



3D Modeling

COS 426, Spring 2019

Princeton University

Adam Finkelstein



Syllabus



I. Image processing

II. Modeling

III. Rendering

IV. Animation

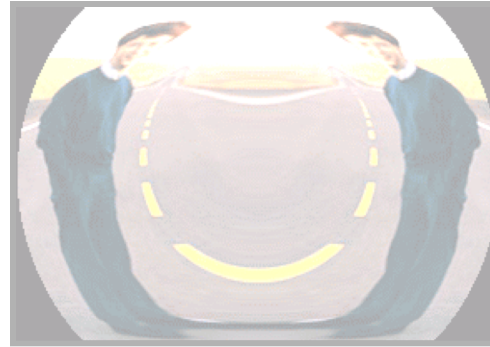
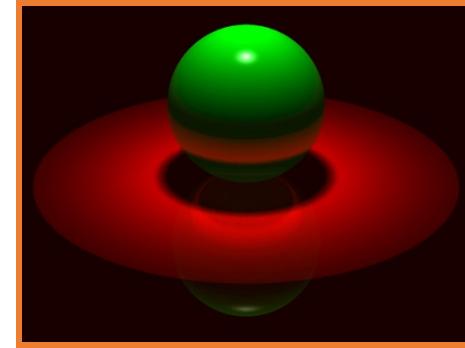
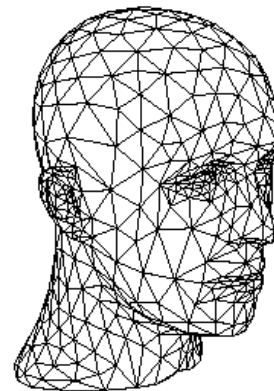


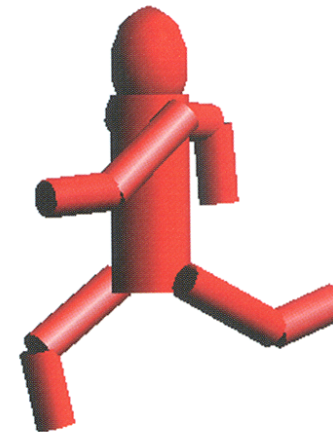
Image Processing
(Rusty Coleman, CS426, Fall99)



Rendering
(Michael Bostock, CS426, Fall99)



Modeling
(Denis Zorin, CalTech)

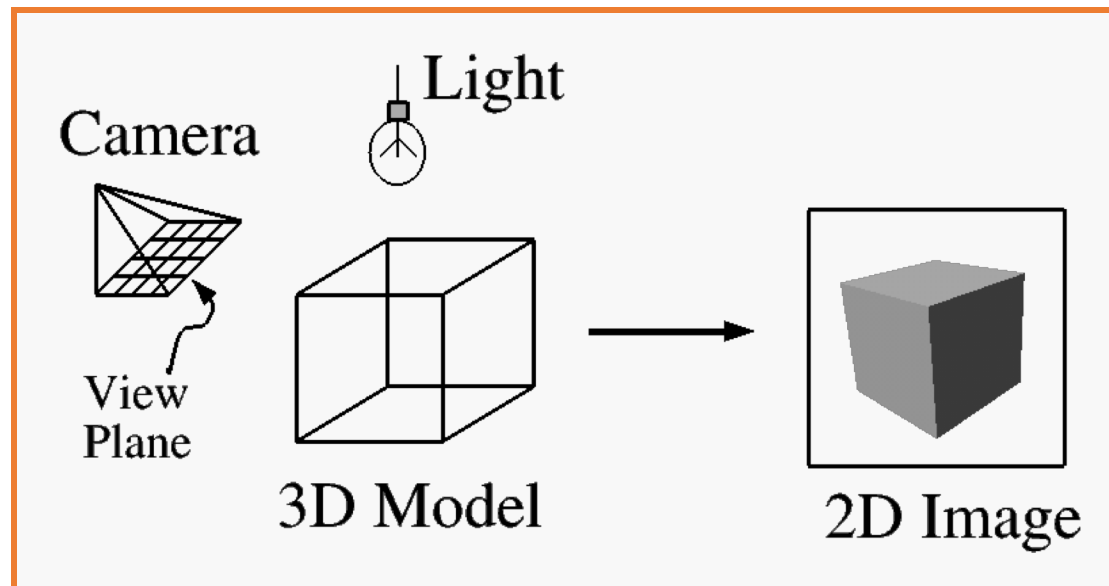


Animation
(Angel, Plate 1)

What is 3D Modeling?



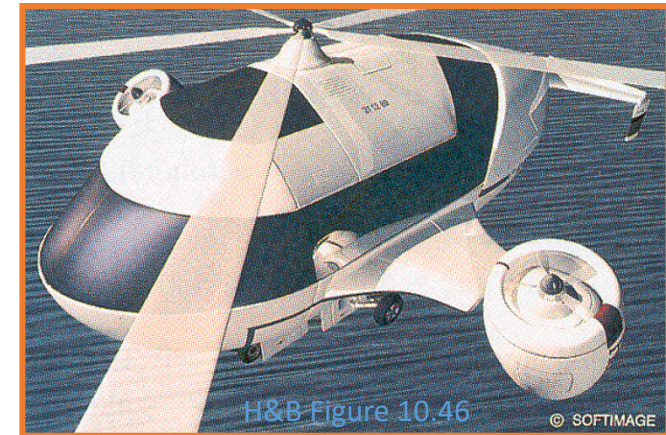
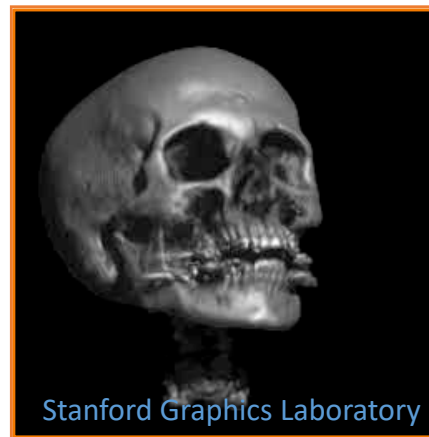
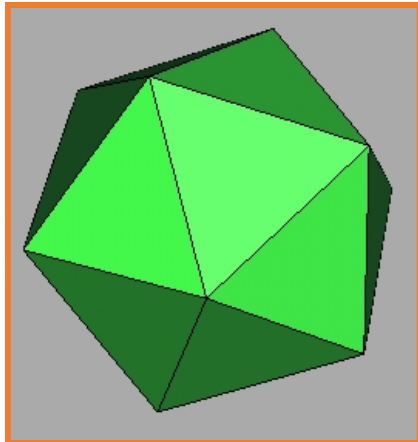
- Topics in computer graphics
 - Imaging = *representing 2D images*
 - Modeling = *representing 3D objects*
 - Rendering = *constructing 2D images from 3D models*
 - Animation = *simulating changes over time*



Modeling



- How do we ...
 - Represent 3D objects in a computer?
 - Acquire computer representations of 3D objects?
 - Manipulate computer representations of 3D objects?



Modeling Background



- Scene is usually approximated by 3D primitives
 - Point
 - Vector
 - Line segment
 - Ray
 - Line
 - Plane
 - Polygon

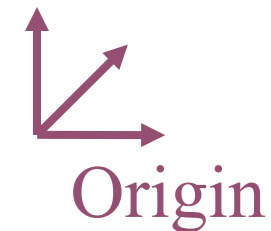
3D Point



- Specifies a location
 - Represented by three coordinates
 - Infinitely small

```
typedef struct {  
    Coordinate x;  
    Coordinate y;  
    Coordinate z;  
} Point;
```

•(x,y,z)

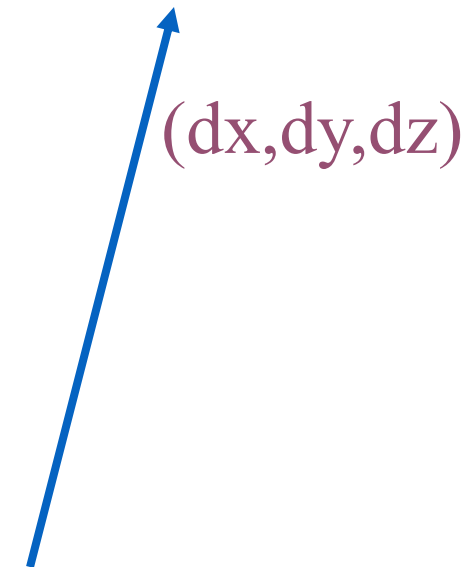


3D Vector



- Specifies a direction and a magnitude
 - Represented by three coordinates
 - Magnitude $||V|| = \sqrt{dx \ dx + dy \ dy + dz \ dz}$
 - Has no location

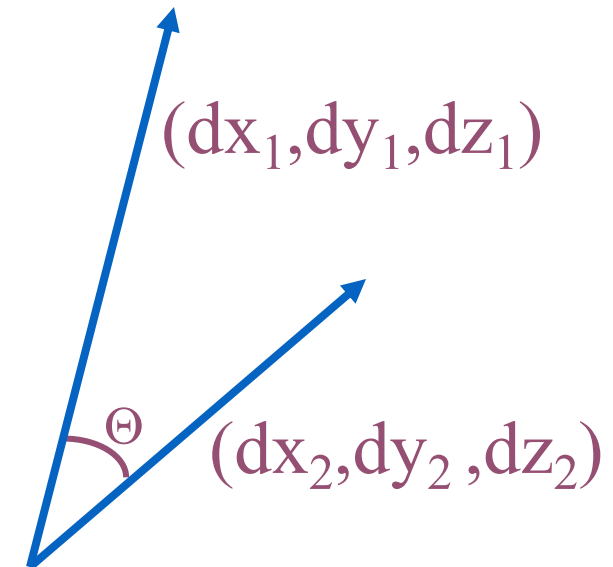
```
typedef struct {  
    Coordinate dx;  
    Coordinate dy;  
    Coordinate dz;  
} Vector;
```



3D Vector



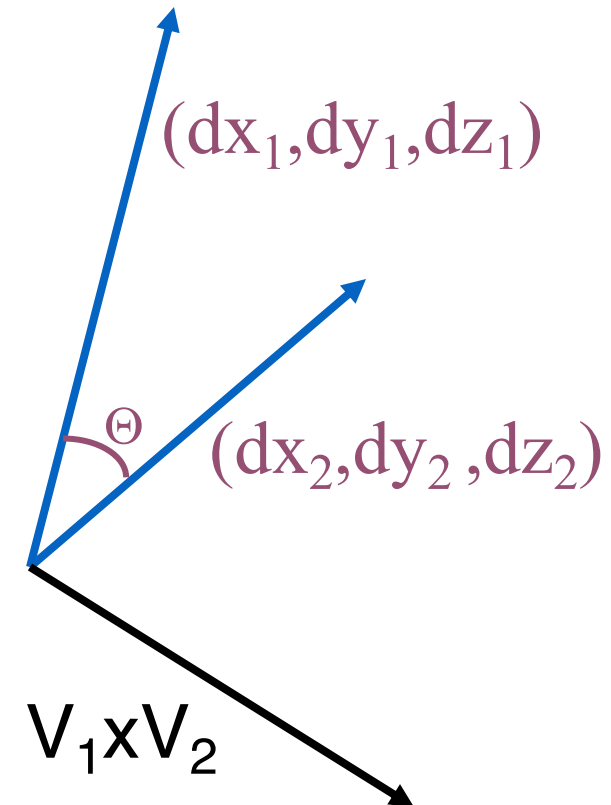
- Dot product of two 3D vectors
 - $V_1 \cdot V_2 = \|V_1\| \|V_2\| \cos(\Theta)$



3D Vector



- Cross product of two 3D vectors
 - $V_1 \times V_2$ = vector perpendicular to both V_1 and V_2
 - $\|V_1 \times V_2\| = \|V_1\| \|V_2\| \sin(\Theta)$

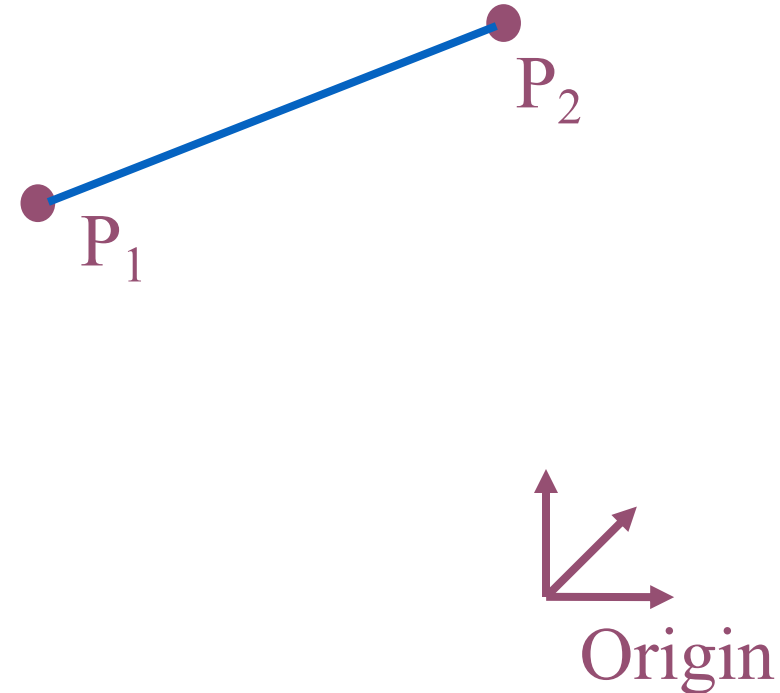


3D Line Segment



- Linear path between two points
 - Parametric representation:
 - $P = P_1 + t (P_2 - P_1), \quad (0 \leq t \leq 1)$

```
typedef struct {  
    Point P1;  
    Point P2;  
} Segment;
```

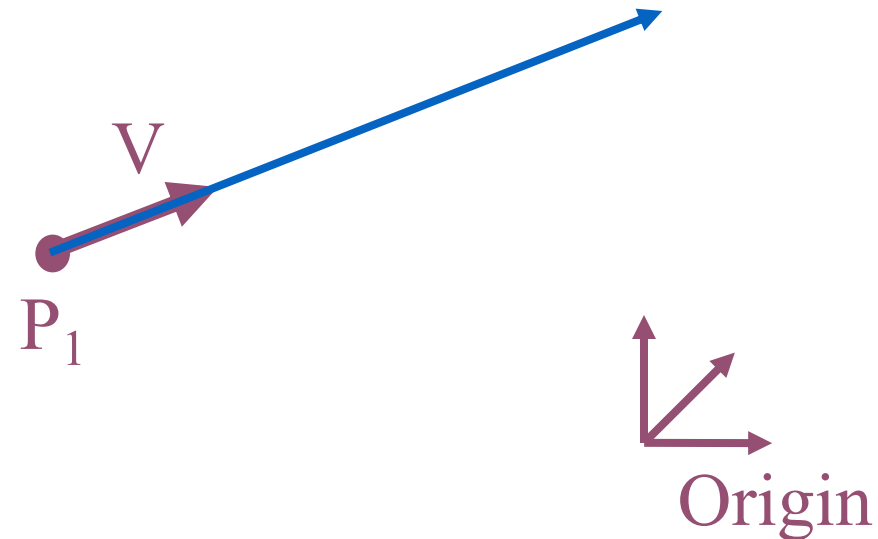


3D Ray



- Line segment with one endpoint at infinity
 - Parametric representation:
 - $P = P_1 + t V, \quad (0 \leq t < \infty)$

```
typedef struct {  
    Point P1;  
    Vector V;  
} Ray;
```

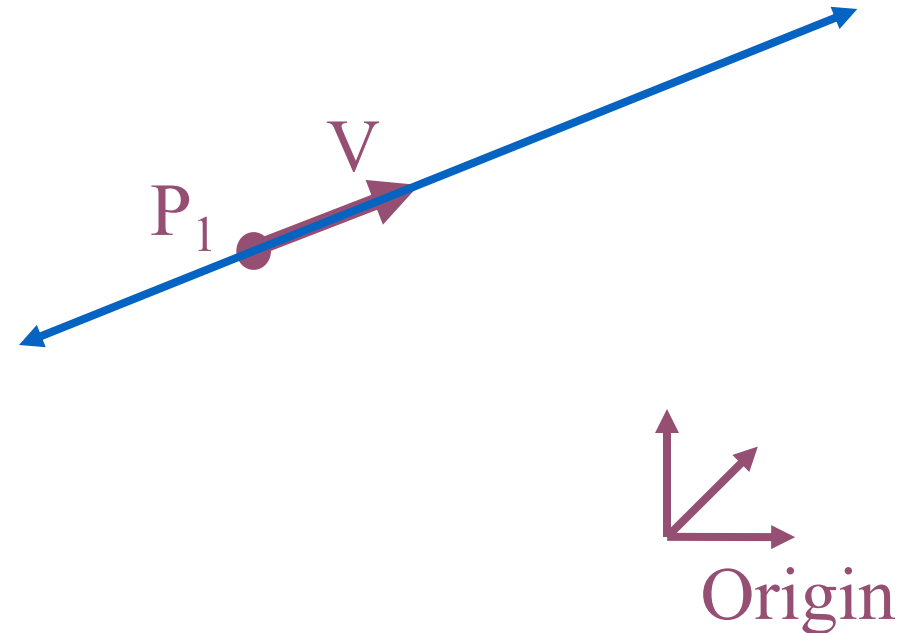


3D Line



- Line segment with both endpoints at infinity
 - Parametric representation:
 - $P = P_1 + t V, \quad (-\infty < t < \infty)$

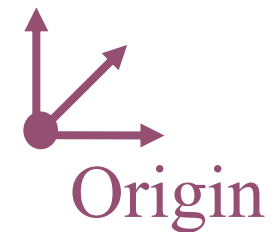
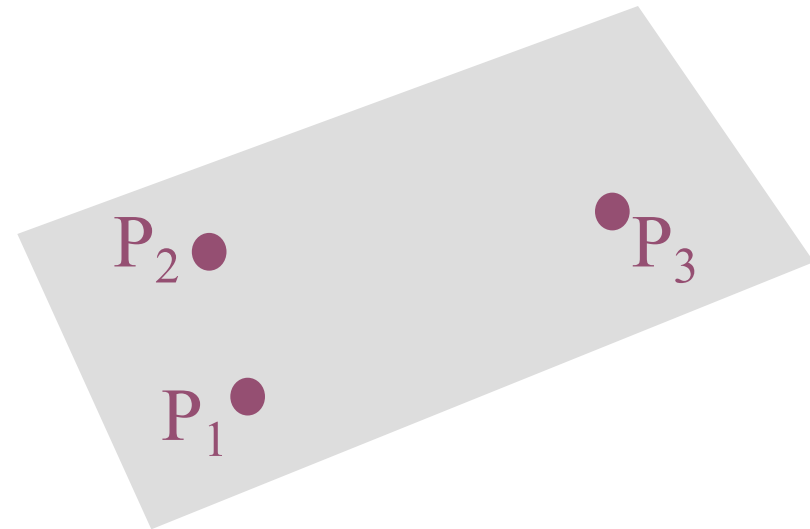
```
typedef struct {  
    Point P1;  
    Vector V;  
} Line;
```



3D Plane



- A linear combination of three points



3D Plane



- A linear combination of three points

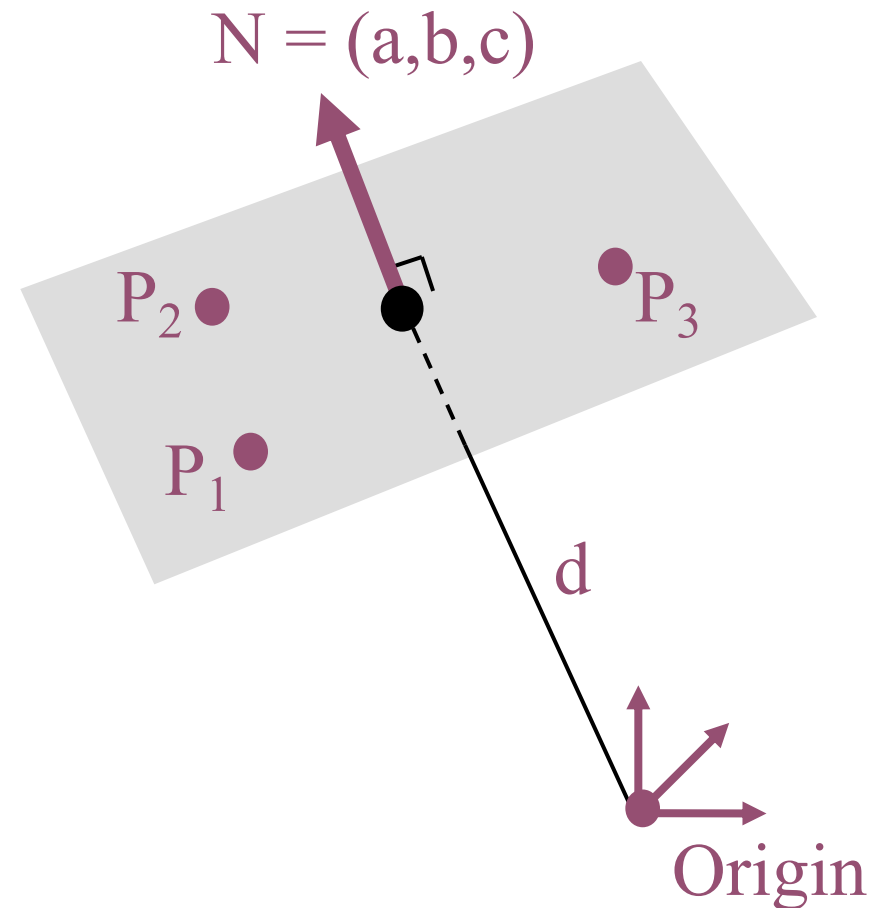
- Implicit representation:

- $P \cdot N - d = 0$, or
 - $ax + by + cz + d = 0$

```
typedef struct {  
    Vector N;  
    Distance d;  
} Plane;
```

- N is the plane “normal”

- Unit-length vector
 - Perpendicular to plane

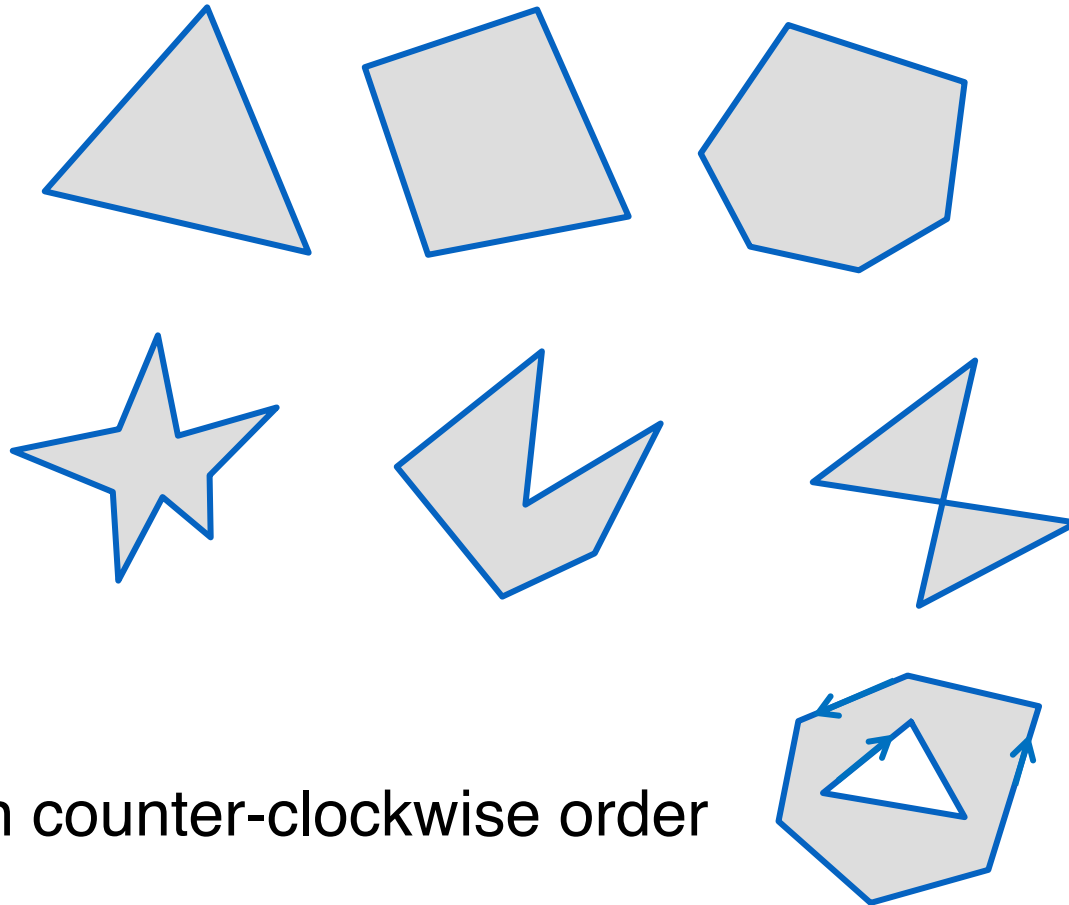


3D Polygon



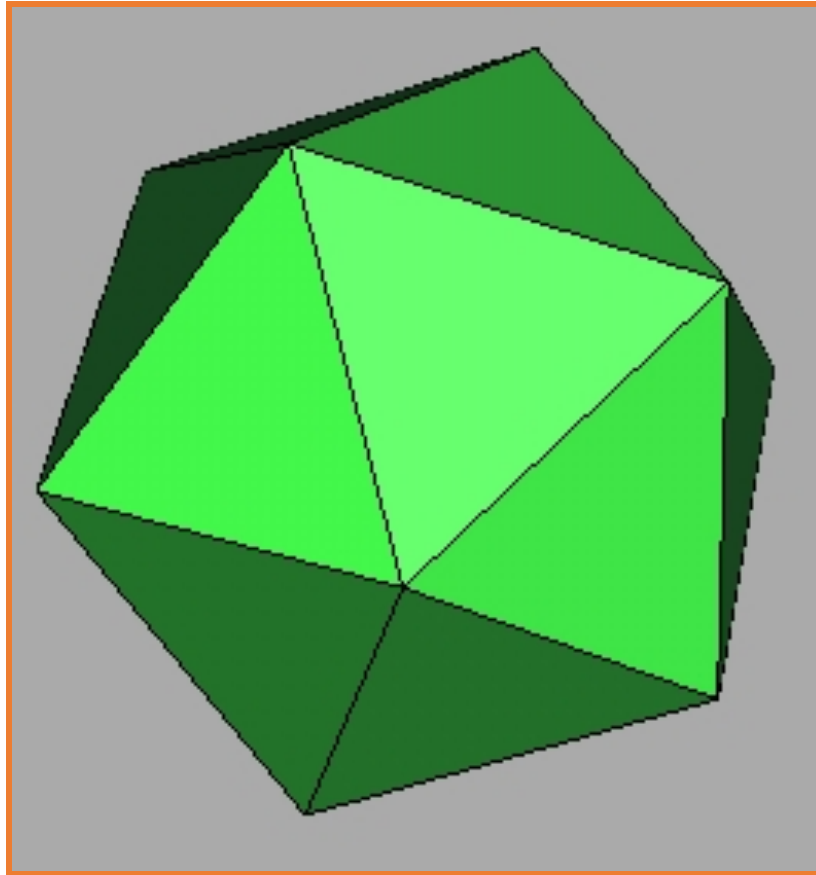
- Set of points “inside” a sequence of coplanar points

```
typedef struct {  
    Point *points;  
    int npoints;  
} Polygon;
```



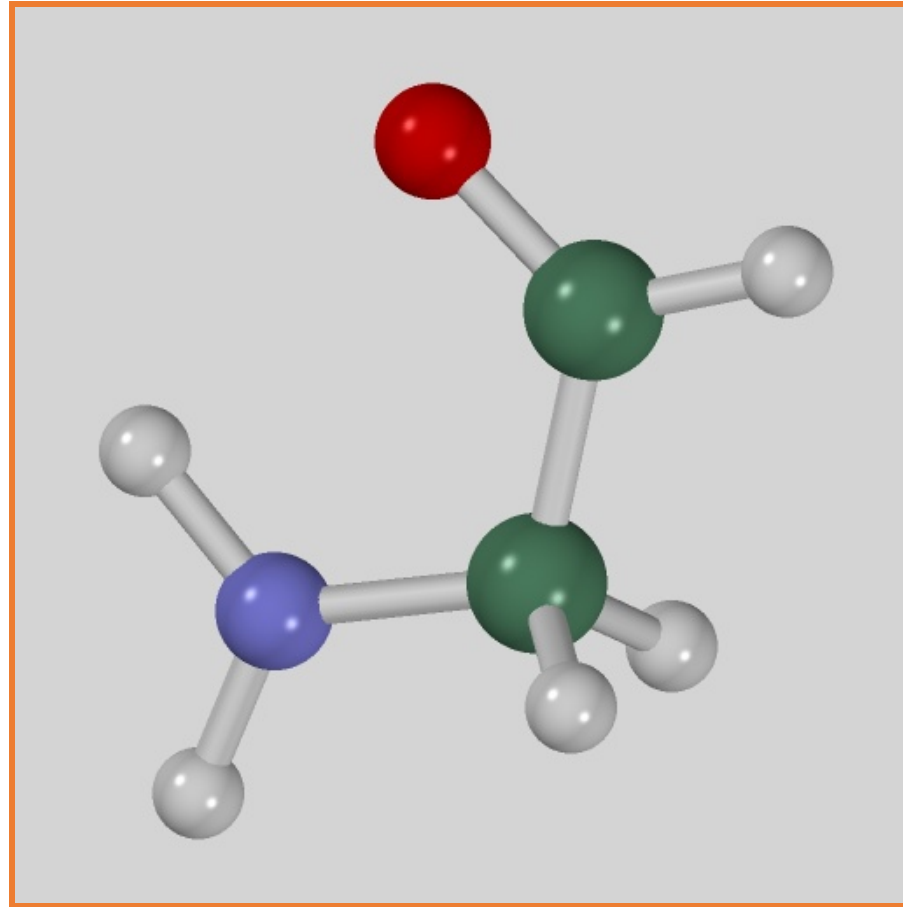
Points are in counter-clockwise order

3D Object Representations



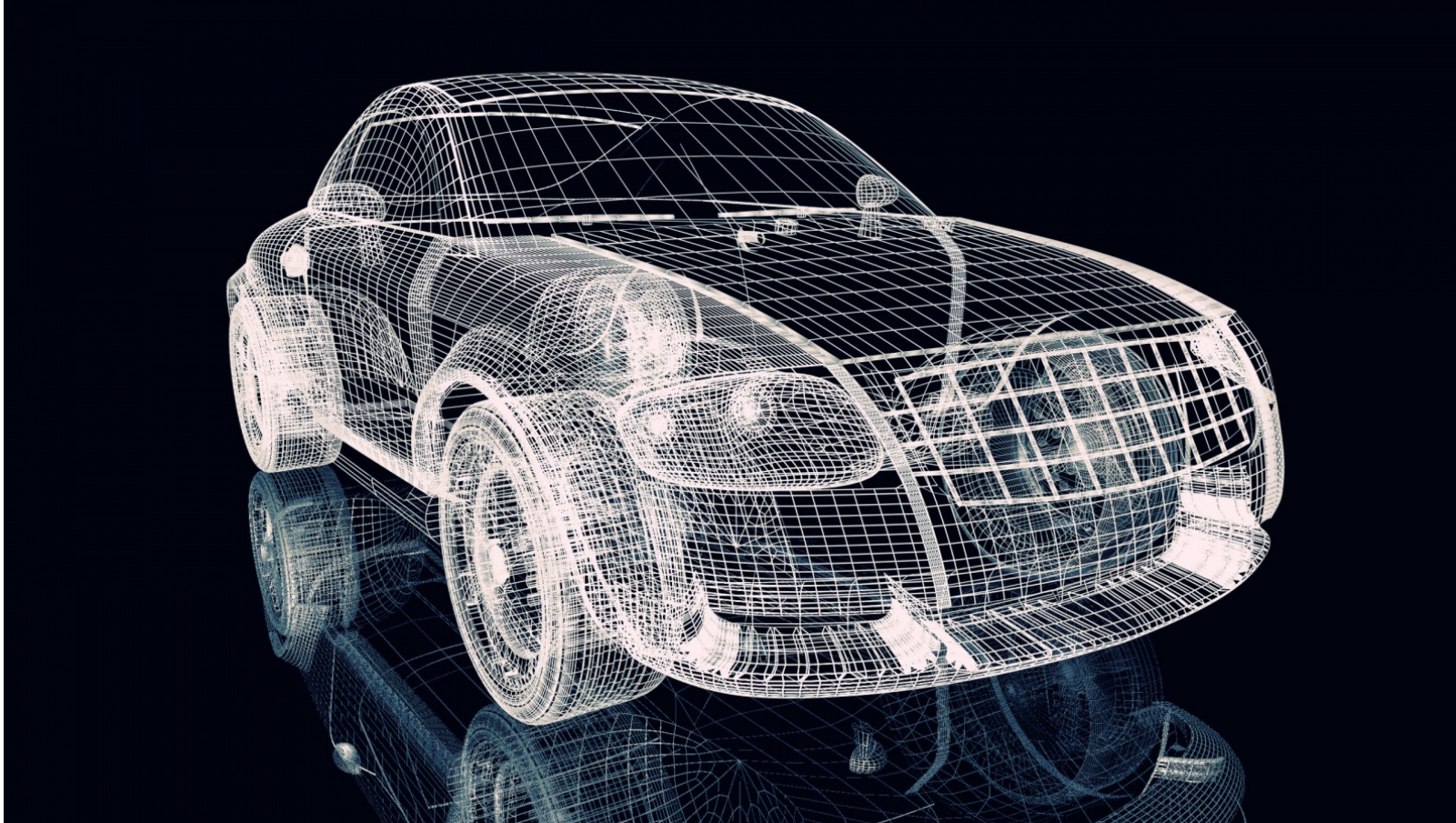
How can this object be represented in a computer?

3D Object Representations



How about this one?

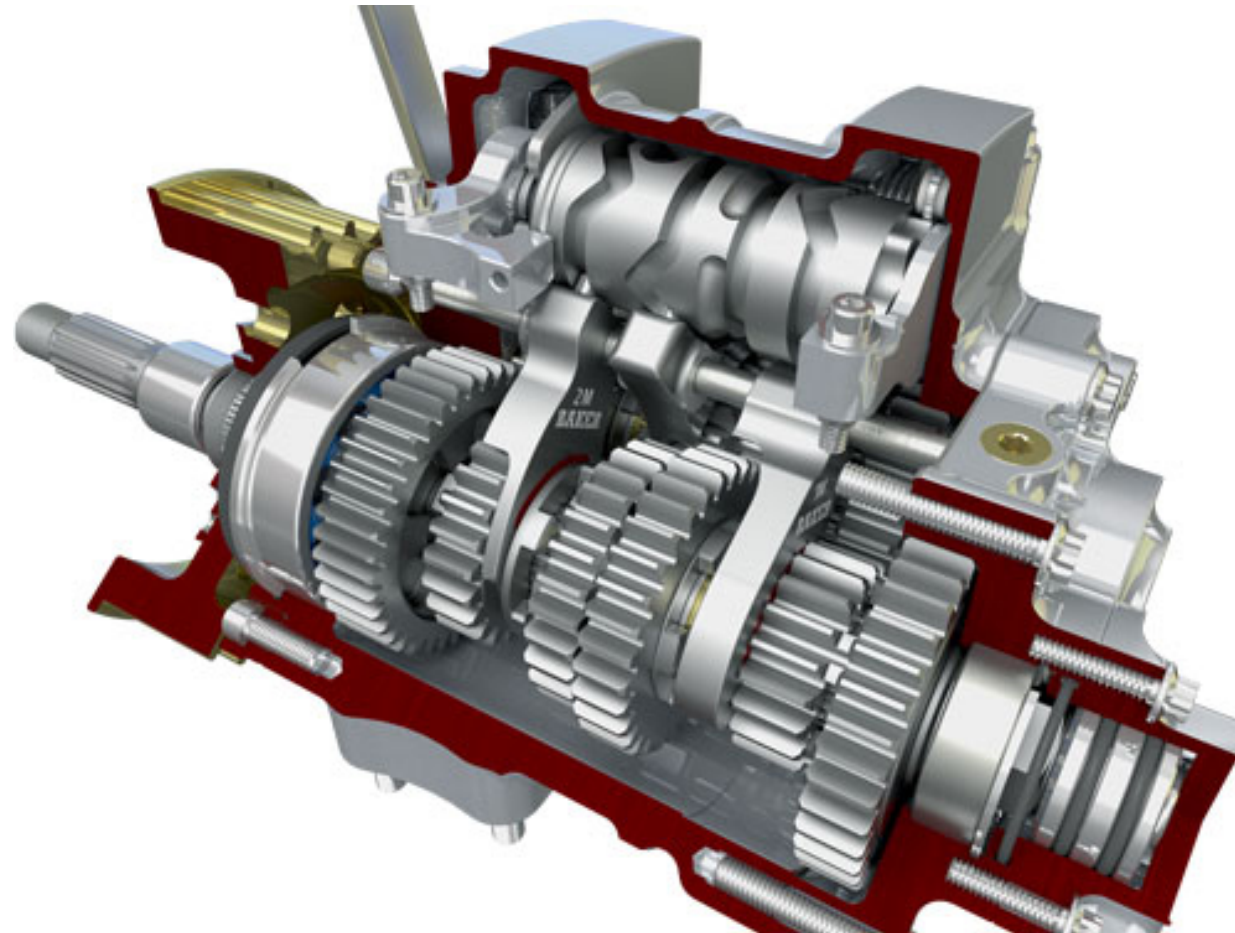
3D Object Representations



Wallpaperonly.net

This one?

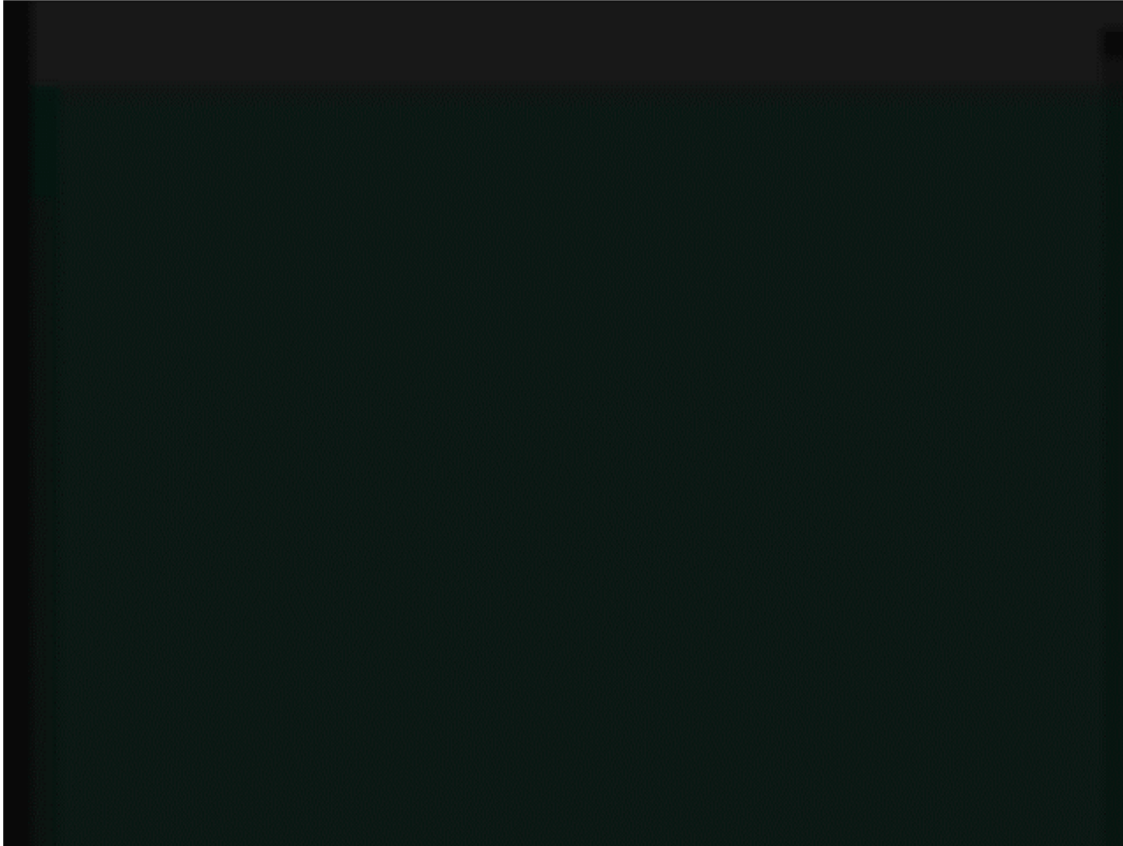
3D Object Representations



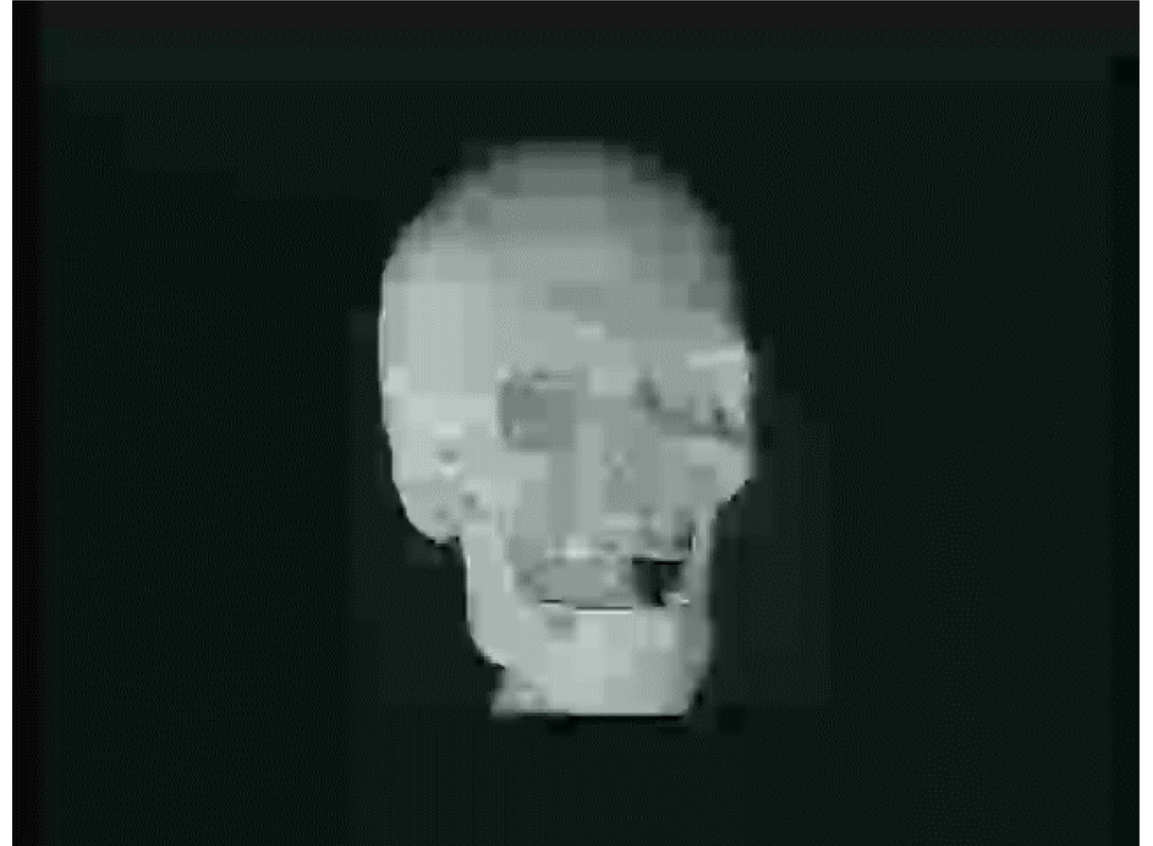
This one?

Solidworks

3D Object Representations

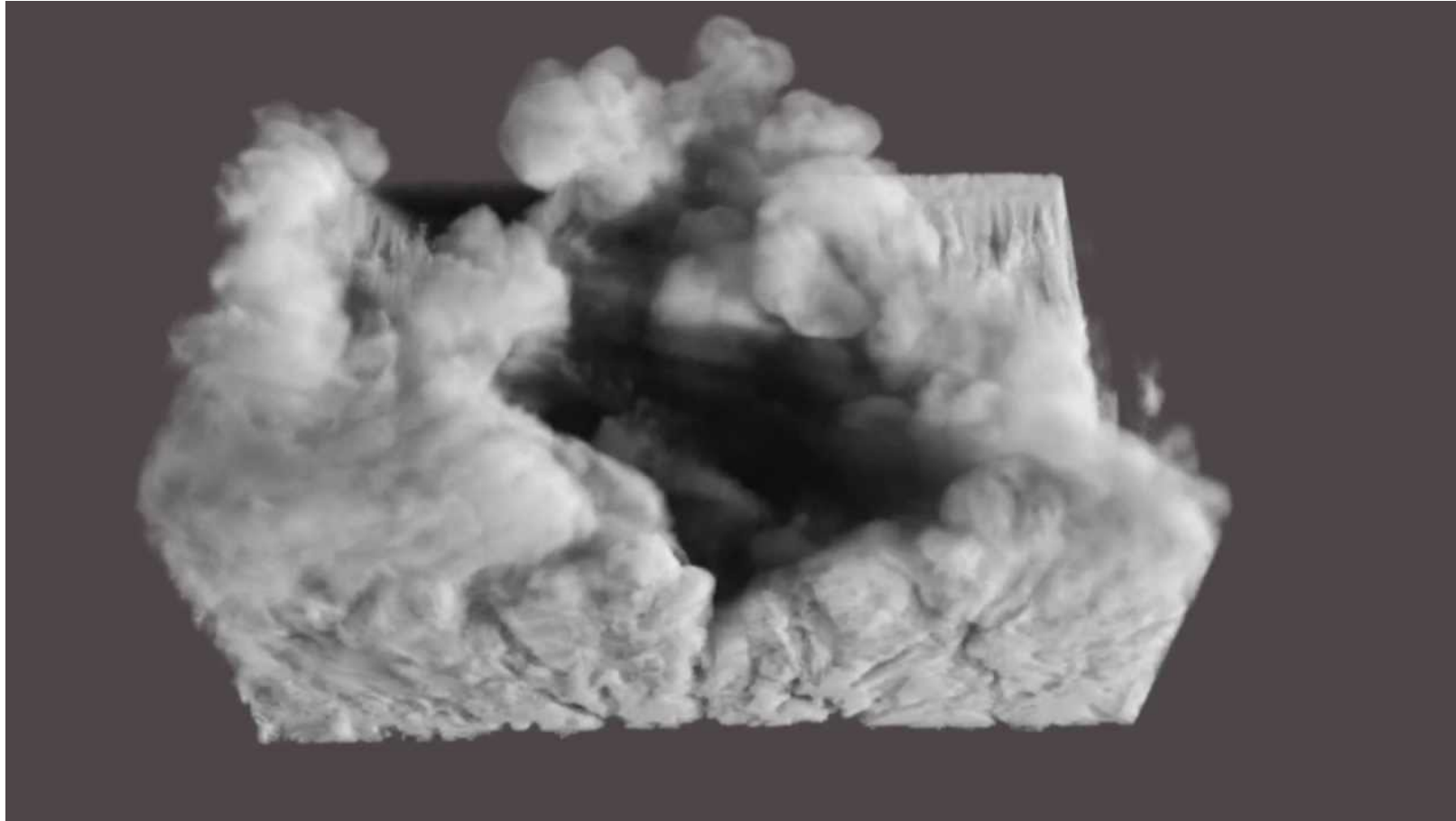


This one?



The visible human

3D Object Representations



This one?

FumeFx

3D Object Representations



- Points
 - Range image
 - Point cloud
- Surfaces
 - Polygonal mesh
 - Subdivision
 - Parametric
 - Implicit
- Solids
 - Voxels
 - BSP tree
 - CSG
 - Sweep
- High-level structures
 - Scene graph
 - Application specific

Equivalence of Representations



- Thesis:
 - Each representation has enough expressive power to model the shape of any geometric object
 - It is possible to perform all geometric operations with any fundamental representation
- Analogous to Turing-equivalence
 - Computers and programming languages are Turing-equivalent, but each has its benefits...

Why Different Representations?



Efficiency for different tasks

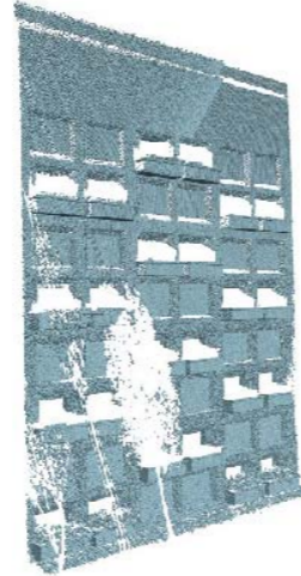
- Acquisition
- Rendering
- Analysis
- Manipulation
- Animation

Data structures determine algorithms

Why Different Representations?

Efficiency for different tasks

- Acquisition
 - Range Scanning
- Rendering
- Analysis
- Manipulation
- Animation



Live Body Scan
Data acquired in 0.01 seconds



Why Different Representations?



Efficiency for different tasks

- Acquisition
 - Computer Vision
- Rendering
- Analysis
- Manipulation
- Animation



Indiana
University



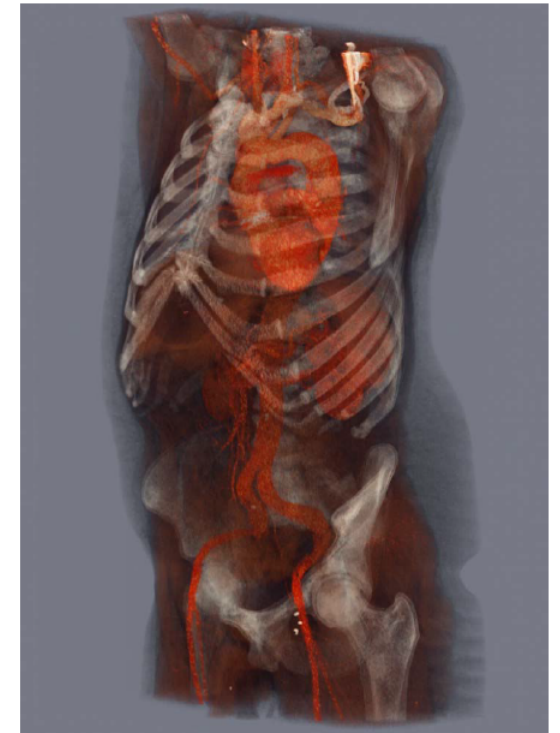
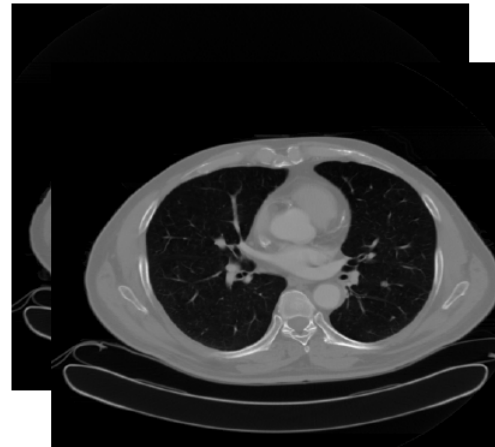
USC

Why Different Representations?



Efficiency for different tasks

- Acquisition
 - Tomography
- Rendering
- Analysis
- Manipulation
- Animation



DGP course notes, Technion

Why Different Representations?



Efficiency for different tasks

- Acquisition
- **Rendering**
 - **Intersection**
- Analysis
- Manipulation
- Animation

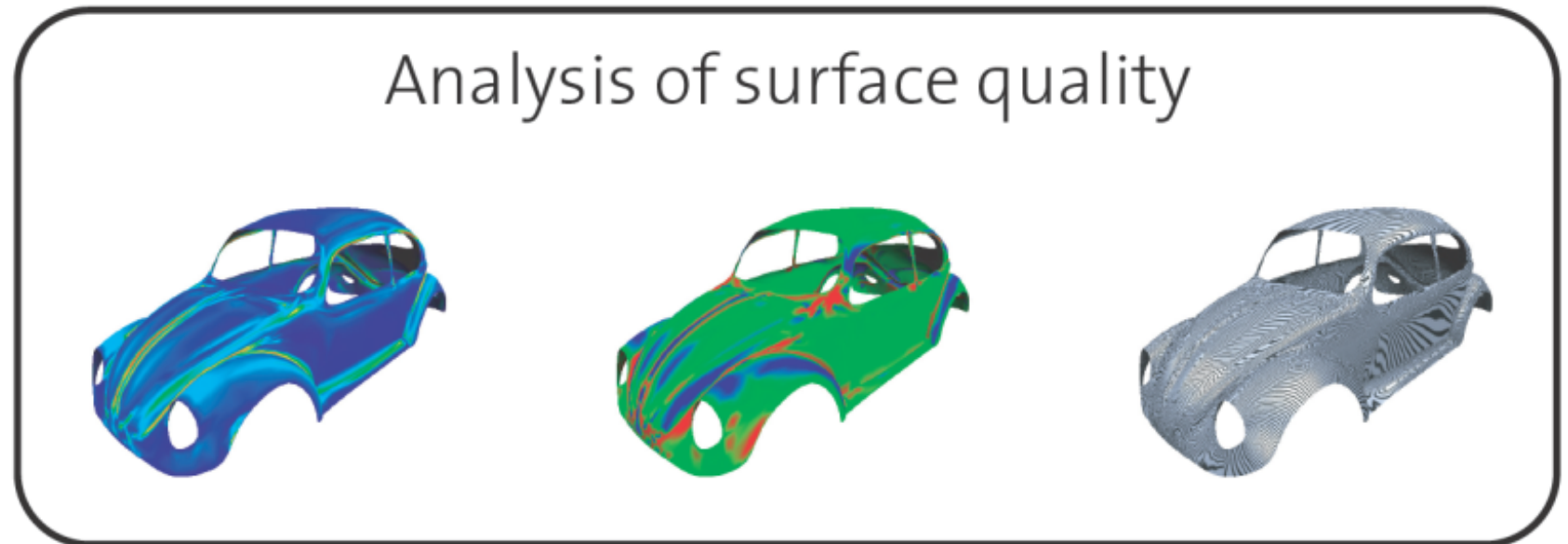


Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- **Analysis**
 - Curvature, smoothness
- Manipulation
- Animation



DGP course notes, Technion

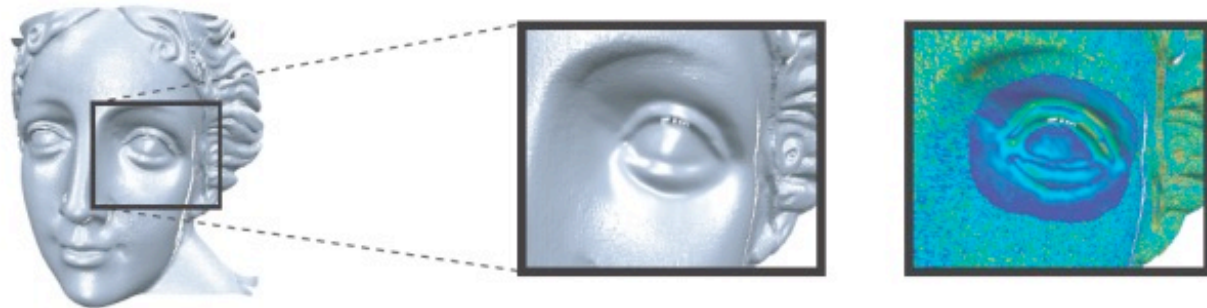
Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- **Analysis**
 - **Fairing**
- Manipulation
- Animation

Surface smoothing for noise removal



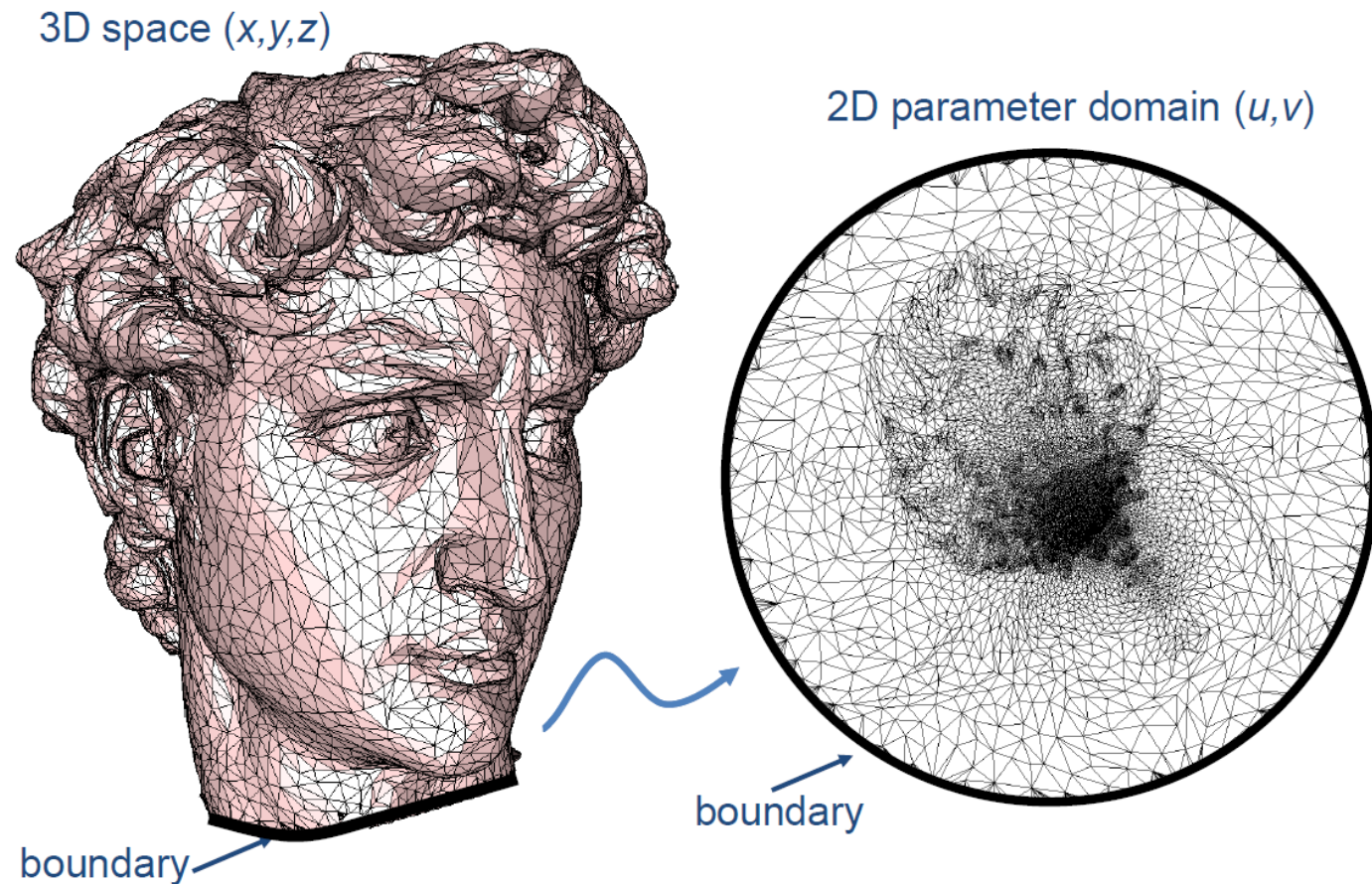
DGP course notes, Technion

Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
 - Parametrization
- Manipulation
- Animation



Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- **Analysis**
 - **Texture mapping**
- Manipulation
- Animation

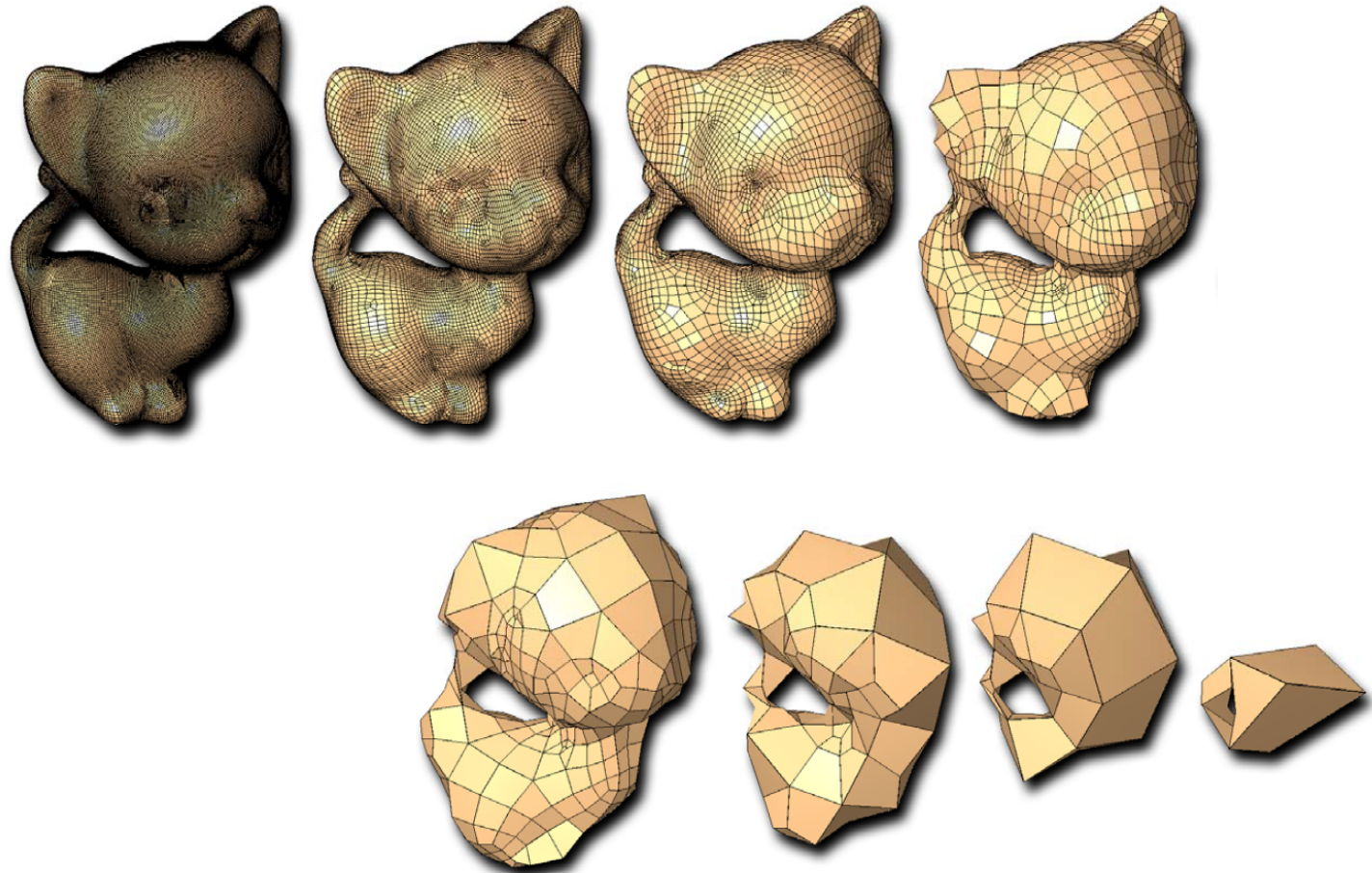


Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
 - Reduction
- Manipulation
- Animation

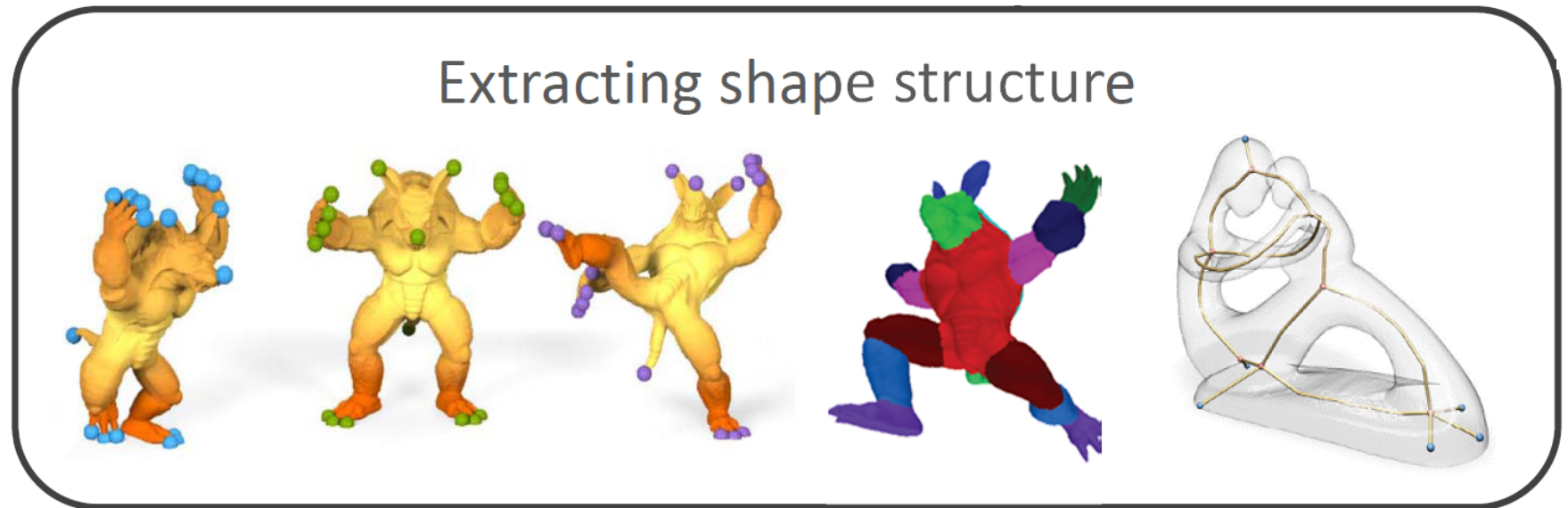


Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- **Analysis**
 - **Structure**
- Manipulation
- Animation



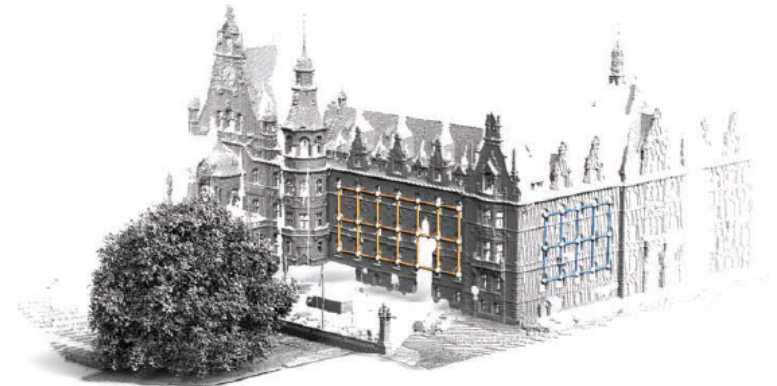
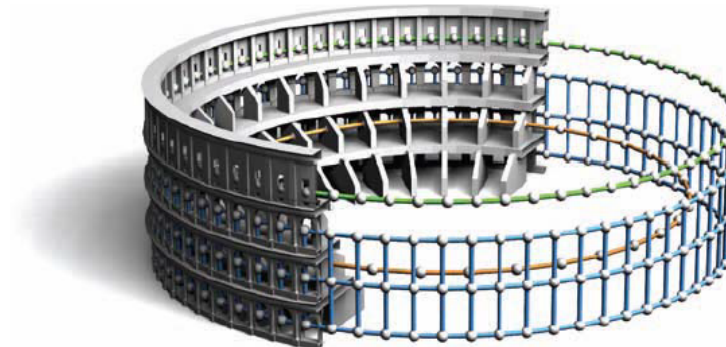
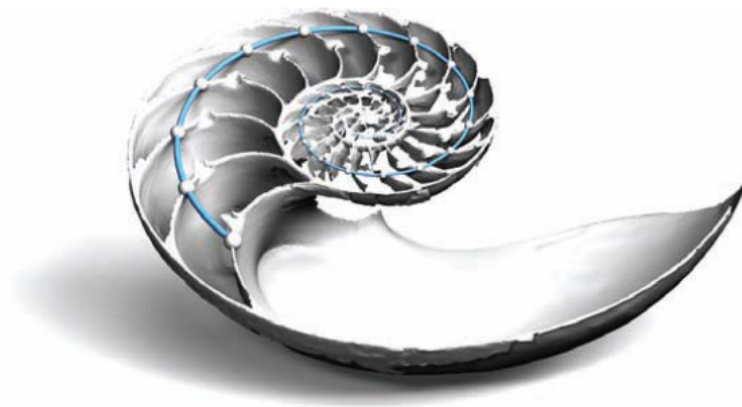
DGP course notes, Technion

Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- **Analysis**
 - Symmetry detection
- Manipulation
- Animation

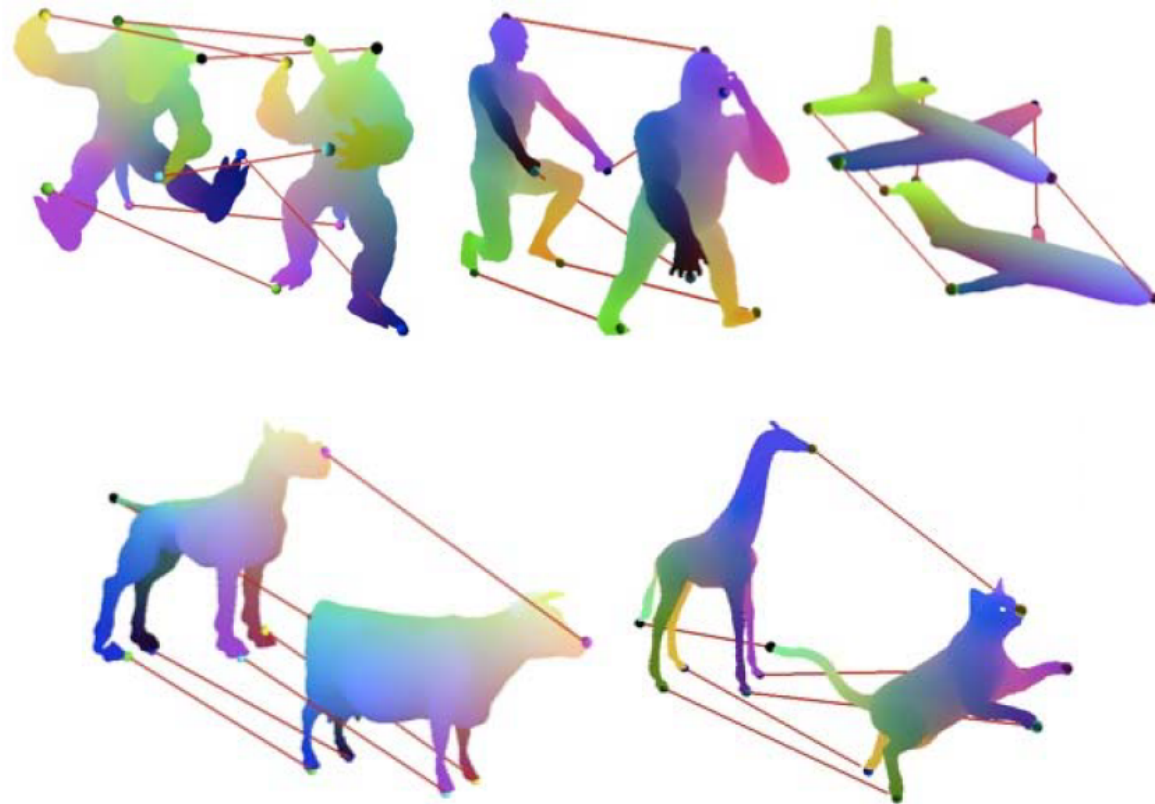


Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- **Analysis**
 - Correspondence
- Manipulation
- Animation

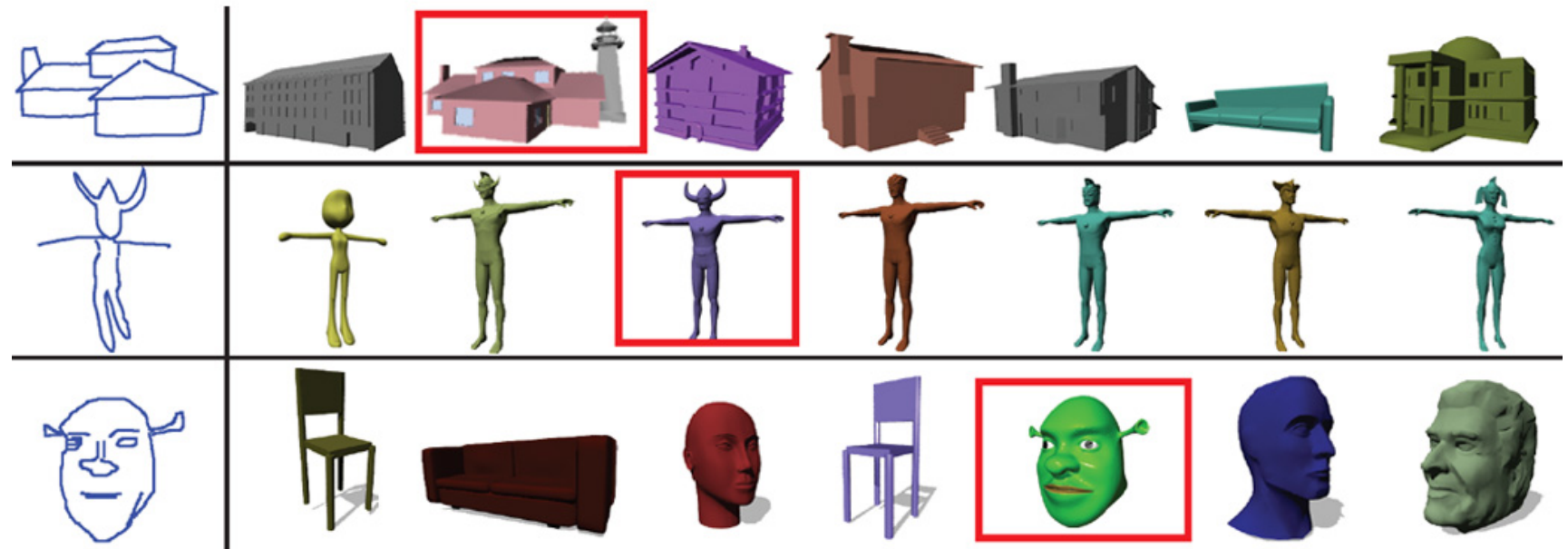


Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- **Analysis**
 - Shape retrieval
- Manipulation
- Animation



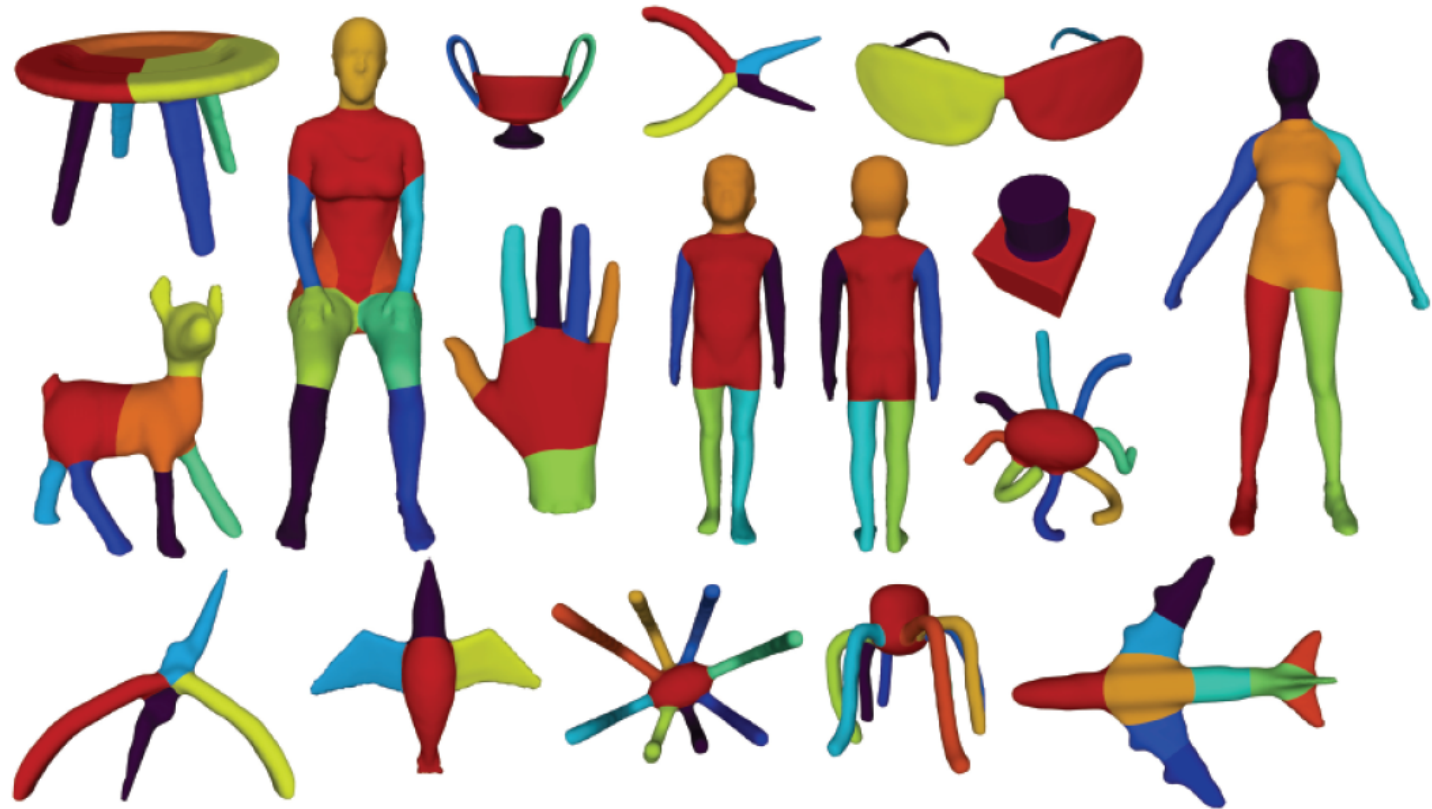
Shao et al. 2011

Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- **Analysis**
 - **Segmentation**
- Manipulation
- Animation

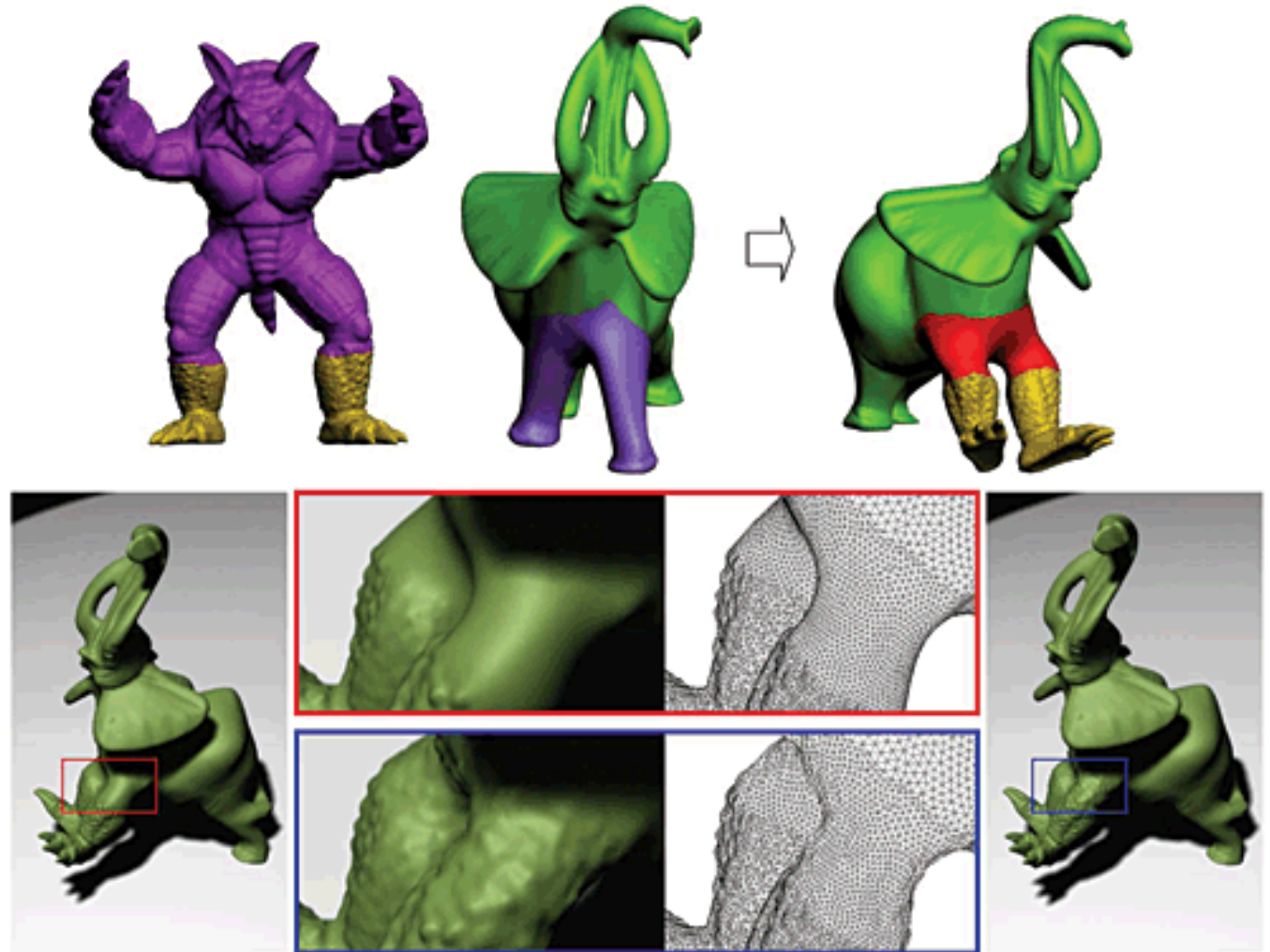


Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
 - Composition
- Manipulation
- Animation



Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
- **Manipulation**
 - Deformation
- Animation



IGL

Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
- **Manipulation**
 - Deformation
- Animation

Freeform and multiresolution modeling



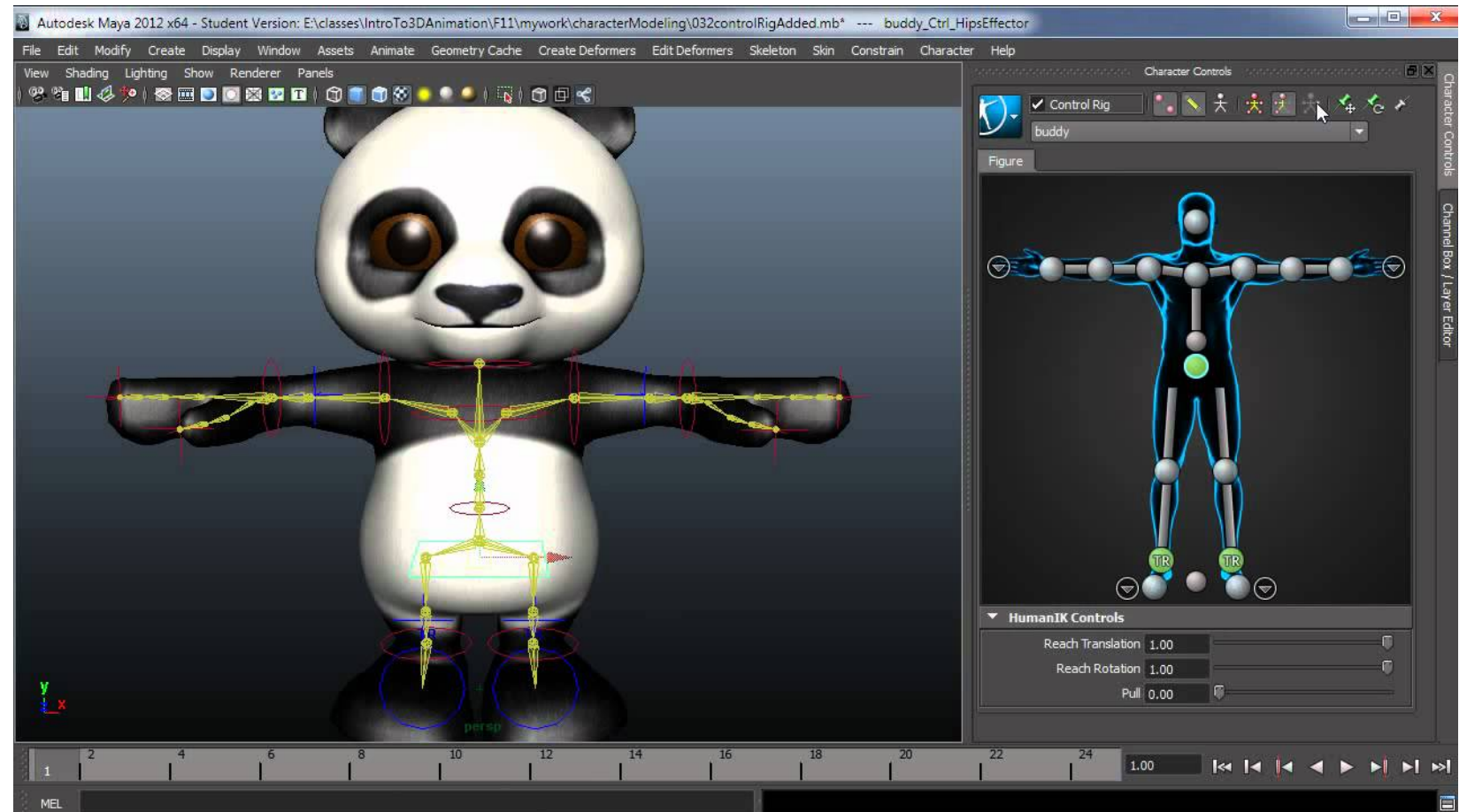
DGP course notes, Technion

Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
- **Manipulation**
 - **Control**
- Animation



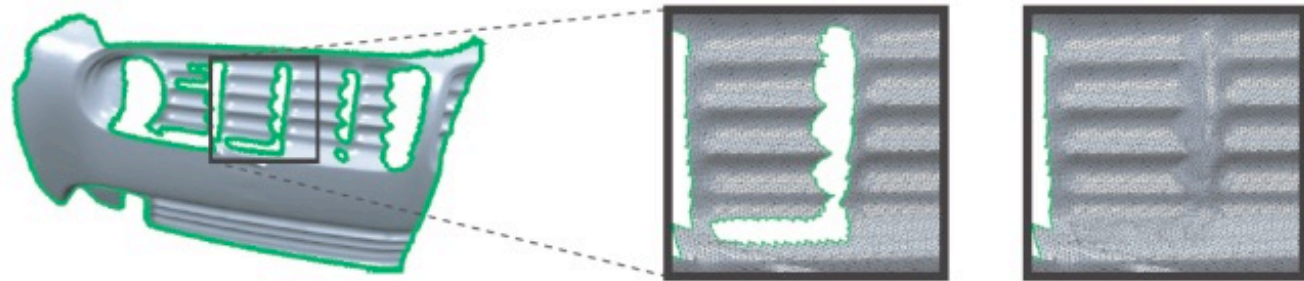
Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
- **Manipulation**
 - Healing
- Animation

Removal of topological and geometrical errors



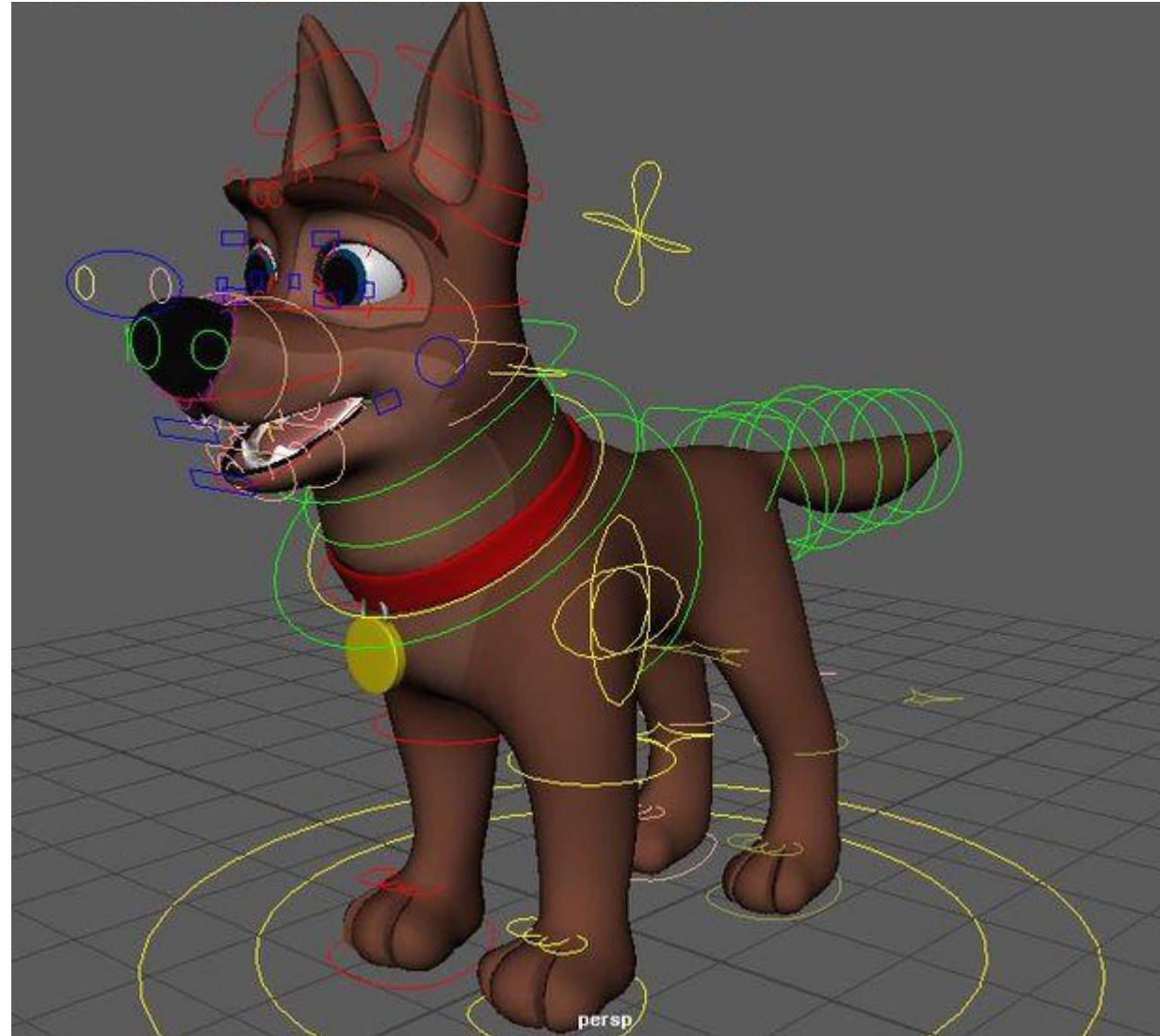
DGP course notes, Technion

Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
- Manipulation
- **Animation**
 - Rigging



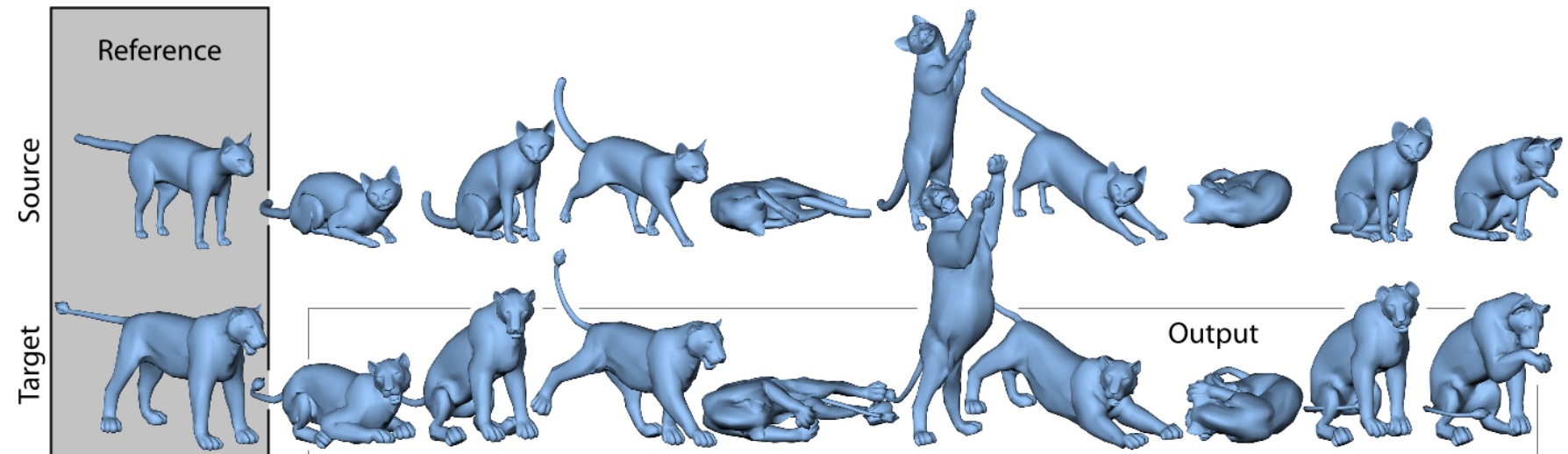
Animation
Buffet

Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
- Manipulation
- **Animation**
 - Deformation transfer



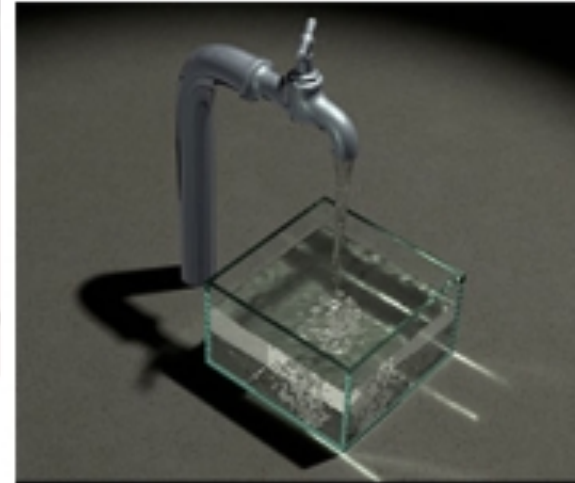
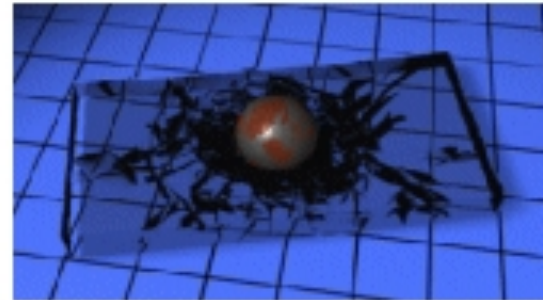
Sumner et al. 2004

Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
- Manipulation
- **Animation**
 - **Simulation**

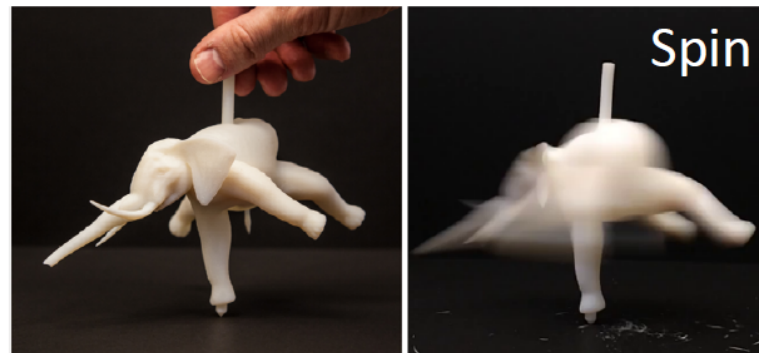


Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
- Manipulation
- **Animation**
 - **Fabrication**



3D Object Representations



- Points
 - Range image
 - Point cloud
- Surfaces
 - Polygonal mesh
 - Subdivision
 - Parametric
 - Implicit
- Solids
 - Voxels
 - BSP tree
 - CSG
 - Sweep
- High-level structures
 - Scene graph
 - Application specific

3D Object Representations



- Points

- Range image
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- High-level structures

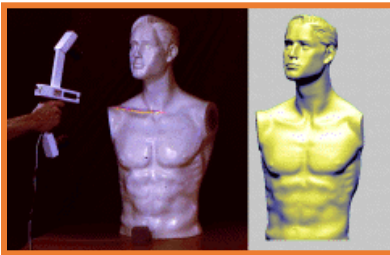
- Scene graph
- Application specific

Range Image

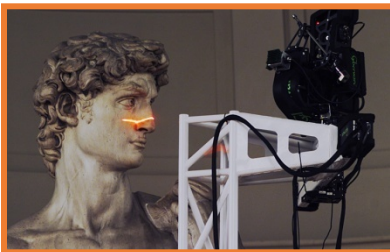


Set of 3D points mapping to pixels of depth image

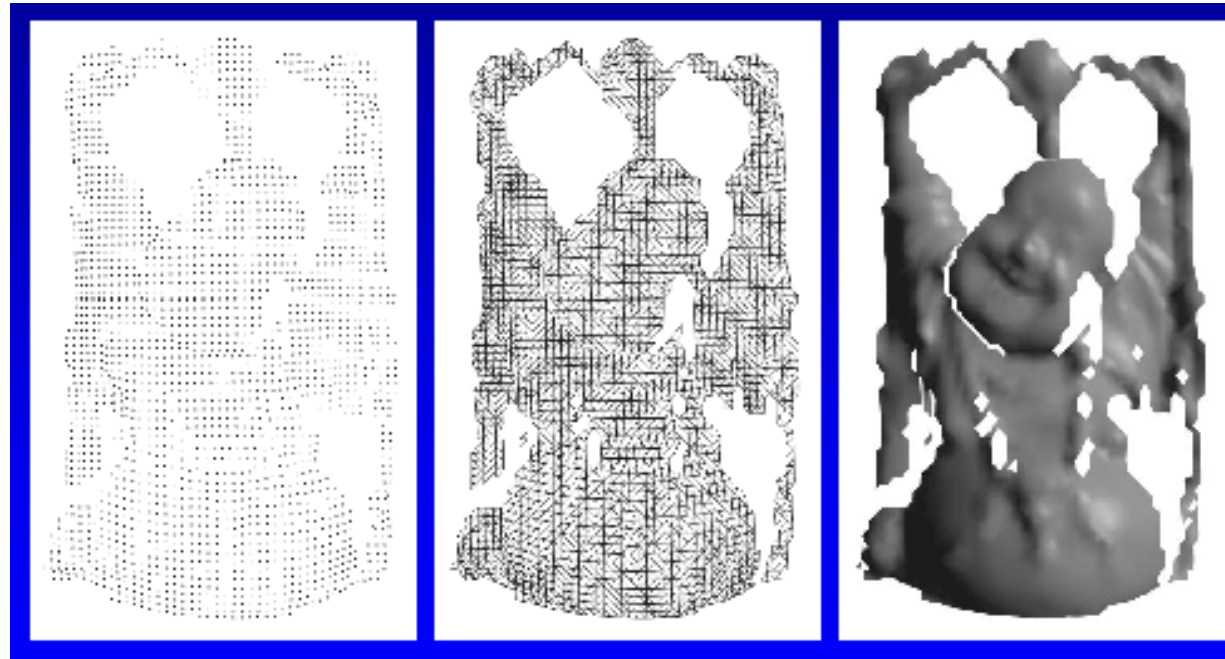
- Can be acquired from range scanner



Cyberware



Stanford



Range Image

Tessellation

Range Surface

Point Cloud



Unstructured set of 3D point samples

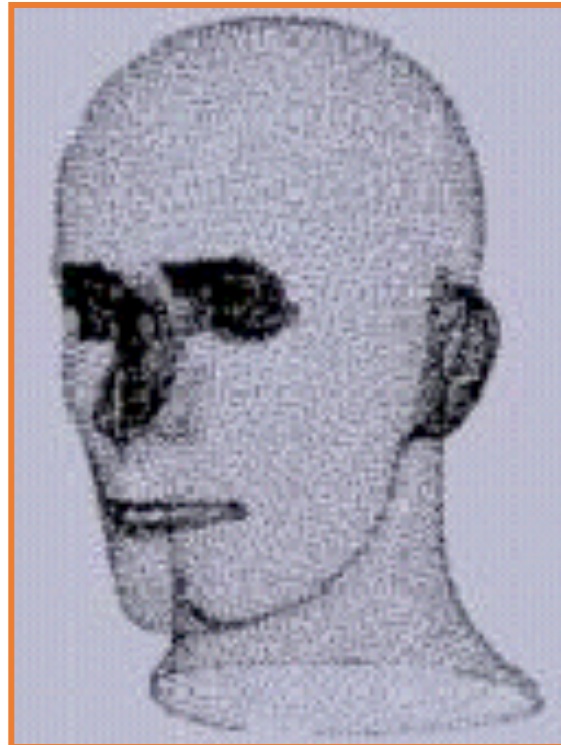
- Acquired from range finder, computer vision, etc



Polhemus



Microscribe-3D



Hoppe



Hoppe

3D Object Representations

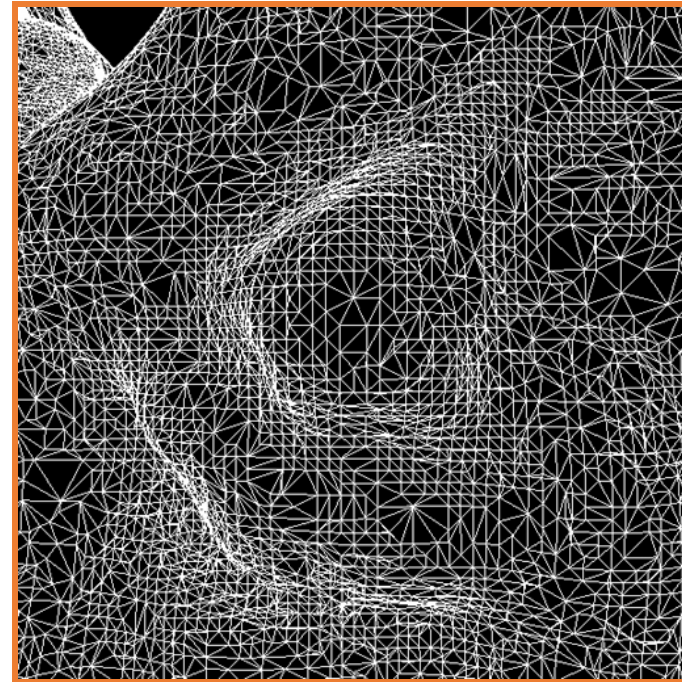


- Points
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Polygonal Mesh



Connected set of polygons (often triangles)

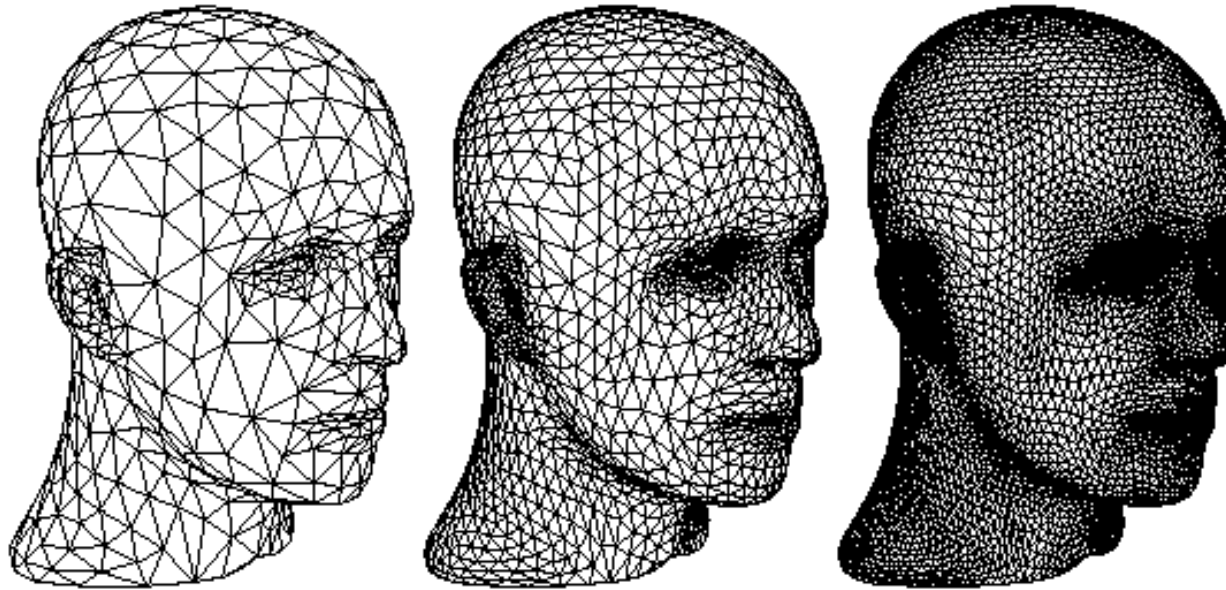


Subdivision Surface



Coarse mesh & subdivision rule

- Smooth surface is **limit** of sequence of refinements



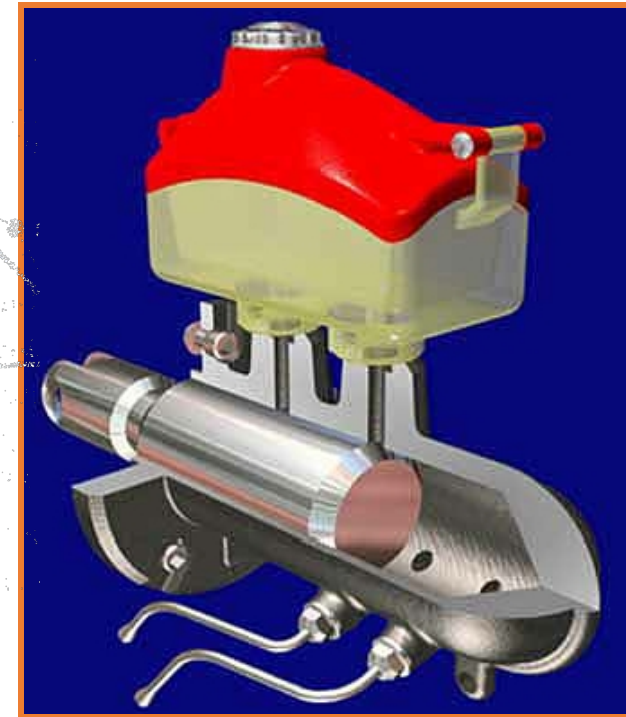
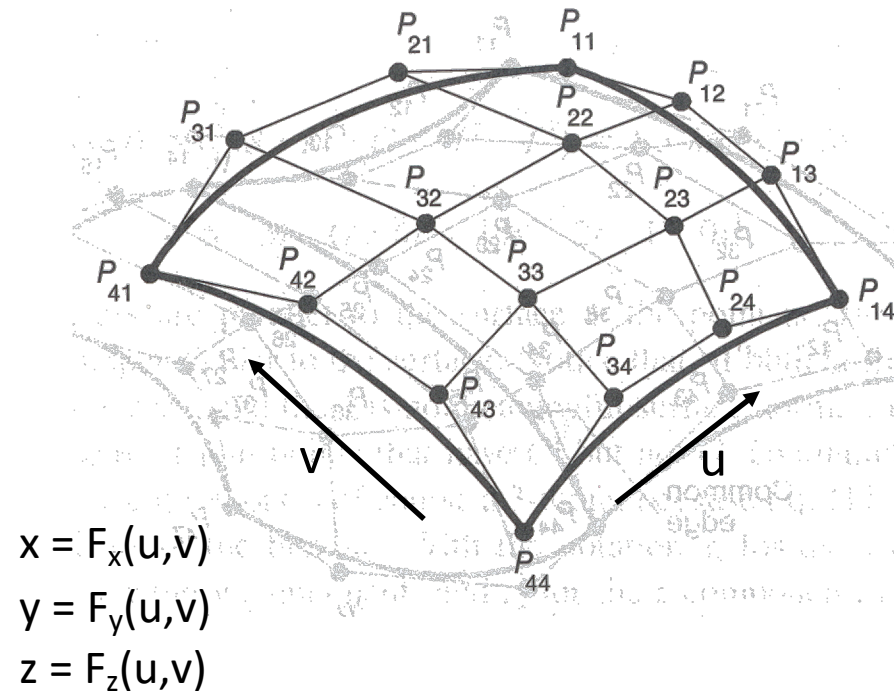
Zorin & Schroeder
SIGGRAPH 99
Course Notes

Parametric Surface



Tensor-product spline patches

- Each patch is parametric function
- Careful constraints to maintain continuity

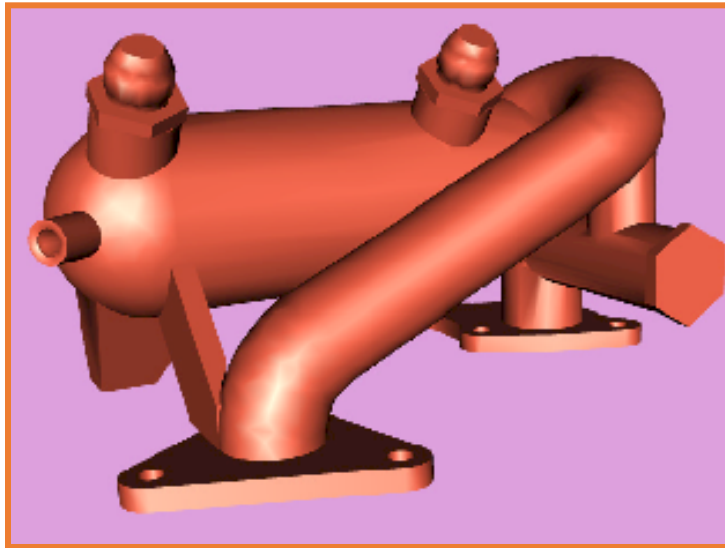


FvDFH Figure 11.44

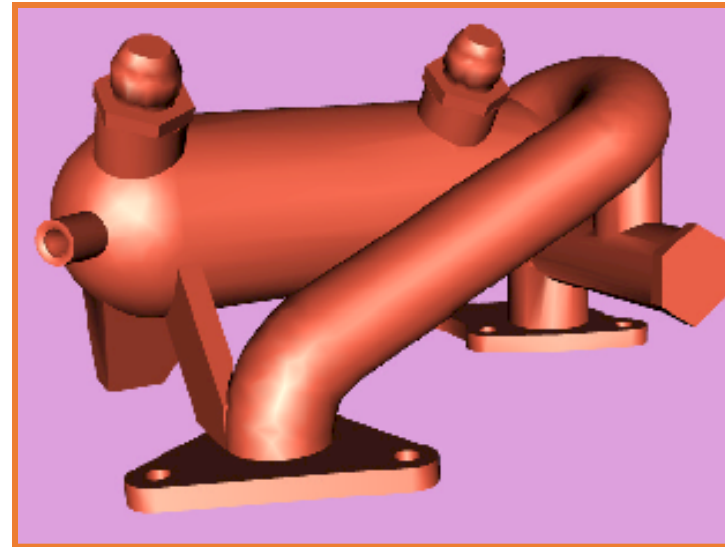
Implicit Surface



Set of all points satisfying: $F(x,y,z) = 0$



Polygonal Model



Implicit Model

Bill Lorensen
SIGGRAPH 99
Course #4 Notes

3D Object Representations



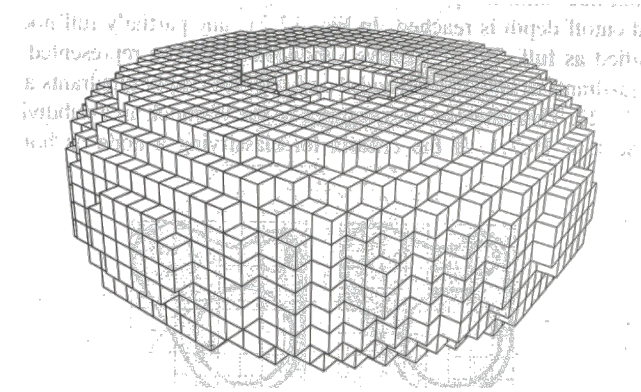
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Voxel grid

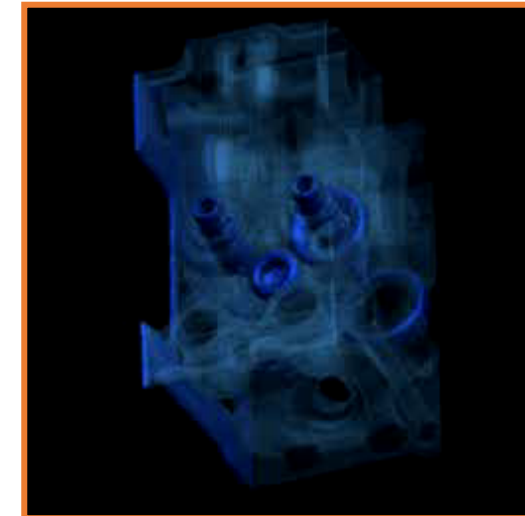


Uniform volumetric grid of samples:

- Occupancy
(object vs. empty space)
- Density
- Color
- Other function
(speed, temperature, etc.)
- Often acquired via
simulation or from
CAT, MRI, etc.



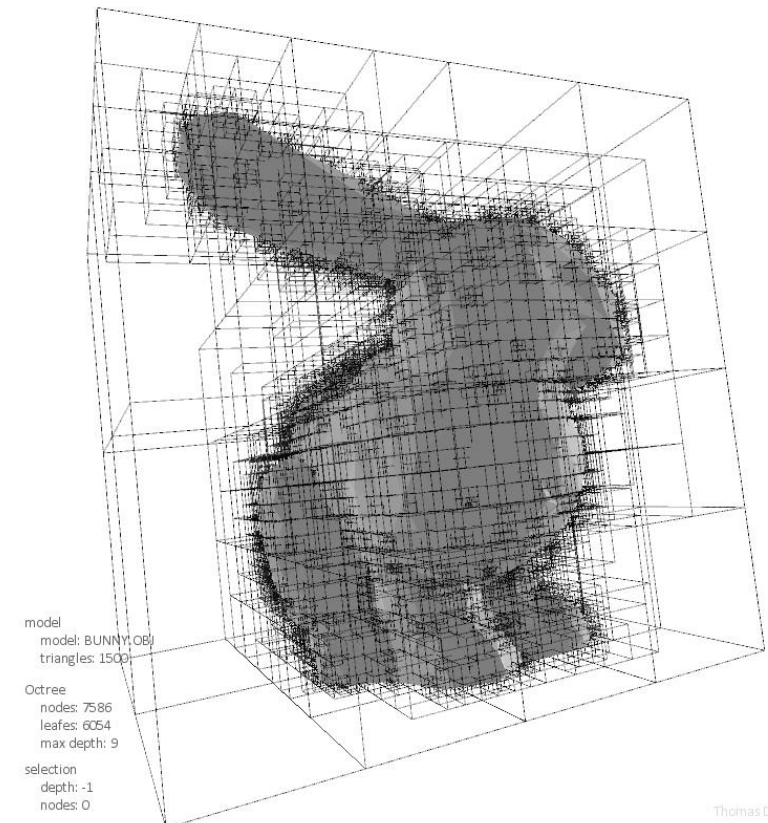
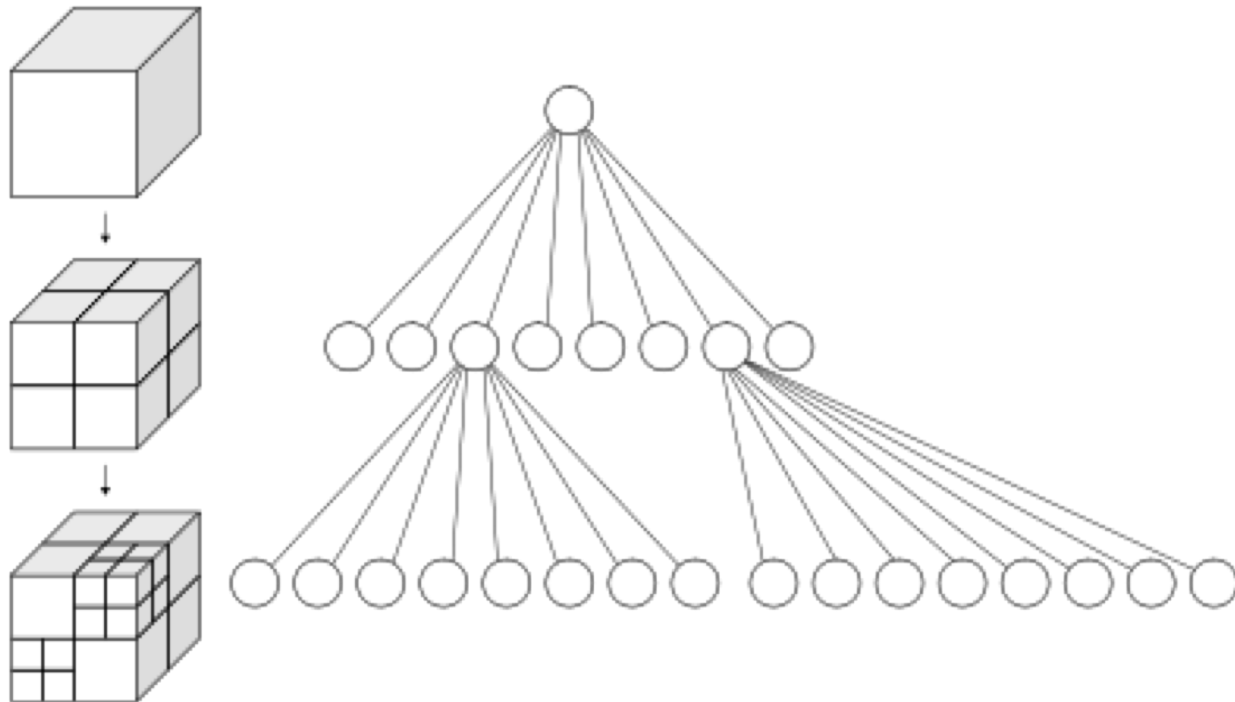
FvDFH Figure 12.20



Octree

The adaptive version of the voxel grid

- Significantly more space efficient
- Makes operations more cumbersome



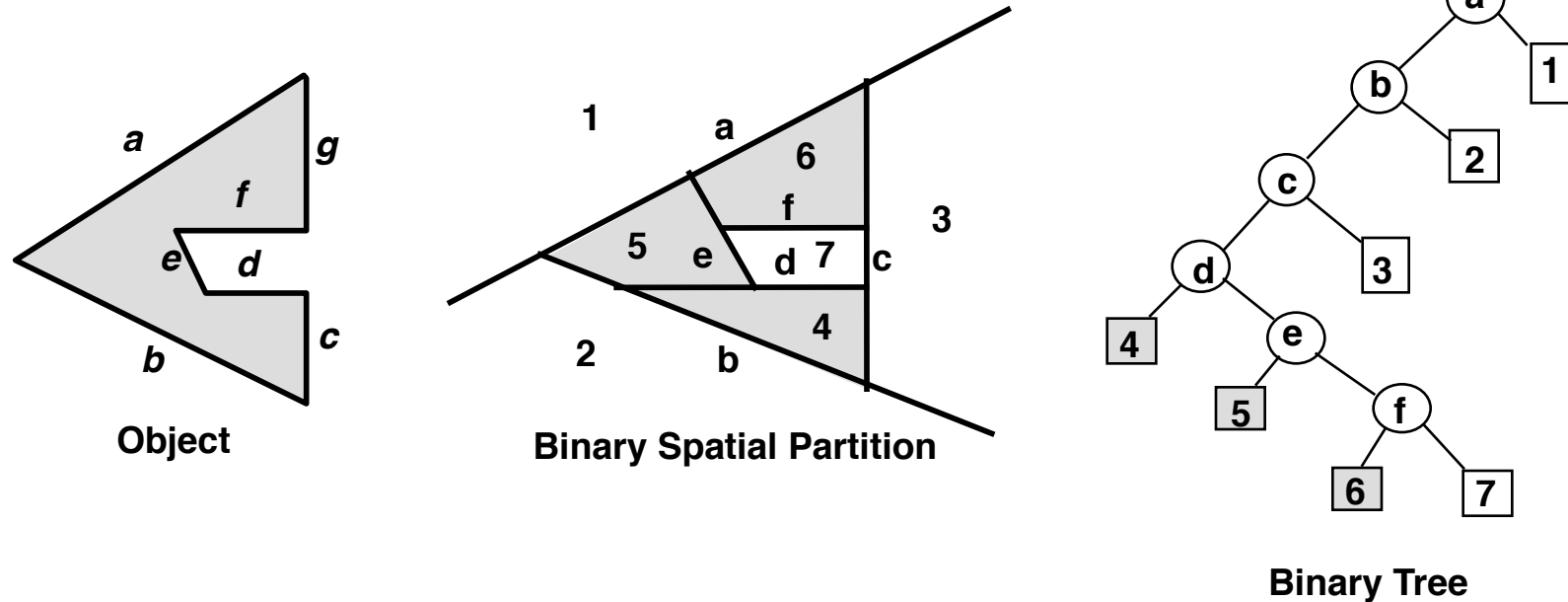
Thomas Diewald

BSP Tree

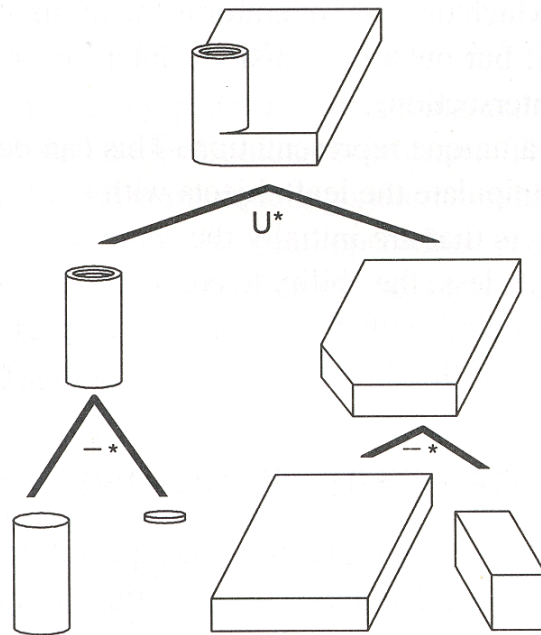


Hierarchical **B**inary **S**pace **P**artition with solid/empty cells labeled

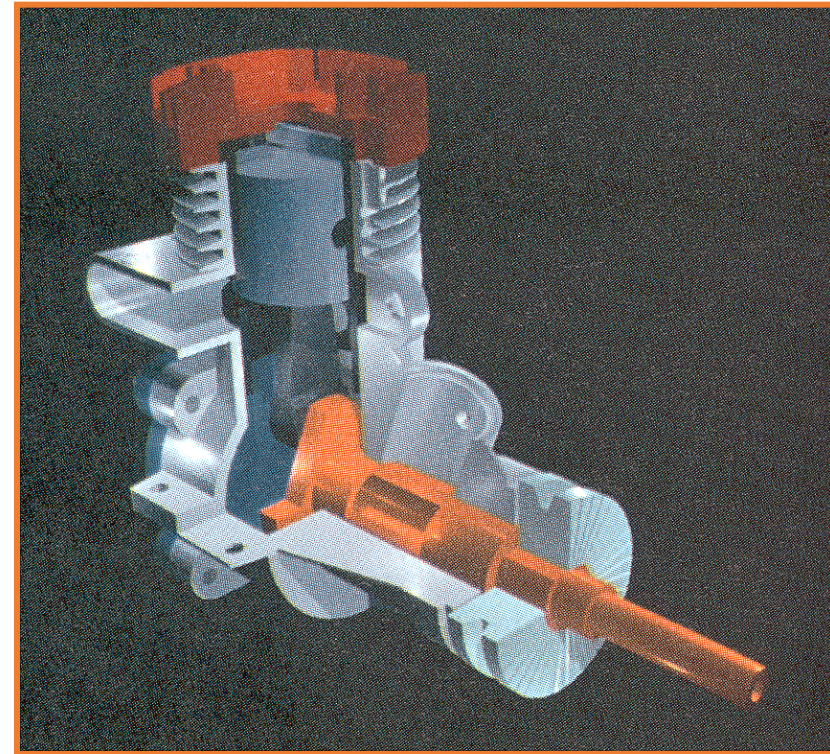
- Constructed from polygonal representations



Constructive **S**olid **G**eometry: set operations (union, difference, intersection) applied to simple shapes



FvDFH Figure 12.27

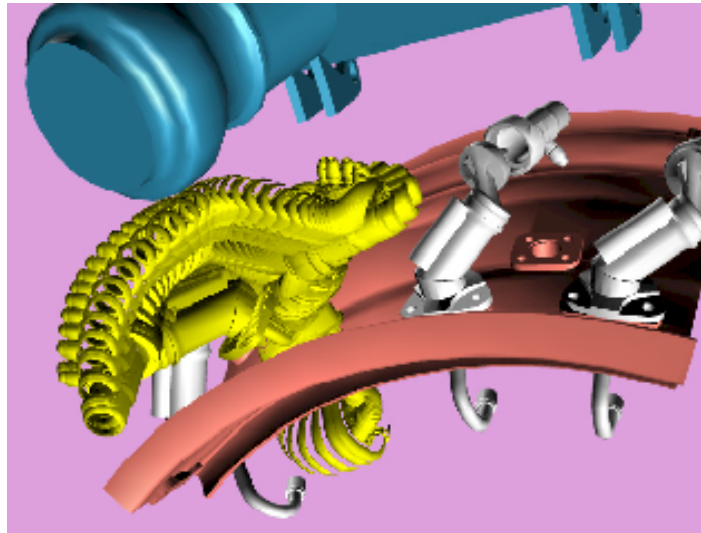


H&B Figure 9.9

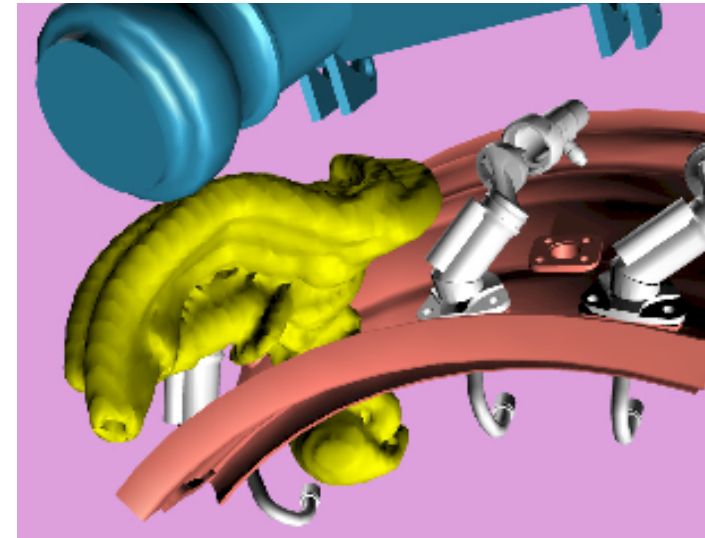
Sweep



Solid swept by curve along trajectory



Removal Path



Sweep Model

Bill Lorensen
SIGGRAPH 99
Course #4 Notes

3D Object Representations



- Points
 - Range image
 - Point cloud
- Surfaces
 - Polygonal mesh
 - Subdivision
 - Parametric
 - Implicit
- Solids
 - Voxels
 - BSP tree
 - CSG
 - Sweep
- High-level structures
 - Scene graph
 - Application specific

Scene Graph



Union of objects at leaf nodes

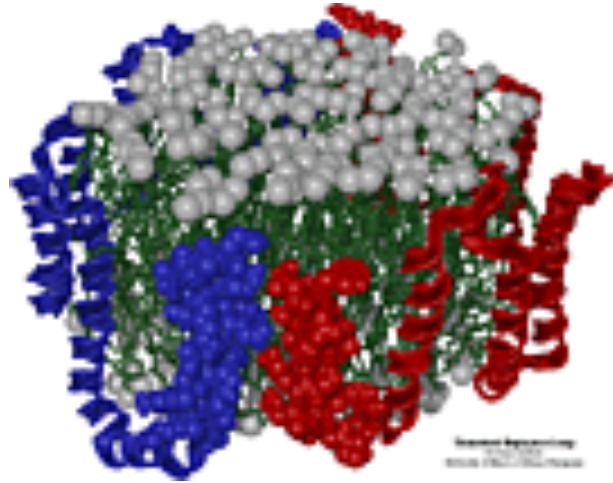


Bell Laboratories

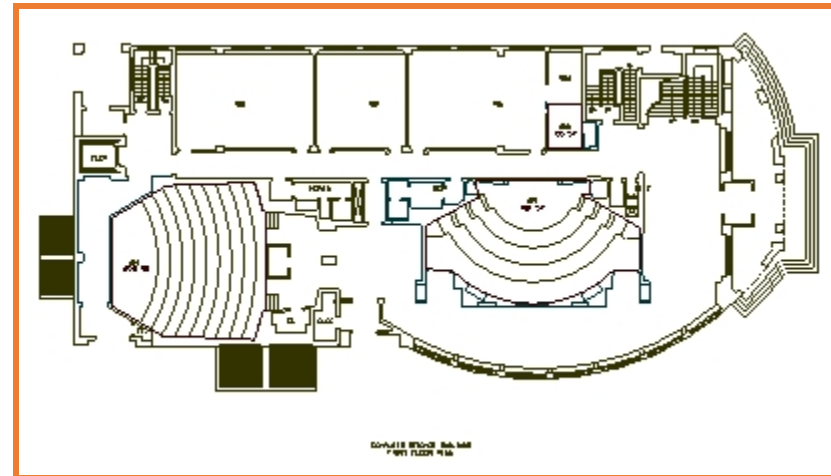


avalon.viewpoint.com

Application Specific

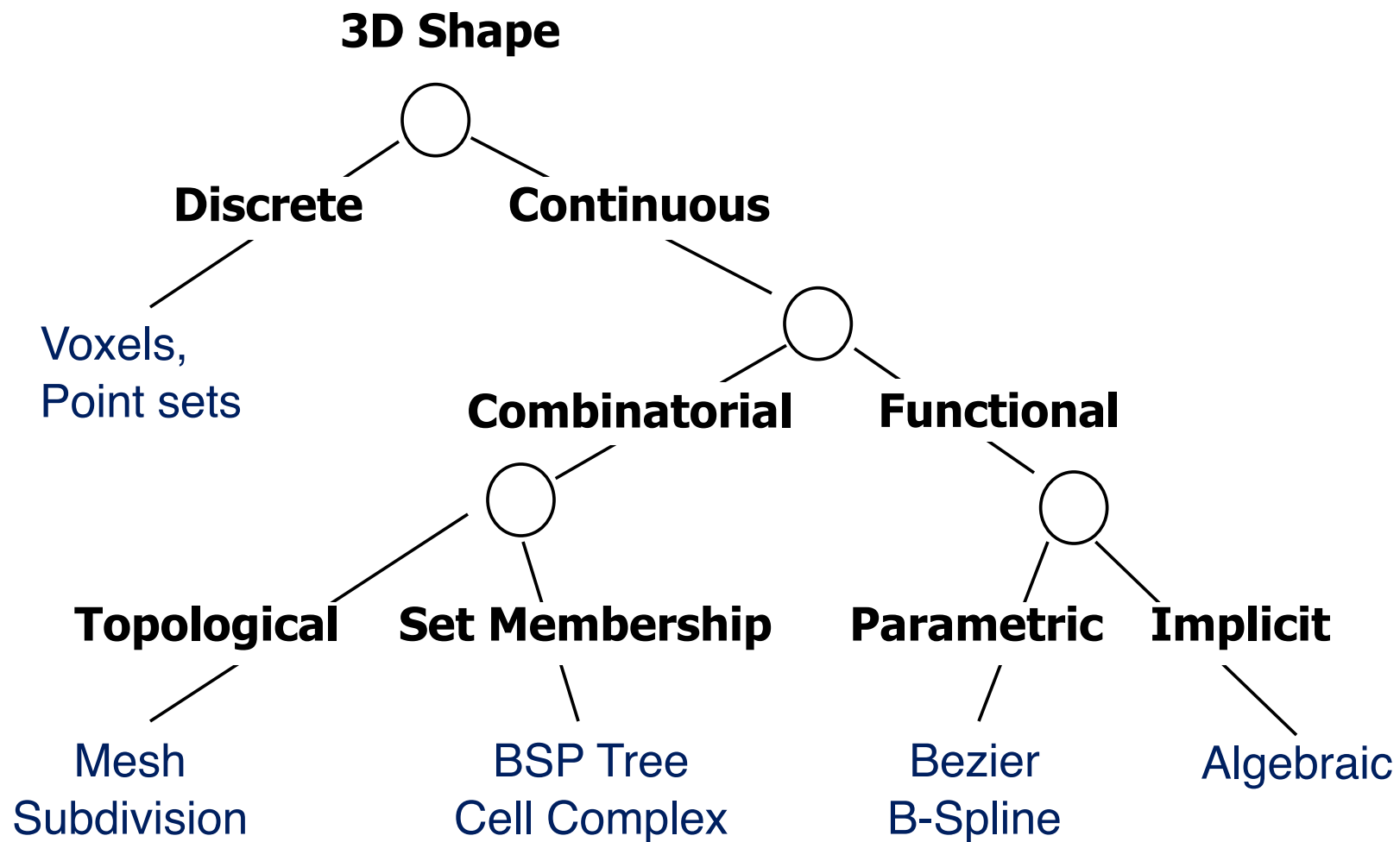


Apo A-1
(Theoretical Biophysics Group,
University of Illinois at Urbana-Champaign)



Architectural Floorplan
(CS Building, Princeton University)

Taxonomy of 3D Representations



Equivalence of Representations



- Thesis:
 - Each representation has enough expressive power to model the shape of any geometric object
 - It is possible to perform all geometric operations with any fundamental representation
- Analogous to Turing-equivalence
 - Computers and programming languages are Turing-equivalent, but each has its benefits...

Computational Differences



- Efficiency
 - Representational complexity (e.g. surface vs. volume)
 - Computational complexity (e.g. $O(n^2)$ vs $O(n^3)$)
 - Space/time trade-offs (e.g. tree data structures)
 - Numerical accuracy/stability (e.g. degree of polynomial)
- Simplicity
 - Ease of acquisition
 - Hardware acceleration
 - Software creation and maintenance
- Usability
 - Designer interface vs. computational engine

Upcoming Lectures



- Points
 - Range image
 - Point cloud
- Surfaces
 - Polygonal mesh
 - Subdivision
 - Parametric
 - Implicit
- Solids
 - Voxels
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 - Sweep
- High-level structures
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 - Application specific