

Image Processing

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Image Processing Operations



- Luminance
 - Brightness
 - Contrast
 - Gamma
 - Histogram equalization
- Color
 - Grayscale
 - Saturation
 - White balance

- Linear filtering
 - Blur & sharpen
 - Edge detect
 - Convolution
- Non-linear filtering
 - Median
 - Bilateral filter
- Dithering
 - Quantization
 - Ordered dither
 - Floyd-Steinberg

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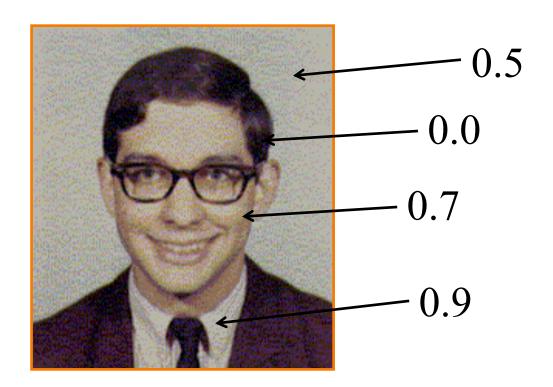
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What is Luminance?



Measures perceived "gray-level" of pixel

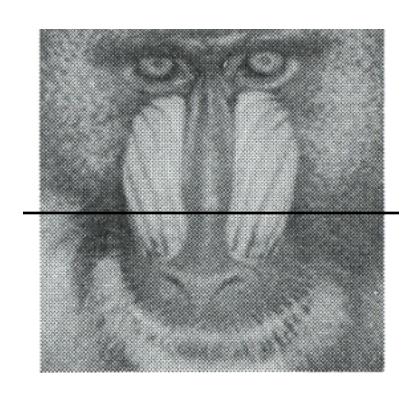
L = 0.30 red + 0.59 green + 0.11 blue

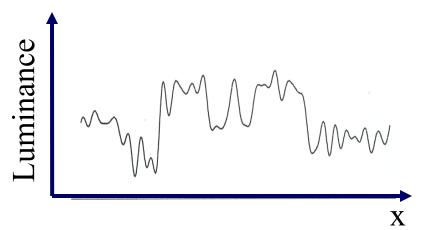


Luminance



Measures perceived "gray-level" of pixel



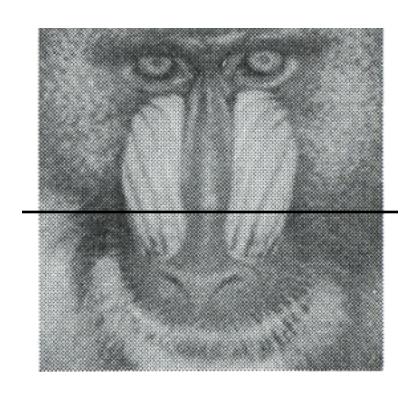


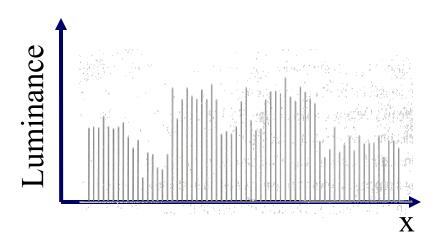
Samples of luminance for pixels on one horizontal row of pixels

Luminance



Measures perceived "gray-level" of pixel



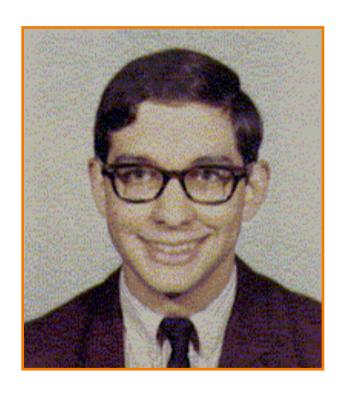


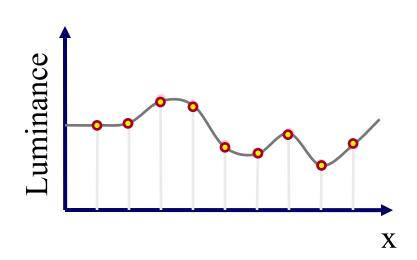
Samples of luminance for pixels on one horizontal row of pixels

Adjusting Brightness



 What must be done to the RGB values to make this image brighter?





Adjusting Brightness



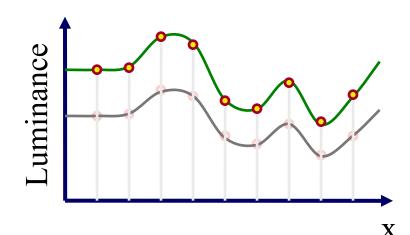
- Method 1: Convert to HSL, scale L, convert back (more on this shortly...)
- Method 2: Scale R, G, and B directly
 - o Multiply each of red, green, and blue by a factor
 - o Must clamp to [0..1] ... always ([0..1] in floating point but often [0,255] for fixed point)



Original



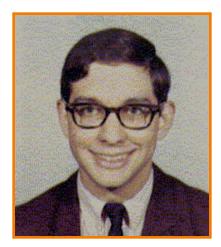
Brighter



Adjusting Contrast



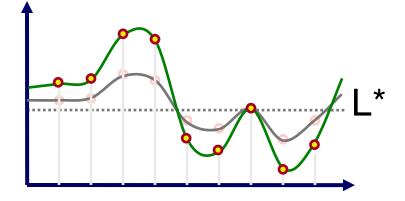
Compute mean luminance L* over whole image
 Scale deviation from L* for each pixel



Original



More Contrast

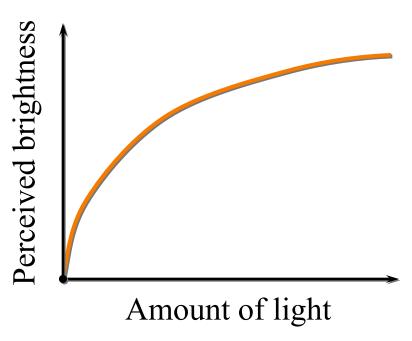


Adjusting Gamma



Apply non-linear function to account for difference between brightness and perceived brightness of display

$$I_{out} = I_{in}^{\gamma}$$

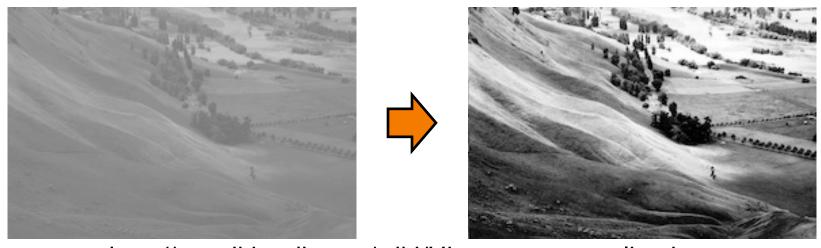


 γ depends on camera and monitor

Histogram Equalization



Change distribution of luminance values to cover full range [0-1]



http://en.wikipedia.org/wiki/Histogram_equalization

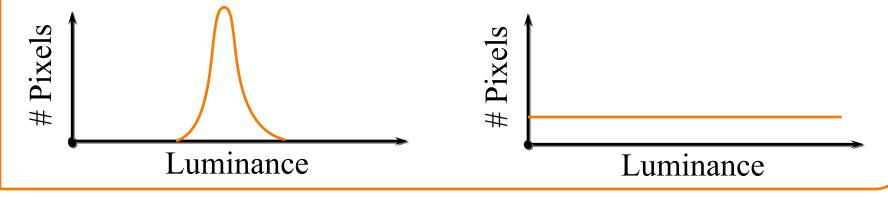


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 - Quantization
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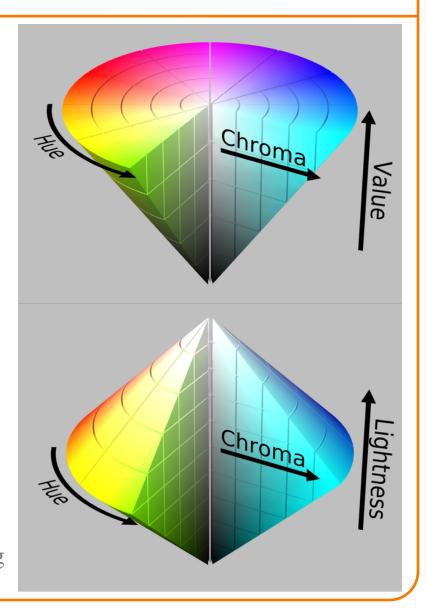
Color processing

- Color models (last lec.)
 - RGB
 - CMY
 - HSV -
 - XYZ
 - La*b*
 - Etc.

HSL

HSV

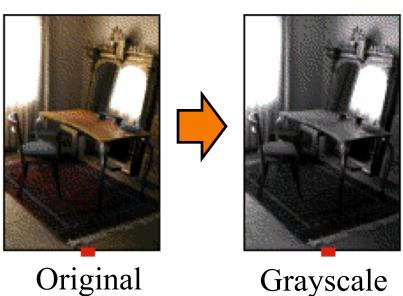
http://commons.wikimedia.org/wiki/ File:HSV_color_solid_cone_chroma_gray.png

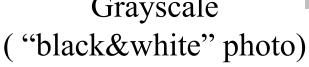


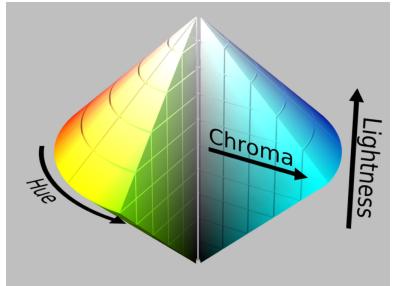
Grayscale



Convert from color to gray-levels



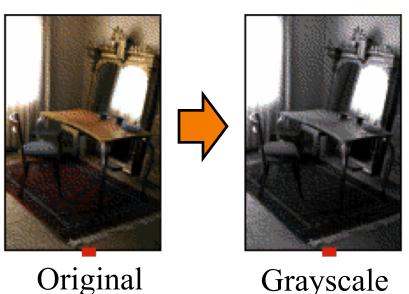


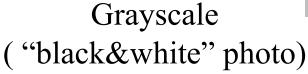


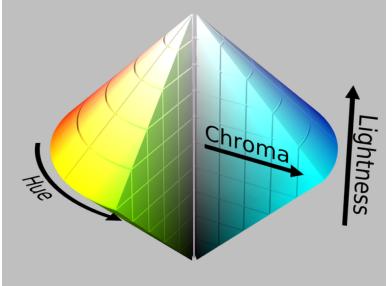
Grayscale



Convert from color to gray-levels







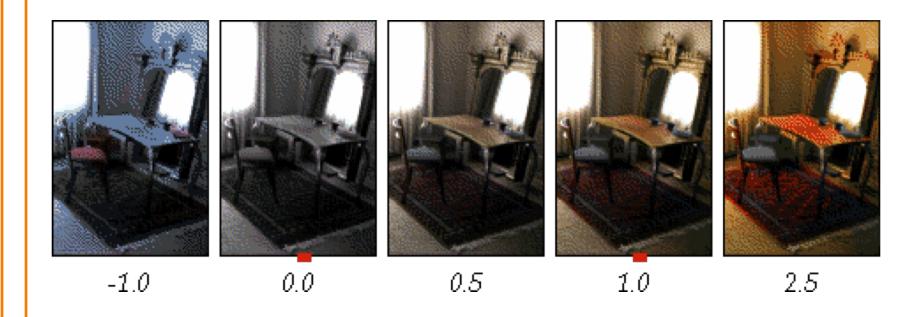
Method 1: Convert to HSL, set S=0, convert back to RGB

Method 2: Set RGB of every pixel to (L,L,L)

Adjusting Saturation



Increase/decrease color saturation of every pixel

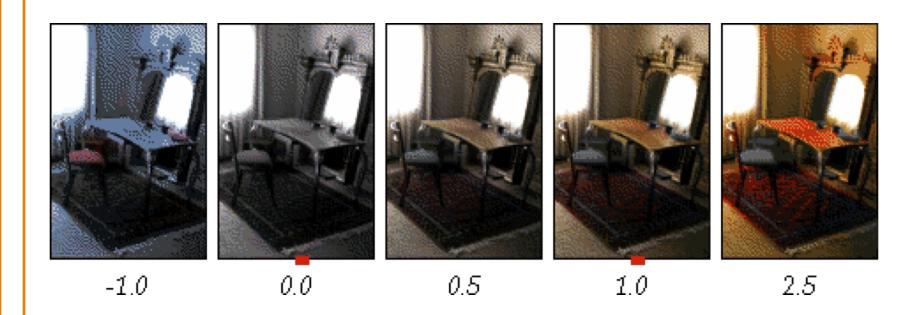


Adjusting Saturation



Chroma

Increase/decrease color saturation of every pixel



Method 1: Convert to HSL, scale S, convert back

Method 2: $R' = L + scale * (R-L) \dots same for G&B$



Adjust colors so that a given RGB value is mapped to a neutral color





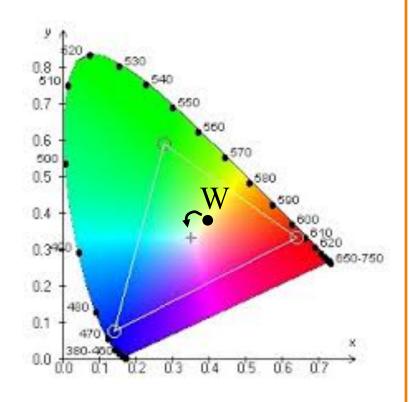




Conceptually:

Provide an RGB value W that should be mapped to white Perform transformation of color space

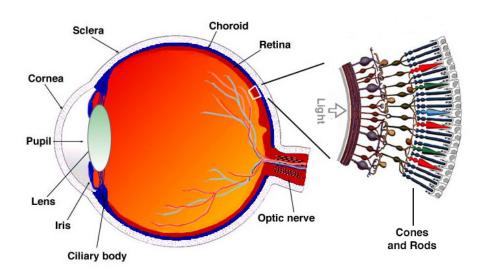




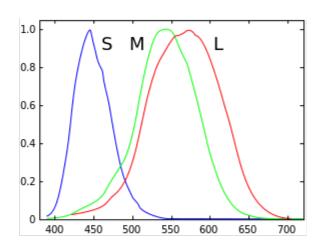


Von Kries method: adjust colors in LMS color space

 LMS primaries represent the responses of the three different types of cones in our eyes



http://www.blueconemonochromacy.org



Wikipedia



For each pixel RGB:

1) Convert to XYZ color space

$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} 0.4124 & 0.3576 & 0.1805 \\ 0.2126 & 0.7152 & 0.0722 \\ 0.0193 & 0.1192 & 0.9502 \end{bmatrix} \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$

2) Convert to LMS color space

$$\begin{bmatrix} L \\ M \\ S \end{bmatrix} = \begin{bmatrix} 0.40024 & 0.7076 & -0.08081 \\ -0.2263 & 1.16532 & 0.0457 \\ 0 & 0 & 0.91822 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}$$

- 3) Divide by L_WM_WS_W the color of "white" in LMS
- 4) Convert back to RGB

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Blur



What is the basic operation for each pixel when blurring an image?





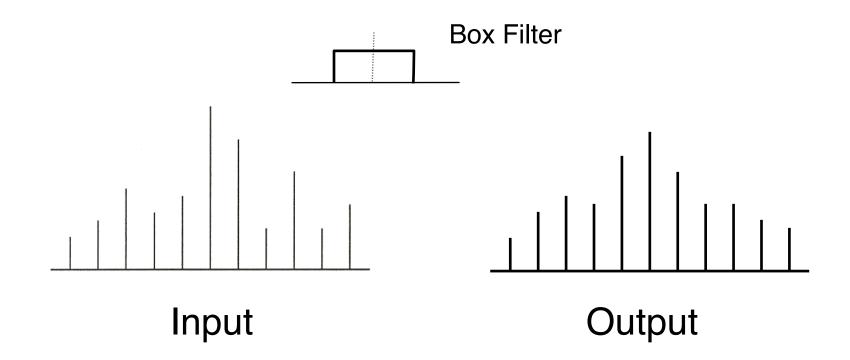


Basic Operation: Convolution



Output value is weighted sum of values in neighborhood of input image

Pattern of weights is the "filter" or "kernel"

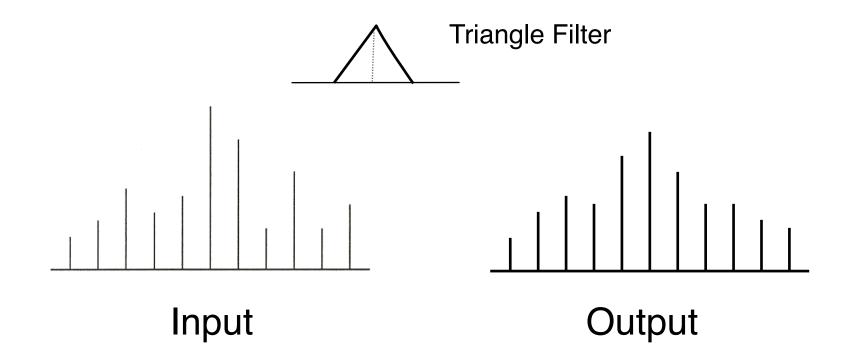


Basic Operation: Convolution



Output value is weighted sum of values in neighborhood of input image

Pattern of weights is the "filter" or "kernel"

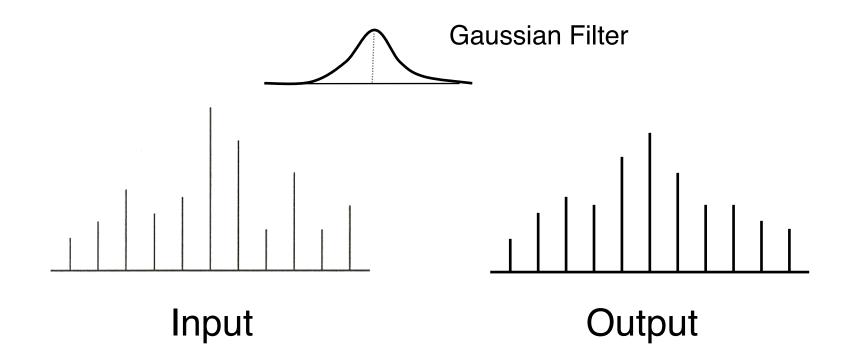


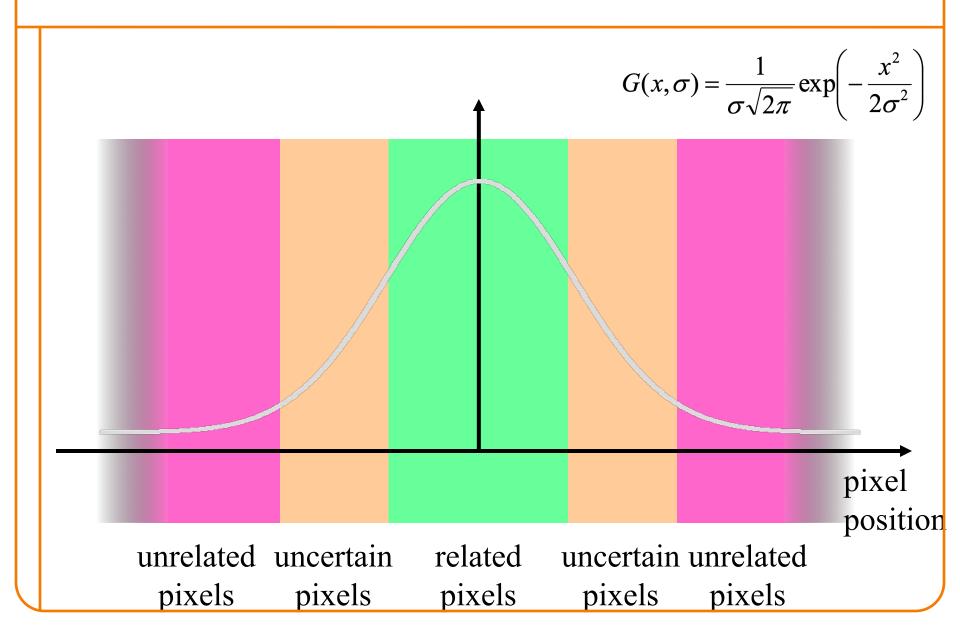
Basic Operation: Convolution



Output value is weighted sum of values in neighborhood of input image

Pattern of weights is the "filter" or "kernel"

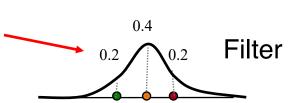


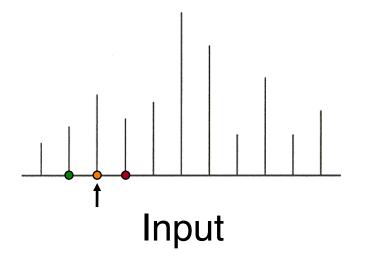


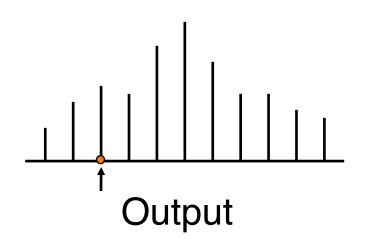


Output value is weighted sum of values in neighborhood of input image

Note to fix slides: weights should sum to 1. Practical solution in next lecture: divide by sum of weights.







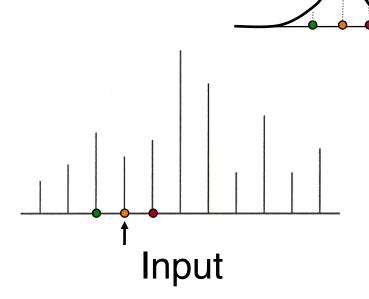
 $G(x,\sigma) = \frac{1}{\sigma\sqrt{2\pi}} \exp\left(-\frac{x^2}{2\sigma^2}\right)$

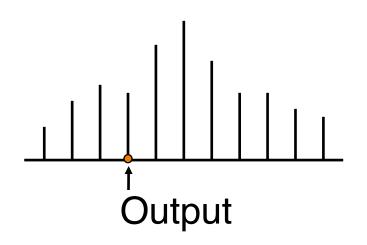
0.4

Filter



$$G(x,\sigma) = \frac{1}{\sigma\sqrt{2\pi}} \exp\left(-\frac{x^2}{2\sigma^2}\right)$$



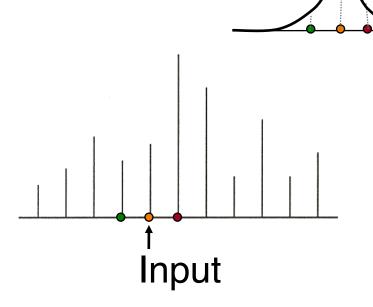


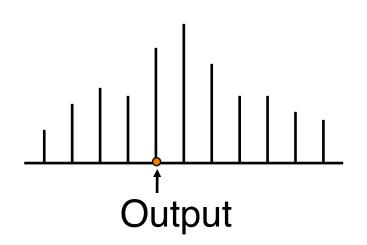
0.4

Filter



$$G(x,\sigma) = \frac{1}{\sigma\sqrt{2\pi}} \exp\left(-\frac{x^2}{2\sigma^2}\right)$$



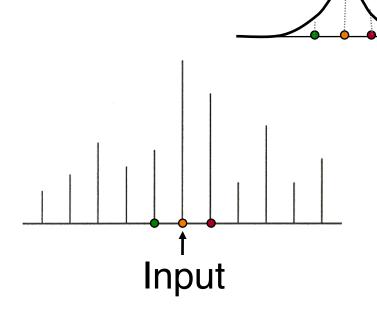


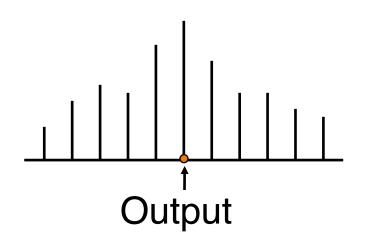
0.4

Filter



$$G(x,\sigma) = \frac{1}{\sigma\sqrt{2\pi}} \exp\left(-\frac{x^2}{2\sigma^2}\right)$$



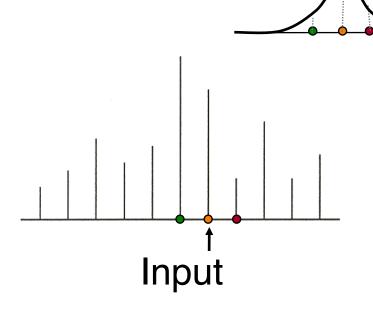


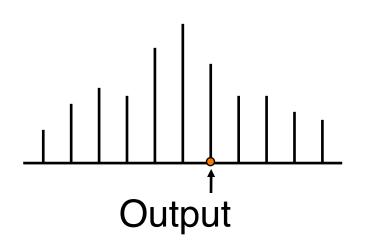
0.4

Filter



$$G(x,\sigma) = \frac{1}{\sigma\sqrt{2\pi}} \exp\left(-\frac{x^2}{2\sigma^2}\right)$$





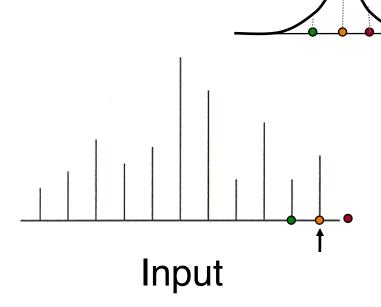
0.4

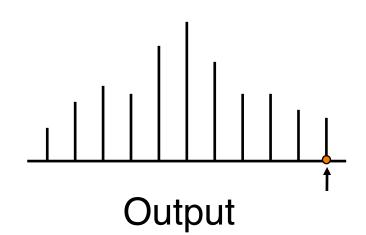
Filter



What if filter extends beyond boundary?

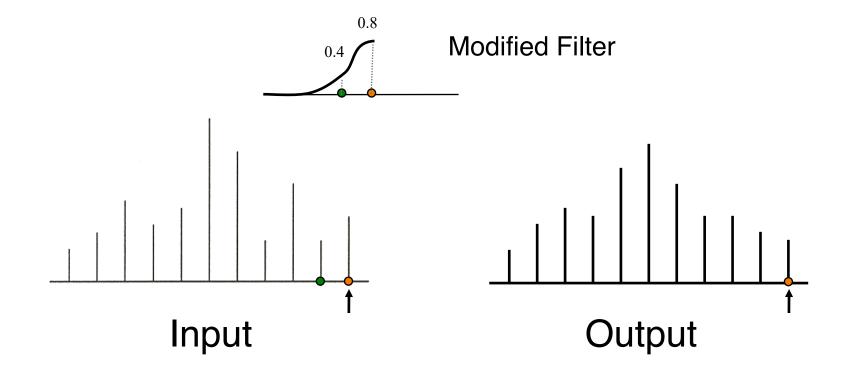
$$G(x,\sigma) = \frac{1}{\sigma\sqrt{2\pi}} \exp\left(-\frac{x^2}{2\sigma^2}\right)$$







What if filter extends beyond boundary?





Output contains samples from smoothed input

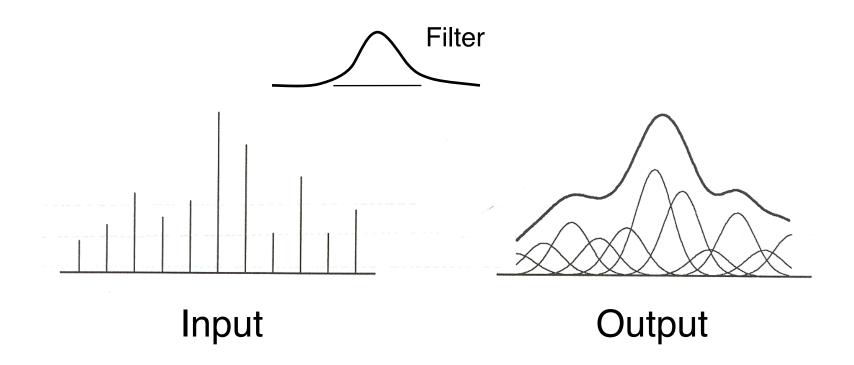


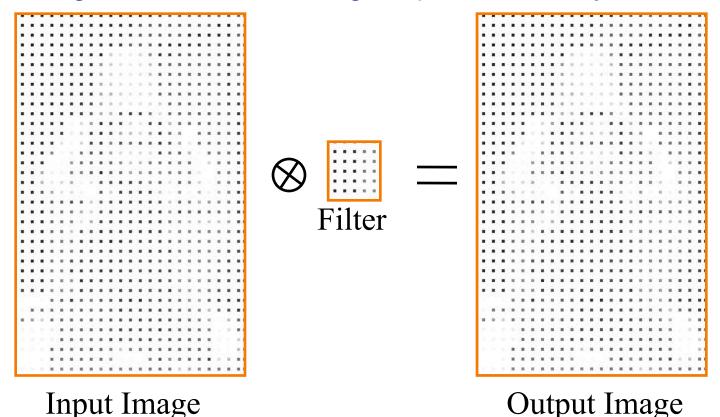
Figure 2.4 Wolberg

Linear Filtering



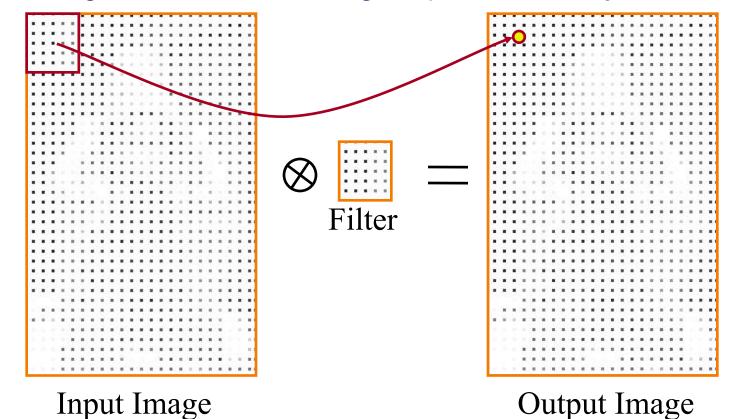
2D Convolution

o Each output pixel is a linear combination of input pixels in 2D neighborhood with weights prescribed by a filter





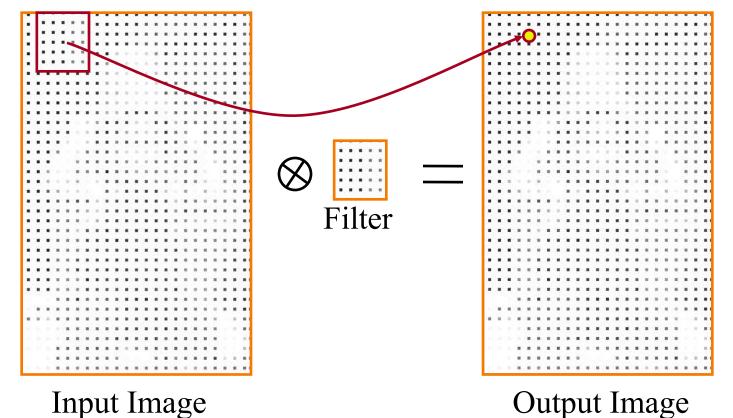
2D Convolution







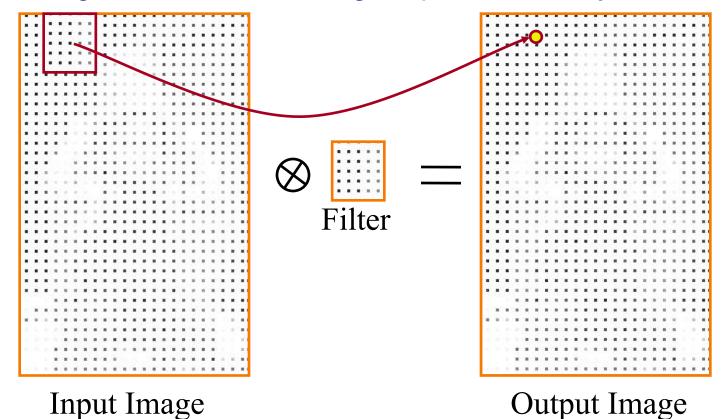
2D Convolution







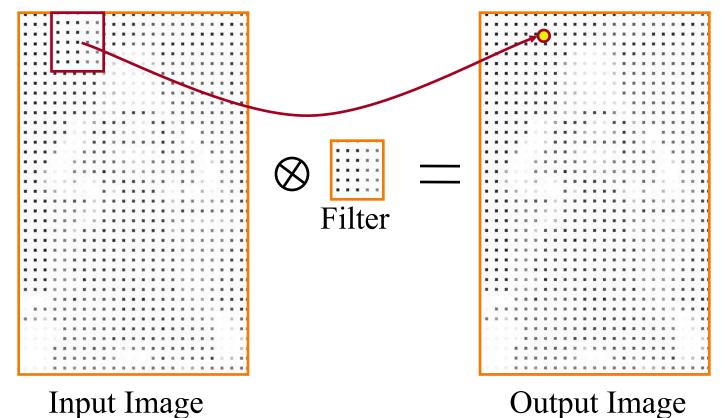
2D Convolution





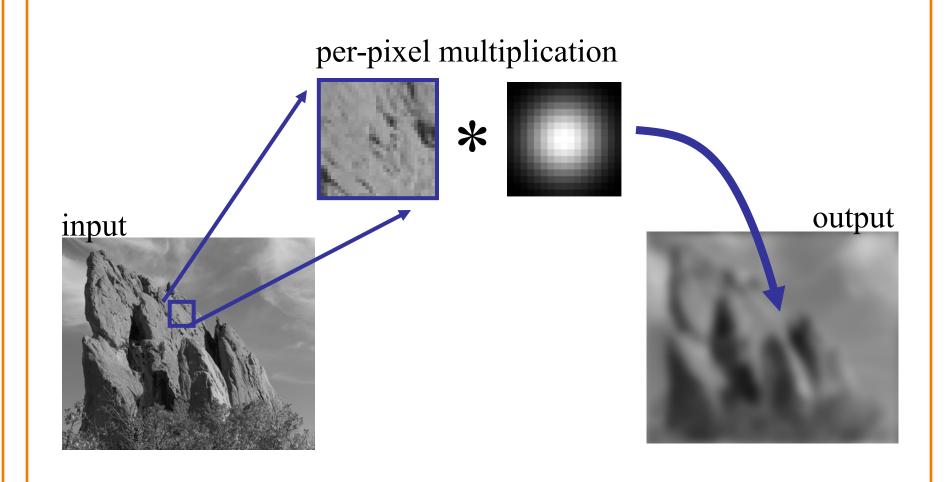


2D Convolution





Gaussian Blur



Gaussian Blur

Output value is weighted sum of values in neighborhood of input image

$$Blur(I_{\mathbf{p}},\sigma) = \frac{1}{W_{\mathbf{p}}} \sum_{\mathbf{q} \in S} G(\|\mathbf{p} - \mathbf{q}\|,\sigma) I_{\mathbf{q}}$$

normalized
Gaussian function





- Many interesting linear filters
 - Blur
 - Edge detect
 - Sharpen
 - Emboss
 - etc.

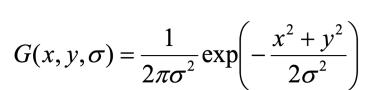
Blur



Convolve with a 2D Gaussian filter



Original





Blur

Filter =
$$\begin{bmatrix} 1/& 2/& 1/\\ /16 & /16 & /16 \\ 2/& 4/& 2/\\ /16 & /16 & /16 \\ 1/& 2/& 1/\\ /16 & /16 & /16 \end{bmatrix}$$

Edge Detection



Convolve with a 2D Laplacian filter that finds differences between neighbor pixels



Original



Detect edges

Filter =
$$\begin{bmatrix} -1 & -1 & -1 \\ -1 & +8 & -1 \\ -1 & -1 & -1 \end{bmatrix}$$

Sharpen



Sum detected edges with original image



Original



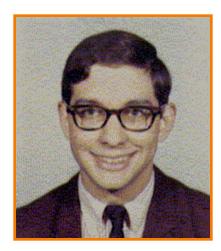
Sharpened

$$Filter = \begin{bmatrix} -1 & -1 & -1 \\ -1 & +9 & -1 \\ -1 & -1 & -1 \end{bmatrix}$$

Emboss



Convolve with a filter that highlights gradients in particular directions



Original



Embossed

$$Filter = \begin{bmatrix} -1 & -1 & 0 \\ -1 & 0 & 1 \\ 0 & 1 & 1 \end{bmatrix}$$

Side Note: Separable Filters



Some filters are separable (e.g., Gaussian)

- First, apply 1-D convolution across every row
- Then, apply 1-D convolution across every column
- HUGE impact on performance (when kernel is big)

Image Processing Operations



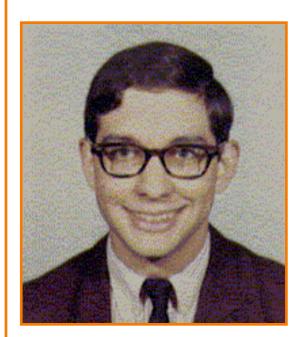
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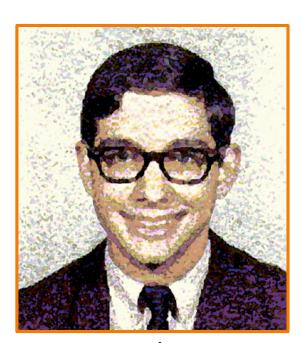
Non-Linear Filtering



Each output pixel is a non-linear function of input pixels in neighborhood (filter depends on input)



Original



Paint

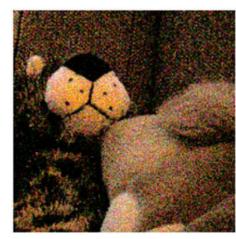


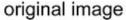
Stained Glass

Median Filter



Each output pixel is median of input pixels in neighborhood







1px median filter



3px median filter

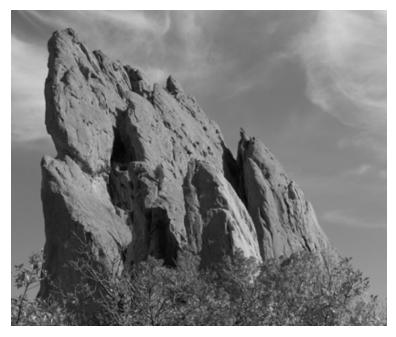


10px median filter

Bilateral Filter



Gaussian blur uses same filter for all pixels Blurs across edges as much as other areas







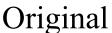
Gaussian Blur

Bilateral Filter



Gaussian blur uses same filter for all pixels Prefer a filter that preserves edges (adapts to content)









Bilateral Filter

Gaussian Blur

Output value is weighted sum of values in neighborhood of input image

$$Blur(I_{\mathbf{p}},\sigma) = \frac{1}{W_{\mathbf{p}}} \sum_{\mathbf{q} \in S} G(\|\mathbf{p} - \mathbf{q}\|,\sigma) I_{\mathbf{q}}$$

normalized
Gaussian function

Bilateral Filter



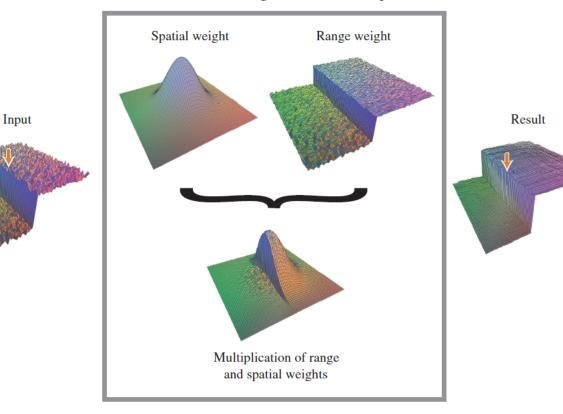
Combine Gaussian filtering in both spatial domain and color domain

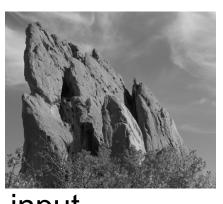
Bilateral Filtering



Combine Gaussian filtering in both spatial domain and color domain

Bilateral filter weights at the central pixel





input

$$\sigma_{\rm r} = 0.1$$



 $\sigma_{\rm r} = 0.25$



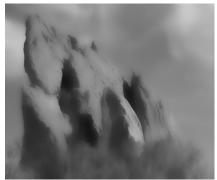
 $\sigma_{\rm r} = \infty$ (Gaussian blur)





 $\sigma_{\rm s} = 2$







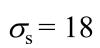








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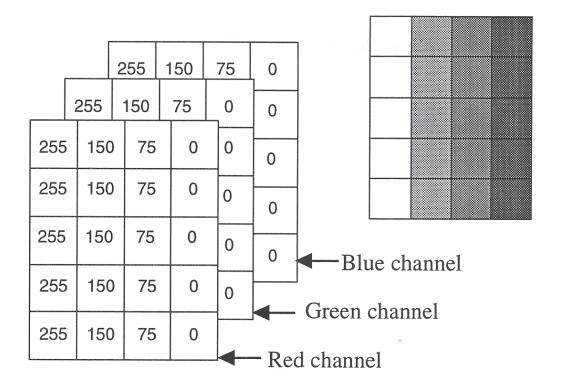
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Quantization



Reduce intensity resolution

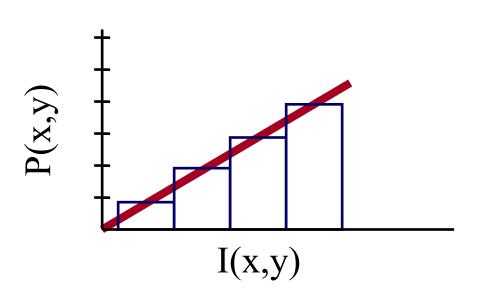
- o Frame buffers have limited number of bits per pixel
- o Physical devices have limited dynamic range

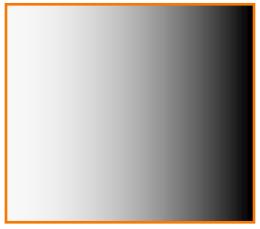


Uniform Quantization

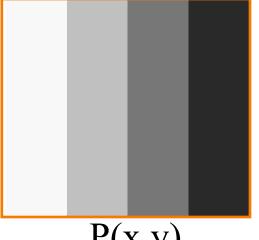


P(x, y) = round(I(x, y))where round() chooses nearest value that can be represented.





I(x,y)



(2 bits per pixel)

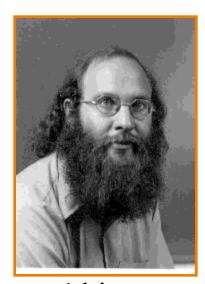
Uniform Quantization



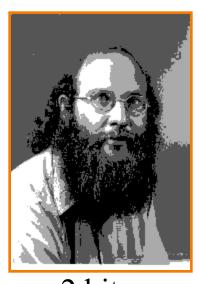
Images with decreasing bits per pixel:



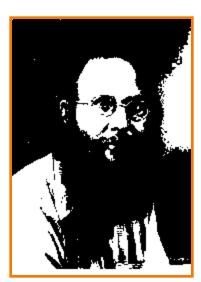
8 bits



4 bits



2 bits



1 bit

Notice contouring.

Reducing Effects of Quantization



Intensity resolution / spatial resolution tradeoff

- Dithering
 - o Random dither
 - o Ordered dither
 - o Error diffusion dither
- Halftoning
 - o Classical halftoning

Dithering

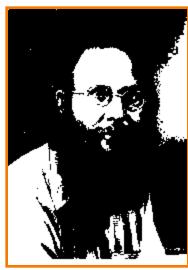


Distribute errors among pixels

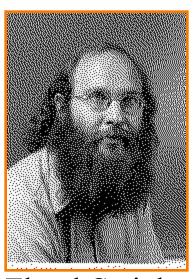
- o Exploit spatial integration in our eye
- o Display greater range of perceptible intensities



Original (8 bits)



Uniform
Quantization
(1 bit)



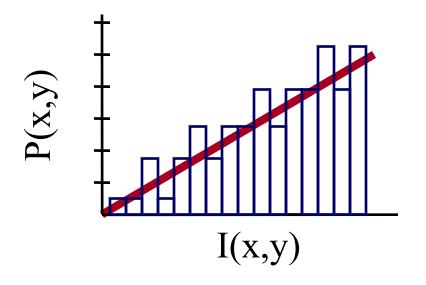
Floyd-Steinberg
Dither
(1 bit)

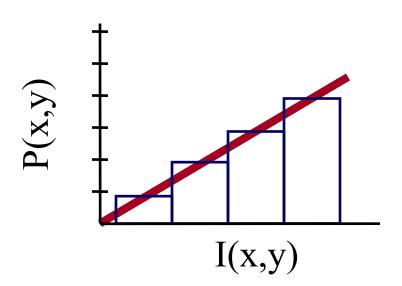
Random Dither



Randomize quantization errors

o Errors appear as noise

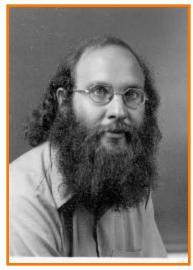




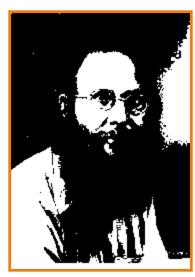
$$P(x, y) = round(I(x, y) + noise(x,y))$$

Random Dither

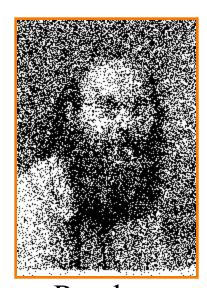




Original (8 bits)



Uniform
Quantization
(1 bit)



Random
Dither
(1 bit)

Ordered Dither



Pseudo-random quantization errors

- o Matrix stores pattern of threshholds
- o Pseudo-code for 1-bit output:

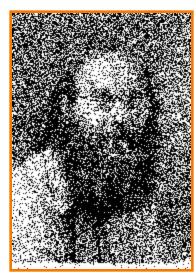
o Can be generalized to n-bit output, by comparing quantization error to threshhold.

Ordered Dither

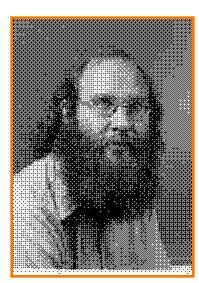




Original (8 bits)



Random
Dither
(1 bit)



Ordered
Dither
(1 bit)

Ordered Dither



Recursion for Bayer's ordered dither matrices

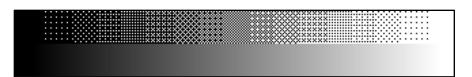
$$D_{n} = \begin{bmatrix} 4D_{n/2} + D_{2}(1,1)U_{n/2} & 4D_{n/2} + D_{2}(1,2)U_{n/2} \\ 4D_{n/2} + D_{2}(2,1)U_{n/2} & 4D_{n/2} + D_{2}(2,2)U_{n/2} \end{bmatrix}$$

$$D_2 = \begin{bmatrix} 3 & 1 \\ 0 & 2 \end{bmatrix}$$

$$D_2 = \begin{bmatrix} 3 & 1 \\ 0 & 2 \end{bmatrix} \qquad D_4 = \begin{bmatrix} 15 & 7 & 13 & 5 \\ 3 & 11 & 1 & 9 \\ 12 & 4 & 14 & 6 \\ 0 & 8 & 2 & 10 \end{bmatrix}$$

4x4 matrix gives 17 gray levels:

https://en.wikipedia.org/wiki/Ordered dithering

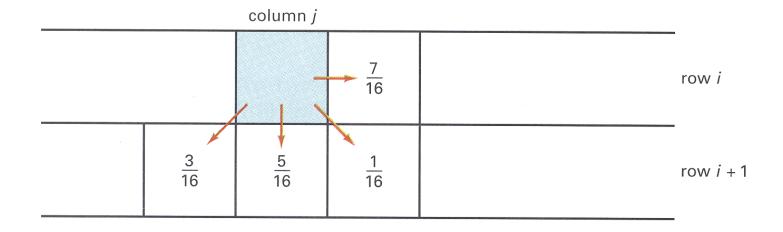


Error Diffusion Dither



Spread quantization error over neighbor pixels

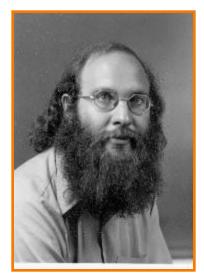
- o Error dispersed to pixels right and below
- o Floyd-Steinberg weights:



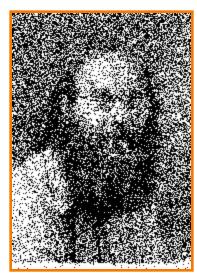
$$3/16 + 5/16 + 1/16 + 7/16 = 1.0$$

Error Diffusion Dither

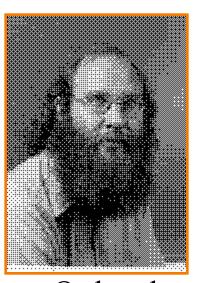




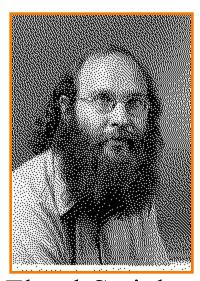
Original (8 bits)



Random
Dither
(1 bit)



Ordered Dither (1 bit)



Floyd-Steinberg
Dither
(1 bit)

Summary



- Color transformations
 - Different color spaces useful for different operations
- Filtering
 - Compute new values for image pixels based on function of old values in neighborhood
- Dithering
 - Reduce visual artifacts due to quantization
 - Distribute errors among pixels
 Exploit spatial integration in our eye