key-value pair from table	
Iterator <key></key>	iterator()	iterator through keys in table	

### Conventions

- Values are not null.
- Method get () returns null if key not present.
- Method put () overwrites old value with new value.

### Intended consequences.

• Easy to implement contains().

public boolean contains(Key key)
{ return get(key) != null; }

• Can implement lazy version of remove ().

# public boolean remove(Key key) { put(key, null); }

### Keys and values

Value type. Any generic type.

### Key type: several natural assumptions.

- Assume keys are comparable, USE compareTo().
- Assume keys are any generic type, use equals () to test equality.
- Assume keys are any generic type, use equals() to test equality and hashcode() to scramble key.

Best practices. Use immutable types for symbol table keys.

- Immutable in Java: string, Integer, BigInteger, ...
- Mutable in Java: Date, GregorianCalendar, StringBuilder, ...

### ST test client

Build ST by associating value i with ith command-line argument.

```
public static void main(String[] args)
{
   ST<String, Integer> st = new ST<String, Integer>();
   for (int i = 0; i < args.length; i++)
      st.put(args[i], i);
   for (String s : st)
      StdOut.println(s + " " + st.get(s));
}</pre>
```

```
        keys
        S
        E
        A
        R
        C
        H
        E
        X
        A
        M
        P
        L
        E

        values
        0
        1
        2
        3
        4
        5
        6
        7
        8
        9
        10
        11
        12
```

STunordered output (one possibility)		ST o	utput
L	11	Α	8
Р	10	С	4
М	9	E	12
Х	7	Н	5
н	5	L	9
C	4	М	11
R	3	Р	10
Α	8	R	3
E	12	S	0
S	0	Х	7

### Elementary ST implementations

- Sequential search.
- Binary search.
- Array vs. linked list.

### Why study elementary implementations?

- Performance benchmarks.
- API details need to be worked out.
- Basis for advanced implementations.
- Method of choice can be one of these in many situations.

Remark. Always good practice to study elementary implementations.

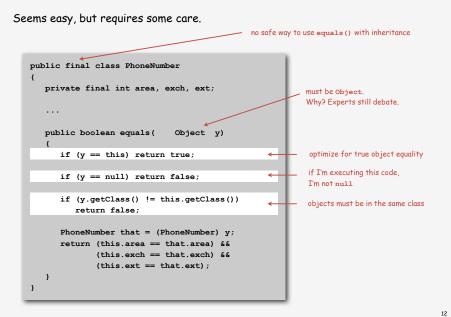
	Java conventions for equals()
	All Java objects implement a method equals().
	Default implementation: (x == y) do x and y refer to the same object?
<ul> <li>API</li> <li>sequential search</li> <li>binary search</li> <li>applications</li> <li>challenges</li> </ul>	<ul> <li>Equivalence relation. For any references x, y and z:</li> <li>Reflexive: x.equals(x) is true.</li> <li>Symmetric: x.equals(y) iff y.equals(x).</li> <li>Transitive: if x.equals(y) and y.equals(z), then x.equals(z).</li> <li>Non-null: x.equals(null) is false.</li> </ul>
	Customized implementations. string, URL, Integer, User-defined implementations. Some care needed.

### Implementing equals ()

### Seems easy.

public class PhoneNumber
<pre>{     private final int area, exch, ext;</pre>
<pre>public boolean equals(PhoneNumber y) {</pre>
ι.
PhoneNumber that = (PhoneNumber) y; return (this.area == that.area) &&
(this.exch == that.exch) &&
<pre>(this.ext == that.ext); }</pre>
}

### Implementing equals ()



### Unordered linked-list ST implementation

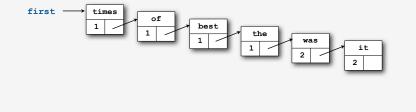
### Maintain a linked list with keys and values.

### Inner Node class.

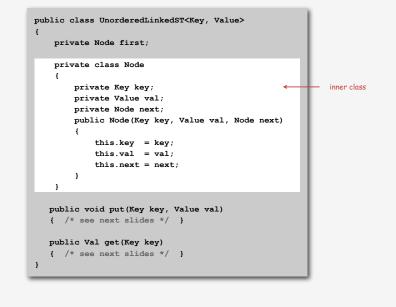
- Instance variable key holds the key.
- Instance variable val holds the value.

### Instance variable(s):

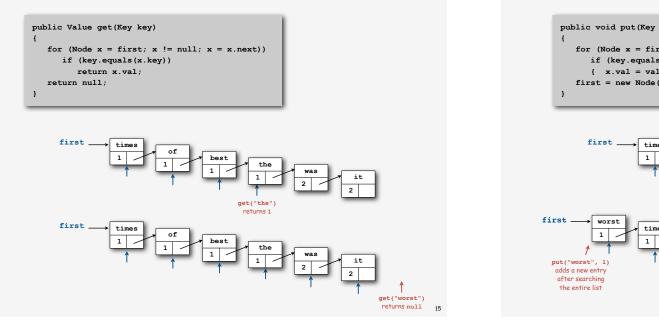
• Node first refers to the first node in the list.







### Unordered linked-list ST implementation (search)



Node data type

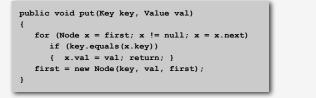
key

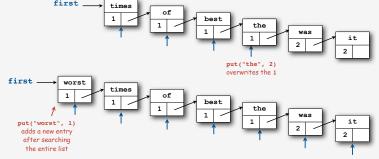
next

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val

### Unordered linked-list ST implementation (insert)





1		first red nodes
S	0	
Е	1	$E 1 \longrightarrow S 0 \qquad \qquad black nodes are accessed$
А	2	$A \rightarrow E \rightarrow S \rightarrow O$ in search
R	3	
С	4	
Н	5	$H \xrightarrow{5} C \xrightarrow{4} R \xrightarrow{3} A \xrightarrow{2} E \xrightarrow{1} S \xrightarrow{0} changed values$
Е	6	$H = S \rightarrow C = A \rightarrow R = A \rightarrow A \rightarrow C \rightarrow$
Х	7	$X 7 \rightarrow H 5 \rightarrow C 4 \rightarrow R 3 \rightarrow A 2 \rightarrow E 6 \rightarrow S 0$
А	8	$X 7 \rightarrow H 5 \rightarrow C 4 \rightarrow R 3 \rightarrow A 8 \rightarrow E 6 \rightarrow S 0 \leftarrow gray nodes are untouched$
М	9	$ \boxed{M 9 \rightarrow X 7 \rightarrow H 5 \rightarrow C 4 \rightarrow R 3 \rightarrow A 8 \rightarrow E 6 \rightarrow S 0 } $
Р	10	$ \begin{array}{c} P \\ 10 \end{array} \rightarrow M \\ 9 \end{array} \rightarrow X \\ 7 \end{array} \rightarrow H \\ 5 \end{array} \rightarrow C \\ 4 \end{array} \rightarrow R \\ 3 \end{array} \rightarrow A \\ 8 \end{array} \rightarrow E \\ 6 \end{array} \rightarrow S \\ 0 \end{array} $
L	11	$ \begin{array}{c} \hline L 11 \rightarrow P 10 \rightarrow M 9 \rightarrow X 7 \rightarrow H 5 \rightarrow C 4 \rightarrow R 3 \rightarrow A 8 \rightarrow E 6 \rightarrow S 0 \end{array} $
Е	12	$ \begin{array}{c} \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \$
		Trace of linked-list ST implementation for standard indexing client

### Unordered array ST implementation

Maintain two parallel arrays with keys and values.

### Instance variables.

- keys[i] holds the ith smallest key.
- vals[i] holds the value associated with the ith smallest key.
- N holds the number of entries.

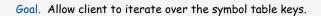
								N = 6	
		0	1	2	3	4	5	6	7
keys [	1	it	was	the	best	of	times	null	null
vals[	1	2	2	1	1	1	1	null	null

### ST implementations: summary

	worst	t case	averag	e case	operations	
ST implementation	search	insert	search hit	insert	on keys	
unordered array	Ν	Ν	N / 2	Ν	equals()	
unordered list	Ν	Ν	N / 2	Ν	equals()	

Challenge. Efficient implementations of search and insert.

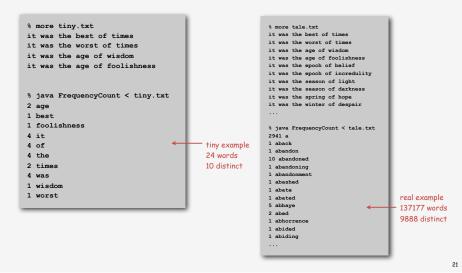
### Iterators



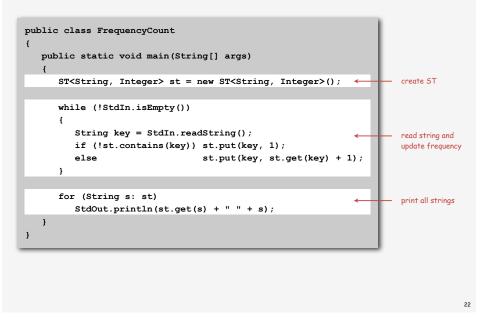
<pre>import java.util.Iterator;</pre>
<pre>public class UnorderedLinkedST<key, value=""> implements Iterable<key> {    </key></key,></pre>
<pre>public Iterator<key> iterator() { return new ListIterator(); }</key></pre>
<pre>private class ListIterator implements Iterator<key> {</key></pre>
<pre>private Node current = first;</pre>
<pre>public boolean hasNext() { return current != null; }</pre>
<pre>public void remove() { }</pre>
<pre>public Key next()</pre>
{     Key key = current.key;
current = current.next;
return key;
}
}

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# Goal. Read a sequence of strings from standard input and print out the number of times each string appears.



### Iterable ST client: frequency counter



### Iterable ST client: A problem?

more tiny.txt	<pre>% more tiny.txt</pre>			
it was the best of times	it was the best of times			
it was the worst of times	it was the worst of times			
it was the age of wisdom	it was the age of wisdom			
it was the age of foolishness	it was the age of foolishness			
<pre>% java FrequencyCount &lt; tiny.txt</pre>	<pre>% java FrequencyCount &lt; tiny.txt</pre>			
2 age	1 foolishness			
1 best	1 wisdom			
1 foolishness	2 age			
4 it	1 worst			
4 of	2 times			
4 the	4 of			
2 times with one ST implementation	1 best with UnorderedLinkedListST			
4 was	4 the			
1 wisdom	4 was			
1 worst	4 it.			

Remark. No requirement that keys are iterated in natural order.

- Not in basic API.
- Not a requirement for some clients.
- Not a problem if postprocessing, e.g. with sort or grep.

### ST implementations: summary

	worst case		average case		ordered	operations
ST implementation	search	insert	search hit	insert	iteration?	on keys
unordered array	N	Ν	N / 2	Ν	no	equals()
unordered list	Ν	Ν	N / 2	Ν	no	equals()

Challenge. Efficient implementations of search, insert, and ordered iteration.

# API sequential search binary search

### Ordered array ST implementation

### Assumption. Keys are comparable.

### Instance variables.

- keys[i] holds the ith smallest key.
- vals[i] holds the value associated with the ith smallest key.
- $\mathbf{N}$  holds the number of entries.

							*	
	0	1	2	3	4	5	6	7
keys[]	best	it	of	the	times	was	null	null
vals[]	1	2	1	1	1	2	null	null

### Main reasons to consider using ordered arrays.

- Provides ordered iteration (for free).
- Can use binary search to significantly speed up search.

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### Unordered array ST implementation (skeleton)

public class OrderedArrayST<Key extends Comparable<Key>, Value> £ than defining a type for entries private Key[] keys; private int N; public OrderedArrayST(int capacity) array doubling code omitted ł keys = (Key[]) new Comparable[capacity]; vals = (Value[]) new Object[capacity]; } public boolean isEmpty() { return N == 0; } public void put(Key key, Value val) { /\* see next slides \*/ } public Value get(Key key) { /\* see next slides \*/ } }

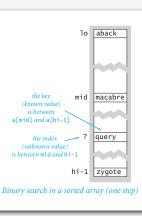
### Binary search

Given a sorted array, determine index associated with a given key.

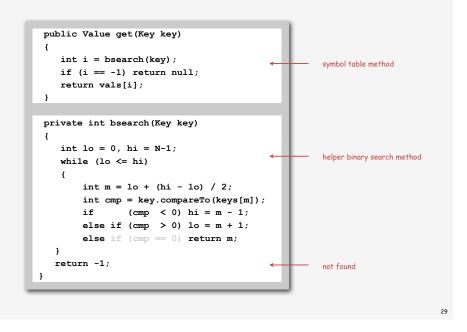
Ex. Dictionary, phone book, book index, ...

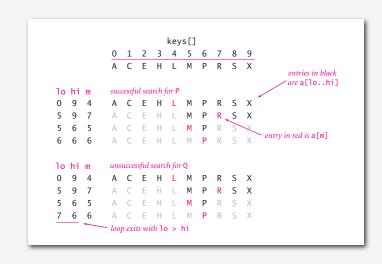
### Binary search algorithm.

- Examine the middle key.
- If it matches, return its index.
- Otherwise, search either the left or right half.



N = 6





### Binary search: mathematical analysis

Proposition. Binary search uses  $\sim \lg N$  compares to search any array of size N.

**Def.** T(N) = number of compares to binary search in a sorted array of size N.

$$= T(N/2) + 1$$

$$\uparrow$$
left or right half

Binary search recurrence. T(N) = T(N/2) + 1 for N > 1, with T(1) = 0.

- Not quite right for odd N.
- Same recurrence holds for many algorithms.

### Solution. $T(N) \sim \lg N$ .

- For simplicity, we'll prove when N is a power of 2.
- True for all N. [see COS 340]

### Binary search recurrence

Binary search recurrence. T(N) = T(N/2) + 1 for N > 1, with T(1) = 0.

Proposition. If N is a power of 2, then  $T(N) = \lg N$ . Pf.

$$T(N) = T(N/2) + 1$$

$$= T(N/4) + 1 + 1$$

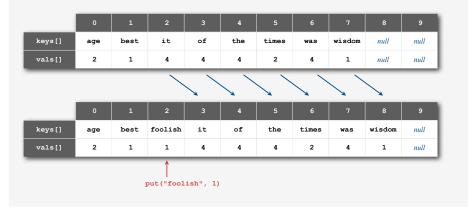
$$= T(N/8) + 1 + 1 + 1$$
apply recurrence to first term
apply recurrence to first term
$$T(N/N) + 1 + 1 + \dots + 1$$

$$= Ig N$$

### Ordered array ST implementation (insert)

### Binary search is little help for insert.

- Can find where to insert new key.
- But still need to move larger keys.



### Ordered array ST implementation: an important special case

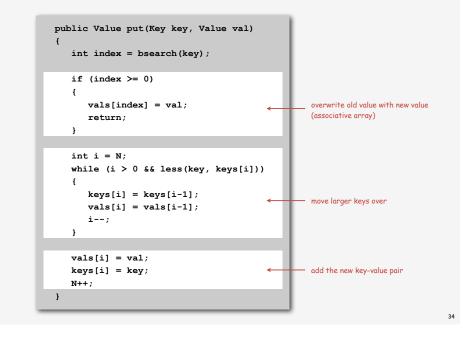
### Method of choice for some clients.

- Sort database by key.
- Insert N key-value pairs in order by key.
- Support searches that never use more than Ig N compares.
- Support occasional (expensive) inserts.

Remark. Takes linear time to insert N keys that are in ascending order if we add the following check to <code>bsearch()</code>.

```
int cmp = key.compareTo(keys[N-1]);
if (cmp == 0) return N-1;
if (cmp > 0) return -1;
```

### Ordered array ST implementation (insert)



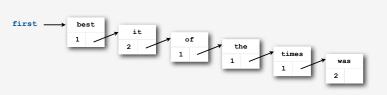
### Ordered linked-list ST implementation

Binary search depends on array indexing for efficiency.

- Q. How to jump to the middle of a linked list?
- A. You can't do it efficiently.

### Ordered link-list ST advantages.

- Support ordered iterator (for free).
- Cuts search/insert time in half (on average) for random search/insert.



CT implementation	worst case		average case		ordered	operations	
ST implementation	search	insert	search hit	insert	iteration?	on keys	
unordered array	Ν	Ν	N / 2	Ν	no	equals()	
unordered list	Ν	Ν	N / 2	Ν	no	equals()	
ordered array	log N	Ν	log N	N / 2	yes	compareTo()	
ordered list	Ν	Ν	N / 2	N / 2	yes	compareTo()	

Next 3 lectures. Efficient implementations of search and insert.

URL is key IP is value



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### ST lookup client

### Command line arguments.

• A comma-separated value (CSV) file.

• Key field.

• Value field.

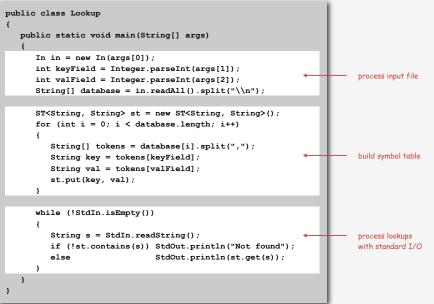
### Ex 1. DNS lookup.



### % more ip.csv

www.princeton.edu,128.112.128.15 www.cs.princeton.edu,128.112.136.35 www.math.princeton.edu,128.112.18.11 www.cs.harvard.edu,140.247.50.127 www.harvard.edu,128.103.60.24 www.yale.edu,130.132.51.8 www.econ.yale.edu,128.36.236.74 www.cs.yale.edu,128.36.229.30 espn.com,199.181.135.201 yahoo.com,66.94.234.13 msn.com,207.68.172.246 google.com,64.233.167.99 baidu.com,202.108.22.33 yahoo.co.jp,202.93.91.141 sina.com.cn,202.108.33.32 ebay.com,66.135.192.87 adobe.com,192.150.18.60 163.com,220.181.29.154 passport.net,65.54.179.226 tom.com, 61.135.158.237 nate.com,203.226.253.11 cnn.com,64.236.16.20 daum.net.211.115.77.211 blogger.com, 66.102.15.100 fastclick.com,205.180.86.4 wikipedia.org,66.230.200.100 rakuten.co.jp,202.72.51.22

### ST lookup client: Java implementation

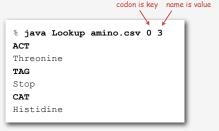


### ST lookup client

### Command line arguments.

- A comma-separated value (CSV) file.
- Key field.
- Value field.

### Ex 2. Amino acids.

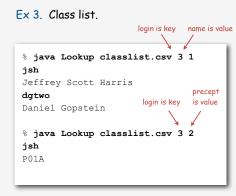


% more amino.csv TTT, Phe, F, Phenylalanine TTC, Phe, F, Phenylalanine TTA, Leu, L, Leucine TTG.Leu.L.Leucine TCT,Ser,S,Serine TCC.Ser.S.Serine TCA, Ser, S, Serine TCG,Ser,S,Serine TAT, Tyr, Y, Tyrosine TAC, Tyr, Y, Tyrosine TAA, Stop, Stop, Stop TAG, Stop, Stop, Stop TGT,Cys,C,Cysteine TGC,Cys,C,Cysteine TGA, Stop, Stop, Stop TGG, Trp, W, Tryptophan CTT, Leu, L, Leucine CTC, Leu, L, Leucine CTA, Leu, L, Leucine CTG, Leu, L, Leucine CCT, Pro, P, Proline CCC, Pro, P, Proline CCA, Pro, P, Proline CCG, Pro, P, Proline CAT, His, H, Histidine CAC, His, H, Histidine CAA.Gln.O.Glutamine CAG,Gln,Q,Glutamine CGT, Arg, R, Arginine CGC, Arg, R, Arginine

### ST lookup client

### Command line arguments.

- A comma-separated value (CSV) file.
- Key field.
- Value field.



% more classlist.csv 10, Bo Ling, P03, bling 10, Steven A Ross, P01, saross 10, Thomas Oliver Horton Conway, P03, oconway 08, Michael R. Corces Zimmerman, P01A, mcorces 09, Bruce David Halperin, P02, bhalperi 09,Glenn Charles Snyders Jr., P03,gsnyders 09, Siyu Yang, P01A, siyuyang 08, Taofik O. Kolade, P01, tkolade 09,Katharine Paris Klosterman, P01A,kkloster SP,Daniel Gopstein,P01,dgtwo 10, Sauhard Sahi, P01, ssahi 10.Eric Daniel Cohen.P01A.edcohen 09,Brian Anthony Geistwhite,P02,bgeistwh 09, Boris Pivtorak, P01A, pivtorak 09, Jonathan Patrick Zebrowski, P01A, jzebrows 09,Dexter James Doyle,P01A,ddoyle 09, Michael Weiyang Ye, P03, ye 08, Delwin Uy Olivan, P02, dolivan 08,Edward George Conbeer,P01A,econbeer 09, Mark Daniel Stefanski, P01, mstefans 09, Carter Adams Cleveland, P03, cclevela 10, Jacob Stephen Lewellen, P02, jlewelle 10,Ilya Trubov, P02,itrubov 09, Kenton William Murray, P03, kwmurray 07, Daniel Steven Marks, P02, dmarks 09, Vittal Kadapakkam, P01, vkadapak 10.Eric Ruben Domb.P01A.edomb 07, Jie Wu, P03, jiewu 08, Pritha Ghosh, P02, prithag 10, Minh Quang Anh Do, P01, mqdo

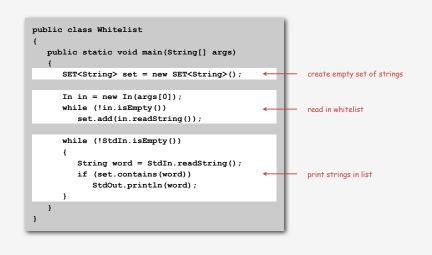
### Set API

### Mathematical set. A collection of distinct keys.

public	class SET <key extend<="" th=""><th>s Comparable<key>&gt;</key></th></key>	s Comparable <key>&gt;</key>
	SET ()	create an empty set
void	add (Key key)	add the key to the set
boolean	contains (Key key)	is the key in the set?
void	remove(Key key)	remove the key from the set
int	size()	return the number of keys in the set
Iterator <key></key>	iterator()	iterator through keys in the set

### Set client example: whitelist

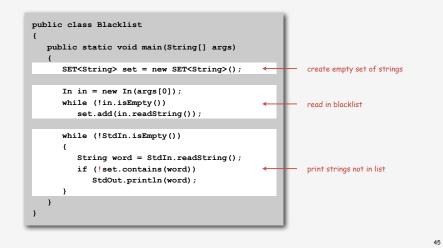
- Read in a list of words from one file.
- Print out all words from standard input that are in the list.



### Q. How to implement?

### Set client example: blacklist

- Read in a list of words from one file.
- Print out all words from standard input that not are in the list.



### Blacklist and whitelist applications

application	purpose	key	in list
spell checker	identify misspelled words	word	dictionary words
browser	mark visited pages	URL	visited pages
parental controls	block sites	URL	bad sites
chess	detect draw	board	positions
spam filter	eliminate spam	IP address	spam addresses
credit cards	check for stolen cards	number	stolen cards

### Searching challenge 1A

Problem. Maintain symbol table of song names for an iPod. Assumption A. Hundreds of songs.

### Which searching method to use?

- 1) Unordered array.
- 2) Ordered linked list.
- 3) Ordered array with binary search.
- 4) Need better method, all too slow.
- 5) Doesn't matter much, all fast enough.

### API

binary search

### challenges

### Searching challenge 1B

Problem. Maintain symbol table of song names for an iPod. Assumption B. Thousands of songs.

### Which searching method to use?

- 1) Unordered array.
- 2) Ordered linked list.
- 3) Ordered array with binary search.
- 4) Need better method, all too slow.
- 5) Doesn't matter much, all fast enough.

### Searching challenge 2A:

Problem. IP lookups in a web monitoring device. Assumption A. Billions of lookups, millions of distinct addresses.

### Which searching method to use?

- 1) Unordered array.
- 2) Ordered linked list.
- 3) Ordered array with binary search.
- 4) Need better method, all too slow.
- 5) Doesn't matter much, all fast enough.

### Searching challenge 2B

Problem. IP lookups in a web monitoring device. Assumption B. Billions of lookups, thousands of distinct addresses.

### Which searching method to use?

- 1) Unordered array.
- 2) Ordered linked list.
- 3) Ordered array with binary search.
- 4) Need better method, all too slow.
- 5) Doesn't matter much, all fast enough.

### Searching challenge 3

Problem. Frequency counts in "Tale of Two Cities." Assumptions. Book has 135,000+ words; about 10,000 distinct words.

### Which searching method to use?

- 1) Unordered array.
- 2) Ordered linked list.
- 3) Ordered array with binary search.
- 4) Need better method, all too slow.
- 5) Doesn't matter much, all fast enough.

### Searching challenge 4

Problem. Spell checking for a book.

Assumptions. Dictionary has 25,000 words; book has 100,000+ words.

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Which searching method to use?

- 1) Unordered array.
- 2) Ordered linked list.
- 3) Ordered array with binary search.
- 4) Need better method, all too slow.
- 5) Doesn't matter much, all fast enough.