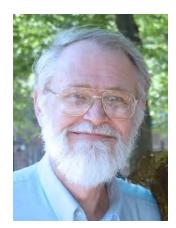
# COS 217: Introduction to Programming Systems

### **Data Structures**

"Every program depends on algorithms and data structures, but few programs depend on the invention of brand new ones."

-- Kernighan & Pike







### Goals of this Lecture



#### Help you learn (or refresh your memory) about:

Common data structures: linked lists and hash tables

#### Why? Deep motivation:

- Common data structures serve as "high level building blocks"
- A mature programmer:
  - Rarely creates programs from scratch
  - Often creates programs using high level building blocks

#### Why? Shallow motivation:

- Provide background pertinent to Assignment 3
- ... especially for those who haven't taken COS 226
- ... especially<sup>2</sup> for those who skipped COS 126

### Symbol Table Data Structure



#### Goal: maintain a collection of key/value pairs

- For these slides, each key is a **string**; each value is an **int**
- Lookup binding by key, get value back
- Unknown number of key-value pairs

#### Examples

- (student name, class year)
  - ("Andrew Appel", 81), ("Jen Rexford", 91), ("JP Singh", 87)
- (baseball player, number)
  - ("Ruth", 3), ("Gehrig", 4), ("Mantle", 7)
- (variable name, value)
  - ("maxLength", 2000), ("i", 7), ("j", -10)

# Agenda



#### **Linked lists**

Hash tables

Hash table issues

Symbol table key ownership

### Linked List Data Structure (for a Symbol Table)



```
struct Node {
                                               Your Assignment 3
   const char *key;
                                               data structures will
   int value;
   struct Node *next;
};
struct List {
   struct Node *first;
};
                              | ?| G| e | h | r | i | g | vo| ? |
                                                   ?|R|u|t|h|\@?|?
                struct
                           struct
 struct
                Node
                           Node
  List
```

NULL

be more general and perhaps more elaborate

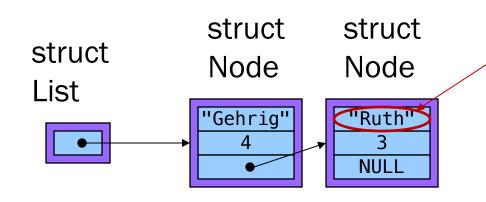
### Linked List Data Structure



```
struct Node {
   const char *key;
   int value;
   struct Node *next;
};

struct List {
   struct Node *first;
};
```

Your Assignment 3 data structures will be more general and perhaps more elaborate



Really this is the address at which a string with contents "Ruth" resides

## Preview of A3/Lecture+2: Encapsulation (wrong!)



#### list.h

Nothing stops a client from doing this!

```
p->first = NULL;
```

If you put the representation here, then it's not an abstract data type, it's just a data type.

#### client.c

```
#include "list.h"
int f(void) {
    struct List *p, *q;
    p = new();
    q = new();
    insert(p,"six",6);
    insert(p,"sept",7);
    insert(q,"cinq",5);
    concat(p,q);
    concat(q,p);
    return nth_value(q,1);
}
```

### list\_linked.c

```
#include "list.h"

struct List *new()
{
    struct List *p;
    p = calloc(1, sizeof(*p));
    if(p == NULL) { cry(); return NULL; }
    return p;
}

void insert(struct List *p, const char* key, int value) {...}

void concat(struct List *p, struct List *q) { ... }

int nth_value(struct List *p, int n) { ... }
```

## Preview of A3/Lecture+2: Encapsulation (right!)



```
Now this code won't compile!
```

```
p->first = NULL;
```

#### client.c

```
#include "list.h"
int f(void) {
   List_T p, q;
   p = new();
   q = new();
   insert(p,"six",6);
   insert(p,"sept",7);
   insert(q,"cinq",5);
   concat(p,q);
   concat(q,p);
   return nth_value(q,1);
}
```

#### list.h

Including only the declaration in header file enforces the abstraction: it keeps clients from accessing fields of the struct, allowing implementation to change

#### list\_linked.c

```
#include "list.h"

struct Node {const char *key; int value; struct Node *next;};

struct List {struct Node *first;};

struct List *new()
{
    struct List *p;
    p = calloc(1, sizeof(*p));
    if(p == NULL) {cry(); return NULL;}
    return p;
}

void insert(struct List *p, const char* key, int value) {...}

void concat(struct List *p, struct List *q) { ... }

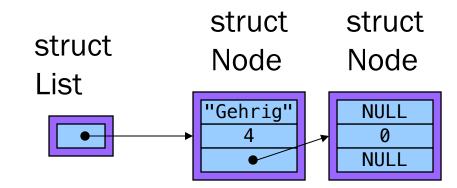
int nth_value(struct List *p, int n) { ... }
```

### Accessing a Linked List



```
struct Node {
   const char *key;
   int value;
   struct Node *next;
};

struct List {
   struct Node *first;
};
```



```
struct List lineup;
struct Node g;
struct Node* r =
    calloc(1,sizeof(struct Node));
g.key = "Gehrig";
lineup.first = &g;
(*lineup.first).value = 4;
lineup.first->value = 4;
(*lineup.first).next = r;
lineup.first->next = r;
```

### Linked List Algorithms



#### Create

- Allocate List structure; set first to NULL
- Performance:  $O(1) \Rightarrow$  fast

#### Add (no check for duplicate key required)

- Insert new node containing key/value pair at front of list
- Performance:  $O(1) \Rightarrow fast$

#### Add (check for duplicate key required)

- Traverse list to check for node with duplicate key
- Insert new node containing key/value pair into list
- Performance:  $O(n) \Rightarrow slow$

## Linked List Algorithms



#### Search

- Traverse the list, looking for given key
- Stop when key found, or reach end
- Performance: ???



# iClicker Question



Q: How fast is searching for a key in a linked list?

A. Always fast - O(1)

B. Always slow - O(n)

C. On average, fast

D. On average, slow

Not well specified:

Depends on order of inserts, queries, etc.

Best answer is D.

### Linked List Algorithms



#### Search

- Traverse the list, looking for given key
- Stop when key found, or reach end
- Performance:  $O(n) \Rightarrow slow$

#### Free

- Free Node structures while traversing
- Free List structure
- Performance:  $O(n) \Rightarrow slow$

# Agenda



Linked lists

#### Hash tables

Hash table issues

Symbol table key ownership

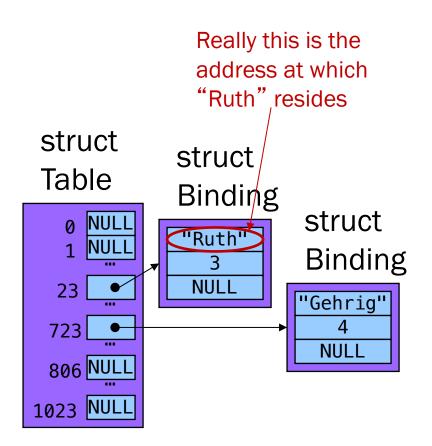
### Hash Table Data Structure (For COS 226 nerds - hashing with separate chaining)





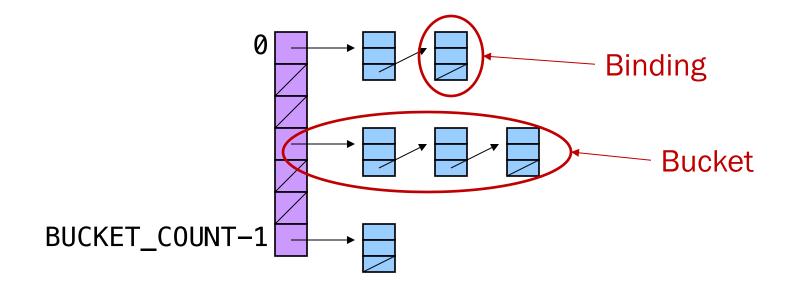
#### Array of linked lists

```
enum { BUCKET_COUNT = 1024 };
struct Binding {
   const char *key;
   int value;
   struct Binding *next;
};
struct Table {
   struct Binding *buckets[BUCKET_COUNT];
};
```



### Hash Table Data Structure





Hash function maps given key to an integer

Mod integer by BUCKET\_COUNT to determine proper bucket

## Hash Table Example



Example: BUCKET\_COUNT = 7

Add (if not already present) bindings with these keys:

• the, cat, in, the, hat



```
First key: "the"
```

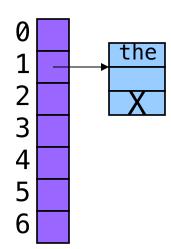
hash("the") = 965156977; 965156977 % 7 = 1

Search buckets [1] for binding with key "the"; not found





Add binding with key "the" and its value to buckets [1]

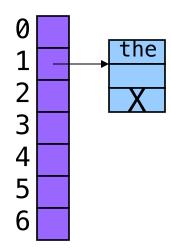




Second key: "cat"

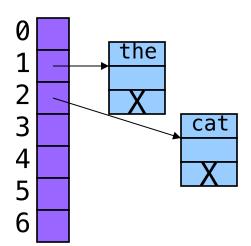
• hash("cat") = 3895848756; 3895848756 % 7 = 2

Search buckets [2] for binding with key "cat"; not found





Add binding with key "cat" and its value to buckets [2]

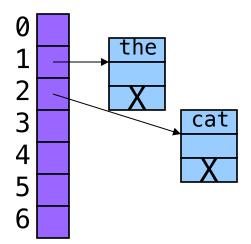




```
Third key: "in"
```

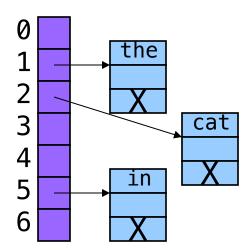
• hash("in") = 6888005; 6888005% 7 = 5

Search buckets [5] for binding with key "in"; not found





Add binding with key "in" and its value to buckets [5]



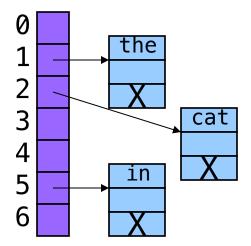


Fourth word: "the"

hash("the") = 965156977; 965156977 % 7 = 1

Search buckets [1] for binding with key "the"; found it!

• Don't change hash table

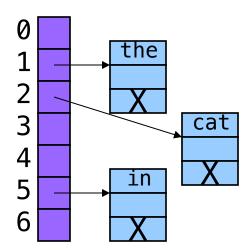




Fifth key: "hat"

hash("hat") = 865559739; 865559739 % 7 = 2

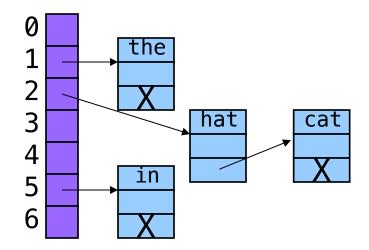
Search buckets [2] for binding with key "hat"; not found





Add binding with key "hat" and its value to buckets [2]

• At front or back?



### Hash Table Algorithms



#### Create

- Allocate Table structure; set each bucket to NULL
- Performance:  $O(1) \Rightarrow$  fast

#### Add

- Hash the given key
- Mod by BUCKET\_COUNT to determine proper bucket
- Traverse proper bucket to make sure no duplicate key
- Insert new binding containing key/value pair into proper bucket
- Performance: ???



## iClicker Question



Q: How fast is adding a key to a hash table?

- A. Always fast
- B. Usually fast, but depends on how many keys are in the table
- C. Usually fast, but depends on how many keys hash to the same bucket
- D. Usually slow
- E. Always slow

C

If bindings are spread across buckets, this is fast (though B is a concern).

Worst case: everything hashes to the same bucket – O(n)

## Hash Table Algorithms



#### Search

- Hash the given key
- Mod by BUCKET\_COUNT to determine proper bucket
- Traverse proper bucket, looking for binding with given key
- Stop when key found, or reach end
- Performance: Usually  $O(1) \Rightarrow$  fast

#### Free

- Traverse each bucket, freeing bindings
- Free Table structure
- Performance:  $O(n) \Rightarrow slow$

# Agenda



Linked lists

Hash tables

#### Hash table issues

Symbol table key ownership

### How Many Buckets?



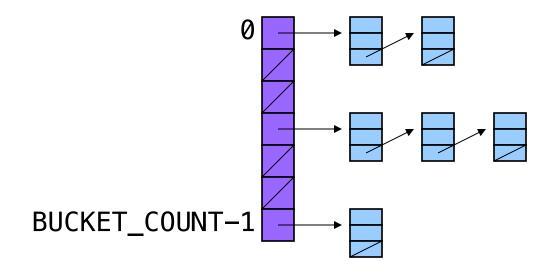
### Many!

• Too few ⇒ large buckets ⇒ slow add, slow search

#### But not too many!

Too many ⇒ memory is wasted

#### This is OK:



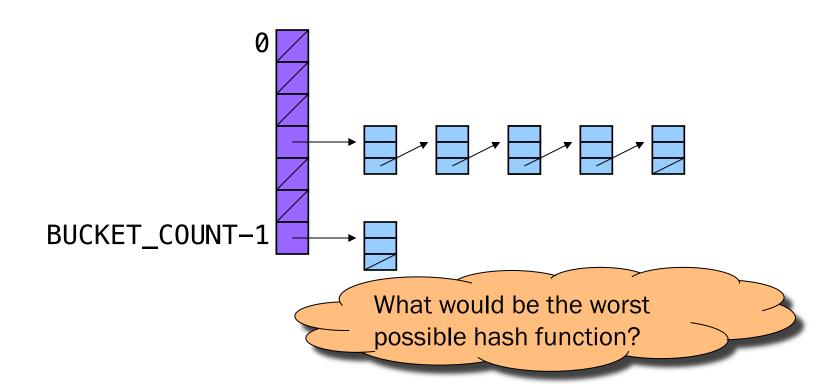
### What Hash Function?



### Should distribute bindings across the buckets well

- Distribute bindings over the range 0, 1, ..., BUCKET\_COUNT-1
- Distribute bindings evenly to avoid very long buckets

#### This is not so good:



## How to Hash Strings?



#### Simple hash schemes don't distribute the keys evenly

- Number of characters, mod BUCKET\_COUNT
- Sum the numeric codes of all characters, mod BUCKET\_COUNT
- ...

#### A reasonably good hash function:

- Weighted sum of characters s<sub>i</sub> in the string s
  - (Σ a<sup>i</sup>s<sub>i</sub>) mod BUCKET\_COUNT
- Best if a and BUCKET\_COUNT are relatively prime (i.e., their GCD is 1)
  - e.g., a = 65599, BUCKET\_COUNT = 1024

## How to Hash Strings?



A bit of math, and translation to code, yields:

```
size_t hash(const char *s, size_t bucketCount)
{
    enum { HASH_MULT = 65599 };
    size_t i;
    size_t h = 0;
    for (i = 0; s[i] != '\0'; i++)
        h = h * HASH_MULT + (size_t)s[i];
    return h % bucketCount;
}
```

# Agenda



Linked lists

Hash tables

Hash table issues

Symbol table key ownership



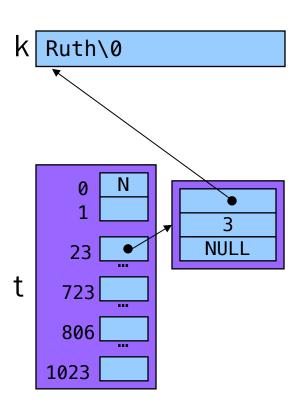
Suppose a hash table function Table\_add() contains this code:





Problem: Consider this calling code:

```
struct Table *t;
char k[100] = "Ruth";
...
Table_add(t, k, 3);
```



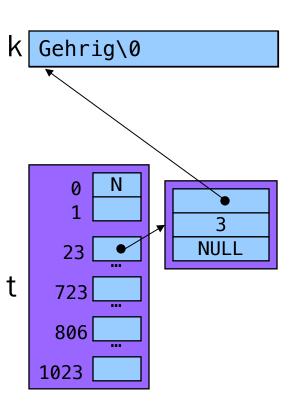


Problem: Consider this calling code:

```
struct Table *t;
char k[100] = "Ruth";
...
Table_add(t, k, 3);
strcpy(k, "Gehrig");
```

k is REALLY &k[0]!

What happens if the client searches t for "Ruth"? For "Gehrig"?





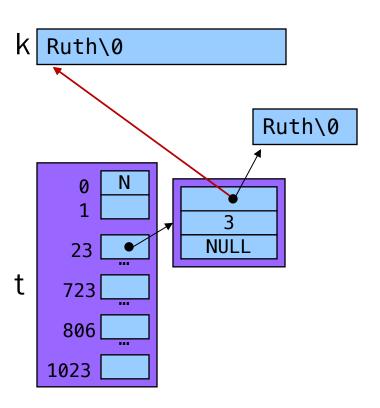
Solution: Table\_add() saves a defensive copy of the given key

What is missing from this code that you should have in yours?



Now consider same calling code:

```
struct Table *t;
char k[100] = "Ruth";
...
Table_add(t, k, 3);
```

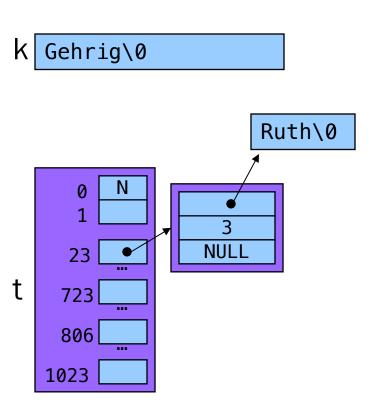




Now consider same calling code:

```
struct Table *t;
char k[100] = "Ruth";
...
Table_add(t, k, 3);
strcpy(k, "Gehrig");
```

Hash table is not corrupted!



### Who Owns the Keys?



#### Then the hash table **owns** its keys

- That is, the hash table allocated the memory in which its keys reside
- Table\_remove() function must also free the memory in which the key resides, not just the binding containing the key

## Summary



### Common data structures and associated algorithms

- Linked list
  - (Maybe) fast add
  - Slow search
- Hash table
  - (Potentially) fast add
  - (Potentially) fast search
  - Very common

#### Hash table issues

- (Initial) Bucket array size
- Hashing algorithms

### Symbol table concerns

Key ownership