

Introducing Assignment 1: Image Processing

COS 426: Computer Graphics (Spring 2022)

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Setup

Same layout as A0:

- Run `python3 -m http.server` (or similar) inside the assignment directory
- Open `http://localhost:8000` in web browser

GUI

COS426 Assignment 1

Image Processing — Interactive Mode

Switch to: [Writeup](#)

Student Name <NetID>



- Push Image
- Batch Mode
- Animation
- MorphLines
- SetPixels
- ▾ Luminance
 - Brightness
 - Contrast
 - Gamma
 - Vignette
 - Histogram
- Color
- Filters
- Dithering
- Resampling
- Composite
- Misc
- Close Controls

- ▾ History
 - ▾ 1: Push Image
 - image name
 - Delete Below
 - ▾ 2: Brightness
 - brightness
 - Delete
- Close Controls

GUI

- Useful functions
 - Push Image
 - Animation: generate gif animation using (min, step, max)
 - MorphLines: specify line correspondences for morphing
 - BatchMode: fix current parameter settings

GUI

- Features to implement
 - SetPixels: set pixels to certain colors (This was A0)
 - Luminance: change pixel luminance
 - Color: remap pixel colors
 - Filter: convolution/box filter
 - Dithering: reduce visual artifacts due to quantization \approx cheat our eyes
 - Resampling: interpolate pixel colors
 - Composite: blending two images
 - Misc

Features

Luminance

- Brightness
- Contrast
- Gamma
- Vignette
- Histogram equalization

Color

- Grayscale
- Saturation
- White balance
- Histogram matching

Filter

- Gaussian
- Sharpen
- Edge detect
- Median
- Bilateral filter

Dithering

- Quantization
- Random dithering
- Floyd-Steinberg error diffusion
- Ordered dithering

Resampling

- Bilinear sampling
- Gaussian sampling
- Translate
- Scale
- Rotate
- Swirl

Composite

- Composite
- Morph

Next week's precept
will focus specifically
on this topic

A few reminders...

- Don't try to exactly replicate example images.
- Choose parameters in your code which give you best looking results.
- Have fun!

Changing Contrast

- GIMP formula
 - $\text{value} = (\text{value} - 0.5) * (\tan ((\text{contrast} + 1) * \text{PI}/4)) + 0.5;$
 - "Difference above mid-value times contrast multiplier, plus mid-value"
 - When contrast=1, $\tan(\text{PI}/2)$ is infinite, think about limit and what is reasonable
 - Clamp pixel to $[0, 1]$ after computing the value.
 - Apply to each channel separately.



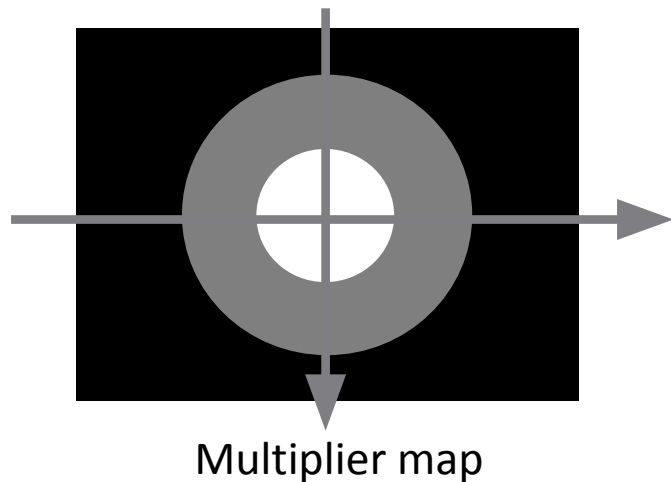
Gamma correction

- $R = R^{\text{gamma}}$, $G = G^{\text{gamma}}$, $B = B^{\text{gamma}}$
- R, G, B are typically in $[0, 1]$ (default in the code base)
- Second arg of `gammaFilter(image, logOfGamma)` is `log(gamma)`
 - So use `gamma = Math.exp(logOfGamma)`
- Exponentiation in JS is “`Math.pow(base, exponent)`” or (ES7 / ES2017+) “`base**pow`”
 - Your browser might not support ES7



Vignette

- Pixels within inner radius remain unchanged
- Pixels outside outer radius are black
- Pixels between innerR and outerR should be multiplied with a value in $[0, 1]$:
 - Multiplier = $1 - (R - \text{innerR}) / (\text{outerR} - \text{innerR})$
 - $R = \sqrt{x^2 + y^2} / \text{halfdiag}$
- Similar to soft brush



Histogram Equalization

Transform an image so that it has flat histogram of luminance values.



Before



After

Histogram Matching

Transform an image so that it has same histogram of luminance values as reference image.

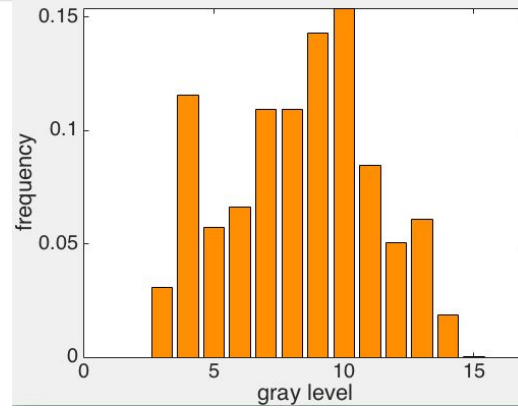


reference image: town

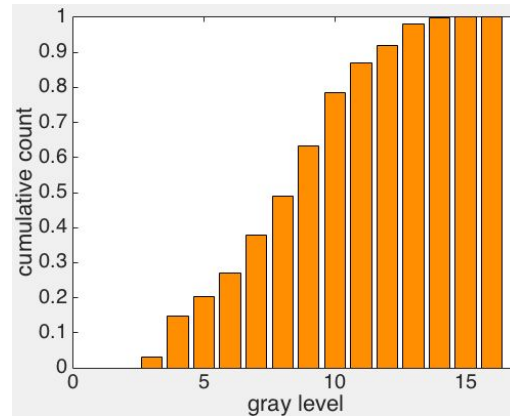


reference image: flower

Histogram Equalization/Matching



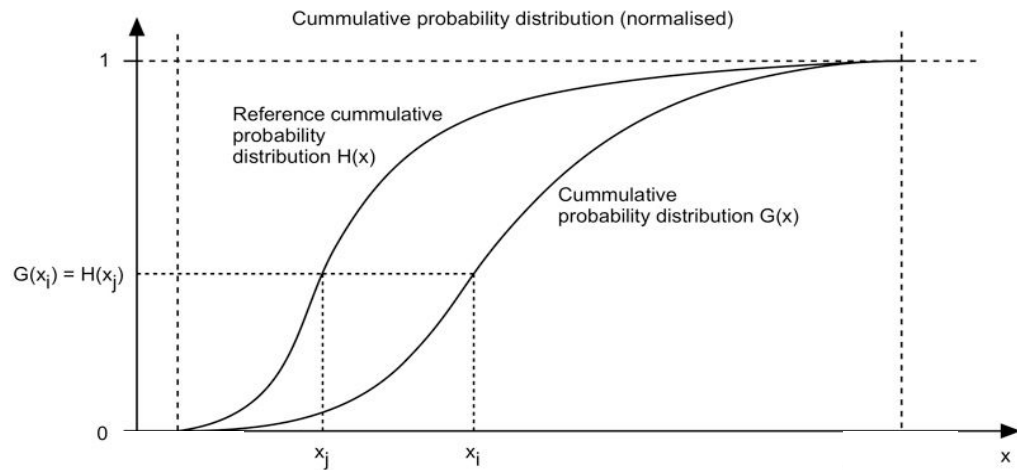
pdf



cdf

Histogram Equalization/Matching

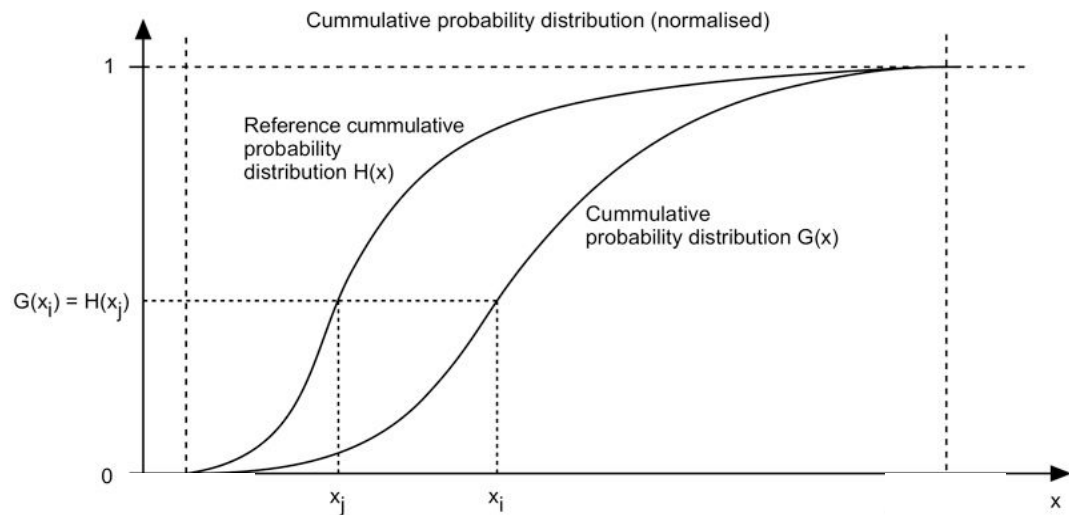
- Image: x
- Number of gray levels: L
- $pdf(i) = \frac{n_i}{n}$ n_i = number of pixels of the i -th gray level
- $cdf(j) = \sum_{i=0}^j pdf(i)$
- Target cdf:
 - Equalization:
 - $cdf_{ref}(i) = \frac{i}{L-1}$
 - Matching:
 - cdf of the reference image



(source:<http://paulbourke.net/miscellaneous/equalisation/>)

Histogram Equalization/Matching

- Target cdf:
 - Equalization:
 - $cdf_{ref}(i) = \frac{i}{L-1}$
 - Matching:
 - cdf of the reference image
- Implementation
 - Equalization
 - $x' = (cdf(x) * (L - 1)) / (L - 1)$
 - Matching
 - $x' = \underset{i}{\operatorname{argmin}} |cdf(x) - cdf_{ref}(i)|$
 - Convert back to gray level: $x' = \frac{x'}{L-1}$



Saturation

- $\text{pixel} = \text{pixel} + (\text{pixel} - \text{gray}(\text{pixel})) * \text{ratio}$
- Do clamp()



White balance

`whitebalance(image, rgb_w)`

$[L_w, M_w, S_w] = \text{rgb2lms}(rgb_w)$

for each pixel x in image

$[L, M, S] = \text{rgb2lms}(\text{image}(x))$

$L = L / L_w$

$M = M / M_w$

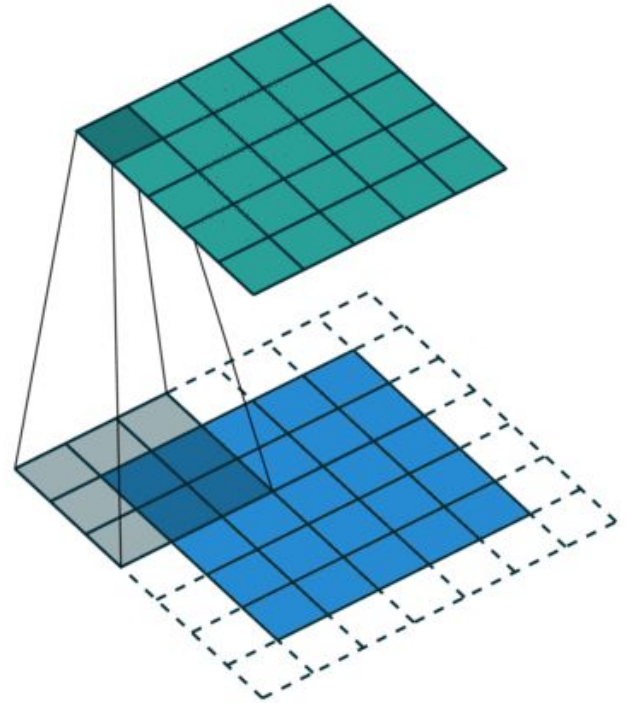
$S = S / S_w$

`image_out(x) = lms2rgb(L, M, S)`

- Hints:
 - Use `rgbToXyz()`, `xyzToLms()`, `lmsToXyz()`, `xyzToRgb()`
 - Do `clamp()`

Convolution (Gaussian/Sharpen/Edge)

w1 w2 w3
w4 w5 w6
w7 w8 w9



Convolution (Gaussian/Sharpen/Edge)

- Weights can be normalized depending on the application
- Variety of ways to handle edges
 - Mirror boundary
 - Zero padding
 - Use part of the kernel only

Gaussian filter

- Create a new image to work on
- Weights should be normalized to sum to 1, otherwise average color changes

$$G(x) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{x^2}{2\sigma^2}}$$

$$\frac{1}{16} \begin{bmatrix} 1 & 2 & 1 \\ 2 & 4 & 2 \\ 1 & 2 & 1 \end{bmatrix}$$

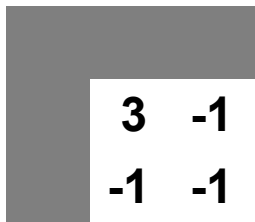
- x = distance to the center of the kernel
- Linear separation optimization:
 - First apply a 1D Gaussian kernel vertically and then a 1D Gaussian kernel horizontally

Edge

Kernel:

-1	-1	-1
-1	8	-1
-1	-1	-1

Inside boundary



At boundary

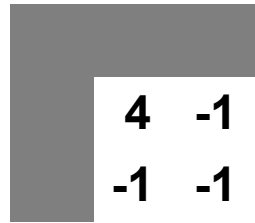
- Weights sum to 0
- Optional to invert the edge map for visualization:
- $\text{pixel} = 1 - \text{pixel}$

Sharpen

- Kernel:

-1	-1	-1
-1	9	-1
-1	-1	-1

Inside boundary



At boundary

- Weights sum to 1

Edge Filter vs Sharpen Filter

-1	-1	-1
-1	8	-1
-1	-1	-1

Edge Filter

-1	-1	-1
-1	9	-1
-1	-1	-1

Sharpen Filter

$\text{Convolution}(\text{Image}, \text{Sharpen Filter}) = \text{Convolution}(\text{Image}, \text{Edge Filter}) + \text{Image}$

Median

- Use a window (similar to convolution)
- Choose the median within the window
- Sorting: sort by RGB separately / sort by luminance
- Optimization: use quick-select to find median
 - Gives median in linear time



1



2



3



4



5

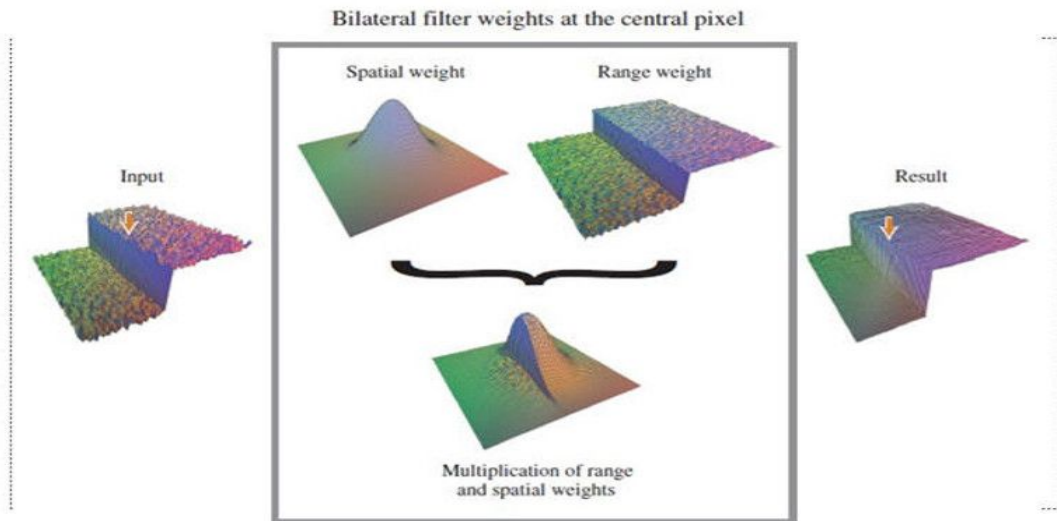
RGB Example

Bilateral

- Combine Gaussian filtering in both spatial domain and color domain
- Weight formula of filter for pixel (i, j): Spatial distance component Color distance component

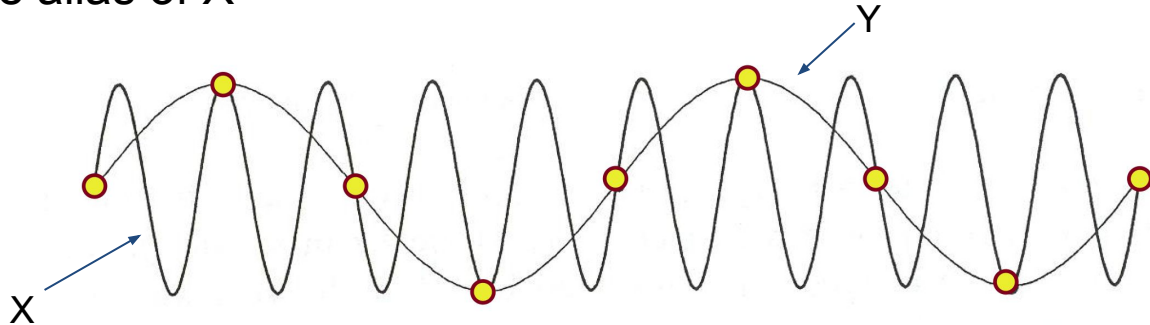
$$w(i, j, k, l) = e^{-\frac{(i-k)^2 + (j-l)^2}{2\sigma_d^2} - \frac{\|I(i, j) - I(k, l)\|^2}{2\sigma_r^2}}$$

- Similar color -> large weights, Different color -> smaller weights

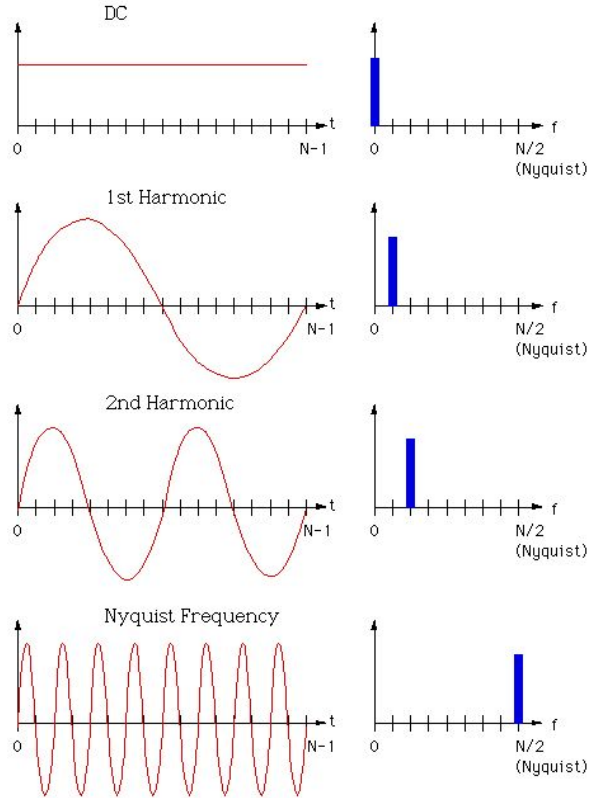


Sampling & Frequencies

- Real-world is continuous, Sensors are discrete
- How many samples do we need to measure real world?
 - Too few samples = aliasing
 - Nyquist rate says that we need to sample at $\geq 2\times$ the highest frequency for perfect reconstruction
- Aliasing is when signal X masquerades as signal Y
 - Y is the alias of X

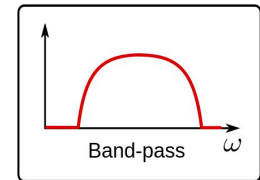
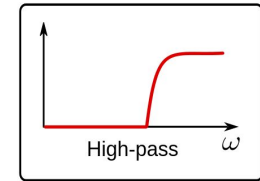
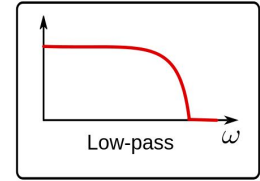
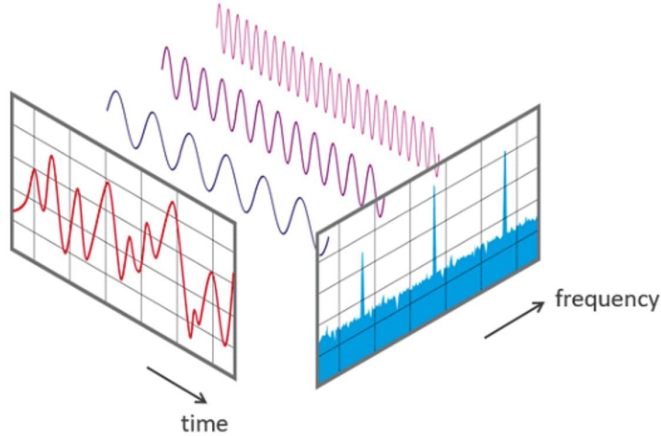


Fourier Transform

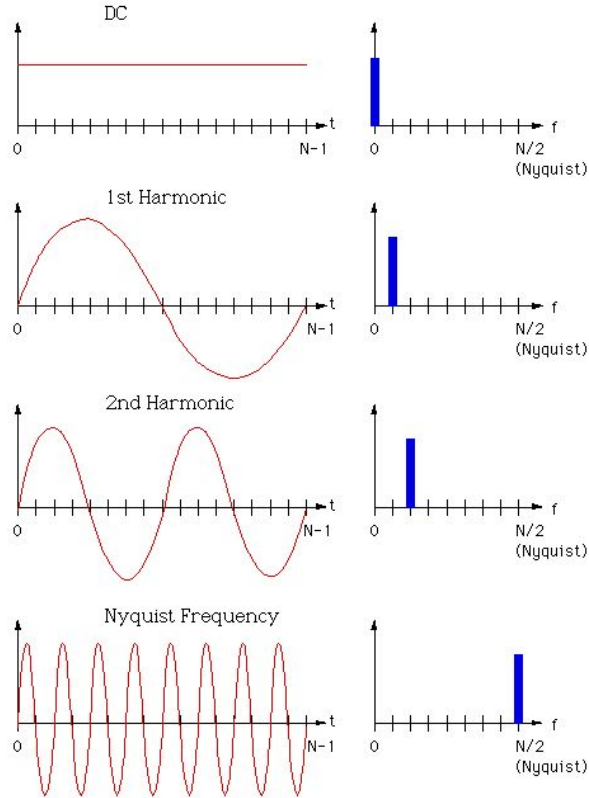


Maps signal from time domain to frequency domain

Use low-pass filter to remove high frequencies and prevent aliasing

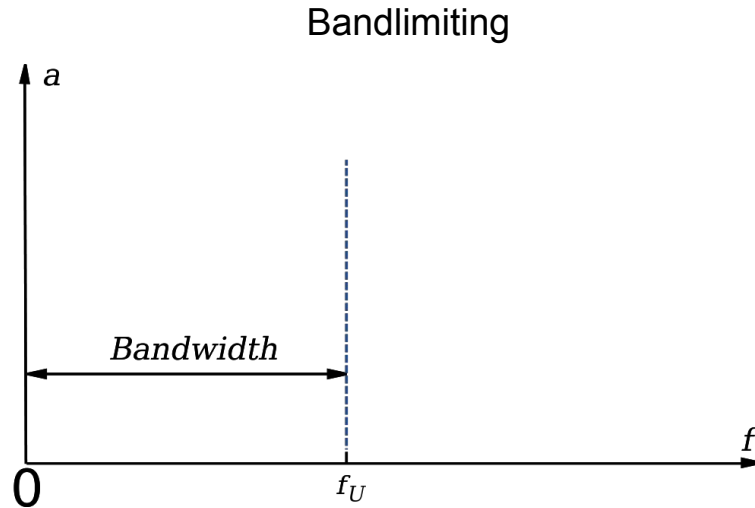


Fourier Transform



Maps signal from time domain to frequency domain

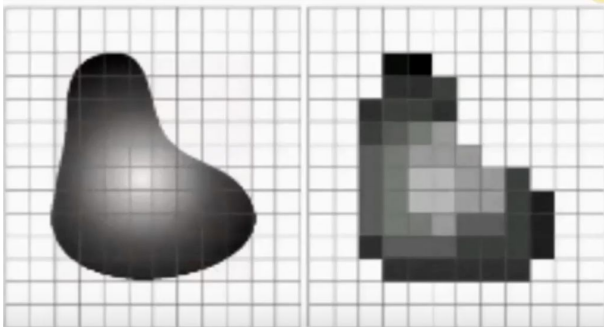
Use low-pass filter to remove high frequencies and prevent aliasing



1D to 2D

- 2D signals follow the same analysis as 1D signals

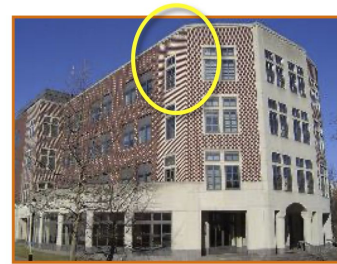
Real world 2D image is sampled by sensor



Aliasing for 2D signals



(Barely) adequate sampling

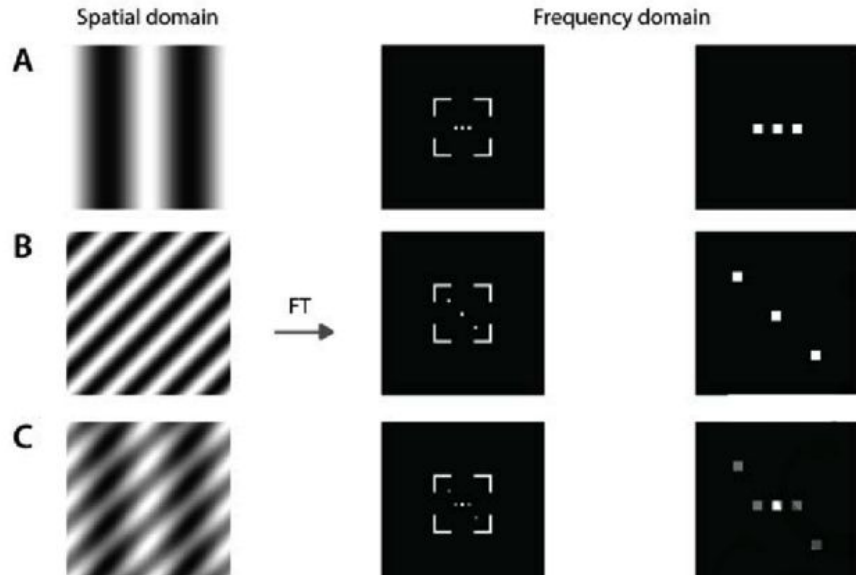


Inadequate sampling

1D to 2D

- 2D signals follow the same analysis as 1D signals

Fourier Analysis for 2D signals



If image resolution is low

- E.g. image compression

Then need to apply band-limiting filter to avoid aliasing

- E.g. Triangle, Gaussian

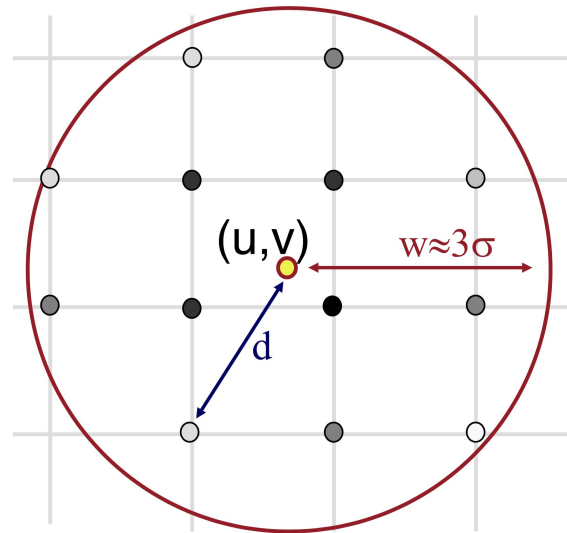
Note that these filters are “finite” filters, they act as approximations to a perfect low pass filter

Resampling

- Gaussian interpolation
 - Weights:

$$G(d, \sigma) = e^{-d^2 / (2\sigma^2)}$$

- Weights need to be normalized, so that sum up to 1
- Use windowSize = 3*sigma
 - Sigma can be 1
- Window can be square

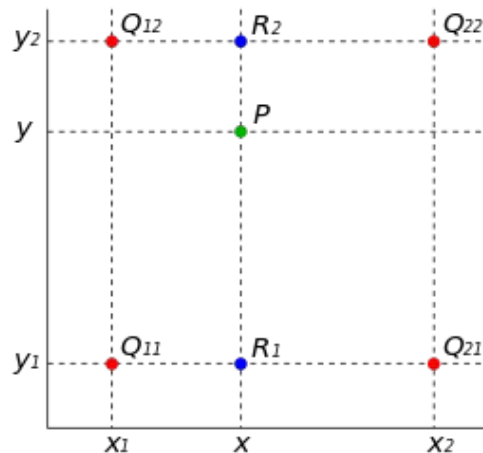


Resampling

- Bilinear interpolation

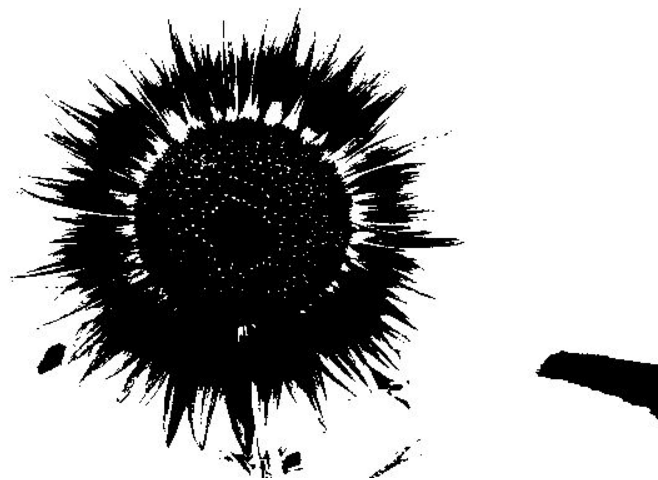
$$f(x, y) = \frac{1}{(x_2 - x_1)(y_2 - y_1)} (f(Q_{11})(x_2 - x)(y_2 - y) + f(Q_{21})(x - x_1)(y_2 - y) + f(Q_{12})(x_2 - x)(y - y_1) + f(Q_{22})(x - x_1)(y - y_1))$$

(from wikipedia)



Quantization

- Quantize a pixel within $[0, 1]$ using n bits
 - $\text{round}(p * (2^n - 1)) / (2^n - 1)$

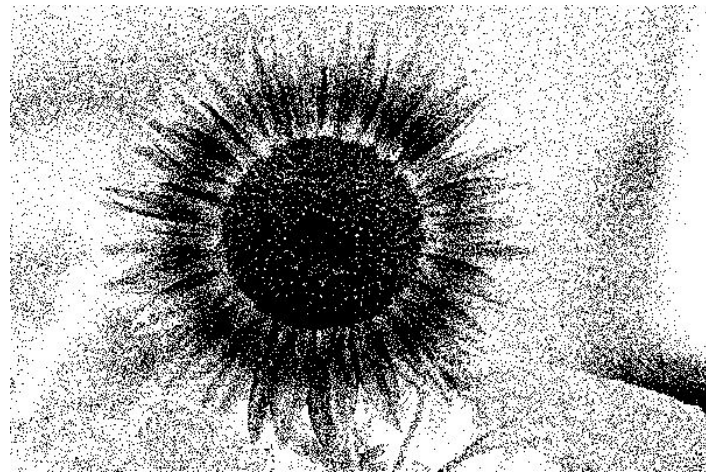


$n=1$ example

Random dithering

- Before quantization:
 - $p = p + (\text{random}() - 0.5)/(2^n - 1)$
 - n is number of bits per channel

Reduce banding with intentional noise



$n=1$ example

Ordered dithering

Pseudo code for n-bit case:

```
i = x mod m
j = y mod m
err = I(x, y) - floor_quantize(I(x, y))
threshold = (D(i, j) + 1) / (m^2 + 1)
if err > threshold
    P(x, y) = ceil_quantize(I(x, y))
else
    P(x, y) = floor_quantize(I(x, y))
```

- $\text{floor_quantize}(p)$
= $\text{floor}(p * (2^{n-1})) / (2^{n-1})$
- $\text{ceil_quantize}(p)$
= $\text{ceil}(p * (2^{n-1})) / (2^{n-1})$

$$m = 4, D = \begin{bmatrix} 15 & 7 & 13 & 5 \\ 3 & 11 & 1 & 9 \\ 12 & 4 & 14 & 6 \\ 0 & 8 & 2 & 10 \end{bmatrix}$$



n=1 example

Q&A
