

# Time



COS 418: Distributed Systems  
Lecture 5

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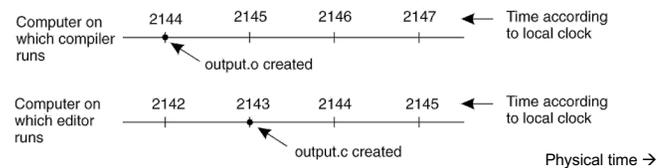
## Today

1. The need for time synchronization
2. “Wall clock time” synchronization
3. Logical Time: Lamport Clocks

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## A distributed edit-compile workflow



- $2143 < 2144 \rightarrow$  make **doesn't call compiler**

Lack of time synchronization result:  
a **possible object file mismatch**

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## What makes time synchronization hard?

1. Quartz oscillator sensitive to temperature, age, vibration, radiation
  - Accuracy ~one part per million: one second of clock drift over 12 days
2. The internet is:
  - Asynchronous: arbitrary message delays
  - Best-effort: messages don't always arrive

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## Today

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2. “Wall clock time” synchronization
  - Cristian’s algorithm, NTP
3. Logical Time: Lamport clocks

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## Just use Coordinated Universal Time?

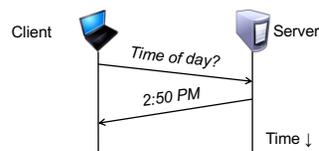
- UTC is broadcast from radio stations on land and satellite (e.g., the Global Positioning System)
  - Computers with receivers can synchronize their clocks with these timing signals
- Signals from land-based stations are accurate to about 0.1–10 milliseconds
- Signals from GPS are accurate to about one microsecond
  - *Why can't we put GPS receivers on all our computers?*

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## Synchronization to a time server

- Suppose a server with an accurate clock (e.g., GPS-receiver)
  - Could simply issue an RPC to obtain the time:



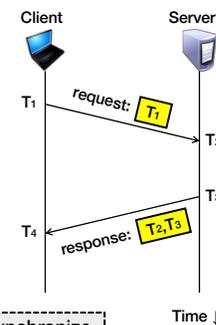
- But this doesn't account for network latency
  - Message delays will have **outdated** server's answer

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## Cristian's algorithm: Outline

1. Client sends a **request** packet, timestamped with its local clock  $T_1$
2. Server timestamps its receipt of the request  $T_2$  with its local clock
3. Server sends a **response** packet with its local clock  $T_3$  and  $T_2$
4. Client locally timestamps its receipt of the server's response  $T_4$



How can the client use these timestamps to synchronize its local clock to the server's local clock?

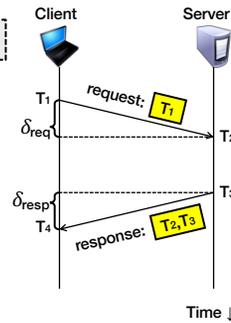
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## Cristian's algorithm: Offset sample calculation

Goal: Client sets clock  $\leftarrow T_3 + \delta_{resp}$

- Client samples round trip time ( $\delta$ )  
 $\delta = \delta_{req} + \delta_{resp} = (T_4 - T_1) - (T_3 - T_2)$



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## Cristian's algorithm: Offset sample calculation

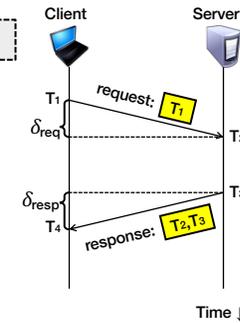
Goal: Client sets clock  $\leftarrow T_3 + \delta_{resp}$

- Client samples round trip time ( $\delta$ )  
 $\delta = \delta_{req} + \delta_{resp} = (T_4 - T_1) - (T_3 - T_2)$

- But client knows  $\delta$ , not  $\delta_{resp}$

Assume:  $\delta_{req} \approx \delta_{resp}$

Client sets clock  $\leftarrow T_3 + \frac{1}{2}\delta$



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## Clock synchronization: Take-away points

- Clocks on different systems will always behave differently
  - Disagreement between machines can result in undesirable behavior
- NTP clock synchronization
  - Rely on timestamps to estimate network delays
  - 100s  $\mu$ s–ms accuracy
  - Clocks never exactly synchronized
- Often **inadequate** for distributed systems
  - Often need to reason about the order of events
  - Might need precision on the order of ns

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## Today

- The need for time synchronization
- “Wall clock time” synchronization
  - Cristian's algorithm, NTP
- Logical Time: Lamport clocks

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## Motivation: Multi-site database replication

- A New York-based bank wants to make its transaction ledger database resilient to whole-site failures
- **Replicate** the database, keep one copy in sf, one in nyc



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## The consequences of concurrent updates

- **Replicate** the database, keep one copy in sf, one in nyc
  - Client sends reads to the nearest copy
  - Client sends update to both copies



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## RFC 677 (1975) "The Maintenance of Duplicate Databases"

"To the extent that the communication paths can be made reliable, and the clocks used by the processes kept close to synchrony, the probability of seemingly strange behavior can be made very small. However, *the distributed nature of the system dictates that this probability can never be zero.*"

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## Idea: Logical clocks

- Landmark 1978 paper by Leslie Lamport
- Insight: only the **events themselves** matter



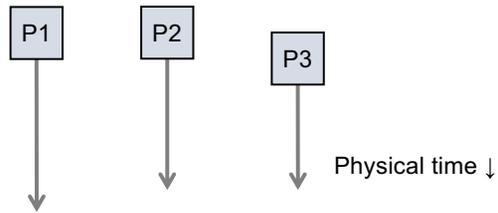
Idea: Disregard the precise clock time  
Instead, capture **just** a "happens before"  
relationship between a pair of events

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## Defining “happens-before” ( $\rightarrow$ )

- Consider three processes: P1, P2, and P3
- Notation: Event a **happens before** event b ( $a \rightarrow b$ )

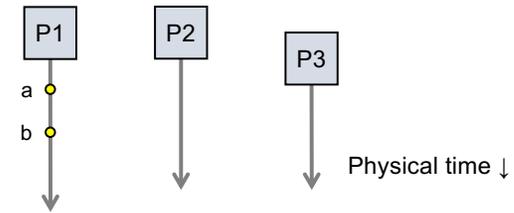


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## Defining “happens-before” ( $\rightarrow$ )

- Can observe event order at a single process

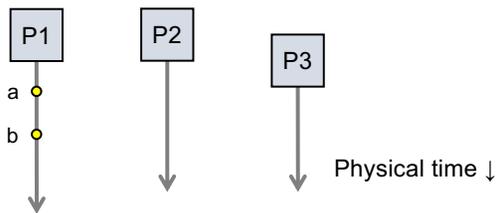


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## Defining “happens-before” ( $\rightarrow$ )

1. If **same process** and a occurs before b, then  $a \rightarrow b$

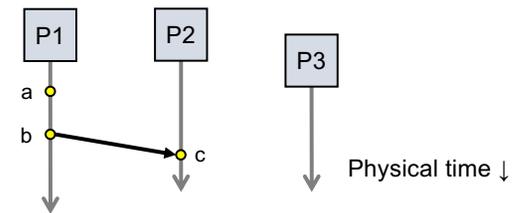


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## Defining “happens-before” ( $\rightarrow$ )

1. If **same process** and a occurs before b, then  $a \rightarrow b$
2. Can observe ordering when processes communicate

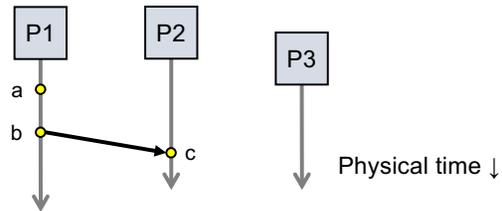


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## Defining “happens-before” ( $\rightarrow$ )

1. If **same process** and **a** occurs before **b**, then  $a \rightarrow b$
2. If **c** is a message receipt of **b**, then  $b \rightarrow c$
3. Can observe ordering transitively

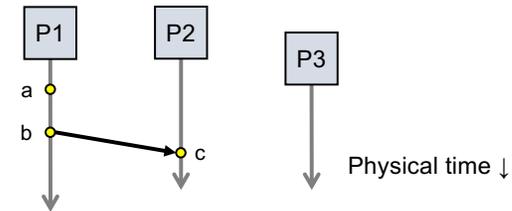


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## Defining “happens-before” ( $\rightarrow$ )

1. If **same process** and **a** occurs before **b**, then  $a \rightarrow b$
2. If **c** is a message receipt of **b**, then  $b \rightarrow c$
3. If  $a \rightarrow b$  and  $b \rightarrow c$ , then  $a \rightarrow c$

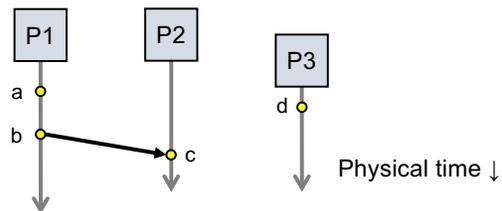


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## Concurrent events

- Not all events are related by  $\rightarrow$
- a, d not related by  $\rightarrow$  so **concurrent**, written as  $a \parallel d$



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## Lamport clocks: Objective

- We seek a **clock time**  $C(a)$  for every event **a**

Plan: Tag events with clock times; use clock times to make distributed system correct

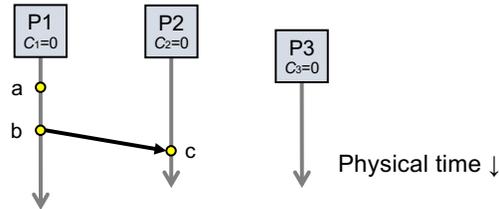
- **Clock condition:** If  $a \rightarrow b$ , then  $C(a) < C(b)$

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### The Lamport Clock algorithm

- Each process  $P_i$  maintains a local clock  $C_i$
- 1. Before executing an event,  $C_i \leftarrow C_i + 1$

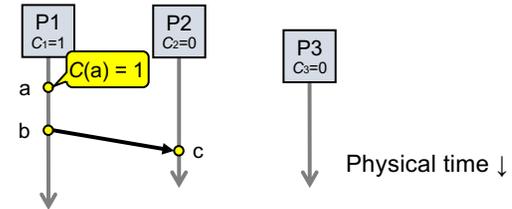


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### The Lamport Clock algorithm

1. Before executing an event a,  $C_i \leftarrow C_i + 1$ :
  - Set event time  $C(a) \leftarrow C_i$

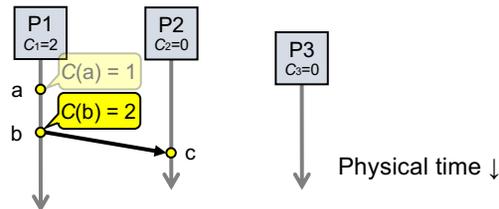


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### The Lamport Clock algorithm

1. Before executing an event b,  $C_i \leftarrow C_i + 1$ :
  - Set event time  $C(b) \leftarrow C_i$

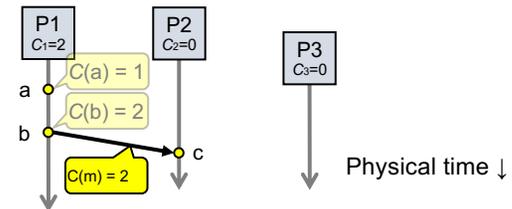


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### The Lamport Clock algorithm

1. Before executing an event b,  $C_i \leftarrow C_i + 1$
2. Send the local clock in the message m

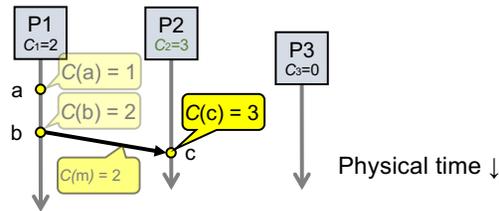


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## The Lamport Clock algorithm

3. On process  $P_j$  receiving a message  $m$ :
- Set  $C_j$  and receive event time  $C(c) \leftarrow 1 + \max\{C_j, C(m)\}$



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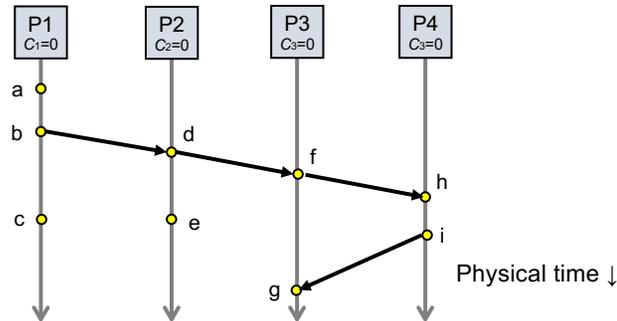
## Lamport Timestamps: Ordering all events

- Break ties by appending the process number to each event:
  - Process  $P_i$  timestamps event  $e$  with  $C_i(e), i$
  - $C(a), i < C(b), j$  when:
    - $C(a) < C(b)$ , or  $C(a) = C(b)$  and  $i < j$
- Now, for any two events  $a$  and  $b$ ,  $C(a) < C(b)$  or  $C(b) < C(a)$ 
  - This is called a total ordering of events

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## Order all these events



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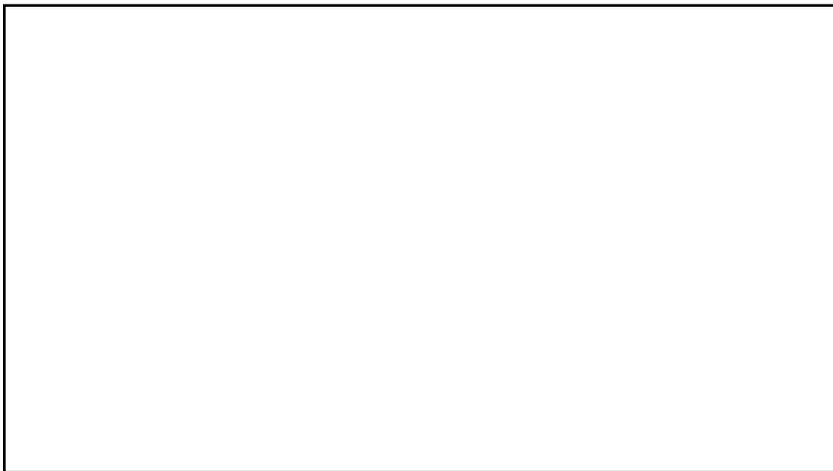
## Take-away points: Lamport clocks

- Can totally-order events in a distributed system: that's useful!
  - We saw an application of Lamport clocks for totally-ordered multicast
- But: while by construction,  $a \rightarrow b$  implies  $C(a) < C(b)$ ,
  - The converse is not necessarily true:
    - $C(a) < C(b)$  does not imply  $a \rightarrow b$  (possibly,  $a \parallel b$ )

Can't use Lamport timestamps to infer causal relationships between events

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