# Introducing Assignment 2: Mesh Processing & Half Edges

COS 426: Computer Graphics (Spring 2022)

# Agenda

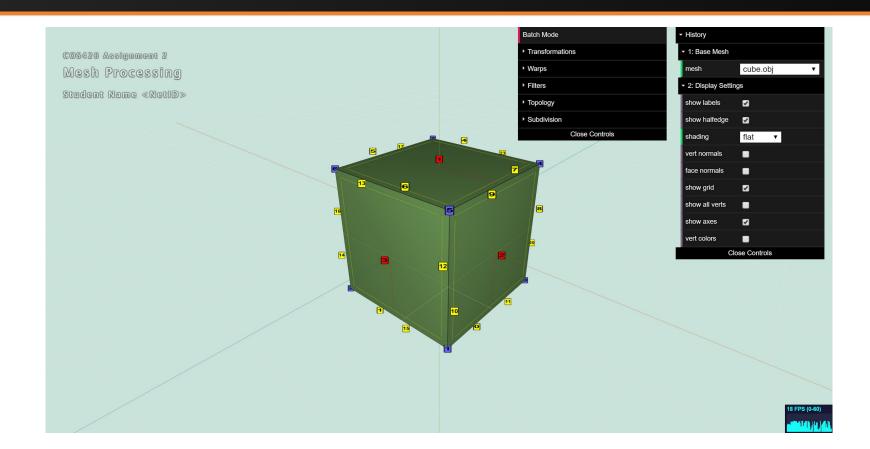
- Brief overview of A2
- Half-edge data structure
  - Definition
  - Traversal
  - Modification

### Setup

### Same as in A0 and A1:

- Run "python3 -m http.server" (or similar) inside the assignment directory
- Open "http://localhost:8000" in web browser

### GUI



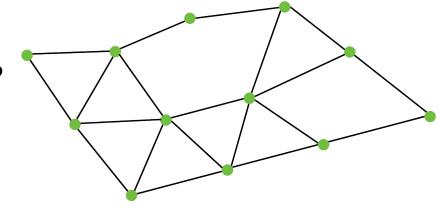
## Tips for Three.js and A2

- For A2 you will be using the Three.js library
  - Simple and efficient primitives for working in 3D
- You should read the docs!
  - Vector3
  - <u>Euler</u> (for rotations)
- Modularity is your friend!
  - You will be writing helper functions. Use them!

### Meshes vs. Images

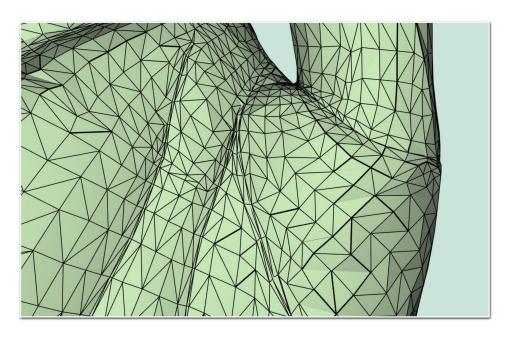
- Images have implicit adjacency information
  - Window around a pixel
  - Easy to express local operations
    - (e.g. convolution)

- What about meshes?
  - How to apply smoothing?



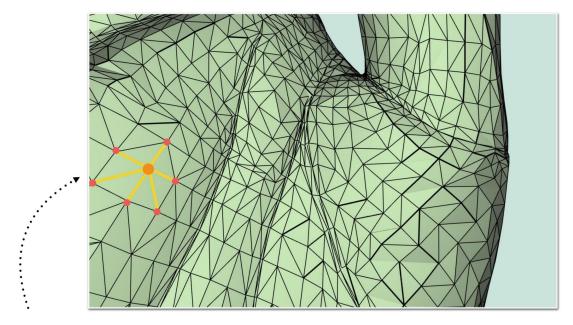
### Meshes

Meshes can be quite dense



### Meshes

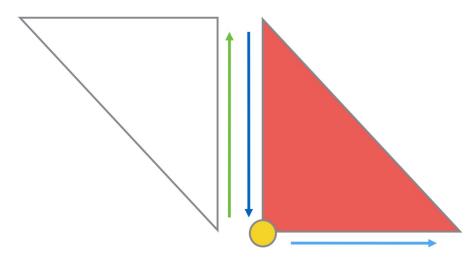
How can we efficiently access adjacency information?



One - Ring Neighborhood

### What is a Half-Edge?

- Imagine splitting each edge in two
  - Each half gets one of the edge's faces
  - Each face, vertex, and half-edge stores some state
  - Conceptually very similar to doubly linked list



# Half-Edge: What State is Stored?

Half Edge	Vertex	Face
Vertex	Position	Half-Edge
Opposite Half-Edge	Outgoing Half-Edge	
Face		
Next Half-Edge		

### Half-Edge Data Structure

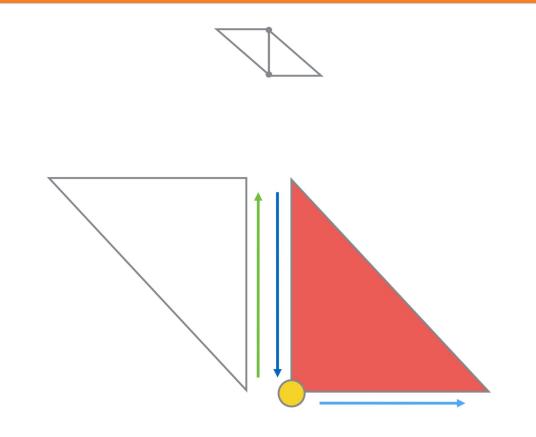
Half Edge

Vertex

Opposite Half-Edge

Face

Next Half-Edge

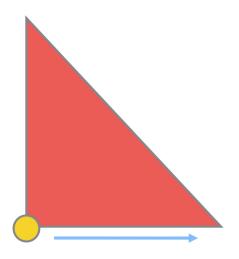


# Half-Edge Data Structure

Vertex

Location

Outgoing Half-Edge



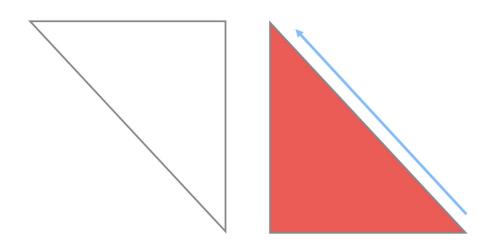
Q: Which half-edge to choose?

A: Pick one arbitrarily

# Half-Edge Data Structure

Face

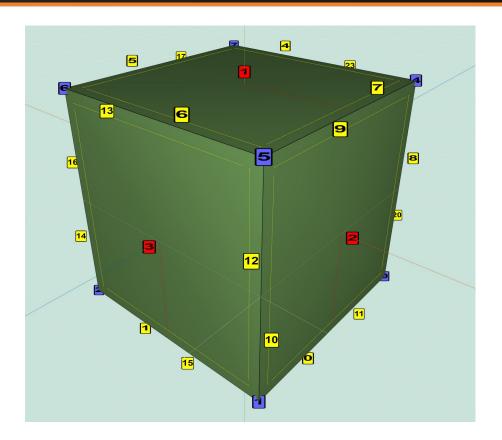
Half-Edge



Q: Which half-edge to choose?

A: Pick one arbitrarily

# Half-Edge Visualization



• Faces:

id

Half-edges:

id

Vertices:

id

### Features

#### **Transformations**

- Translation
- Rotation
- Scale

#### **Traversal**

Various edge/vertex/face helpers

#### **Analysis**

- Face Area
- Per-vertex Normals
- Average Edge Lengths

#### Warps

- Twist
- Inflate
- Wacky

#### **Filters**

- Noise
- Smoothing
- Sharpening
- Curvature

#### Topology

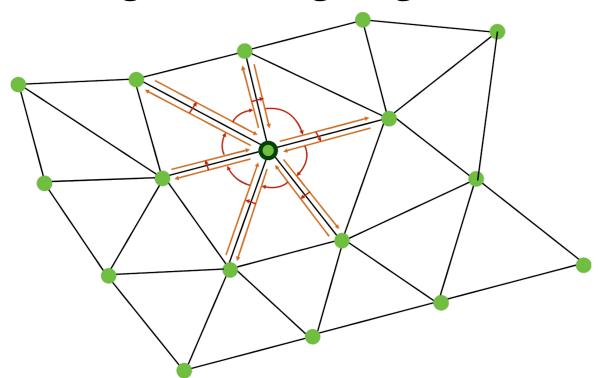
- Triangulate
- Truncate
- Extrude
- Split Long Edges

#### Subdivision

- Triangle Topology
- Loop
- Quad Topology
- Catmull-Clark

### Traversal (Vertices on vertex)

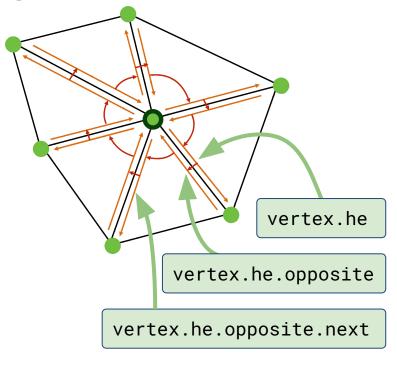
How do we get one-ring neighbors of a vertex?



### Traversal (Vertices on vertex)

How do we get one-ring neighbors of a vertex?

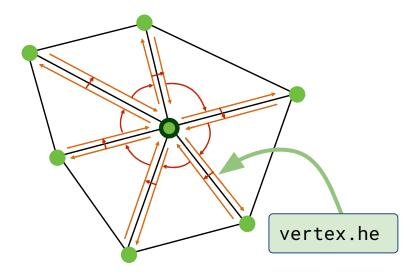
```
original_he = vertex.he;
he = original_he;
do {
    // some calculations
    he = he.opposite.next
} while (he != original_he)
```



### Traversal (Vertex Normals)

- Vertex Normals are defined as a weighted average of the normals of adjacent faces (weighted by face area)
- How would you compute vertex normals given face normals and areas?

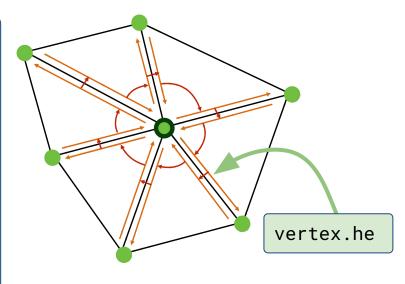
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### Traversal (Vertex Normals)

- Vertex Normals are defined as a weighted average of the normals of adjacent faces (weighted by face area)
- How would you compute vertex normals given face normals and areas?

```
original_he = vertex.he;
he = original_he;
v_normal.set(0,0,0);
do {
   f_normal = he.face.normal;
   area = he.face.area;
   v_normal.add(f_normal*area);
   he = he.opposite.next
} while (he != original_he)
v_normal.normalize()
```

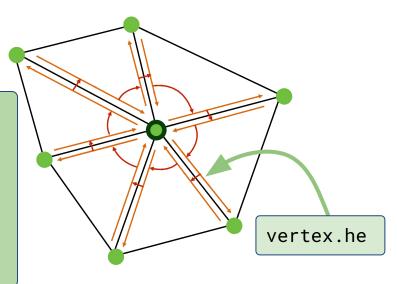


### Traversal (Vertex Normals)

- Vertex Normals are defined as a weighted average of the normals of adjacent faces (weighted by face area)
- How would you compute vertex normals given face normals and areas?

Easier way: use facesOnVertex()!

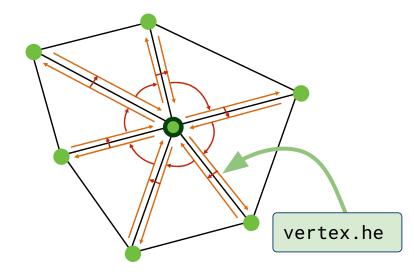
```
fs = mesh.facesOnVertex(v);
v_normal.set(0,0,0);
for (let f of fs) {
    v_normal.add(f.normal * f.area);
}
v_normal.normalize()
```



### Traversal (Laplacian Smoothing)

 Similarly, in uniform Laplacian smoothing, each vertex moves towards the average of it and its neighbors.

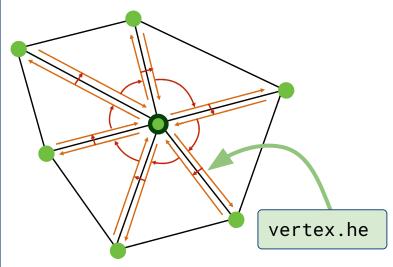
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    // some calculations
    he = he.opposite.next
} while (he != original_he)
```



### Traversal (Laplacian Smoothing)

 Similarly, in uniform Laplacian smoothing, each vertex moves towards the average of it and its neighbors.

```
original_he = vertex.he;
he = original_he;
avg_pos.set(0,0,0);
do {
   avg_pos.add(he.vertex.pos);
   he = he.opposite.next
} while (he != original_he)
avg_pos.add(-vertex*num_neigh);
new_pos = vertex + avg_pos * delta;
```



### Traversal (Laplacian Smoothing)

- Some tips for uniform Laplacian smoothing:
  - You can use verticesOnVertex() to simplify your code!
  - Be careful not to modify your mesh before you've computed offsets for all vertices!
    - (Similar to filters in A1 that modified the image)

### Traversal (Cotan Laplacian Smoothing)

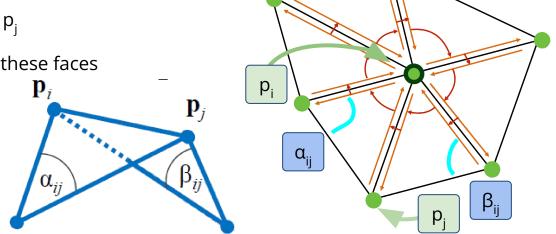
Cotangent Laplacian smoothing

```
avg_pos.add(he.vertex.pos);
                            ⇒ avg_pos.add(w*he.vertex.pos);
                            ⇒ total w
num_neigh
```

- Notes:
  - p<sub>i</sub> = center vert

  - İterate over all neighboring p<sub>j</sub>
     p<sub>i</sub>, p<sub>j</sub> will share two faces
     α<sub>ij</sub>, β<sub>ij</sub> are the far angles on these faces

$$w = \frac{\cot(\alpha_{ij}) + \cot(\beta_{ij})}{2}$$

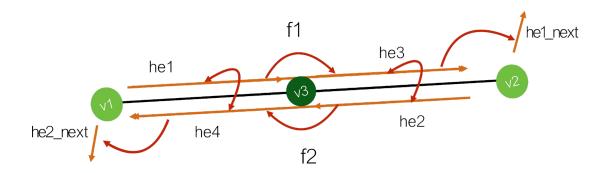


### Data Structure Modification

- Take a look meshUtils.js for the all the primitives
  - splitEdgeMakeVert()
  - joinEdgeKillVert()
  - splitFaceMakeEdge()
  - joinFaceKillEdge()

### Data Structure Modification (splitEdge)

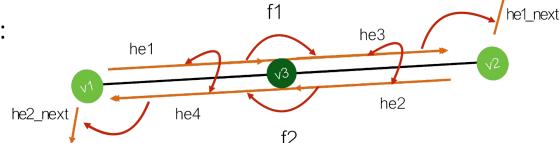
How to add new vertices to an existing half-edge data structure? splitEdgeMakeVert(v1,v2,factor):



### Data Structure Modification (splitEdge)

### splitEdgeMakeVert(v1,v2,factor):

- addVertex
- addHalfEdge
- he.vertex, he.opposite



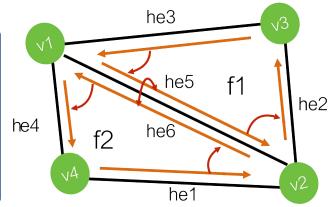
### Data Structure Modification (splitFace)

How to add new edges to an existing half-edge data structure?

splitFaceMakeEdge(f, v1, v2, vertOnF, switchFaces)

```
f2 = addFace();
he5.next = he2;
he5 = addHalfEdge(v1,v2,f1);
he6 = addHalfEdge(v2,v1,f2);
he5.next = he5;
he1.next = he6;
he6.next = he4;

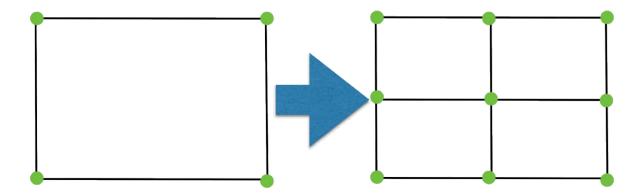
f1.halfedge = he5;
he6.opposite = he5;
f2.halfedge = he6;
```



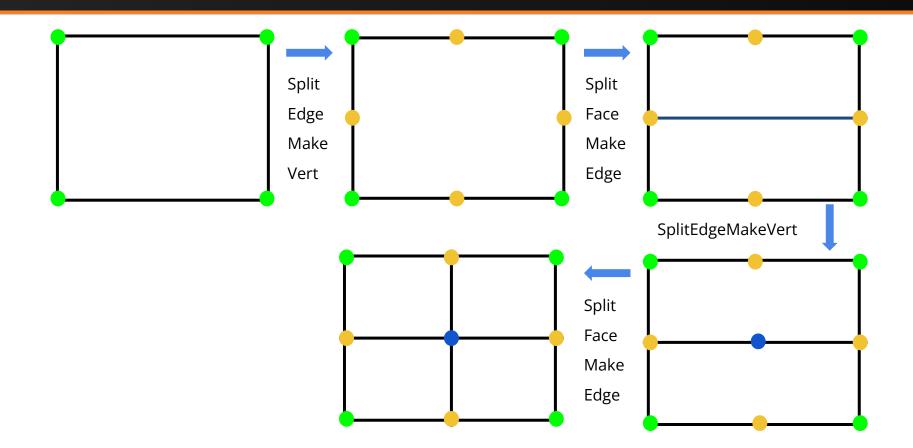
- Optional args: (for advanced filters, like Extrude)
  - vertOnF: if provided, this vert will still be on the original face.
  - switchFaces: if true, vertOnF is placed on the new face instead

### Data Structure Modification (subdividing)

- How would you go about subdividing a quad face?
  - You're given split edge and split face
  - Just use those guaranteed validity of mesh after use!



### Data Structure Modification(subdividing)



Q&A