# Image Compositing \& Morphing 

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## Digital Image Processing

- Changing pixel values • Moving image locations
- Linear: scale, offset, etc.
- Nonlinear: gamma, saturation, etc.
- Histogram equalization
- Filtering over neighborhoods
- Blur \& sharpen
- Detect edges
- Median
- Bilateral filter
- Scale
- Rotate
- Warp
- Combining images
- Composite
- Morph
- Quantization
- Spatial / intensity tradeoff
- Dithering


## Types of Transparency

- Refraction
- Light is bent as it goes through an object
- Can focus light: caustics
- Can be color-dependent: dispersion



## Types of Transparency

- Refraction
- Subsurface scattering
- Translucent materials

- Light leaves at different position than it entered



## Types of Transparency

- Refraction
- Subsurface scattering
- Today: compositing
- Separate image into layers with known order
- Pixelwise combination: each pixel in each layer
 can be transparent, opaque, or somewhere in between


## Example



Jurassic Park (1993)

## Image Composition

- Issues:
- Segmenting image into regions
- Blending into single image seamlessly


## Image Composition

- Issues:
$>$ Segmenting image into regions
- Blending into single image seamlessly


## Image Matting

- Chroma keying (blue- or green-screen)
- Photograph object in front of screen with known color



## Image Matting

- Specify segmentation by hand
- Purely manual: draw matte every frame
- Semi-automatic: graph-cut (draw a few strokes) Separate image regions along minimal cuts (where edges measure differences between adjacent pixels)



## Image Matting

- Novel methods, e.g. flash matting



## Image Matting

- Portrait mode in Google Pixel Phone



## Image Matting

## - Portrait mode in Google Pixel Phone



## Image Composition

- Issues:
- Segmenting image into regions
> Blending into single image seamlessly


## Image Blending

- Ingredients
- Background image
- Foreground image with blue background
- Method
- Non-blue foreground pixels overwrite background



## Blending with Alpha Channel

Per-pixel "alpha" channel: controls the linear interpolation between foreground and background pixels when elements are composited.


## Alpha Channel

- Encodes pixel coverage information
- $\quad \alpha=0$ : no coverage (or transparent)
- $\quad \alpha=1$ : full coverage (or opaque)
- $0<\alpha<1$ : partial coverage (or semi-transparent)
- Example: $\alpha=0.3$



## Alpha Blending: "Over" Operator

$C=A$ over $B$
$C=\alpha_{A} A+\left(1-\alpha_{A}\right) B$


## Compositing Algebra

- Suppose we put A over B over background G

- How much of $B$ is blocked by $A$ ?

$$
\alpha_{\mathrm{A}}
$$

- How much of $B$ shows through $A$

$$
\left(1-\alpha_{A}\right)
$$

- How much of $G$ shows through both $A$ and $B$ ?

$$
\left(1-\alpha_{A}\right)\left(1-\alpha_{B}\right)
$$

## Compositing Algebra

- Suppose we put A over B over background G

- Final result?

$$
\begin{gathered}
\alpha_{A} A+\left(1-\alpha_{A}\right) \alpha_{B} B+\left(1-\alpha_{A}\right)\left(1-\alpha_{B}\right) G \\
=\alpha_{A} A+\left(1-\alpha_{A}\right)\left[\alpha_{B} B+\left(1-\alpha_{B}\right) G\right] \\
=A \text { over }[B \text { over } G]
\end{gathered}
$$

Must perform "over" back-to-front: right associative!

## Other Compositing Operations

- How can we combine 2 partially covered pixels?
- 4 regions ( $0, A, B, A B$ )
- 3 possible colors (0, A, B)



## Blending with Alpha

Composition algebra - 12 combinations

$$
C^{\prime}=F_{A} \alpha_{A} A+F_{B} \alpha_{B} B
$$

| Operation | $F_{A}$ | $F_{B}$ |
| :--- | :---: | :---: |
| Clear | 0 | 0 |
| A | 1 | 0 |
| B | 0 | 1 |
| A over B | 1 | $1-\alpha_{A}$ |
| B over A | $1-\alpha_{B}$ | 1 |
| A in B | $\alpha_{B}$ | 0 |
| B in A | 0 | $\alpha_{A}$ |
| A out B | $1-\alpha_{B}$ | 0 |
| B out A | 0 | $1-\alpha_{A}$ |
| A atop B | $\alpha_{B}$ | $1-\alpha_{A}$ |
| B atop A | $1-\alpha_{B}$ | $\alpha_{A}$ |
| A xor B | $1-\alpha_{B}$ | $1-\alpha_{A}$ |


clear

$B$ in $A$


B out A


A


A out B


A atop B


B


B over A

$B$ atop A


A over B


A xor b

## Blending with Alpha

Composition algebra - 12 combinations

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| B | 0 | 1 |
| A over B | 1 | $1-\alpha_{A}$ |
| B over A | $1-\alpha_{B}$ | 1 |
| A in B | $\alpha_{B}$ | 0 |
| B in A | 0 | $\alpha_{A}$ |
| A out B | $1-\alpha_{B}$ | 0 |
| B out A | 0 | $1-\alpha_{A}$ |
| A atop B | $\alpha_{B}$ | $1-\alpha_{A}$ |
| B atop A | $1-\alpha_{B}$ | $\alpha_{A}$ |
| A x or B | $1-\alpha_{B}$ | $1-\alpha_{A}$ |



## Image Composition Example



Stars


Planet

## Image Composition Example



BFire


FFire
[Porter\&Duff Computer Graphics 18:3 1984]

## Image Composition Example



BFire out Planet


Composite
[Porter\&Duff Computer Graphics 18:3 1984]

## COS426 Examples



Darin Sleiter


## Poisson Image Blending


sources

destinations

cloning

seamless cloning

## Poisson Image Blending

Beyond simple compositing

- Solve for image samples that follow gradients of source subject to boundary conditions imposed by dest


$$
\min _{f} \iint_{\Omega}|\nabla f-\mathbf{v}|^{2} \text { with }\left.f\right|_{\partial \Omega}=\left.f^{*}\right|_{\partial \Omega}
$$

## Poisson Image Blending


source/destination

cloning

seamless cloning

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## Image Morphing

- Animate transition between two images

(a)


(b)


(C)

Figure 16-9
Transformation of an STP oil ca into an engine block. (Courtesy of Silicon Graphics, Inc.)

## Cross-Dissolving

- Blend images with "over" operator
- alpha of bottom image is 1.0
- alpha of top image varies from 0.0 to 1.0
blend $(\mathrm{i}, \mathrm{j})=(1-\mathrm{t}) \operatorname{src}(\mathrm{i}, \mathrm{j})+\mathrm{tdst}(\mathrm{i}, \mathrm{j}) \quad(0 \leq t \leq 1)$

$\mathrm{t}=0.0$
$t=0.5$


## Image Morphing

- Combines warping and cross-dissolving



## Beier \& Neeley Example



## Warp $_{0}$

Warp $_{1}$

## Beier \& Neeley Example



## Beier \& Neeley Example



Black or White, Michael Jackson (1991)

## Warping Pixel Locations



The original basis


The warped basis

$$
\begin{gathered}
u=\frac{(\boldsymbol{X}-\boldsymbol{P}) \cdot(\boldsymbol{Q}-\boldsymbol{P})}{\|\boldsymbol{Q}-\boldsymbol{P}\|^{2}} \\
\boldsymbol{v}=\frac{(\boldsymbol{X}-\boldsymbol{P}) \cdot \text { Perpendicular }(\boldsymbol{Q}-\boldsymbol{P})}{\|\boldsymbol{Q}-\boldsymbol{P}\|} \\
\boldsymbol{X}^{\prime}=\boldsymbol{P}^{\prime}+\boldsymbol{u} \cdot\left(\boldsymbol{Q}^{\prime}-\boldsymbol{P}^{\prime}\right)+\frac{\boldsymbol{v} \cdot \text { Perpendicular }\left(\boldsymbol{Q}^{\prime}-\boldsymbol{P}^{\prime}\right)}{\left\|\boldsymbol{Q}^{\prime}-\boldsymbol{P}^{\prime}\right\|}
\end{gathered}
$$

This generates one warp per line, each of which is a simple rotation and non-uniform scale (scaling is only done along the axis of the line). These warps must then be averaged to get the final warp. In the original paper, the weights for the average are tuned with the formula below. The dist variable is the distance of the point from the line segment, and the length variable is the length of the line segment.

$$
\text { weight }=\left(\frac{\text { length }^{p}}{a+\text { dist }^{b}}\right)^{b}
$$

The equations give several parameters to tune, and I got the best results when $a=0.001, b=2$, and $p=0$. Ignoring the length of the line segments (by setting $p$ to zero) gave better results than when the length was taken in to account. I used seven contours with 28 line segments to represent the features of each face.

## Warping Pseudocode

WarpImage(Image, $\left.L_{\text {src }}[\ldots], L_{\text {dst }}[\ldots]\right)$ begin
foreach destination pixel $\mathrm{p}_{\text {dst }}$ do psum $=(0,0)$ wsum = 0 foreach line $L_{\text {dst }}[i]$ do $p_{\text {src }}[i]=p_{\text {dst }}$ transformed by $\left(L_{\text {dst }}[i], L_{\text {src }}[i]\right)$ psum $=$ psum $+p_{\text {srcl }}[i]$ * weight[i] wsum += weight[i]
end
$\mathrm{p}_{\text {src }}=$ psum / wsum
$\operatorname{Result}\left(\mathrm{p}_{\text {dst }}\right)=\operatorname{Resample}\left(\mathrm{p}_{\text {src }}\right)$
end
end

## Morphing Pseudocode

GenerateAnimation(Image ${ }_{0}, \mathrm{~L}_{0}[\ldots]$, Image $_{1}, \mathrm{~L}_{1}[\ldots]$ ) begin
foreach intermediate frame time $t$ do for $i=1$ to number of line pairs do
$L[i]=$ line $t^{\text {th }}$ of the way from $L_{0}[i]$ to $L_{1}[i]$ end
Warp $_{0}=$ Warplmage $\left(\right.$ Image $\left._{0}, \mathrm{~L}_{0}, \mathrm{~L}\right)$ Warp $_{1}=$ WarpImage $\left(\right.$ Image $\left._{1}, \mathrm{~L}_{1}, \mathrm{~L}\right)$ foreach pixel p in Finallmage do Result(p) $=(1-t)$ Warp $_{0}+t$ Warp $_{1}$
end
end

## COS426 Example



Amy Ousterhout

## COS426 Examples



Sam Payne
Matt Matl

## Image Composition Applications

- "Computational photography":
new photographic effects that inherently use multiple images + computation
- Example: stitching images into a panorama



## Image Composition Applications

- Flash / No flash



## Image Composition Applications

- Photo montage

[Michael Cohen]


## Image Composition Applications

- Stoboscopic images

[Michael Cohen]


## Image Composition Applications

- Extended depth-of-field

[Michael Cohen]


# Scene Completion Using Millions of Photographs 

James Hays and Alexei A. Efros

SIGGRAPH 2007

Slides by J. Hays and A. Efros


Hays et al. SIGGRAPH 07


Hays et al. SIGGRAPH 07


Hays et al. SIGGRAPH 07

## Image Completion



Hays et al. SIGGRAPH 07

## Image Completion

### 2.3 Million unique images from Flickr



Hays et al. SIGGRAPH 07


Scene Completion Result
Hays et al. SIGGRAPH 07

## Image Completion Algorithm



Input image


Mosaicing


Image Collection


200 matches


Hays et al. SIGGRAPH 07


Hays et al. SIGGRAPH 07


Hays et al. SIGGRAPH 07


Hays et al. SIGGRAPH 07


Hays et al. SIGGRAPH 07

## Summary

- Image compositing
- Alpha channel
- Porter-Duff compositing algebra
- Image morphing
- Warping
- Compositing
- Computational photography

