

# COS 217: Introduction to Programming Systems

Virtual Memory, Storage Hierarchy, and Caching



**PRINCETON UNIVERSITY**

# Agenda



## Virtual Memory

Virtual vs. physical memory

Page tables

Page faults



## Storage and Locality

The storage hierarchy

Spatial and temporal locality

Caching



## Effective Caching

Block size

Eviction policy

Order of operations



# Processes

## Program

- Executable code
- A static entity

## Process

- An instance of a program in execution
- A dynamic entity: has a time dimension
- Each process runs one program
  - E.g. the process with Process ID 12345 might be running emacs
- One program can run in multiple processes
  - E.g. PID 12345 might be running emacs, and PID 23456 might also be running emacs – for the same user or for a different user

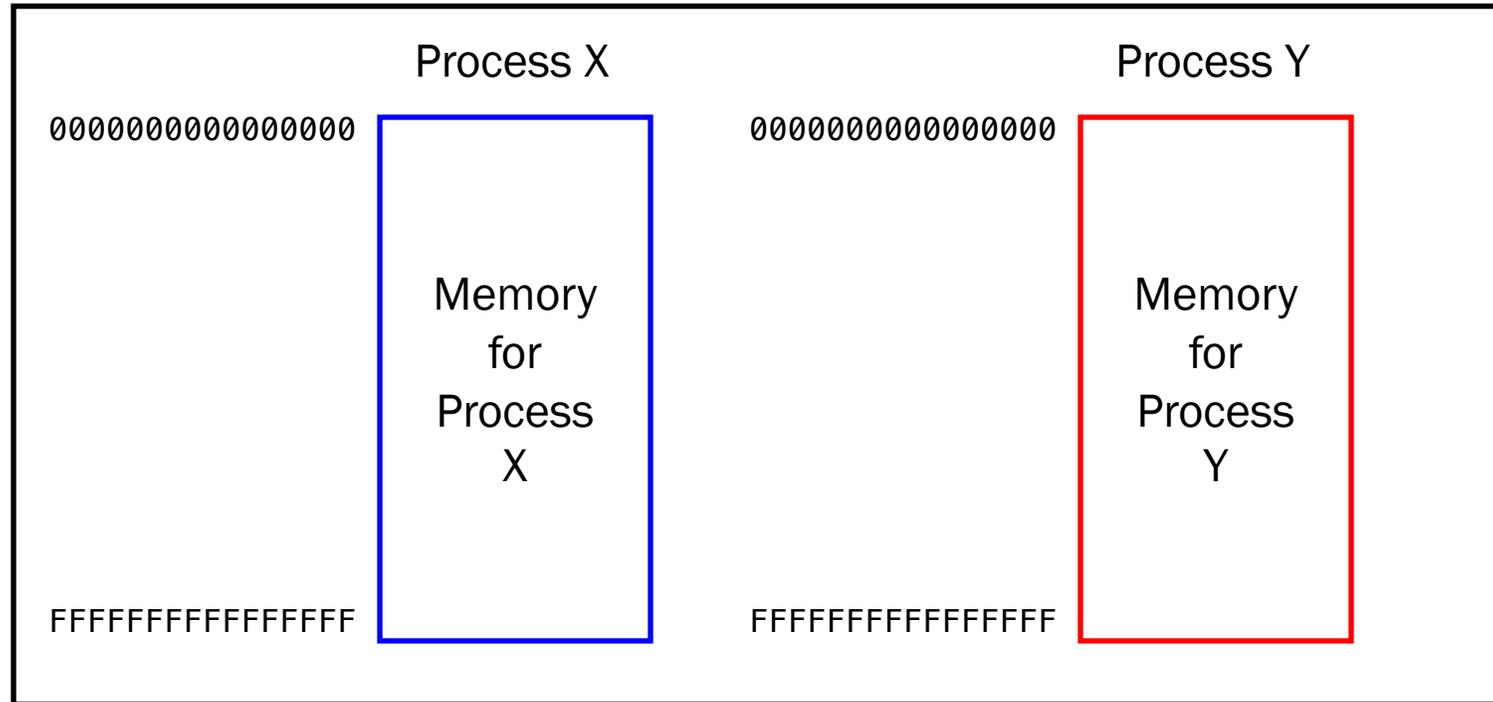


# Processes: Two Key Illusions

1. Processes believe they have *private control flow* (i.e., they own the whole CPU, all the time)
2. Processes believe they have a *private address space* (i.e., they own all the memory that the machine has or could have)



# Private Address Space: Illusion



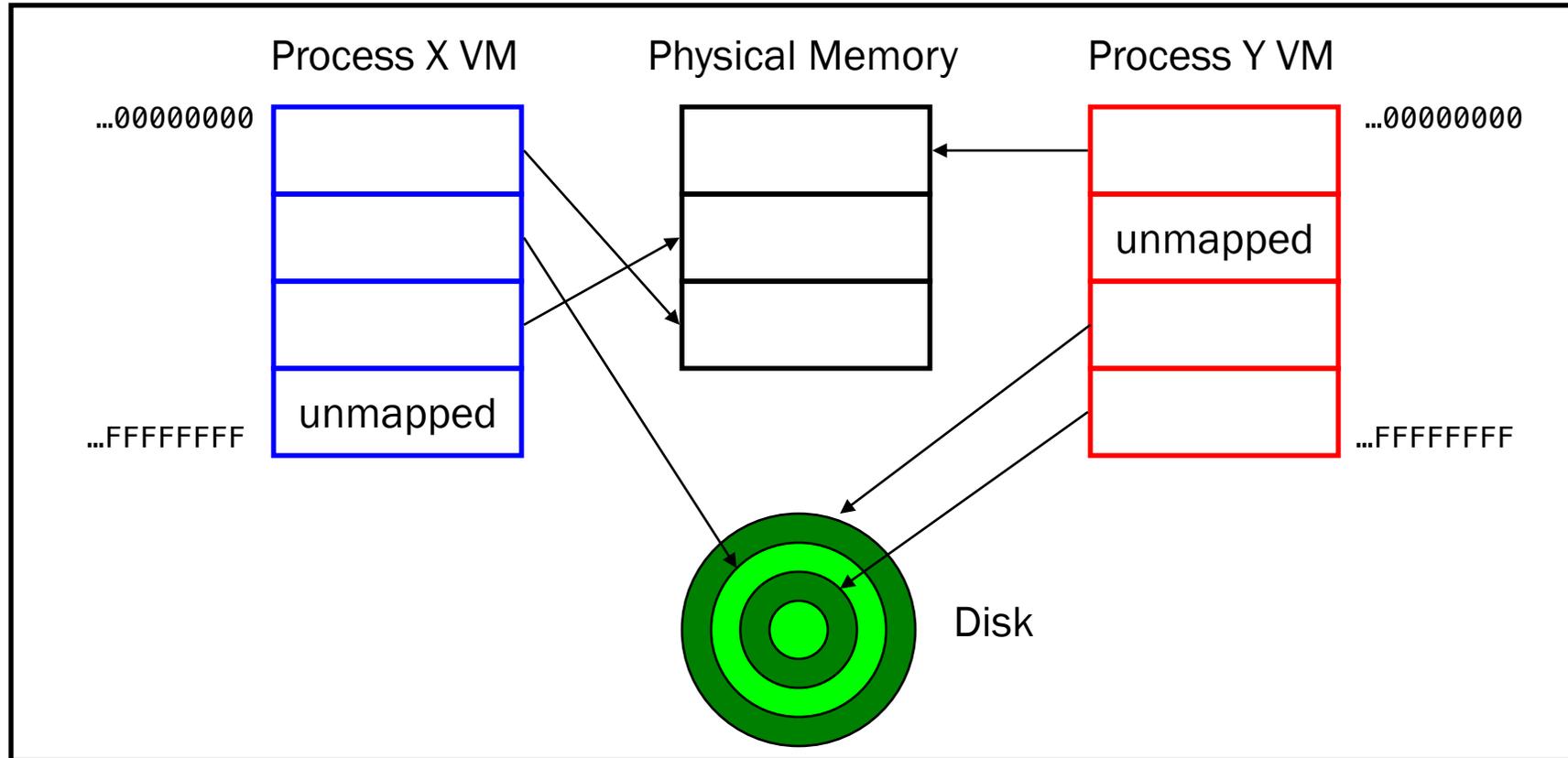
Each process sees main memory as

Huge:  $2^{64} = 16$  EB (16 exabytes) of memory  $\approx 10^{19}$  bytes

Uniform: contiguous memory locations from 0 to  $2^{64}-1$



# Private Address Space: Reality



Memory is divided into **pages**

- At any time, some pages are in physical memory, some on disk ( $\approx$  in a file)
- OS and hardware swap pages between physical memory and disk
- Multiple processes share physical memory



# Virtual & Physical Addresses

## Question

- How do OS and hardware implement virtual memory?

## Answer (part 1)

- Distinguish between **virtual addresses** and **physical addresses**



# Virtual & Physical Addresses (cont.)

## Virtual address



- Identifies a location in a particular process's virtual memory
  - Independent of size of physical memory
  - Independent of other concurrent processes
- Consists of virtual page number & offset
- Used by **application programs**

## Physical address



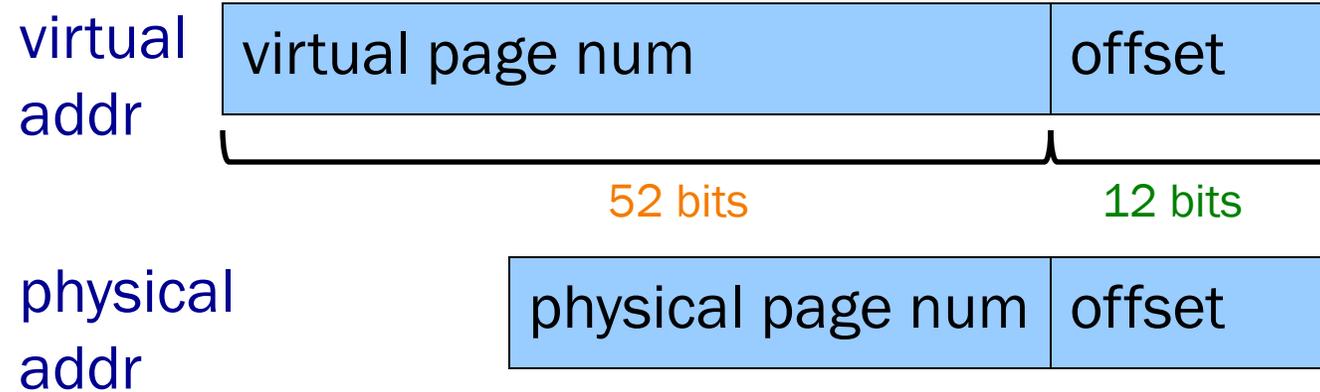
- Identifies a location in physical memory
- Consists of physical page number & offset
- Known only to **OS** and **hardware**

Note:

- Offset is same in virtual addr and corresponding physical addr



# ArmLab Virtual & Physical Addresses

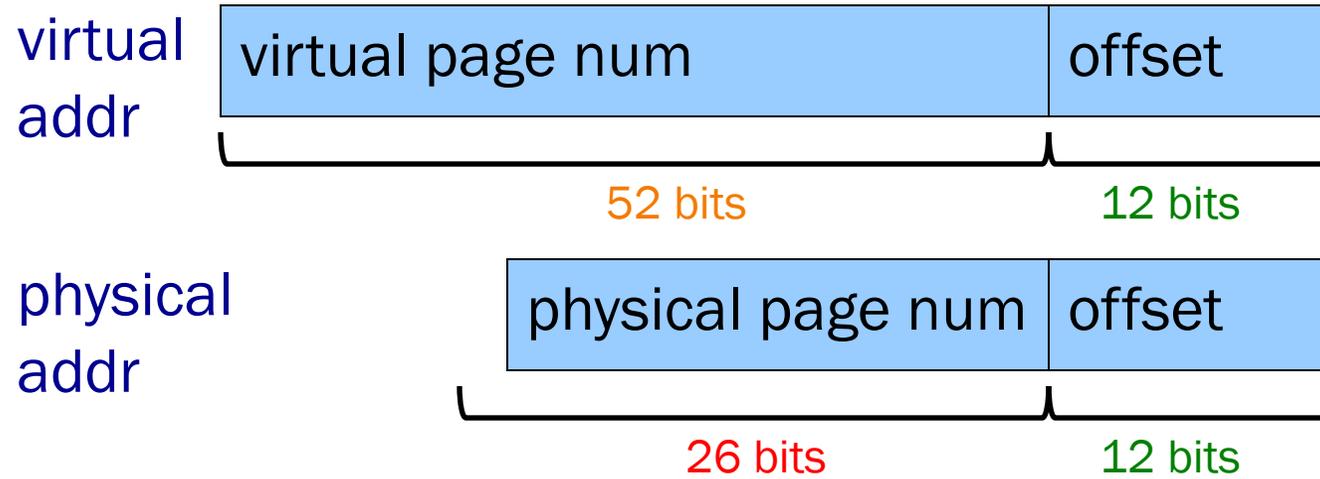


## On ArmLab:

- Each **virtual** address consists of 64 bits
  - There are  $2^{64}$  bytes of virtual memory (per process)
- Each **offset** is 12 bits
  - Each page consists of  $2^{12}$  (4096) bytes
- Each **virtual page number** consists of  $64 - 12 = 52$  bits
  - There are  $2^{52}$  virtual pages



# ArmLab Virtual & Physical Addresses



## On ArmLab:

- Each **physical** address consists of 38 bits
  - There are  $2^{38}$  (256G) bytes of physical memory (per computer)
- Each offset is 12 bits
  - Each page consists of  $2^{12}$  bytes
- Each physical page number consists of  $38 - 12 = 26$  bits
  - There are  $2^{26}$  physical pages



# Page Tables

## Question

- How do OS and hardware implement virtual memory?

## Answer (part 2)

- Maintain a **page table** for each process (stored in physical memory)



# Page Tables (cont.)

## Page Table for Process 1234

Virtual Page Num	Physical Page Num or Disk Addr
0	Physical page 5
1	(unmapped)
2	Spot X on disk
3	Physical page 8

...

...

**Page table** maps each in-use virtual page to:

- A physical page, or
- A spot on disk



# Storing Page Tables

## Question

- Where are the page tables themselves stored?

## Answer

- In main memory

## Question

- What happens if a page table is swapped out to disk???!?

## Answer

- It hurts! So don't do that, then!
- OS is responsible for swapping
- Special logic in OS “pins” page tables to physical memory
  - So they never are swapped out to disk



# Page Faults

## Question

- How do OS and hardware implement virtual memory?

## Answer (part 3)

- Trigger a **page fault** for accesses to virtual pages that are swapped out (on disk)



# Page Faults

- Process executes instruction that references virtual memory
- CPU determines virtual page
- CPU checks if required virtual page is in physical memory: **no!**
  - CPU generates **page fault**
  - OS gains control of CPU
  - OS (potentially) evicts some page from physical memory to disk, loads required page from disk to physical memory
  - OS returns control of CPU to process – to **same instruction**
- Process executes instruction that references virtual memory
- CPU checks if required virtual page is in physical memory: **yes**
- CPU does load/store from/to physical memory

Virtual memory enables the illusion of private address spaces



# VM Effects on Security and Speed



Q: What effect does virtual memory have on the security and speed of processes?

	Security	Speed
A.		
B.		
C.		
D.		

Let's start by considering security...



# Consequences of Virtual Memory

## Memory protection among processes

- Process's page table references only physical memory pages that the process currently owns
- Process can't accidentally/maliciously affect physical memory used by another process

## Memory protection within processes

- Permission bits in page-table entries indicate whether page is read-only, etc.
- Allows CPU to prohibit
  - Writing to RODATA & TEXT sections
  - Access to protected (OS owned) virtual memory



# VM Effects on Security and Speed



Q: What effect does virtual memory have on the security and speed of processes?

	Security	Speed
A.		
B.		
C.		
D.		

OK, so part of the answer is:

Security



But what about speed?



# Revisiting Page Tables...

## Question

- Doesn't each logical memory access require **two** physical memory accesses – one to access the page table, and one to access the desired datum?

## Answer

- Conceptually, yes!  
(And page tables are stored hierarchically as trees, so it can be even worse than 2 accesses!)

## Question

- Isn't that inefficient?

## Answer

- Conceptually: yes, but in actuality not really ... let's see why!



# Agenda



## Virtual Memory

Virtual vs. physical memory

Page tables

Page faults



## Storage and Locality

The storage hierarchy

Spatial and temporal locality

Caching



## Effective Caching

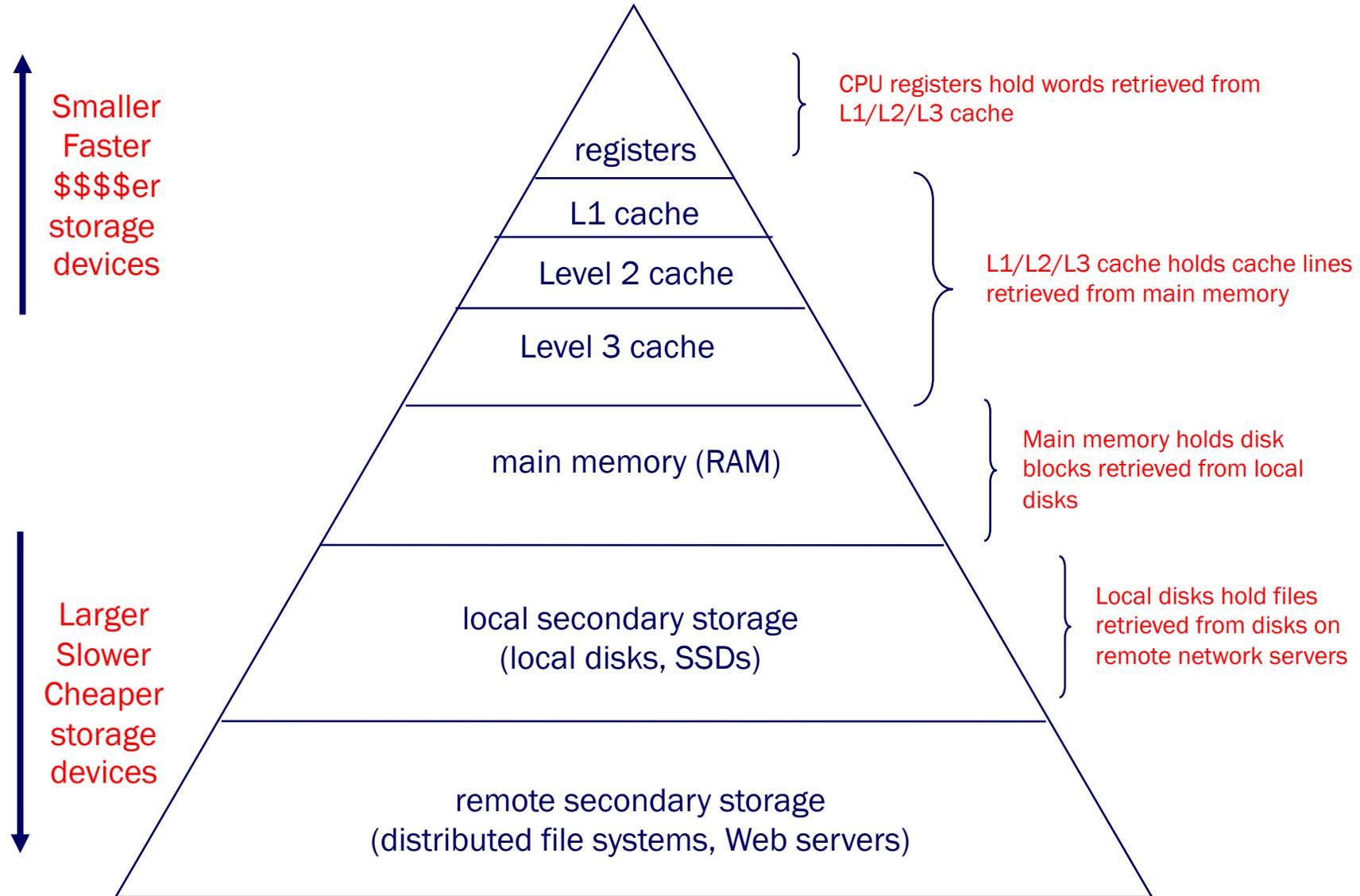
Block size

Eviction policy

Order of operations



# Typical Storage Hierarchy





# Typical Storage Hierarchy

## Factors to consider:

- Capacity
- Latency (how long to do a read)
- Bandwidth (how many bytes/sec can be read)
  - Weakly correlated to latency: reading 1 MB from a hard disk isn't much slower than reading 1 byte
- Volatility
  - Do data persist in the absence of power?



# Typical Storage Hierarchy

## Registers

- **Latency:** 0 cycles
- **Capacity:** 8-256 registers (31 8-byte general purpose registers in AArch64)

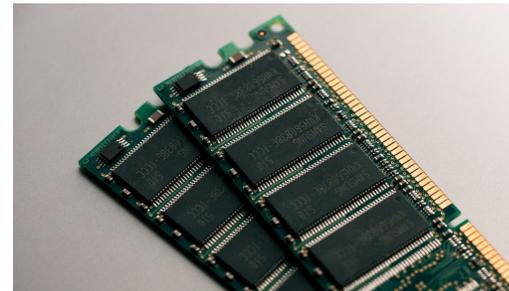


## L1/L2/L3 Cache

- **Latency:** 1 to 40 cycles
- **Capacity:** 32KB to 32MB

## Main memory (RAM)

- **Latency:** ~ 50-100 cycles
  - 100 times slower than registers
- **Capacity:** GB





# Typical Storage Hierarchy

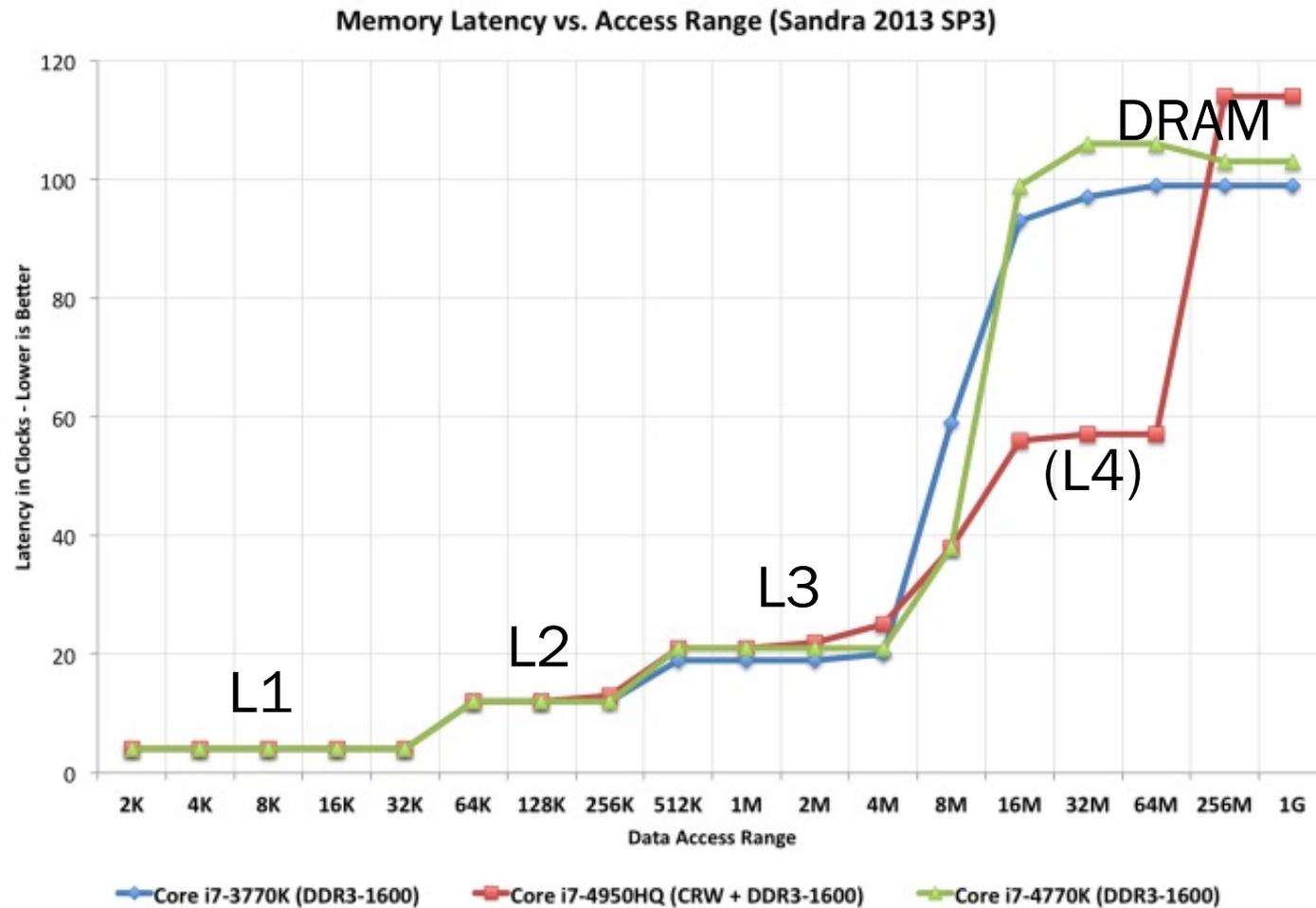
## Local secondary storage: disk drives

- Solid-State Disk (SSD):
  - Flash memory (nonvolatile)
  - **Latency:** 0.1 ms (~ 300k cycles)
  - **Capacity:** 128 GB – several TB
- Hard Disk:
  - Spinning magnetic platters, moving heads
  - **Latency:** 10 ms (~ 30M cycles)
  - **Capacity:** 1 – dozens of TB





# Cache / RAM Latency





# Disks

HDD



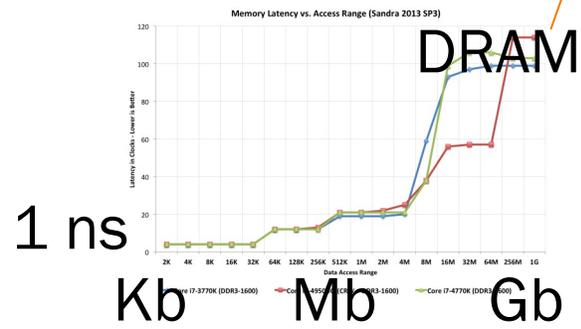
1 ms

SSD

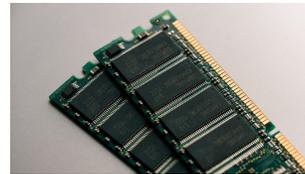


1  $\mu$ s

DRAM



1 ns



Kb

Mb

Gb

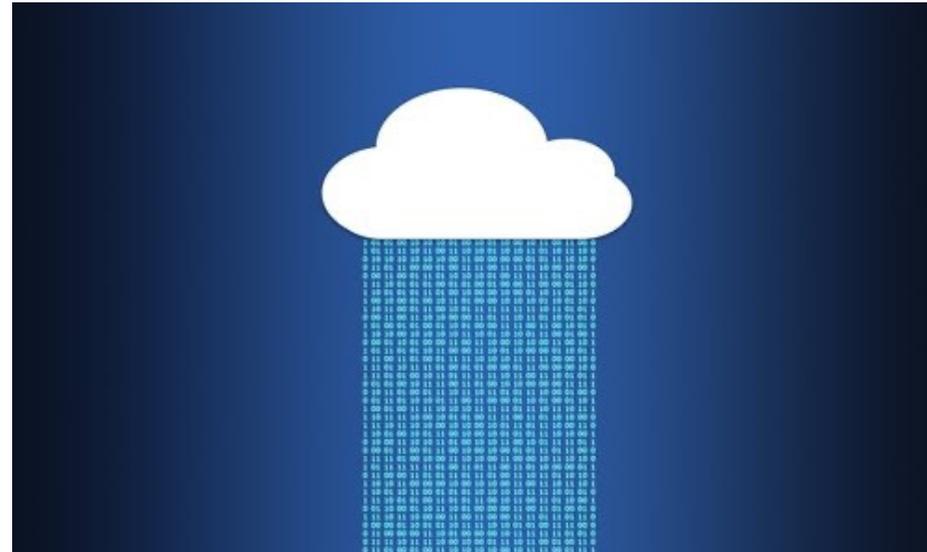
Tb



# Typical Storage Hierarchy

## Remote secondary storage (a.k.a. “the cloud”)

- **Latency:** tens of milliseconds
  - Limited by the speed of light (and network bandwidth)
- **Capacity:** essentially unlimited





# Storage Device Speed vs. Size

## Facts:

- CPU needs sub-nanosecond access to data to run instructions at full speed
- **Fast** storage (sub-nanosecond) is small (100-1000 bytes)
- **Big** storage (gigabytes) is slow (15 nanoseconds)
- **Huge** storage (terabytes) is *glacially* slow (milliseconds)

## Goal:

- Need many gigabytes of memory,
- but with fast (sub-nanosecond) average access time

## Solution: **locality** allows **caching**

- Most programs exhibit good **locality**
- A program that exhibits good locality will benefit from proper **caching**, which enables good **average** performance



# Locality

## Two kinds of **locality**

- **Temporal** locality
  - If a program references item X now,  
then it probably will reference X again soon
- **Spatial** locality
  - If a program references item X now,  
then it probably will reference item at address  $X \pm 1$  soon

Most programs exhibit good temporal and spatial locality



# Locality Example

## Locality example

```
sum = 0;  
for (i = 0; i < n; i++)  
    sum += a[i];
```

Typical code  
(good overall locality)

### Temporal locality

- *Data:* Whenever the CPU accesses `sum`, it accesses `sum` again shortly thereafter
- *Instructions:* Whenever the CPU executes `sum += a[i]`, it executes `sum += a[i]` again shortly thereafter

### Spatial locality

- *Data:* Whenever the CPU accesses `a[i]`, it accesses `a[i+1]` shortly thereafter
- *Instructions:* Whenever the CPU executes `sum += a[i]`, it executes `i++` (which are the next machine language instructions) shortly thereafter

# Caching



## Cache

- Fast access, small capacity storage device
- Acts as a staging area for a subset of the items in a slow access, large capacity storage device

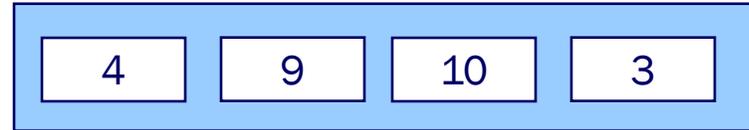
## Good locality + proper caching

- ⇒ Most storage accesses can be satisfied by cache
- ⇒ Overall storage performance improved



# Caching in a Storage Hierarchy

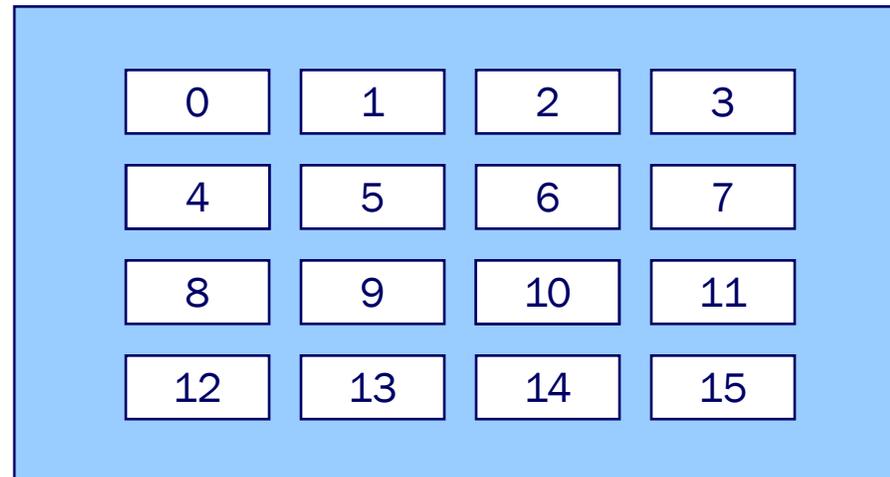
Level k:



Smaller, faster device at level k caches a subset of the blocks from level k+1

Blocks copied between levels

Level k+1:



Larger, slower device at level k+1 is partitioned into blocks



# Cache Hits and Misses

## Cache hit

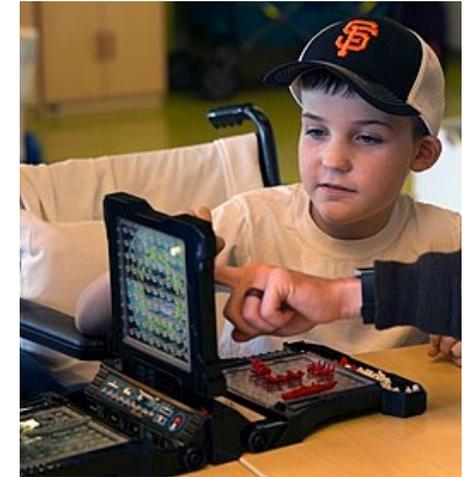
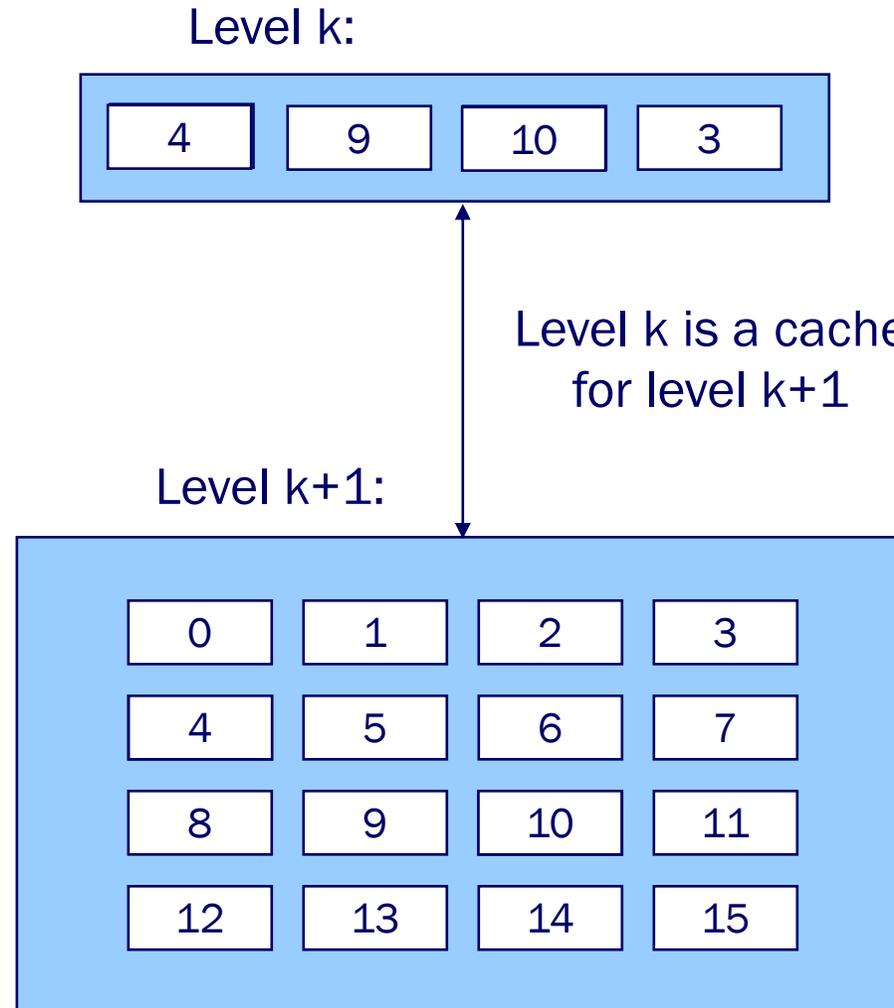
- E.g., request for block 10
- Access block 10 at level k
- Fast!

## Cache miss

- E.g., request for block 8
- **Evict** some block from level k
- Load block 8 from level k+1 to level k
- Access block 8 at level k
- Slow!

## Caching goal:

- Maximize cache hits
- Minimize cache misses





# VM Effects on Security and Speed



Q: What effect does virtual memory have on the security and speed of processes?

	Security	Speed
A.		
B.		
C.		
D.		

So, with caching, we *finally* arrive at the answer:

Security	Speed
	often little or no change



# Agenda



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Virtual vs. physical memory

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Page faults



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## Effective Caching

Block size

Eviction policy

Order of operations



# Do Exam Questions Exhibit Temporal Locality?



Here's a real question from an old exam:

For caching in a memory hierarchy,  
what is the best motivation for a *larger* cache block size?

A. Temporal Locality

B. Spatial Locality

C. Both

D. Neither

B

Spatial locality makes use of subsequent data after a given read, so keeping more data that is about to be used is a win.



# Cache Block Size

## Large block size:

- + do data transfer less often
- + take advantage of spatial locality
- longer time to complete data transfer
- less advantage of temporal locality

**Small block size:** the opposite

**Typical:** Lower in pyramid  $\Rightarrow$  slower data transfer  $\Rightarrow$  larger block sizes

Device	Block Size
Register	8 bytes
L1/L2/L3 cache line	128 bytes
Main memory page	4KB or 64KB
Disk block	512 bytes to 4KB
Disk transfer block	4KB (4096 bytes) to 64MB (67108864 bytes)

# Cache Management



Device	Managed by:
Registers (cache of L1/L2/L3 cache and main memory)	Compiler, using complex code-analysis techniques Assembly lang programmer
L1/L2/L3 cache (cache of main memory)	Hardware, using simple algorithms
Main memory (cache of local sec storage)	Hardware and OS, using virtual memory with complex algorithms (since accessing disk is expensive)
Local secondary storage (cache of remote sec storage)	End user, by deciding which files to download



# Cache Eviction Policies

## Best eviction policy: “oracle”

- Always evict a block that is *never* accessed again, or...
- Always evict the block accessed the *furthest in the future*
- Impossible in the general case

## Worst eviction policy

- Always evict the block that will be accessed next!
- Causes **thrashing**
- Impossible in the general case!



# Cache Eviction Policies

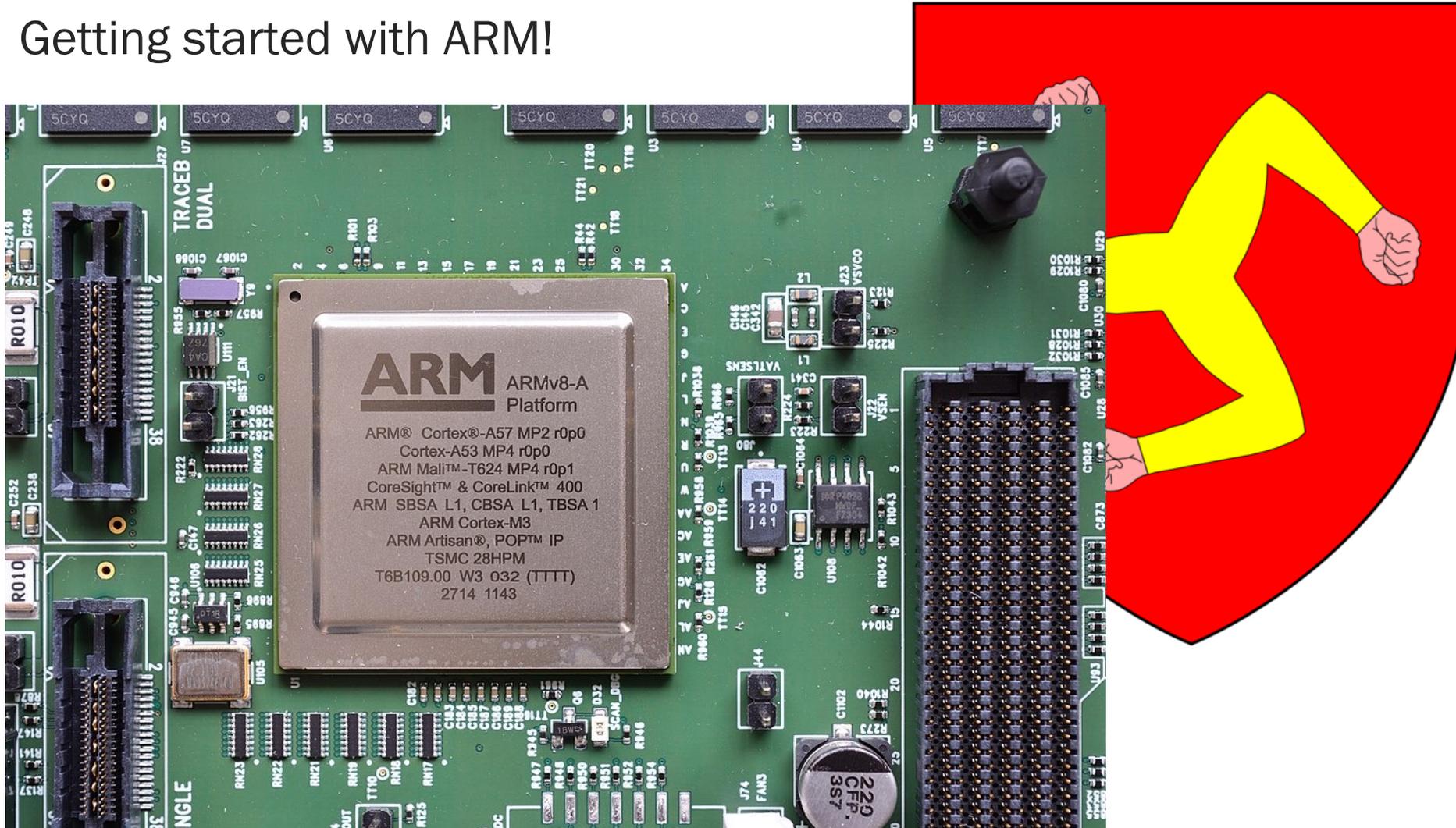
## Reasonable eviction policy: **LRU policy**

- Evict the “Least Recently Used” (LRU) block
  - With the assumption that it will not be used again (soon)
- Good for straight-line code
- (can be) bad for (large) loops
- Expensive to implement
  - Often simpler approximations are used
  - See Wikipedia “Page replacement algorithm” topic



# Next time ...

Getting started with ARM!



# Appendix: Locality/Caching Example – Matrix Multiplication



## Matrix multiplication

- Matrix = two-dimensional array
- Multiply n-by-n matrices A and B
- Store product in matrix C

## Performance depends upon

- Effective use of caching (as implemented by **system**)
- Good locality (as implemented by **you**)



# Appendix: Locality/Caching Example – Matrix Multiplication

Two-dimensional arrays are stored in either **row-major** or **column-major** order

a	0	1	2
0	18	19	20
1	21	22	23
2	24	25	26

row-major	col-major
a[0][0] 18	a[0][0] 18
a[0][1] 19	a[1][0] 21
a[0][2] 20	a[2][0] 24
a[1][0] 21	a[0][1] 19
a[1][1] 22	a[1][1] 22
a[1][2] 23	a[2][1] 25
a[2][0] 24	a[0][2] 20
a[2][1] 25	a[1][2] 23
a[2][2] 26	a[2][2] 26

C uses **row-major** order

- Access in row order  $\Rightarrow$  good spatial locality
- Access in column order  $\Rightarrow$  poor spatial locality

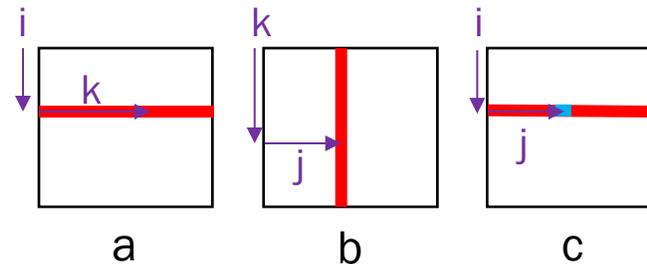


# Appendix: Locality/Caching Example – Matrix Multiplication

```
for (i=0; i<n; i++)  
  for (j=0; j<n; j++)  
    for (k=0; k<n; k++)  
      c[i][j] += a[i][k] * b[k][j];
```

## Reasonable cache effects

- Good locality for A
- Bad locality for B
- Good locality for C



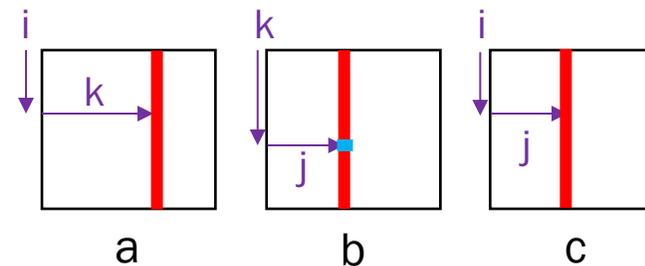


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  for (k=0; k<n; k++)  
    for (i=0; i<n; i++)  
      c[i][j] += a[i][k] * b[k][j];
```

## Poor cache effects

- Bad locality for A
- Bad locality for B
- Bad locality for C



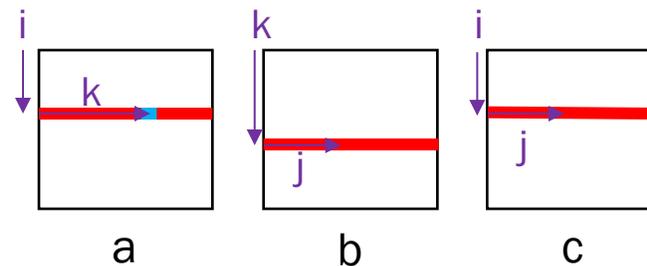


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    for (j=0; j<n; j++)  
      c[i][j] += a[i][k] * b[k][j];
```

## Good cache effects

- Good locality for A
- Good locality for B
- Good locality for C





# Another ghost of exams past ...



Suppose that C laid out arrays in column-major order instead of row-major order. What would be the *most efficient* loop ordering for matrix multiplication to maximize performance through good locality?

- A. i k j (Same as row-major)
- B. i j k
- C. j k i
- D. j i k
- E. k i j
- F. k j i

```
for (i=0; i<n; i++)  
  for (k=0; k<n; k++)  
    for (j=0; j<n; j++)  
      c[i][j] += a[i][k] * b[k][j];
```

C: j k i

Exactly what makes this bad for all three in row-major makes it ideal for column-major: a and c have good spatial b has good temporal, spatial