

**Precept Outline**

- Review of Lectures 13 and 14:
  - Hash Tables
  - K-d Trees

**Relevant Book Sections**

- Book chapters: 3.4

**A. Review: Hash Tables + K-d Trees**

Your preceptor will briefly review key points of this week's lectures.

**B. Hash Tables****Part 1: Linear probing vs. separate chaining**

Consider the following sequence of (integer) insertions into an empty hash table of capacity 11, where the hash function  $h(i)$  returns  $i \% 11$ :

15, 90, 53, 100, 34, 65, 20

Suppose that the symbol table is implemented as a *linear-probing* hash table. Which positions of the `keys[]` array contain null values after all 7 insertions?

Suppose we perform the same sequence of insertions with the same hash function, but use a *separate-chaining* table instead. What linked list sizes are present in the table after all 7 insertions?

**C. K-d Trees**

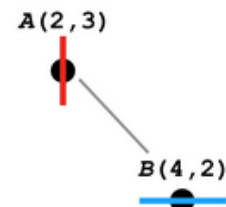
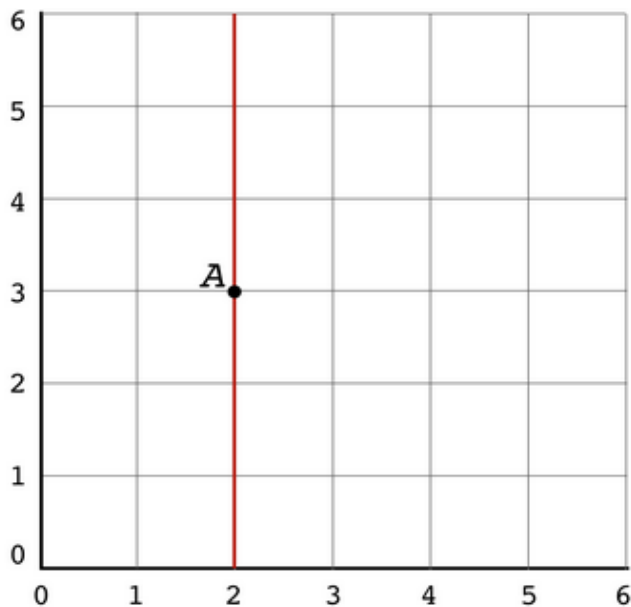
Draw the 2d-tree that results from inserting the following points:

A	B	C	D	E	F	G
(2, 3)	(4, 2)	(4, 5)	(3, 3)	(1, 5)	(4, 4)	(1, 1)

Additionally, draw each point on the grid, as well as the vertical or horizontal line that runs through the point and partitions the plane or a subregion thereof.

**Recall:** We take the convention that while inserting, we move left if the coordinate of the inserted point is less than the coordinate of the current node; and go right if it is greater than **or equal**.

Use the images below to draw your grid/tree.



Determine each point's bounding box and fill them into the table below.

<b>A</b>	$[-\infty, \infty] \times [-\infty, \infty]$
<b>B</b>	
<b>C</b>	
<b>D</b>	
<b>E</b>	
<b>F</b>	
<b>G</b>	

Number the (non-null) nodes in the sequence they are visited by a *range query* with the rectangle shown below. Which subtrees are pruned? (Some null subtrees may be pruned, and some may not be.)

**Remember.** The range search algorithm recursively searches in both the left and right subtrees unless the bounding box of the *current* node does not intersect the query rectangle. If both do, our convention is to visit the left one first.

