

Introducing Assignment 1: Image Processing

COS 426: Computer Graphics (Spring 2020)

Setup

Same as in A0:

- Run `python3 -m http.server` (or similar) inside the assignment directory
- Open `http://localhost:8000` in web browser

GUI

COS426 Assignment 1

Image Processing — Interactive Mode

Switch to: [Writeup](#)

Student Name <NetID>



Push Image

Batch Mode

Animation

MorphLines

▸ SetPixels

▾ Luminance

Brightness

Contrast

Gamma

Vignette

Histogram

▸ Color

▸ Filters

▸ Dithering

▸ Resampling

▸ Composite

▸ Misc

Close Controls

▾ History

▾ 1: Push Image

image name

Delete Below

▾ 2: Brightness

brightness

Delete

Close Controls

GUI

- Useful functions
 - Push Image
 - Animation: generate gif animation using (min, step, max)
 - MorphLines: specify line correspondences for morphing
 - BatchMode: fix current parameter settings

GUI

- Features to implement
 - SetPixels: set pixels to certain colors (This was A0)
 - Luminance: change pixel luminance
 - Color: remap pixel colors
 - Filter: convolution/box filter
 - Dithering: reduce visual artifacts due to quantization \approx cheat our eyes
 - Resampling: interpolate pixel colors
 - Composite: blending two images
 - Misc

Features

Luminance

- Brightness
- Contrast
- Gamma
- Vignette
- Histogram equalization

Color

- Grayscale
- Saturation
- White balance
- Histogram matching

Filter

- Gaussian
- Sharpen
- Edge detect
- Median
- Bilateral filter

Dithering

- Quantization
- Random dithering
- Floyd-Steinberg error diffusion
- Ordered dithering

Resampling

- Bilinear sampling
- Gaussian sampling
- Translate
- Scale
- Rotate
- Swirl

Composite

- Composite
- Morph

Next week's precept
will focus specifically
on this topic

A few reminders...

- Don't try to exactly replicate example images.
- Choose parameters which give you best results.
- Have fun!

Changing Contrast

- GIMP formula (**use this!**)
 - $\text{value} = (\text{value} - 0.5) * (\tan ((\text{contrast} + 1) * \text{PI}/4)) + 0.5;$
 - "Difference above mid-value times contrast multiplier, plus mid-value"
- Notes:
 - When contrast=1, $\tan(\text{PI}/2)$ is infinite. Using Math.PI can avoid this issue.
 - Clamp pixel to $[0, 1]$ after computing the value.
 - Apply to each channel separately.



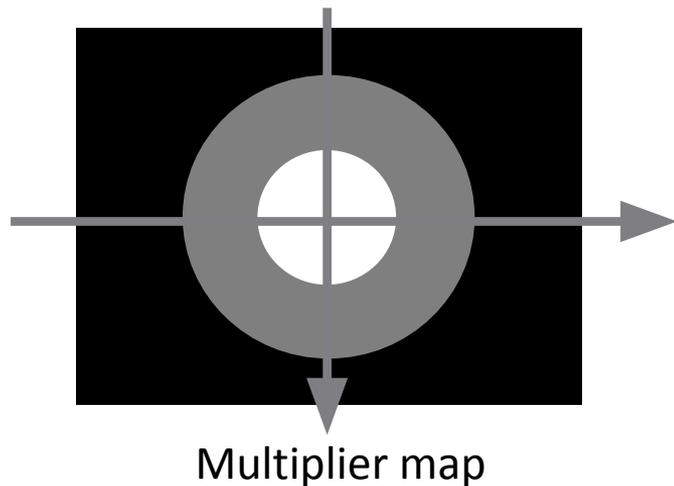
Gamma correction

- $R = R^{\text{gamma}}$
- $G = G^{\text{gamma}}$
- $B = B^{\text{gamma}}$
- R, G, B are typically in $[0, 1]$ (default in the code base)
- Second arg of `gammaFilter(image, logOfGamma)` is `log(gamma)`
 - So use `gamma = Math.exp(logOfGamma)`
- Exponentiation in JS is “`Math.pow(base, exponent)`” or (ES7 / ES2017+) “`base**pow`”
 - Your browser might not support ES7



Vignette

- Pixels within innerR remain unchanged
- Pixels outside outerR are black
- Pixels between innerR and outerR should be multiplied with a value in $[0, 1]$:
 - Multiplier = $1 - (R - \text{innerR}) / (\text{outerR} - \text{innerR})$
 - $R = \sqrt{x^2 + y^2} / \text{halfdiag}$
- Think about the soft brush



Histogram Equalization

Transform an image so that it has flat histogram of luminance values.



Before



After

Histogram Matching

Transform an image so that it has same histogram of luminance values as reference image.

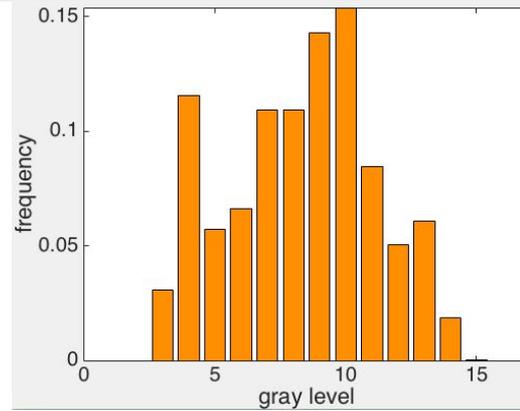


reference image: town

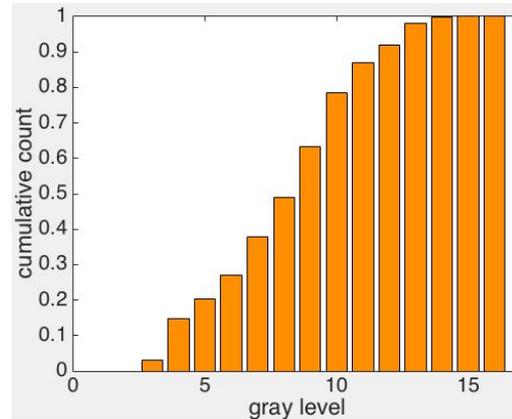


reference image: flower

Histogram Equalization/Matching



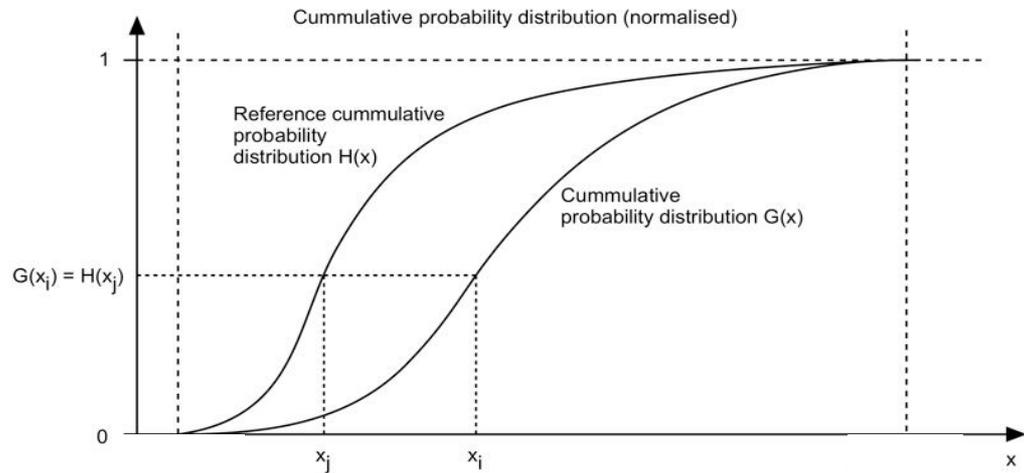
pdf



cdf

Histogram Equalization/Matching

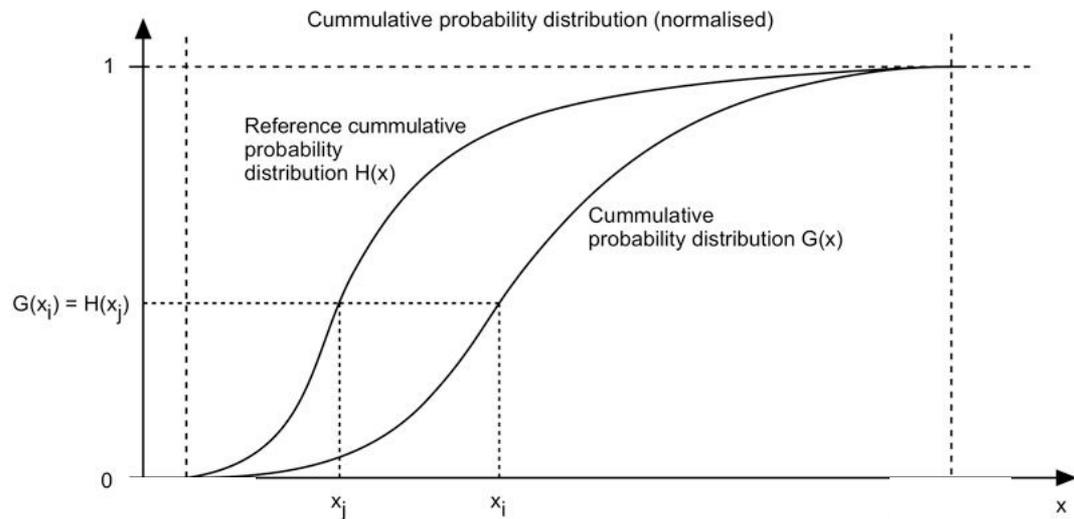
- Image: x
- Number of gray levels: L
- $pdf(i) = \frac{n_i}{n}$ n_i = number of pixels of the i -th gray level
- $cdf(j) = \sum_{i=0}^j pdf(i)$
- Target cdf:
 - Equalization:
 - $cdf_{ref}(i) = \frac{i}{L-1}$
 - Matching:
 - cdf of the reference image



(source:http://paulbourke.net/texture_colour/equalisation/)

Histogram Equalization/Matching

- Target cdf:
 - Equalization:
 - $cdf_{ref}(i) = \frac{i}{L-1}$
 - Matching:
 - cdf of the reference image
- Implementation
 - Equalization
 - $x' = (cdf(x) * (L - 1)) / (L - 1)$
 - Matching
 - $x' = \underset{i}{\operatorname{argmin}} |cdf(x) - cdf_{ref}(i)|$
 - Convert back to gray level: $x' = \frac{x'}{L-1}$



Saturation

- $\text{pixel} = \text{pixel} + (\text{pixel} - \text{gray}(\text{pixel})) * \text{ratio}$
- Do clamp()



White balance

`whitebalance(image, rgb_w)`

$[L_w, M_w, S_w] = \text{rgb2lms}(rgb_w)$

for each pixel x in image

$[L, M, S] = \text{rgb2lms}(\text{image}(x))$

$L = L / L_w$

$M = M / M_w$

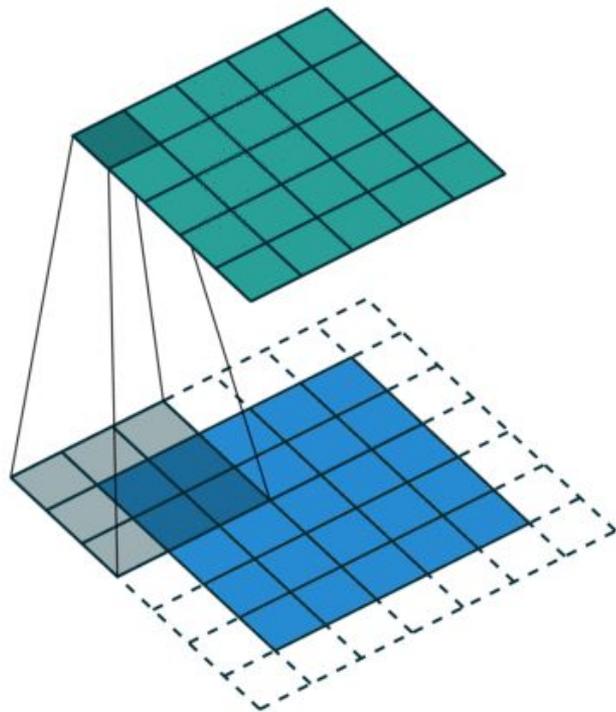
$S = S / S_w$

`image_out(x) = lms2rgb(L, M, S)`

- Hints:
 - Use `rgbToXyz()`, `xyzToLms()`, `lmsToXyz()`, `xyzToRgb()`
 - Do `clamp()`

Convolution (Gaussian/Sharpen/Edge)

w1 w2 w3
w4 w5 w6
w7 w8 w9



Convolution (Gaussian/Sharpen/Edge)

- Weights can be normalized depending on the application
- Edges? (choose your own adventure)
 - Mirror boundary
 - Zero padding
 - Use part of the kernel only

Gaussian filter

- Create a new image to work on
- Weights should be normalized, so that they sum to 1.

- Formula:

$$G(x) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{x^2}{2\sigma^2}}$$

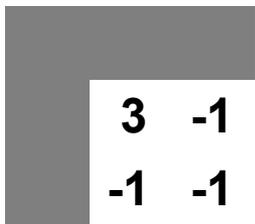
- x = distance to the center of the kernel
- Speed up (linear separation):
 - First apply a 1D Gaussian kernel vertically and then a 1D Gaussian kernel horizontally
 - **You need to do this**

Edge

Kernel:

-1	-1	-1
-1	8	-1
-1	-1	-1

Inside boundary



At boundary

- Don't normalize weights
- Optional to invert the edge map for visualization:
- $\text{pixel} = 1 - \text{pixel}$

Sharpen

- Kernel:

-1	-1	-1
-1	9	-1
-1	-1	-1

Inside boundary



At boundary

- Don't normalize weights

Edge Filter vs Sharpen Filter

-1	-1	-1
-1	8	-1
-1	-1	-1

Edge Filter

-1	-1	-1
-1	9	-1
-1	-1	-1

Sharpen Filter

$\text{Convolution}(\text{Image}, \text{Sharpen Filter}) = \text{Convolution}(\text{Image}, \text{Edge Filter}) + \text{Image}$

Median

- Use a window (similar to convolution)
- Choose the median within the window
- Sorting: sort by RGB separately / sort by luminance
- Optimization: use quick-select to find median
 - **Important algorithm!** Gives median in linear time



1



2



3



4



5

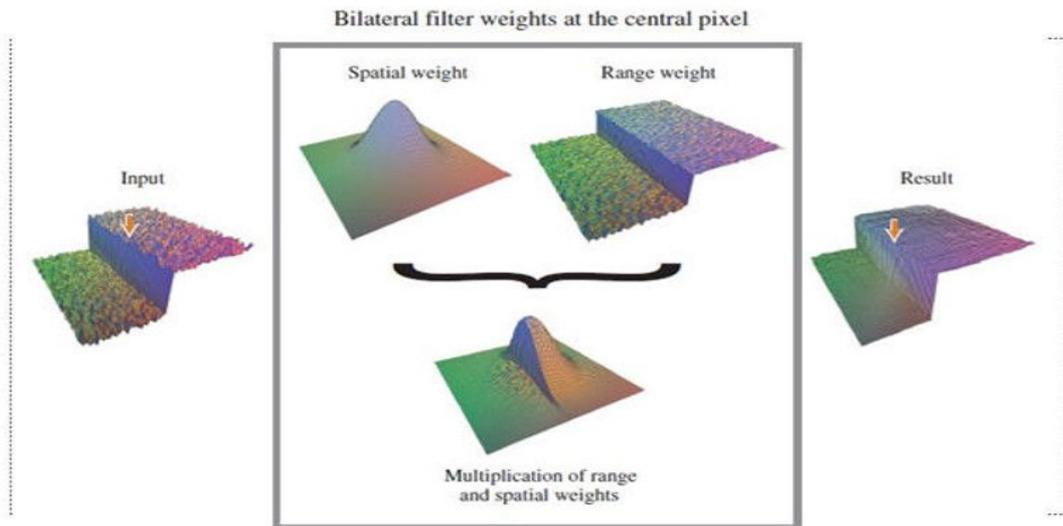
RGB Example

Bilateral

- Combine Gaussian filtering in both spatial domain and color domain
- Weight formula of filter for pixel (i, j): Spatial distance component Color distance component

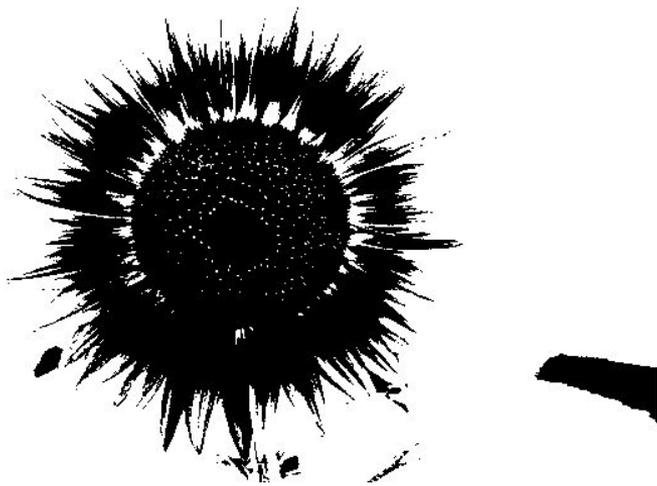
$$w(i, j, k, l) = e^{-\frac{(i-k)^2 + (j-l)^2}{2\sigma_d^2} - \frac{\|I(i, j) - I(k, l)\|^2}{2\sigma_r^2}}$$

- Similar color -> large weights, Different color -> smaller weights



Quantization

- Quantize a pixel within $[0, 1]$ using n bits
 - $\text{round}(p * (2^n - 1)) / (2^n - 1)$

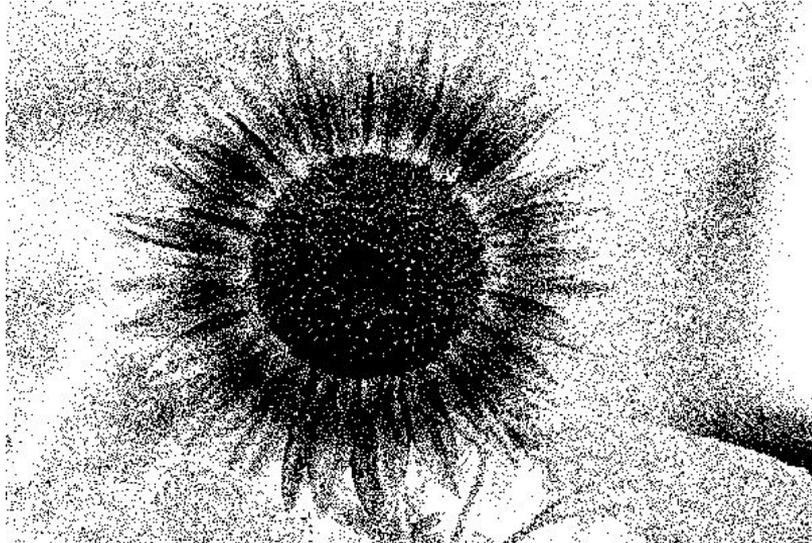


$n=1$ example

Random dithering

- Before quantization:
 - $p = p + (\text{random}() - 0.5)/(2^{n-1})$
 - n is number of bits per channel

$n=1$ example



Ordered dithering

Pseudo code for n-bit case:

```
i = x mod m
```

```
j = y mod m
```

```
err = I(x, y) - floor_quantize(I(x, y))
```

```
threshold = (D(i, j) + 1) / (m2 + 1)
```

```
if err > threshold
```

```
    P(x, y) = ceil_quantize(I(x, y))
```

```
else
```

```
    P(x, y) = floor_quantize(I(x, y))
```

- floor_quantize(p)
= floor(p * (2ⁿ⁻¹)) / (2ⁿ⁻¹)
- ceil_quantize(p)
= ceil(p * (2ⁿ⁻¹)) / (2ⁿ⁻¹)

$$m = 4, D = \begin{bmatrix} 15 & 7 & 13 & 5 \\ 3 & 11 & 1 & 9 \\ 12 & 4 & 14 & 6 \\ 0 & 8 & 2 & 10 \end{bmatrix}$$



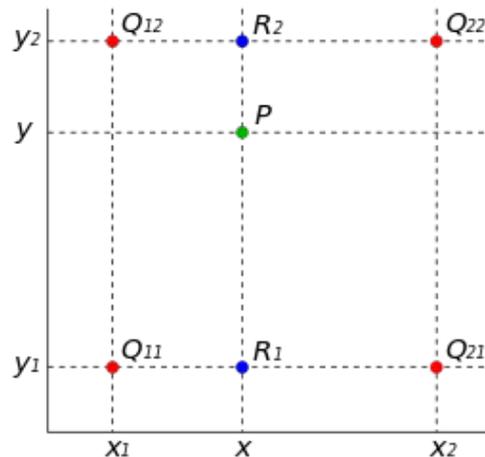
n=1 example

Resampling

- Bilinear interpolation

$$f(x, y) = \frac{1}{(x_2 - x_1)(y_2 - y_1)} (f(Q_{11})(x_2 - x)(y_2 - y) + f(Q_{21})(x - x_1)(y_2 - y) + f(Q_{12})(x_2 - x)(y - y_1) + f(Q_{22})(x - x_1)(y - y_1))$$

(from wikipedia)

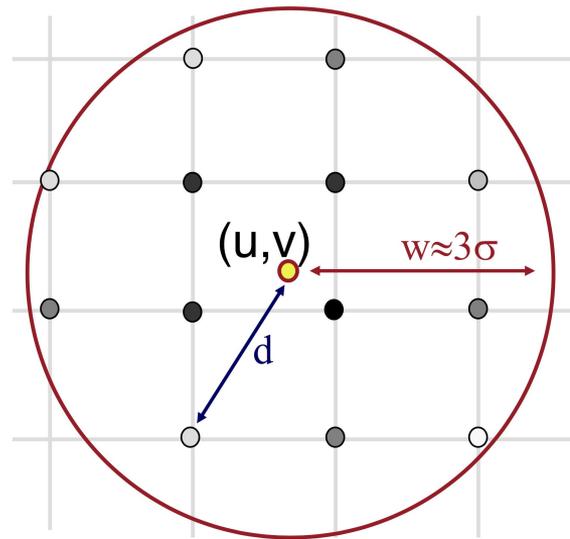


Resampling

- Gaussian interpolation
 - Weights:

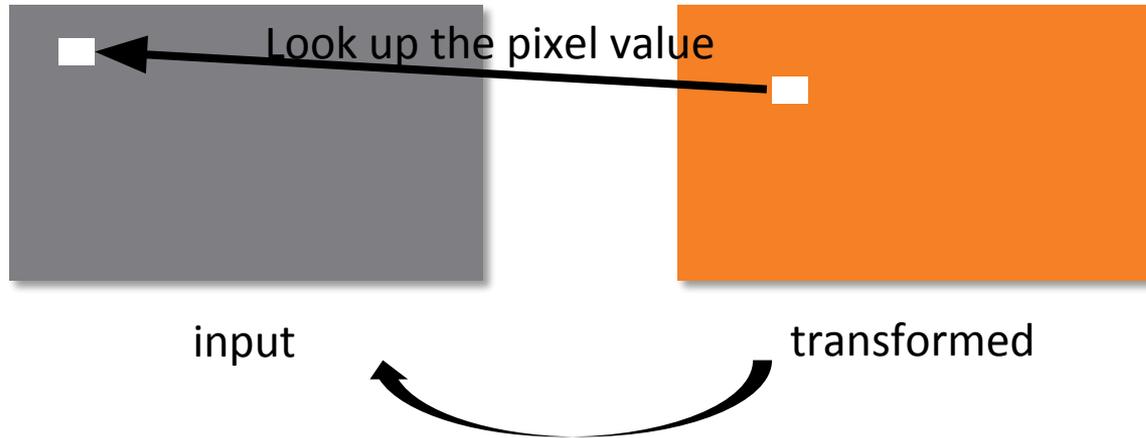
$$G(d, \sigma) = e^{-d^2 / (2\sigma^2)}$$

- Weights need to be normalized, so that sum up to 1
- Use windowSize = 3*sigma
 - Sigma can be 1
- Window can be square



Transformation (translate/scale/rotate/swirl)

- Inverse mapping



Inverse mapping guarantees that every pixel in the transformed image is filled!

Transformation (translate/scale/rotate/swirl)

- To fill in a pixel in the target image, apply the inverse transform to the pixel location and look it up in the input image (with resampling technique) for pixel value.
- i.e. For translation of $x' = x + tx$, $y' = y + ty$:

$$l'(x', y') = l(x' - tx, y' - ty)$$

- i.e. For scale of $x' = x * sx$, $y' = y * sy$:

$$l'(x', y') = l(x' / sx, y' / sy)$$

Composite

- $\text{output} = \text{alpha} * \text{foreground} + (1 - \text{alpha}) * \text{background}$
- alpha is the alpha channel foreground



backgroundImg



foregroundImg



foregroundImg(alpha channel)



Result

Morph

- Basic concepts
 - transform the background image to the foreground image
 - alpha = 0: show background
 - alpha = 1: show foreground
 - alpha is the blending factor / timestamp
- General approach
 - specify correspondences (morphLines.html)
 - create an intermediate image with interpolated correspondences (alpha)
 - warp the background image to the intermediate image
 - warp the foreground image to the intermediate image
 - blend using alpha

Morph

```
GenerateAnimation(Image0, L0[...], Image1, L1[...])
begin
  foreach intermediate frame time t do
    for i = 1 to number of line pairs do
      L[i] = line t-th of the way from L0 [i] to L1 [i]
    end
    Warp0 = WarpImage(Image0, L0, L)
    Warp1 = WarpImage(Image1, L1, L)
    foreach pixel p in FinalImage do
      Result(p) = (1-t) Warp0 + t Warp1
    end
  end
end
```

Warp Image

$$\bullet u = \frac{(X-P) \cdot (Q-P)}{\|Q-P\|^2}$$

$$\bullet v = \frac{(X-P) \cdot \text{Perpendicular}(Q-P)}{\|Q-P\|} \quad \text{unit vector}$$

If $Q - P = (x, y)$,

$\text{Perpendicular}(Q - P) = (y, -x)$

$$\bullet X' = P' + u \cdot (Q' - P') + \frac{v \cdot \text{Perpendicular}(Q' - P')}{\|Q' - P'\|} \quad \text{unit vector}$$

$\bullet \text{dist} = \text{shortest distance from } X \text{ to } PQ$

$\bullet 0 \leq u \leq 1: \text{dist} = |v|$

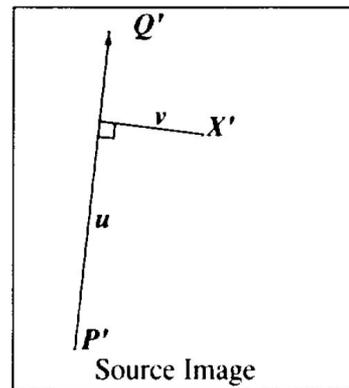
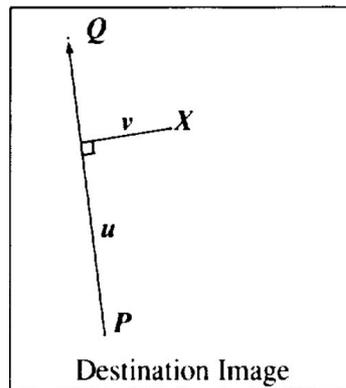
$\bullet u < 0: \text{dist} = \|X - P\|$

$\bullet u > 1: \text{dist} = \|X - Q\|$

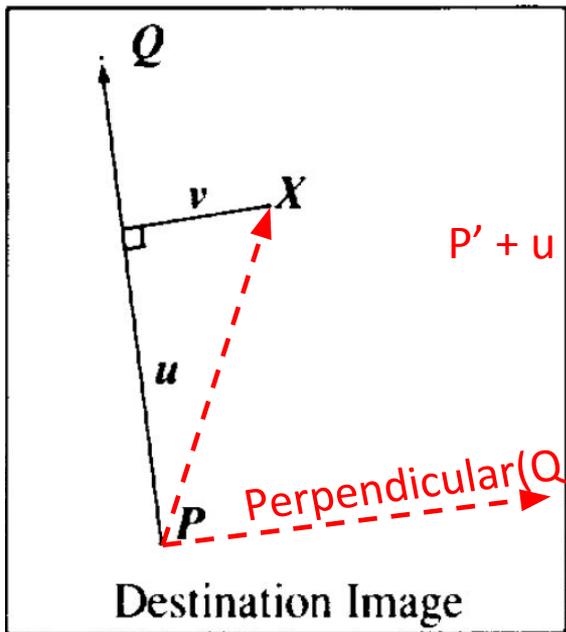
$$\bullet \text{weight} = \left(\frac{\text{length}^p}{a + \text{dist}} \right)^b$$

\bullet we use $p = 0.5, a = 0.01, b = 2$

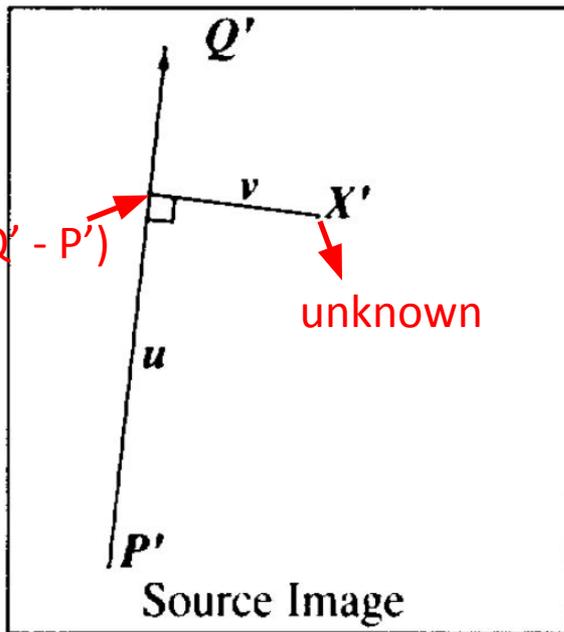
Contribution of line segment PQ to the warping of X's location



Warp Image



Warped background or foreground (currently black)



Pixel source (background or foreground)

Warp Image

For each pixel X in the destination

$$DSUM = (0,0)$$

$$weightsum = 0$$

For each line $P_i Q_i$

calculate u, v based on $P_i Q_i$

calculate X'_i based on u, v and $P'_i Q'_i$

calculate displacement $D_i = X'_i - X_i$ for this line

$dist$ = shortest distance from X to $P_i Q_i$

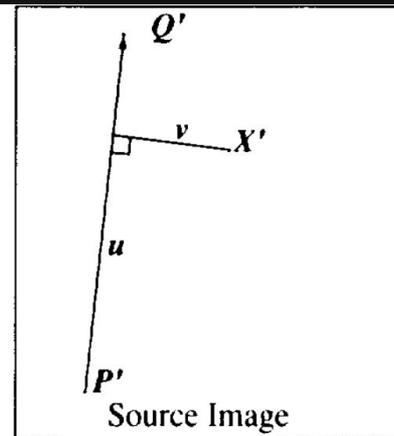
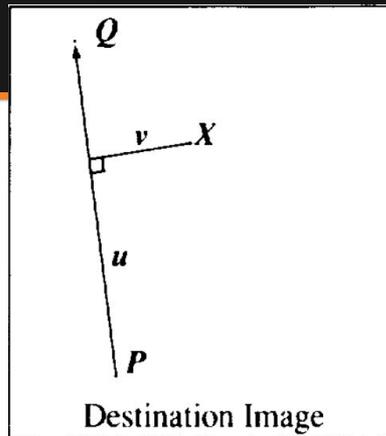
$$weight = (length^p / (a + dist))^b$$

$$DSUM += D_i * weight$$

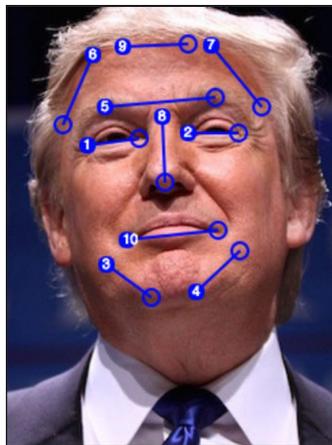
$$weightsum += weight$$

$$X' = X + DSUM / weightsum$$

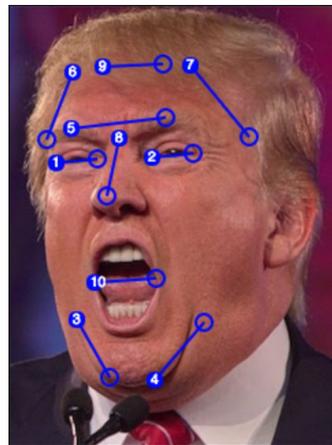
$$destinationImage(X) = sourceImage(X')$$



Interpolate Morph Lines



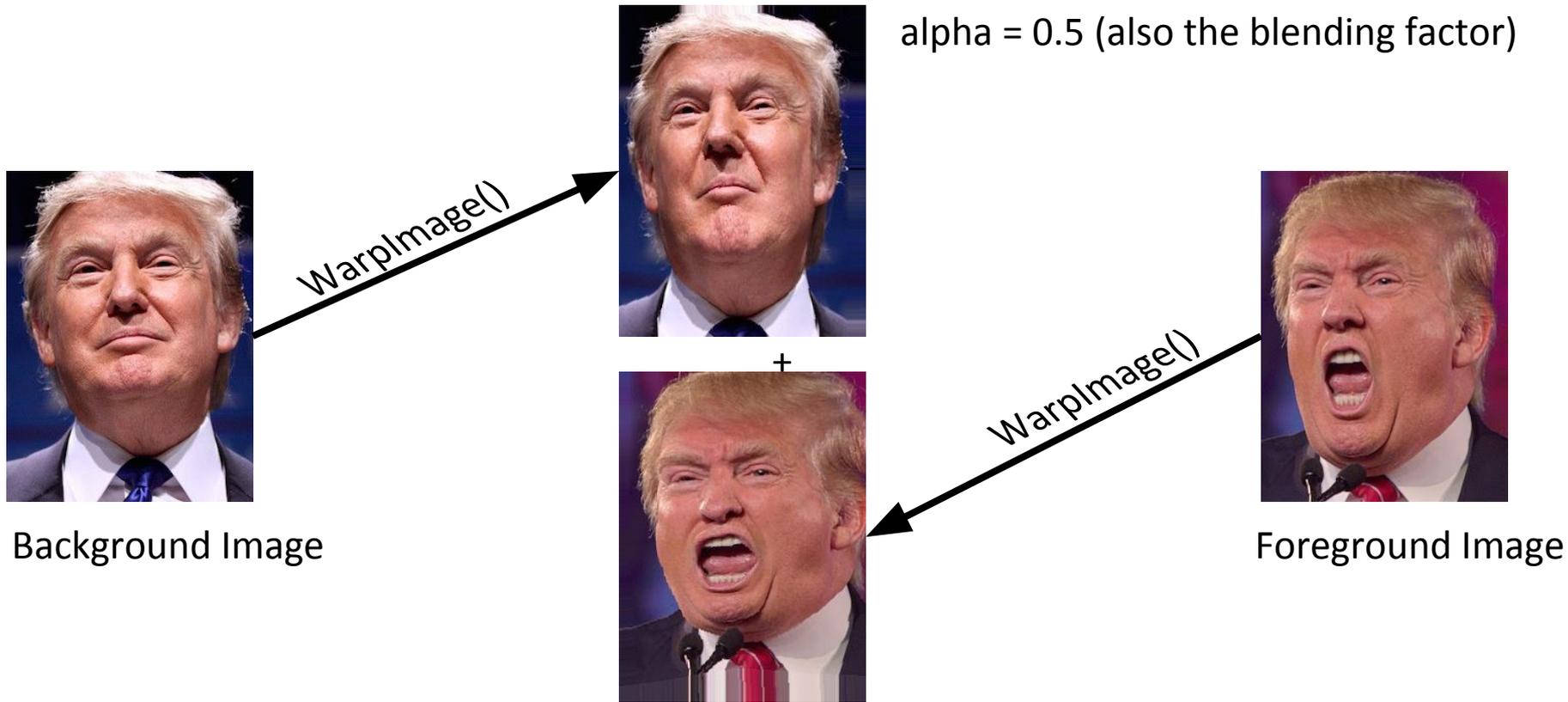
Background Image



Foreground Image

$$\text{current_line}[i] = (1 - \alpha) * \text{background_lines}[i] + \alpha * \text{foreground_lines}[i]$$

Blending



Blending

$\alpha = 0.5$ (also the blending factor)



Background Image



Foreground Image

Q&A
