



<https://algs4.cs.princeton.edu>

## KRUSKAL'S ALGORITHM DEMO

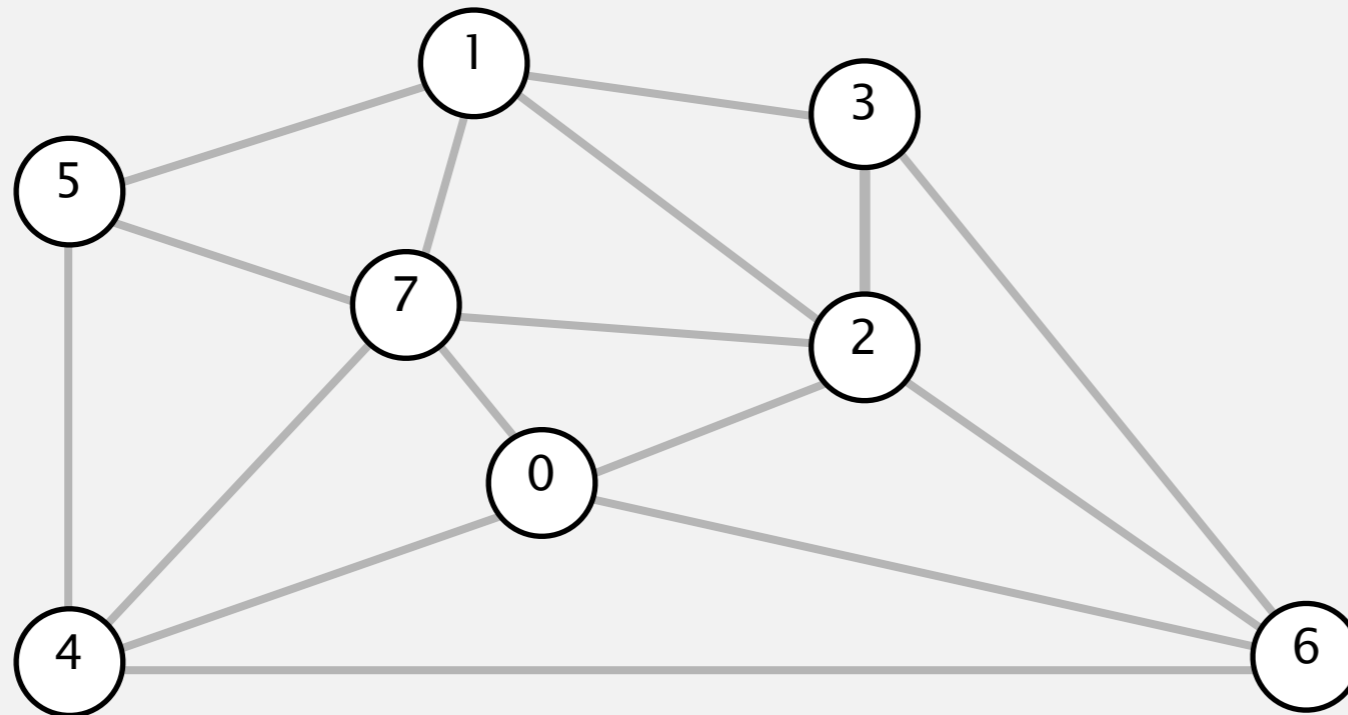
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# Kruskal's algorithm demo

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Consider edges in ascending order of weight.

- Add next edge to  $T$  unless doing so would create a cycle.



**an edge-weighted graph**

graph edges  
sorted by weight



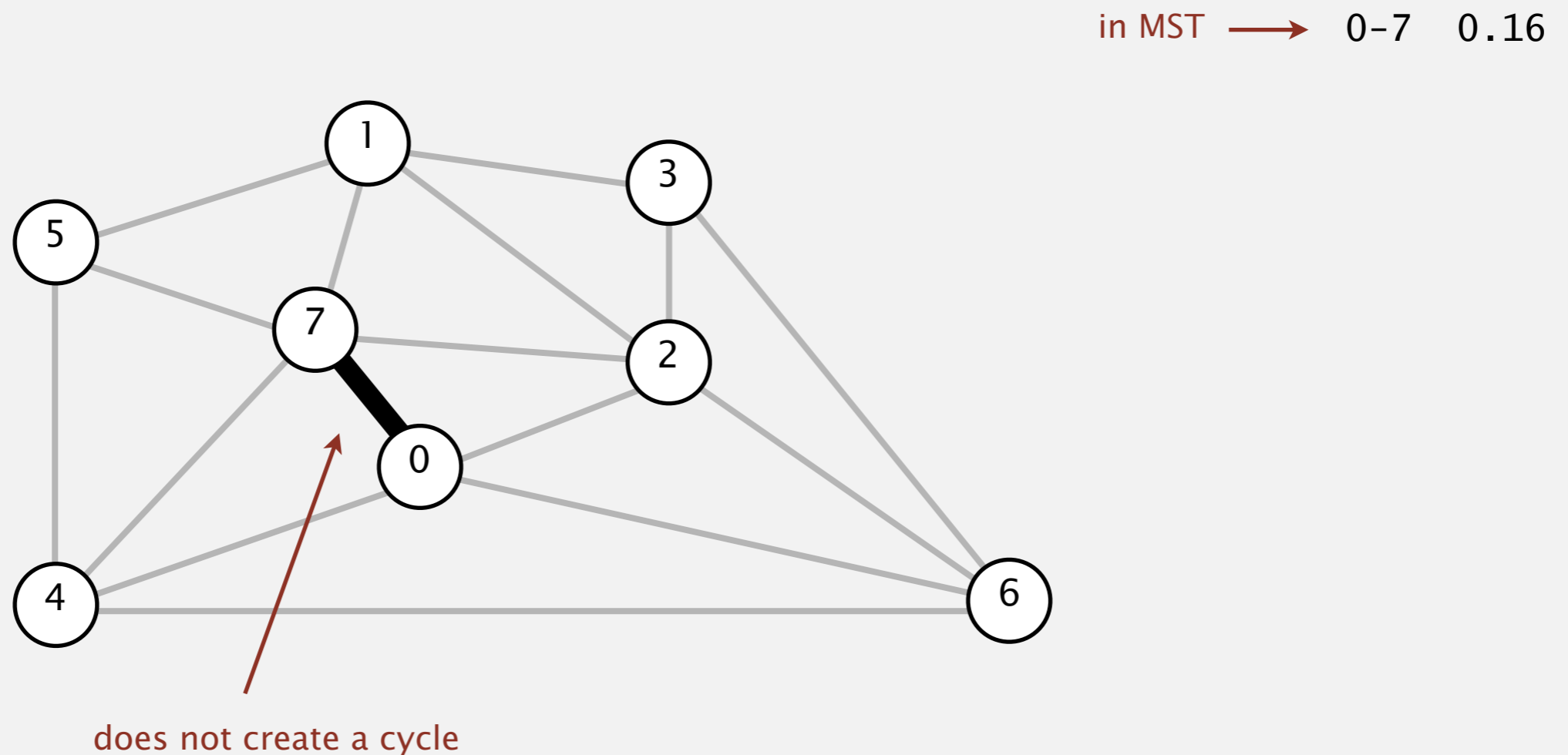
|     |      |
|-----|------|
| 0-7 | 0.16 |
| 2-3 | 0.17 |
| 1-7 | 0.19 |
| 0-2 | 0.26 |
| 5-7 | 0.28 |
| 1-3 | 0.29 |
| 1-5 | 0.32 |
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| 4-5 | 0.35 |
| 1-2 | 0.36 |
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| 0-4 | 0.38 |
| 6-2 | 0.40 |
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| 6-4 | 0.93 |

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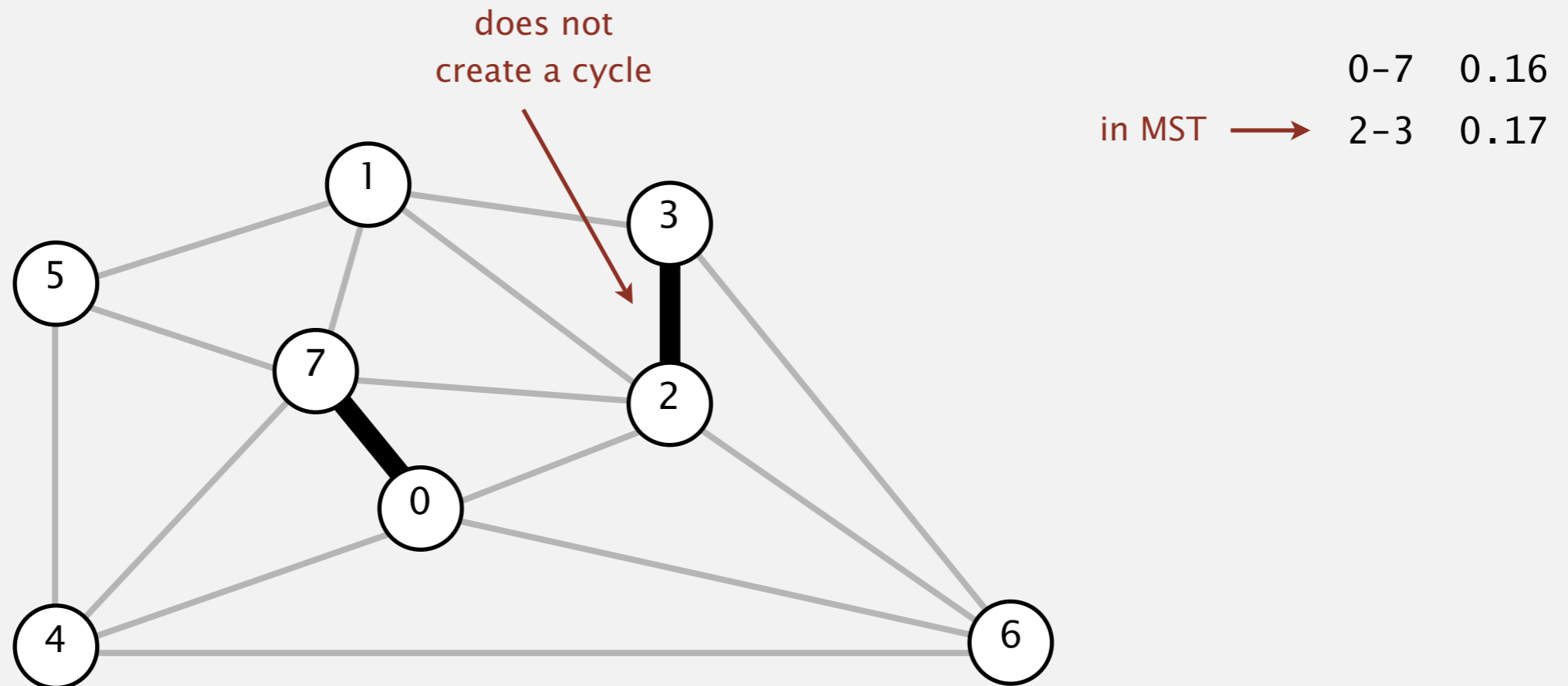


# Kruskal's algorithm demo

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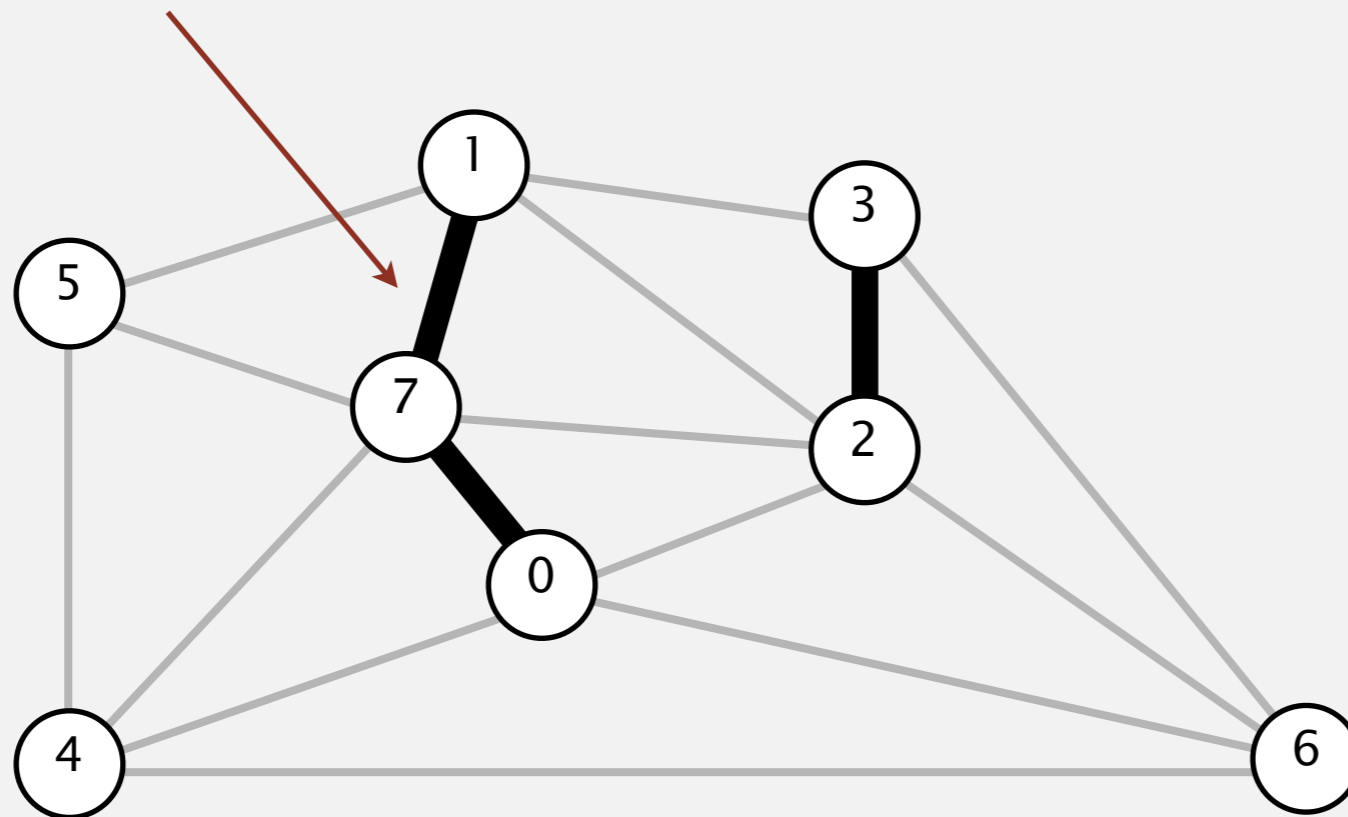
# Kruskal's algorithm demo

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does not create a cycle



in MST →

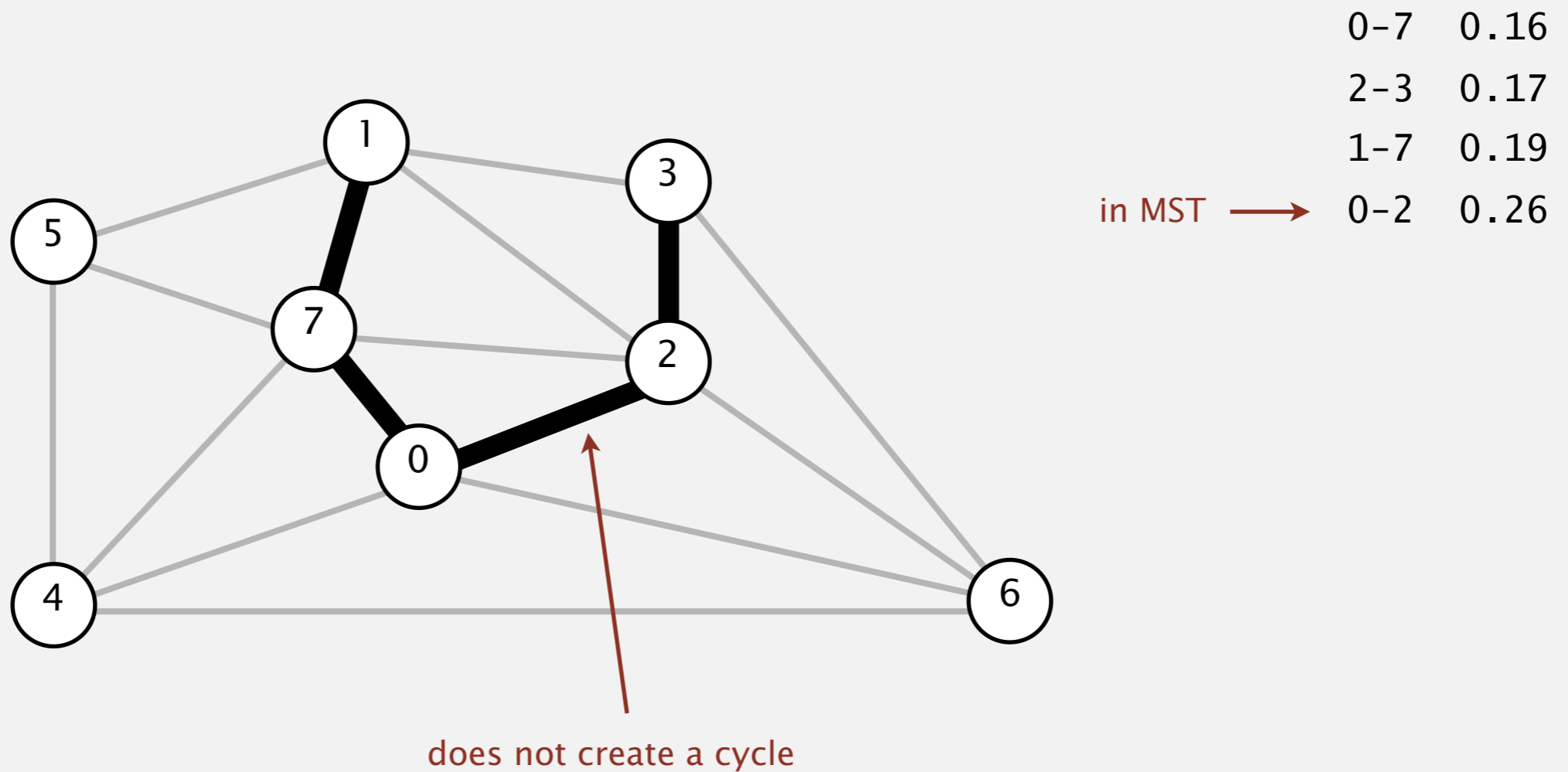
|     |      |
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| 0-7 | 0.16 |
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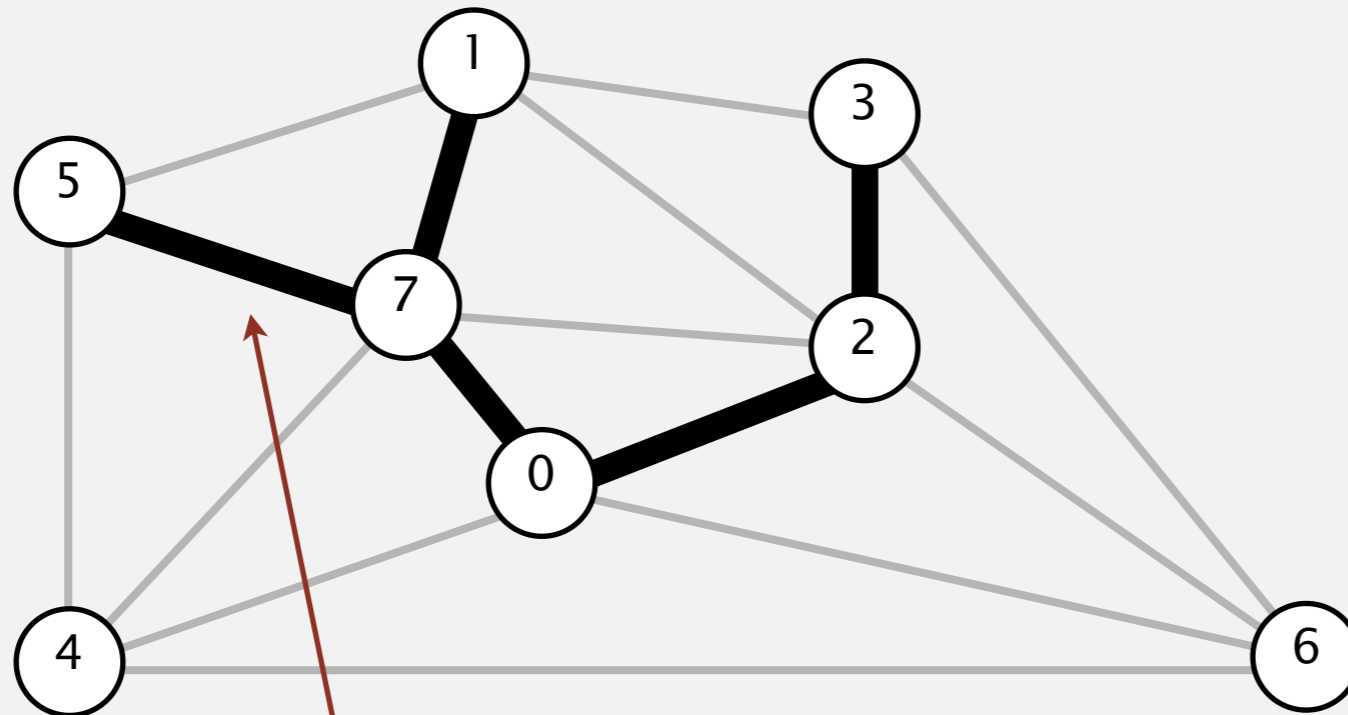


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in MST →

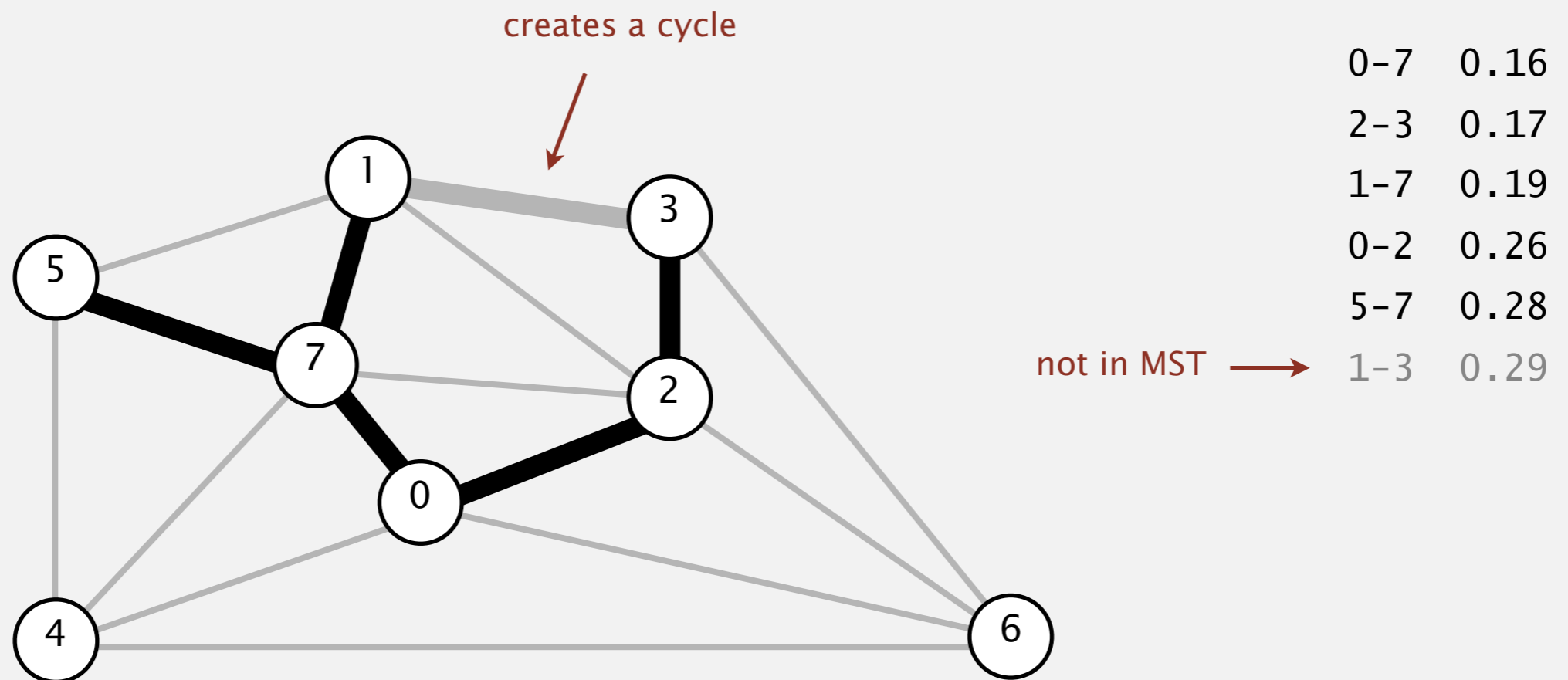
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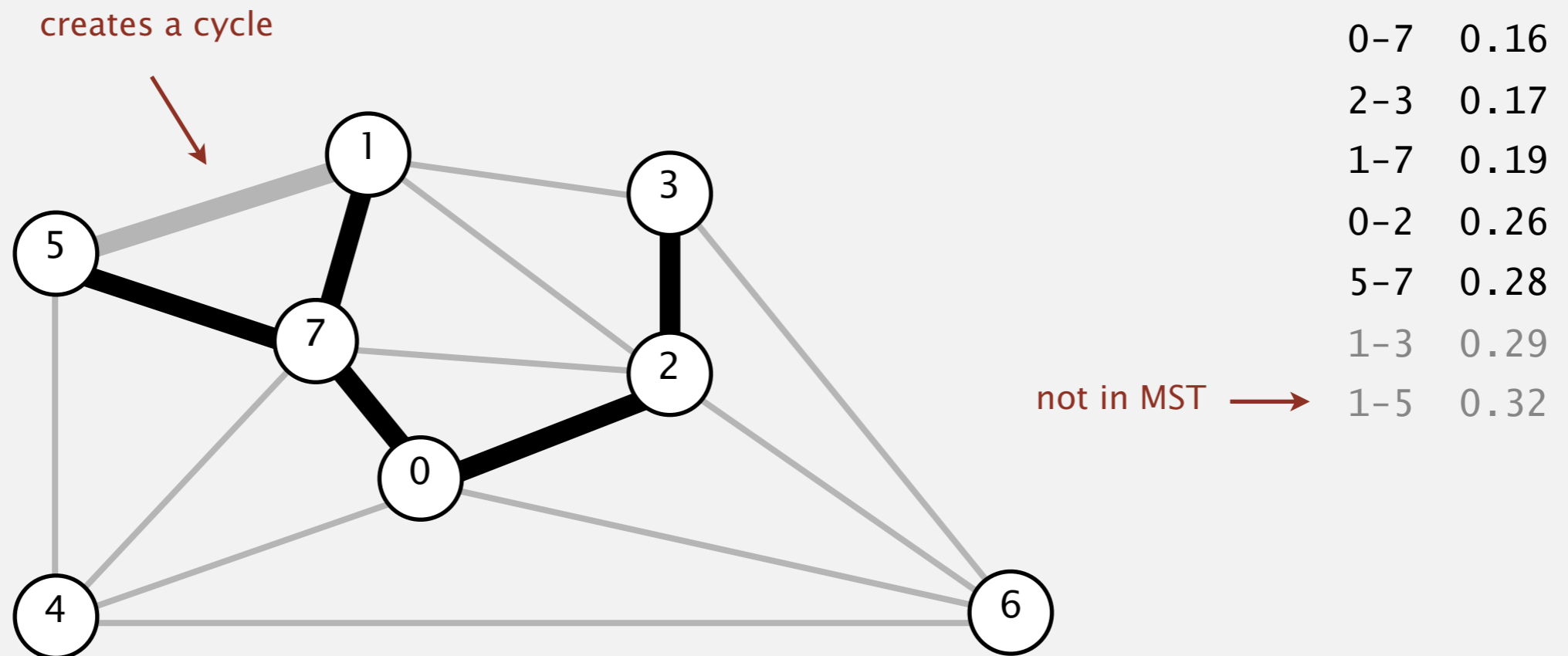


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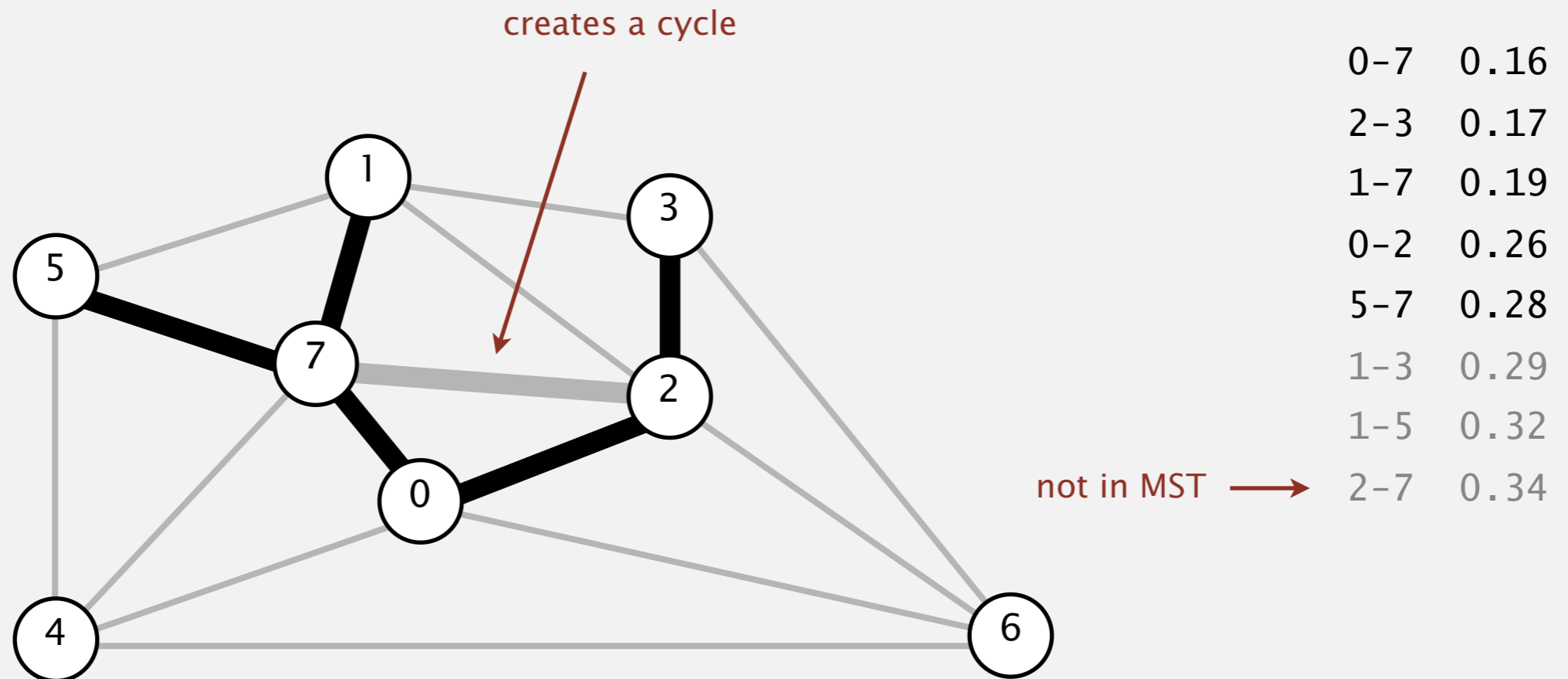


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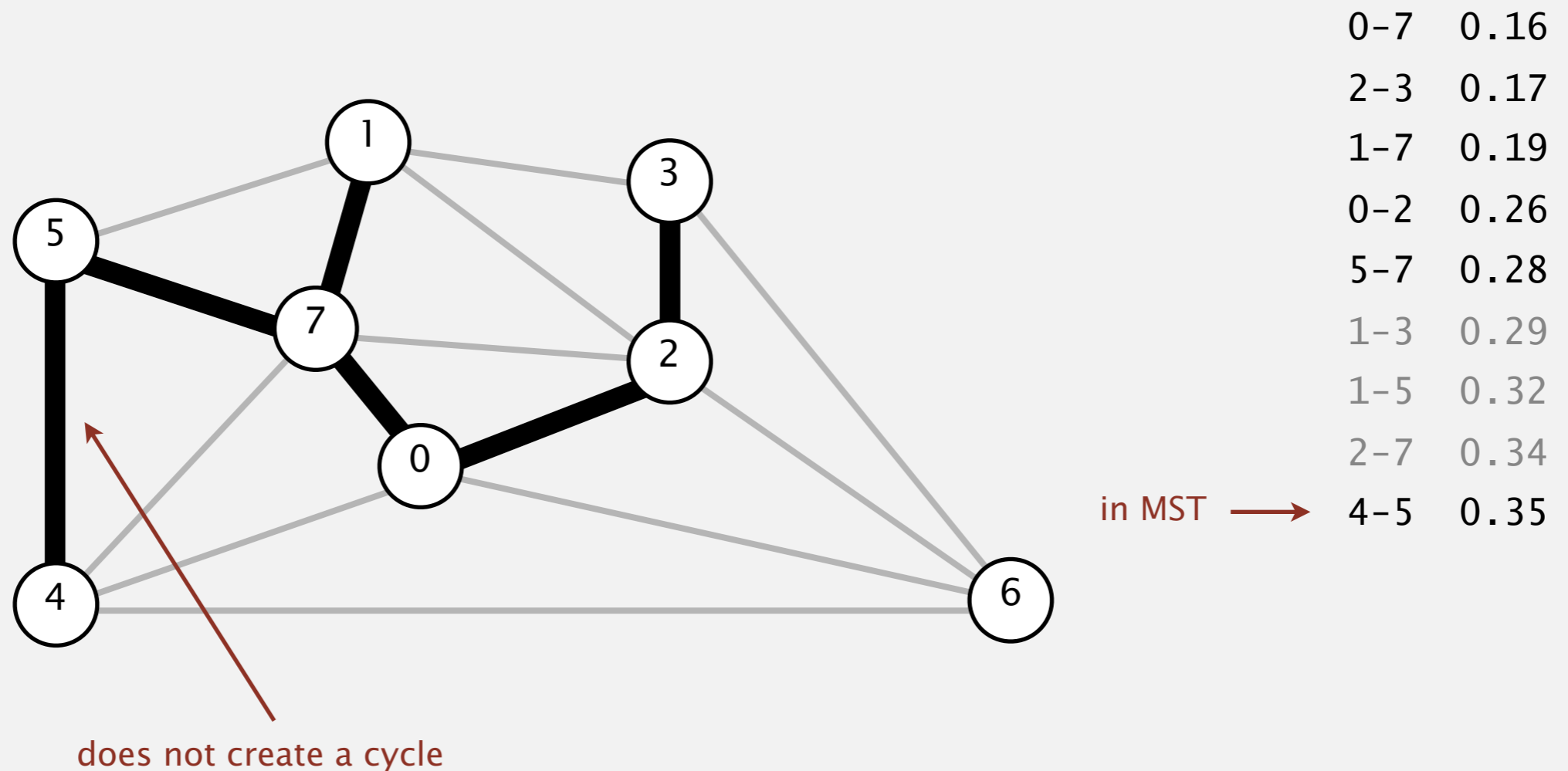


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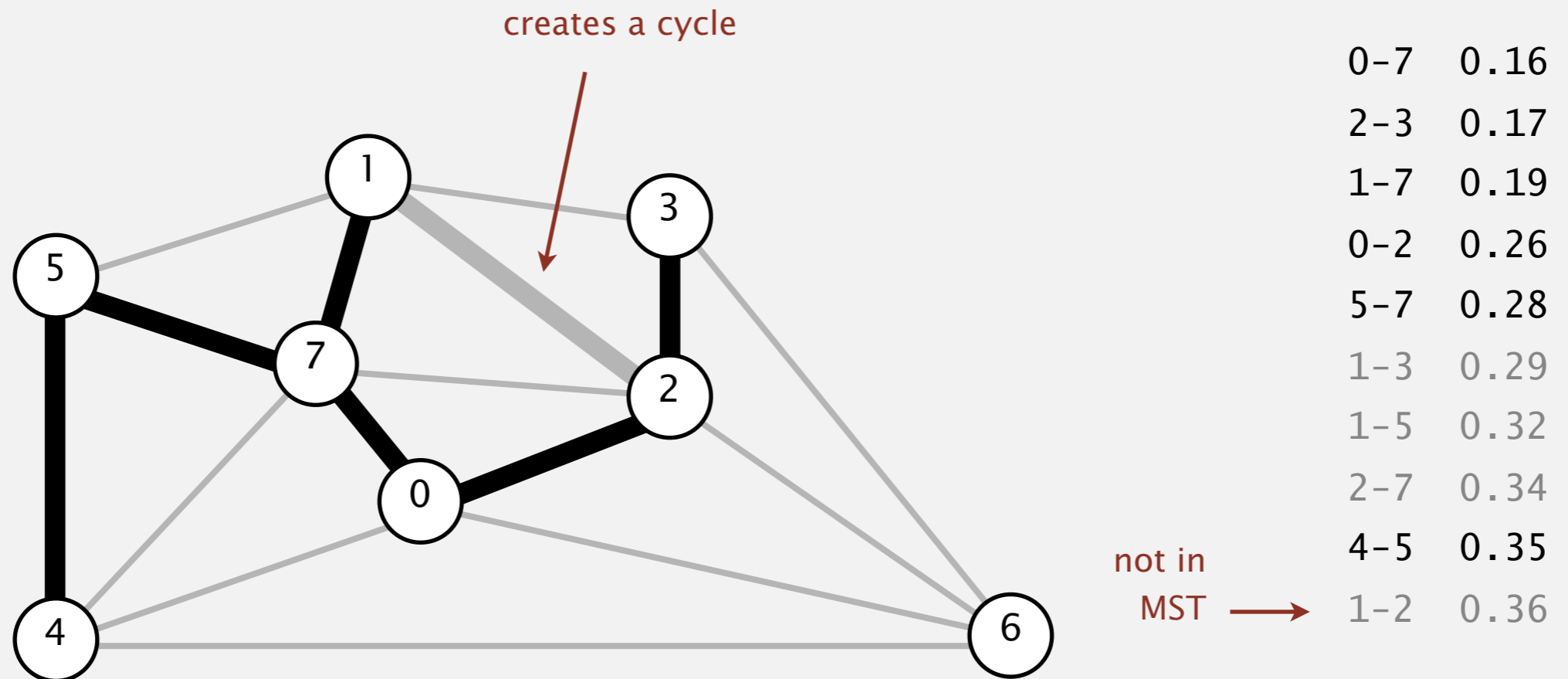


# Kruskal's algorithm demo

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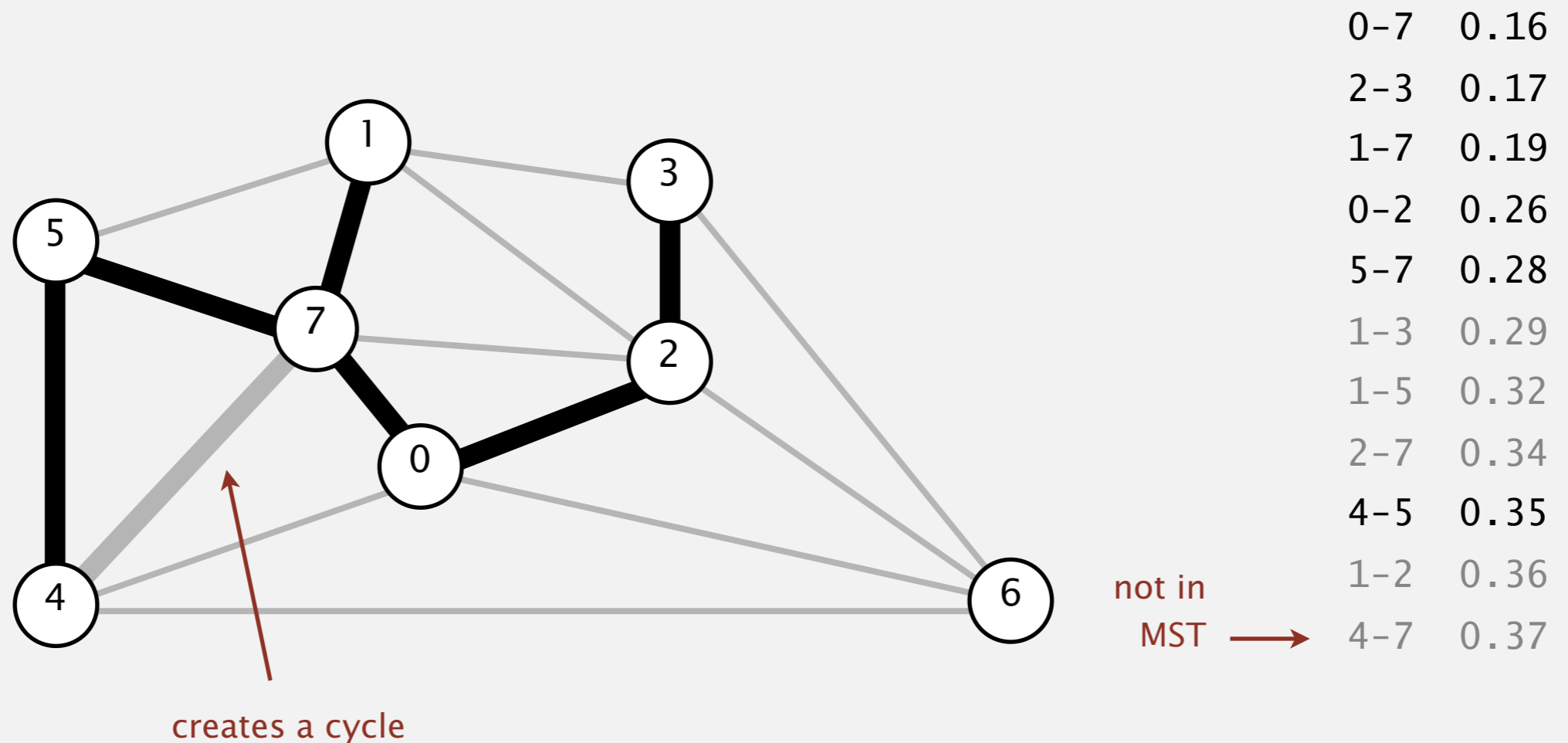
- Add next edge to  $T$  unless doing so would create a cycle.



# Kruskal's algorithm demo

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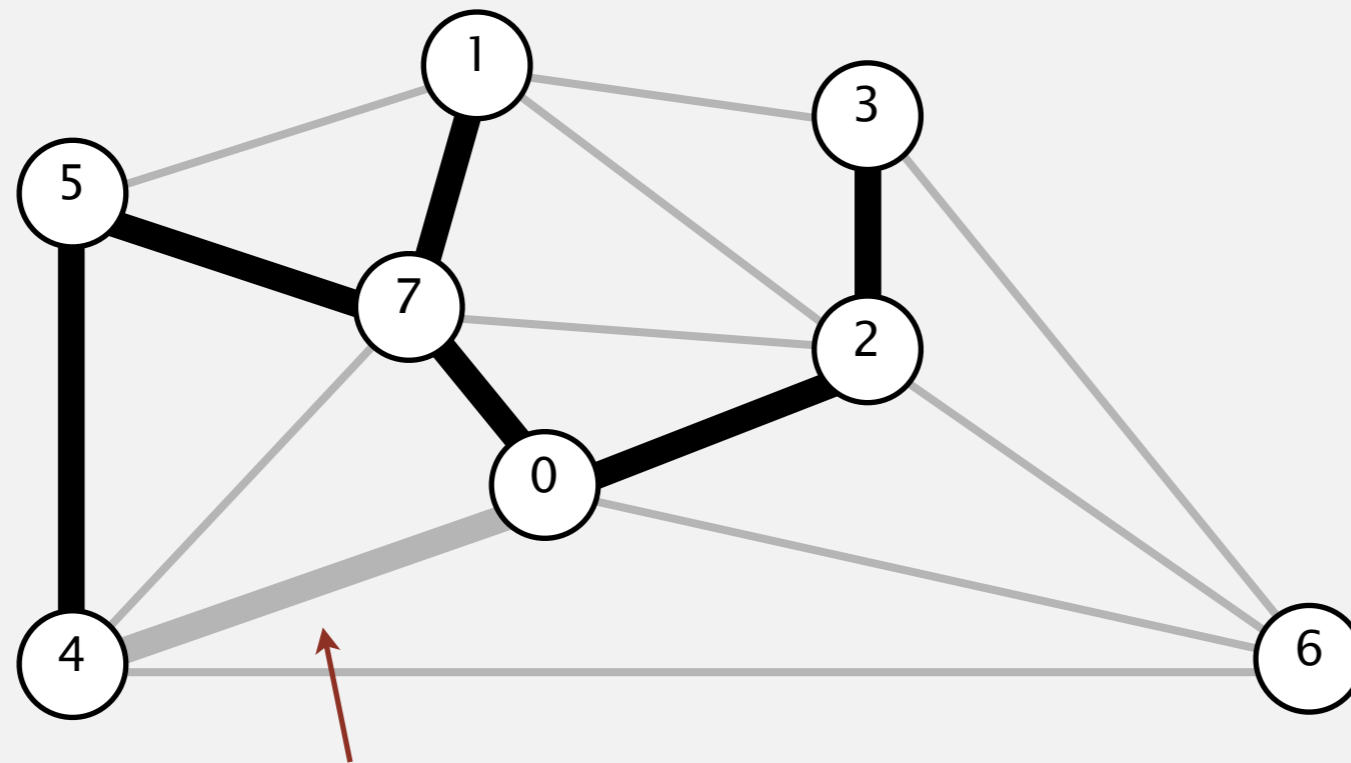


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creates a cycle

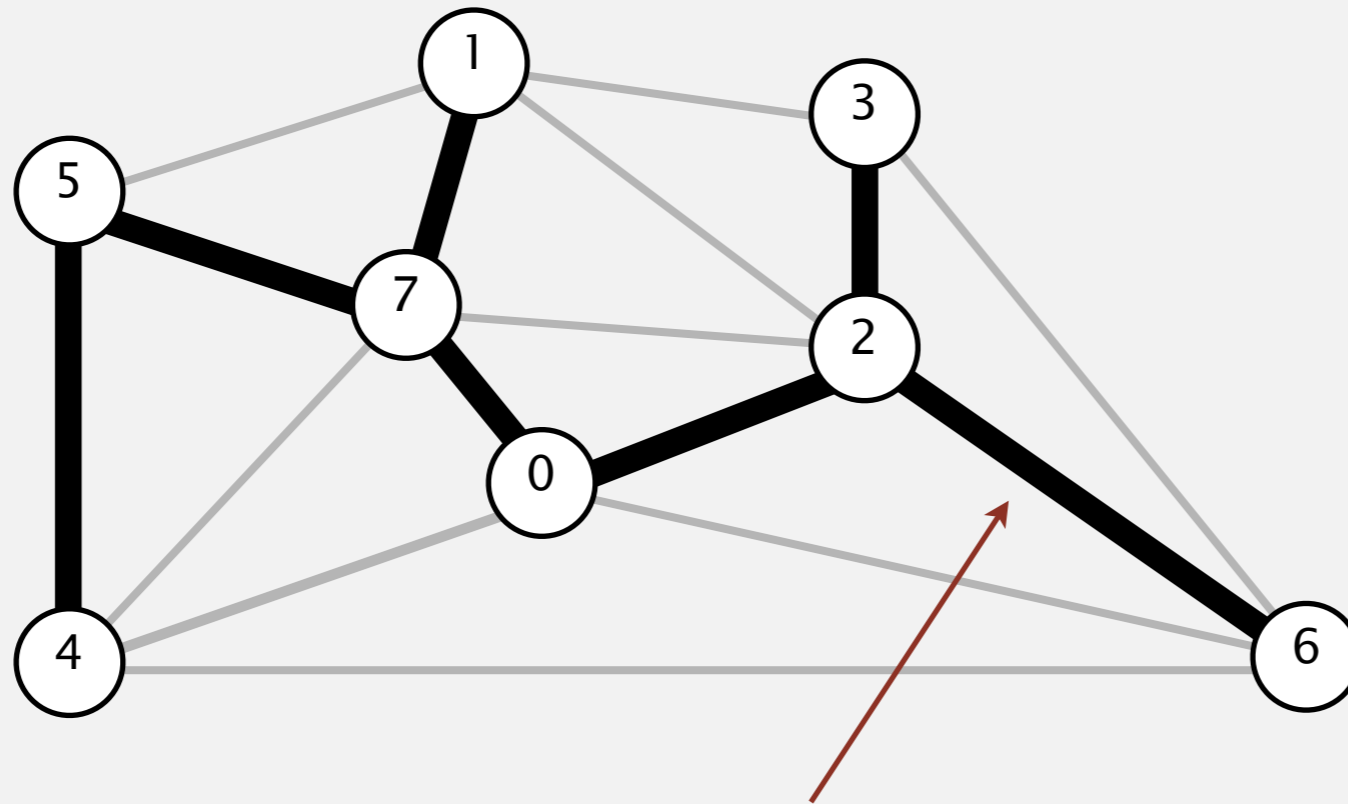
not in MST →

# Kruskal's algorithm demo

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Consider edges in ascending order of weight.

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does not create a cycle

in MST →

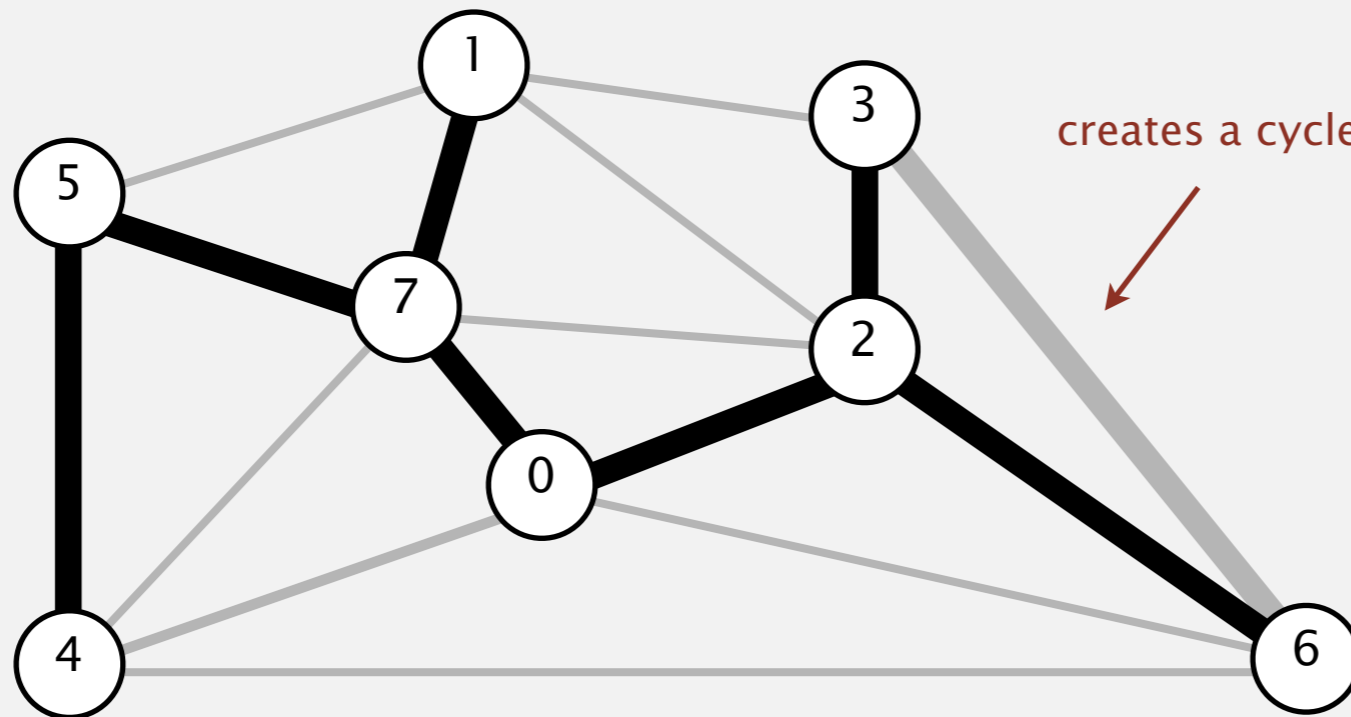
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not in MST →

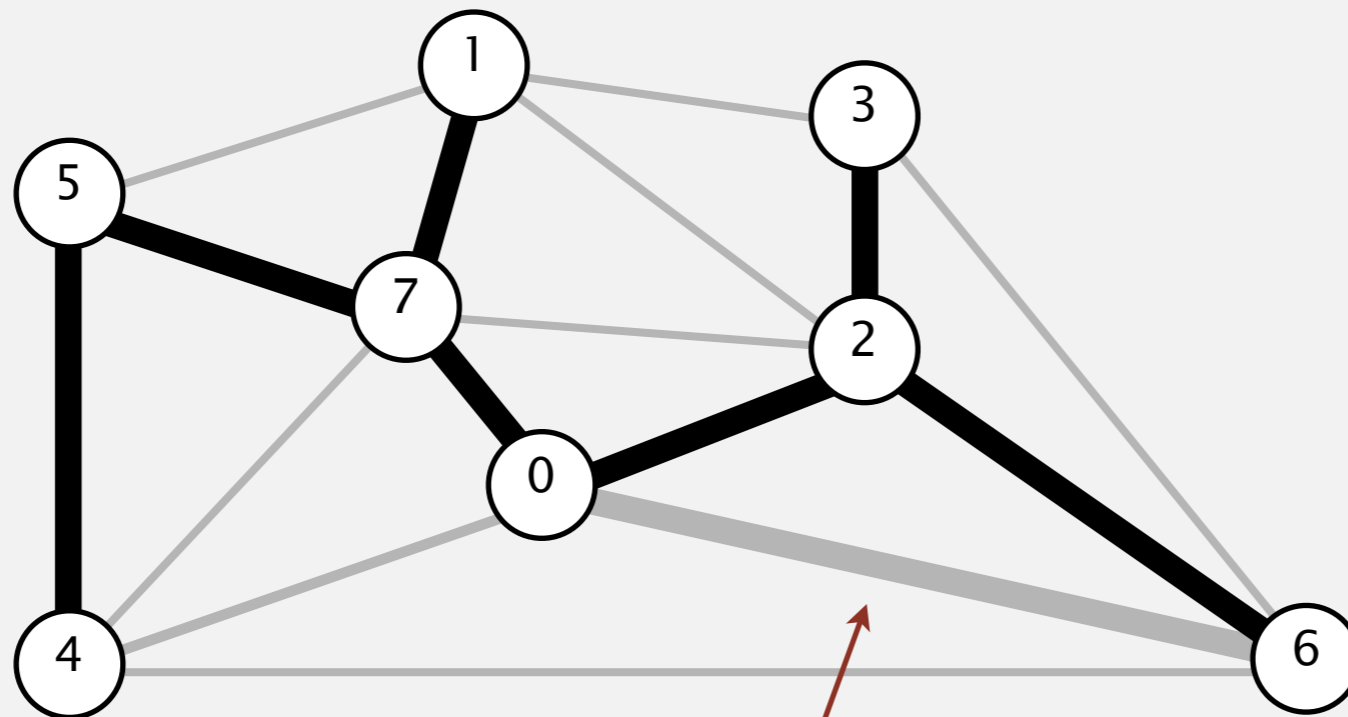


# Kruskal's algorithm demo

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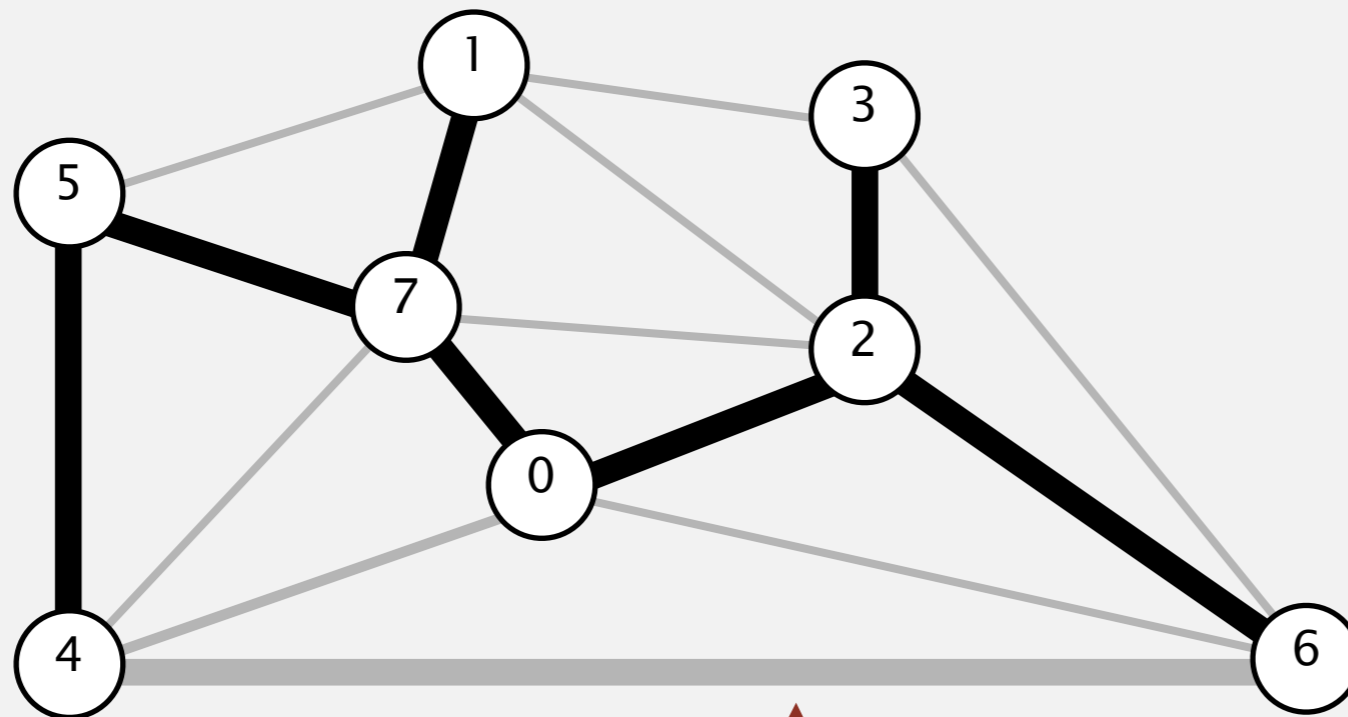
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not in MST →

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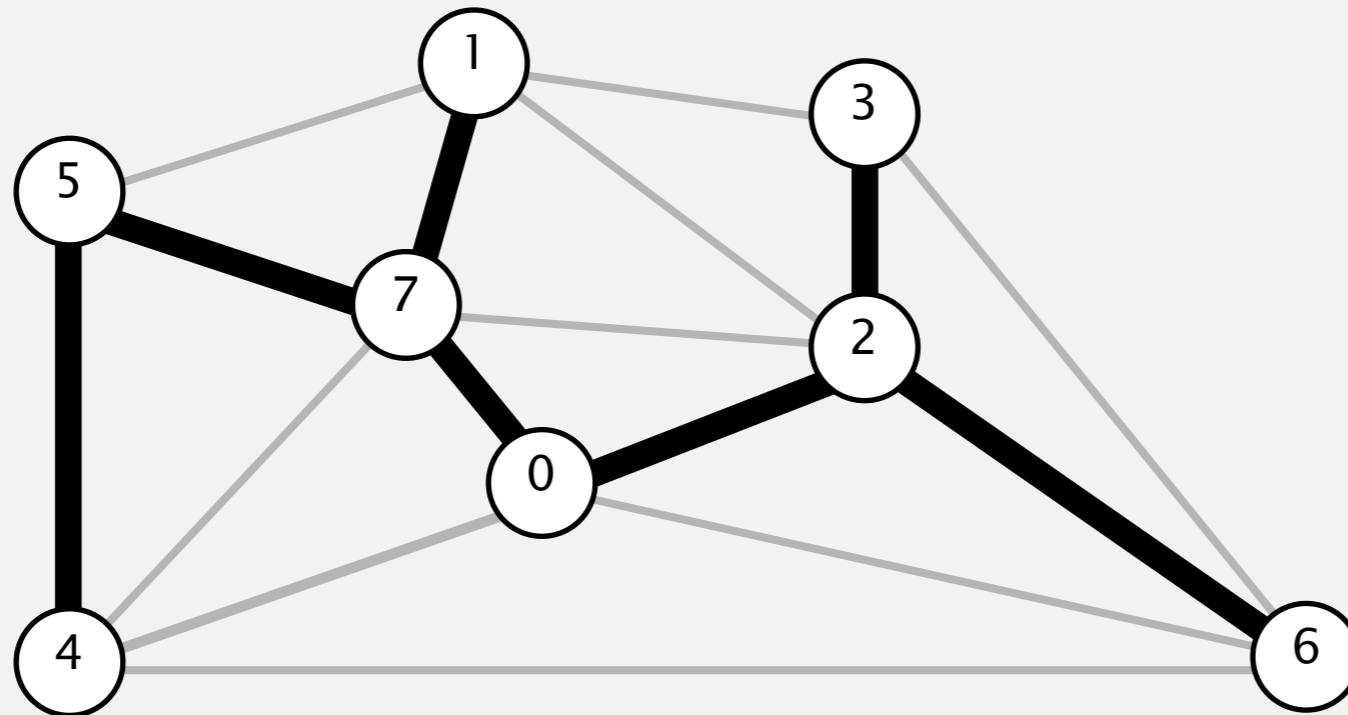
not in MST →

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**a minimum spanning tree**

|     |      |
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