

# Parallelism and Concurrency

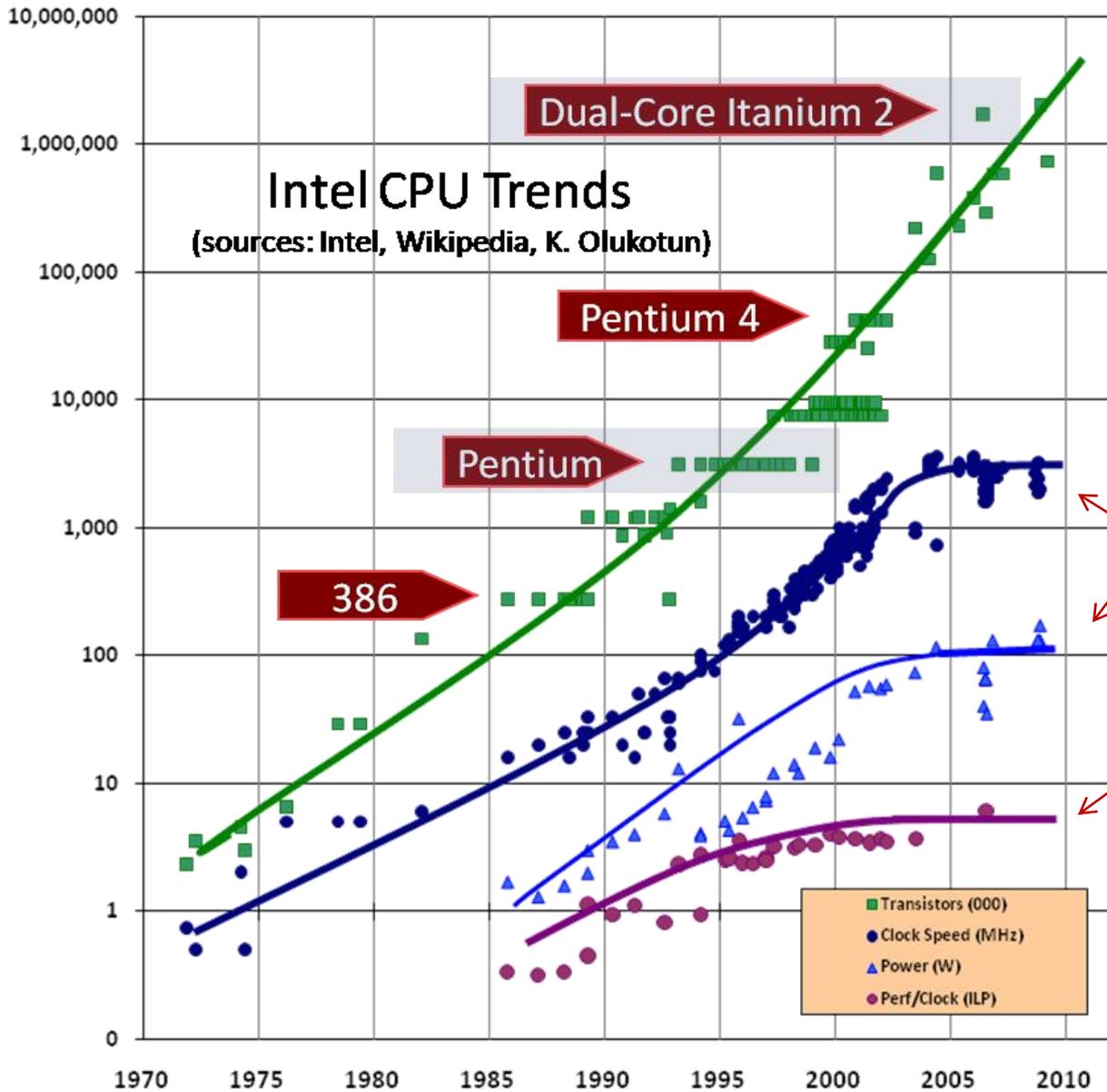
COS 326

David Walker

Princeton University

# Data Centers: Generation Z Super Computers

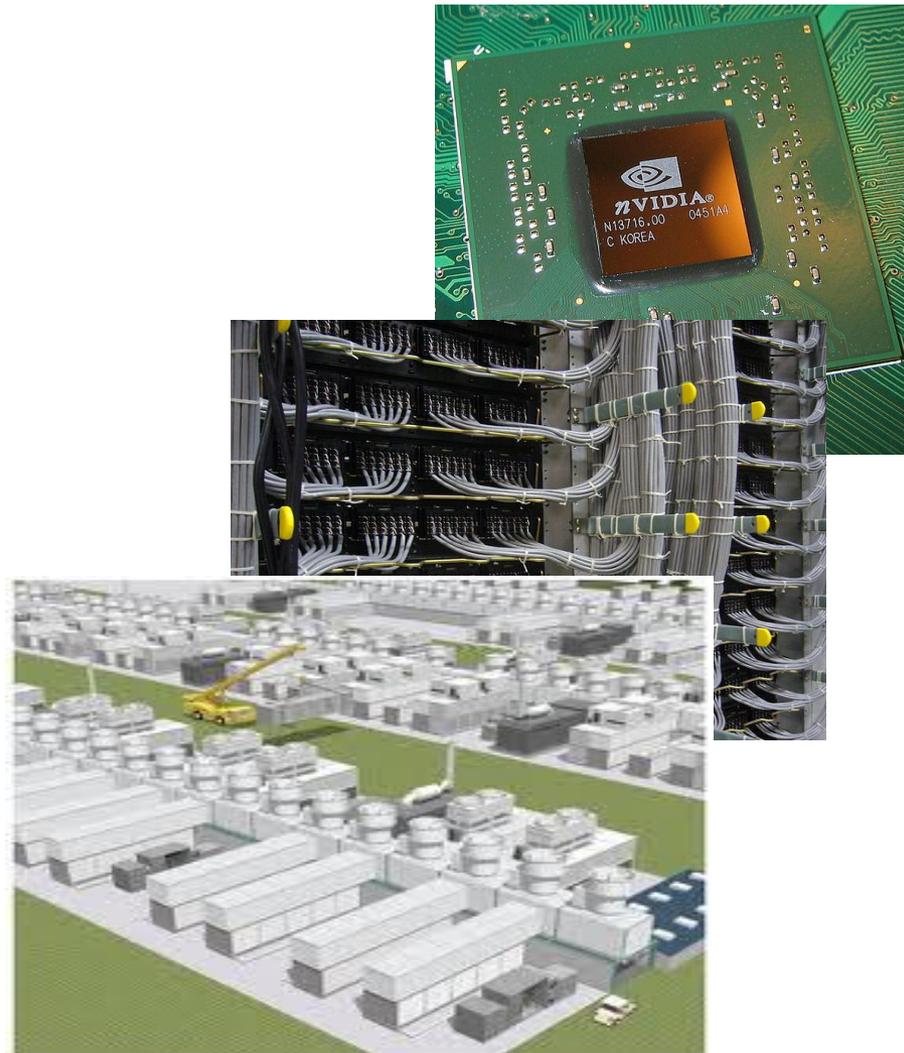
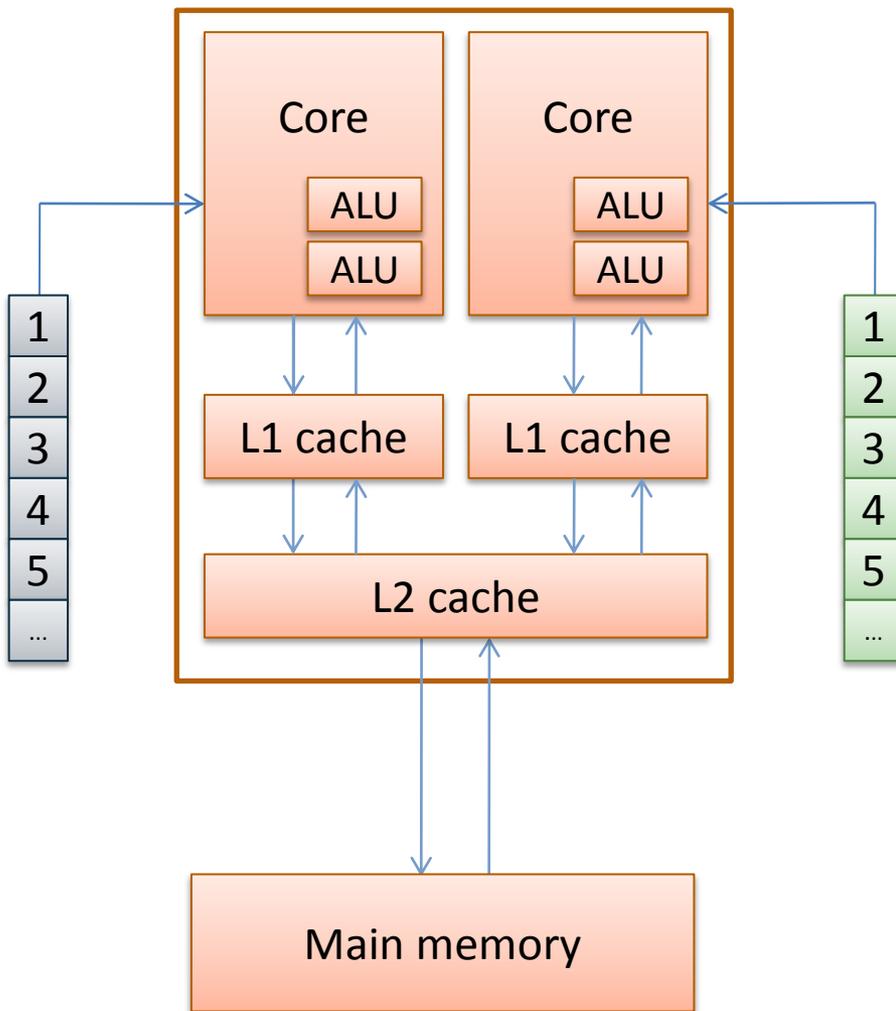




Power to chip peaking

Darn!  
Intel engineers no longer optimize my programs while I watch TV!

# Last Time: Multi-core Hardware & Data Centers



# Sounds Great!

- So my old programs will run 2x, 4x, 48x, 256x, 1024x faster?

# Sounds Great!

- So my old programs will run 2x, 4x, 48x, 256x, 1024x faster?
  - no way!

# Sounds Great!

- So my old programs will run 2x, 4x, 48x, 256x, 1024x faster?
  - no way!
  - to upgrade from Intel 386 to 486, the app writer and compiler writer did not have to do anything (much)
    - IA 486 interpreted the same sequential stream of instructions; it just did it faster
    - this is why we could watch TV while Intel engineers optimized our programs for us
  - to upgrade from Intel 486 to dual core, we need to figure out how to split a single stream of instructions in to two streams of instructions that collaborate to complete the same task.
    - *without work & thought, our programs don't get any faster at all*
    - *it takes ingenuity to generate efficient parallel algorithms from sequential ones*

# **PARALLEL AND CONCURRENT PROGRAMMING**

# Speedup

- *Speedup*: the ratio of parallel program execution time to sequential program execution time.
- If  $T(p)$  is the time it takes to run a computation on  $p$  processors

$$\text{speedup}(p) = T(p)/T(1)$$

- A parallel program has *perfect speedup* (aka *linear speedup*) if

$$T(p)/T(1) = \text{speedup} = p$$

- *Bad news: Not every program can be effectively parallelized.*
  - in fact, very few programs will scale with perfect speedups.
  - we certainly can't achieve perfect speedups automatically
  - limited by sequential portions, data transfer costs, ...

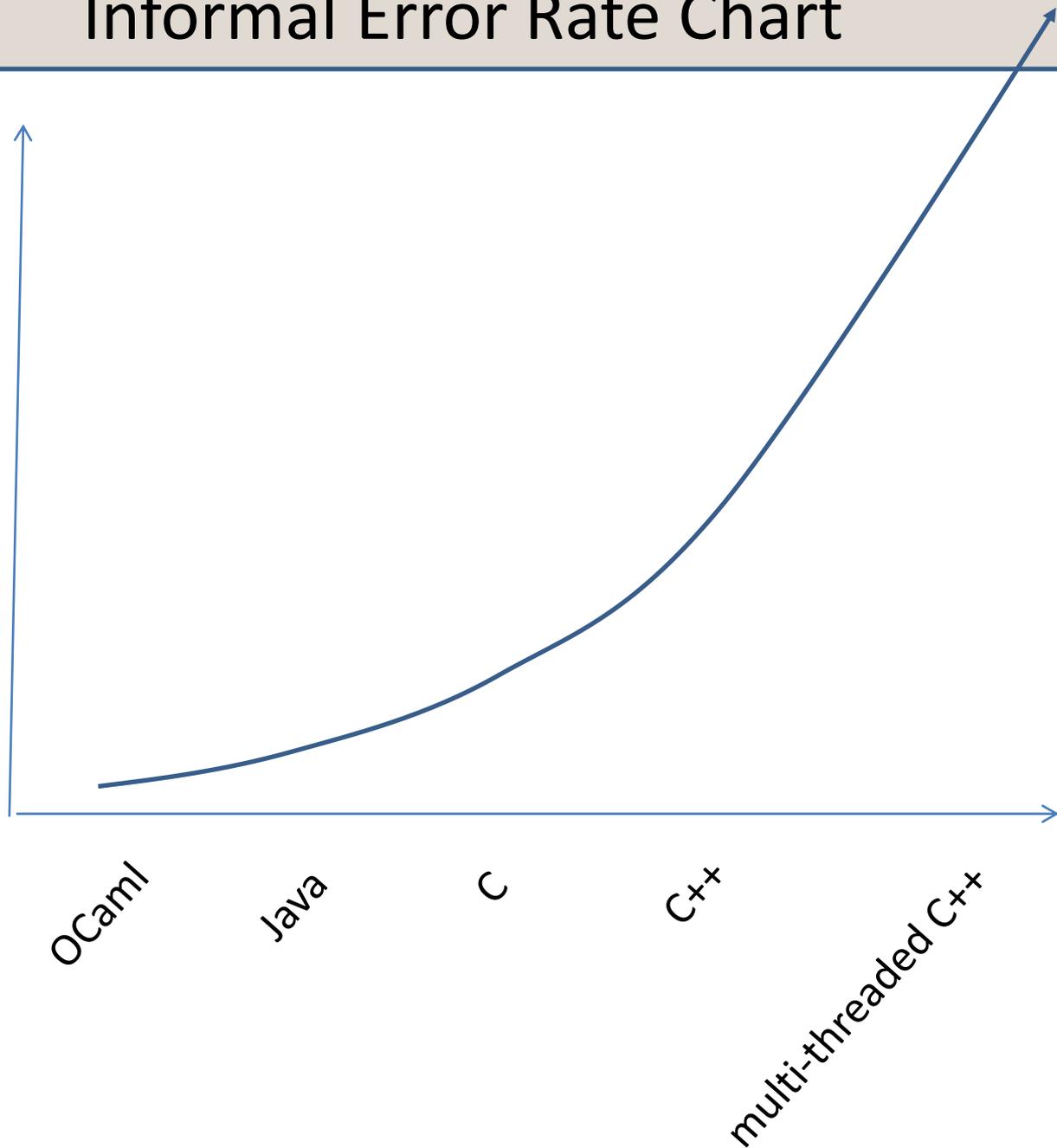
# Most Troubling...

Most, *but not all*, parallel and concurrent programming models are far harder to work with than sequential ones:

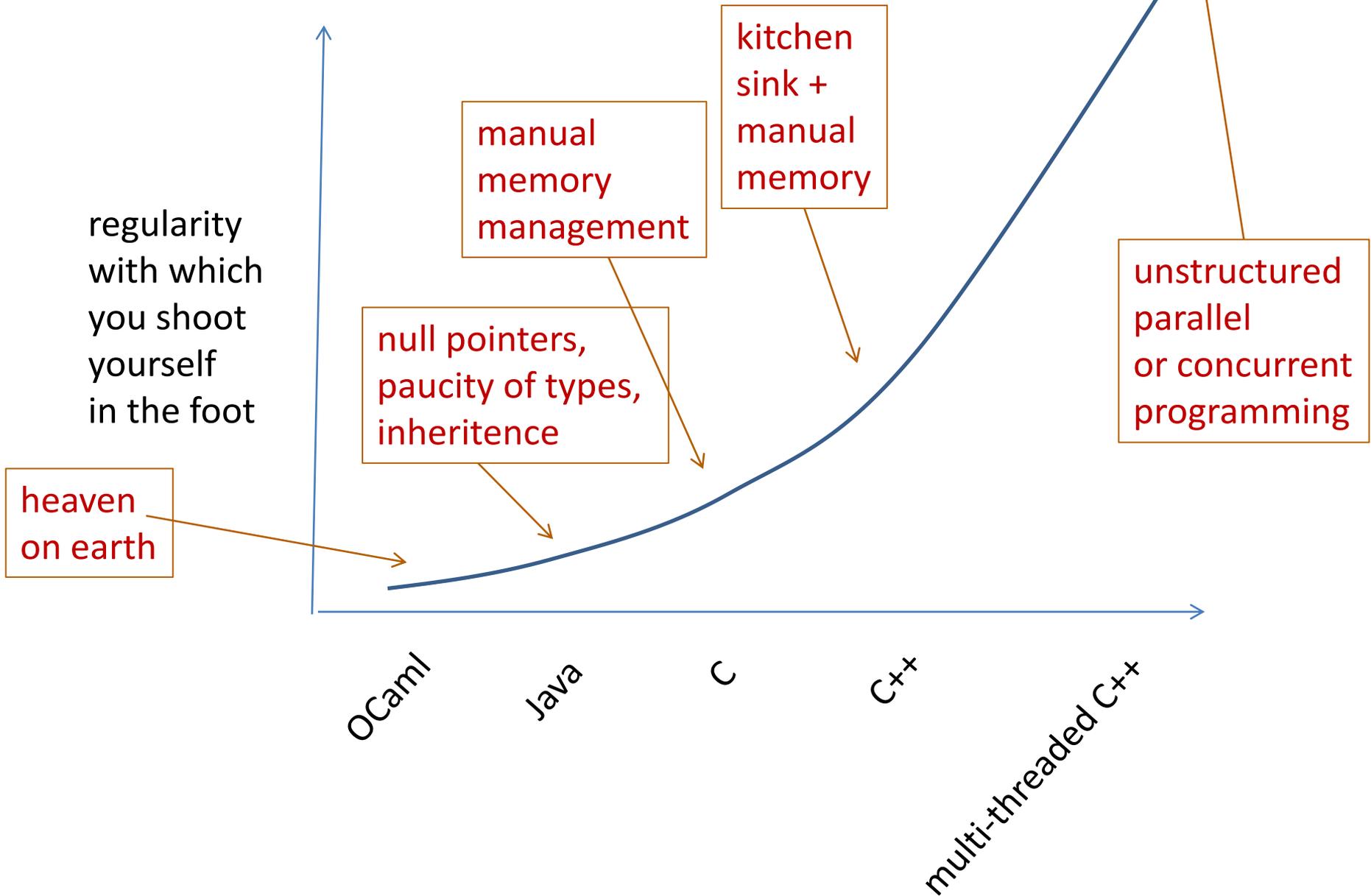
- *They introduce non-determinism*
  - the root of (almost all) evil
  - program parts suddenly have many different outcomes
    - they have different outcomes *on different runs*
    - debugging requires considering *all of the possible outcomes*
    - horrible *heisenbugs* hard to track down
- *They are non-modular*
  - module A implicitly influences the outcomes of module B
- *They introduce new classes of errors*
  - race conditions, deadlocks
- *They introduce new performance/scalability problems*
  - busy-waiting, sequentialization, contention,

# Informal Error Rate Chart

regularity  
with which  
you shoot  
yourself  
in the foot



# Informal Error Rate Chart



# Solid Parallel Programming Requires

1. Good sequential programming skills.
  - all the things we've been talking about: use modules, types, ...
2. Deep knowledge of the application.
3. *Pick a correct-by-construction parallel programming model*
  - whenever possible, a parallel model with semantics that coincide with sequential semantics
    - whenever possible, reuse well-tested libraries that hide parallelism
  - whenever possible, a model that cuts down non-determinism
  - whenever possible, a model with fewer possible concurrency bugs
  - if bugs can arise, know and use safe programming patterns
4. Careful engineering to ensure scaling.
  - unfortunately, there is sometimes a tradeoff:
    - reduced non-determinism can lead to reduced resource utilization
  - synchronization, communication costs may need optimization

# **OUR FIRST PARALLEL PROGRAMMING MODEL: THREADS**

# Threads: A Warning

- *Concurrent Threads: the classic shoot-yourself-in-the-foot concurrent programming model*
  - all the classic error modes
- Why Threads?
  - almost all programming languages will have a threads library
    - OCaml in particular!
  - you need to know where the pitfalls are
  - the assembly language of concurrent programming paradigms
    - we'll use threads to build several higher-level programming models

# Threads

- Threads: an abstraction of a processor.
  - programmer (or compiler) decides that some work can be done in parallel with some other work, e.g.:

```
let _ = compute_big_thing() in
let y = compute_other_big_thing() in
...
```

- we *fork* a thread to run the computation in parallel, e.g.:

```
let t = Thread.create compute_big_thing () in
let y = compute_other_big_thing () in
...
```

# Intuition in Pictures

```
let t = Thread.create f () in  
let y = g () in  
...
```



processor 1

```
time 1 Thread.create  
time 2 execute g ()  
time 3 ...
```

processor 2

```
(* doing nothing *)  
execute f ()  
...
```



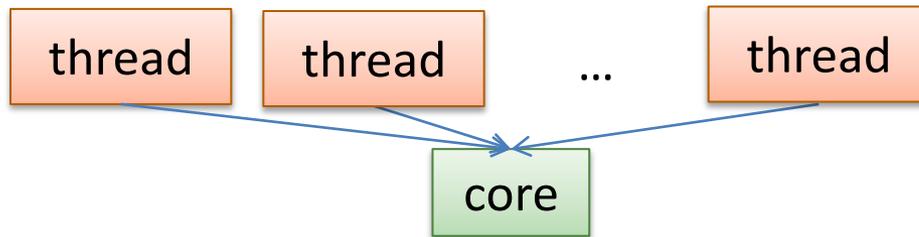
# Of Course...

Suppose you have 2 available cores and you fork 4 threads. In a typical multi-threaded system,

- the operating system provides *the illusion* that there are an infinite number of processors.
  - not really: each thread consumes space, so if you fork too many threads the process will die.
- it *time-multiplexes* the threads across the available processors.
  - about every 10 msec, it stops the current thread on a processor, and switches to another thread.
  - so a thread is really a *virtual processor*.

# OCaml, Concurrency and Parallelism

Unfortunately, even if your computer has 2, 4, 6, 8 cores, OCaml cannot exploit them. It multiplexes all threads over a single core



Hence, OCaml provides concurrency, but not parallelism. *Why?* Because OCaml (like Python) has no parallel run time or garbage collector. Lots of other functional languages (Haskell, F#, ...) do.

Fortunately, when thinking about *program correctness*, it doesn't matter that OCaml is not parallel -- I will often pretend that it is. But we won't be able to get the same kinds of speedups. :-)

# Coordination

```
Thread.create : ('a -> 'b) -> 'a -> Thread.t  
  
let t = Thread.create f () in  
let y = g () in  
...
```

How do we get back the result that `t` is computing?

# First Attempt

```
let r = ref None
let t = Thread.create (fun _ -> r := Some(f ())) in
let y = g() in
  match r with
    | Some v -> (* compute with v and y *)
    | None -> ???
```

## Second Attempt

```
let r = ref None
let t = Thread.create (fun _ -> r := Some(f ())) in
let y = g() in
let rec wait() =
  match r with
  | Some v -> v
  | None -> wait()
in
let v = wait() in
  (* compute with v and y *)
```

# Two Problems

```
let r = ref None
let t = Thread.create (fun _ -> r := Some(f ())) in
let y = g() in
let rec wait() =
  match r with
  | Some v -> v
  | None -> wait()
in
let v = wait() in
  (* compute with v and y *)
```

First, we are *busy-waiting*.

- consuming cpu without doing something useful.
- the processor could be either running a useful thread/program or power down.

# Two Problems

```
let r = ref None
let t = Thread.create (fun _ -> r := Some(f ())) in
let y = g() in
let rec wait() =
  match r with
  | Some v -> v
  | None -> wait()
in
let v = wait() in
  (* compute with v and y *)
```

Second, an operation like `r := Some v` may not be *atomic*.

- `r := Some v` requires us to copy the bytes of `Some v` into the `ref r`
- we might see part of the bytes (corresponding to `Some`) before we've written in the other parts (e.g., `v`).
- So the waiter might see the wrong value.

# Atomicity

Consider the following:

```
let inc(r:int ref) = r := (!r) + 1
```

and suppose two threads are incrementing the same ref r:

Thread 1

inc(r);

!r

Thread 2

inc(r);

!r

If r initially holds 0, then what will Thread 1 see when it reads r?

# Atomicity

The problem is that we can't see exactly what instructions the compiler might produce to execute the code.

It might look like this:

## Thread 1

```
EAX := load(r);
```

```
EAX := EAX + 1;
```

```
store EAX into r
```

```
EAX := load(r)
```

## Thread 2

```
EAX := load(r);
```

```
EAX := EAX + 1;
```

```
store EAX into r
```

```
EAX := load(r)
```

# Atomicity

But a clever compiler might optimize this to:

## Thread 1

```
EAX := load(r);
```

```
EAX := EAX + 1;
```

```
store EAX into r
```

```
EAX := load(r)
```

## Thread 2

```
EAX := load(r);
```

```
EAX := EAX + 1;
```

```
store EAX into r
```

```
EAX := load(r)
```

# Atomicity

Furthermore, we don't know when the OS might interrupt one thread and run the other.

## Thread 1

```
EAX := load(r);
```

```
EAX := EAX + 1;
```

```
store EAX into r
```

```
EAX := load(r)
```

## Thread 2

```
EAX := load(r);
```

```
EAX := EAX + 1;
```

```
store EAX into r
```

```
EAX := load(r)
```

(The situation is similar, but not quite the same on multi-processor systems.)

# Interleaving & Race Conditions

We can calculate the possible outcomes for a multi-threaded program by considering all of the possible interleavings of the *atomic* actions performed by each thread.

- Subject to the *happens-before* relation.
  - can't have a child thread's actions happening before a parent forks it.
  - can't have later instructions execute earlier *in the same thread*.
- Here, *atomic* means indivisible actions.
  - For example, on most machines reading or writing a 32-bit word is atomic.
  - But, writing a multi-word object is usually *not* atomic.
  - Most operations like “ $b := b - w$ ” are implemented in terms of a series of simpler operations such as “ $r1 = \text{read}(b)$ ;  $r2 = \text{read}(w)$ ;  $r3 = r1 - r2$ ;  $\text{write}(b, r3)$ ”
  - To better understand what is and isn't atomic demands detailed knowledge of the compiler and the underlying architecture (see CS61, CS161 for this kind of detail.)

Reasoning about all interleavings is *hard*.

- The number of interleavings grows exponentially with the number of statements.
- It's hard for us to tell what is and isn't atomic in a high-level language.

# Atomicity

One possible interleaving of the instructions:

## Thread 1

EAX := load(r);

EAX := EAX + 1;

store EAX into r

EAX := load(r)

## Thread 2

EAX := load(r);

EAX := EAX + 1;

store EAX into r

EAX := load(r)

What answer do we get?

# Atomicity

Another possible interleaving:

## Thread 1

EAX := load(r);

EAX := EAX + 1;

store EAX into r

EAX := load(r)

## Thread 2

EAX := load(r);

EAX := EAX + 1;

store EAX into r

EAX := load(r)

What answer do we get this time?

# Atomicity

Another possible interleaving:

## Thread 1

EAX := load(r);

EAX := EAX + 1;

store EAX into r

EAX := load(r)

## Thread 2

EAX := load(r);

EAX := EAX + 1;

store EAX into r

EAX := load(r)

What answer do we get this time?

**Moral:** The system is responsible for *scheduling* execution of instructions.

**Moral:** This can lead to an enormous degree of *non-determinism*.

# Atomicity

In fact, today's multi-core processors don't treat memory in a *sequentially consistent* fashion.

## Thread 1

```
EAX := load(r);
```

```
EAX := EAX + 1;
```

```
store EAX into r
```

```
EAX := load(r)
```

## Thread 2

```
EAX := load(r);
```

```
EAX := EAX + 1;
```

```
store EAX into r
```

```
EAX := load(r)
```

That means that *we can't even assume that what we will see corresponds to some interleaving of the threads' instructions!*

Beyond the scope of this class (and my brain...)

# One Solution (using join)

```
let r = ref None
let t = Thread.create (fun _ -> r := Some(f ())) in
let y = g() in
  Thread.join t ;
match r with
| Some v -> (* compute with v and y *)
| None -> failwith "impossible"
```

# One Solution (using join)

```
let r = ref None
let t = Thread.create (fun _ -> r := Some(f ())) in
let y = g() in
  Thread.join t ;
match r with
| Some v -> (* compute with v and y *)
| None -> failwith "impossible"
```

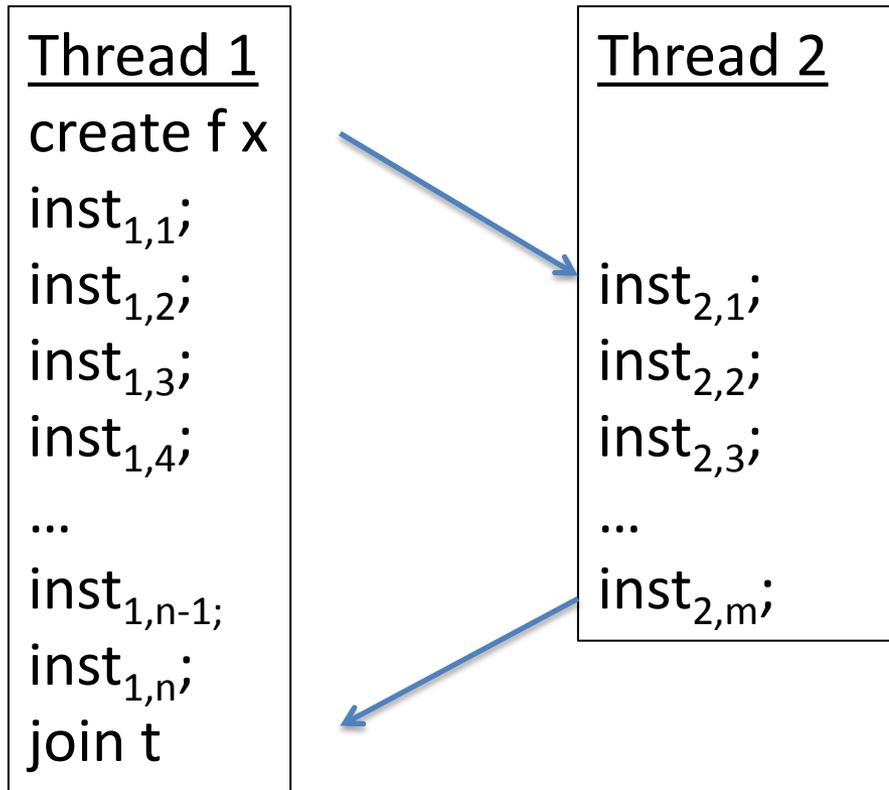
Thread.join t causes the current thread to *wait* until the thread t terminates.

# One Solution (using join)

```
let r = ref None
let t = Thread.create (fun _ -> r := Some(f ())) in
let y = g() in
  Thread.join t ;
  match r with
  | Some v -> (* compute with v and y *)
  | None -> failwith "impossible"
```

So after the join, we know that any of the operations of t have *completed*.

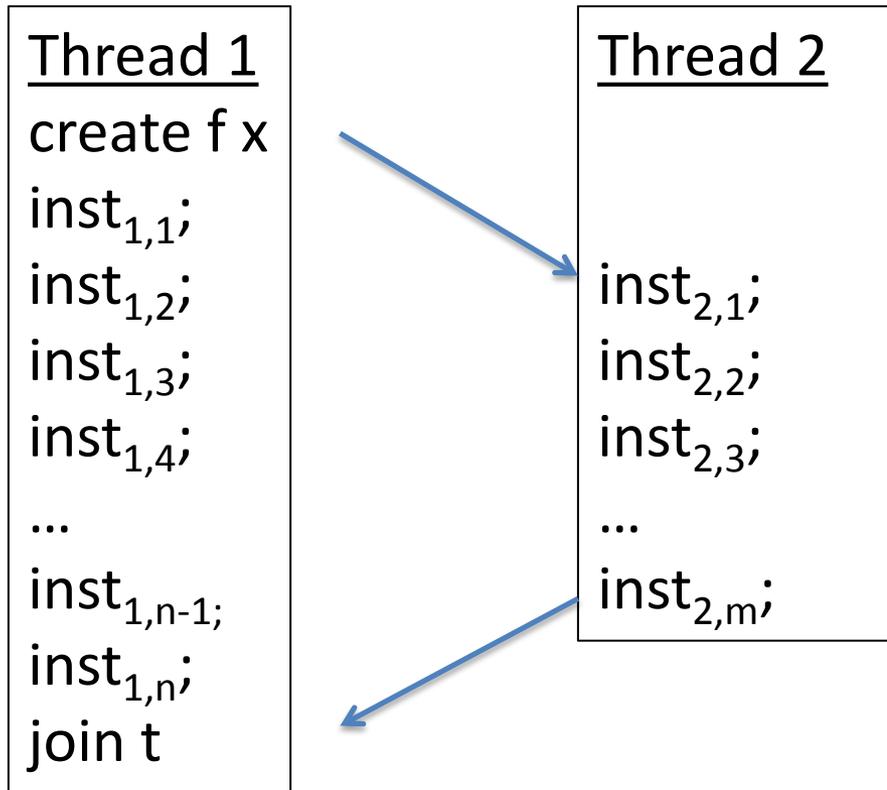
# In Pictures



We know that for each thread the previous instructions must happen before the later instructions.

So for instance, `inst1,1` must happen before `inst1,2`.

# In Pictures



We also know that the fork must happen before the first instruction of the second thread.

# In Pictures

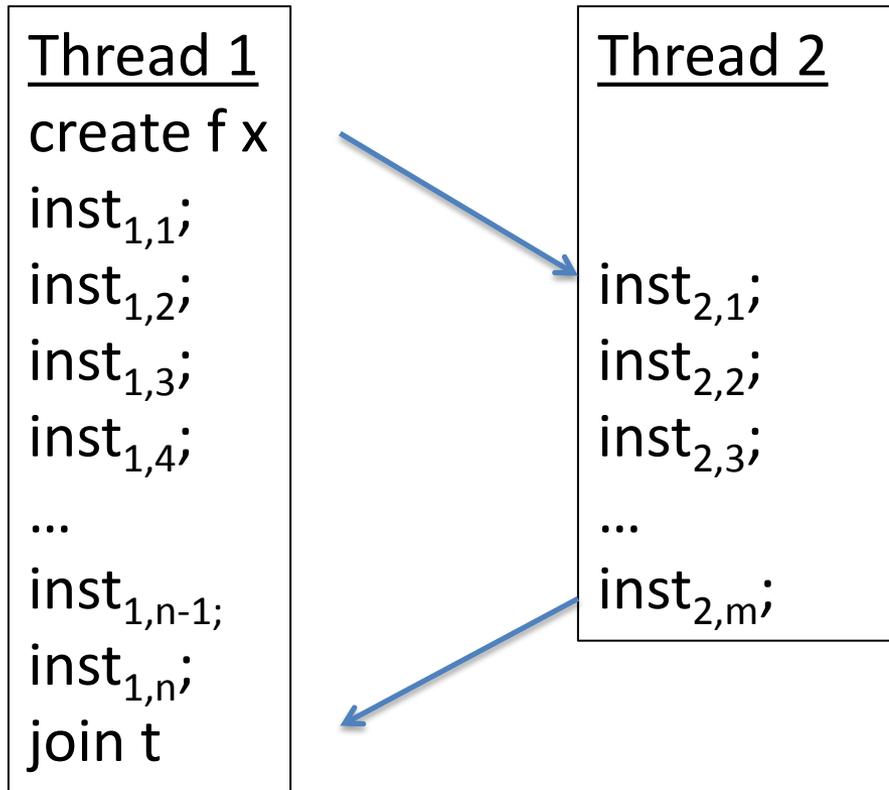
Thread 1  
create f x  
inst<sub>1,1</sub>;  
inst<sub>1,2</sub>;  
inst<sub>1,3</sub>;  
inst<sub>1,4</sub>;  
...  
inst<sub>1,n-1</sub>;  
inst<sub>1,n</sub>;  
join t

Thread 2  
inst<sub>2,1</sub>;  
inst<sub>2,2</sub>;  
inst<sub>2,3</sub>;  
...  
inst<sub>2,m</sub>;

We also know that the fork must happen before the first instruction of the second thread.

And thanks to the join, we know that all of the instructions of the second thread must be completed before the join finishes.

# In Pictures



However, in general, we do not know whether `inst1,i` executes before or after `inst2,j`.

In general, *synchronization instructions like fork and join reduce the number of possible interleavings.*

*Synchronization cuts down non-determinism.*

In the absence of synchronization we don't know anything...

# **FUTURES: A PARALLEL PROGRAMMING ABSTRACTION**

# Futures

The fork-join pattern we just saw is so common, we'll create an abstraction for it:

```
module type FUTURE =
sig
  type 'a future

  (* future f x forks a thread to run f(x)
     and stores the result in a future when complete *)
  val future : ('a->'b) -> 'a -> 'b future

  (* force f causes us to wait until the
     thread computing the future value is done
     and then returns its value. *)
  val force : 'a future -> 'a
end
```

# Future Implementation

```
module Future : FUTURE =  
struct  
  type `a future = {tid    : Thread.t          ;  
                    value  : `a option ref }  
  
  let future(f:`a->'b) (x:`a) : `b future =  
    let r = ref None in  
    let t = Thread.create (fun () -> r := Some(f x)) ()  
    in  
    {tid=t ; value=r}  
  
  let force (f:`a future) : `a =  
    Thread.join f.tid ;  
    match !(f.value) with  
    | Some v -> v  
    | None -> failwith "impossible!"  
  
end
```

# Now using Futures

```
let x = future f () in  
let y = g () in  
let v = force x in  
(* compute with v and y *)
```

# Back to the Futures

```
module type FUTURE =  
sig  
  type 'a future  
  
  val future : ('a->'b) -> 'a -> 'b future  
  val force : 'a future -> 'a  
end
```

```
val f : unit -> int  
val g : unit -> int
```

with futures library:

```
let x = future f () in  
let y = g () in  
let v = force x in  
y + v
```

without futures library:

```
let r = ref None  
let t = Thread.create  
    (fun _ -> r := Some(f ()))  
    ()  
  
in  
let y = g() in  
Thread.join t ;  
match !r with  
  Some v -> y + v  
| None -> failwith "impossible"
```

# Back to the Futures

```
module type FUTURE =  
sig  
  type 'a future  
  
  val future : ('a->'b) -> 'a -> 'b future  
  val force : 'a future -> 'a  
end
```

```
val f : unit -> int  
val g : unit -> int
```

with futures library:

```
let x = future f () in  
let y = g () in  
let v = force x in  
y + v
```

without futures library:

```
let r = ref None  
let t = Thread.create  
    (fun _ -> r := Some(f ()))  
    ()  
  
in  
let y = g() in  
Thread.join t ;  
match !r with  
  Some v -> y + v  
| None -> failwith "impossible"
```

what happens if  
we delete these  
lines?

# Back to the Futures

```
module type FUTURE =  
sig  
  type 'a future  
  
  val future : ('a->'b) -> 'a -> 'b future  
  val force : 'a future -> 'a  
end
```

```
val f : unit -> int  
val g : unit -> int
```

with futures library:

```
let x = future f () in  
let y = g () in  
let v = force x in  
y + x
```

without futures library:

```
let r = ref None  
let t = Thread.create  
    (fun _ -> r := Some(f ()))  
    ()  
  
in  
let y = g() in  
Thread.join t ;  
match !r with  
  Some v -> y + v  
| None -> failwith "impossible"
```

what happens if  
we use x and  
forget to force?

# Back to the Futures

```
module type FUTURE =
sig
  type 'a future

  val future : ('a->'b) -> 'a -> 'b future
  val force : 'a future -> 'a
end
```

```
val f : unit -> int
val g : unit -> int
```

with futures library:

```
let x = future f () in
let y = g () in
let v = force x in
y + x
```

**Moral:** Futures + typing ensure entire categories of errors can't happen -- you protect yourself from your own stupidity

without futures library:

```
let r = ref None
let t = Thread.create
      (fun _ -> r := Some(f ()))
      ()
in
let y = g() in
Thread.join t ;
match !r with
  Some v -> y + v
| None -> failwith "impossible"
```

# Back to the Futures

```
module type FUTURE =  
sig  
  type 'a future  
  
  val future : ('a->'b) -> 'a -> 'b future  
  val force : 'a future -> 'a  
end
```

```
val f : unit -> int  
val g : unit -> int
```

with futures library:

```
let x = future f () in  
let v = force x in  
let y = g () in  
y + x
```

what happens if you  
relocate force, join?

without futures library:

```
let r = ref None  
let t = Thread.create  
    (fun _ -> r := Some(f ()))  
    ()  
  
in  
Thread.join t ;  
let y = g() in  
match !r with  
  Some v -> y + v  
| None -> failwith "impossible"
```

# Back to the Futures

```
module type FUTURE =  
sig  
  type 'a future  
  
  val future : ('a->'b) -> 'a -> 'b future  
  val force : 'a future -> 'a  
end
```

```
val f : unit -> int  
val g : unit -> int
```

with futures library:

```
let x = future f () in  
let v = force x in  
let y = g () in  
y + x
```

**Moral:** Futures are  
not a universal savior

without futures library:

```
let r = ref None  
let t = Thread.create  
          (fun _ -> r := Some(f ()))  
          ()  
  
in  
  Thread.join t ;  
  let y = g() in  
  match !r with  
  | Some v -> y + v  
  | None -> failwith "impossible"
```

# An Example: Mergesort on Arrays

```
let mergesort (cmp:'a->'a->int) (arr : 'a array) : 'a array =  
  let rec msort (start:int) (len:int) : 'a array =  
    match len with  
      | 0 -> Array.of_list []  
      | 1 -> Array.make 1 arr.(start)  
      | _ -> let half = len / 2 in  
          let a1 = msort start half in  
            let a2 = msort (start + half) (len - half) in  
              merge a1 a2  
and merge (a1:'a array) (a2:'a array) : 'a array =  
  let a = Array.make (Array.length a1 + Array.length a2) a1.(0) in  
  let rec loop i j k =  
    match i < Array.length a1, j < Array.length a2 with  
      | true, true -> if cmp a1.(i) a2.(j) <= 0 then  
          (a.(k) <- a1.(i) ; loop (i+1) j (k+1))  
          else (a.(k) <- a2.(j) ; loop i (j+1) (k+1))  
      | true, false -> a.(k) <- a1.(i) ; loop (i+1) j (k+1)  
      | false, true -> a.(k) <- a2.(j) ; loop i (j+1) (k+1)  
      | false, false -> ()  
  
  in  
    loop 0 0 0 ; a  
in  
  msort 0 (Array.length arr)
```

# An Example: Mergesort on Arrays

```
let mergesort (cmp:'a->'a->int) (arr : 'a array) : 'a array =
  let rec msort (start:int) (len:int) : 'a array =
    match len with
    | 0 -> Array.of_list []
    | 1 -> Array.make 1 arr.(start)
    | _ -> let half = len / 2 in
            let a1 = msort start half in
            let a2 = msort (start + half) (len - half) in
            merge a1 a2
  and merge (a1:'a array) (a2:'a array) : 'a array =
    let a = Array.make (Array.length a1 + Array.length a2) a1.(0) in
    let rec loop i j k =
      match i < Array.length a1, j < Array.length a2 with
      | true, true -> if cmp a1.(i) a2.(j) <= 0 then
          (a.(k) <- a1.(i) ; loop (i+1) j (k+1))
          else (a.(k) <- a2.(j) ; loop i (j+1) (k+1))
      | true, false -> a.(k) <- a1.(i) ; loop (i+1) j (k+1)
      | false, true -> a.(k) <- a2.(j) ; loop i (j+1) (k+1)
      | false, false -> ()
    in
      loop 0 0 0 ; a
  in
    msort 0 (Array.length arr)
```

Opportunity for  
parallelization

# Making Mergesort Parallel

```
let mergesort (cmp:'a->'a->int) (arr : 'a array) : 'a array =  
  let rec msort (start:int) (len:int) : 'a array =  
    match len with  
      | 0 -> Array.of_list []  
      | 1 -> Array.make 1 arr.(start)  
      | _ -> let half = len / 2 in  
          let a1_f = Future.future (msort start) half in  
          let a2 = msort (start + half) (len - half) in  
            merge (Future.force a1_f) a2  
and merge (a1:'a array) (a2:'a array) : 'a array =  
  let a = Array.make (Array.length a1 + Array.length a2) a1.(0) in  
  let rec loop i j k =  
    match i < Array.length a1, j < Array.length a2 with  
      | true, true -> if cmp a1.(i) a2.(j) <= 0 then  
          (a.(k) <- a1.(i) ; loop (i+1) j (k+1))  
          else (a.(k) <- a2.(j) ; loop i (j+1) (k+1))  
      | true, false -> a.(k) <- a1.(i) ; loop (i+1) j (k+1)  
      | false, true -> a.(k) <- a2.(j) ; loop i (j+1) (k+1)  
      | false, false -> ()  
  
  in  
    loop 0 0 0 ; a  
  
in  
  msort 0 (Array.length arr)
```

# Divide-and-Conquer

This is an instance of a basic *divide-and-conquer* pattern in parallel programming

- take the problem to be solved and divide it in half
- fork a thread to solve the first half
- simultaneously solve the second half
- synchronize with the thread we forked to get its results
- combine the two solution halves into a solution for the whole problem.

**Warning:** the fact that we only had to rewrite 2 lines of code for mergesort made the parallelization transformation look deceptively easy

- we also had to verify that any two threads did not touch overlapping portions of the array -- if they did we would have to again worry about scheduling non-determinism

# Caveats

There is some overhead for creating a thread.

- On a uni-processor, parallel code will run *slower* than the sequential code.

Even on a multi-processor, we probably do *not always* want to fork a thread

- when the sub-array is small, faster to sort it than to fork a thread to sort it.
  - similar to using insertion sort when arrays are small vs. quicksort
- this is known as a *granularity problem*
  - more parallelism than we can effectively take advantage of.

In a good implementation of futures, a compiler and run-time system might look to see whether the cost of doing the fork is justified by the amount of work that will be done. Today, it's up to you to figure this out... 😞

- typically, use parallel divide-and-conquer until
  - (a) we have generated *at least* as many threads as there are processors
    - often *more threads* than processors because different jobs take different amounts of time to complete and we would like to keep all processors busy
  - (b) the sub-arrays have gotten small enough that it's not worth forking.

We're not going to worry about these performance-tuning details but rather focus on the distinctions between *parallel* and *sequential algorithms*.

# Another Example

```
type 'a tree = Leaf | Node of 'a node
and 'a node = {left   : 'a tree ;
                value  : 'a      ;
                right  : 'a tree }
```

```
let rec fold (f:'a -> 'b -> 'b -> 'b) (u:'b)
            (t:'a tree) : 'b =
  match t with
  | Leaf -> u
  | Node n ->
    f n.value (fold f u n.left) (fold f u n.right)
```

```
let sum (t:int tree) = fold (+) 0 t
```

# Another Example

```
type 'a tree = Leaf | Node of 'a node
and 'a node = {left   : 'a tree ;
                value  : 'a      ;
                right  : 'a tree }
```

```
let rec pfold (f:'a -> 'b -> 'b -> 'b) (u:'b)
            (t:'a tree) : 'b =
  match t with
  | Leaf -> u
  | Node n ->
    let l_f = Future.future (pfold f u) n.left in
    let r = pfold f u n.right in
    f n.value (Future.force l_f) r
```

```
let sum (t:int tree) = pfold (+) 0 t
```

## Note

- If the tree is imbalanced, then we're not going to get the same speedup as if it's balanced.
- Consider the degenerate case of a list.
  - The forked child will terminate without doing any useful work.
  - So the parent is going to have to do all that work.
  - Pure overhead... 😞
- In general, lists are a horrible data structure for parallelism.
  - *we can't cut the list in half in constant time*
  - for arrays and trees, we can do that (assuming the tree is balanced.)

# Side Effects?

```
type 'a tree = Leaf | Node of 'a node
and 'a node = { left   : 'a tree ;
                 value  : 'a      ;
                 right  : 'a tree }
```

```
let rec pfold (f:'a -> 'b -> 'b -> 'b) (u:'b)
            (t:'a tree) : 'b =
  match t with
  | Leaf -> u
  | Node n ->
    let l_f = Future.future (pfold f u) n.left in
    let r = pfold f u n.right in
    f n.value (Future.force l_f) r
```

```
let print (t:int tree) =
  pfold (fun n _ _ -> Printf.print "%d\n" n) ()
```

# Huge Point

*If code is purely functional, then it never matters in what order it is run.*

*If f () and g () are pure then all of the following are equivalent:*

```
let x = f () in
let y = g () in
e
```

```
let x_f = future f () in
let y    = g ()          in
let x    = force x_f    in
e
```

```
let y = g () in
let x = f () in
e
```

```
let y_g = future g () in
let x    = f ()          in
let y    = force y_g    in
e
```

As *side-effect*,

- This is why, IMHO, *imperative* languages where even the simplest of program phrases involves a side effect, are doomed.
- Of course, we've been saying this for 30 years!
- See J. Backus's Turing Award paper, "*Can Programming be Liberated from the von Neumann Style? A Functional Style and Its Algebra of Programs.*"

<http://www.cs.cmu.edu/~crary/819-f09/Backus78.pdf>

# **MANAGING MUTABLE DATA**

# Consider a Bank Account ADT

```
type account = { name : string; mutable bal : int }

let create (n:string) (b:int) : account =
  { name = n; bal = b }

let deposit (a:account) (amount:int) : unit =
  if a.bal + amount < max_balance then
    a.bal <- a.bal + amount

let withdraw (a:account) (amount:int) : int =
  if a.bal >= amount then (
    a.bal <- a.bal - amount;
    amount
  ) else 0
```

# What happens here?

```
val bank : account array

let rec atm (loc:string) =
  let id = getAccountNumber() in
  let w = getWithdrawAmount() in
  let d = withdraw (bank.(id)) w in
  dispenseDollars d ;
  atm loc

let world () =
  Thread.create atm "Princeton, Nassau" ;
  Thread.create atm "NYC, Penn Station" ;
  Thread.create atm "Boston, Lexington Square"
```

# Bad Situation

- Suppose two ATMs, running in separate threads, try to perform a withdrawal from the same bank account around the same time.
- For example, suppose bank.(0) is an account that starts with \$100 in its balance.
- And suppose we have two threads, each executing the service loop, trying to withdraw \$50 and \$75 respectively.

# Simplifying the situation...

$b = 100$

```
let w = 50 in
if b > w then
  (b <- b - w ;
   w)
else
  0
```

```
let w = 75 in
if b > w then
  (b <- b - w ;
   w)
else
  0
```

# Simplifying the situation...

$b = 100$

```
let w = 50 in
if b > w then
  (b <- b - w ;
   w)
else
  0
```

```
let w = 75 in
if b > w then
  (b <- b - w ;
   w)
else
  0
```

$b = 50$

# Simplifying the situation...

$b = 100$

```
let w = 50 in  
if b > w then  
  (b <- b - w ;  
   w)  
else  
  0
```

```
let w = 75 in  
if b > w then  
  (b <- b - w ;  
   w)  
else  
  0
```

$b = 25$

# Another schedule ...

**b = 100**

```
let w = 50 in  
if b > w then
```

```
let w = 75 in  
if b > w then  
  (b <- b - w ;  
   w)  
else 0
```

```
(b <- b - w ;  
 w)  
else  
  0
```

**b = -25**

# Good for you ... (less so for the bank)

b = 100

```
let w = 50 in
  if b > w then
    b - w
  (b <- b - w ;
   w)
else 0
```

```
let w = 75 in
  if b > w then
    (b <- b - w ;
     w)
  else 0
```

b = 50

# Good for you ... (less so for the bank)

b = 100

```
let w = 50 in
  if b > w then
    b - w
  (b <- b - w ;
   w)
else 0
```

```
let w = 75 in
  if b > w then
    (b <- b - w ;
     w)
  else 0
```

b = 50

Yet we  
paid out  
\$125!!!

# More Synchronization: Locks

This is not a problem we can fix with fork/join.

- The ATMs shouldn't ever terminate!
- Yet join only allows us to wait until one thread terminates.

Instead, we're going to use a *mutex lock* to synchronize threads.

- mutex is short for “mutual exclusion”
- locks will give us a way to introduce some controlled access to resources – in this case, the bank accounts.
- controlled access to a shared resource is a *concurrency problem*, not a *parallelization problem*

**END**