## UPDATE PROPAGATION IN BAKUNIN DATA NETWORKS

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#### Abstract

In a Bakunin network data are replicated at all nodes in order to achieve very high data availability. Nodes operate autonomously, executing transactions even when they are cut off from the rest of the system. This means that transactions may read stale data. In spite of this, serializability can be guaranteed by placing restrictions on the types of transactions that a node can execute. These restrictions take the form of an acyclic Read-Access Graph. In addition, a special update propagation protocol is used to ensure that all nodes see data updates in the same order. In this paper we present several such protocols. The protocols take advantage of the particular structure of the read-access graph to expedite propagation. We also define the notion of virtual serializability. It is a weaker form of serializability that allows speedier propagation.

#### 1. Introduction.

High data availability in the face of failures can be achieved through data replication and distribution. However, conventional concurrency control mechanisms [Bern81] halt transaction processing when certain communications failures occur. Thus, if a node or group of nodes is cut off from the rest of the system, they will be unable to access the data they have. This clearly hurts availability. In some applications it is important *not* to halt transaction processing when communication failures occur, and hence researchers have been studying more flexible mechanisms.

Until recently, a clean partition model has been used to study such high availability mechanisms BlKa85], [Davi84], [Giff83], [Park81], [SkWr84]. This model assumes that at any given time it is possible to tell whether the network is partitioned and if so, how the nodes are grouped. Although arguments can be presented in favor of this model, one must acknowledge that it does not always correctly depict real systems. In reality, it may be very difficult to detect when partitions occur and when they are repaired. This was the motivation for several researchers to take a different approach to the problem, namely to make no assumptions about detectability of partitions and even communication failures in general [Davi85], [Sari85]. We call this new failure model the dynamic failure model.

Most of the work that has been done so far on the dynamic failure model suffers from one common drawback: it does not guarantee serializability. Instead, it introduces some weak correctness criteria. In the present paper we suggest a scheme that provides a high degree of availability and, at the same time, preserves serializability as the correctness criterion. In addition, we introduce a new correctness criterion called *virtual serializability*. With it we can improve availability still further. Virtual

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serializability is a little weaker than strict serializability, but substantially stronger than other criteria suggested for high availability databases.

The proposed scheme is characterized by highly autonomous behavior of individual nodes with respect to transaction processing. No attempts at explicit inter-node concurrency control are made. Instead, correctness of execution is enforced by a combination of certain data access restrictions and special update propagation protocols. Thus, on the one hand, individual nodes are endowed with absolute freedom (in scheduling their transactions), and on the other hand, overall harmony (of execution correctness) is nevertheless achieved. Because of this property, we have termed such systems *Bakunin data networks*, after the 19th century Russian political theorist of anarchist convictions.

#### 2. The Database Model.

A distributed database system is viewed as a collection of nodes interconnected by some communication network, which store a set of data items. We assume that the database is fully replicated, *i.e.*, each node has a complete copy of it. Nodes are fail-stop [ScSc83]. Links can fail at any time, and we make no assumptions concerning the detectability of these failures.

In our scheme, the entire database is logically divided into k non-overlapping subsets of data items, called *fragments*, denoted  $F_1, F_2, ..., F_k$ . Each node has a copy of every fragment. Each fragment  $F_i$  is controlled by a unique node  $N(F_i)$  responsible for updating items in the fragment. We call the process at  $N(F_i)$ that controls  $F_i$  the agent of  $F_i$ , or  $A(F_i)$ . For simplicity we assume that each node (and agent) controls only one fragment. (This last assumption can easily be relaxed.)

A transaction is taken to be a sequence of any number of atomic read or write actions [Eswa76]. Each transaction executes at a single node (we say it is *local* to that node) and can only update the fragment whose agent resides at that node, but it can, in general, read copies of other fragments. (Since there are local copies of all fragments, these reads are performed at the updating node.) Subsequently, all resulting updates are propagated throughout the system. Let  $T_i$  be an arbitrary transaction, then  $U(T_i)$ denotes the list of all updates generated by  $T_i$ .

We assume the existence of a reliable multicast mechanism which ensures that all messages are eventually delivered to their destinations and no messages are delivered out of order. Each node continues processing transactions as long as it stays operational, regardless of the status of the communication network. Each node has a local concurrency control mechanism used to schedule transactions within that node. However, there is no (explicit) global concurrency control. In particular, read and write accesses to data never have to be coordinated with other nodes. We will also assume that all nodes control some fragment. (Nodes that do not can be considered as controlling an empty fragment.)

In order to specify how transactions originating at different nodes are restricted in which fragments they are allowed to read, other than the one controlled by their own node, we will use the following graph formalism.

**Definition** 2.1. The readaccess graph (RAG) is a directed graph G = (V, E), where  $V = \{F_1, F_2, \ldots, F_n\}$  and  $E = \{(F_i, F_j) : i \neq j \text{ and a transaction T that is initiated by <math>A(F_i)$  can read a data object contained in  $F_j$ .

Figure 2.1 shows an example of a readaccess graph with three fragments:  $F_1$ ,  $F_2$  and  $F_3$ . Suppose that  $A(F_i)$  resides at node *i*, for i = 1, 2, 3. Then transactions that run at node 1 can read items in fragments  $F_1$  and  $F_2$ , those running at node 2 can read items in fragments  $F_2$  and  $F_3$ , and those running at node 3 can read items in fragments  $F_1$  and  $F_3$ .



#### Figure 2.1

Since we assumed a one-to-one correspondence between fragments and computer nodes, we shall sometimes refer to the vertices of RAGsas computer nodes rather than fragments, whenever it is more convenient.

### 2.1. The Generic Update Propagation Protocol.

Let all the nodes of the RAG be numbered 1 through *n*. Let R(i) be the set of all nodes from which node *i* receives update messages  $(R: \{1, ..., n\} \rightarrow 2^{\{1, ..., n\}})$ . Let S(i) be the set of all nodes to which node *i* sends update messages  $(S: \{1, ..., n\} \rightarrow 2^{\{1, ..., n\}})$ . R and S are called propagation functions. Functions R and S are mutually redundant since one is the inverse of the other. However, we have chosen to introduce both of them in order to facilitate the forthcoming discussions.

Every node i will maintain two lists, which are initially empty. They are UPDATES(i) and OUT(i). The protocol consists of three concurrent procedures.

- (1) (Permanently in execution at node  $i, 1 \le i \le n$ .) For every local tranaction  $T_j$ , append  $U(T_j)$  to UPDATES(i). The order in which different transactions' updates are appended to the list is determined by the local serialization order.
- (2) (Executed at node  $i, 1 \le i \le n$ , upon receipt of  $OUT(j), j \in R(i)$ .) Append OUT(j) to UPDATES(i) and atomically install all updates from OUT(j) in the local copy of the database. Make sure that for every local transaction  $T_j$  which is serialized before these updates (and none other)  $U(T_j)$  is appended to UPDATES(i) before OUT(j).
- (3) (Iterated with arbitrary intervals at node  $i, 1 \le i \le n$ .) Atomically copy UPDATES(i) to OUT(i). Send OUT(i) to all nodes in S(i). Reinitialize UPDATES(i)to empty.
- Note: Since UPDATES(i) is accessed concurrently by several procedures, it is essential that a locking mechanism be used.

Propagation functions establish a logical order of update propagation. They have nothing to do with physical routing of messages. Thus, OUT(i) is addressed to nodes in S(i), but how it gets there is not important as long as the nodes not in S(i) through which the message may be routed do not attempt to process it.

Note that, strictly speaking, updates in  $U(T_s)$ , where  $T_s$  is a transaction updating fragment  $F_i$ , are needed only at those nodes that control fragments  $F_j$  such that  $(F_j, F_i)$  is an edge in the RAG, for only those nodes will ever

read the data updated<sup> $\dagger$ </sup>. We will ignore any redundancies for simplicity's sake. However, it is a straightforward matter to introduce an optimization provision in the protocol that would prune out update lists of those updates that are known not to be needed by any node down the chain.

On the abstract level, a distributed database system can be described by a combination of its RAG and propagation functions. In subsequent sections we shall study different such combinations and their properties.

#### 3. Availability and Related Notions.

The main motivation for studying Bakunin data networks is the very high level of availability they can offer. The ability of every individual node to schedule and execute transactions without having to "consult" any other nodes implies that transactions continue being processed at that node as long as the node stays operational. No communication delays or failures can affect this ability.

This property of Bakunin networks does not come for free, of course. In order to insure that the given correctness criteria are not violated by the anarchy in scheduling, we have to curtail somewhat the amount of data available for access at each node. Besides, in some cases it may be necessary to choose the propagation functions in such a way as to restrict the routes of update propagation, which implies delayed delivery of updates at some nodes, or less update availability, so to speak.

The word availability was used three times in the two preceding paragraphs, and each time it had a somewhat different meaning. To clarify the matters, we discuss here briefly the notions involved.

#### Static Availability.

We use the term static availability to refer to the ability of computer nodes (users) to access certain portions of the entire body of data as determined by the system design (e.g., because of security considerations). The restrictions of static availability do not bear any temporal character. They are set once and for all, for

<sup>&</sup>lt;sup>†</sup> This is true only for systems in which all the agents are stationary, *i.e.*, fixed at their respective nodes. Such systems are the sole subject of the present paper. However, see [GaKo87] for moving agents.

every node (user). To say that a certain fragment is statically available at a certain node (to a certain user) is to imply that this fragment can be accessed at the node at all times except possibly when accessing it may jeopardize data consistency (e.g., during communication failures). On the other hand, if a fragment is not statically available to a node (user), it cannot be accessed by such even when it is safe from the viewpoint of data consistency. RAGs serve as an example of how static availability can be curtailed.

#### Dynamic Availability.

This term refers to the ability of nodes (users) to access, over time, the portions of data that are statically available to them. A loss of dynamic availability (in replicated systems) can occur to prevent a violation of data consistency that may typically be experienced due to communication failures such as partitions.

# Prompt Delivery of Updates (or Update Availability).

The last of the three related notions has to do with the extent to which the system utilizes currently functional communication links in order to propagate updates as quickly as possible. High levels of static and dynamic availability are of no value if updates produced at one node are not delivered to other nodes or delivered with big time delays. Consider, for example, a distributed system with full static and dynamic availability at every node, *i.e.*, all data can be accessed anywhere in the system at any time (barring node failures, of course). Suppose further that updates produce by transactions running at one node never reach other nodes. Clearly, such collection of nodes can hardly even be called a system.

All three notions are closely interrelated. Most of the known techniques for dealing with network partitions do not make any restrictions to static availability (aside from those required by data security considerations). As a result, either dynamic availability (as in [Giff83], [SkWr84]) or correctness (as in [BIKa85], [Davi84], [Park81], [Sari85]) suffers. Bakunin data networks, in contrast to other approaches, compromises neither dynamic availability nor correctness in the least. This is achieved at the price of restricted static availability and, in some cases, delayed delivery of updates. It is not one of the subjects of this paper to discuss to what extent a loss of static availability can be detrimental (except for presenting a brief example in the following section), but in [GaKo87] it is argued that for many systems full static availability is not necessary.

#### **3.1.** How to Evaluate Protocols.

In Section 2.1 we presented a general update propagation framework from which an entire family of protocols can be derived by choosing different propagation functions R and S. We are going to use two basic criteria for selecting R and S. First, they must be such as to ensure the required correctness properties. Second, they must provide, as much as possible, prompt delivery of updates. In this section we are going to discuss the second criterion, which will be also referred to as performance of a protocol.

Clearly, the basis for the evaluation of performance should be how fast updates are delivered to the node which needs them. Of course, this largely depends on the topology of the communication network, its current load and status, the bandwidth of its links, etc., but all factors being equal different protocols (different propagation functions) will perform differently.

Consider two nodes in the distributed system, *i* and *j*. Suppose, there is an edge from *i* to *j* in the *RAG*. That means that transactions executing at node *i* can read data from the fragment controlled by node *j*. In that case, it is desirable that updates generated at *j* be delivered to *i* as promptly as possible in order for the transactions at *i* to be able to read upto-date information. Therefore, a protocol that allows node *j* to ship its updates directly to *i* for installation in the local copy is the most favorable to node *i*. Such a protocol would have  $i \in S(j)$  (and  $j \in R(i)$ ).

**Definition 3.1.** Let G = (V, E) be a *RAG* with corresponding propagation functions *R* and *S*. Then  $G_p = (V, E_p)$  is called a propagation graph if  $E_p = \{(i, j): i, j \in V \text{ and } j \in S(i) \ (i \in R(j))\}.$ 

**Definition 3.2.** Let G and  $G_p$  be as above. A path from node *i* to node *j* in  $G_p$  is called *characteristic* if it is a shortest path from *i* to *j* in  $G_p$  and  $(i, j) \in E$ .

A propagation graph describes the order in which updates are propagated in the network and installed in the local copies of different nodes. The length of a characteristic path indicates how far an update has to travel (in the logical sense) before it reaches a node where it is needed. Intuitively, a "good" protocol would result in a propagation graph with as short characteristic paths as possible for as many pairs of nodes as possible. Note that if two nodes, say i and j, are not connected by an edge in the RAG, then we are not really interested in the length of the shortest paths from i to j or from j to i, because neither of the nodes processes transactions that read data from the fragment controlled by the other.

Ideally, we would like to have a protocol that results in a propagation graph of which the corresponding RAG is a subgraph. Then all characteristic paths would be of length 1. This situation is achieved when  $i \in S(j)$ , for every  $(i, j) \in E$ . However, as we shall see in the subsequent sections, it is not always possible to have propagation functions that guarantee both good performance and adherence to the required correctness criteria.

## 4. Retaining Serializability as Correctness Criterion.

In this section we study systems (*i.e.*, RAG— propagation functions combinations) that guarantee serializability of transaction execution. We begin with a fairly simple observation that the RAG must be acyclic if we want to guarantee serializability at all times, even during failures. To show the need for this, consider the example of Figure 2.1. Suppose that a partition occurs and leaves each node in complete isolation. If the nodes continue processing transactions — and that is what we are after — the global schedule may not be serializable. For instance, if transaction  $T_1$  runs at node 1, reads  $b \in F_2$ , and writes  $a \in F_1$ , transaction  $T_2$  runs at node 2, reading  $c \in F_3$  and writing b, and transaction  $T_3$  runs at node 3, reading a and writing c, the results cannot be integrated to match any serial schedule. Note that the above holds true for any possible propagation functions.

Consequently, all the systems that we shall study in this section will be characterized by acyclic RAGs only.

Restricting RAGs to be acyclic clearly reduces the static availability of the system. But this is the price we pay for maintaining high dynamic availability. A valid question that can arise at this point is whether such a restriction of static availability is justifiable. We argue that in many applications it is.

Consider, for example, an airline reservation application. The database contains information on flight schedules, customer reservations, and seat assignments. Copies are to be placed at several computers, including machines at the airports where this airline operates. High dynamic availability is required for this application. For example, we would like to assign passengers to their seats at the airport even if that machine is cut off from the rest of the system. On the other hand, in this example, it is not necessary to run all types of transactions at any node. For example, it is unlikely that a flight schedule will be changed at an airport. (The actual departure time may be changed, but this is another matter.) Flight schedules are probably handled at a central airline office, and it is this machine that needs to be able to execute schedule changes. Similarly, the central office most likely is not expected to be responsible for seat assignment on any given flight. Thus, one can see that full static availability is not important here.

Each node has a copy of every fragment. There are six fragments: the flight schedules (F), the west coast reservations  $(R_w)$ , the east coast reservations  $(R_e)$ , and the seat assignments at airports A, B, and C  $(S_A, S_B, S_C)$ . (Our airline only flies out of three airports. We also assume that the reservations data are split into two parts).

Each fragment  $G_i$  is controlled by a unique node  $N(G_i)$  responsible for updating items in the fragment. For simplicity we assume that each node controls only one fragment. Thus, our system will have six nodes: one at the airline headquarters where the schedules are changed, two computers for handling reservations, and one computer at each of the three airports for seat assignments.

The read patterns of the transactions are represented by the RAG in Figure 4.1. Transactions that change schedules do not need to read data outside this fragment, so node F has no outgoing arcs. To make a reservation, a transaction must be aware of the schedules, so there are arcs  $R_e \rightarrow F$  and  $R_w \rightarrow F$ . Finally, transactions that give a customer a seat at the airport need to see the schedule and the reservations (a passenger without a reservation does not get a seat); hence  $S_A \rightarrow R_e$ ,  $S_A \rightarrow R_w$ ,  $S_A \rightarrow F$ , and so on.



#### Figure 4.1

Note that the RAG is acyclic. Thus in this example we were able to use the inherent structure of update and read operations to painlessly incorporate the required static availability restrictions in the scheme.

#### 4.1. Acyclic RAGs: The General Case.

In this subsection we aim at finding the propagation functions for systems characterized by acyclic RAGs such that serializability can be guaranteed for all possible transaction schedules. Let G = (V, E) be an acyclic RAG. Suppose that  $ord: V \rightarrow \{1, ..., n\}$  is a topological order on the vertices of G, *i.e.*, for any two vertices i and j, if (i, j) is an edge in G, ord(i) < ord(j). (A topological order must exist if G is acyclic.) Then define functions R and S as follows:

$$R(i) = \begin{cases} ord^{-1}(ord(i)+1) \} & \text{if } 1 \le ord(i) < n \\ \emptyset & \text{if } ord(i) = n \end{cases}$$
(4.1a)

$$S(i) = \begin{cases} \{ ord^{-1}(ord(i)-1) \} & \text{if } 1 < ord(i) \le n \\ \emptyset & \text{if } ord(i)=1 \end{cases} (4.1b)$$

For the purpose of notational convenience, we assume, without loss of generality, that the original numbering of nodes in G corresponds to a topological order. Then we can rewrite the above definitions in a more digestable form:

$$R(i) = \begin{cases} \{i+1\} & \text{if } 1 \le i < n \\ \emptyset & \text{if } i = n \end{cases}$$
(4.2a)

$$S(i) = \begin{cases} \{i-1\} & \text{if } 1 < i \le n \\ \emptyset & \text{if } i = 1 \end{cases}$$
(4.2b)

**Definition 4.1.** Let  $l \in V$  be such that ord(l) = 1 (with our simplifying assumption, l = 1). Then for a pair of transactions  $T_i$  and  $T_j$ ,  $T_i < T_j$  if  $U(T_i)$  is installed at node *l* before  $U(T_j)$ .

**Lemma 4.1.** If for every edge  $(T_i, T_j)$  in the serialization graph,  $T_i < T_j$ , then the serialization graph is acyclic.

**Proof.** Suppose not. Let  $C = (T_1, ..., T_k, T_1)$  be a cycle in the serialization graph. It is easy to see that relation < is transitive. Therefore we must have  $T_1 < T_1$ , which is clearly impossible.  $\Box$ 

**Lemma 4.2.** Let R and S be the propagtion functions defined in (4.2a) and (4.2b). Then for every edge  $(T_i, T_j)$  in the serialization graph  $T_i < T_j$ .

**Proof.** Consider any pair of transactions  $T_i$  and  $T_j$  such that  $(T_i, T_j)$  is in the edge set of the serialization graph.

Case 1. Transactions  $T_i$  and  $T_j$  are local to the same node, say node  $q, 1 \leq q \leq n$ . Since  $(T_i, T_j)$  is an edge in the graph,  $T_i$  must be serialized (locally) before  $T_j$ . Hence,  $U(T_i)$  is effectively installed in the local copy of the database before  $U(T_j)$ . Moreover, they are appended to UPDATES(q) in the same order, and thus, will be installed in that order in the copies at nodes q - 1, ..., 1.

Case 2. Transaction  $T_i$  is local to node q, transaction  $T_j$  is local to node r, and  $1 \leq q < r \leq n$ . This means that  $T_j$  overwrites a value read by  $T_i$ . Therefore,  $T_i$  is serialized at node q before  $U(T_j)$ . Consequently,  $U(T_i)$  is appended to UPDATES(q) before  $U(T_j)$ . This, in turn, implies that nodes q - 1, ..., 1 install  $U(T_i)$  before  $U(T_j)$ .

Case 3. As in Case 3, except r < q. Here,  $T_j$  reads a value written by  $T_i$ . Therefore,  $U(T_i)$  is serialized at node r before  $T_j$ ,  $U(T_i)$  is appended to UPDATES(r) before  $U(T_j)$ , and finally,  $U(T_i)$  is installed at nodes r - 1, ..., 1before  $U(T_i)$ .

Cases 1, 2, and 3 exhaust all possibilities. Thus,  $T_i < T_j$ .  $\Box$ 

Lemmas 4.1 and 4.2 together establish the following theorem.

**Theorem 4.1.** Let R and S be the propagation functions defined in (4.2a) and (4.2b). Then the schedule for any execution characterized by an acyclic RAG is serializable. Note that acyclicity of G was not used explicitly in the proof of the lemmas. This property is essential, however, in order to guarantee the existence of a topological numbering.

#### 4.2. A Special Case: tf-RAGs.

The topological protocol of Section 4.1 may be too restrictive in some cases. In particular, if the RAG is a tree, possibly with forward edges, then a protocol that propagates updates up the tree can be constructed. It performs better than the topological protocol and still guarantees serializability.

**Definition 4.2.** Let G = (V, E) be a directed graph. If G has a depth-first search (DFS) tree (forest) that contains tree and forward edges only, then G is called a *tf-graph*.

Let G be the given RAG, which is a tfgraph. Let D be a DFS forest of G with no cross or back edges. Without loss of generality, we can assume that D is a tree, for if it is not, it must consist of disconnected trees, in which case each of them can be treated independently. Then:

 $R(i) = \{j: j \text{ is a child of } i \text{ in } D\} \quad (4.3a)$ 

 $S(i) = \{j: j \text{ is the parent of } i \text{ in } D\} (4.3b)$ 

**Definition 4.3.** Let r be the root of D. Then  $T_i <_{tf} T_j$  if  $U(T_i)$  is installed at node r before  $U(T_j)$ .

**Lemma 4.3.** If for every edge  $(T_i, T_j)$  in the serialization graph  $T_i <_{tf} T_j$ , then the serialization graph is acyclic.

**Proof.** Similar to Lemma 4.1.

**Lemma 4.4.** Let G be a tf-RAG. Let R and S be the propagation functions defined in (4.3a) and (4.3b). Let  $(T_i, T_j)$  be an edge in the global serilaization graph. Then  $T_i <_{tf} T_j$ .

## Proof.

Let  $T_i$  be local to node v and  $T_j$  to node w.

Case 1. Transactions  $T_i$  and  $T_j$  are local to the same node (v = w). Since  $(T_i, T_j)$  is an edge in the serialization graph,  $T_i$  must be serialized before  $T_j$  at v. Therefore,  $U(T_i)$  is effectively installed in the local copy before  $U(T_j)$ . The same order of installation is preserved at all nodes that are ancestors of v in D, including r. Case 2. (v, w) is an edge in D (either tree or forward). Clearly, at node  $v, U(T_i)$  is installed before  $U(T_j)$ . The same order of installation must hold for any ancestor of v because  $U(T_i)$  is appended to UPDATES(v) before  $U(T_j)$ , and the only way that  $U(T_j)$  can get to v's ancestors is through v itself (propagation occurs along tree edges only). Thus at node r $U(T_i)$  is installed before  $U(T_j)$ .

Case 3. (w, v) is an edge in D. Similar to Case 2.

Cases 1, 2, and 3 exhaust all possibilities. Thus  $T_i <_{tf} T_j$ .  $\Box$ 

**Theorem 4.2.** Let G = (V, E) be a tf-RAG. Let R and S be the propagation functions defined in (4.3a) and (4.3b). Then any execution characterized by G, R and S is serializable.

**Proof.** Follows trivially from Lemmas 4.4 and 4.3.  $\Box$ 





To illustrate the advantage of the protocol presented in this section over the topological protocol, consider the example of Figure 4.2. We are interested in the length of characteristic paths (*lcp*) between four pairs of nodes (one for very edge in the *RAG* of Figure 4.2(a)). From Figures 4.2(b) and 4.2(c) we see that the tfpropagation results in all but one of these paths being of length 1, while the topological propagation yields two characteristic paths of length greater than 1. It is not hard to see that, in general, the tf-propagation can always do at least as well as the topological propagation (for tf-*RAG*s).

#### 4.3. A Special Case: Loopless RAGs.

For some RAGs we can devise an even more efficient protocol than the tf-graph one. These RAGs are ones without any "loops," i.e., without undirected cycles. In this case we can propagate updates along all RAG edges, obtaining the best possible performance. Although the result can be expressed simply, the proof is substantially harder than the others we have presented.

**Definition 4.4.** [GaKo87] Let G = (V, E)be our *RAG*. The *local serialization graph* of node  $v \in V$  is a directed graph whose vertex set contains all transactions local to v or to any node w such that  $(v, w) \in E$ . Its edges are computed according to the following rules:

- (i) For any two transactions local to v, it is determined whether there is a directed edge between them according to the standard dependency rules for centralized databases [Eswa79].
- (ii) Let transaction  $T_i$  be local to node v, transaction  $T_j$  local to some node w, and  $(v, w) \in E$ . Then if there is a data item d in the fragment controlled by w that is read by  $T_i$  and updated by  $T_j$ , and the update to d produced by  $T_j$  is installed at node v before  $T_i$  reads d, put in an edge  $(T_j, T_i)$ ; if the update is installed after  $T_i$  reads d, put in an edge  $(T_i, T_j)$ .
- (iii) For a pair of transactions  $T_i$  and  $T_j$  local to the same node w ((v, w)  $\in E$ ), put in an edge ( $T_i, T_j$ ) if  $T_i$  is installed by v before  $T_j$ , an edge ( $T_j, T_i$ ) otherwise.
- (iv) There is no edge between two transactions local to different nodes both of which are distinct from v.

**Definition 4.5.** A *legal* transaction schedule is the one for which all local serialization graphs are acyclic.

Definitions 4.4 and 4.5 formalize the workings of the local concurrency control mechanisms at every computer node. Note that rule (ii) of Definition 4.4 corresponds to the requirement that updates from nonlocal transactions be installed atomically and in the order in which they arrive.

**Definition 4.6.** Let G = (V, E) be a (global) serialization graph. Let  $(T_i, T_j)$  be an edge in it such that  $T_i$  and  $T_j$  are local to (distinct) nodes v and w of the corresponding RAG, respec-

tively. Then we say that edge  $(T_i, T_j)$  spans edge (v, w) or (w, v), whichever is present in the  $RAG.^{\dagger}$ 

**Definition 4.7.** Let G = (V, E) be a (global) serialization graph and let C be a cycle in it. Let  $G_C$  be the subgraph of the corresponding RAG that contains all the edges that are spanned by edges on C. Then C is said to be based on subgraph  $G_C$ .

**Definition 4.8.** Let G = (V, E) be a directed graph. A subgraph L of G is called a *loop* if, when the directions on its edges are ignored, it forms a simple cycle.

**Theorem 4.3.** A loopless RAG guarantees a serializable transaction execution schedule with any choice of functions R and S in the update propagation protocol.

**Proof.** As before G = (V, E) is the RAG. Let C be a cycle in the (global) serialization graph. Let  $G_C = (V_C, E_C)$  be the subgraph of G on which C is based. We will show, by induction on k, the cardinality of  $V_C$ , that C cannot exist. For k = 1 it is obviously true. Suppose it is also true for all k < l. Now let k = l. Since G is loopless, so is  $G_C$ , and there must be some node  $v \in V_C$  which is the head or the tail of only one edge. The general strategy of the proof will be to arrive at a contradiction by transforming Cinto a new cycle which still corresponds to a legal schedule but is based on a smaller subgraph of the RAG (with the cardinality of the vertex set equal to l-1). Consider the following two cases.

Case 1. v is the tail of an edge. Let w be the head of this edge, i. e.,  $(v, w) \in E_C$ . Let u be the number of paths on cycle C that consist exclusively of transactions local to v. (In Figure 4.3, u = 3. These paths are represented by solid lines. For our purposes, a single node can be considered a path.) For j = 1, ..., u, let  $T_{lj}$  be the vertex on C that immediately precedes the *j*-th path, and  $T_{m_j}$ , the vertex that immediately follows it. Since w is the only node in S that shares an edge with v, one can conclude that transactions  $T_{lj}$  and  $T_{m_j}$ , for all j = 1, ..., u, are local to w. Finally let P denote the collection of (disjoint paths) on C that consist of transactions local to nodes other than v.

<sup>&</sup>lt;sup>†</sup> Note that one of these two edges must be in the RAG for edge  $(T_i, T_j)$  to be present in G.



**Figure 4.3.** Cycle C(u = 3).

Let  $L_w$  denote the local serialization graph of node w. We will show, by induction on u, that P cannot be totally contained in  $L_w$ . First, let u = 1. In this case P consists of just one path, a path from  $T_{m_1}$  to  $T_{l_1}$ . Suppose that P is totally contained in  $L_w$ . This implies that  $T_{m_1}$  must have been executed at node w before  $T_{l_1}$ . But since the order of installation of these transactions' updates at v must be the same, there is an edge  $(T_{m_1}, T_{l_1})$  in  $L_v$ , the local serialization graph of node v. There is also a path from  $T_{l_1}$  to  $T_{m_1}$  in  $L_v$ . Hence,  $L_v$  contains a cycle, which is impossible for a legal schedule. Thus, for u = 1, P cannot be totally contained in  $L_w$ .

Proceeding by induction, suppose that for some u - 1, P cannot be totally contained in  $L_w$ . Assume C has u paths on it consisting exclusively of transactions local to v. Let X be one such path (from  $T_{l_1}$  to  $T_{m_1}$ ). Let us introduce a new data item d into the fragment controlled by w. This new item will be read only by transaction  $T_{l_1}$  and overwritten only by  $T_{m_1}$  (in that order). This creates an edge  $(T_{l_1}, T_{m_1})$  in the (global) serialization graph as well as in  $L_w$ (if it was not there before). Let us call the technique of artificially creating a precedence edge shortcutting. Note that when we shortcut from  $T_{l_1}$  to  $T_{m_1}$ , no cycle is created in  $L_w$  (otherwise there would have been a cycle in the (global) serialization graph with P of size 1, which was shown not to be possible). Thus the modified

schedule is still legal. However, we end up with a cycle in the (global) serialization graph with P of size u - 1, which contradicts the induction hypothesis. Thus, we conclude that C cannot exist.

Now we are forced to assume that if a cycle C does exist, P is not totally contained in  $L_w$ . This implies that if we shortcut from  $T_{l_j}$  to  $T_{m_j}$ , for all j, the result will be a cycle in the serialization graph that is based on a subgraph of G with l-1 nodes. However,  $L_w$  will remain acyclic, and hence, the schedule will still be legal. (Note that other local serialization graphs are unaffected by shortcutting since the newly introduced data items can be read and overwritten only by transactions local to w.) This contradicts the induction hypothesis (induction on k). Thus the serialization graph must be acyclic.

Case 2. Assume that v is the head of an edge  $((w, v) \in E)$ . Let C be a cycle in the serialization graph, and let P be as before. Since in this case  $L_w$  contains all transactions local to v, P cannot be totally contained in  $L_w$  (otherwise P plus transactions local to v would form a cycle within  $L_w$ , rendering the corresponding schedule illegal). Thus, we can shortcut from  $T_{l_j}$  to  $T_{m_j}$ , for all j, without violating the legality of the schedule and, at the same time, creating a cycle based on a subgraph of G with l-1 nodes, which is in contradiction with the induction hypothesis.  $\Box$ 

Since loopless RAGs permit the choice of any propagation functions, we can always achieve the perfect propagation graph. Thus, we can, clearly, do better than with either topological or tf-propagation.

#### 4.4. More on the General Case.

In this subsection we combine the results of Sections 4.1 and 4.2 to derive a more powerful propagation protocol for the general case. Let G = (V, E)be an acyclic RAG.Let  $L = (V_L, E_L)$  be the subgraph of G consisting of all the edges that lie on a loop. Let  $L_1 = (V_{L_1}, E_{L_1}), ..., L_m = (V_{L_m}, E_{L_m})$  be the weakly connected components of L [Chri75]. For each i = 1, ..., m, let  $||V_{L_i}|| = k_i$ , and let  $ord_i: V_{L_i} \rightarrow \{1, 2, ..., k_i\}$  be a topological order on the vertices of  $L_i$ . Then define the propagation functions as follows:

$$R_{1}(v) = \{ ord_{i}^{-1}(ord_{i}(v)+1) \}$$

$$\bigcup \{ w \colon w \in V - V_{L} \text{ and } (v,w) \in E \}$$

$$R_{2}(v) = \{ w \colon w \in V - V_{L} \text{ and } (v,w) \in E \}$$

$$R_{2}(v) = \{ w \colon w \in V \text{ and } (v,w) \in E \}$$

$$R(v) = \begin{cases} R_1(v) & \text{if } v \in V_{L_i} \text{ and } ord_i(v) < k_i \\ R_2(v) & \text{if } v \in V_{L_i} \text{ and } ord_i(v) = k_i \text{ (4.4a)} \\ R_3(v) & \text{if } v \in V - V_L \end{cases}$$

$$S_{1}(v) = \{ ord_{i}^{-1}(ord_{i}(v)-1) \}$$

$$\bigcup \{ w \colon w \in V - V_{L} \text{ and } (v,w) \in E \}$$

$$S_{2}(v) = \{ w \colon w \in V - V_{L} \text{ and } (w,v) \in E \}$$

$$S_{3}(v) = \{ w \colon w \in V \text{ and } (w,v) \in E \}$$

$$S(v) = \begin{cases} S_1(v) & \text{if } v \in V_{L_i} \text{ and } ord_i(v) > 1 \\ S_2(v) & \text{if } v \in V_{L_i} \text{ and } ord_i(v) = 1 \\ S_3(v) & \text{if } v \in V - V_L \end{cases}$$
(4.4b)

Informally, the above definition of functions Rand S means that the nodes of each subgraph  $L_i$ propagate updates among themselves strictly in a topological order. In addition, propagation takes place along every edge not in  $E_L$  (in reverse direction of the edge).

We redefine relation < of Section 4.1 to apply to a pair of transactions that are local to nodes in the same weakly connected component of L. Thus,  $T_i < T_j$  iff  $T_i$  and  $T_j$  are local to nodes v and w respectively,  $v, w \in V_{L_r}$  for some r,  $1 \le r \le m$ , and  $U(T_i)$  is installed at node  $ord_r^{-1}(1)$ before  $U(T_j)$ .

**Lemma 4.5.** If functions R and S are defined as in (4.4a) and (4.4b), then for every edge  $(T_i, T_j)$  in the serialization graph where  $T_i$  and  $T_j$  are local to nodes v and w respectively and  $v, w \in V_{L_r}$  for some  $r, 1 \le r \le m$ , we have  $T_i < T_j$ .

**Proof.** The proof is very similar to that of Lemma 4.2, except that now we have to consider the possibility of  $U(T_j)$  reaching node  $ord_r^{-1}(1)$  via nodes not in  $L_r$ . However, that would imply the existence of an undirected path between w and  $ord_r^{-1}(1)$  with nodes not in  $L_r$ , which, in turn, means that those nodes must be in the same weakly connected component of L as w and  $ord_r^{-1}(1)$ , a contradiction.  $\Box$  **Lemma 4.6.** Let  $G_s$  be a global serialization graph that contains a cycle C. Let  $G_r$  be the corresponding RAG. Finally, let C be based on  $G_C$ , a subgraph of  $G_r$ . Then  $G_C$  must contain a loop.

**Proof.** Suppose  $G_C$  does not contain a loop. Consider a new database that consists of just those fragments that are vertices of  $G_C$  and whose read access patterns are defined by  $G_C$ . Suppose that only those transactions that are vertices on C are executed, and the resulting schedule is the one defined by C. Then C is the global serialization graph for the described execution and, as such, must be acyclic by Theorem 4.3, a contradiction.  $\Box$ 

**Theorem 4.4.** An execution characterized by an acyclic  $RAG \ G = (V, E)$  and the propagation functions of (4.4a) and (4.4b) is guaranteed to be serializable.

**Proof.** Suppose to the contrary. Let C be a cycle in the serialization graph. We show that C cannot exist. The proof is by induction on t, the number of loops that are in the subgraph of G on which C is based.

From Lemma 4.6 it follows that for t = 0 C cannot exist. So let us assume that no cycle can exist in the serialization graph that is based on a subgraph of G with fewer than t loops, and consider cycle C that is based on a subgraph with t loops, t > 0.

Let  $L_r$  be one of the weakly connected components of L that contribute loops to the subgraph on which C is based. (At least one such component must exist since t > 0.) Let  $T_r^1, ..., T_r^s$  be all transactions on C that are local to nodes in  $L_r$  and such that if edge  $(T_r^i, T)$  is on C, then T is local to a node not in  $L_r$ , for all  $i, 1 \leq i \leq s$ . Further, let  $Q_r^i$  be a transaction on Clocal to a node in  $L_r$  and such that all transactions on the path from  $T_r^i$  to  $Q_r^i$  that is part of Care local to nodes outside of  $L_r$ , for all  $i, 1 \leq i \leq s$ . That is, all  $T_r^i$ 's are points at which C exits  $L_r$  and all  $Q_r^i$ 's are points at which Centers  $L_r$ .<sup>†</sup>

If for every i,  $T_r^i < Q_r^i$ , then we can shortcut from  $T_r^i$  to  $Q_r^i$  (as in the proof of Theorem 4.3). Therefore we end up with a new cycle in the serialization graph that is based

<sup>&</sup>lt;sup>†</sup> Note that words *enter* and *exit* are used somewhat loosely here because C is a cycle not in G but in the serialization graph.

totally within  $L_r$ . It follows trivially from Lemma 4.5, however, that no such cycle can exist. So assume that  $Q_r^i < T_r^i$ , for some *i*. Then by shortcutting from  $Q_r^i$  to  $T_r^i$  we get a new cycle, based on a subgraph of *G* with fewer than *t* loops. (It consists of the path from  $T_r^i$  to  $Q_r^i$  that goes exclusively through the nodes not in  $L_r$ , except for its endpoints, and the artificial edge  $(Q_r^i, T_r^i)$ .) But by the induction hypothesis this is not possible.  $\Box$ 

## 5. Virtual Serializability as Correctness Criterion.

In this section we introduce a new correctness criterion for transaction processing in distributed systems, called *virtual serializability*. It is less strict than serializability, *i.e.*, all serializable schedules are also virtually serializable, but some virtually serializable ones are not serializable in the usual sense.

Before giving a formal definition of the property, we will try to intuitively motivate it. Because of the constraints that we introduced on transaction processing, the following interesting phenomenon is noted. Among all nonserializable schedules, there are some that cannot be identified as such by any transaction. In other words, every transaction in the schedule reads data that could be produced by a serial schedule, even though the global schedule is not serializable.



#### Figure 5.1.

To illustrate let us consider some examples. Figure 5.1 shows a RAG and a corresponding serialization graph with a cycle. The fact that the schedule is nonserializable can be detected at node 1 since transaction  $T_1$  reads

inconsistent values of data items from fragments  $F_2$  and  $F_3$ . These values are inconsistent because they depend on different versions of fragment  $F_4$ , before and after transaction  $T_4$  was run.

In the example of Figure 5.2, however, the nonserializable behavior cannot be seen by any of the transactions. Since nodes 2 and 3 do not read data outside of their respective fragments, the fragments cannot become inconsistent (in the sense of the previous paragraph). Thus neither node 1 nor 4 can detect the anomaly. Moreover, the cycle in Figure 5.2(b) was formed because node 1 saw the effects of transaction  $T_2$  before those of  $T_3$  and node 4 saw the reverse. Thus fragment  $F_1$  may now be inconsistent with fragment  $F_4$ . However, since there is no legal transaction that can read both of these two fragments, this situation will go undetected.



## Figure 5.2.

**Definition 5.1.** A cycle C in the serialization graph is called *observable* if it can be split into two edge-disjoint paths such that one of them consists solely of dependency edges and the other, solely of precedence edges. (An edge  $(T_i, T_j)$  is a dependency edge if  $T_j$  reads the value of a data item written by  $T_i$ ; it is a precedence edge if  $T_i$  reads the value of a data item overwritten by  $T_i$  [Bern79].)

The cycle in Figure 5.1(b) is observable (edges  $(T_1, T_2)$  and  $(T_2, T_4)$  are precedence edges;  $(T_4, T_3)$  and  $(T_3, T_1)$  are dependency edges), whereas the cycle in Figure 5.2 is not observable.

The significance of an observable cycle is that there is a transaction on it,  $T_1$ , that may read inconsistent data (see Figure 5.3).  $T_1$  is the first transaction on the precedence path and the last transaction on the dependency path. When it executes, it reads the new version of fragment  $F_3$  but the old version of fragment  $F_2$ . Since the former depends on the state of fragment  $F_m$ after the execution of  $T_m$  and the latter depends on the state of  $F_m$  before the execution of  $T_m$ , they are inconsistent. The conclusion that we can draw from this is that observable cycles justify their name.



Figure 5.3. Observable cycle. Transaction  $T_i$  is local to  $N(F_i)$ , for all *i*.

**Definition 5.2.** A transaction schedule is called *virtually serializable* if the corresponding serialization graph has no observable cycles.

**Definition 5.3.** Let  $L = (V_L, E_L)$  be a *RAG* loop. Let vertex  $s \in V_L$  be such that no edge in  $E_L$  is incident upon it. Let vertex  $t \in V_L$  be such that no edge in  $E_L$  is incident from it. Then s is called a *loop source* of L, and t, a *loop sink* of L.

Clearly, if a loop doesn't have loop sources or loop sinks, it is a (directed) cycle. Also, it is easy to see that the number of loop sources in a loop is always equal to the number of loop sinks.

**Definition 5.4.** L is a single-source (singlesink) loop if it contains exactly one source (sink). It is a multi-source (multi-sink) loop otherwise.

Lemma 5.1. (Acyclic) *RAGs* with no single-source loops guarantee virtually serializable schedules regardless of the choice of propagation functions.

**Proof.** Let  $G_r$  be an acyclic RAG with no single-source loops. Suppose that C is an observable cycle in the serialization graph. First of all, note that a precedence edge between two transactions that are local to different nodes always repeats the direction of the RAG edge between those nodes, whereas a dependency edge always goes in the opposite direction.

Since  $G_r$  has no single-source loops (or cycles), C must be based on a subgraph of  $G_r$  that includes a multi-source loop. But then C cannot be split in two paths as required by Definition 5.1 because the direction of edges along the loop changes more than twice (see Figure 5.2(a)). Therefore C is not observable.  $\Box$ 

Since cycles in RAGs can cause the creation of cycles in serialization graphs (including observable cycles) regardless of how propagation functions are defined, we still restrict ourselves to acyclic RAGs, just as we did in Section 4.

Replacing serializability with virtual serializability as correctness criterion helps make update propagation less restrictive. For RAGswith no single-source loops, for insatnce, update propogation can be totally unrestricted (even in the presence of multi-source loops). Recall for comparison, however, that to acheive serializability, we had to use restricted protocols for update propagation in the presence of any kind of loops.

For general acyclic RAGs, we can also make an improvement in the efficiency of the protocols, provided we can be satisfied with virtual serializability. Let G = (V, E) be a RAG. Let  $G_S = (V_S, E_S)$  be a subgraph that contains all the edges of G that lie on single-source loops. Let  $ord: V_S \rightarrow \{1, ..., k\}$ , where k is the cardinality of  $V_S$ , be a topological order on the vertices of  $G_S$ . Define the propagation functions as follows:

$$R_{1}(i) = \{ ord^{-1}(ord(i) + 1) \}$$
$$\bigcup \{ j: j \in V - V_{S} \text{ and } (i, j) \in E \}$$
$$R_{2}(i) = \{ j: j \in V - V_{S} \text{ and } (i, j) \in E \}$$
$$R_{3}(i) = \{ j: j \in V \text{ and } (i, j) \in E \}$$

$$R(i) = \begin{cases} R_1(i) & \text{if } i \in V_S \text{ and } ord(i) < k \\ R_2(i) & \text{if } i \in V_S \text{ and } ord(i) = k \\ R_3(i) & \text{if } i \in V - V_S \end{cases}$$
(5.1a)

$$S_{1}(i) = \{ ord^{-1}(ord(i) - 1) \}$$
$$\bigcup \{ j: j \in V - V_{S} \text{ and } (j, i) \in E \}$$
$$S_{2}(i) = \{ j: j \in V - V_{S} \text{ and } (j, i) \in E \}$$
$$S_{3}(i) = \{ j: j \in V \text{ and } (j, i) \in E \}$$

$$S(i) = \begin{cases} S_1(i) & \text{if } i \in V_S \text{ and } ord(i) > 1\\ S_2(i) & \text{if } i \in V_S \text{ and } ord(i) = 1 \quad (5.1b)\\ S_3(i) & \text{if } i \in V - V_S \end{cases}$$

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In simple terms, this means that the nodes of subgraph  $G_S$  enact among themselves a topological propagation protocol, whereas the nodes not in  $G_S$  propagate updates along all edges in  $E - E_S$  (in reverse direction of the edges). In addition, propagation occurs along every edge connecting a node in  $G_S$  and a node not in  $G_S$ .

**Theorem 5.1.** Propagation functions R and S defined in (5.1a) and (5.1b) guarantee virtual serializability for schedules characterized by acyclic RAGs.

**Proof.** Suppose this is not true. Let C be an observable cycle in the global serialization graph. From Definition 5.1 and the observation in the proof of Lemma 5.1, it follows that the subgraph on which C is based must be a singlesource loop. Therefore, C is based on a subgraph of  $G_S$ . ( $G_S$  contains all edges on singlesource loops.)

The nodes of  $G_S$ , according to (5.1a) and (5.1b), engage in a topological propagation. In the absence of nodes outside  $G_S$ , Lemma 4.2 (and hence Theorem 4.1) would be valid and there could be no cycles like C. However, it could be the case that update propagations by nodes outside  $G_S$  invalidate Lemma 4.2. We now show that this is not the case.

Consider the edge  $(T_j, T_i)$  in C. If  $T_i$  and  $T_i$  are local to the same node, or if the edge is a dependency edge, then whatever node receives  $U(T_i)$  must receive  $U(T_i)$  first.  $(U(T_i)$  is added to UPDATES(i) before  $U(T_i)$ ; see Section 2.1.) Therefore,  $T_j < T_i$ . However, if  $(T_j, T_i)$  is a precedence edge,  $U(T_i)$  is sent out of node *i* without  $U(T_i)$ . If  $U(T_i)$  were only transmitted along the topological propagation chain, then  $U(T_i)$  would arrive first at all nodes, including the last one, l  $(l = ord^{-1}(1))$ . However, by following a path outside  $G_S$ ,  $U(T_i)$  can conceivably skip ahead of  $U(T_i)$  and arrive at *l* first. For this to happen, there must be a RAG path leading to the node where  $T_i$  executed, say v, and originating at some other node in  $G_C$ , call it w. (Actually, ord(w) < ord(v).) As mentioned earlier, the path (except the endpoints) must be outside  $G_S$ , else  $U(T_i)$  could not skip ahead.

However, any (unidirectional) path connecting two vertices in a single-source loop creates another single-source loop. (Recall that the RAG is acyclic.) Therefore, the path must also be in  $G_S$ , a contradiction.  $\Box$ 

#### 6. Conclusions.

We believe that Bakunin data networks offer a valuable alternative to known mechanisms for managing replicated data. Our mechanism yields a high degree of data availability and node autonomy while still ensuring serializability (or virtual serializability). It tolerates arbitrary communications failures, including network partitions that are not consistently detected.

The major drawback is that transactions must be pre-analyzed and the resulting RAGmust be acyclic. (Although we did not discuss it here, these assumptions can be periodically relaxed. However, to avoid inconsistencies, some type of locking must be performed in these cases. The result is that availability suffers.) We believe that this is not a limitation of our particular approach, but an inherent property of dynamic failure environments. If for a particular application it is essential to run arbitrary transactions, then one must either give up serializability or the ability to operate in dynamic failure environments. If the application demands serializability and operation in the face of unpredictable communication failures, then the transactions must be simple enough so that they can be pre-analyzed. Furthermore, it is necessary to structure the application so that updates to a fragment originate at a single node and the resulting RAG is acyclic.

If a Bakunin approach is used, then the major implementation problem is the propagation of updates. If transactions running at a node  $N(F_1)$  read data from fragment  $F_2$ , it is important that the updates from  $N(F_2)$  reach  $N(F_1)$  as expediently as possible. For loopless RAGs and for no-single-source-loop RAGs under virtual serializability, we have obtained the most efficient propagation protocols possible. For other RAGs, our protocols yield good performance, although finding the best one is an open question. For instance, the chain protocol operates correctly with any topological ordering on the nodes, but finding the best ordering for a particular communication network may be a difficult problem.

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