# O'Caml Datatypes

COS 326 David Walker Princeton University

# O'Caml So Far

- We have seen a number of basic types:
  - int
  - float
  - char
  - string
  - bool
- We have seen a few structured types:
  - pairs
  - tuples
  - options
  - lists
- In this lecture, we will see some more general ways to define our own new types and data structures

# Type Abbreviations

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• These abbreviations can be helpful documentation:

```
let distance (p1:point) (p2:point) : float =
    let square x = x *. x in
    let (x1,y1) = p1 in
    let (x2,y2) = p2 in
    sqrt (square (x2 -. x1) +. square (y2 -. y1))
```

But they add nothing of *substance* to the language
 they are equal in every way to an existing type

# Type Abbreviations

• We have already seen some type abbreviations:

• As far as O'Caml is concerned, you could have written:

```
let distance (p1:float*float)
        (p2:float*float) : float =
    let square x = x *. x in
    let (x1,y1) = p1 in
    let (x2,y2) = p2 in
    sqrt (square (x2 -. x1) +. square (y2 -. y1))
```

- Since the types are equal, you can substitute the definition for the name wherever you want
  - we have not added any new data structures

# DATA TYPES

• O'Caml provides a general mechanism called a data type for defining new data structures that consist of many alternatives



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• Creating values:



```
type color = Blue | Yellow | Green | Red
let c1 : color = Yellow
let c2 : color = Red
```

• Using data type values:

```
let print_color (c:color) : unit =
  match c with
  | Blue ->
  | Yellow ->
  | Green ->
  | Red ->
```

use pattern matching to determine which color you have; act accordingly

```
type color = Blue | Yellow | Green | Red
let c1 : color = Yellow
let c2 : color = Red
```

• Using data type values:

```
let print_color (c:color) : unit =
  match c with
  | Blue -> print_string "blue"
  | Yellow -> print_string "yellow"
  | Green -> print_string "green"
  | Red -> print_string "red"
```

type color = Blue | Yellow | Green | Red

• oops!:

```
let print_color (c:color) : unit =
  match c with
  | Blue -> print_string "blue"
  | Yellow -> print_string "yellow"
  | Red -> print_string "red"
```

Warning 8: this pattern-matching is not exhaustive. Here is an example of a value that is not matched: Green

# Data Types Can Carry Additional Values

• Data types are more than just enumerations of constants:

```
type point = float * float
type simple_shape =
  Circle of point * float
| Square of point * float
```

- Read as: a simple\_shape is either:
  - a Circle, which contains a pair of a point and float, or
  - a Square, which contains a pair of a point and float





### Data Types Can Carry Additional Values

• Data types are more than just enumerations of constants:

```
type point = float * float
type simple shape =
  Circle of point * float
 Square of point * float
let origin : point = (0.0, 0.0)
let circ1 : simple shape = Circle (origin, 1.0)
let circ2 : simple shape = Circle ((1.0, 1.0), 5.0)
let square : simple shape = Square (origin, 2.3)
```

### Data Types Can Carry Additional Values

• Data types are more than just enumerations of constants:

```
type point = float * float
type simple_shape =
  Circle of point * float
| Square of point * float
let simple_area (s:simple_shape) : float =
  match s with
  | Circle (_, radius) -> 3.14 *. radius *. radius
  | Square (_, side) -> side *. side
```

### Compare

• Data types are more than just enumerations of constants:

```
type point = float * float
type simple_shape =
  Circle of point * float
| Square of point * float
let simple_area (s:simple_shape) : float =
  match s with
  | Circle (_, radius) -> 3.14 *. radius *. radius
  | Square (_, side) -> side *. side
```

type my shape = point \* float

let simple\_area (s:my\_shape) : float =
 (3.14 \*. radius \*. radius) ???? (side \*. side)









```
type point = float * float
type radius = float
type side = float
type shape =
    Square of side
    [ Ellipse of radius * radius
    [ RtTriangle of side * side
    [ Polygon of point list
```

```
let area (s : shape) : float =
  match s with
  | Square s ->
  | Ellipse (r1, r2)->
  | RtTriangle (s1, s2) ->
  | Polygon ps ->
```

#### a data type also defines a pattern for matching



```
type point = float * float
type radius = float
type side = float
type shape =
    Square of side
    Ellipse of radius * radius
    RtTriangle of side * side
    Polygon of point list
```

```
let area (s : shape) : float =
  match s with
    | Square s -> s *. s
    | Ellipse (r1, r2)-> r1 *. r2
    | RtTriangle (s1, s2) -> s1*.s2/.2.
    | Polygon ps -> ???
```

#### a data type also defines a pattern for matching

- How do we compute polygon area?
- For convex polygons:
  - Case: the polygon has fewer than 3 points:
    - it has 0 area! (it is a line or a point or nothing at all)
  - Case: the polygon has 3 or more points:
    - Compute the area of the triangle formed by the first 3 vertices
    - Delete the second vertex to form a new polygon
    - Sum the area of the triangle and the new polygon



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    - Compute the area of the triangle formed by the first 3 vertices
    - Delete the second vertex to form a new polygon
    - Sum the area of the triangle and the new polygon
- Note: This is a beautiful inductive algorithm:
  - the area of a polygon with n points is computed in terms of a smaller polygon with only n-1 points!







```
let tri_area (p1:point) (p2:point) (p3:point) : float =
    let a = distance p1 p2 in
    let b = distance p2 p3 in
    let c = distance p3 p1 in
    let s = 0.5 *. (a +. b +. c) in
    sqrt (s *. (s -. a) *. (s -. b) *. (s -. c))
```

```
let rec poly_area (ps : point list) : float =
  match ps with
  | p1 :: p2 :: p3 :: tail ->
     tri_area p1 p2 p3 +. poly_area (p1::p3::ps)
  | _ -> 0.
```

```
let area (s : shape) : float =
  match s with
   | Square s -> s *. s
   | Ellipse (r1, r2)-> r1 *. r2
   | RtTriangle (s1, s2) -> s1*.s2/.2.
   | Polygon ps -> poly_area ps
```

# **INDUCTIVE DATA TYPES**

- We can use data types to define inductive data
- A binary tree is:
  - a Leaf containing no data
  - a Node containing a key, a value, a left subtree and a right subtree

- We can use data types to define inductive data
- A binary tree is:
  - a Leaf containing no data
  - a Node containing a key, a value, a left subtree and a right subtree

```
type key = string
type value = int

type tree =
  Leaf
| Node of key * value * tree * tree
```

```
type key = int
type value = string
type tree =
  Leaf
| Node of key * value * tree * tree
```

let rec insert (t:tree) (k:key) (v:value) : tree =

```
type key = int
type value = string
type tree =
  Leaf
| Node of key * value * tree * tree
```



```
type key = int
type value = string
type tree =
  Leaf
| Node of key * value * tree * tree
```

```
let rec insert (t:tree) (k:key) (v:value) : tree =
match t with
    | Leaf -> Node (k, v, Leaf, Leaf)
    | Node (k', v', left, right) ->
```

```
type key = int
type value = string
type tree =
  Leaf
| Node of key * value * tree * tree
```

```
type key = int
type value = string
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```

```
type key = int
type value = string
type tree =
  Leaf
| Node of key * value * tree * tree
```

## Inductive data types: Another Example

- Recall, we used the type "int" to represent natural numbers
  - but that was kind of broken: it also contained negative numbers
  - we had to use a dynamic test to guard entry to a function:

```
let double (n : int) : int =
    if n < 0 then
        raise (Failure "negative input!")
    else
        double_nat n</pre>
```

 it would be nice if there was a to define the natural numbers exactly, and use OCaml's type system to guarantee no client ever attempts to double a negative number

- Recall, a natural number n is either:
  - zero, or
  - m + 1
- We use a data type to represent this definition exactly:

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```
type nat = Zero | Next of nat
```

- Recall, a natural number n is either:
  - zero, or
  - m + 1
- We use a data type to represent this definition exactly:

```
type nat = Zero | Next of nat
let rec nat_to_int (n : nat) : int =
match n with
Zero -> 0
| Next n -> 1 + nat_to_int n
```

- Recall, a natural number n is either:
  - zero, or
  - m + 1
- We use a data type to represent this definition exactly:

```
type nat = Zero | Next of nat
let rec nat_to_int (n : nat) : int =
match n with
Zero -> 0
| Next n -> 1 + nat_to_int n
let rec double_nat (n : nat) : nat =
match n with
| Zero -> Zero
| Next m -> Next (Next (double_nat m))
```

# **AN EXERCISE IN TYPE DESIGN**

# Example Type Design

- A GML document consists of:
  - a list of elements
- An element is either:
  - a word or markup applied to an element
- Markup is either:
  - italicize, bold, or a font name

# Example Type Design

- A GML document consists of:
  - a list of elements
- An element is either:
  - a word or markup applied to an element
- Markup is either:
  - italicize, bold, or a font name

```
type markup = Ital | Bold | Font of string
type elt =
  Words of string list
| Markup of markup * elt
type doc = elt list
```

### **Example Data**

```
type markup = Ital | Bold | Font of string
type elt =
  Words of string list
| Markup of markup * elt
type doc = elt list
let d = [ Markup (Bold,
```

```
Markup (Font "Arial",
    Words ["Chapter";"One"]));
Words ["It"; "was"; "a"; "dark";
        "&"; "stormy; "night."; "A"];
Markup (Ital, Words["shot"]);
Words ["rang"; "out."] ];;
```

- Change all of the "Arial" fonts in a document to "Courier".
- Of course, when we program functionally, we implement change via a function that
  - receives one data structure as input
  - builds a new (different) data structure as an output

• Change all of the "Arial" fonts in a document to "Courier".

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type markup = Ital | Bold | Font of string
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• Change all of the "Arial" fonts in a document to "Courier".

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• Technique: approach the problem top down, work on doc first:



• Change all of the "Arial" fonts in a document to "Courier".

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type markup = Ital | Bold | Font of string
type elt =
  Words of string list
| Markup of markup * elt
type doc = elt list
```

• Technique: approach the problem top down, work on doc first:

```
let rec chfonts (elts:doc) : doc =
  match elts with
  [] ->
  | hd::tl ->
```

• Change all of the "Arial" fonts in a document to "Courier".

```
type markup = Ital | Bold | Font of string
type elt =
  Words of string list
| Markup of markup * elt
type doc = elt list
```

• Technique: approach the problem top down, work on doc first:

```
let rec chfonts (elts:doc) : doc =
  match elts with
  [] -> []
      hd::tl -> (chfont hd)::(chfonts tl)
```

• Change all of the "Arial" fonts in a document to "Courier".

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type markup = Ital | Bold | Font of string
type elt =
  Words of string list
| Markup of markup * elt
type doc = elt list
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• Change all of the "Arial" fonts in a document to "Courier".

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• Change all of the "Arial" fonts in a document to "Courier".

```
type markup = Ital | Bold | Font of string
type elt =
  Words of string list
| Markup of markup * elt
type doc = elt list
```

• Next work on changing a markup:

let chmarkup (m:markup) : markup =

• Change all of the "Arial" fonts in a document to "Courier".

```
type markup = Ital | Bold | Font of string
type elt =
  Words of string list
| Markup of markup * elt
type doc = elt list
```

• Next work on changing a markup:

```
let chmarkup (m:markup) : markup =
  match m with
  | Font "Arial" -> Font "Courier"
  | _ -> m
```

# Summary: Changing fonts in an element

- Change all of the "Arial" fonts in a document to "Courier"
- Lesson: function structure follows type structure

```
let chmarkup (m:markup) : markup =
 match m with
  | Font "Arial" -> Font "Courier"
  | −> m
let rec chfont (e:elt) : elt =
 match e with
  | Words ws -> Words ws
  | Markup(m,e) -> Markup(chmarkup m, chfont e)
let rec chfonts (elts:doc) : doc =
 match elts with
  | [] \rightarrow []
  | hd::tl -> (chfont hd)::(chfonts tl)
```

# **Poor Style**

• Consider again our definition of markup and markup change:

```
type markup =
  Ital | Bold | Font of string

let chmarkup (m:markup) : markup =
  match m with
  | Font "Arial" -> Font "Courier"
  | _ -> m
```

# **Poor Style**

• What if we make a change:

```
type markup =
  Ital | Bold | Font of string | TTFont of string
let chmarkup (m:markup) : markup =
  match m with
  | Font "Arial" -> Font "Courier"
  | _ -> m
```

the underscore silently catches all possible alternatives

this may not be what we want -- perhaps there is an Arial TT font

it is better if we are alerted of all functions whose implementation may need to change

### **Better Style**

• Original code:

```
type markup =
  Ital | Bold | Font of string
let chmarkup (m:markup) : markup =
  match m with
  | Font "Arial" -> Font "Courier"
  | Ital | Bold -> m
```

### **Better Style**

• Updated code:

```
type markup =
  Ital | Bold | Font of string | TTFont of string
let chmarkup (m:markup) : markup =
  match m with
  | Font "Arial" -> Font "Courier"
  | Ital | Bold -> m
```

## **Better Style**

• Updated code, fixed:

```
type markup =
  Ital | Bold | Font of string | TTFont of string
 let chmarkup (m:markup) : markup =
  match m with
    | Font "Arial" -> Font "Courier"
    | TTFont "Arial" -> TTFont "Courier"
    | TTFont s -> TTFont s
    | Ital | Bold -> m
```

• Lesson: use the type checker where possible to help you maintain your code

# To Summarize

- Design recipe for writing Ocaml code:
  - write down English specifications
    - try to break problem into obvious sub-problems
  - write down some sample test cases
  - write down the signature (types) for the code
  - use the signature to guide construction of the code:
    - tear apart inputs using pattern matching
      - make sure to cover all of the cases! (Ocaml will tell you)
    - handle each case, building results using data constructor
      - this is where human intelligence comes into play
      - the "skeleton" given by types can almost be done automatically!
    - clean up your code
  - use your sample tests (and ideally others) to ensure correctness

# A couple of practice problems

- Write a function that gets rid of immediately redundant markup in a document. That is, Markup(Ital, Markup(Ital,e)) can be simplified to Markup(Ital,e)
  - write maps and folds over markups
- Design a datatype to describe bibliography entries for publications. Some publications are journal articles, others are books, and others are conference papers. Journals have a name, number and issue; books have an ISBN number; All of these entries should have a title and author.
  - design a sorting function
  - design maps and folds over your bibliography entries

# END