Hint on HW#8, problem 1a $\,$

Use the universal portfolios algorithm and its analysis.

Also, here is a fact from calculus that you might find helpful. If c_1, \ldots, c_N are nonnegative integers (with $N \ge 2$), then

$$\int \left(\prod_{i=1}^N b_i^{c_i}\right) d\mu(\mathbf{b}) = \frac{\prod_{i=1}^N (c_i!)}{\left(N - 1 + \sum_{i=1}^N c_i\right)!}$$

where, as in class, the integral is over all vectors $\mathbf{b} = \langle b_1, \dots, b_N \rangle \in [0, 1]^N$ with $\sum_{i=1}^N b_i = 1$.