



# Character Animation

COS 426, Spring 2018

Princeton University

# Computer Animation



- Describing how 3D objects (& cameras) move over time



Pixar

# Computer Animation



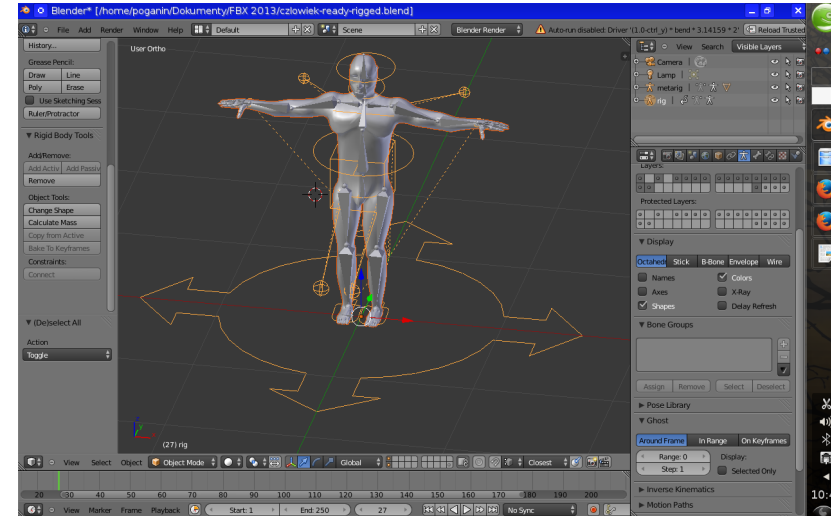
- Challenge is balancing between ...
  - Animator control
  - Physical realism



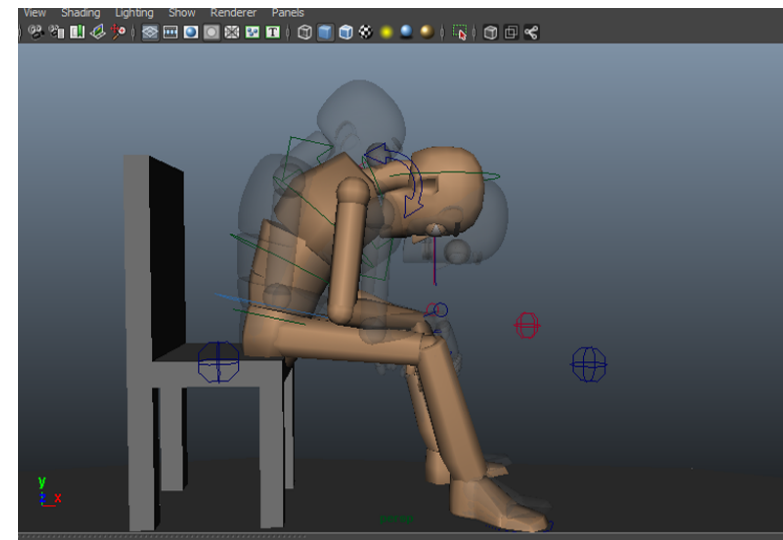
# Computer Animation



- Manipulation
  - Posing
  - Configuration control
  
- Interpolation
  - Keyframes
  - In-betweens



<https://blenderartists.org/>

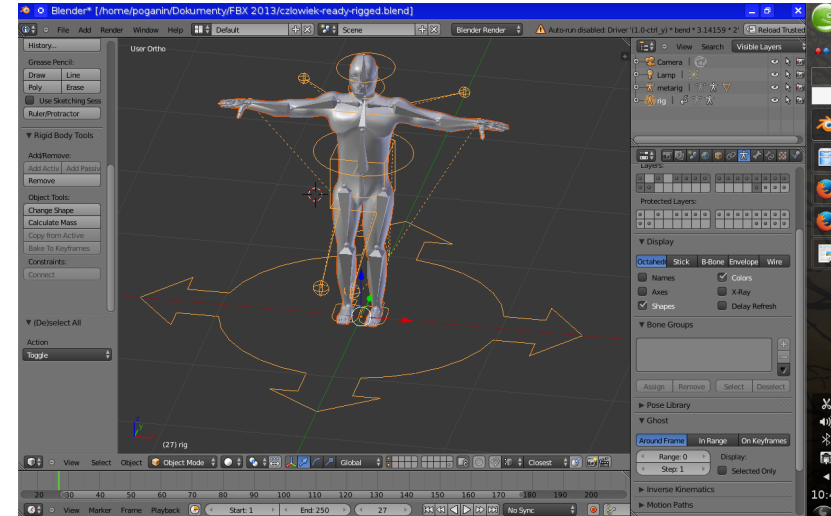


[focus.gscept.com](http://focus.gscept.com)

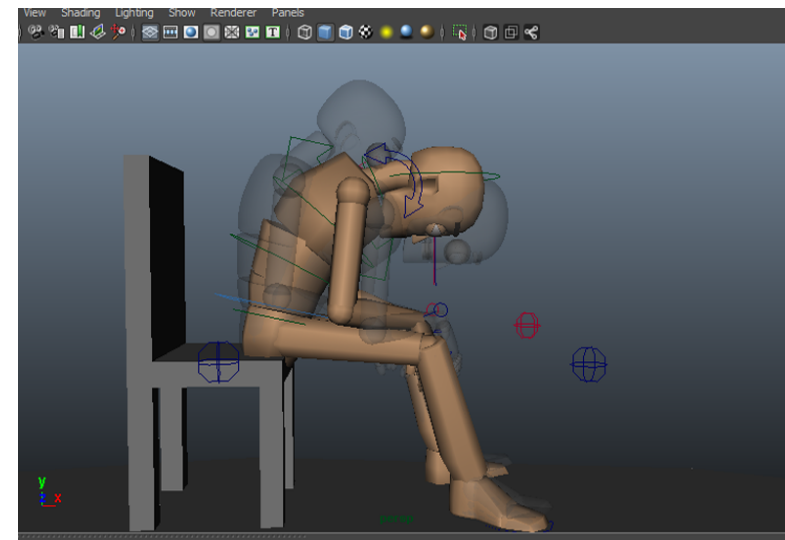
# Character Animation Methods



- Modeling (manipulation)
  - Deformation
  - Blendshapes
  - Skeletons
- Interpolation
  - Key-framing
  - Kinematics
  - Motion Capture



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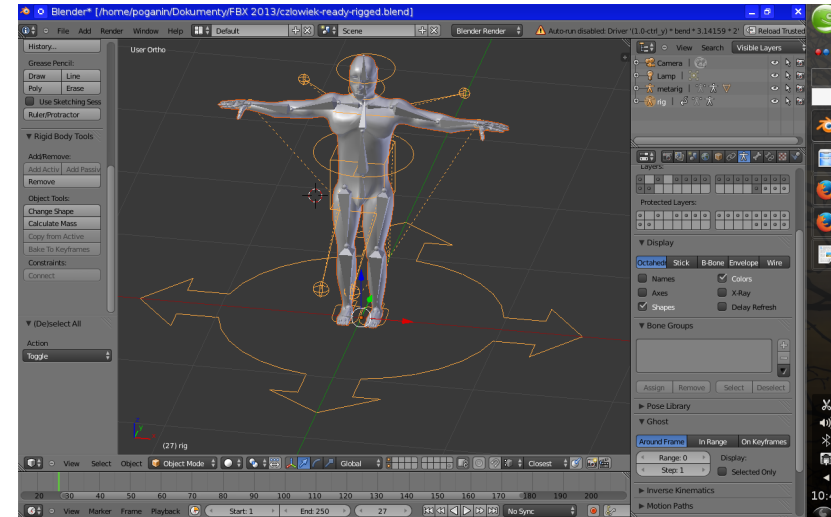


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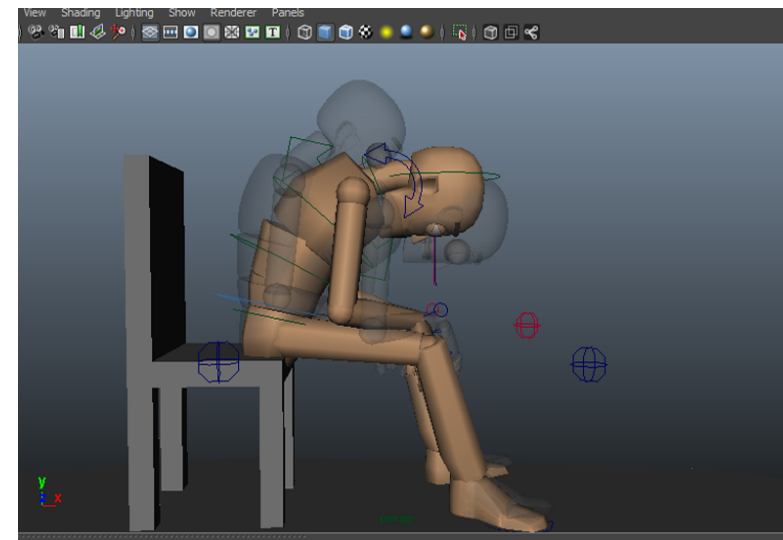
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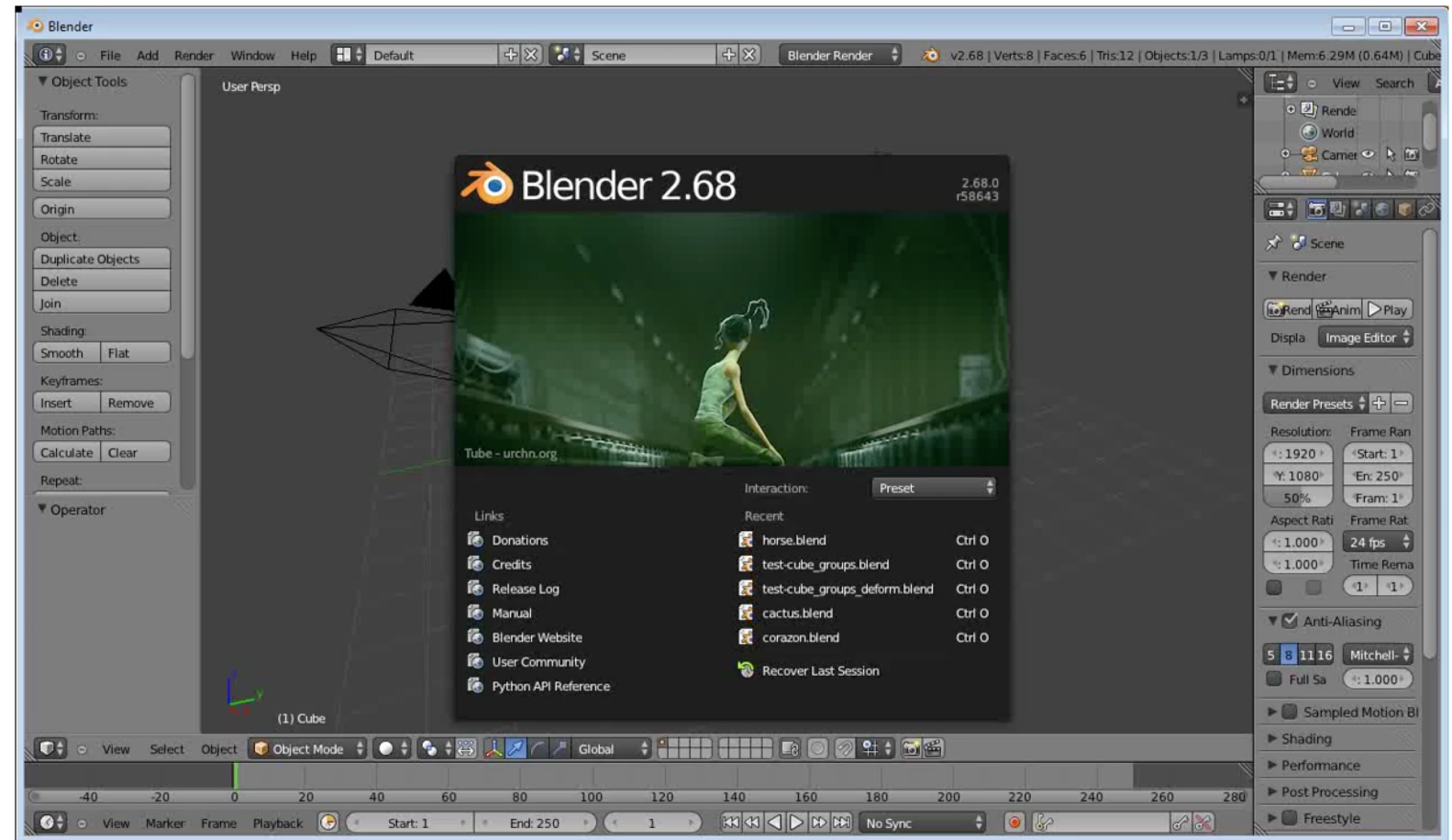
[focus.gscept.com](http://focus.gscept.com)

# Deformation



- How to change a character's pose?
  - Every vertex directly
  - Intuitive computation

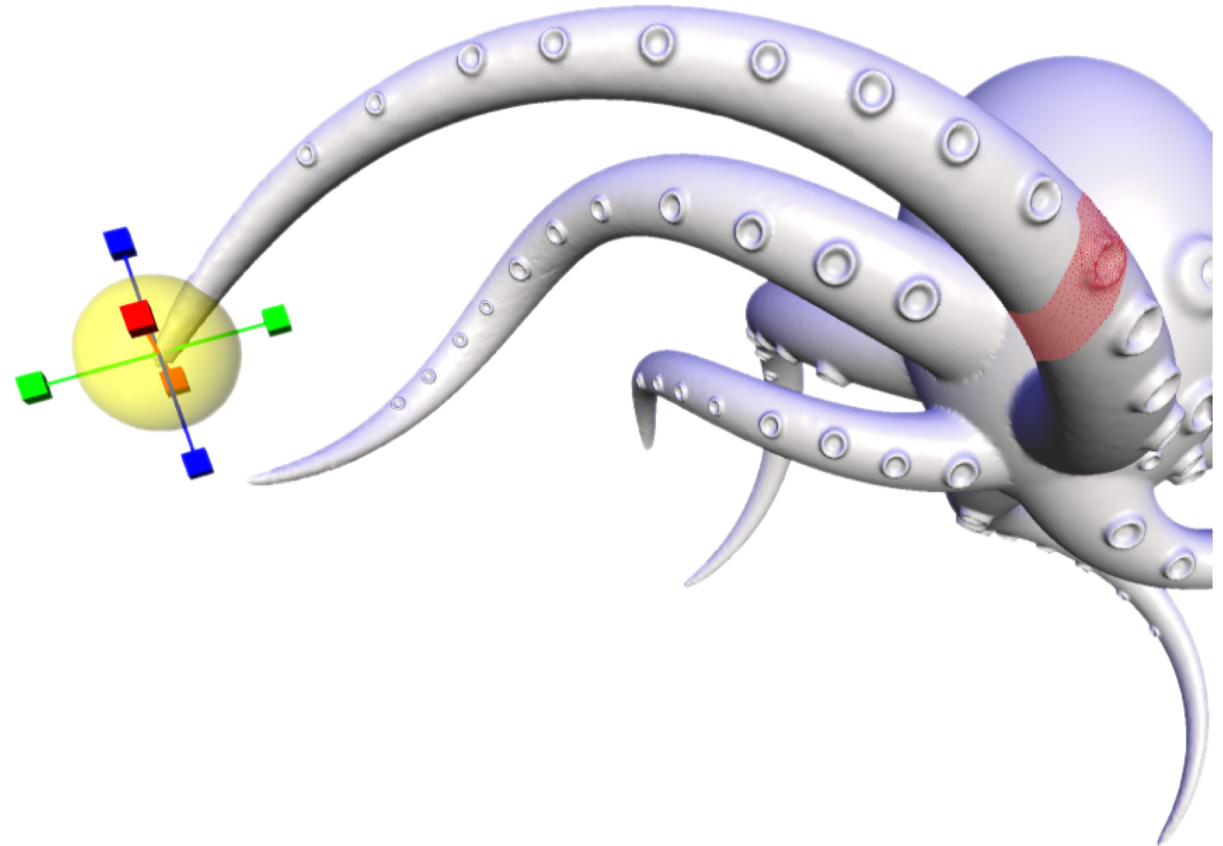
[https://www.youtube.com/watch?v=oxkf\\_N-QCNI](https://www.youtube.com/watch?v=oxkf_N-QCNI)



# Deformation



- A HUGE variety of methods
  - Laplacian mesh editing
  - ARAP
  - CAGE Base
  - Barycentric coordinates
  - Heat diffusion
  - Variational
  - ...

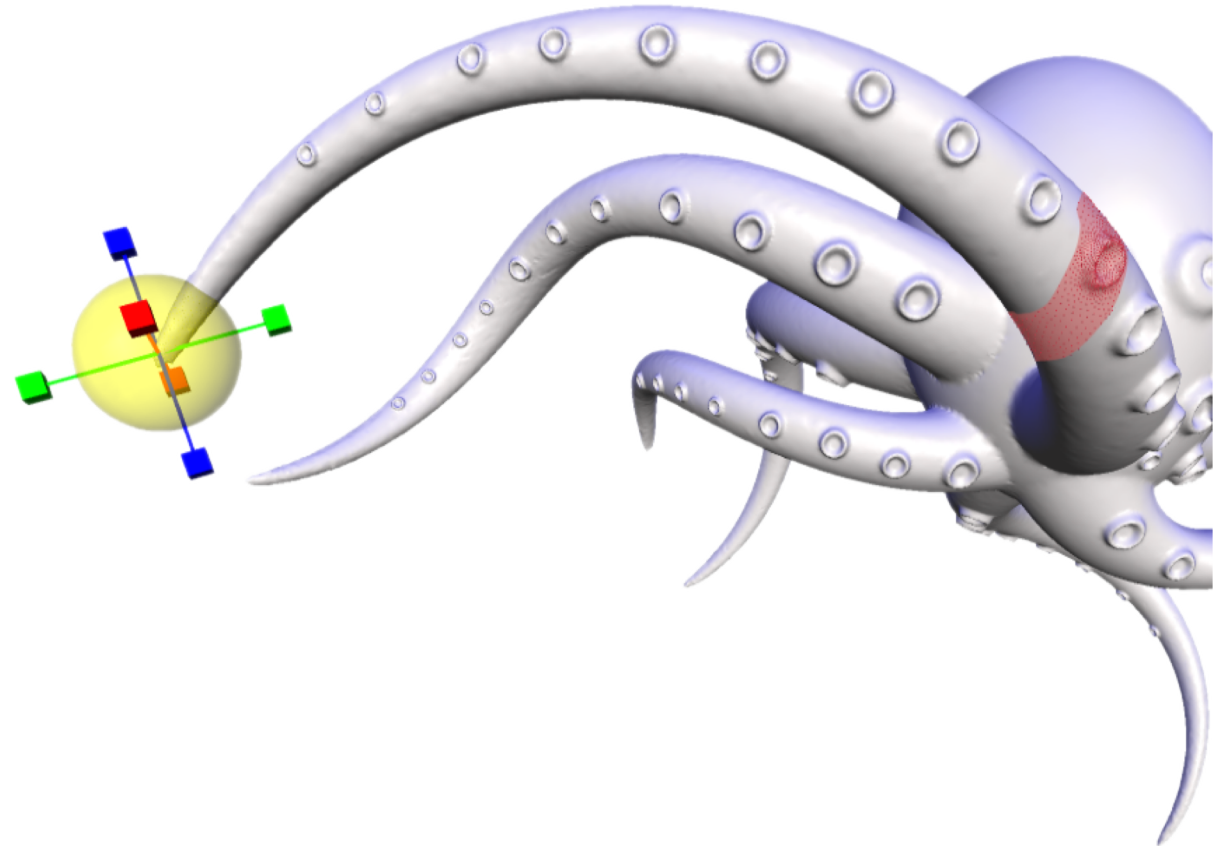




# Deformation



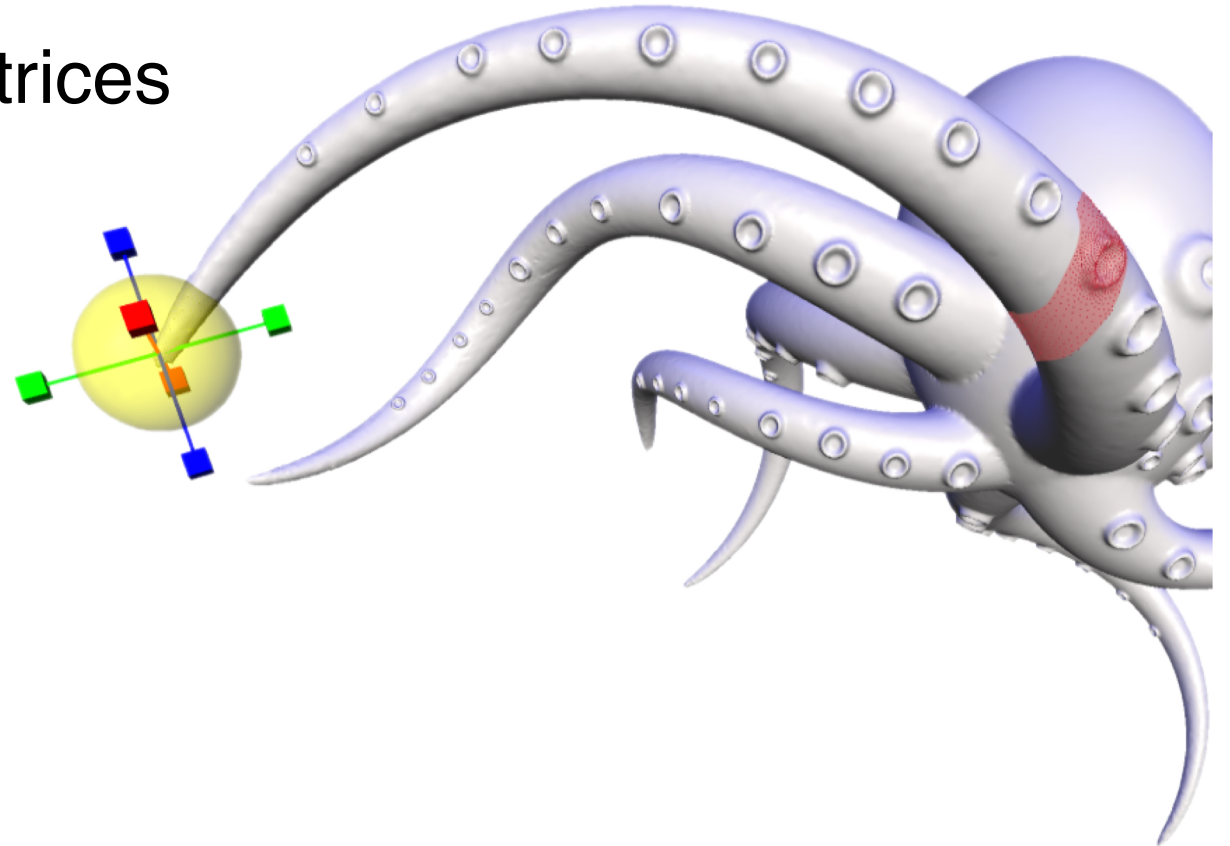
- A HUGE variety of methods
  - Laplacian mesh editing
  - ARAP
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  - Barycentric coordinates
  - Heat diffusion
  - Variational
  - ...



# Laplacian Mesh Editing



- Local detail representation – enables **detail preservation** through various modeling tasks
- Representation with **sparse** matrices
- Efficient **linear** surface reconstruction



# Overall framework



1. Compute differential representation

$$\delta_i = L(v_i) = v_i - \frac{1}{d_i} \sum_{j \in N(i)} v_j$$

2. Pose modeling constraints

$$v'_i = u_i, \quad i \in \mathcal{C}$$

3. Reconstruct the surface – in least-squares sense

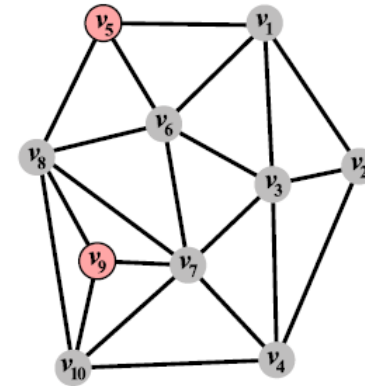
$$\begin{pmatrix} L \\ L_c \end{pmatrix} \mathbf{V} = \begin{pmatrix} \boldsymbol{\delta} \\ \mathbf{U} \end{pmatrix}$$

# Differential coordinates?



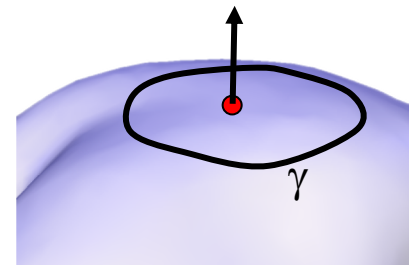
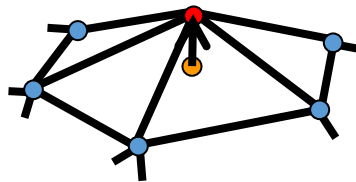
- In matrix form:

$$L_{ij} = \begin{cases} -w_{ij} & i \neq j \\ \sum_{j \in 1\text{ring}_i} w_{ij} & i = j \\ 0 & \text{else} \end{cases}$$



4	-1	-1	-1	-1					
-1	3	-1	-1						
-1	-1	5	-1	-1	-1				
	-1	-1	4		-1				-1
-1				3	-1	-1			
-1		-1			4	-1	-1		
		-1	-1		-1	6	-1	-1	-1
				-1	-1	-1	6	-1	-1
						-1	-1	3	-1
			-1		-1	-1	-1		4

- They represent the **local** detail / local shape description
  - The direction approximates the normal
  - The size approximates the mean curvature







# Example



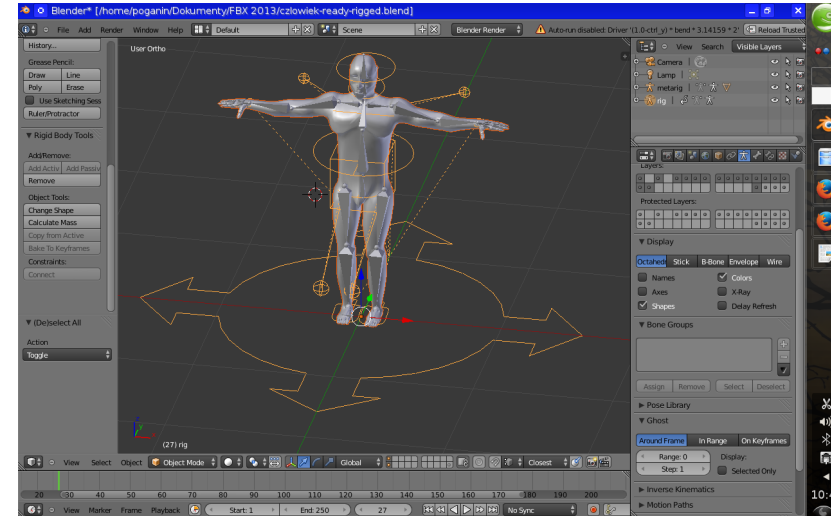
## Laplacian Mesh Editing

A short editing session  
with the *Octopus*

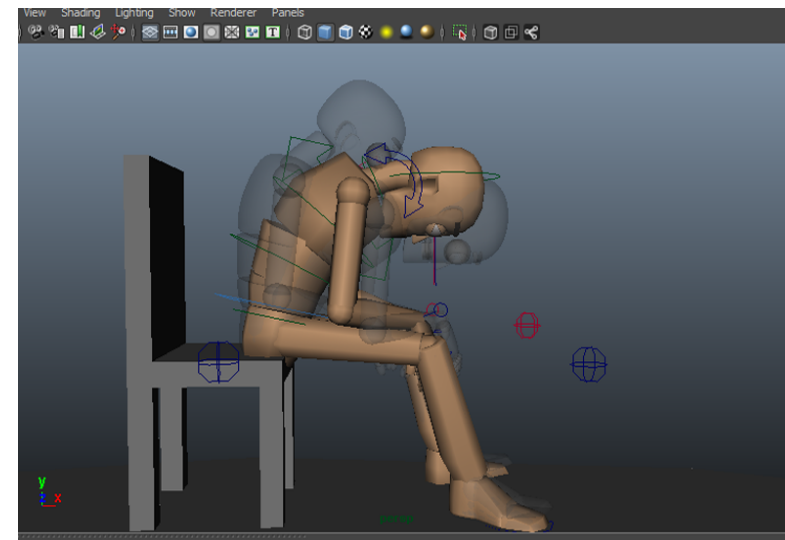
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- Modeling (manipulation)
  - Deformation
  - **Blendshapes**
  - Skeletons
- Interpolation
  - Key-framing
  - Kinematics
  - Motion Capture



<https://blenderartists.org/>



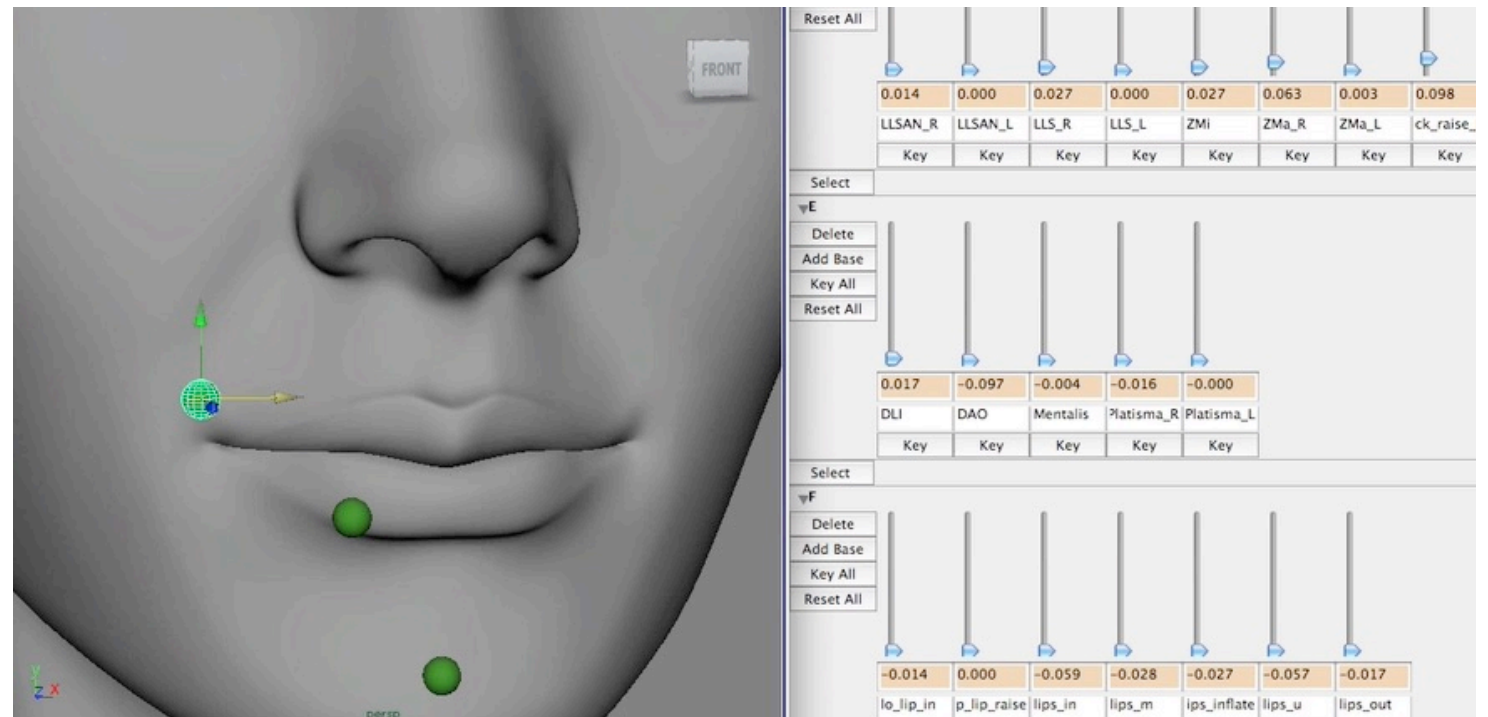
[focus.gscept.com](http://focus.gscept.com)



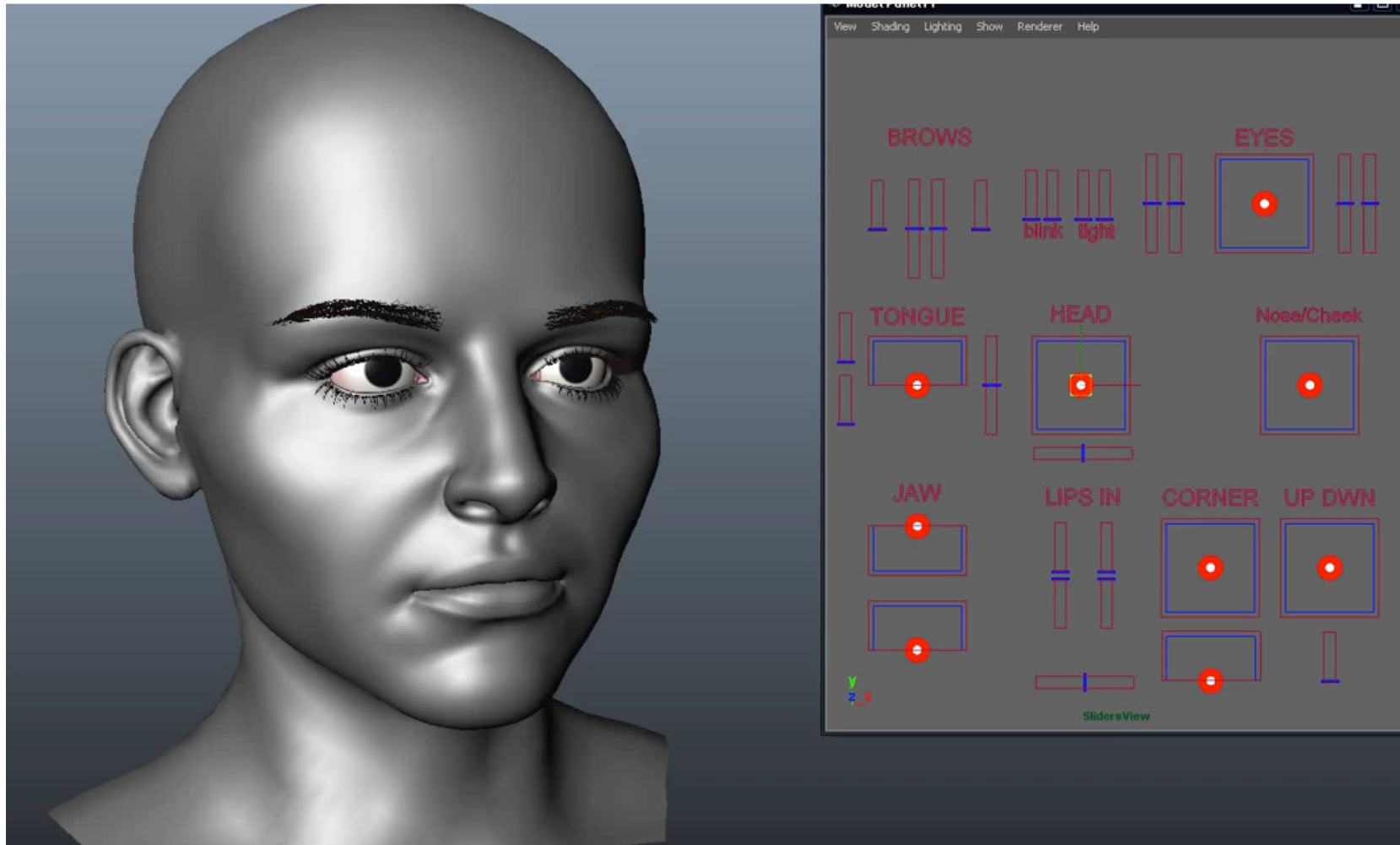
# Blendshapes



- Blendshapes are an approximate semantic parameterization
- Linear blend of predefined poses



# Blendshapes

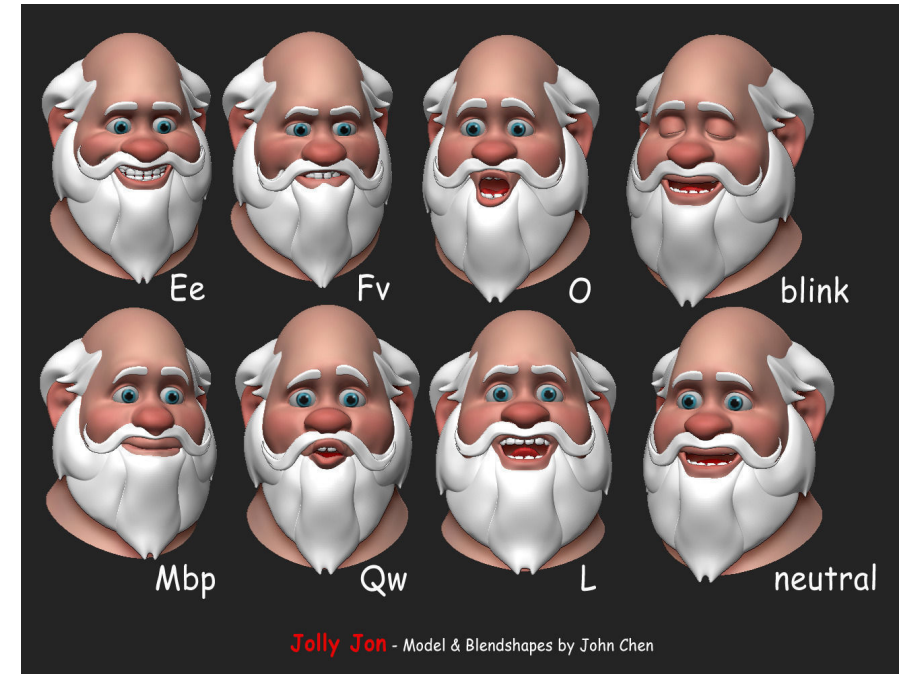


<https://www.youtube.com/watch?v=KPDFMpuK2fQ>

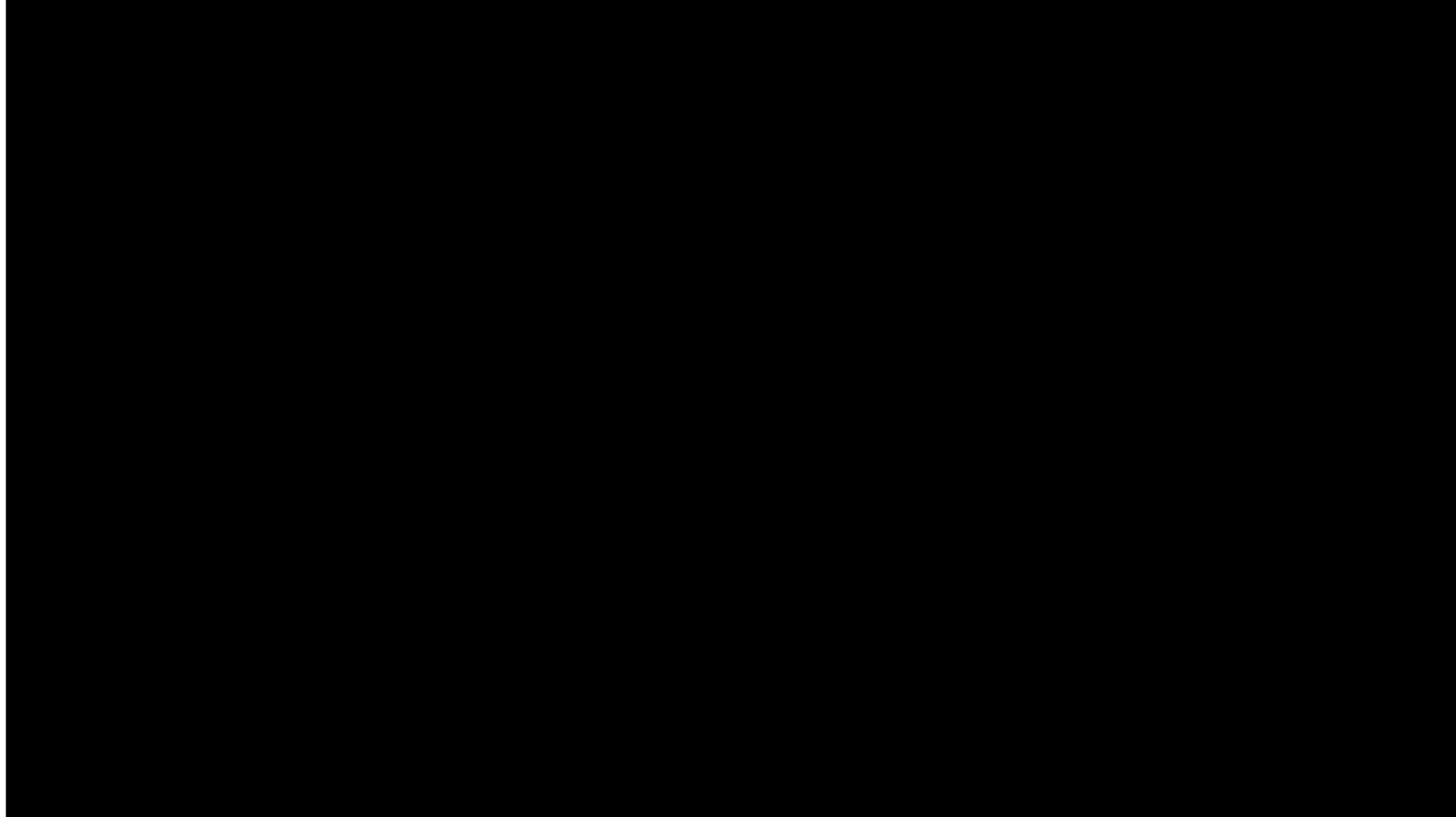
# Blendshapes



- Usually used for difficult to pose complex deformations
  - Such faces
- Given:
  - A mesh  $M = (V, E)$  with  $m$  vertices
  - $n$  configurations of the same mesh,  $M_b = (V_b, E), b = 1 \dots n$
- A new configuration is simply:
  - $M' = (\sum_{b=1 \dots n} w_b V_b, E)$
- Delta formulation:
  - $M' = (\sum_{b=1 \dots n} V_0 + w_b (V_b - V_0), E)$
  - A bit more convenient
- $M_0$  - the rest pose,  $w_b$  blend weights



# Blendshapes

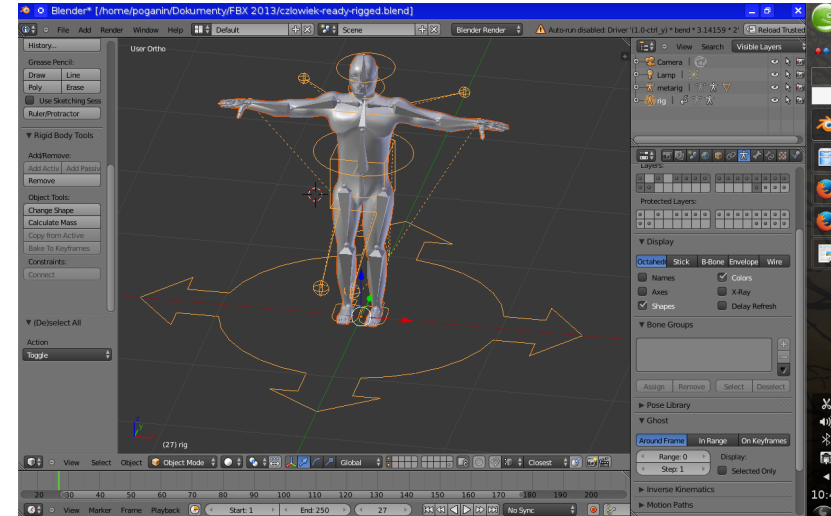


<https://www.youtube.com/watch?v=zvUfiKQI5jQ>

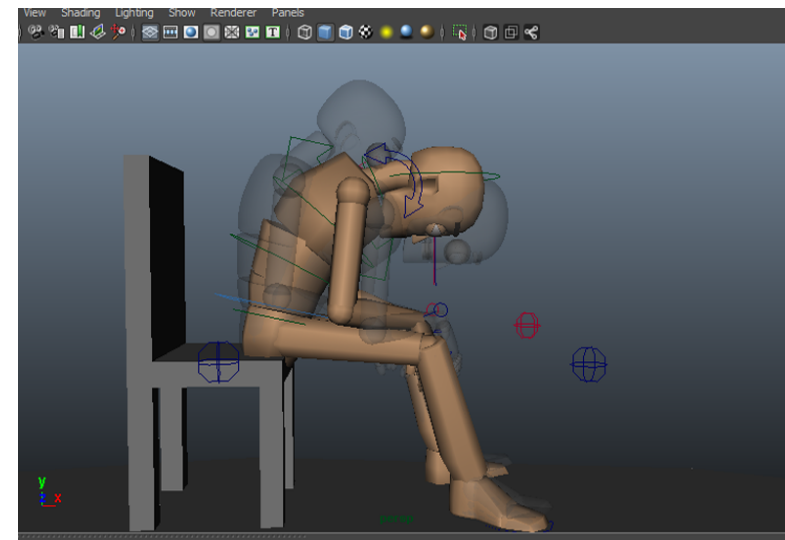
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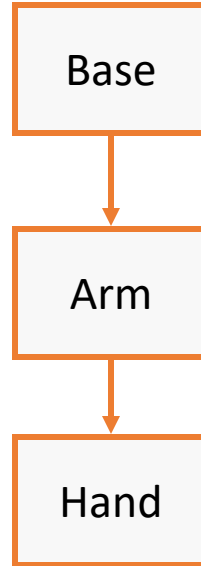


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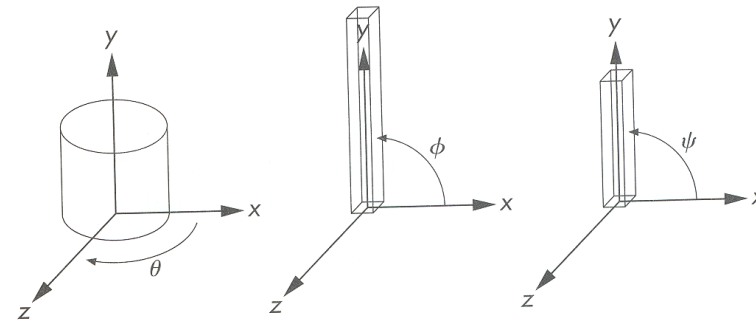
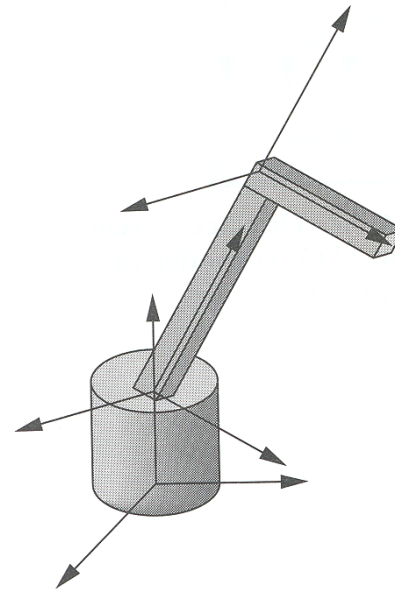
# Articulated Figures



- Character poses described by set of rigid bodies connected by “joints”



Scene Graph

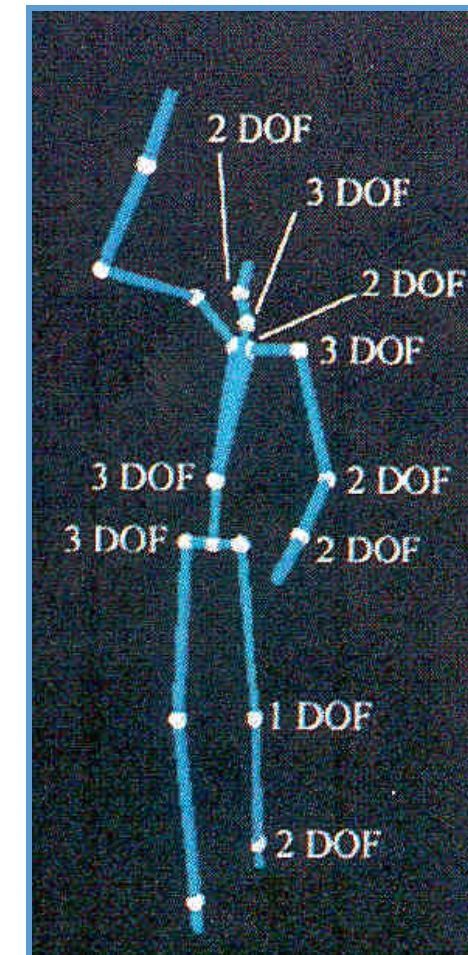
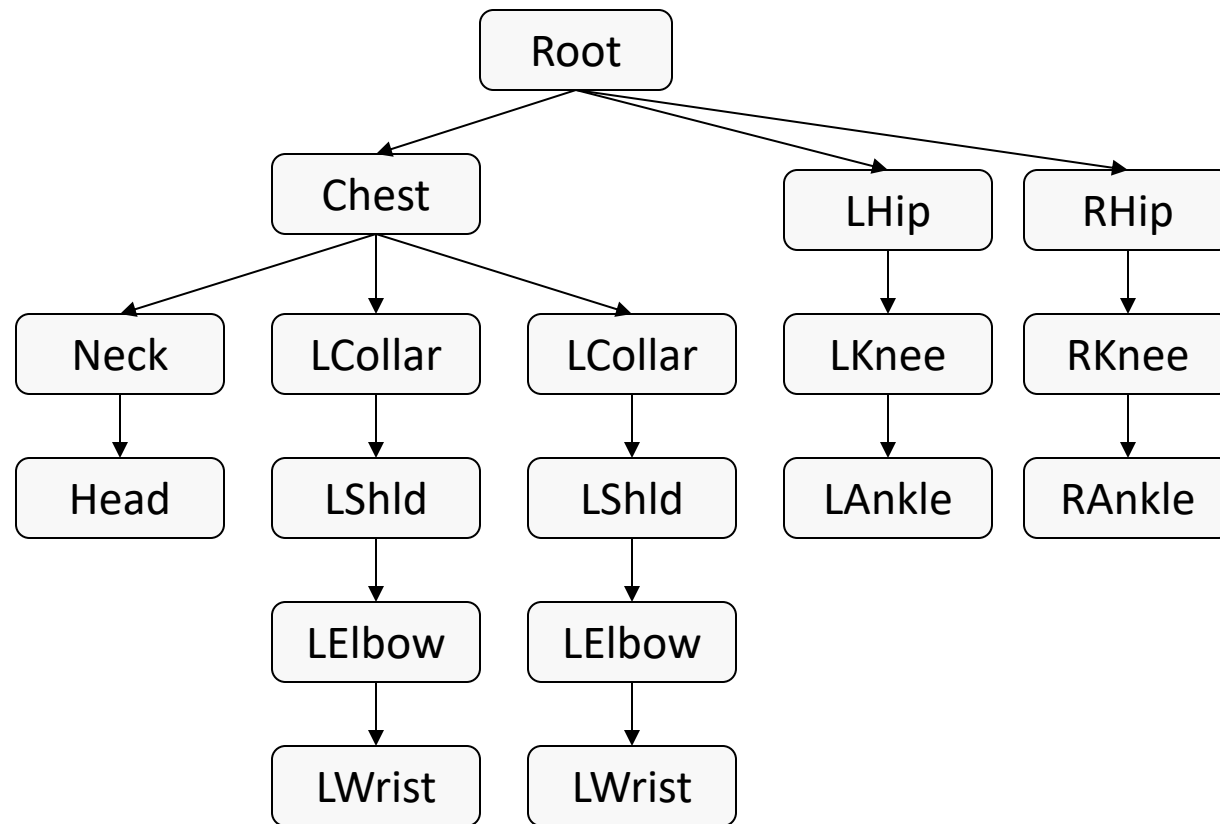


Angel Figures 8.8 & 8.9

# Articulated Figures

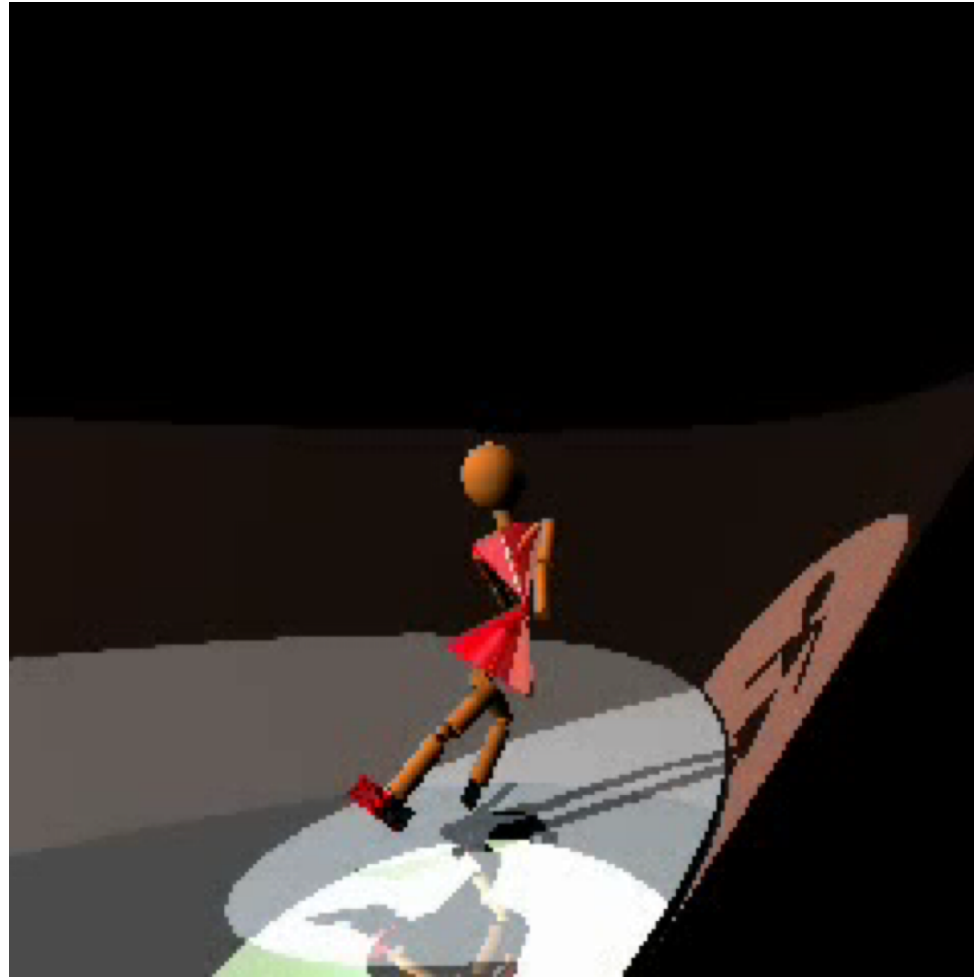


- Well-suited for humanoid characters



Rose et al. '96

# Example: Ice Skating



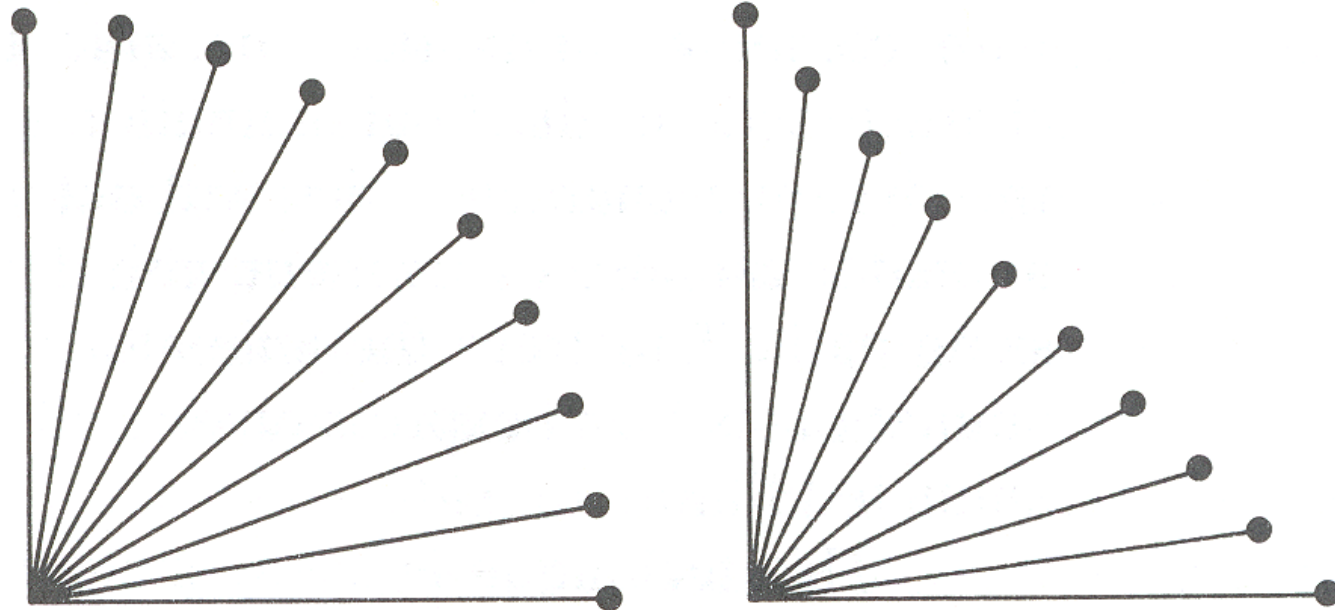
(Mao Chen, Zaijin Guan, Zhiyan Liu, Xiaohu Qie,  
CS426, Fall98, Princeton University)



# Articulated Figures



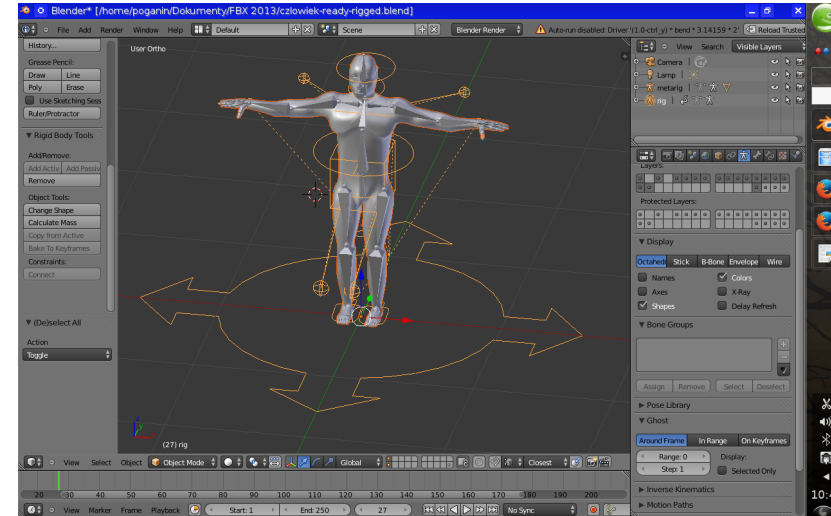
- Animation focuses on **joint angles**, or **general transformations**



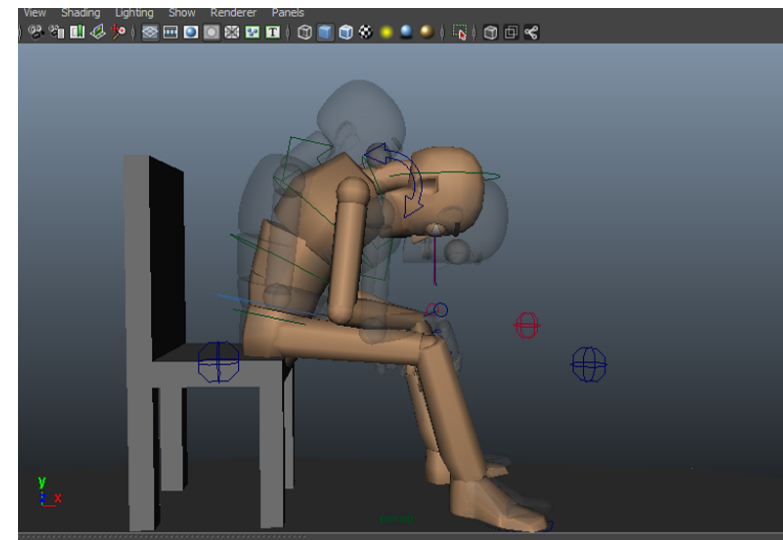
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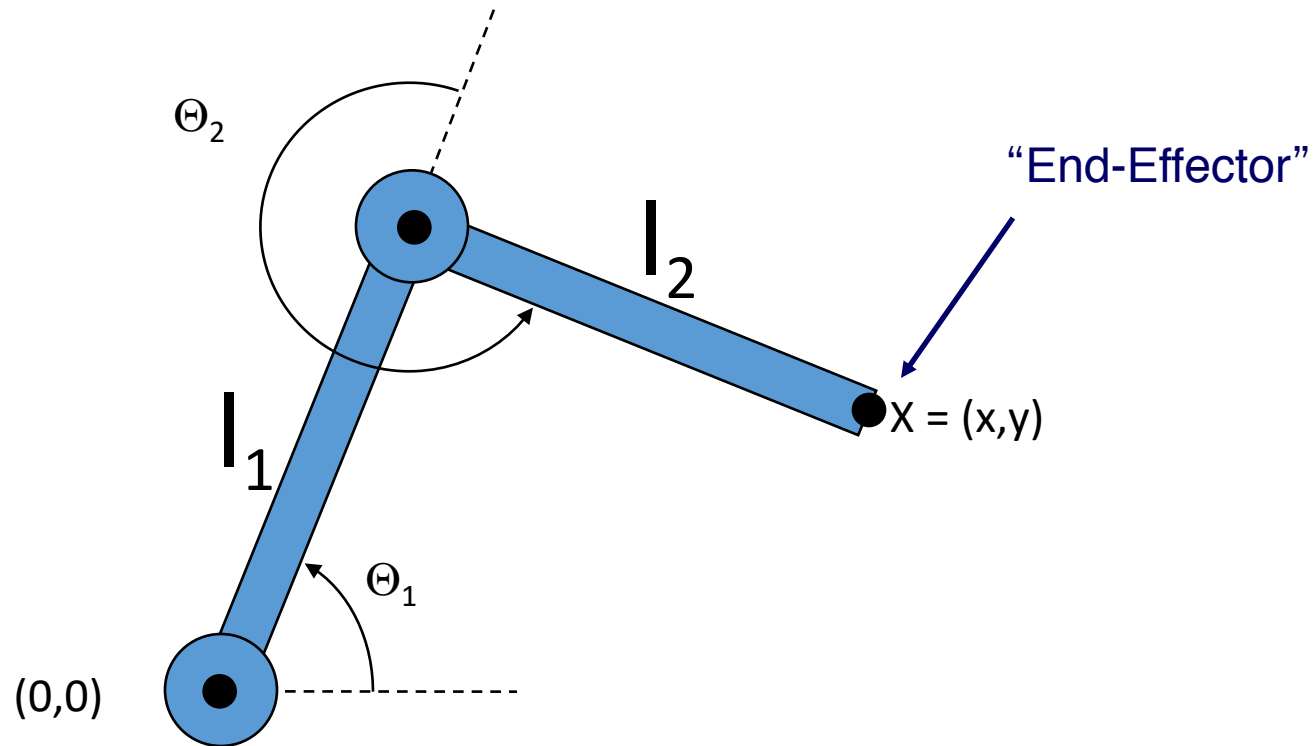


[focus.gscept.com](http://focus.gscept.com)

# Forward Kinematics



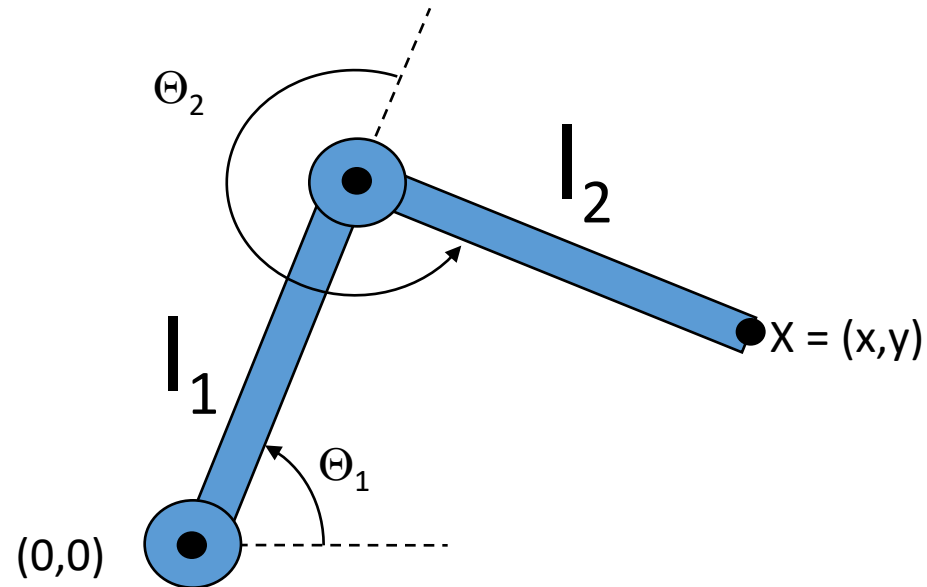
- Describe motion of articulated character



# Forward Kinematics



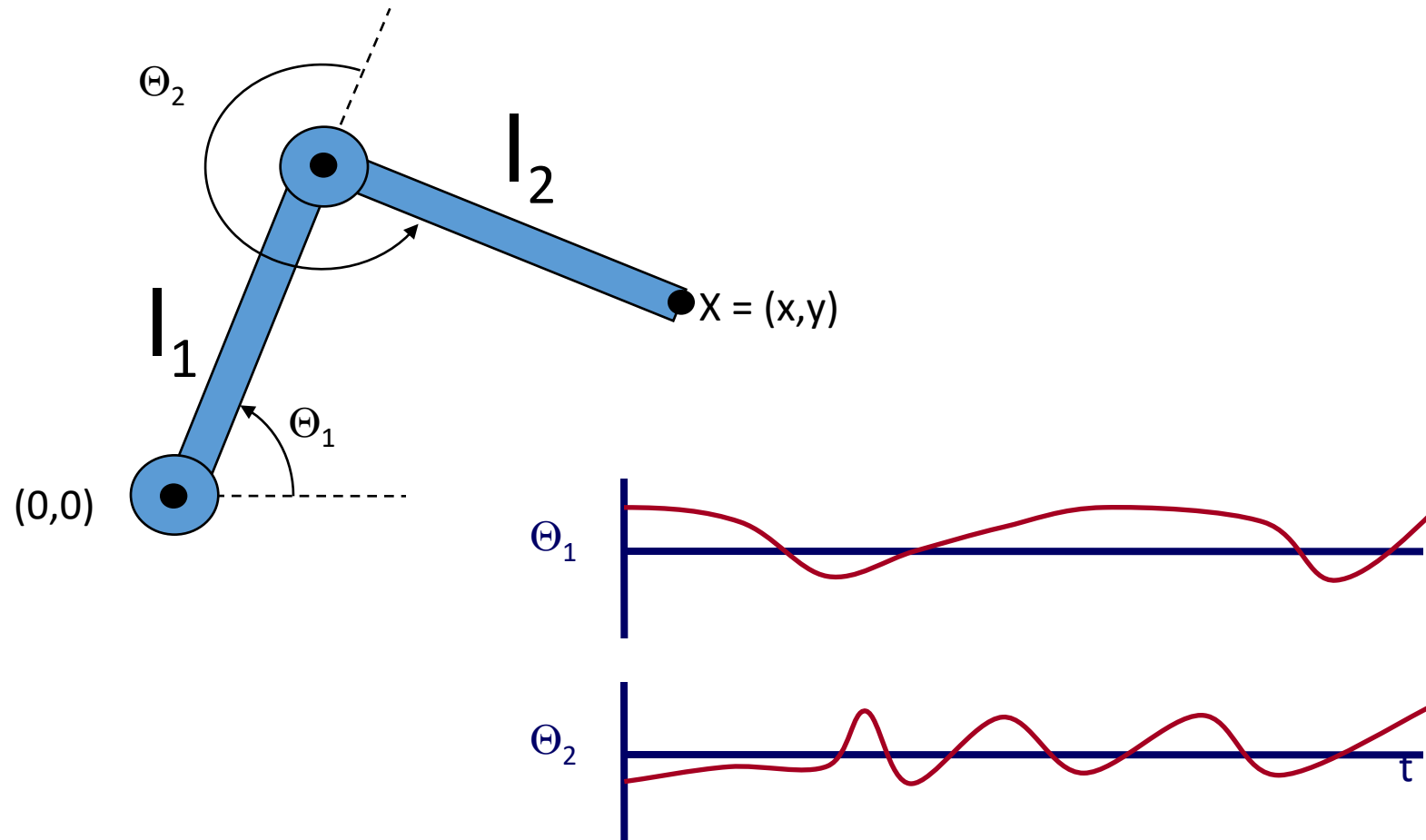
- Animator specifies joint angles:  $\Theta_1$  and  $\Theta_2$
- Computer finds positions of end-effector:  $X$



$$X = (l_1 \cos \Theta_1 + l_2 \cos(\Theta_1 + \Theta_2), l_1 \sin \Theta_1 + l_2 \sin(\Theta_1 + \Theta_2))$$

# Forward Kinematics

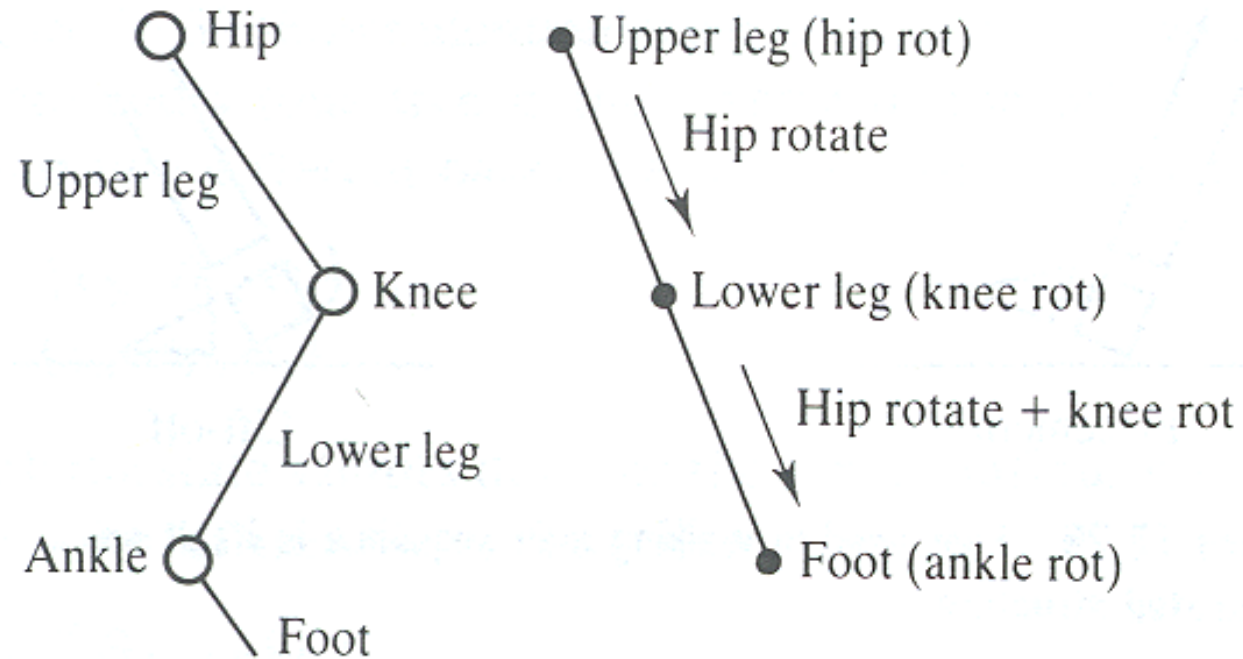
- Joint motions specified e.g. by spline curves



# Example: Walk Cycle



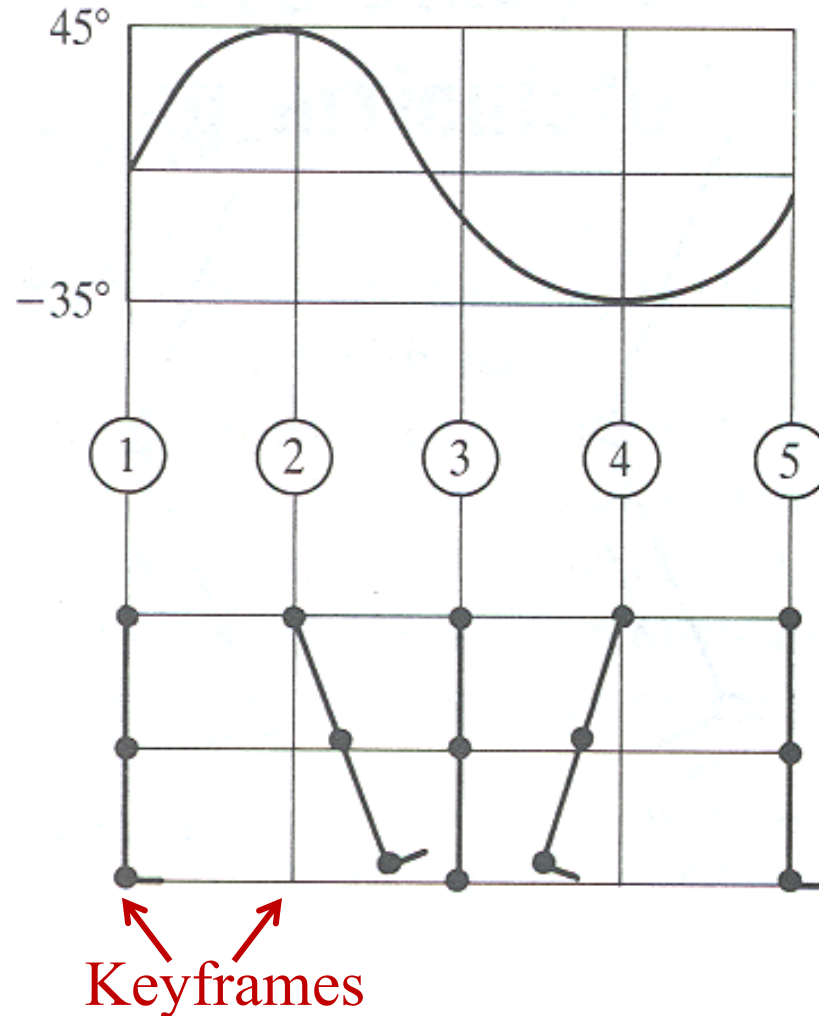
- Articulated figure:



# Example: Walk Cycle



- Hip joint orientation:

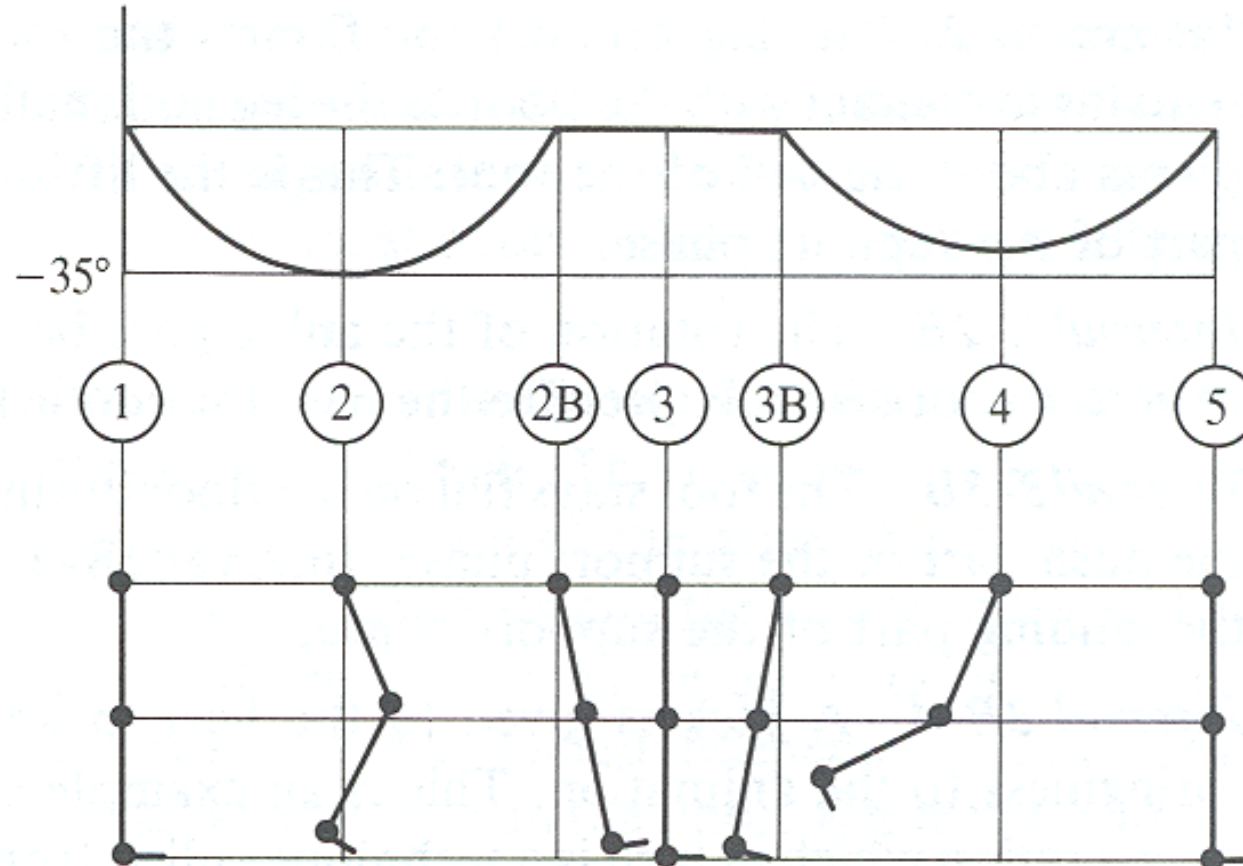


Watt & Watt

# Example: Walk Cycle



- Knee joint orientation:

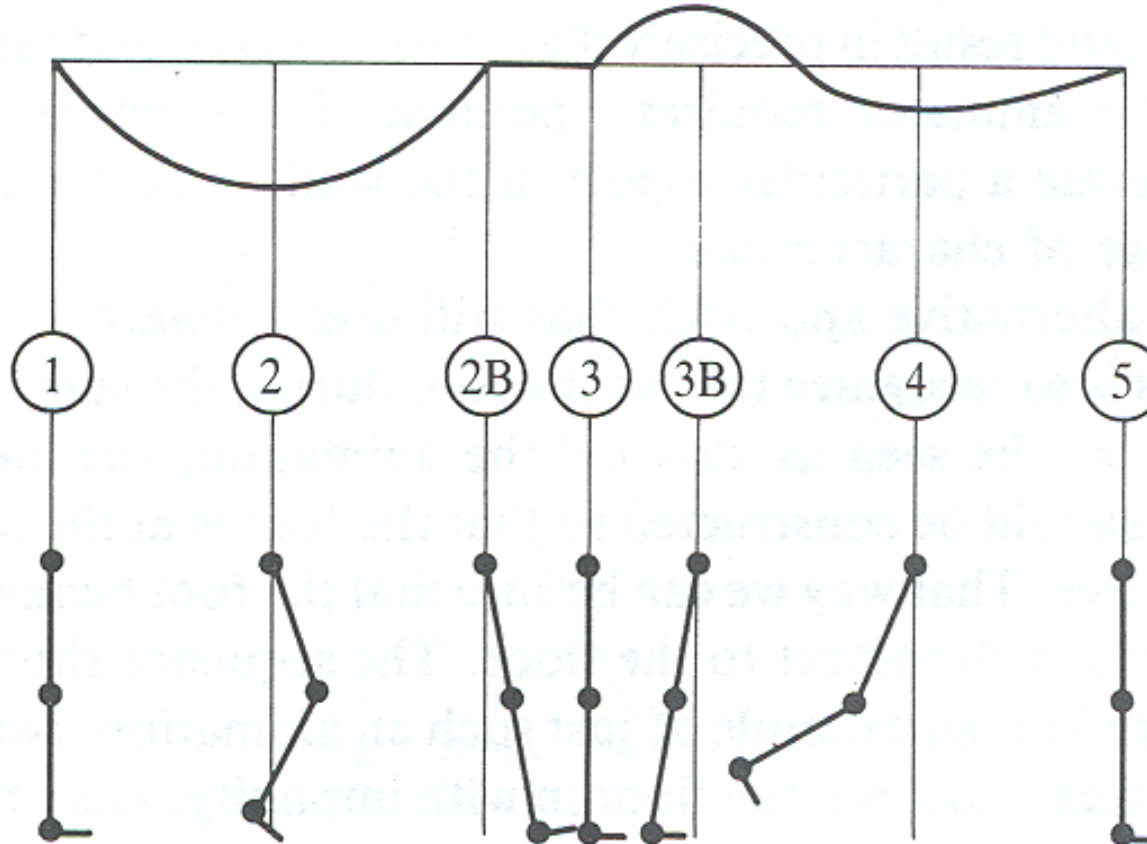




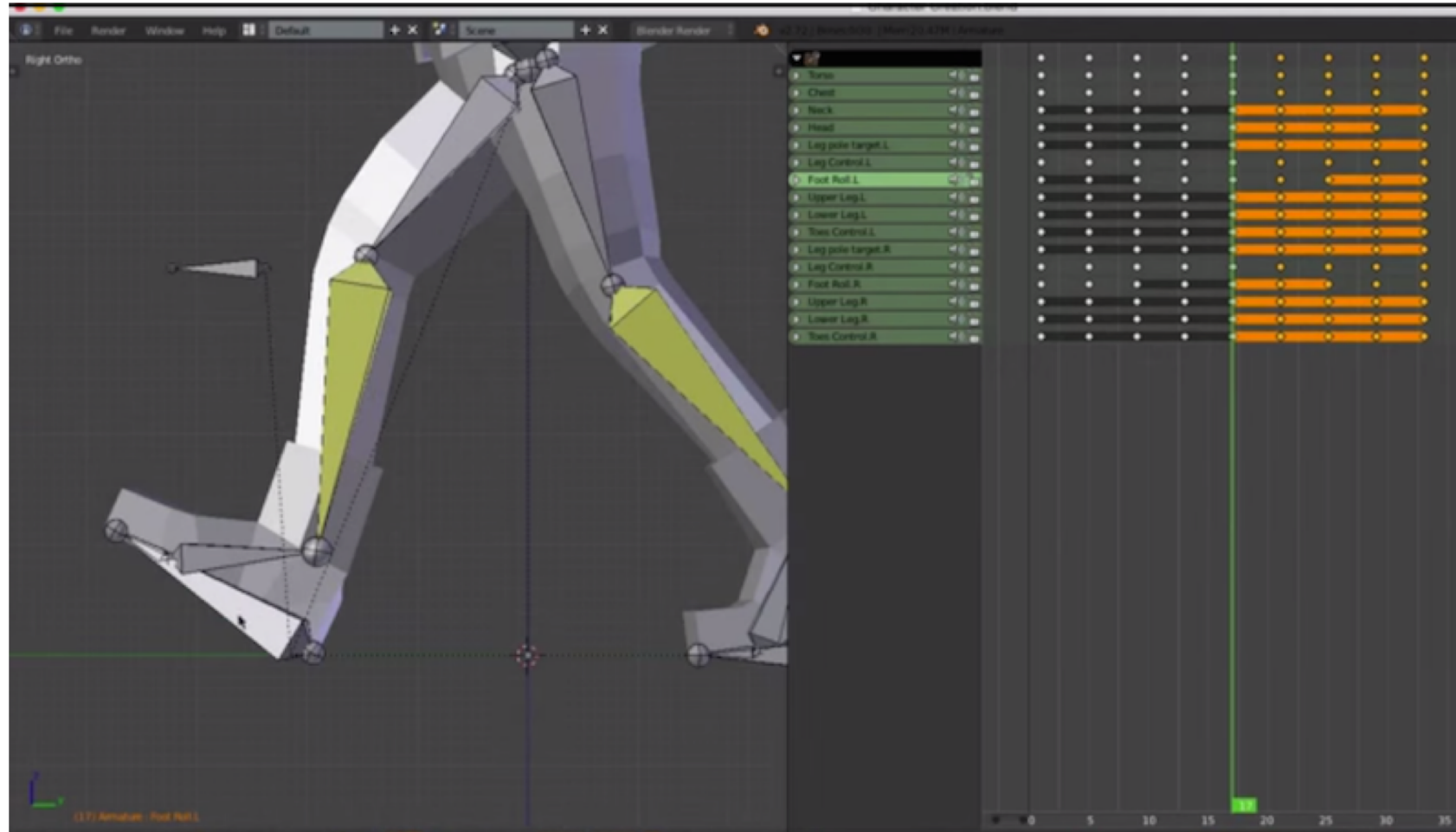
# Example: Walk Cycle



- Ankle joint orientation:



# Example: walk cycle

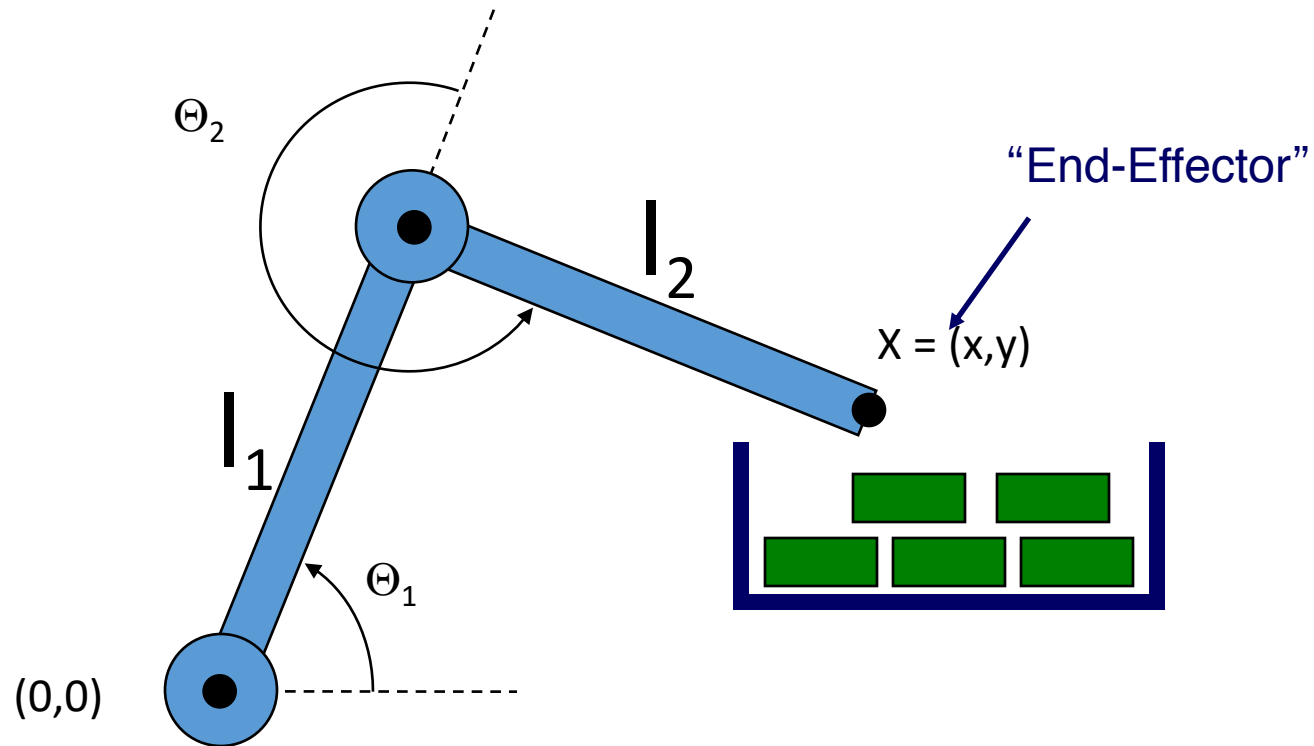


<https://www.youtube.com/watch?v=DuUWxUitJos>

# Inverse Kinematics



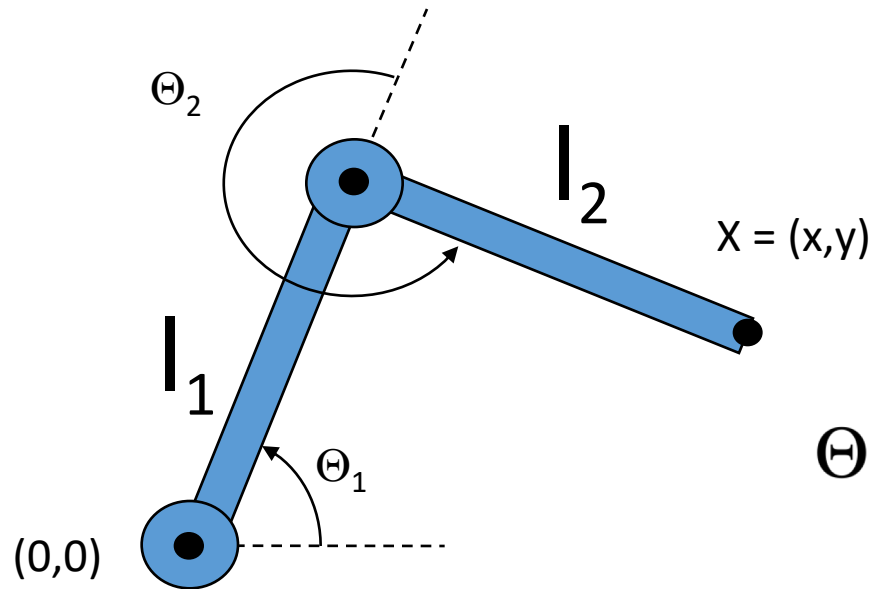
- What if animator knows position of “end-effector”?



# Inverse Kinematics



- Animator specifies end-effector positions:  $X$
- Computer finds joint angles:  $\Theta_1$  and  $\Theta_2$ :



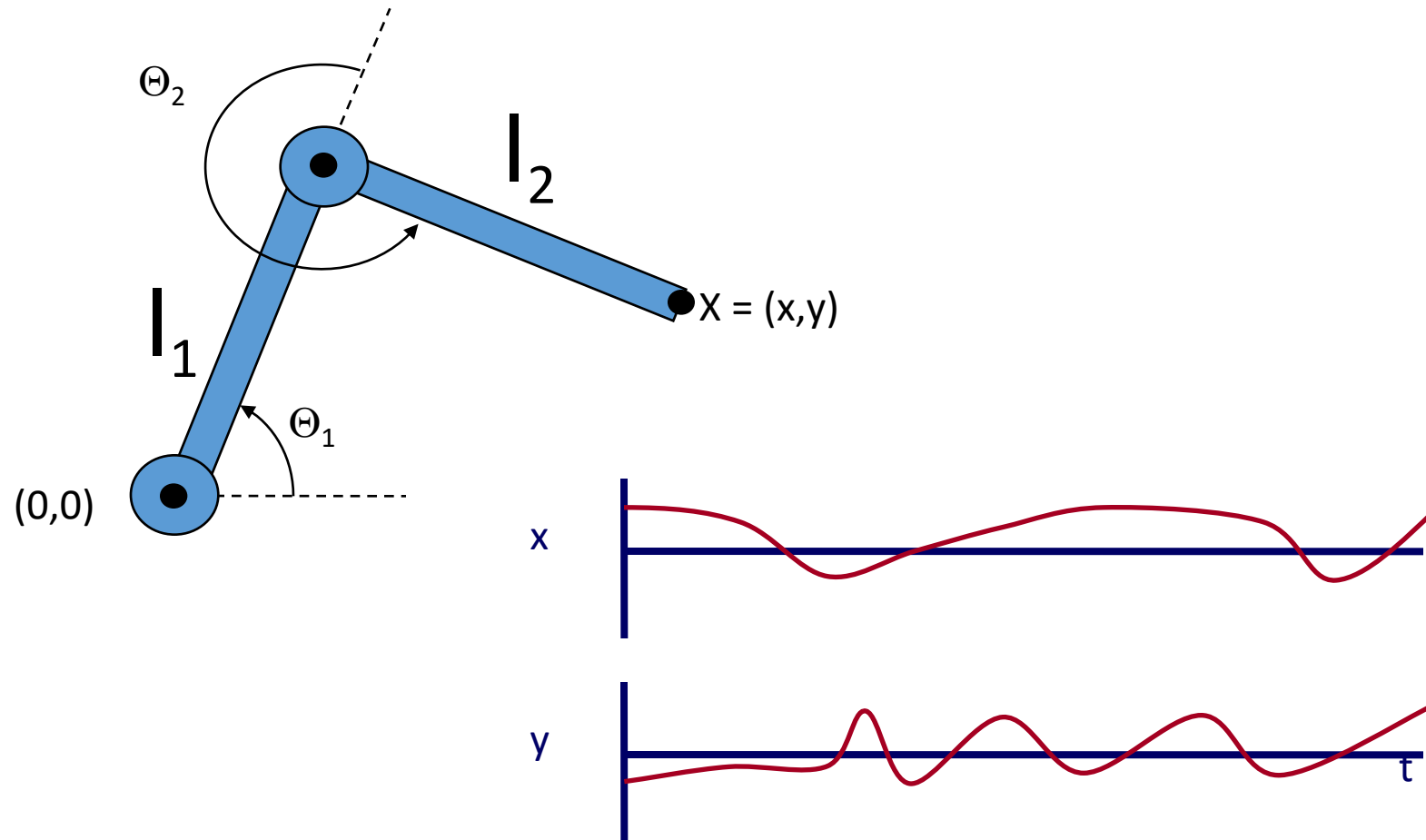
$$\Theta_2 = \cos^{-1} \left( \frac{x^2 + y^2 - l_1^2 - l_2^2}{2l_1l_2} \right)$$

$$\Theta_1 = \frac{-(l_2 \sin(\Theta_2)x + (l_1 + l_2 \cos(\Theta_2))y)}{(l_2 \sin(\Theta_2))y + (l_1 + l_2 \cos(\Theta_2))x}$$

# Inverse Kinematics



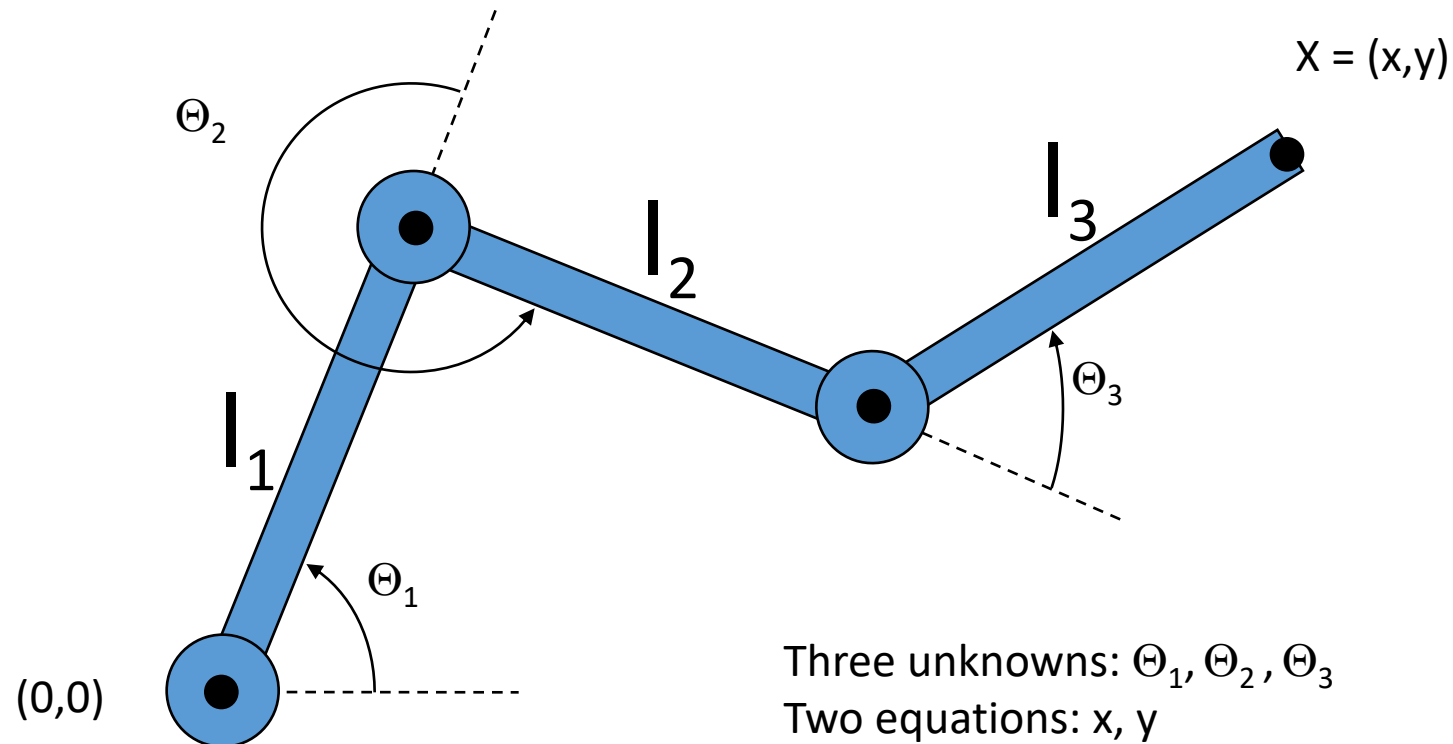
- End-effector positions can be specified by spline curves



# Inverse Kinematics



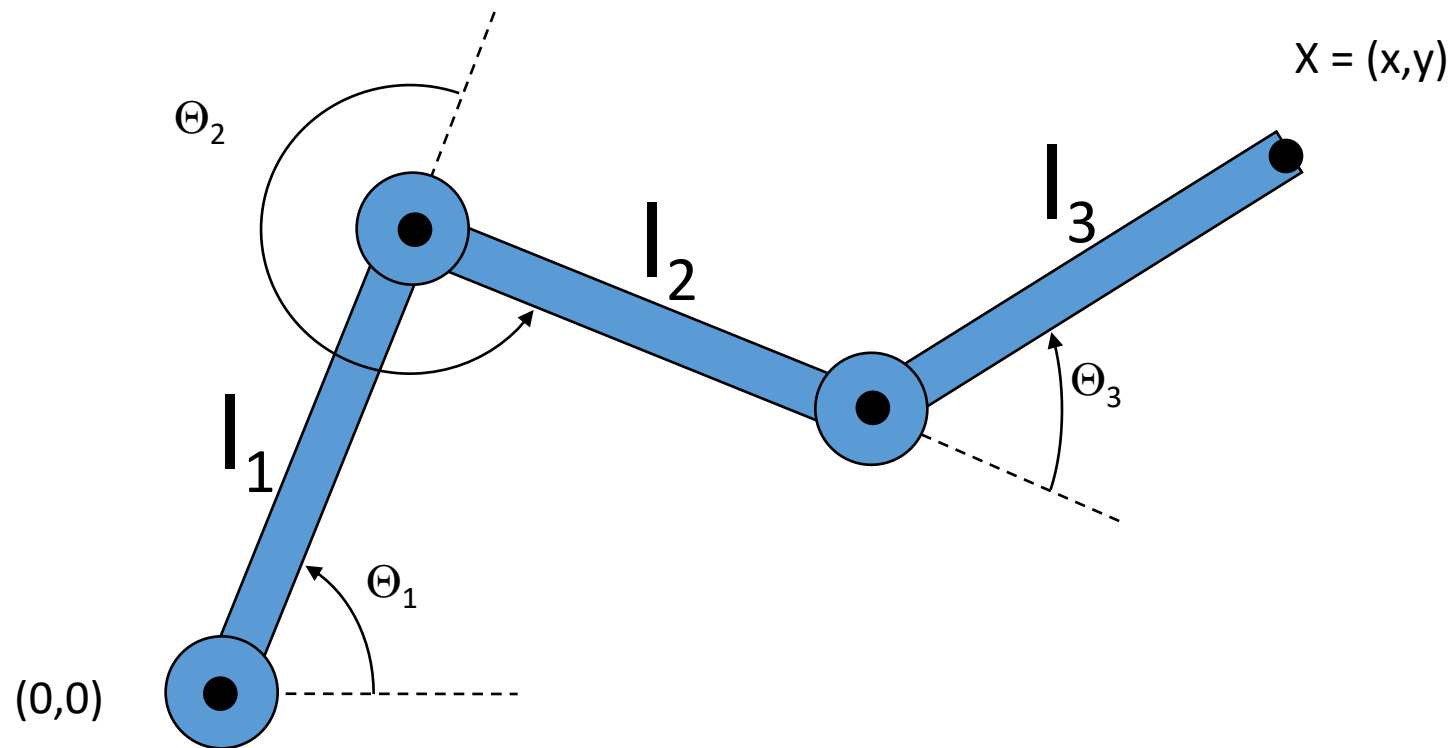
- Problem for more complex structures
  - System of equations is usually under-constrained
  - Multiple solutions



# Inverse Kinematics



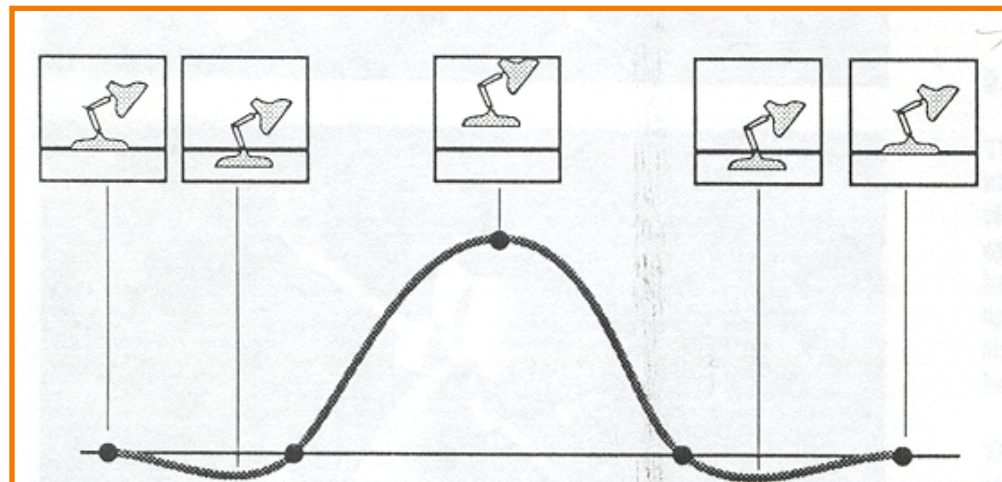
- Solution for more complex structures:
  - Find best solution (e.g., minimize energy in motion)
  - Non-linear optimization



# Kinematics



- Advantages
  - Simple to implement
  - Complete animator control
- Disadvantages
  - Motions may not follow physical laws
  - Tedious for animator



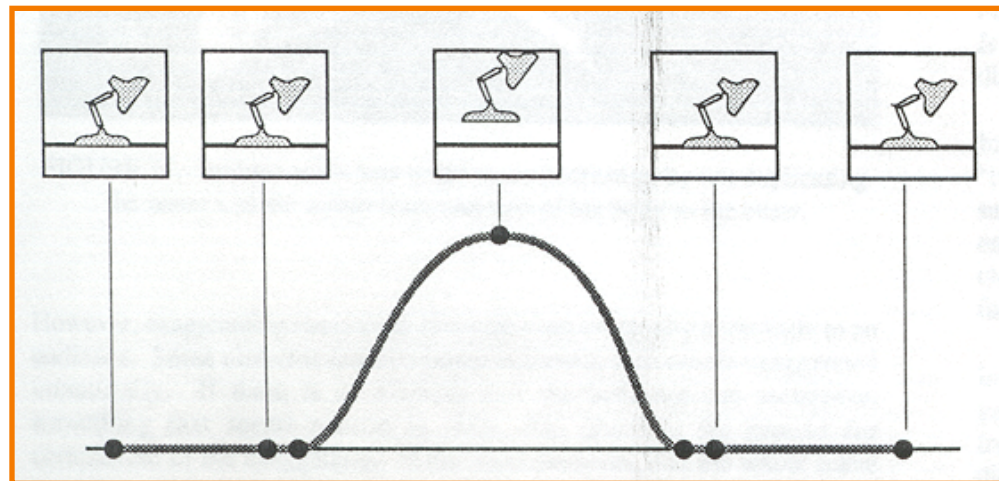
Lasseter '87



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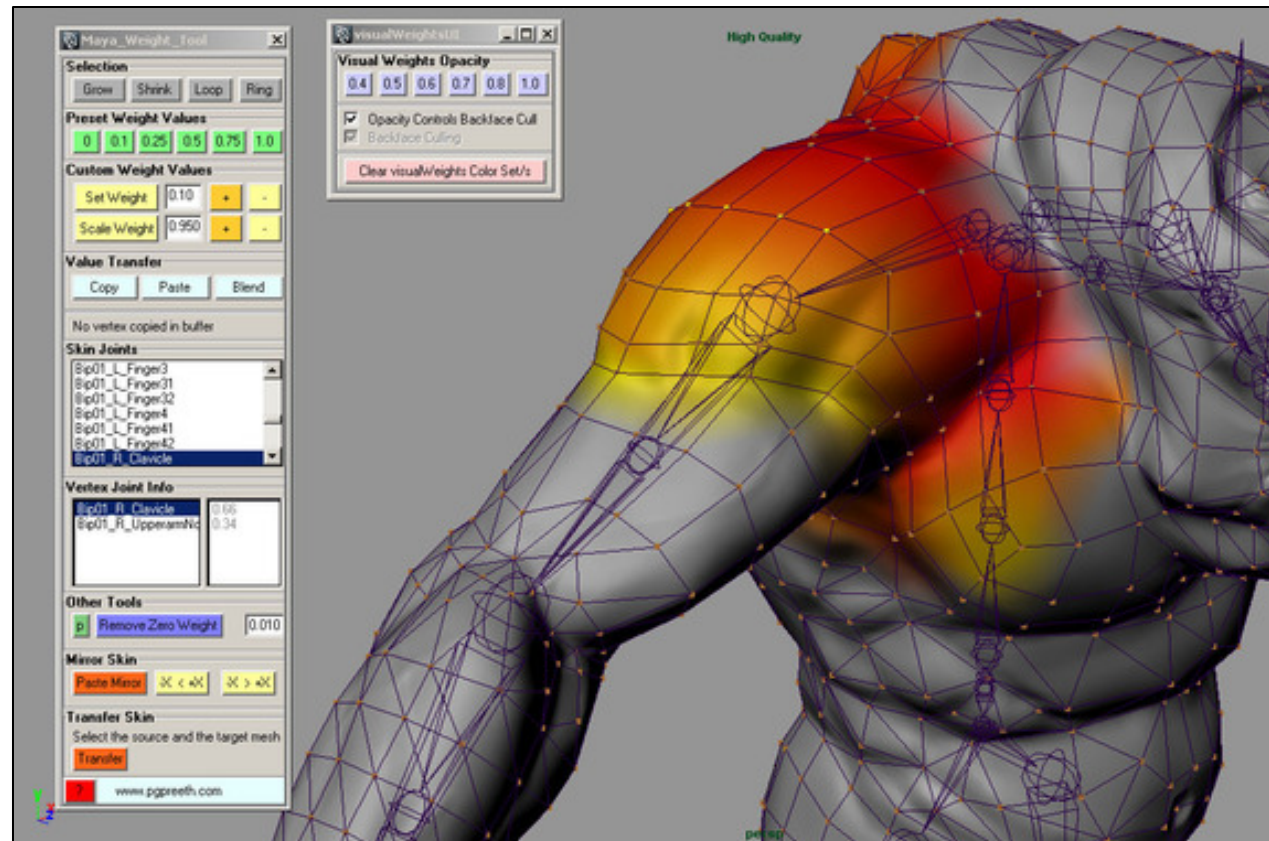


Lasseter '87

# Beyond Skeletons...



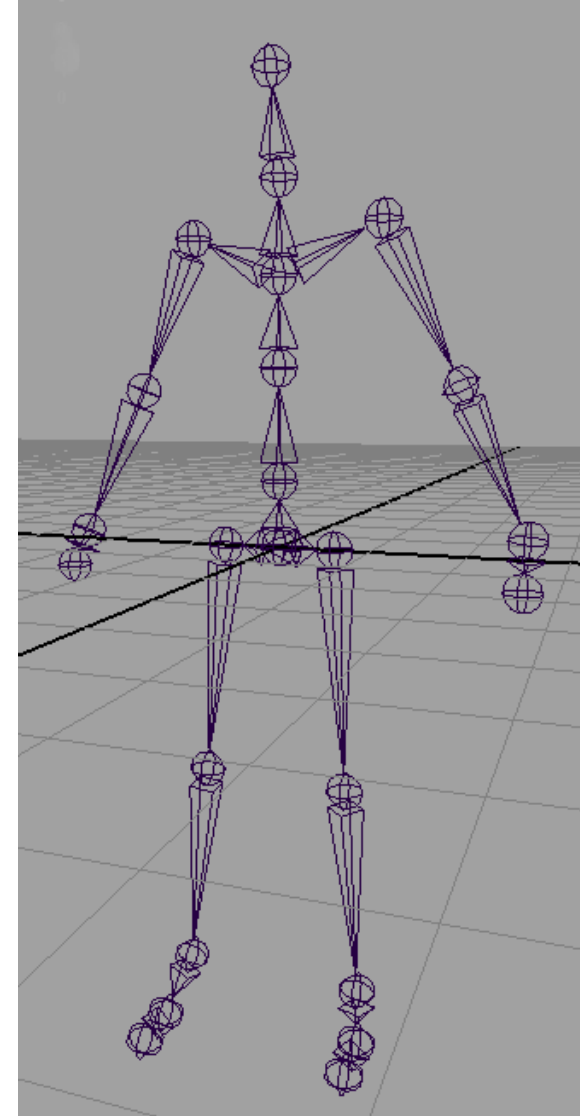
- Skinning



# Kinematic Skeletons



- Hierarchy of transformations (“bones”)
  - Changes to parent affect all descendent bones
- So far: bones affect objects in scene or parts of a mesh
  - Equivalently, each point on a mesh acted upon by one bone
  - Leads to discontinuities when parts of mesh animated
- Extension: each point on a mesh acted upon by more than one bone



# Linear Blend Skinning



- Each vertex of skin potentially influenced by all bones
  - Normalized weight vector  $w^{(v)}$  gives influence of each bone transform
  - When bones move, influenced vertices also move

- Computing a transformation  $T_v$  for a skinned vertex

- For each bone
  - Compute global bone transformation  $T_b$  from transformation hierarchy
- For each vertex
  - Take a linear combination of bone transforms
  - Apply transformation to vertex in original pose

$$T_v = \sum_{b \in B} w_b^{(v)} T_b$$

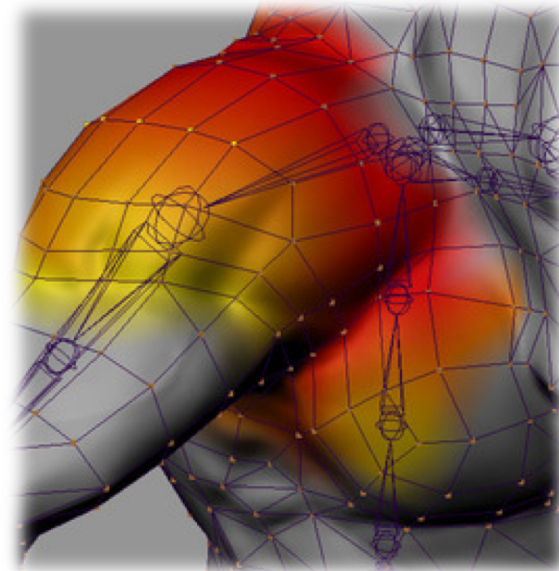
- Equivalently, transformed vertex position is weighted combination of positions transformed by bones

$$v_{transformed} = \sum_{b \in B} w_b^{(v)} (T_b v)$$

# Assigning Weights: “Rigging”



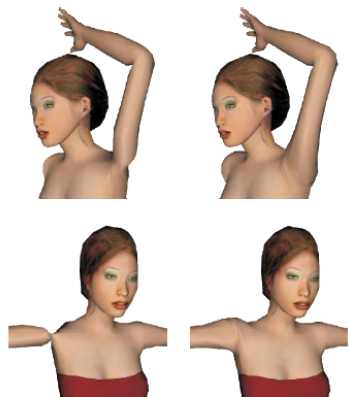
- Painted by hand
- Automatic: function of relative distances to nearest bones
  - Smoothness of skinned surface depends on smoothness of weights!



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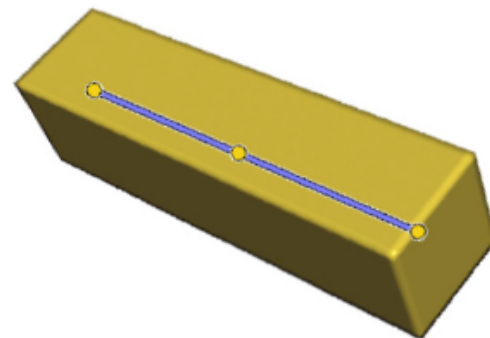


- Painted by hand
- Automatic: function of relative distances to nearest bones
  - Smoothness of skinned surface depends on smoothness of weights!
  - Other problems with extreme deformations
    - Many solutions

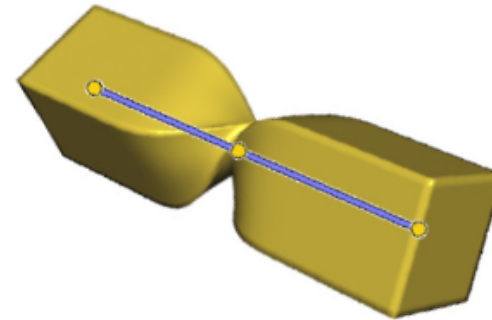


[Kavan et al. SG '08]

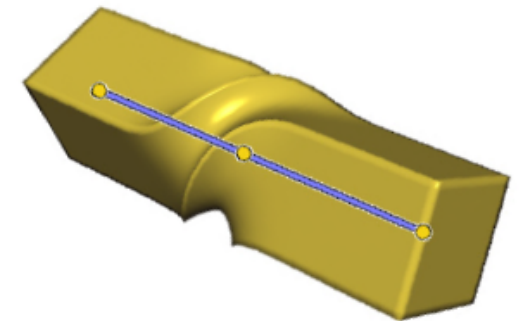
Figure 14: Comparison of linear (left) and dual quaternion (right) blending. Dual quaternions preserve rigidity of input transformations and therefore avoid skin collapsing artifacts.



Rest pose



Linear blend skinning



Dual quaternion skinning

[Kavan, SG'14 course]

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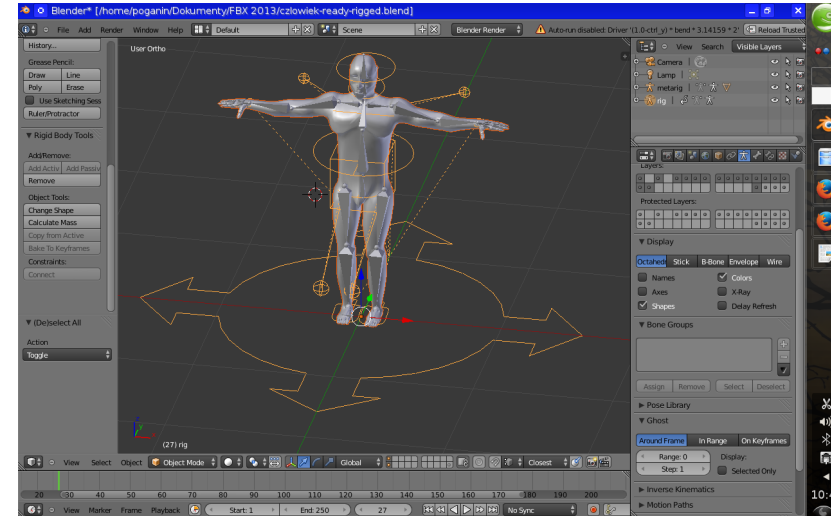


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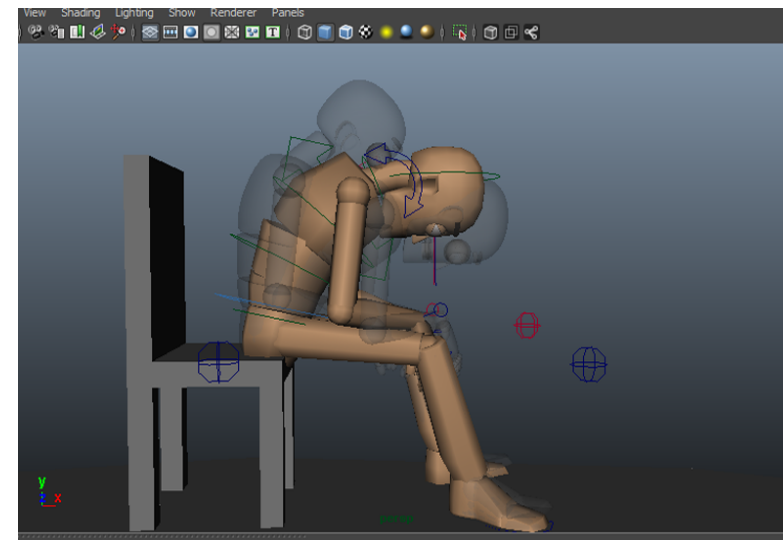
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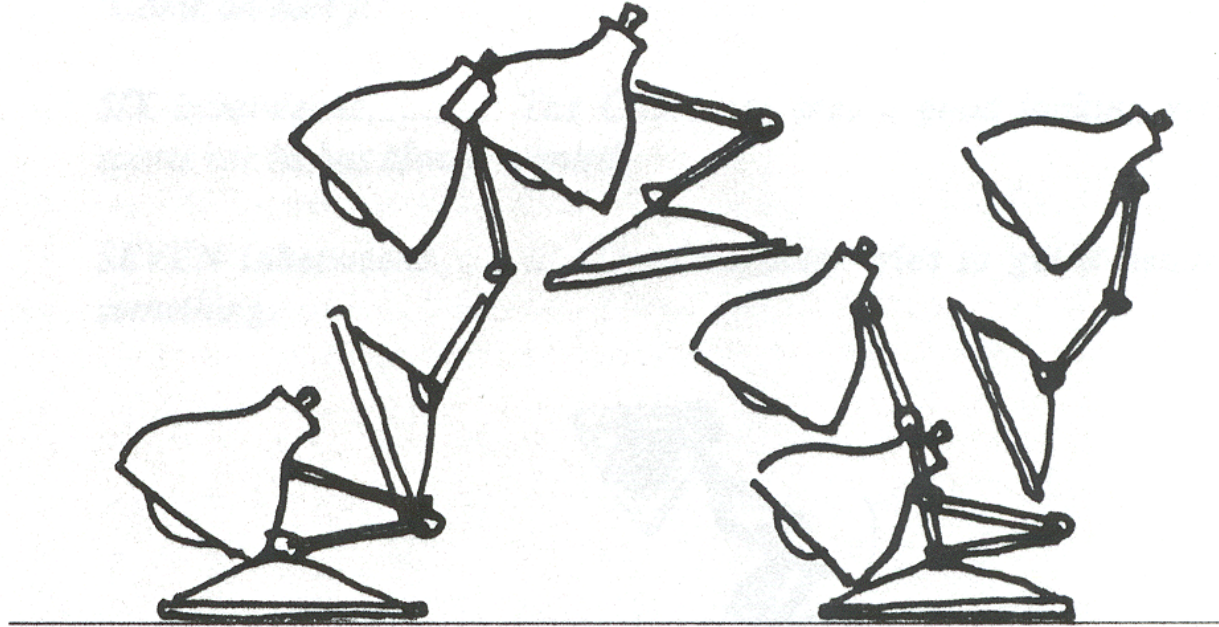
[focus.gscept.com](http://focus.gscept.com)



# Keyframe Animation



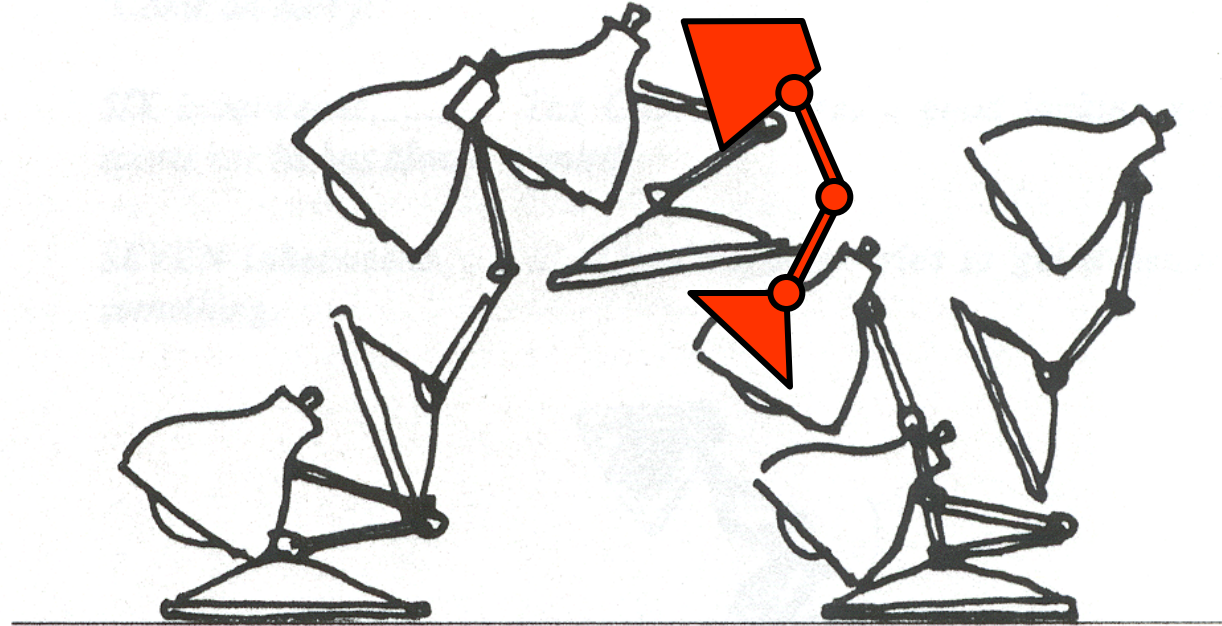
- Define character poses at specific time steps called “keyframes”



# Keyframe Animation



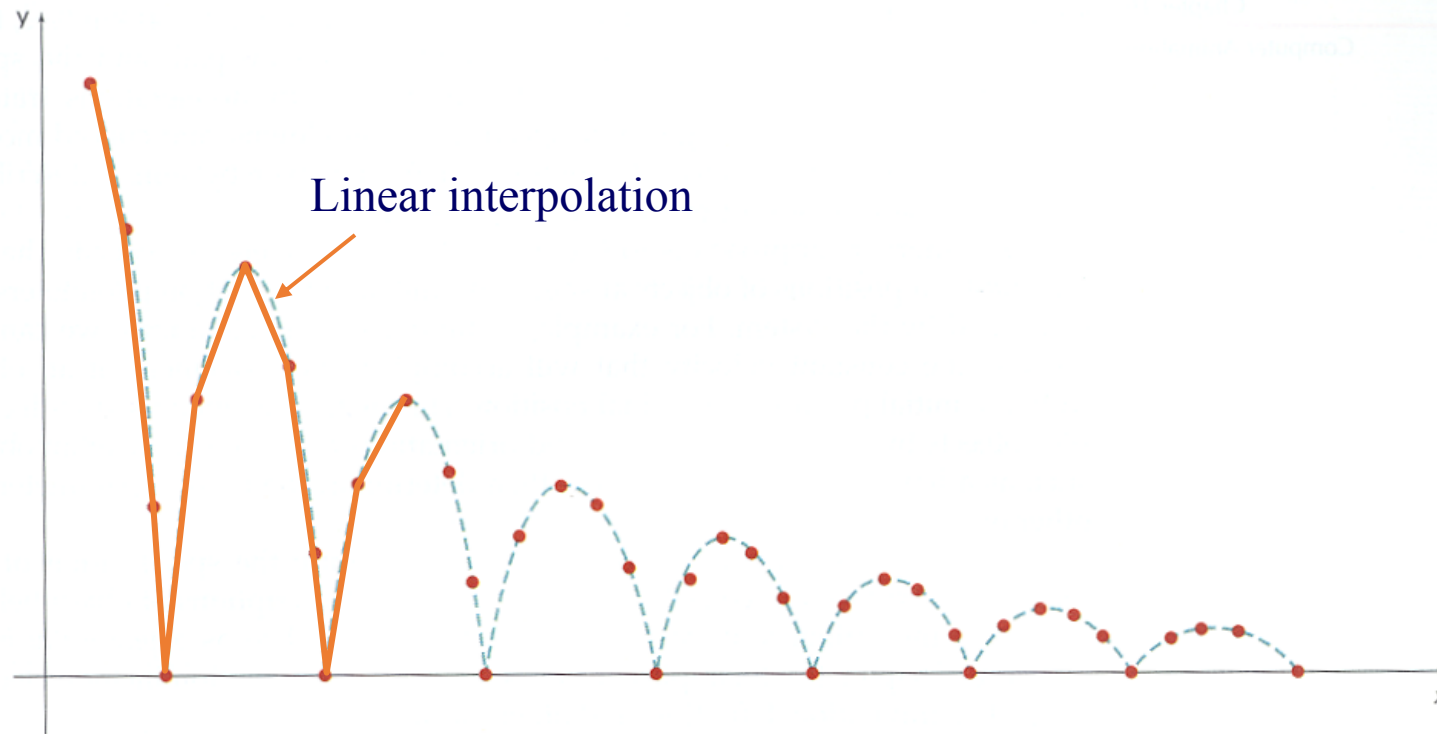
- Interpolate variables describing keyframes to determine poses for character in between



# Keyframe Animation



- Inbetweening:
  - Linear interpolation - usually not enough continuity

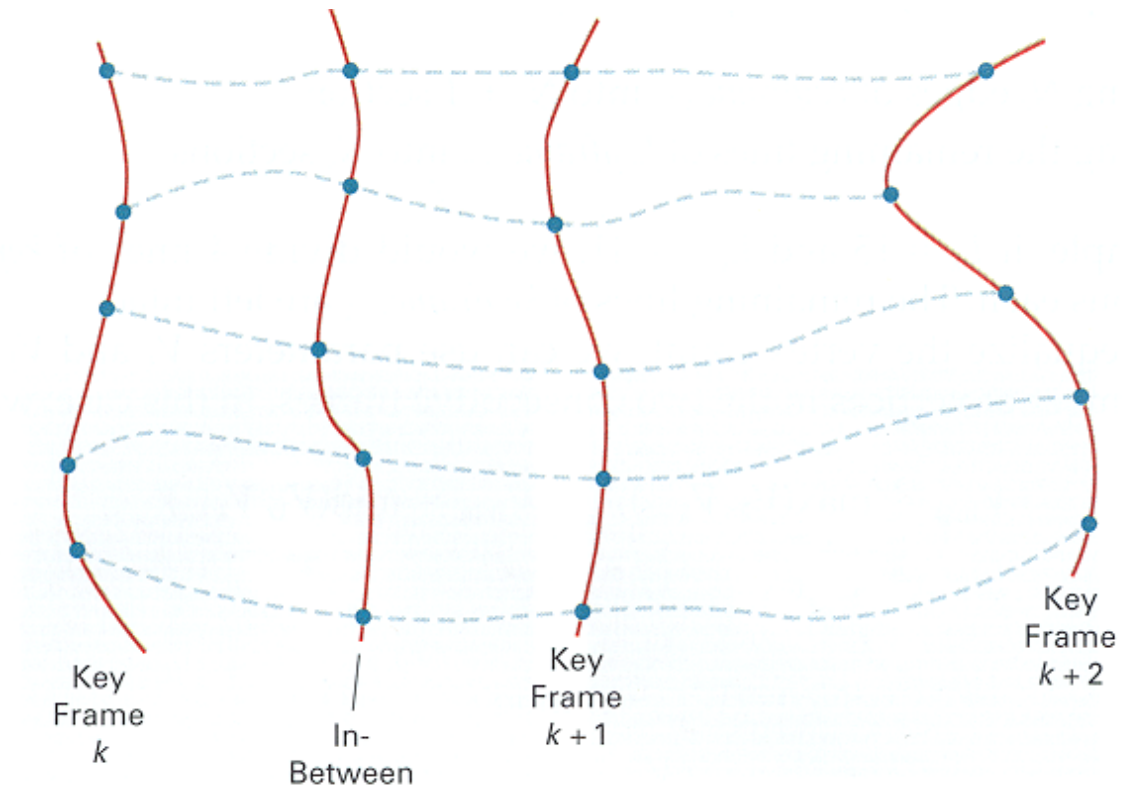


H&B Figure 16.16

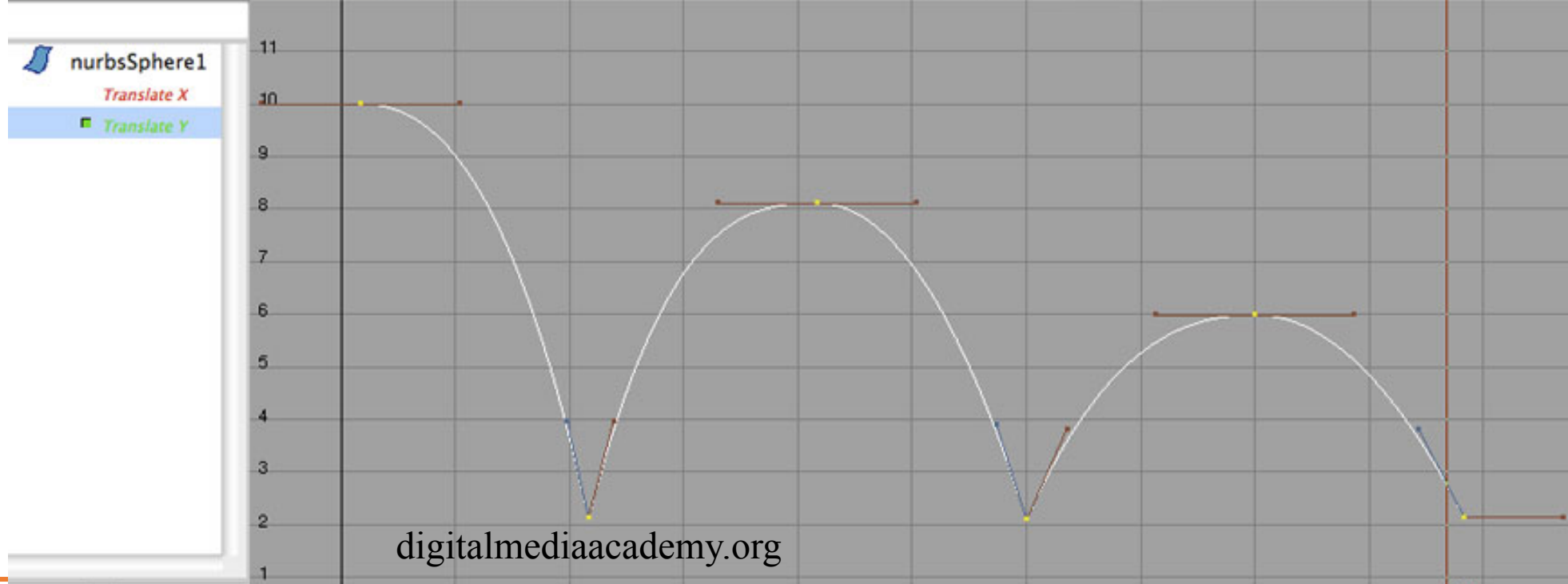
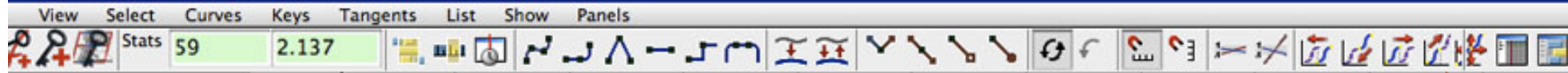
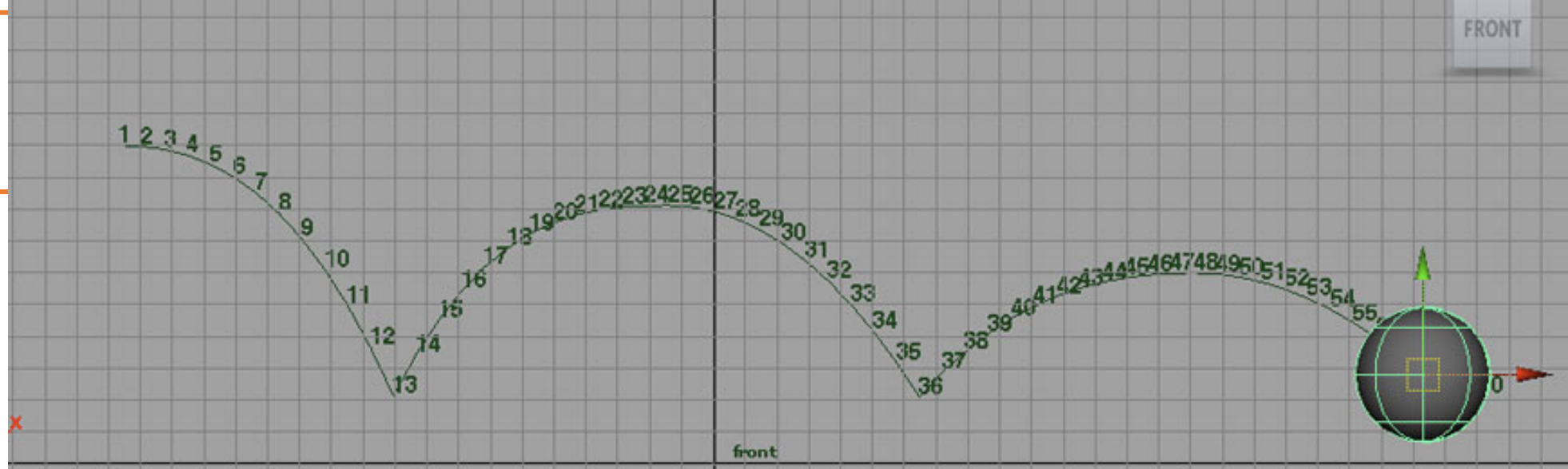
# Keyframe Animation



- Inbetweening:
  - Spline interpolation - maybe good enough



H&B Figure 16.11



# Example: Ball Boy



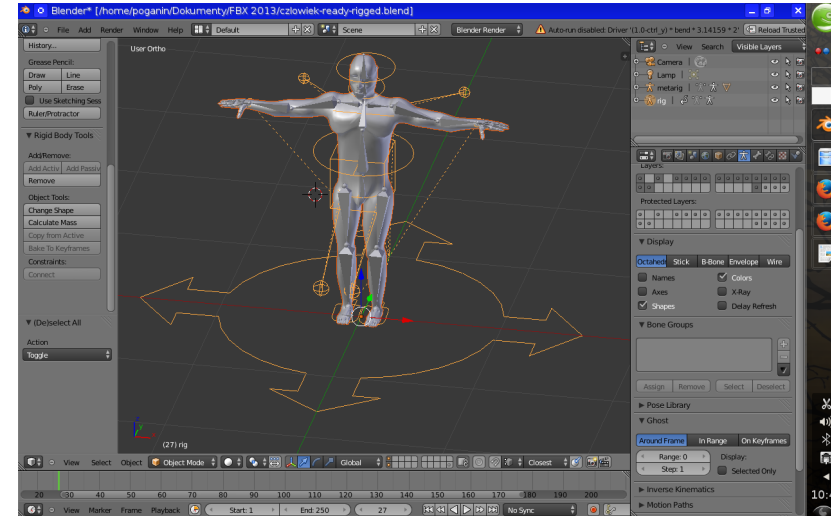
“Ballboy”

Fujito, Milliron, Ngan, & Sanocki  
Princeton University

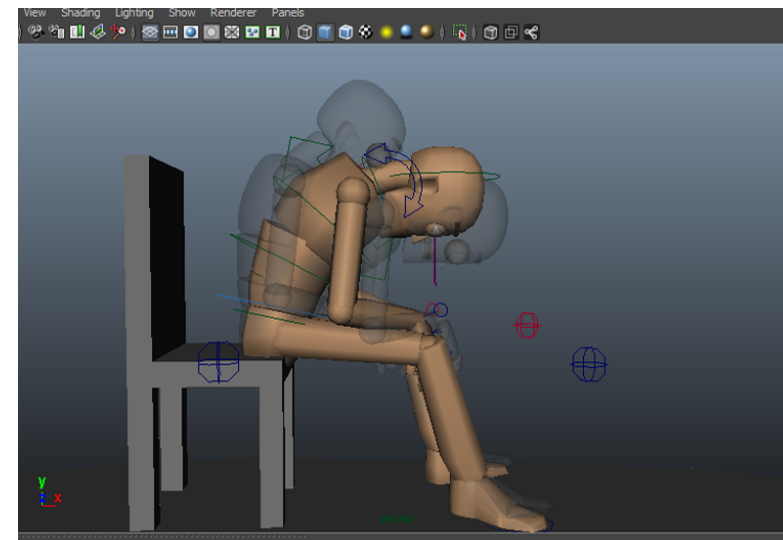
# Character Animation Methods



- Modeling (manipulation)
  - Deformation
  - Blendshapes
  - Skeletons
- Interpolation
  - Key-framing
  - Kinematics
  - Motion Capture



<https://blenderartists.org/>

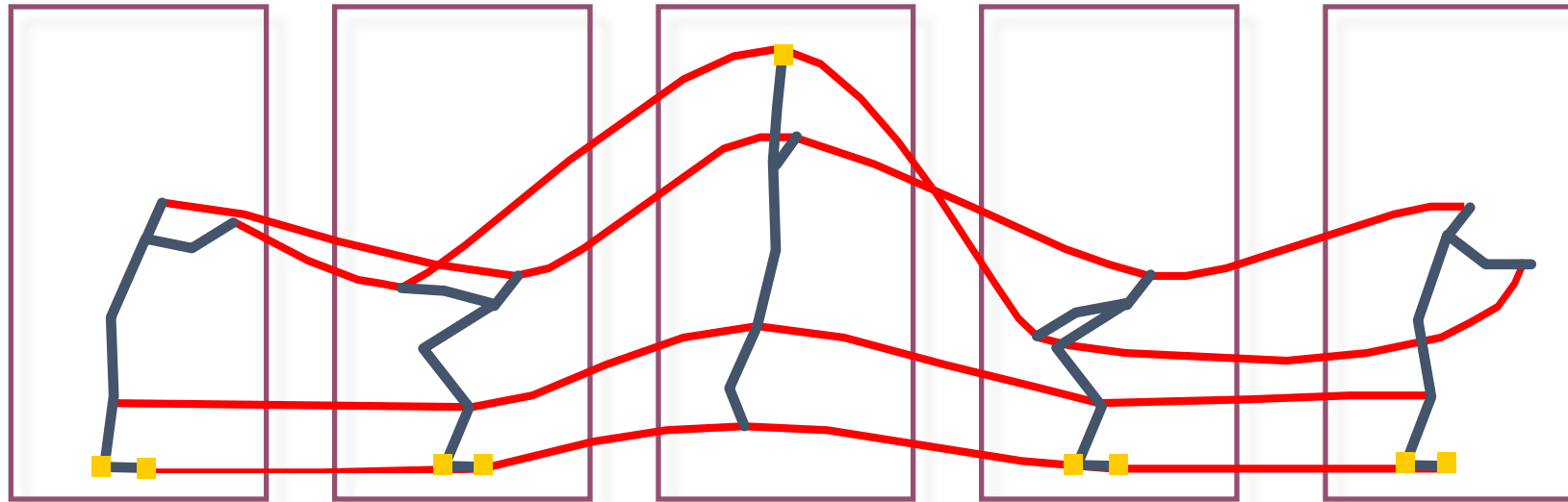


[focus.gscept.com](http://focus.gscept.com)

# Motion Capture



- Measure motion of real characters and then simply “play it back” with kinematics



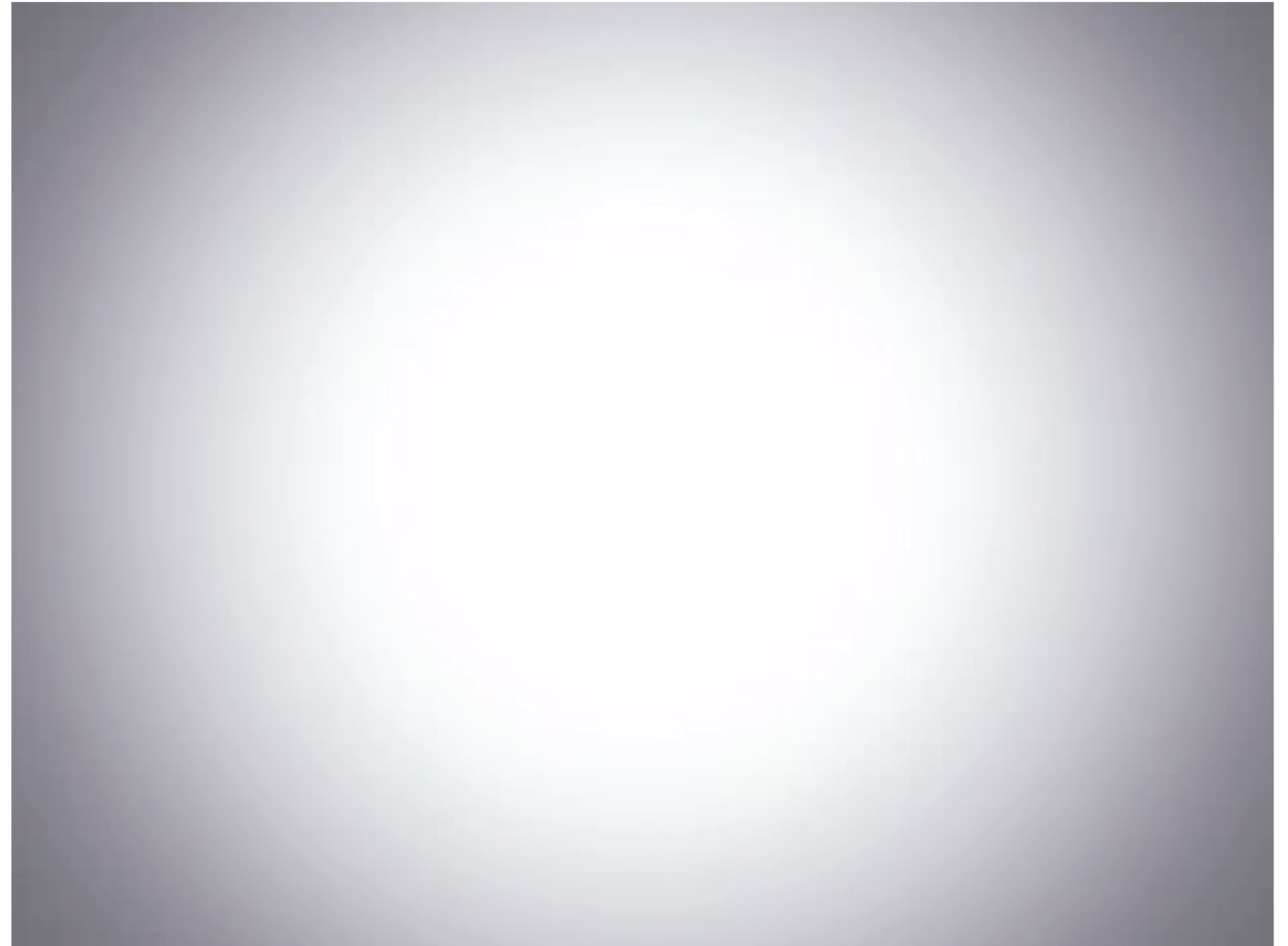
Captured Motion



# Motion Capture



- Measure human motion
- Play back with kinematics

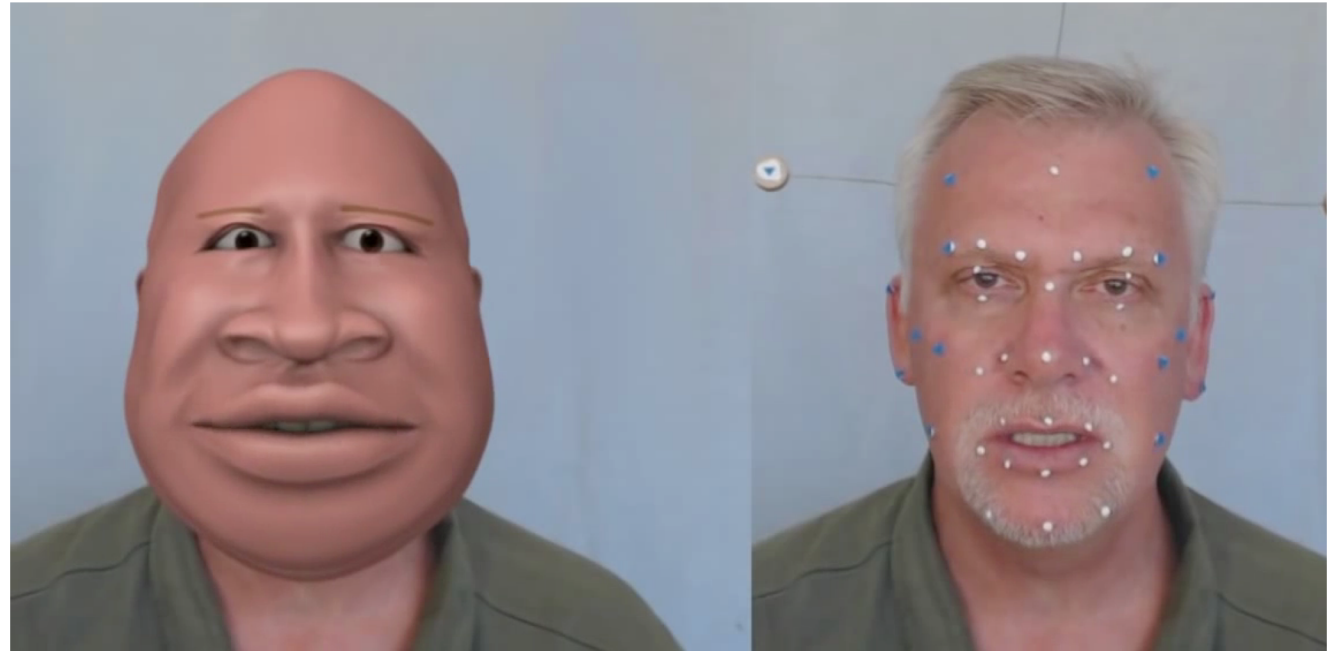


<https://www.youtube.com/watch?v=MVvDw15-3e8>

# Motion Capture



- Could be applied on different parameters
  - Skeleton Transformations
  - Direct mesh deformation
- Advantage:
  - Physical realism
- Challenge:
  - Animator control



# Summary



- Kinematics
  - Animator specifies poses (joint angles or positions) at keyframes and computer determines motion by kinematics and interpolation
- Dynamics
  - Animator specifies physical attributes, constraints, and starting conditions and computer determines motion by physical simulation
- Motion capture
  - Computer captures motion of real character and provides tools for animator to edit it