Precept Outline

Relevant Book Sections

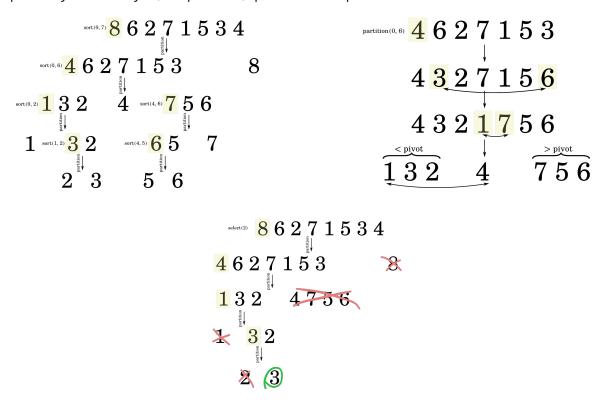
• Review of Lectures 7 and 8:

• Book chapters: 2.3, 2.4 and 2.5

- Quicksort
- Heaps and Priority Queues

A. Review: Quicksort + Heaps

Your preceptor will briefly review key points of this week's lectures. Here are some images representing examples they will show you, for partition, quicksort and quickselect.



B. Priority Queues

Part 1: Runtime

Consider the following code which uses a binary-heap based *minimum priority queue* (MinPQ). Assume that $n \ge k$, and that a[] is an **immutable** array containing arbitrary integers.

```
void foo(int k, int[] a) {
   MinPQ<Integer> pq = new MinPQ<Integer>();
   for (int i = 0; i < a.length; i++) {
      pq.insert(a[i]);
      if (pq.size() > k) pq.delMin();
   }
   for (int i = 0; i < k; i++)
      StdOut.println(pq.delMin());
}</pre>
```

Give a succinct description (that could, e.g., be a commercints in terms of the array a[] and the parameter k .	ent before the first line) of what the method foo
What is the order of growth of the running time of the co	ode as a function of both n and k ?
Suppose we were to remove line 5. What is the code's ou	utput? And what is the order of growth?
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Part 2: Data Structure Design (Fall'19 Midterm)	
Ture 2. Duta Structure Design (run 15 Materin)	
Design a data type to implement a <i>double-ended priority</i> key, deleting a smallest key, and deleting a largest key. you may choose among them arbitrarily.)	
To do so, create a MinMaxPQ data type that implements t	he following API:
nublic class MinMayDOckey sytands Commanable Kersy	\ (
<pre>public class MinMaxPQ<key comparable<key="" extends=""> MinMaxPQ()</key></pre>	<pre>/ { // create an empty priority queue</pre>
<pre>void insert(Key x)</pre>	<pre>// add x to the priority queue</pre>

// return a smallest key

Key min()

```
Key max()
Key delMin()
Key delMax()
// return a largest key
// return and remove a smallest key
// return and remove a largest key
```

Here are the performance requirements:

- The insert(), delMin(), and delMax() must take time proportional to $\log n$ or better in the worst case, where n is the number of keys in the priority queue.
- The min() and max() methods must take constant time in the worst case.

In your answer mention: the instance variables you'll use, your implementation of $\min()/\max()$, your implementation of $\operatorname{insert}(x)$ and your implementation of $\operatorname{delMin}()/\operatorname{delMax}()$.

Notes: To describe your solution, use either English prose or Java code (or a combination of the two). If your solution uses an algorithm or data structure from the course, do not reinvent it; simply describe how you are applying it.

C. Algorithm Design: The Hotel Problem

You are the manager of a (tall and narrow) hotel with one room in each of n floors. Early in the morning (before you arrived), n guests showed up at the same time, told the front desk their preference – a floor that is either "high" or "low" – and were assigned rooms arbitrarily (without consideration for their preferences).

preferences).			
By the end of the process, high floors. Moreover, no	assignment by swapping parall guests who prefer low find guest may end up in a roomay only be moved up, and $O(n)$.	loors should be on floor m they prefer less than	s below those who prefer their original assignmen