Scan Conversion

COS 426, Spring 2021

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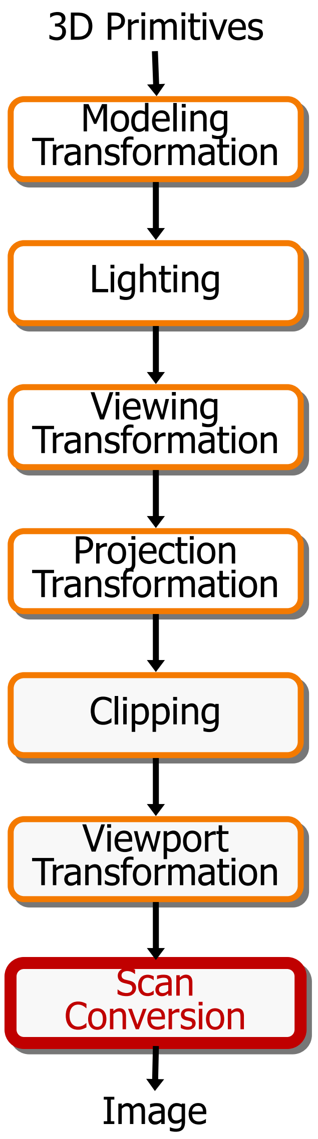
Princeton University

3D Rendering Pipeline (for direct illumination)



Rasterization

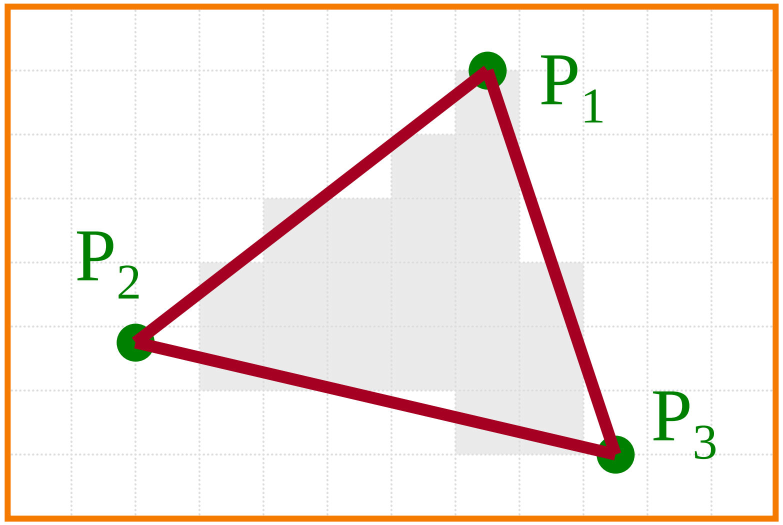
- Scan conversion
  - Determine which pixels to fill
- Shading
  - Determine a color for each filled pixel
- Texture mapping
  - Describe shading variation within polygon interiors
- Visible surface determination
  - Figure out which surface is front-most at every pixel

Rasterization

- Scan conversion (last time)
  - Determine which pixels to fill
- ➢ Shading
  - Determine a color for each filled pixel
- Texture mapping
  - Describe shading variation within polygon interiors
- Visible surface determination
  - Figure out which surface is front-most at every pixel

Shading

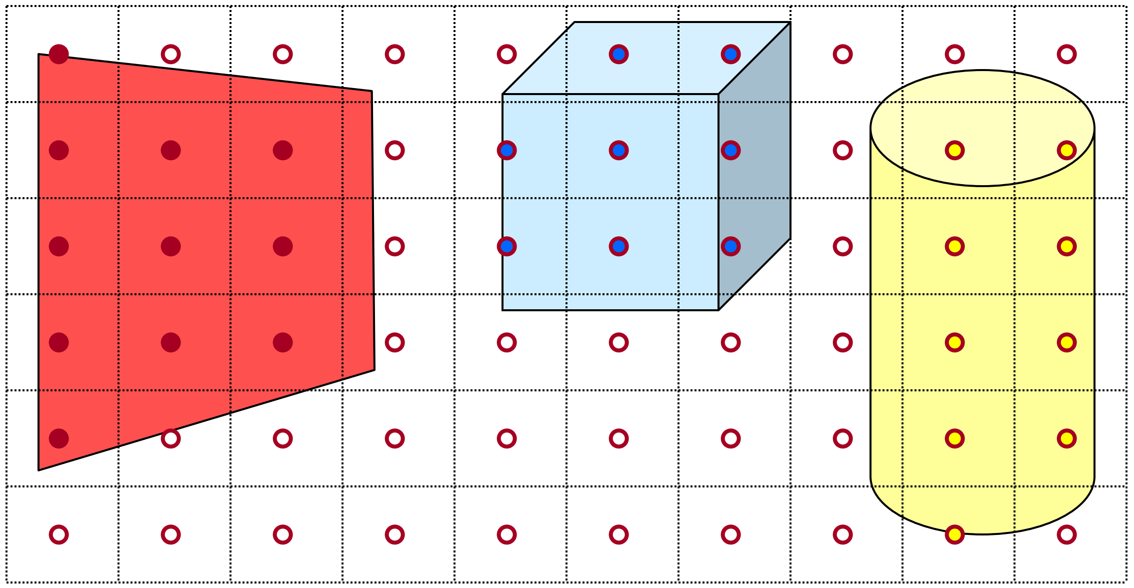
- How do we choose a color for each filled pixel?



Emphasis on methods that can be implemented in hardware

Ray Casting

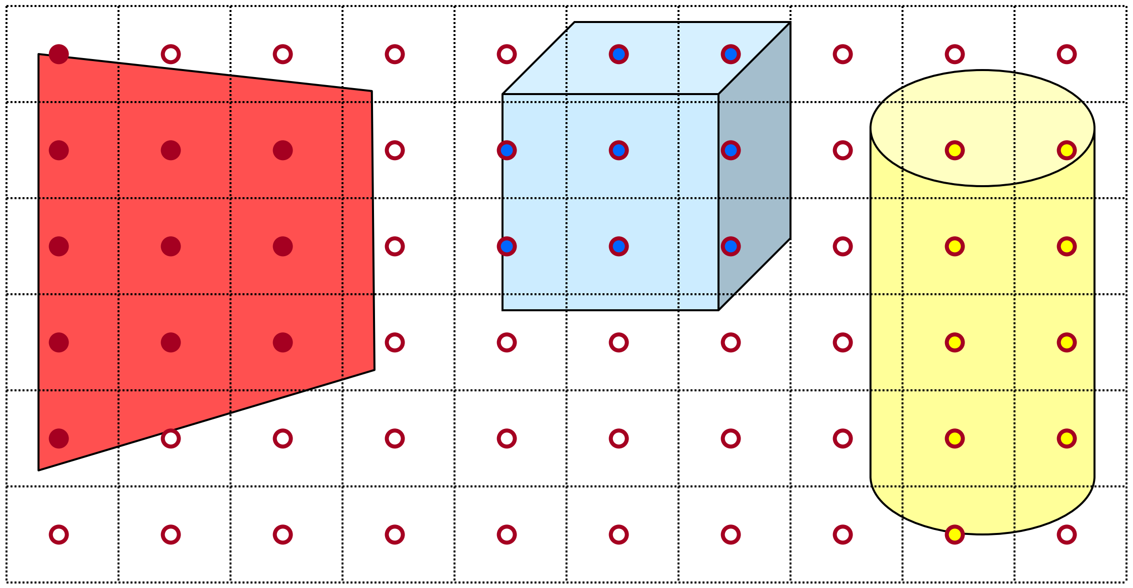
- Simplest shading approach is to perform independent lighting calculation for every pixel



$$I = I_E + K_A I_{AL} + \sum_i \left(K_D (N \cdot L_i) I_i + K_S (V \cdot R_i)^n I_i \right)$$

Polygon Shading

- Can take advantage of spatial coherence
  - Illumination calculations for pixels covered by same primitive are related to each other



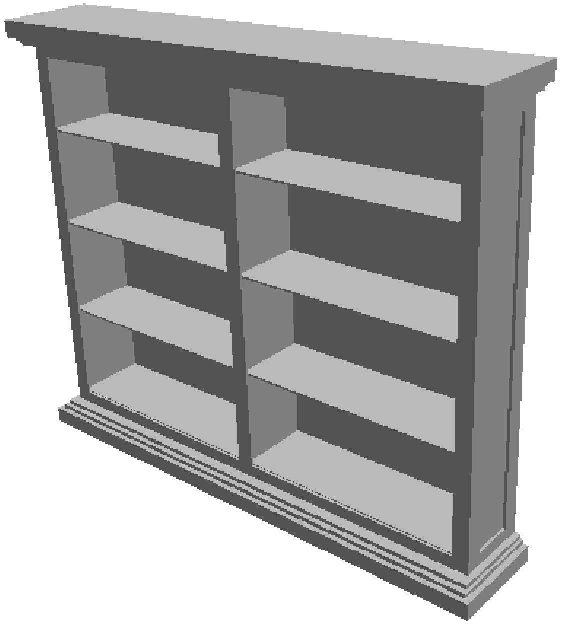
$$\boxed{I = I_E + K_A I_{AL} + \sum_i \left(K_D (N \cdot L_i) I_i + K_S (V \cdot R_i)^n I_i \right)}$$

Polygon Shading Algorithms

- **Flat Shading**
- Gouraud Shading
- Phong Shading

Flat Shading

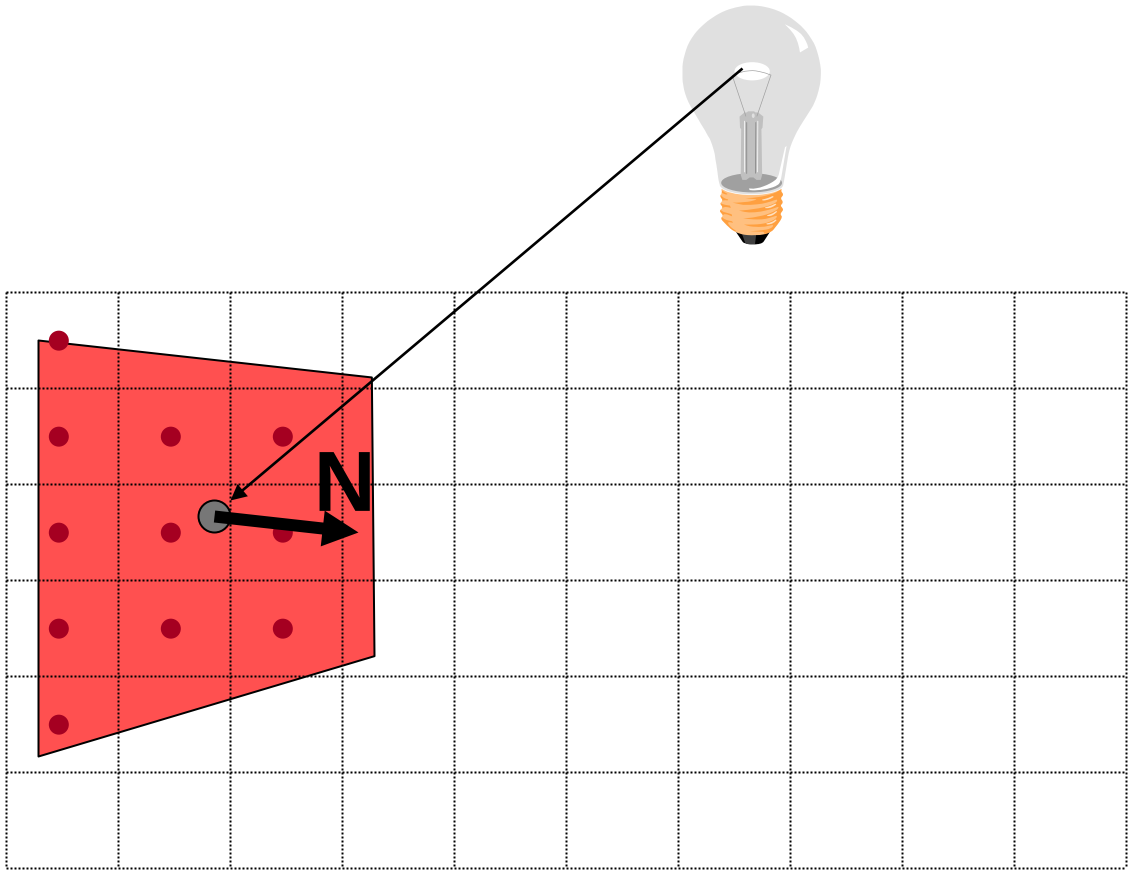
- What if a faceted object is illuminated only by directional light sources and is viewed from infinitely far away



$$\boxed{I = I_E + K_A I_{AL} + \sum_i \left(K_D (N \cdot L_i) I_i + K_S (V \cdot R_i)^n I_i \right)}$$

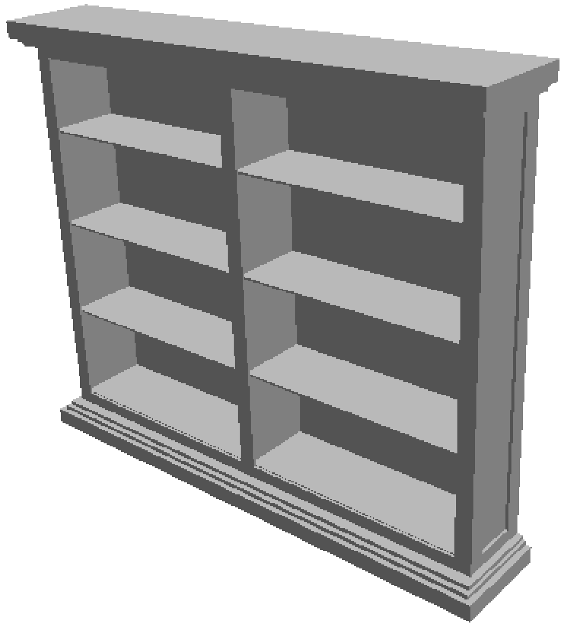
Flat Shading

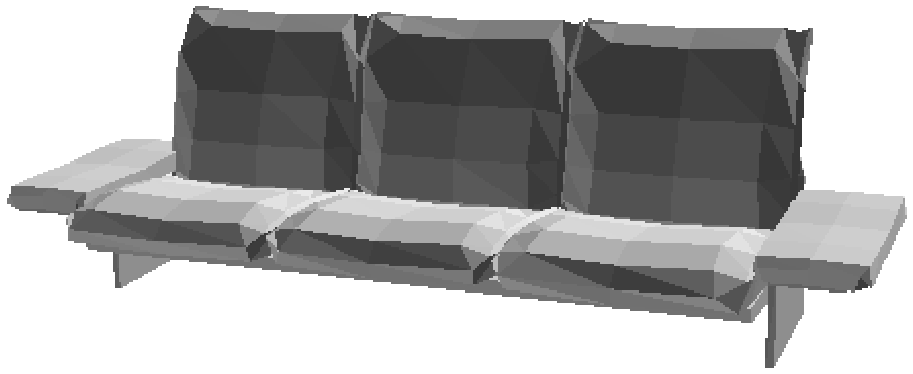
- One illumination calculation per polygon
  - Assign all pixels inside each polygon the same color



Flat Shading

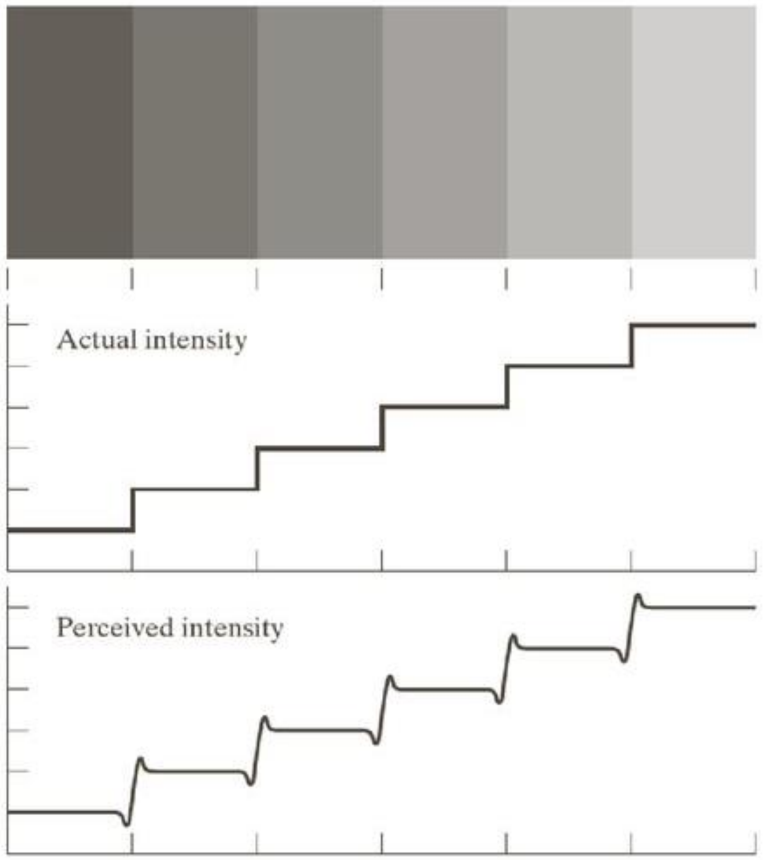
- Objects look like they are composed of polygons
  - OK for polyhedral objects
  - Not so good for smooth surfaces





Mach Band Effect

- Edges between adjacent shades of gray are perceived as exaggerated.

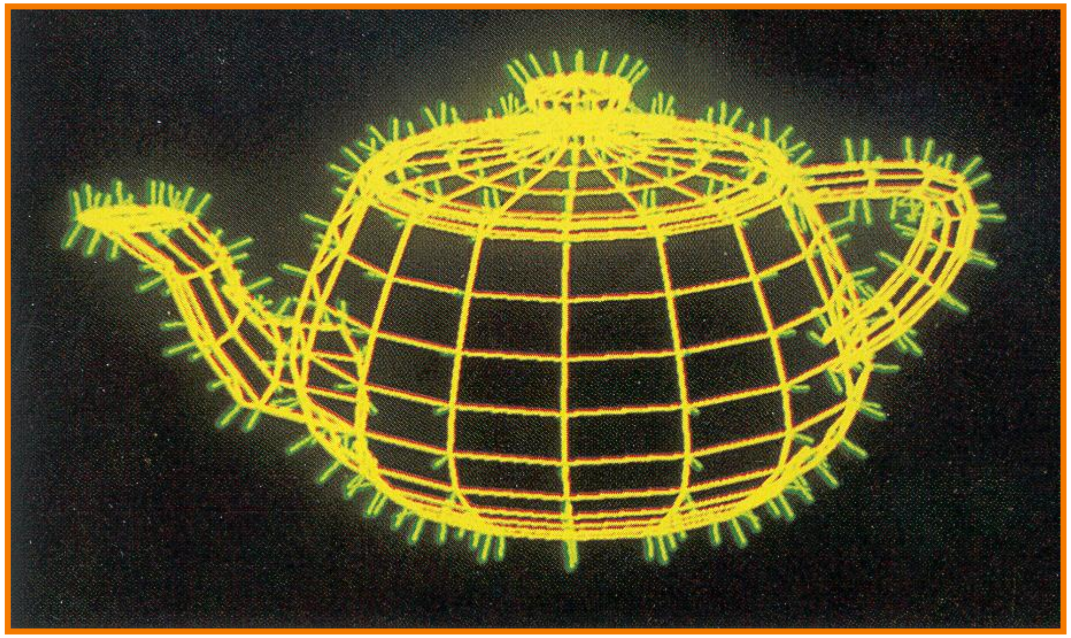


Polygon Shading Algorithms

- Flat Shading
- **Gouraud Shading**
- Phong Shading

Gouraud Shading

- What if smooth surface is represented by polygonal mesh with a normal at each vertex?

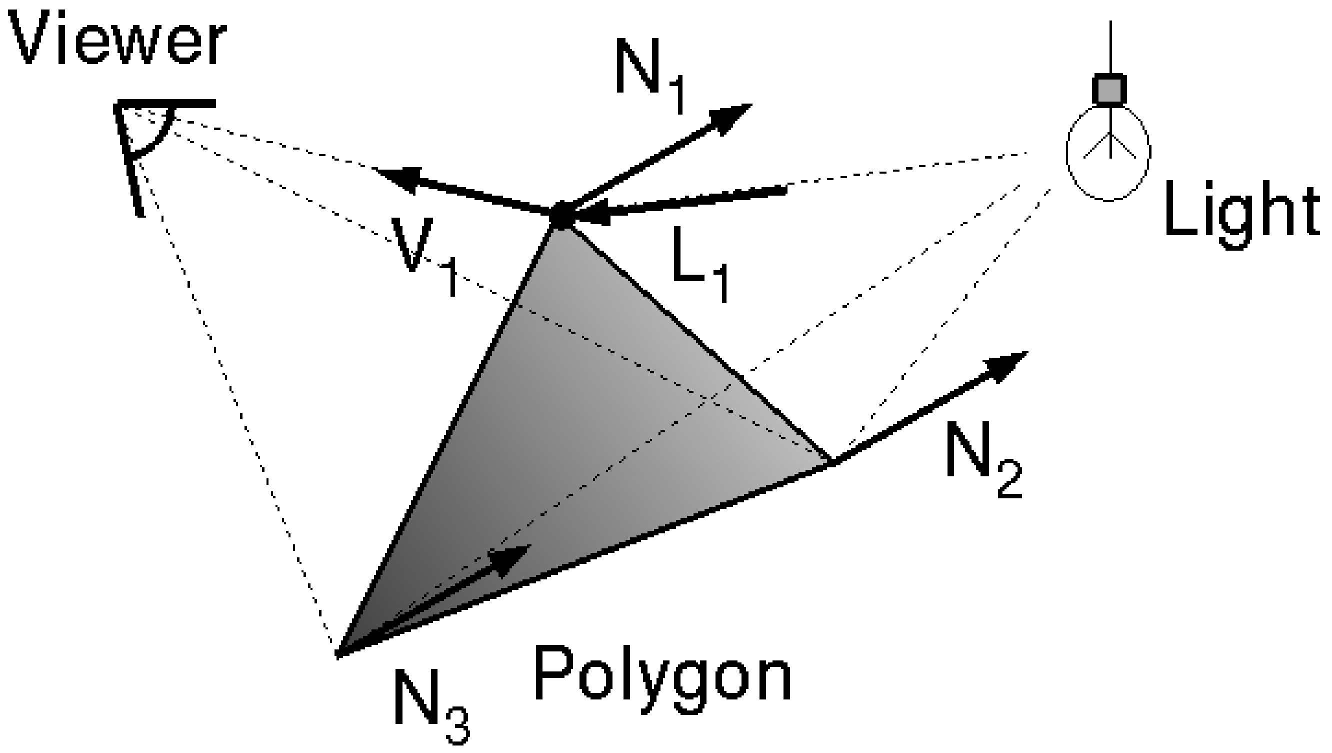


Watt Plate 7

$$I = I_E + K_A I_{AL} + \sum_i \left(K_D (N \cdot L_i) I_i + K_S (V \cdot R_i)^n I_i \right)$$

Gouraud Shading

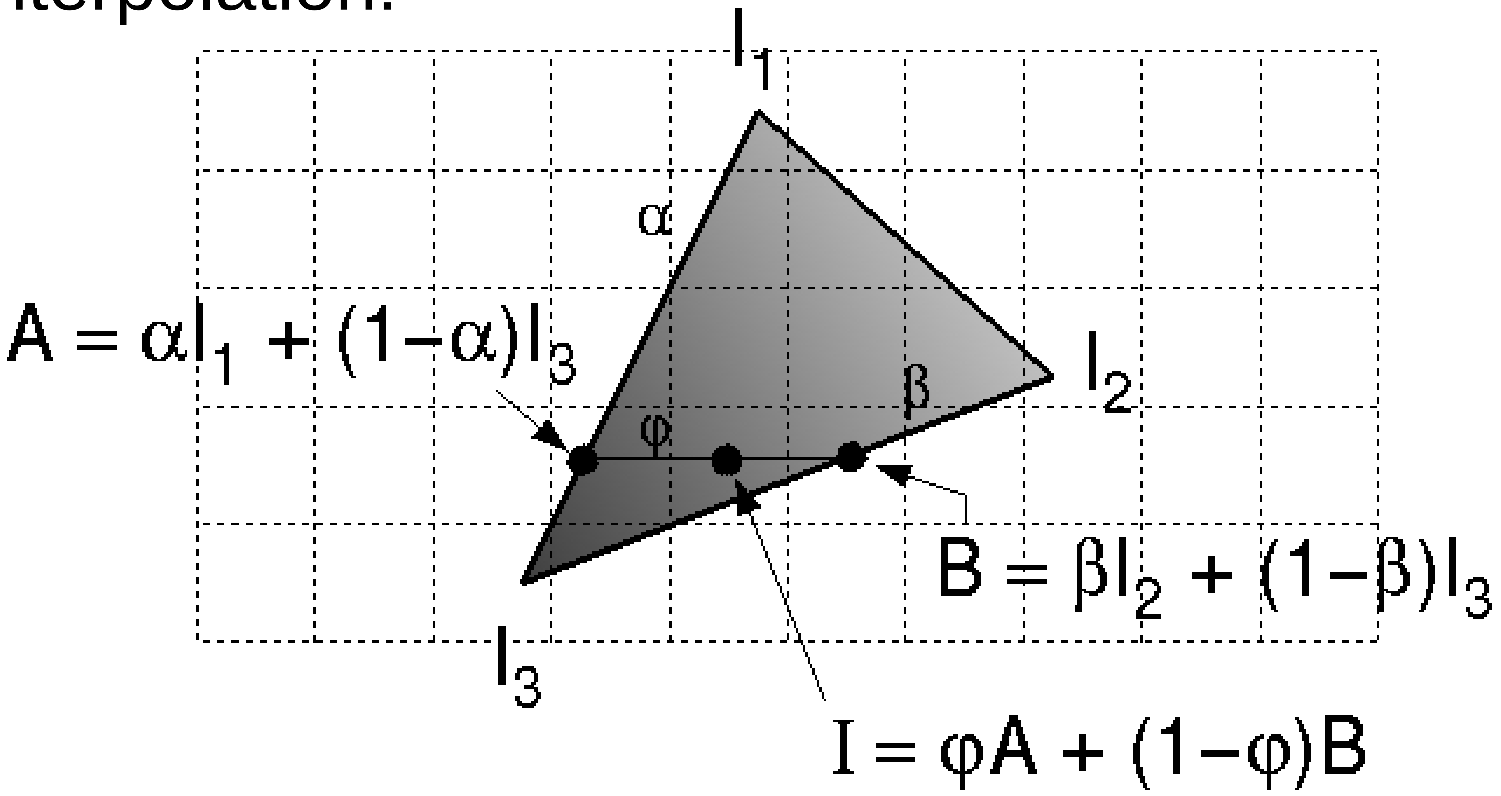
- One lighting calculation per vertex
  - Assign pixels inside polygon by interpolating colors computed at vertices



Gouraud Shading

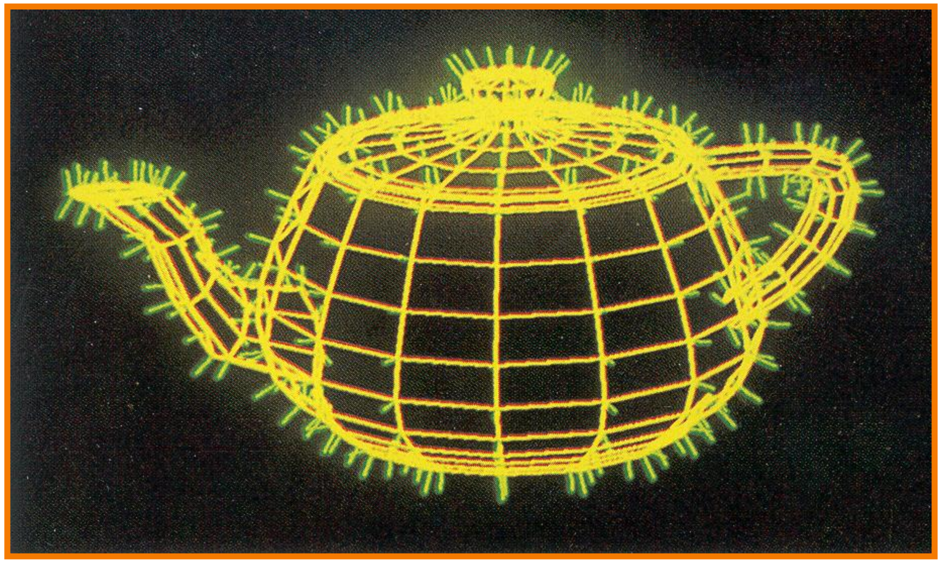
Bilinear interpolation of colors at vertices

- down and across scan lines = barycentric interpolation!


I_1
I_2
I_3
α
β
φ
$A = \alpha I_1 + (1-\alpha) I_3$
$B = \beta I_2 + (1-\beta) I_3$
$I = \varphi A + (1-\varphi) B$

Gouraud Shading

- Smooth shading over adjacent polygons
  - Curved surfaces
  - Illumination highlights
  - Soft shadows

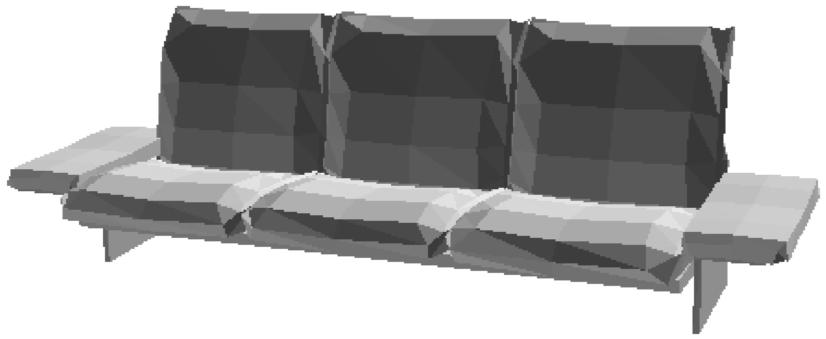


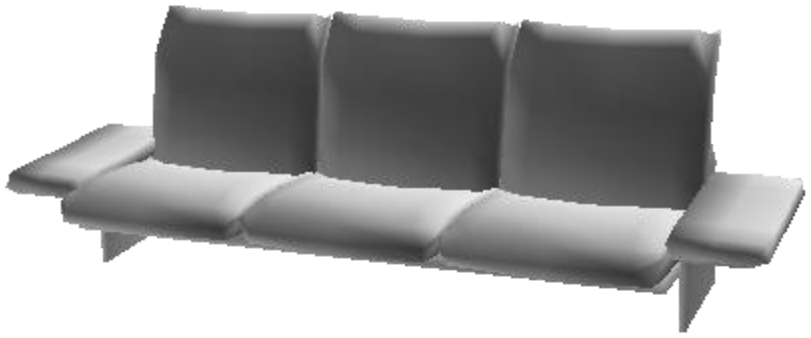
Mesh with shared normals at vertices

Watt Plate 7

Gouraud Shading

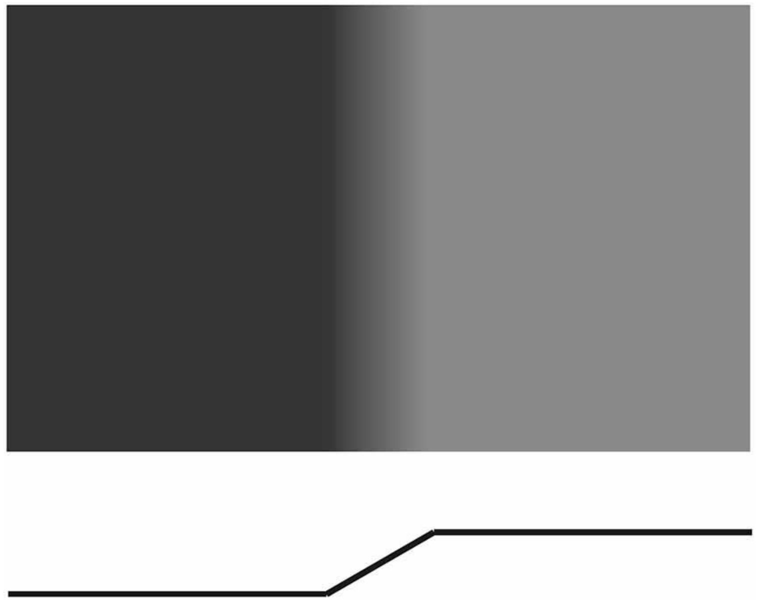
- Produces smoothly shaded polygonal mesh
  - Piecewise linear (!) approximation
  - Need fine mesh to capture subtle lighting effects

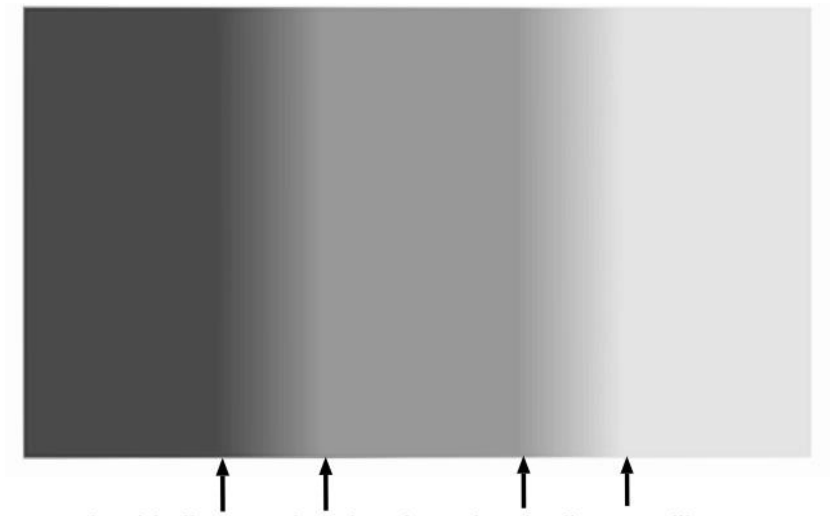

Flat Shading


Gouraud Shading

Mach Band Effect

- Mach Band Effect also affects Gouraud Shading for piecewise linear interpolation.



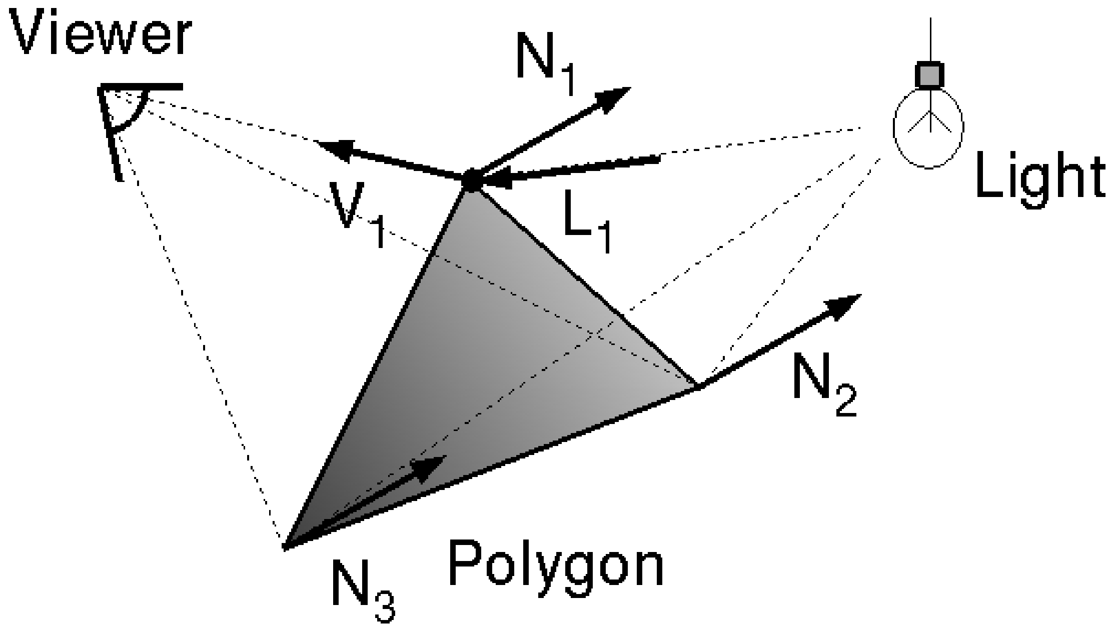

The thin lines or "bands" along the gradient are illusory.

Polygon Shading Algorithms

- Flat Shading
- Gouraud Shading
- **Phong Shading** (≠ Phong reflectance model)

Phong Shading

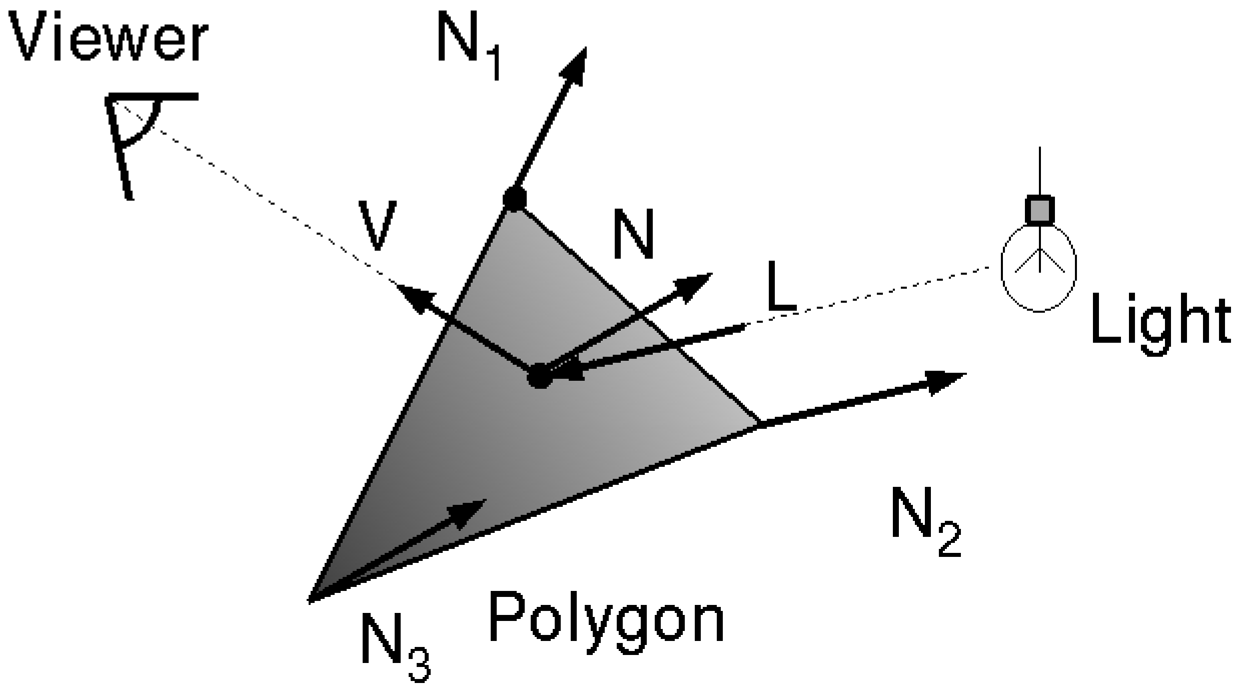
- What if polygonal mesh is too coarse to capture illumination effects in polygon interiors?



$$I = I_E + K_A I_{AL} + \sum_i \left(K_D (N \cdot L_i) I_i + K_S (V \cdot R_i)^n I_i \right)$$

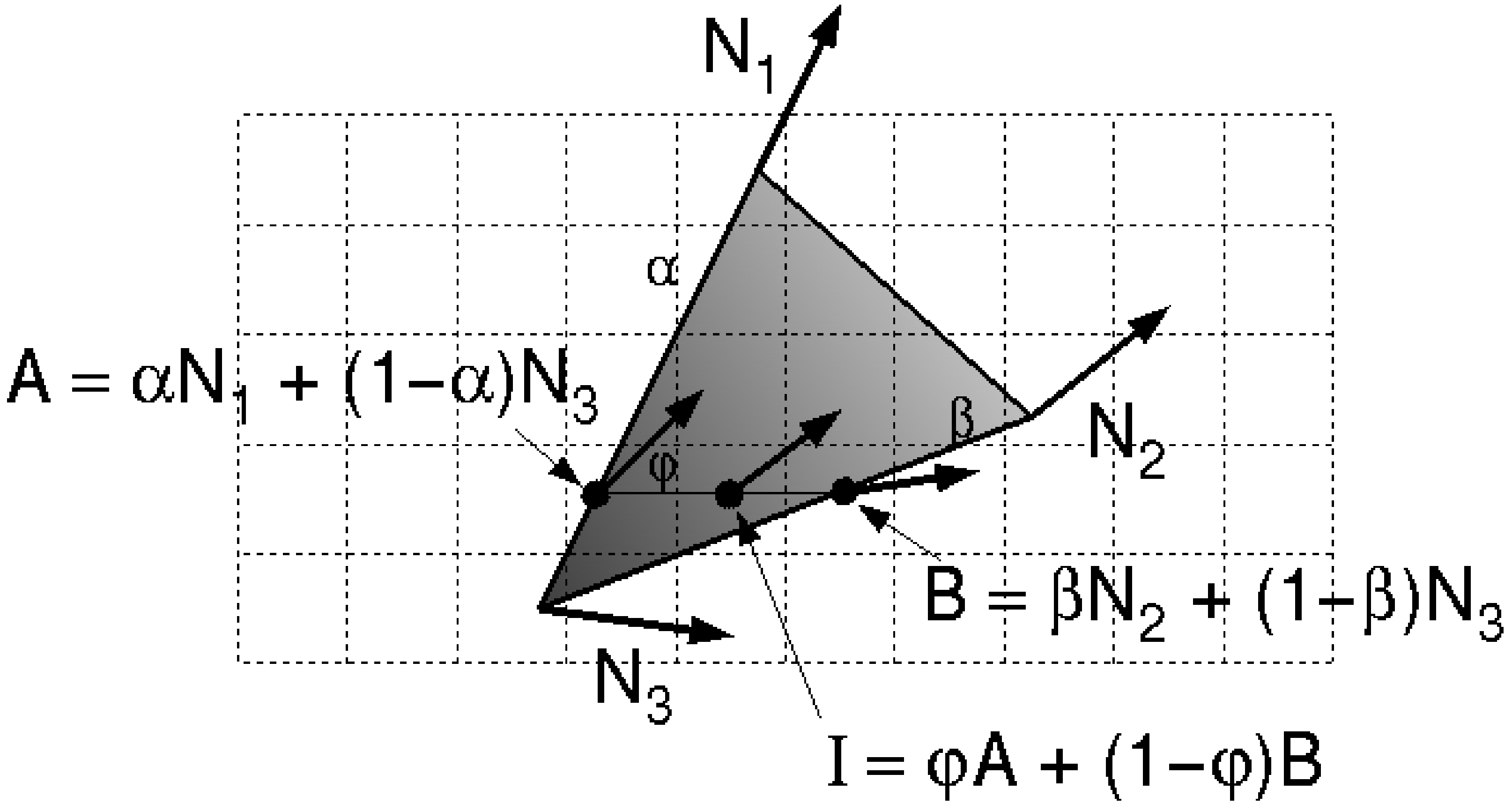
Phong Shading

- One lighting calculation per pixel
  - Approximate surface normals for points inside polygons by bilinear interpolation of normals from vertices



Phong Shading

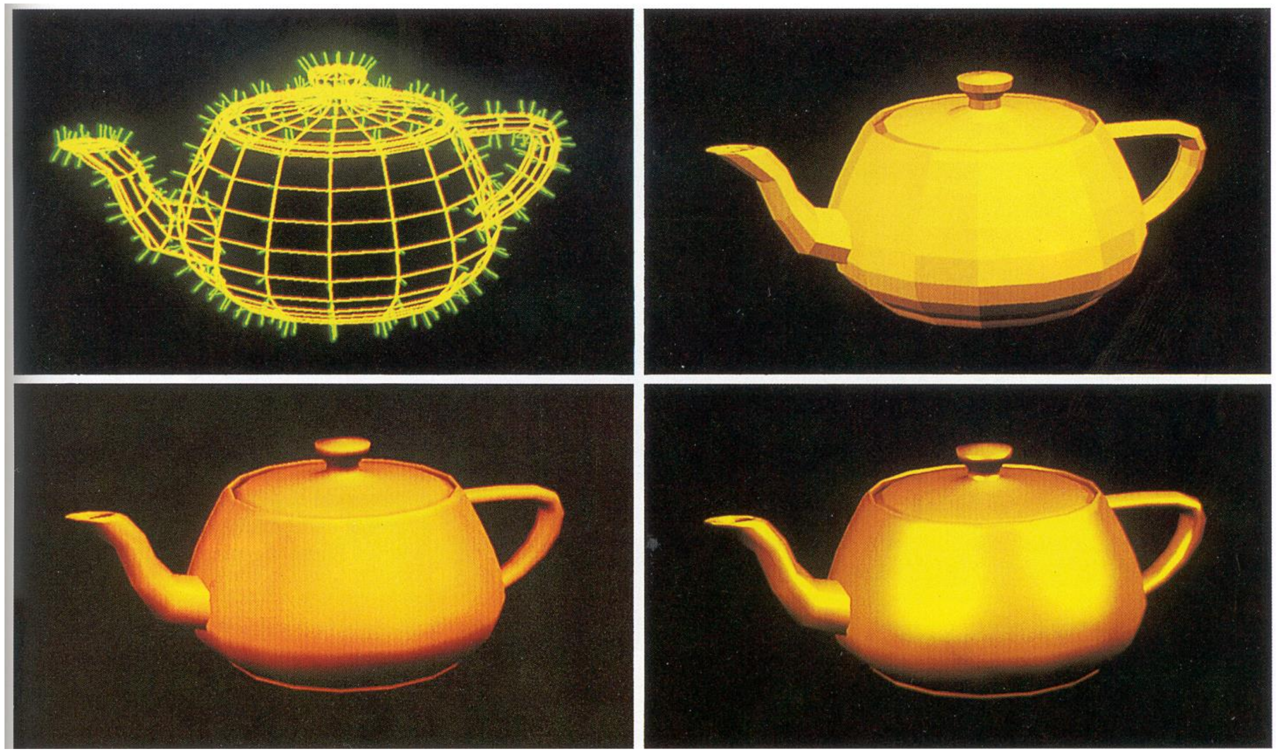
Bilinear interpolation of surface normals at vertices



N_1
α
$A = \alpha N_1 + (1-\alpha)N_3$
φ
β
N_2
$B = \beta N_2 + (1-\beta)N_3$
N_3
$I = \varphi A + (1-\varphi)B$

Polygon Shading Algorithms

Wireframe Flat



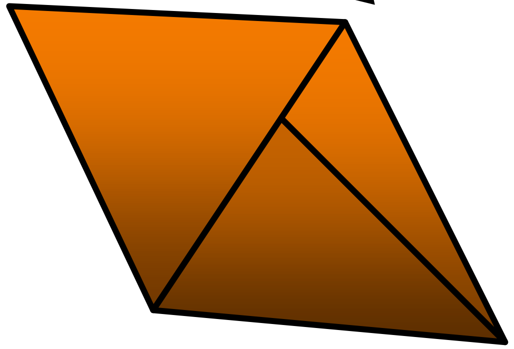
Gouraud Phong

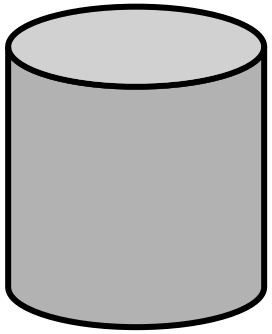
Demo: https://threejs.org/docs/scenes/material-browser.html#MeshPhongMaterial

Watt Plate 7

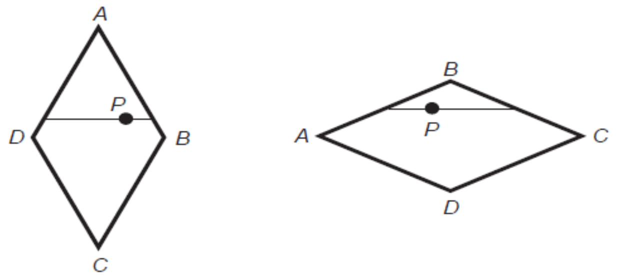
Shading Issues

- Problems with interpolated shading:
  - Polygonal silhouettes still obvious
  - Perspective distortion (due to screen-space interpolation)
  - Problems computing shared vertex normals
  - Problems at T-junctions





The results of interpolated-shading is not independent of the projected polygons position (Foley Figure 14.22).



Rasterization

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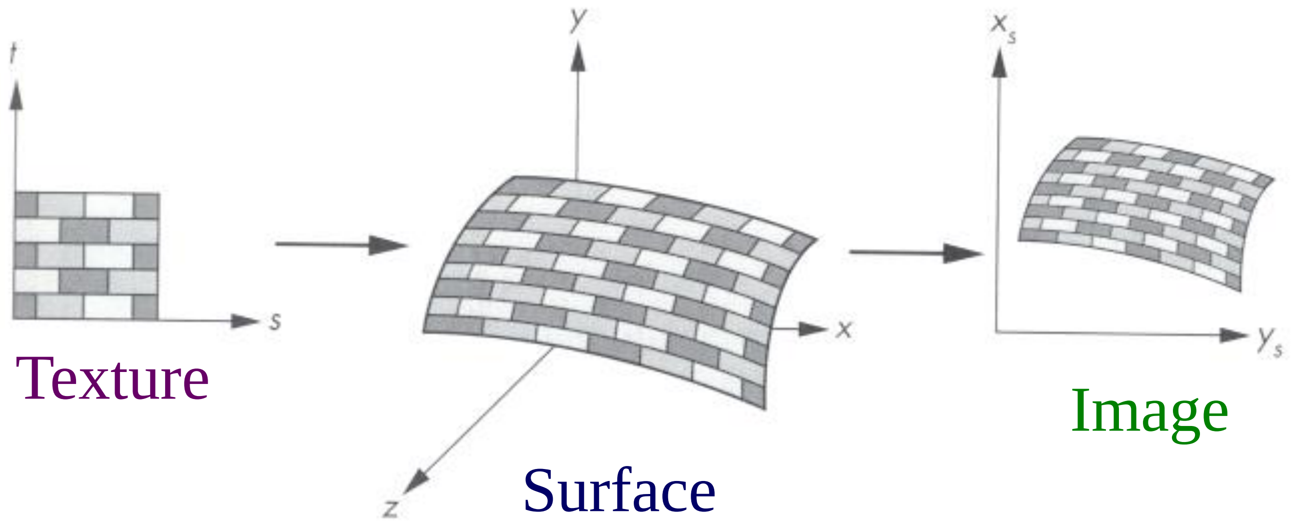
Textures

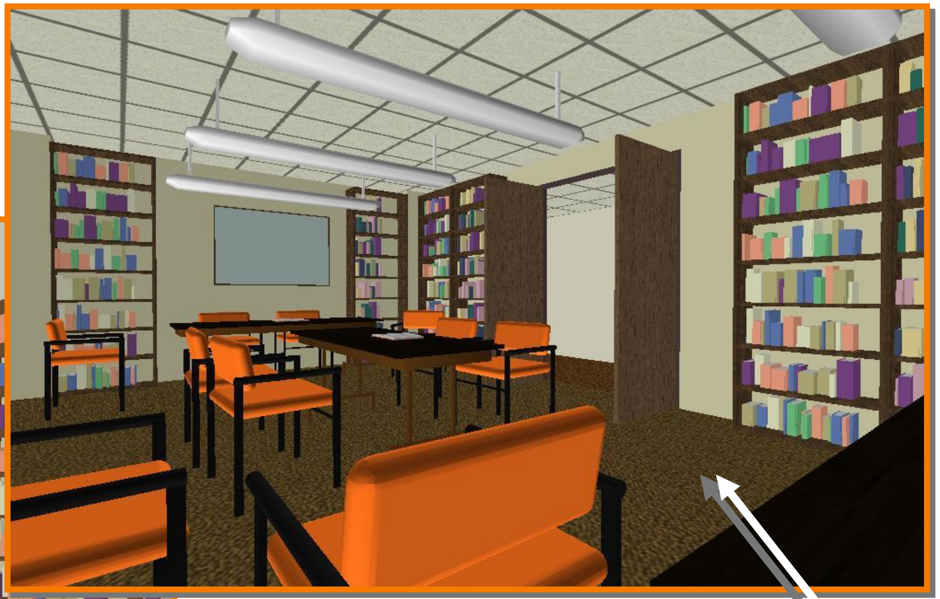
- Describe **color variation** in interior of 3D polygon
    - When scan converting a polygon, **vary pixel colors** according to values fetched from a texture image



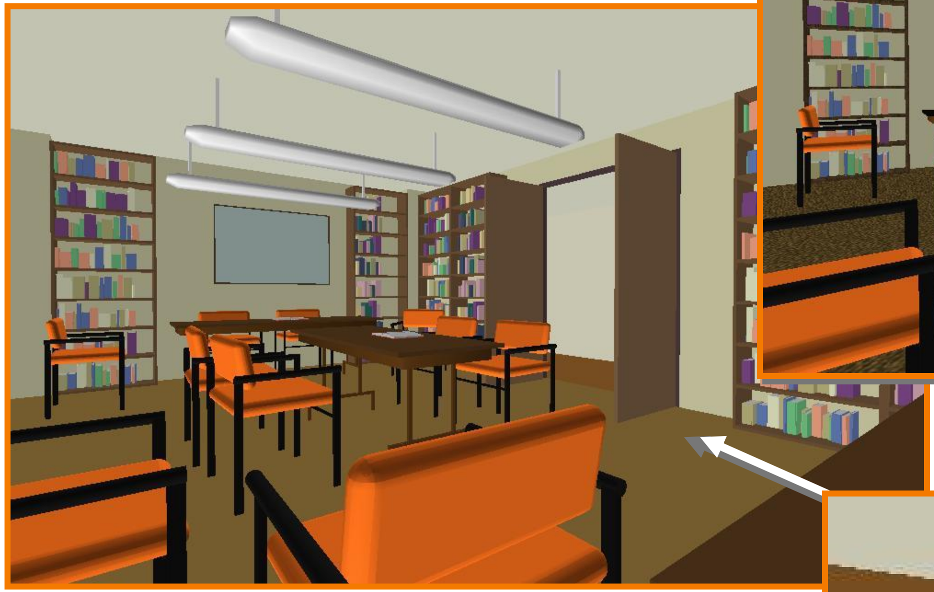
Angel Figure 9.3

Surface Textures

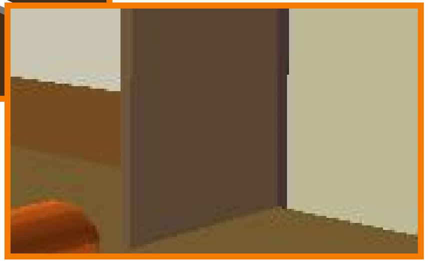
- Add visual detail to surfaces of 3D objects

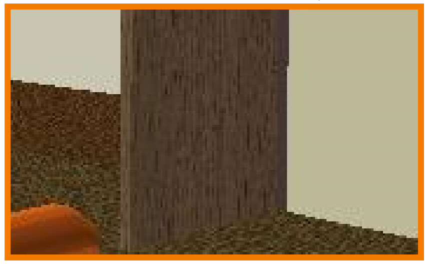


With surface texture



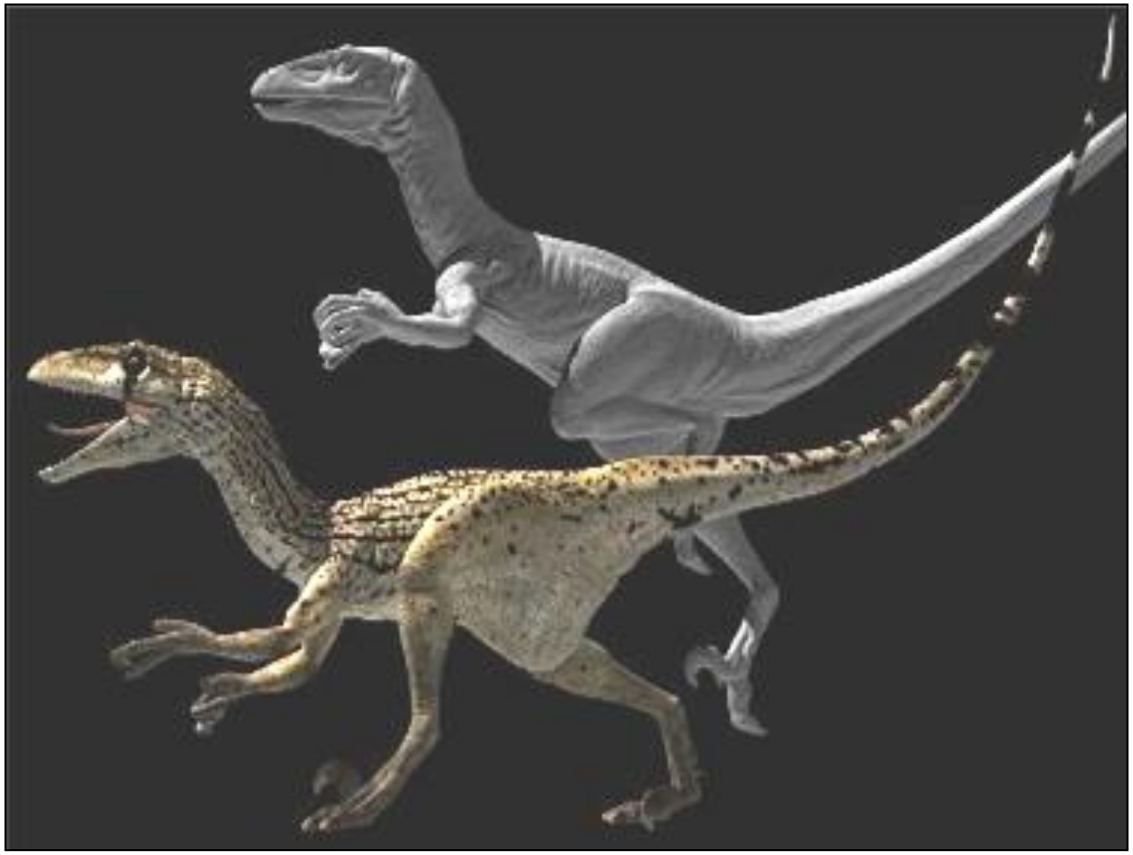
Polygonal model





Textures

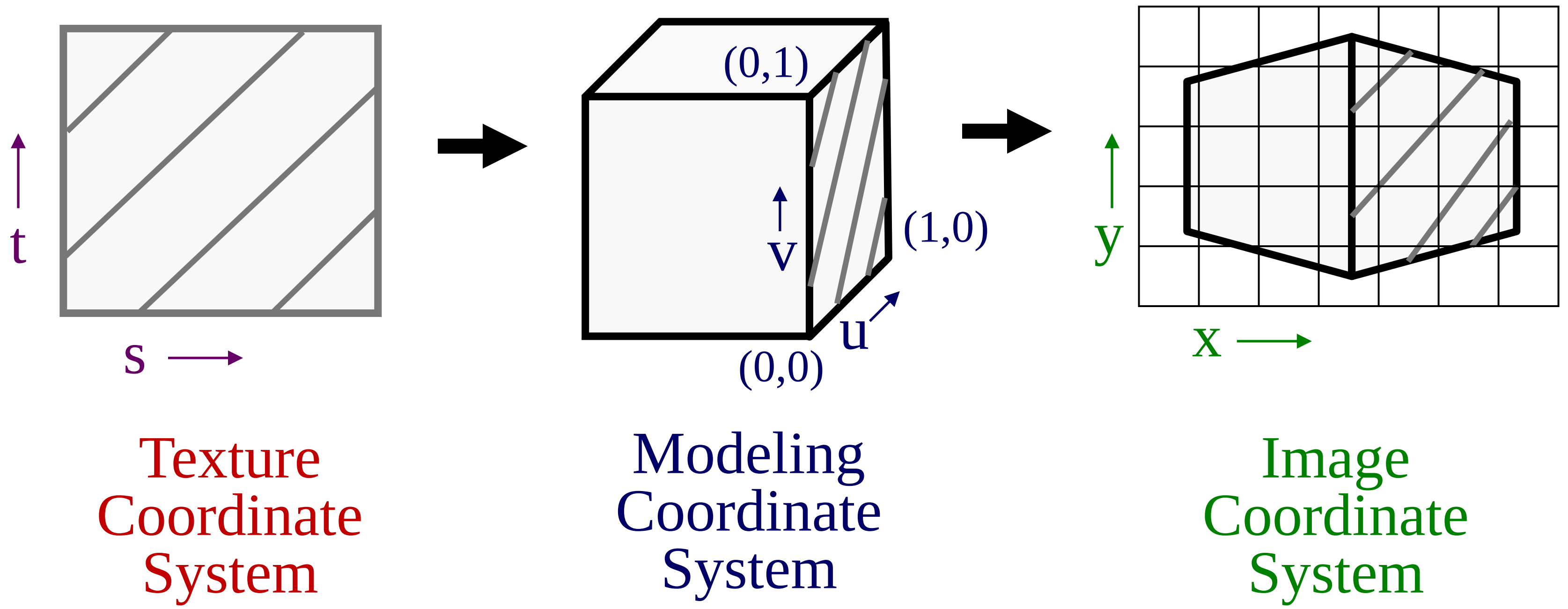
- Add visual detail to surfaces of 3D objects



[Daren Horley]

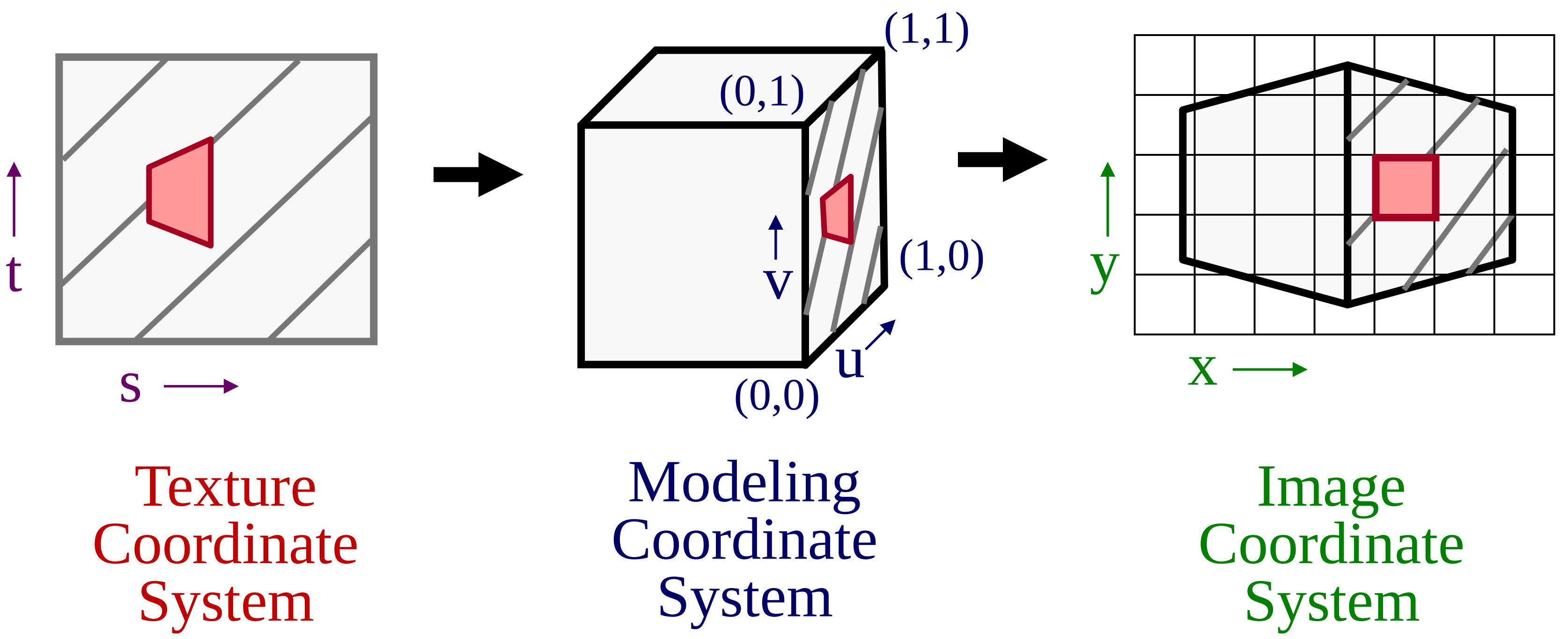
Texture Mapping

- Steps:
  1. Define texture
  2. Specify mapping from texture to surface
  3. Look up texture values during scan conversion



Texture Mapping

- When scan converting, map from …
  - image coordinate system (x,y) to
  - modeling coordinate system (u,v) to
  - texture image (s,t)



Texture Overview

- Texture mapping stages
  - Parameterization
  - Mapping
  - Filtering
- Texture mapping applications
  - Modulation textures
  - Illumination mapping
  - Bump mapping
  - Environment mapping
  - Image-based rendering
  - Non-photorealistic rendering

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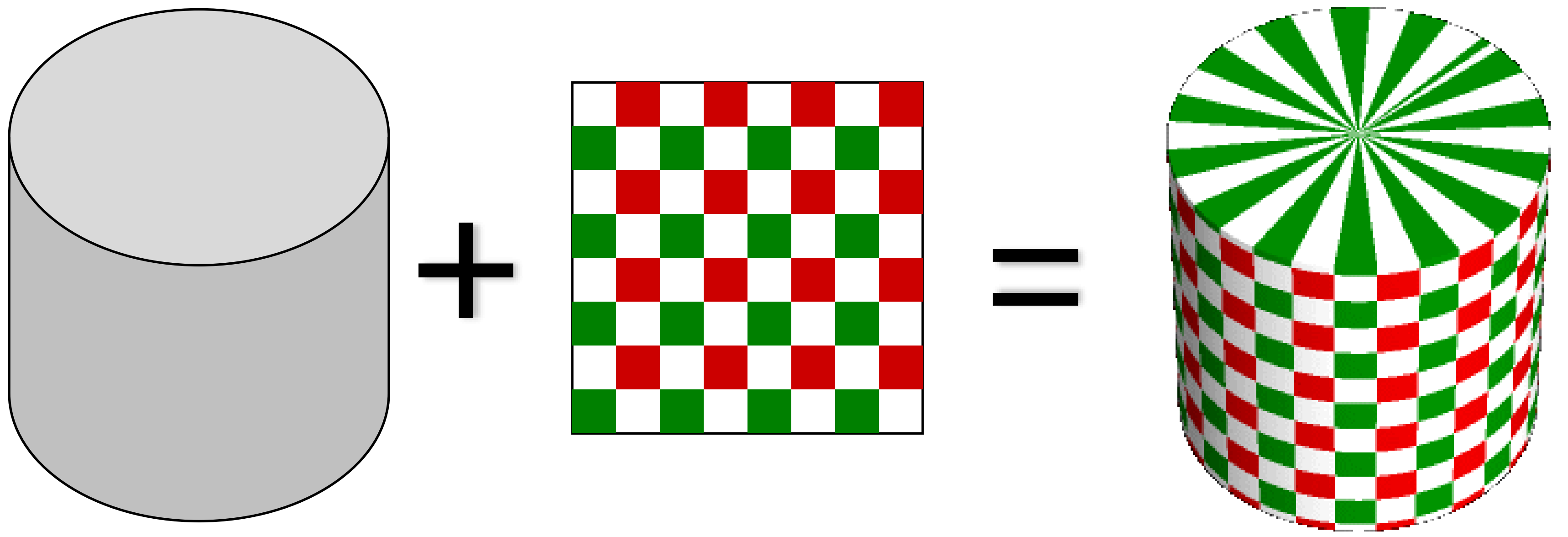
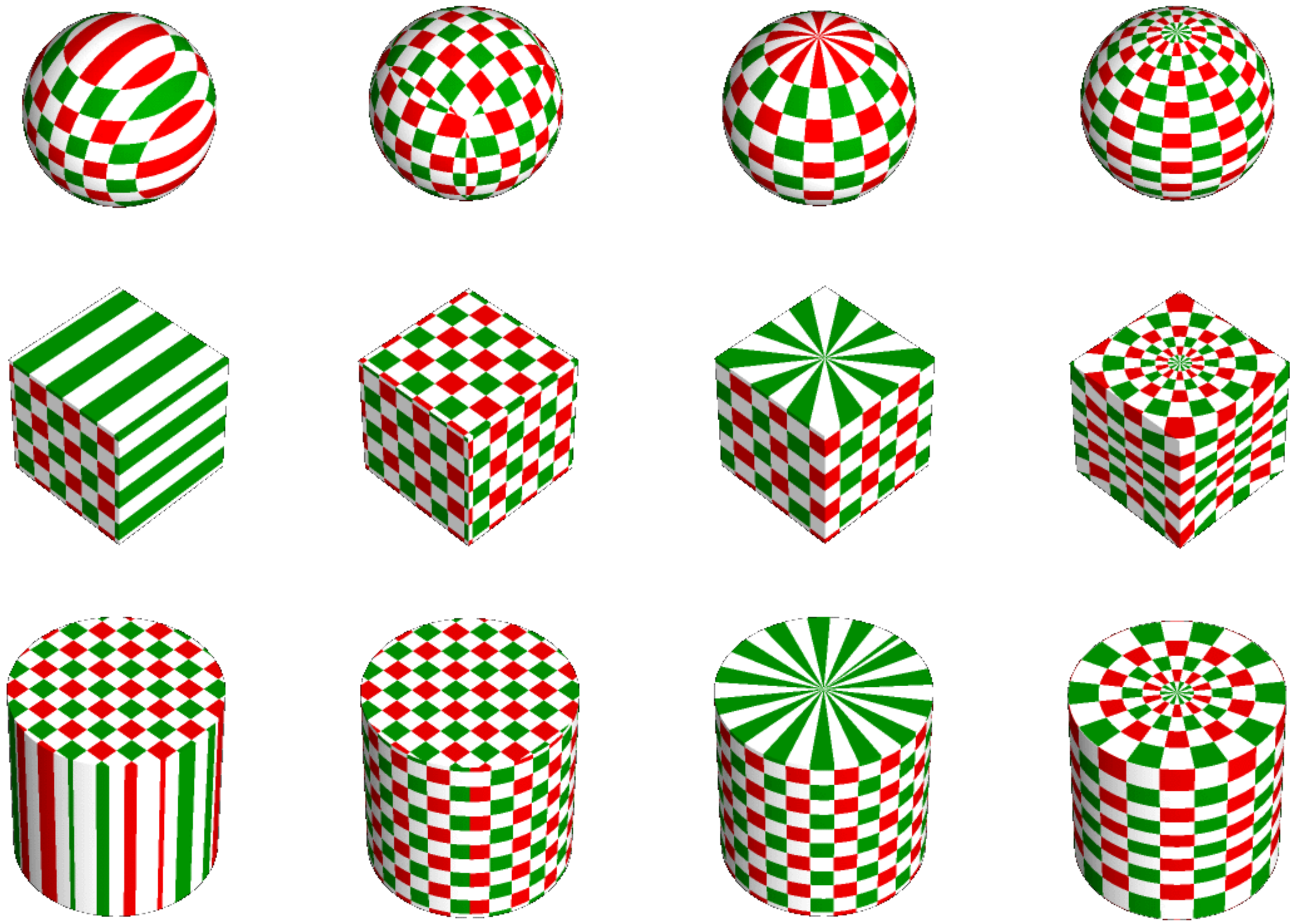
Texture Parameterization



- Q: How do we decide ***where* on the geometry** each color from the image should go?

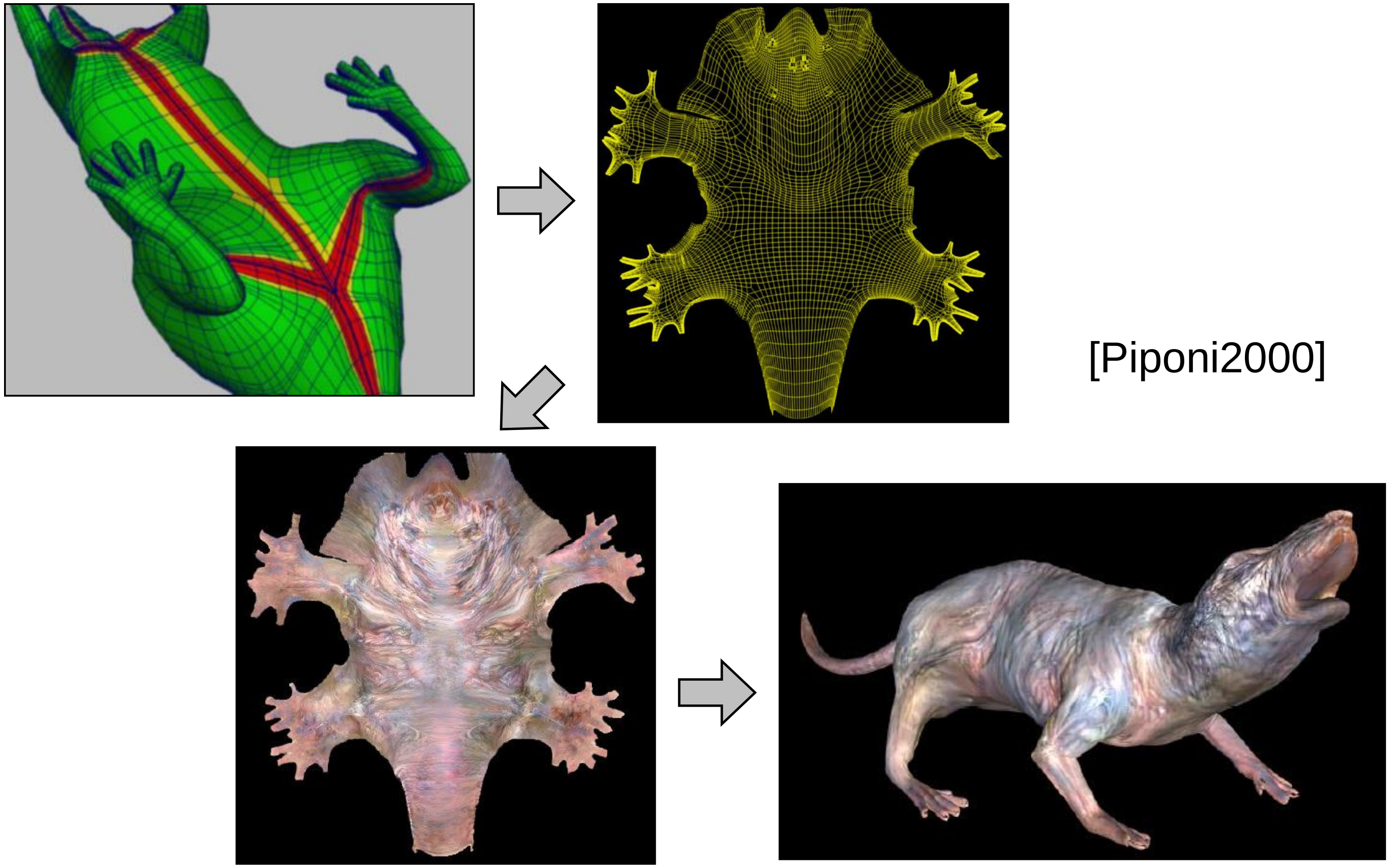
Texture Parameterization



[Paul Bourke]

Texture Parameterization

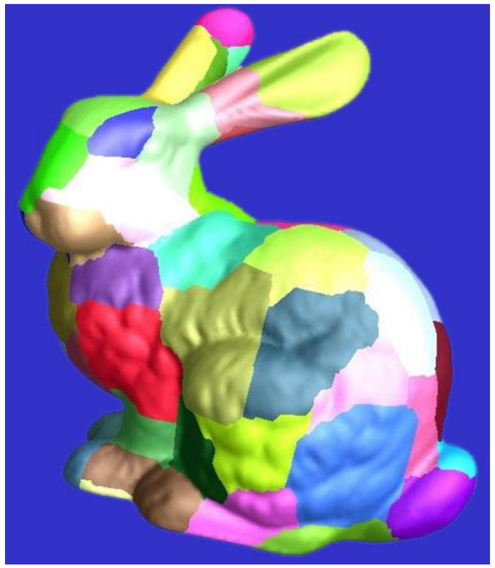
Option1: unfold the surface

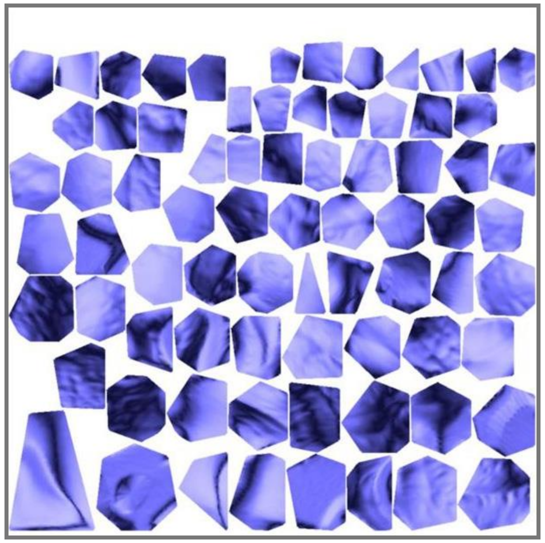


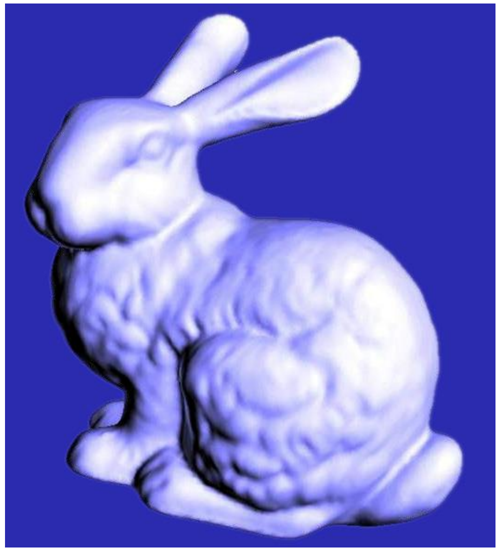
[Piponi2000]

Texture Parameterization

Option2: make an atlas


charts


atlas


surface

[Sander2001]

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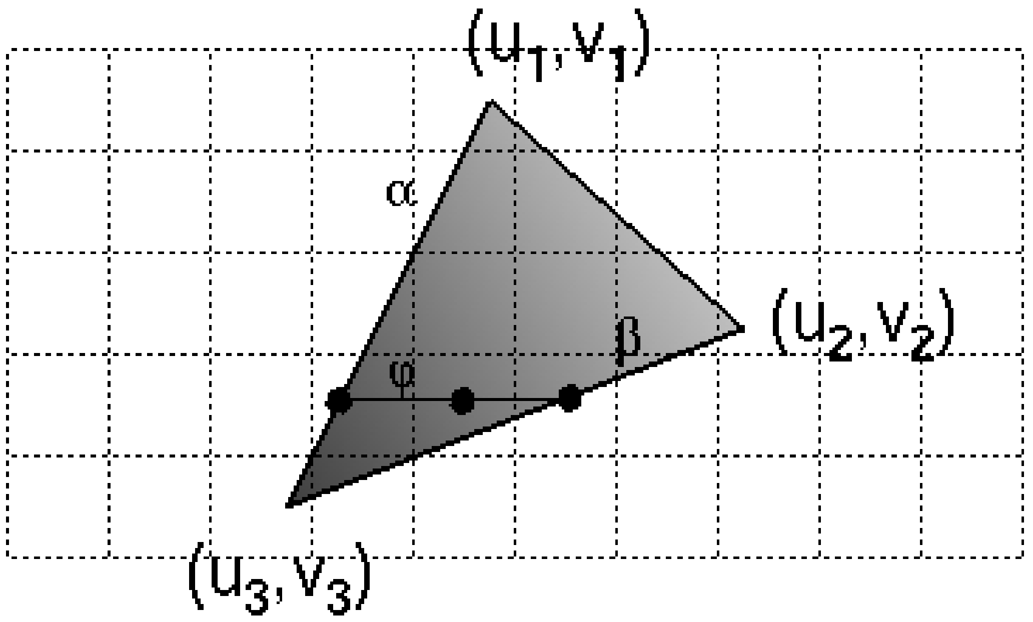
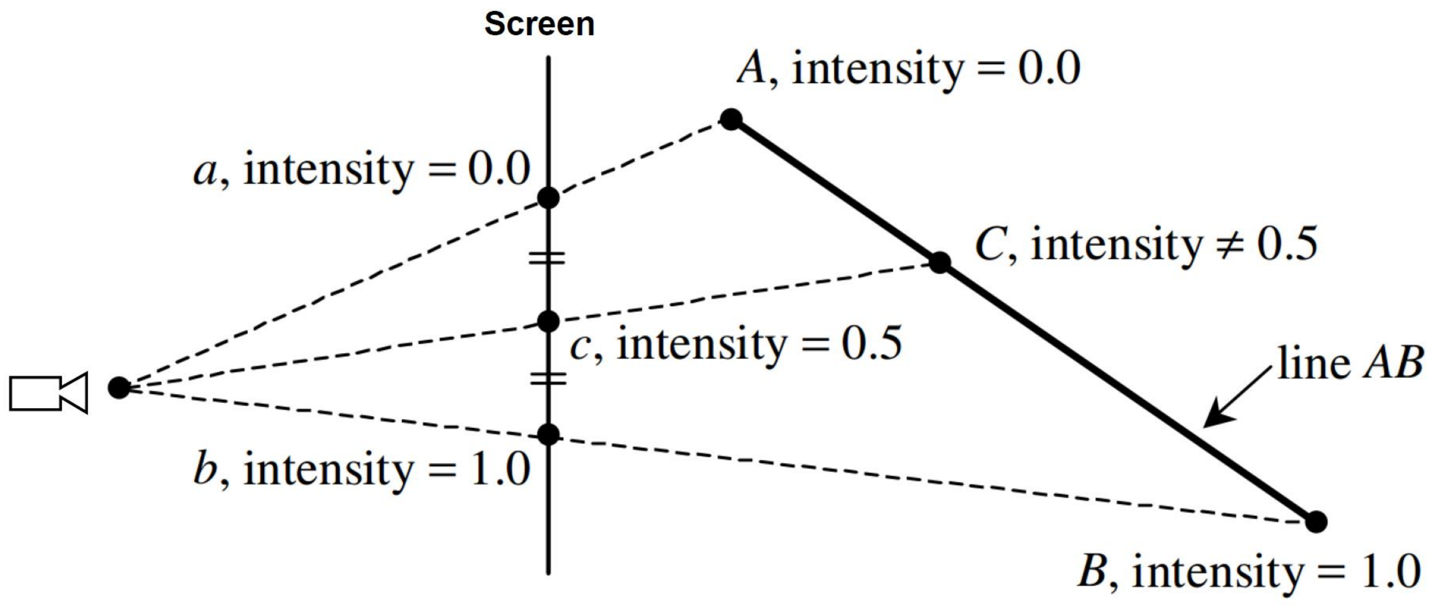
Texture Mapping

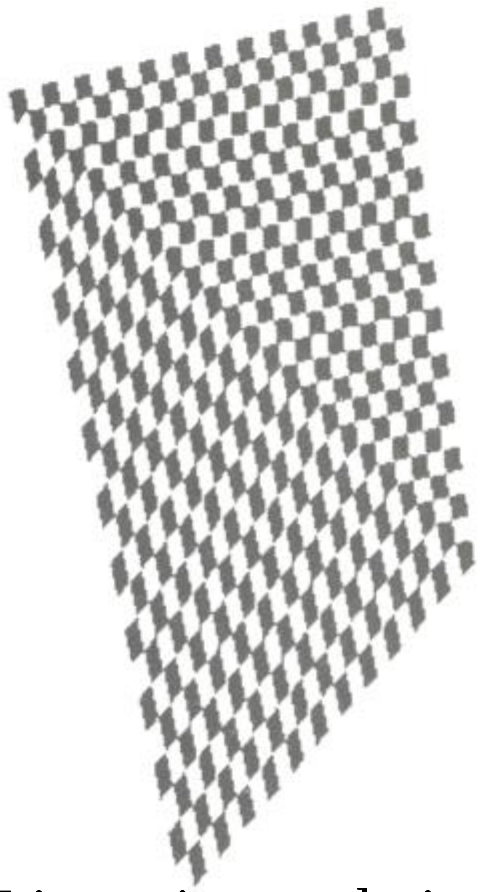
- Scan conversion
  - Interpolate texture coordinates down/across scan lines
  - Distortion due to bilinear interpolation approximation
    - » Cut polygons into smaller ones, or
    - » Perspective divide at each pixel

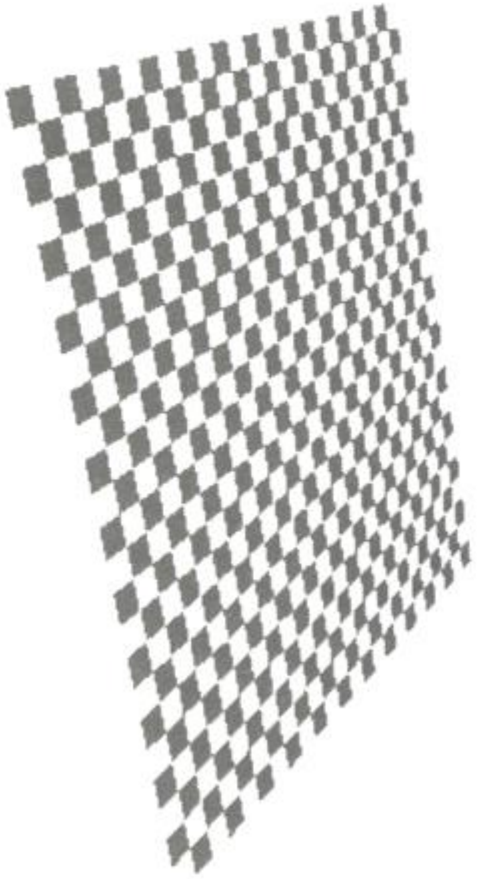


Perspective Divide



Perspective Divide


Linear interpolation
of texture coordinates


Correct interpolation
with perspective divide

Hill Figure 8.42

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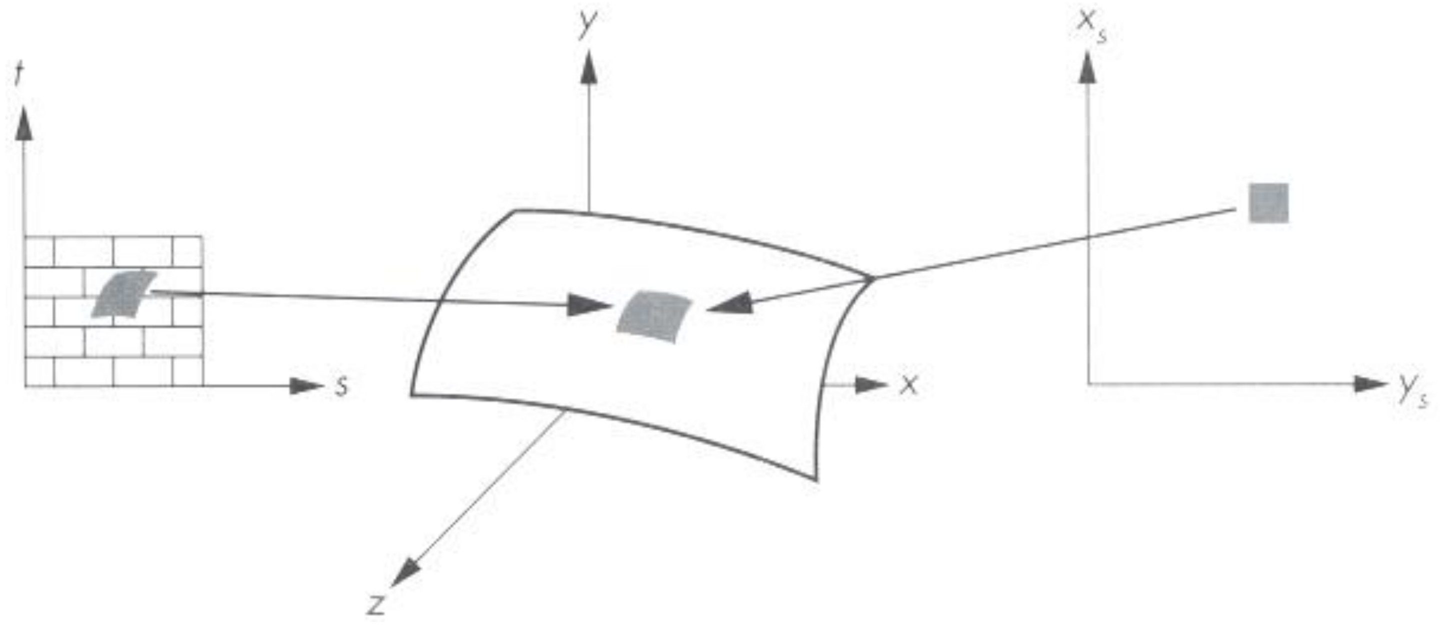
Texture Filtering

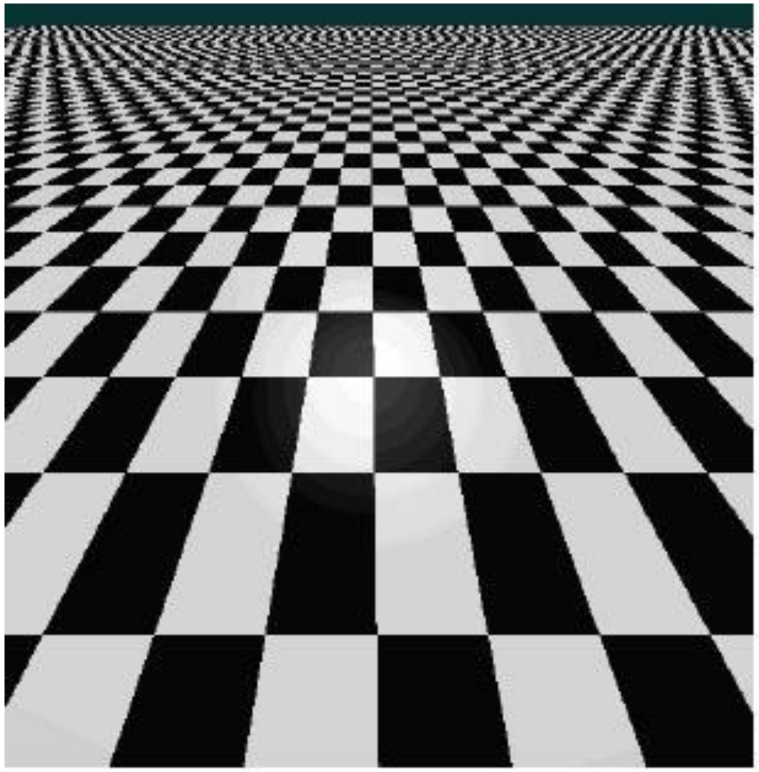
- Must sample texture to determine color at each pixel in image

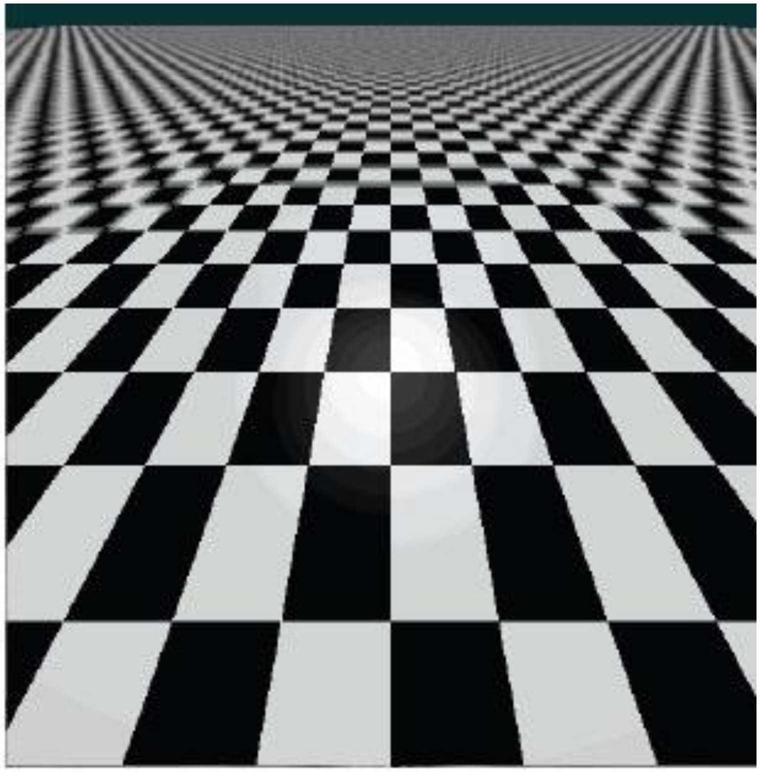


Angel Figure 9.4

Texture Filtering

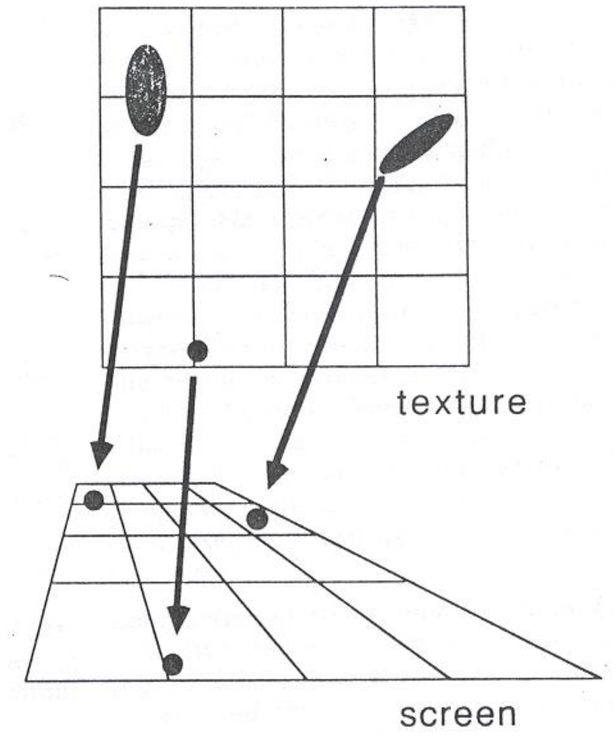
- Aliasing is a problem


Point sampling


Area filtering

Texture Filtering

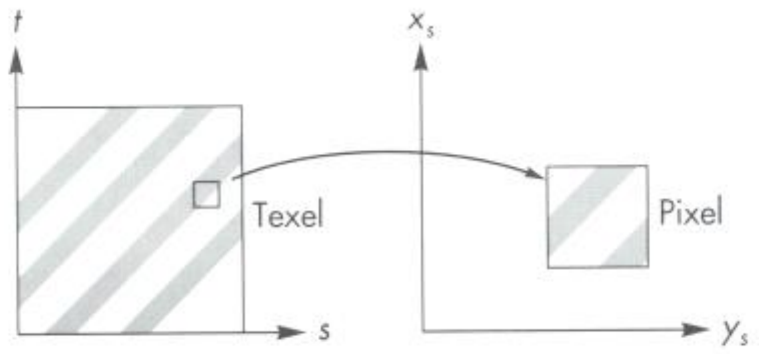
- Ideally, use elliptically shaped convolution filters



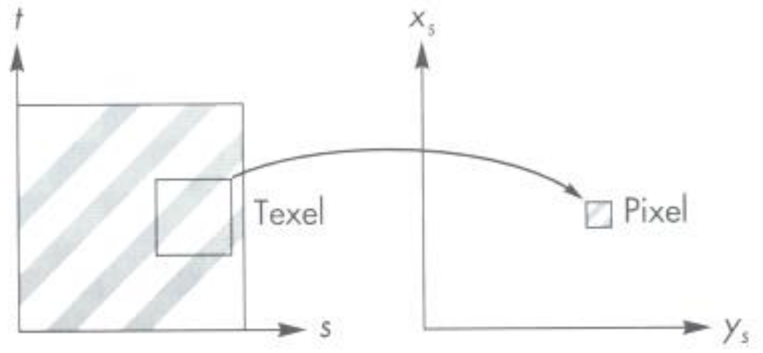
In practice, use rectangles or squares

Texture Filtering

- Size of filter depends on projective warp
  - Compute prefiltered images to avoid run-time cost
    - » Mipmaps
    - » Summed area tables



Magnification

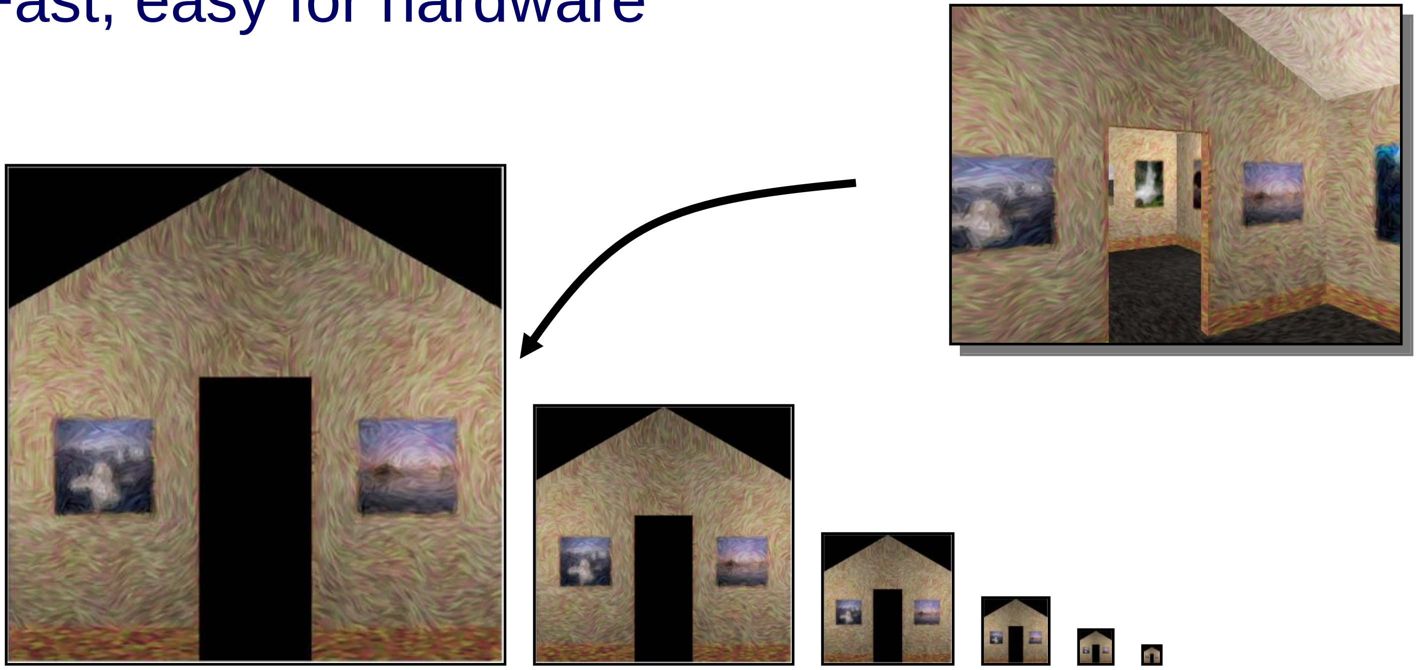


Minification

Angel Figure 9.14

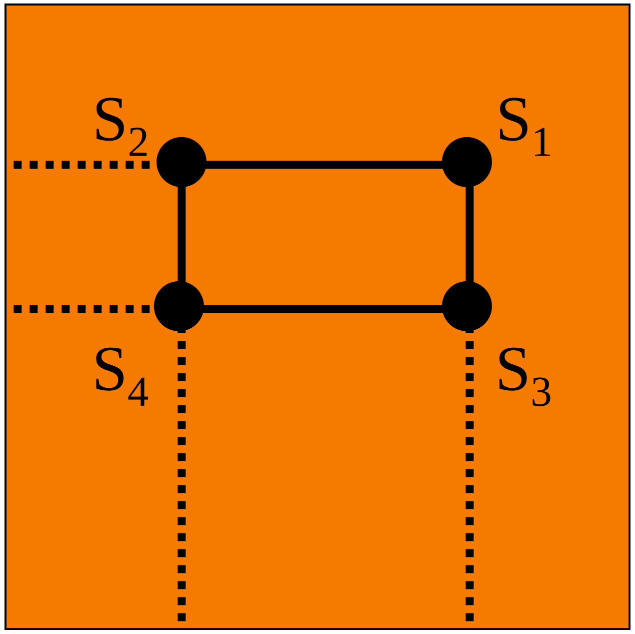
Mipmaps

- Keep textures prefiltered at multiple resolutions
  - Usually powers of 2
  - For each pixel, linearly interpolate between two closest levels (i.e., trilinear filtering)
  - Fast, easy for hardware



Summed-area tables

- At each texel keep sum of all values down & left
  - To compute sum of all values within a rectangle, simply combine four entries: $S_1 - S_2 - S_3 + S_4$
  - Better ability to capture oblique projections, but still not perfect



  - (Mipmaps are more common.)

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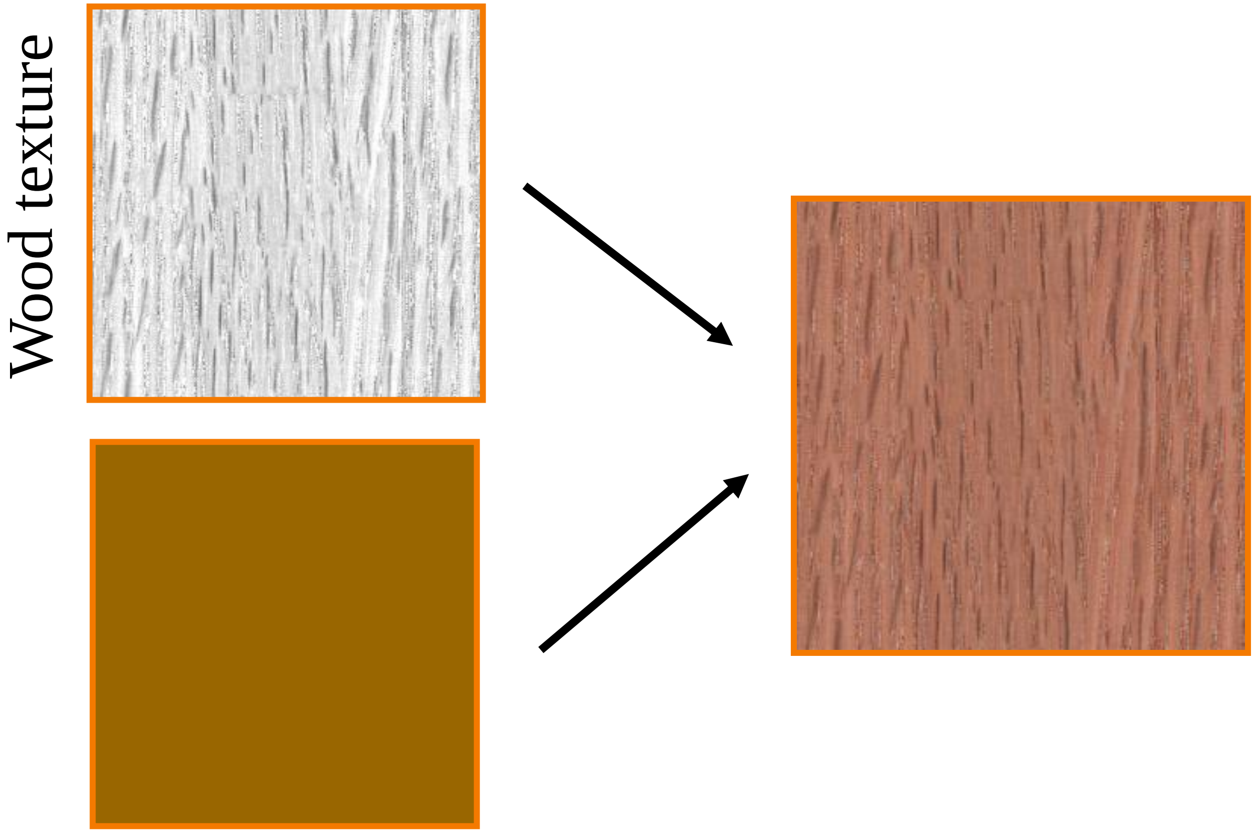
Modulation textures

Texture values scale result of lighting calculation



Texture value

$$\boxed{I = \underset{\big\uparrow}{T}(s,t)\left(I_E + K_A I_A + \sum_L \left(K_D (N \cdot L) + K_S (V \cdot R)^n\right) S_L I_L + K_T I_T + K_S I_S\right)}$$

Illumination Mapping

Map texture values to surface material parameter

- K_A
- K_D
- K_S
- K_T
- n

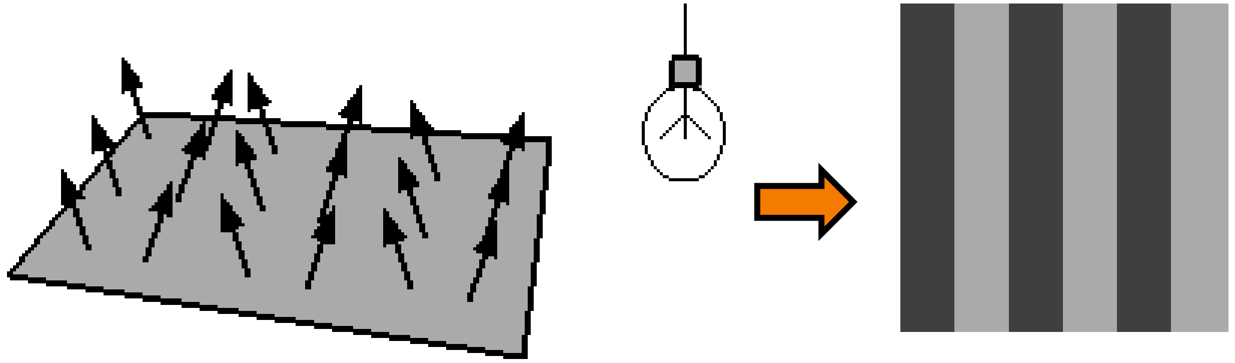
Texture value

$$I = I_E + K_A I_A + \sum_L \left(\underset{\uparrow}{K_D}(s,t)(N \cdot L) + K_S (V \cdot R)^n \right) S_L I_L + K_T I_T + K_S I_S$$

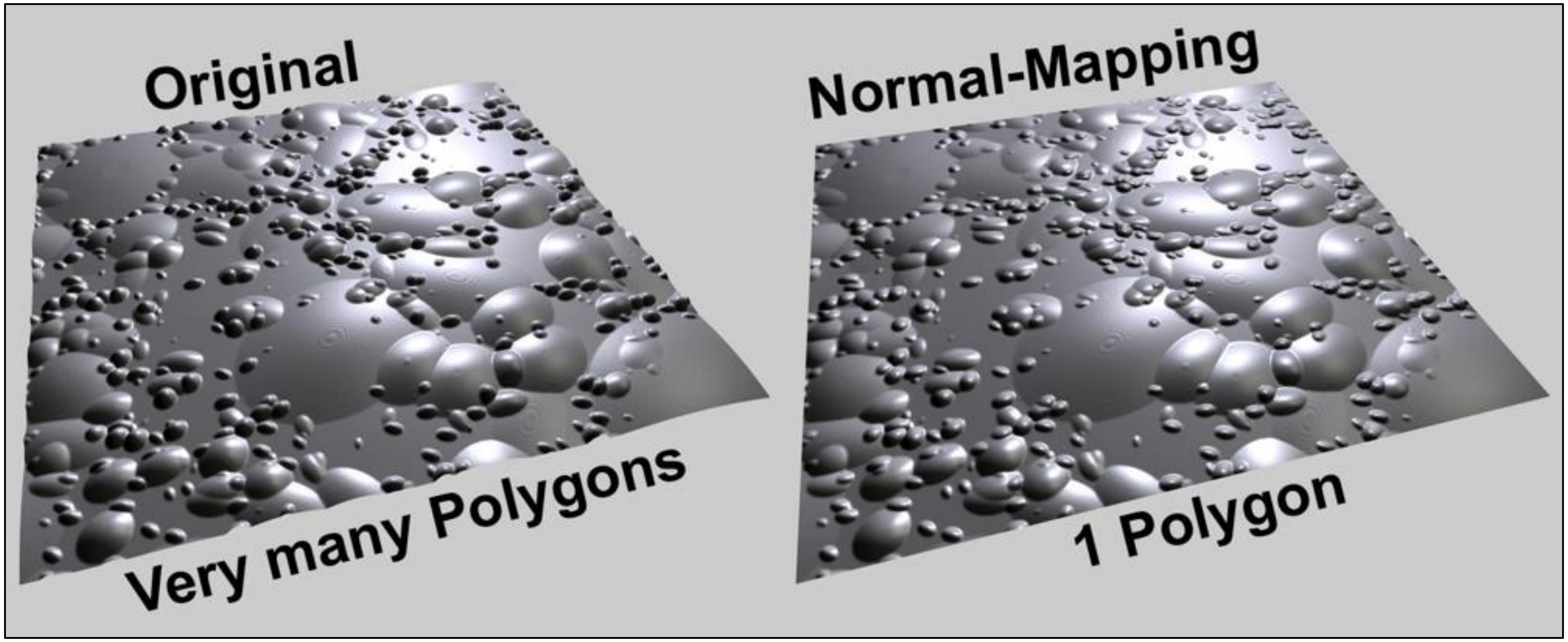
Bump/Normal Mapping

Texture values perturb surface normals:

- Encode normals (or offsets) in RGB
- Use gradient of grayscale image ("bump")



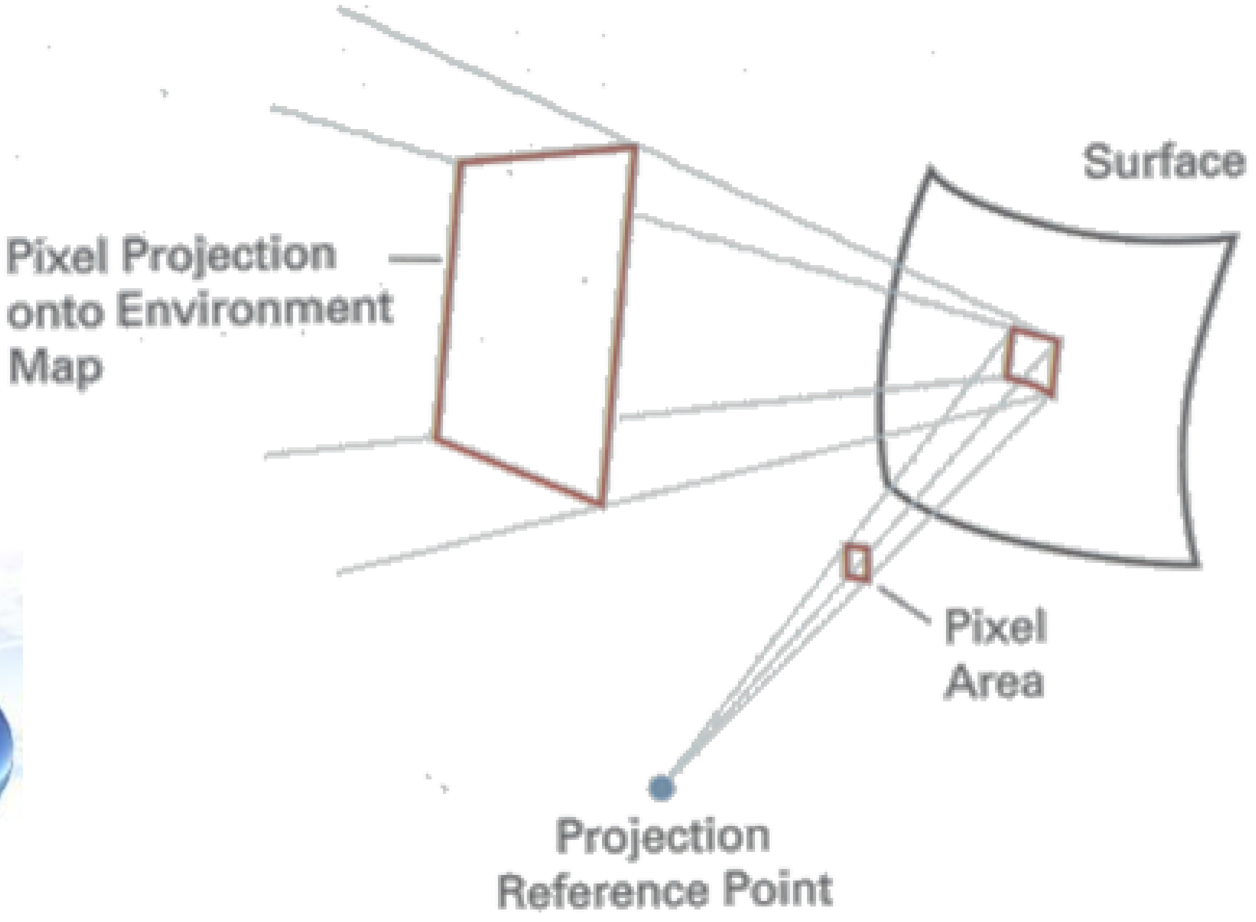
Normal Mapping



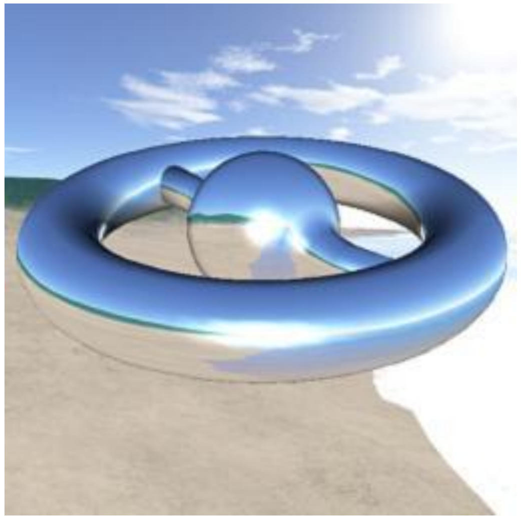
Graphisoft.com

Environment Mapping

Texture values are reflected off surface patch


Pixel Projection onto Environment Map
Surface
Pixel Area
Projection Reference Point

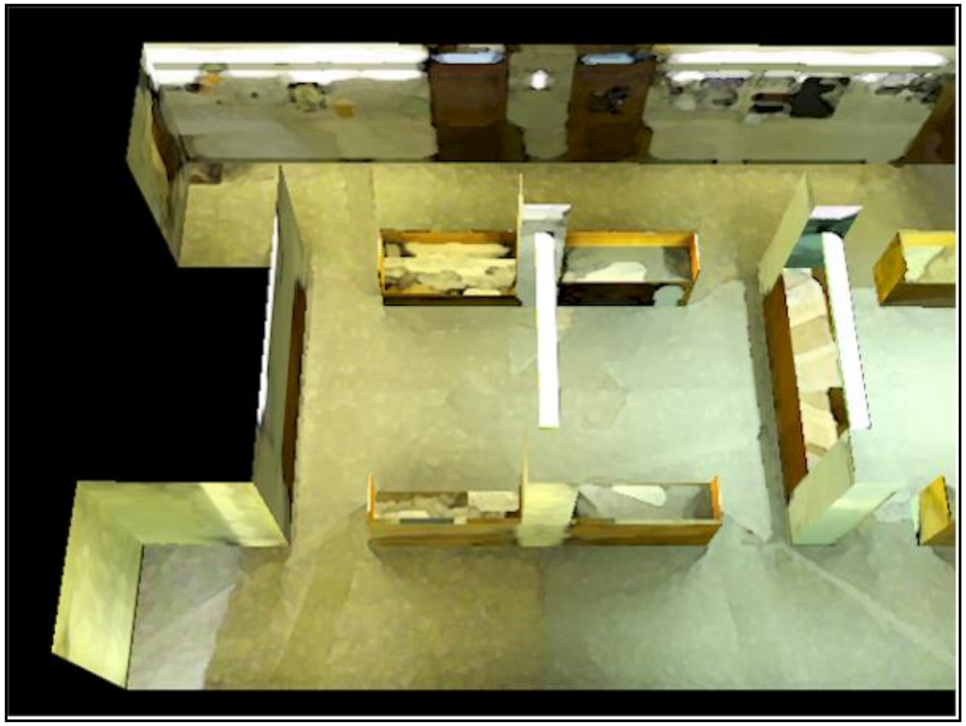
Gamer3D/Wikipedia



H&B Figure 14.93

Image-Based Rendering

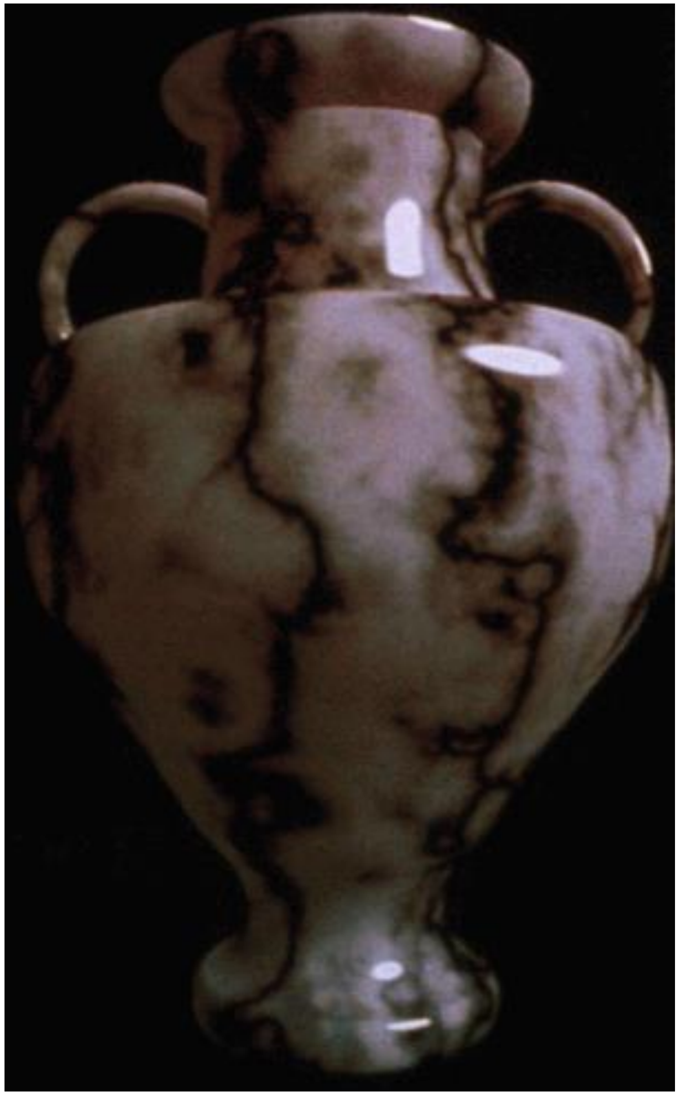
Map photographic textures to provide details for coarsely detailed polygonal model



Solid textures

Texture values indexed by 3D location (x,y,z)

- Expensive storage, or
- Compute on the fly, e.g. Perlin noise →



Texture Summary

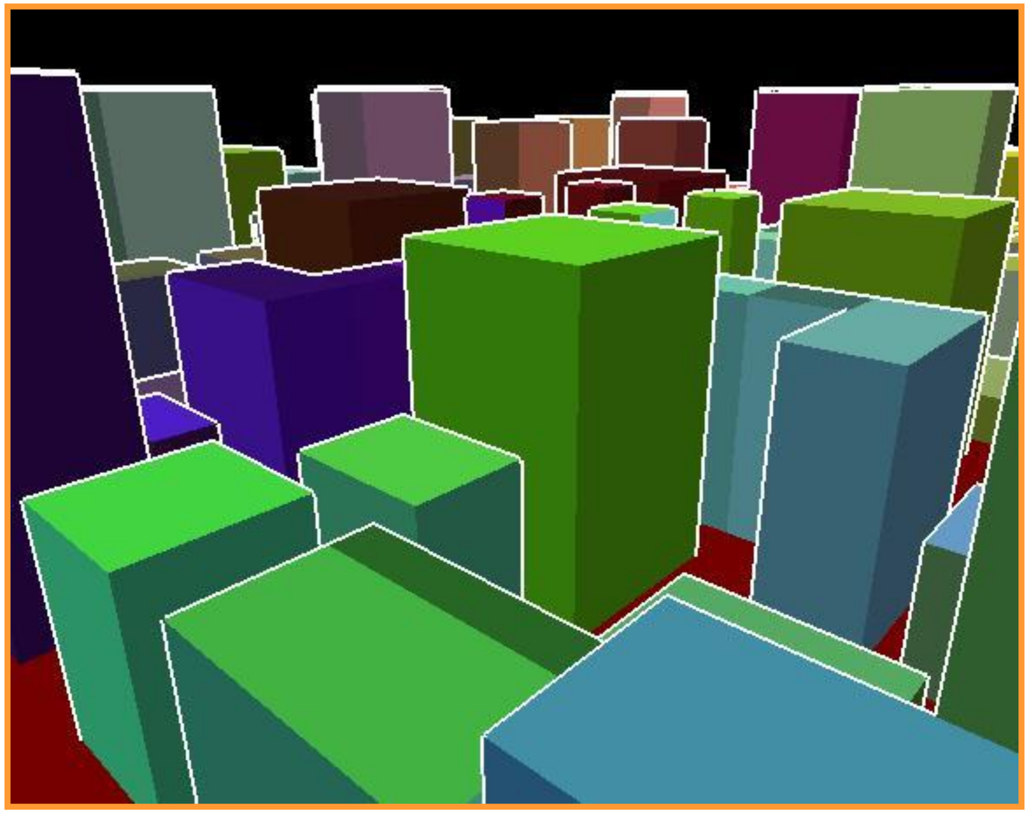
- Texture mapping stages
  - Parameterization
  - Mapping
  - Filtering
- Texture mapping applications
  - Modulation textures
  - Illumination mapping
  - Bump mapping
  - Environment mapping
  - Image-based rendering
  - Volume textures

Rasterization

- Scan conversion
  - Determine which pixels to fill
- Shading
  - Determine a color for each filled pixel
- Texture mapping
  - Describe shading variation within polygon interiors
- ➢ Visible surface determination
  - Figure out which surface is front-most at every pixel

Visible Surface Determination

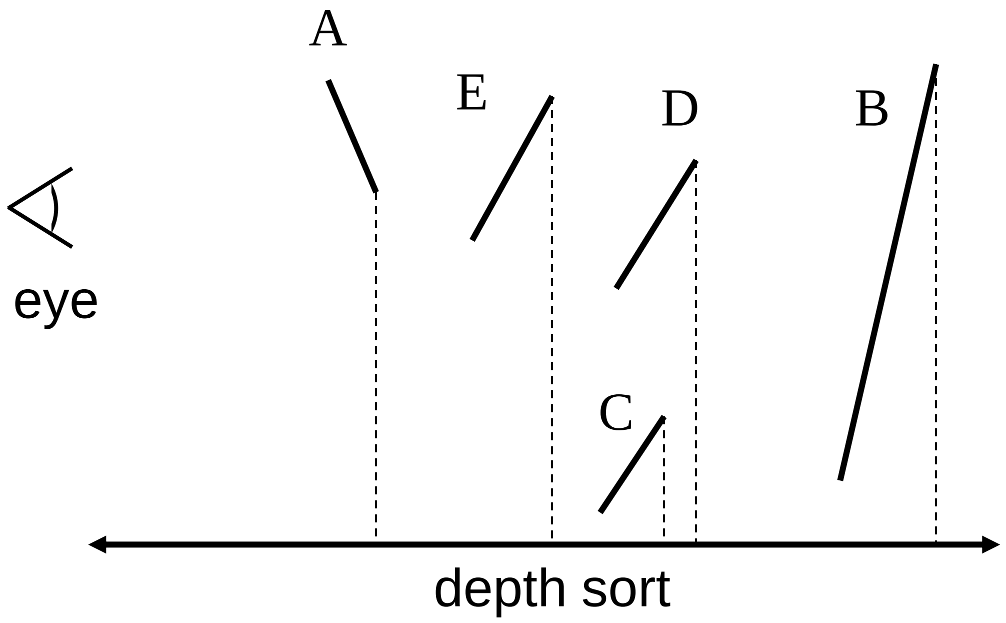
Make sure only front-most surface contributes to color at every pixel



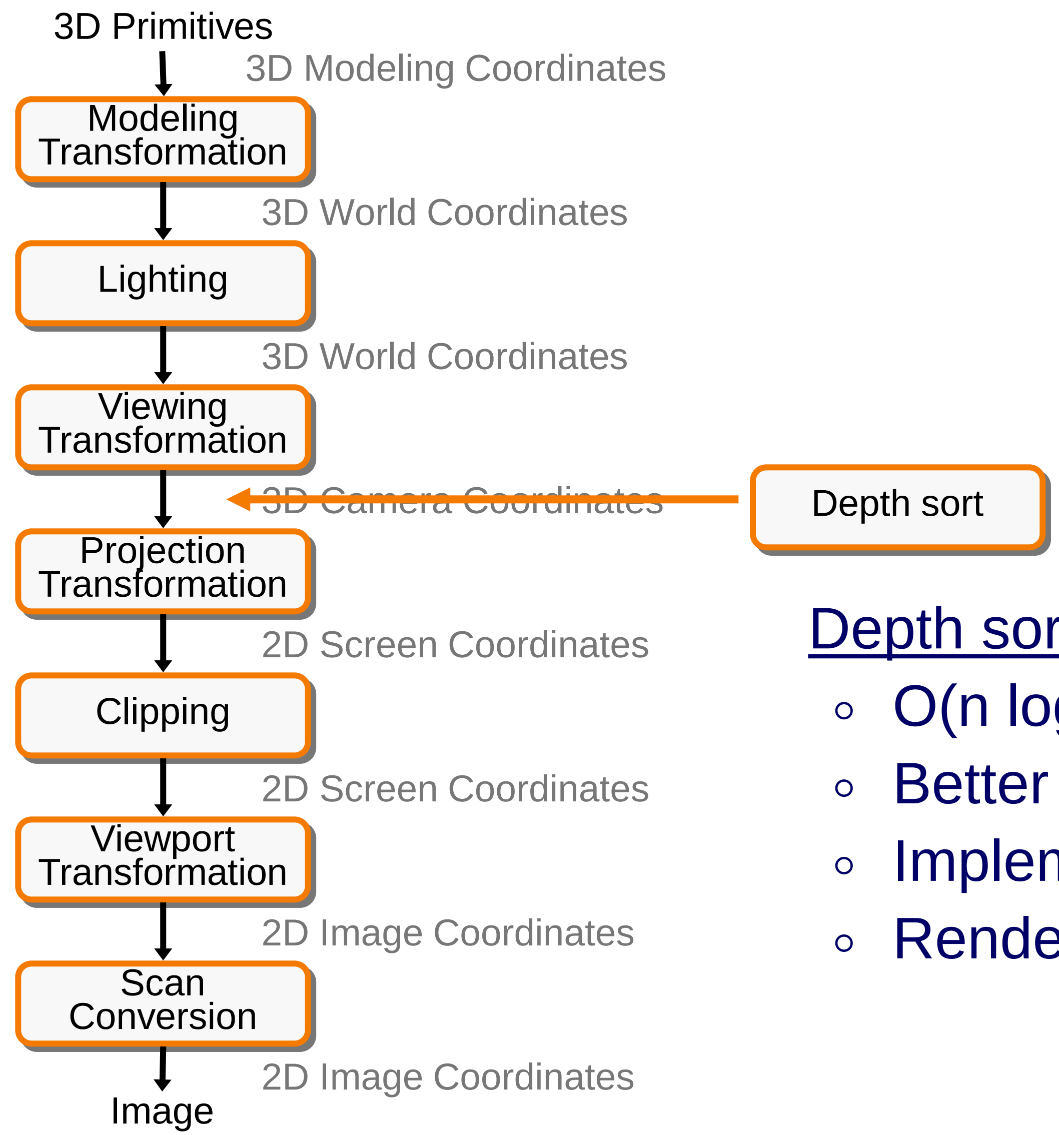
Depth sort

"Painter's algorithm"

1. First **sort surfaces** in order of decreasing maximum depth
2. Scan convert surfaces in back-to-front order, overwriting pixels



3D Rendering Pipeline



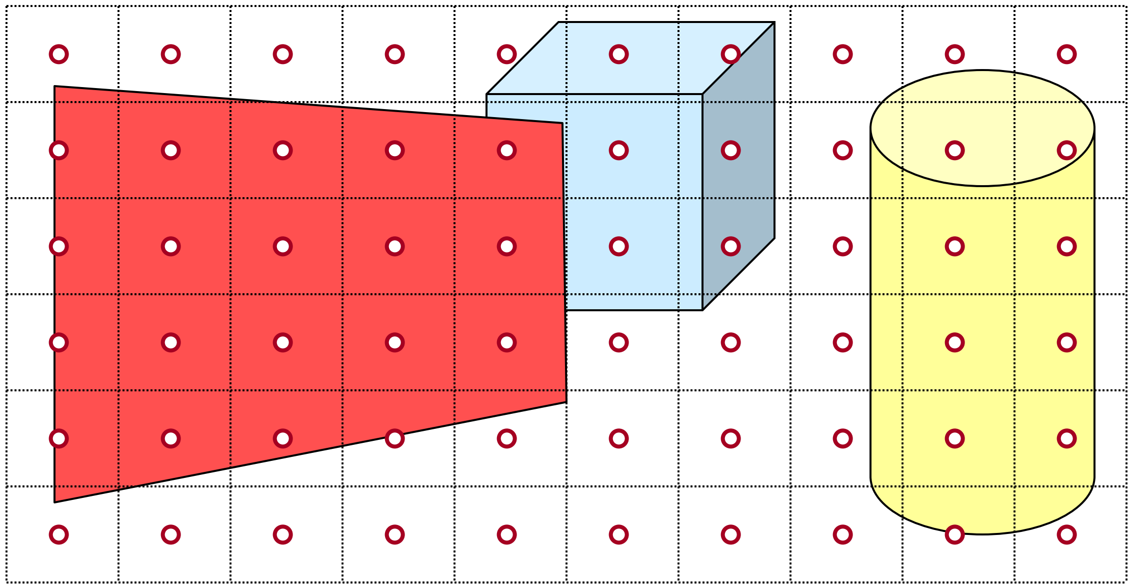
<u>Depth sort comments</u>

- O(n log n)
- Better with frame coherence?
- Implemented in software
- Render every polygon

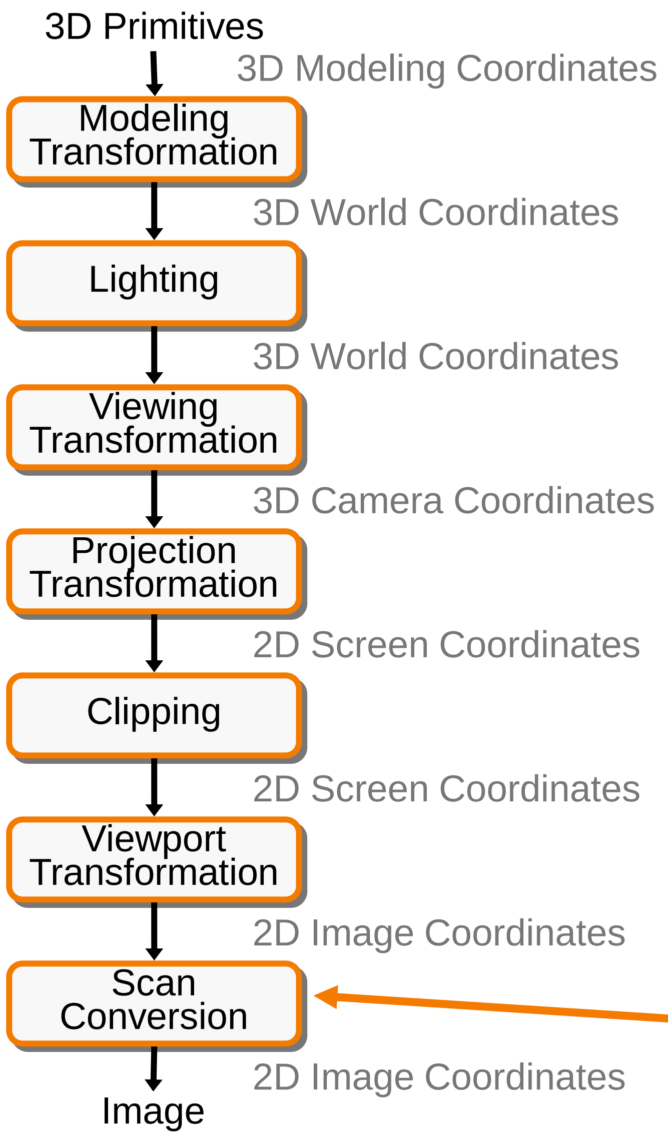
Z-Buffer

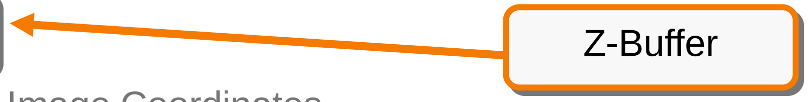
Maintain **color & depth of closest** object per pixel

- Framebuffer now RGBAz – initialize z to far plane
- Update only pixels with depth closer than in z-buffer
- Depths are interpolated for in-primitive pixels from vertices, just like colors



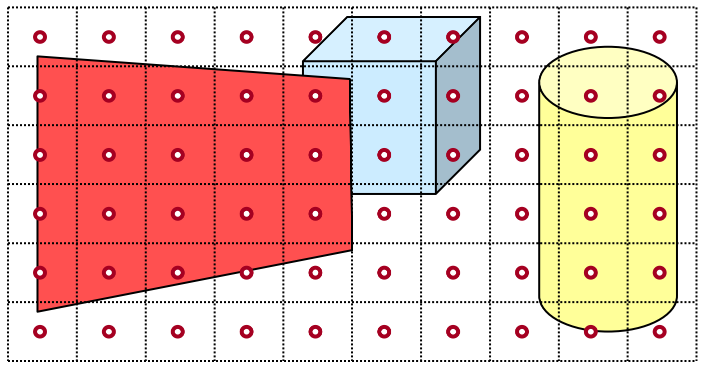
Z-Buffer



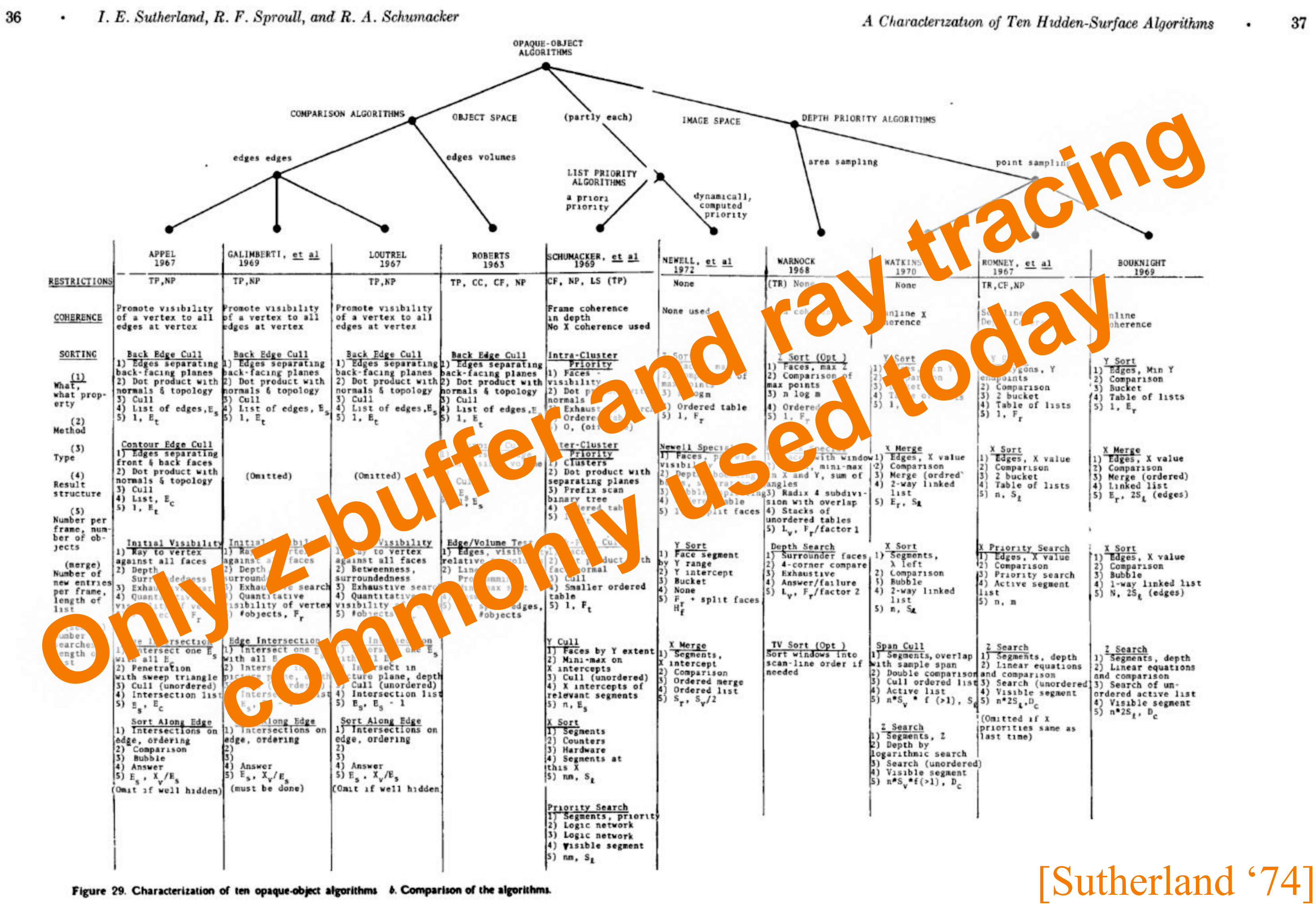


Z-buffer comments

+ Polygons rasterized in any order
+ Process one polygon at a time
+ Suitable for hardware pipeline
- Requires extra memory for z-buffer
◦ Commonly in hardware



Hidden Surface Removal Algorithms



36 • I. E. Sutherland, R. F. Sproull, and R. A. Schumacker
A Characterization of Ten Hidden-Surface Algorithms • 37
OPAQUE-OBJECT ALGORITHMS
COMPARISON ALGORITHMS
OBJECT SPACE
(partly each)
IMAGE SPACE
DEPTH PRIORITY ALGORITHMS
edges edges
edges volumes
LIST PRIORITY ALGORITHMS
a priori priority
dynamically computed priority
area sampling
point sampling
APPEL 1967
GALIMBERTI, et al 1969
LOUTREL 1967
ROBERTS 1963
SCHUMACKER, et al 1969
NEWELL, et al 1972
WARNOCK 1968
WATKINS 1970
ROMNEY, et al 1967
BOUKNIGHT 1969
RESTRICTIONS
COHERENCE
SORTING
Figure 29. Characterization of ten opaque-object algorithms b. Comparison of the algorithms.

Only z-buffer and ray tracing commonly used today

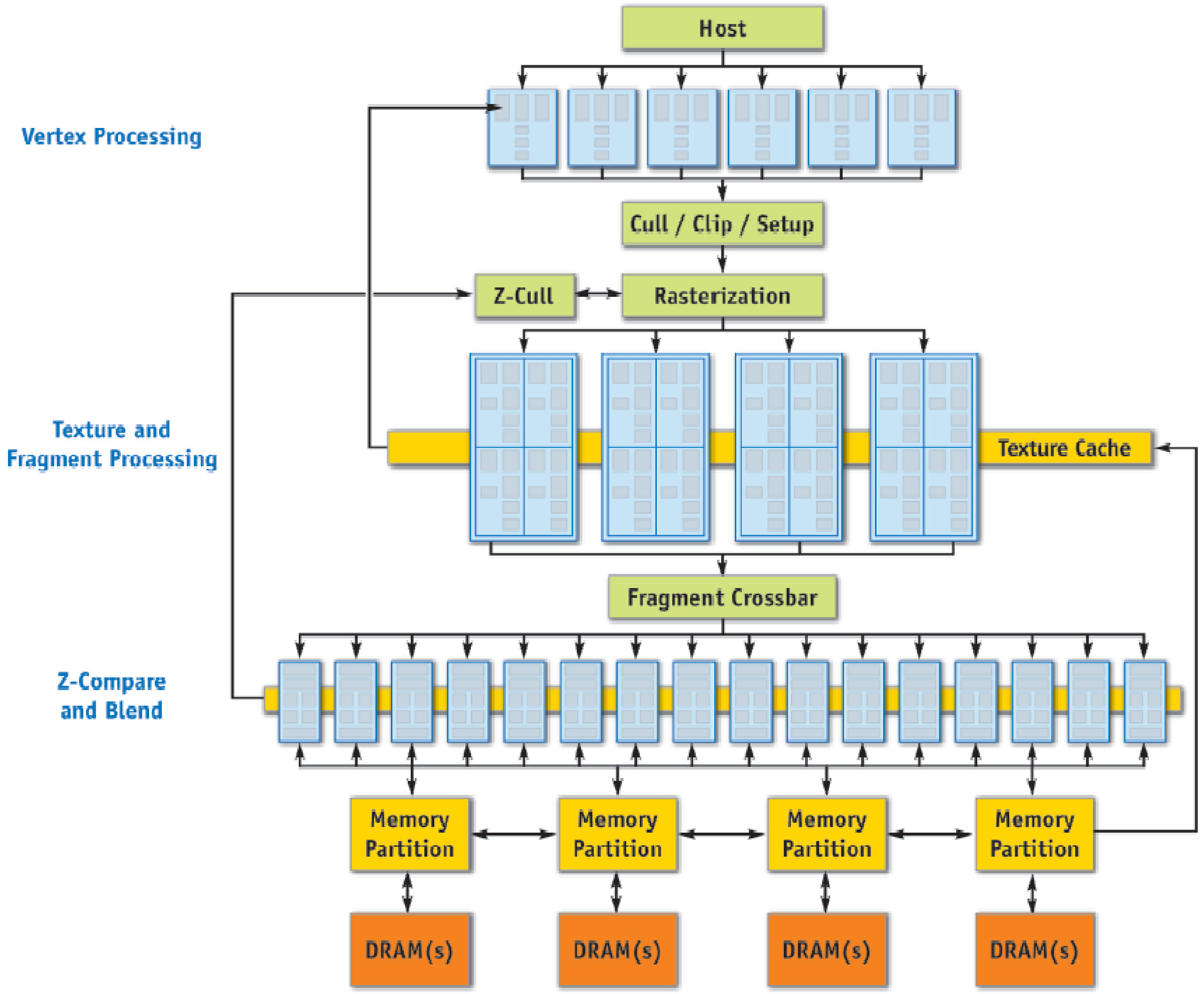
[Sutherland '74]

Rasterization Summary

- Scan conversion
  - Sweep-line algorithm
- Shading algorithms
  - Flat, Gouraud
- Texture mapping
  - Mipmaps
- Visibiliity determination
  - Z-buffer

This is all in hardware

GPU Architecture

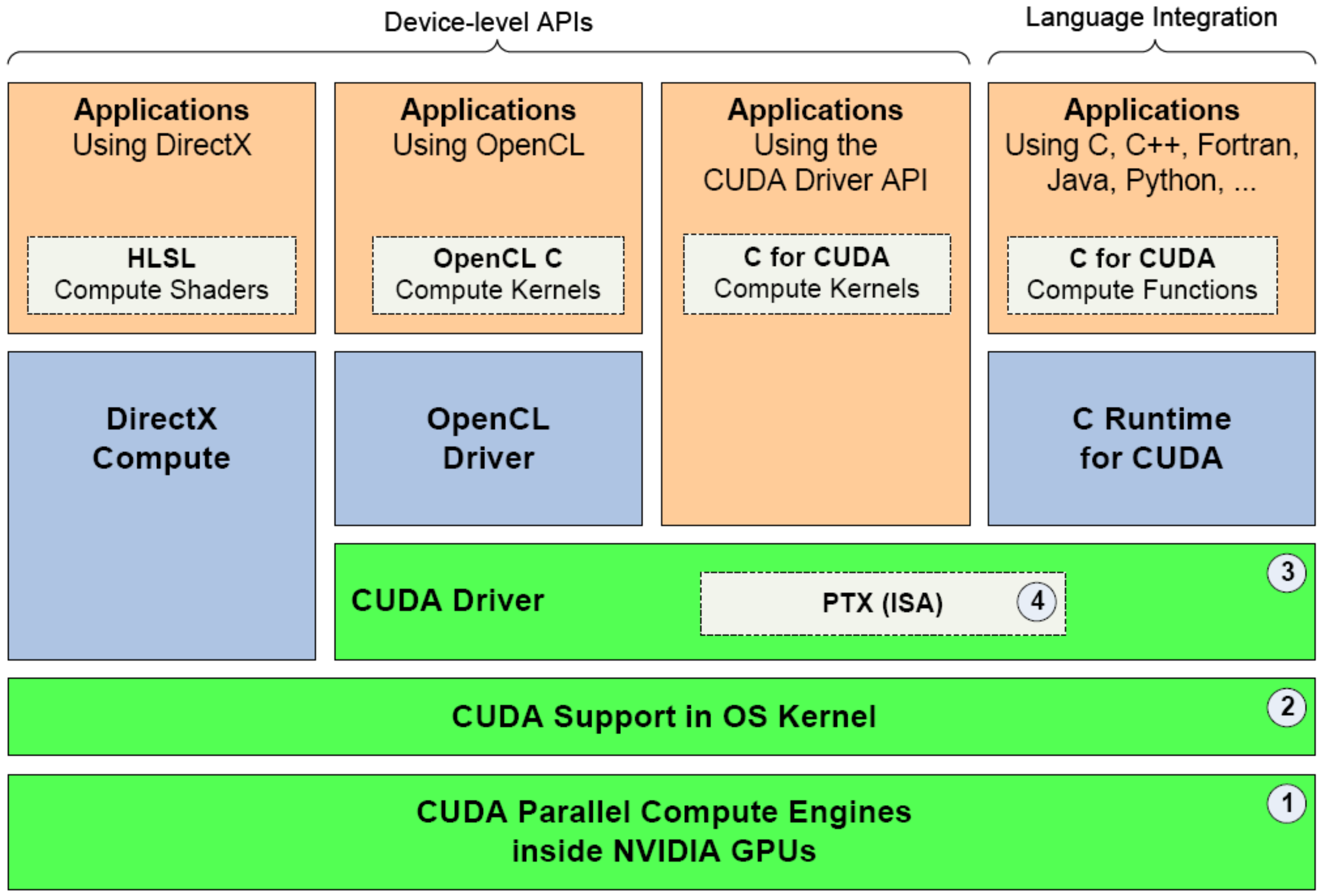


GeForce 6 Series Architecture

GPU Gems 2, NVIDIA

Actually …

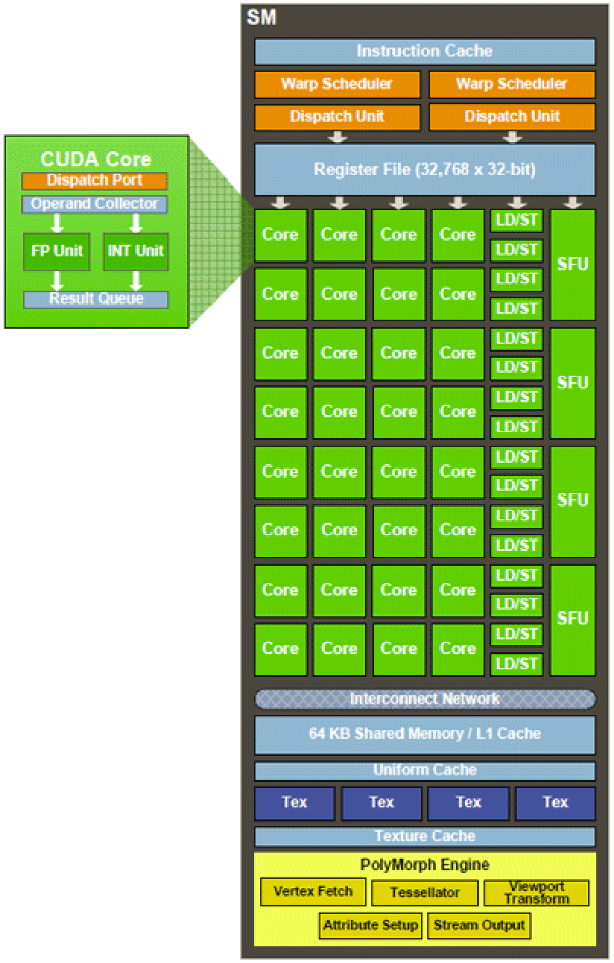
- Modern graphics hardware is programmable

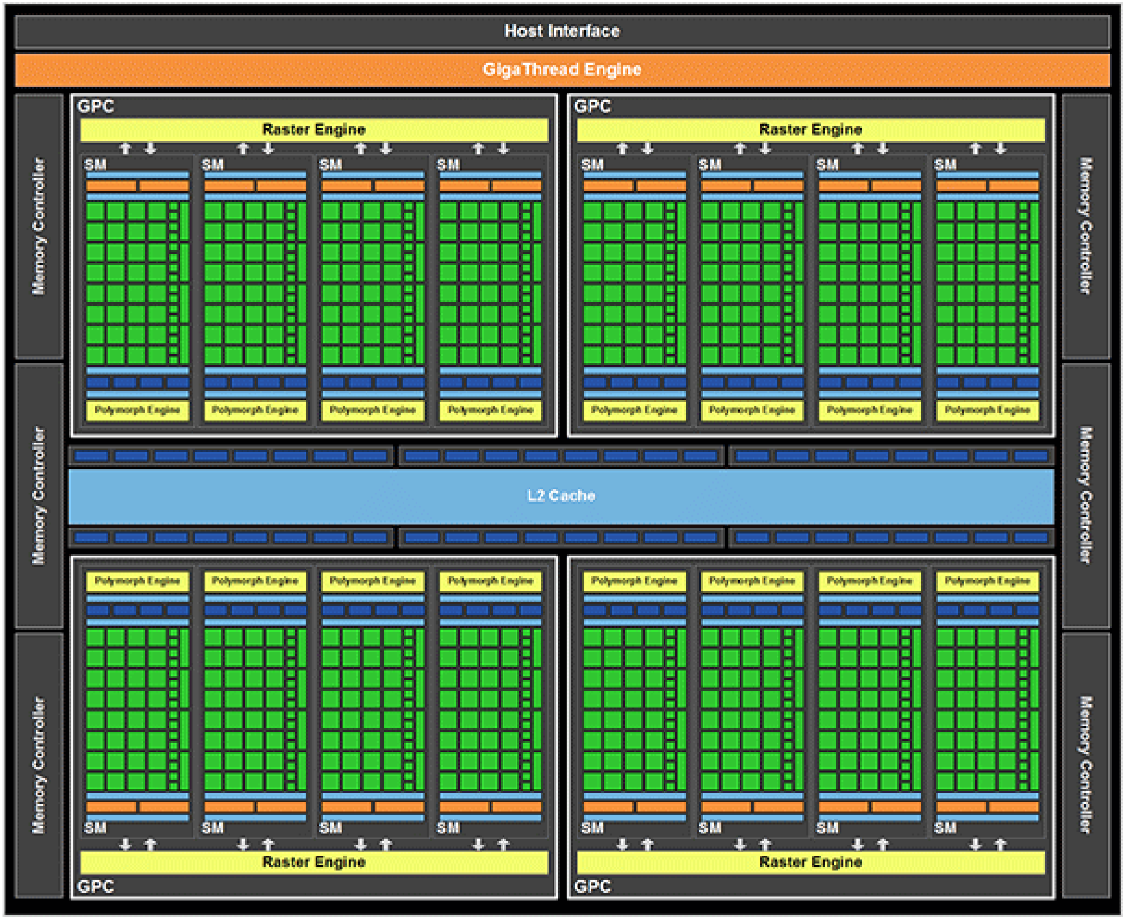

Device-level APIs
Language Integration
Applications Using DirectX
HLSL Compute Shaders
Applications Using OpenCL
OpenCL C Compute Kernels
Applications Using the CUDA Driver API
C for CUDA Compute Kernels
Applications Using C, C++, Fortran, Java, Python, ...
C for CUDA Compute Functions
DirectX Compute
OpenCL Driver
C Runtime for CUDA
CUDA Driver
PTX (ISA)
4
3
CUDA Support in OS Kernel
2
CUDA Parallel Compute Engines inside NVIDIA GPUs
1

www.nvidia.com/cuda

Trend …

- GPU is general-purpose parallel computer





www.nvidia.com/cuda