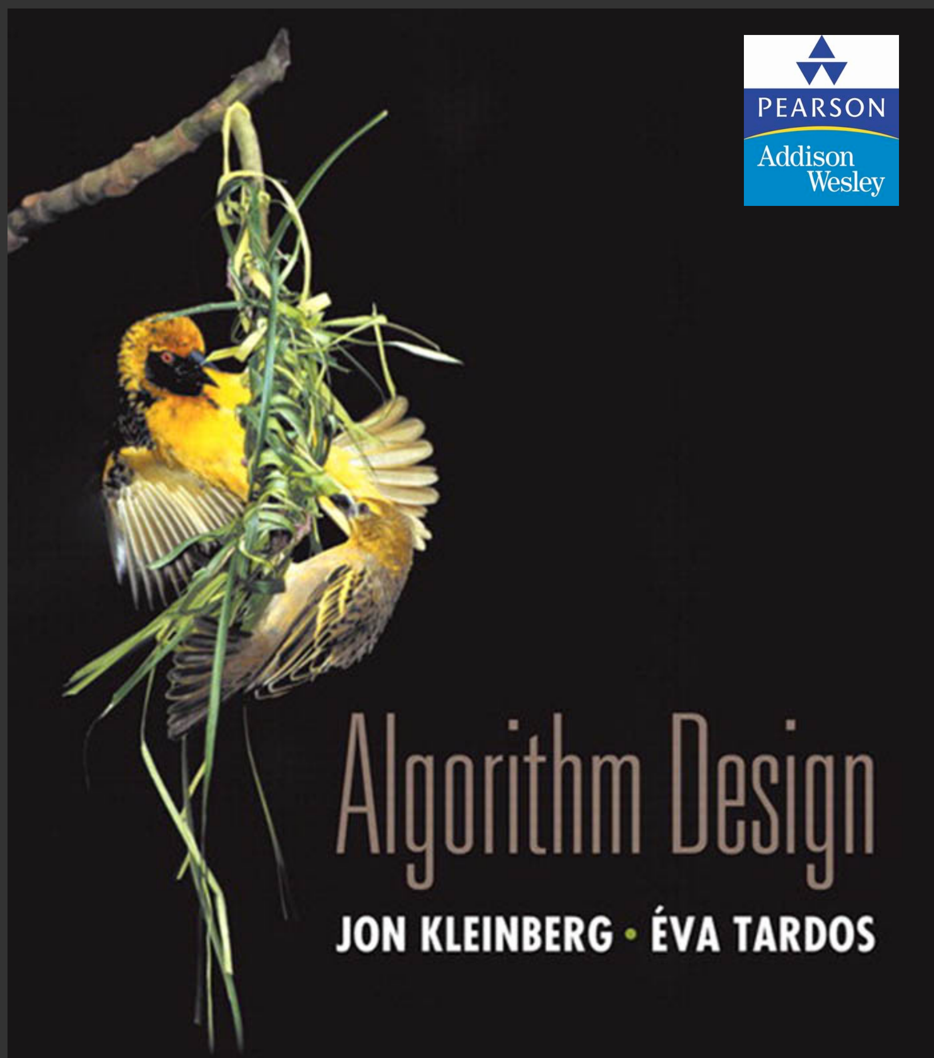


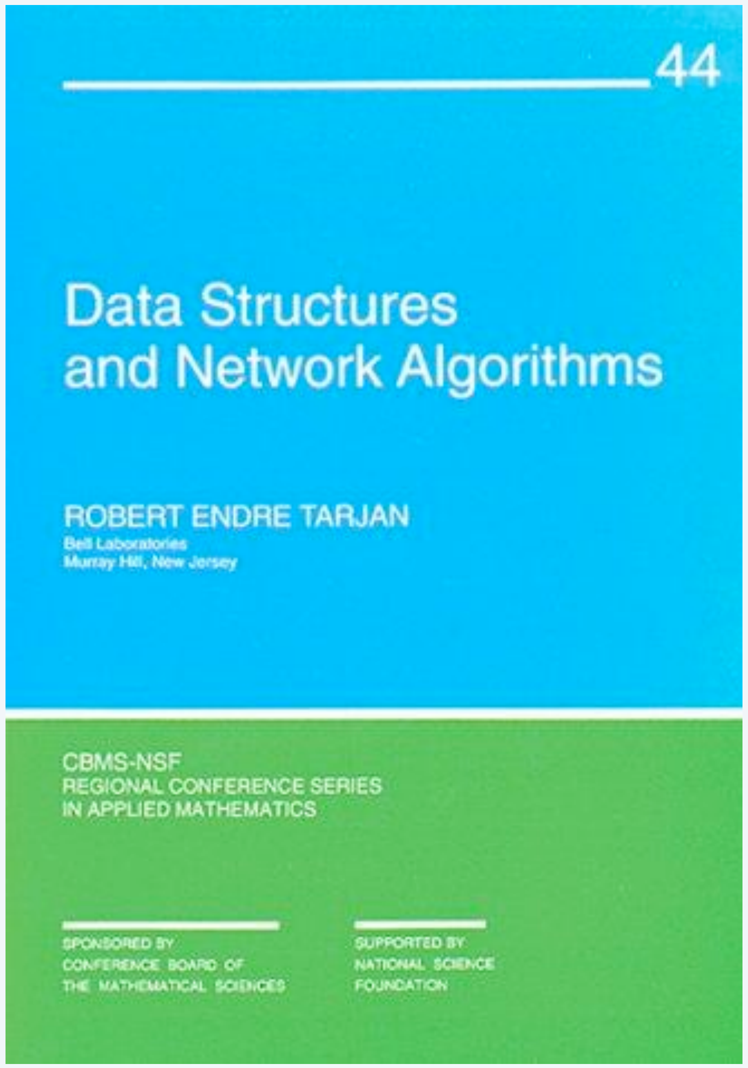
Lecture slides by Kevin Wayne

http://www.cs.princeton.edu/~wayne/kleinberg-tardos

4. Greedy Algorithms II

- *red-rule blue-rule demo*
- *Prim's algorithm demo*
- *Kruskal's algorithm demo*
- *reverse-delete algorithm demo*
- *Boruvka's algorithm demo*

Last updated on 2/26/18 4:51 PM



SECTION 6.1

4. GREEDY ALGORITHMS II

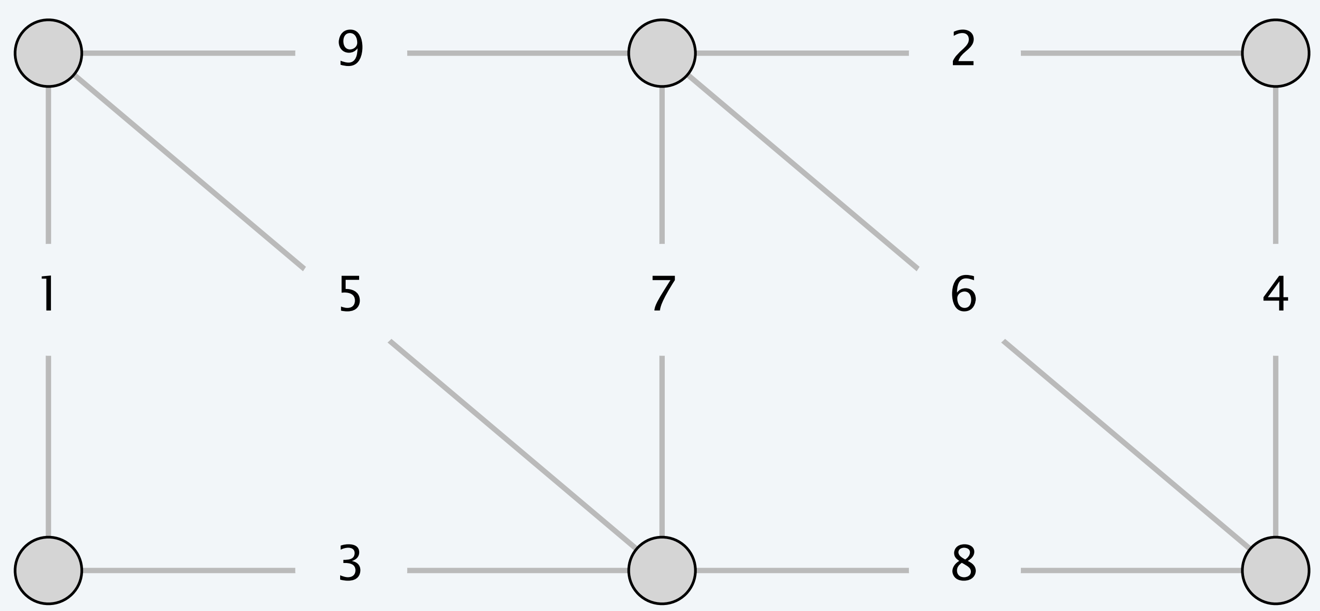
- *red-rule blue-rule demo*
- *Prim's algorithm demo*
- *Kruskal's algorithm demo*
- *reverse-delete algorithm demo*
- *Boruvka's algorithm demo*

Red-rule blue-rule demo

Red rule. Let C be a cycle with no red edges. Select an uncolored edge of C of max weight and color it red.

Blue rule. Let D be a cutset with no blue edges. Select an uncolored edge in D of min weight and color it blue.

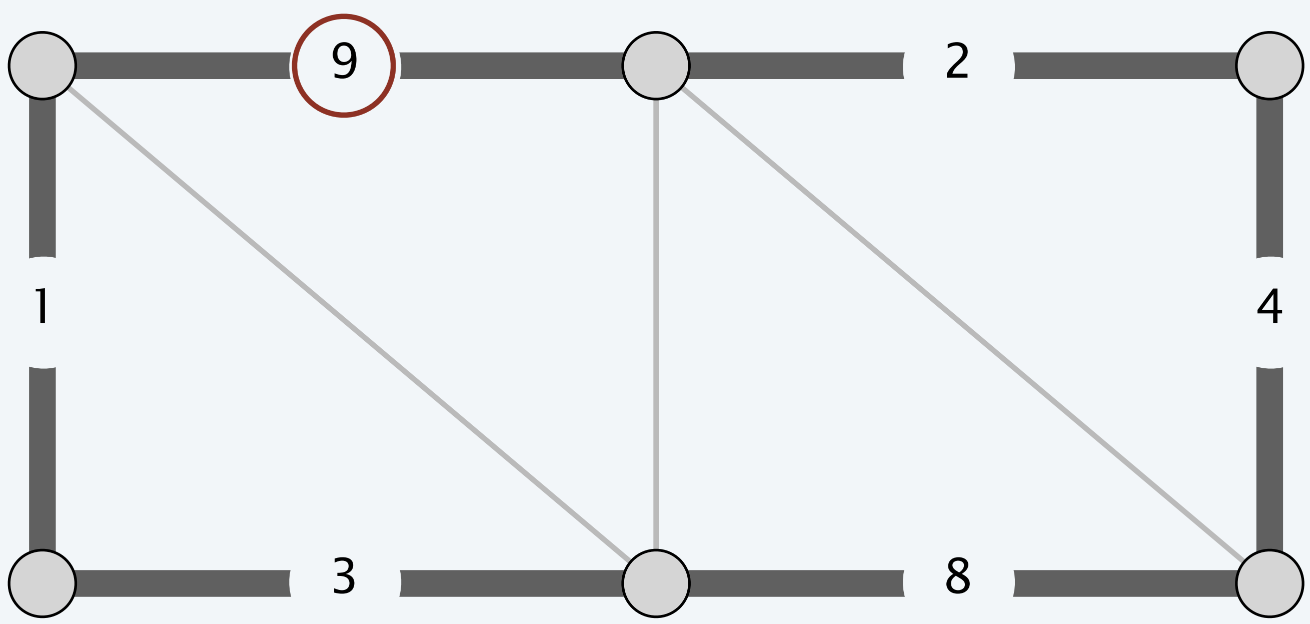
the input graph



Red-rule blue-rule demo

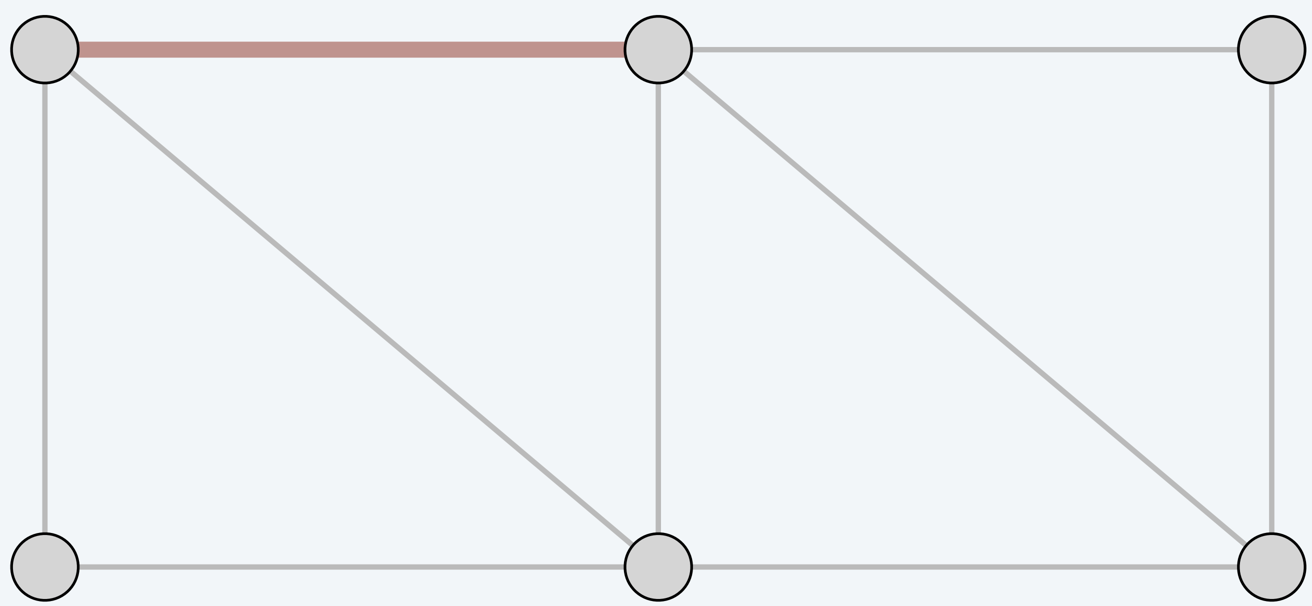
Red rule. Let C be a cycle with no red edges. Select an uncolored edge of C of max weight and color it red.

apply the red rule to the cycle



Red-rule blue-rule demo

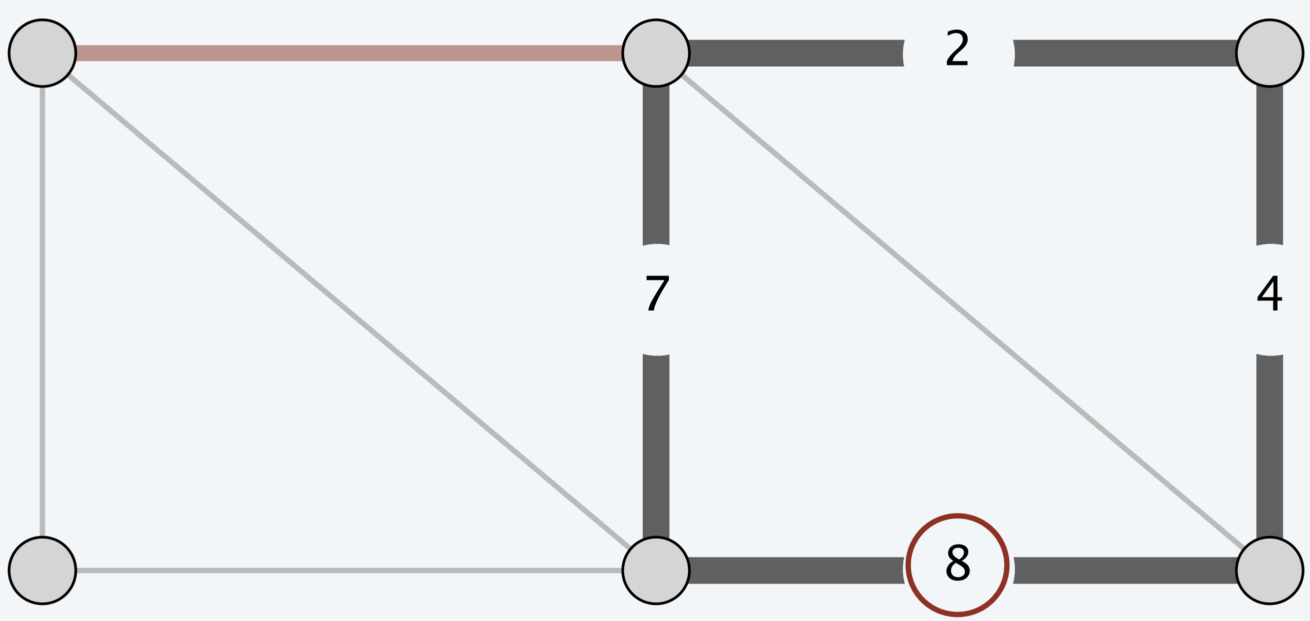
current set of red and blue edges



Red-rule blue-rule demo

Red rule. Let C be a cycle with no red edges. Select an uncolored edge of C of max weight and color it red.

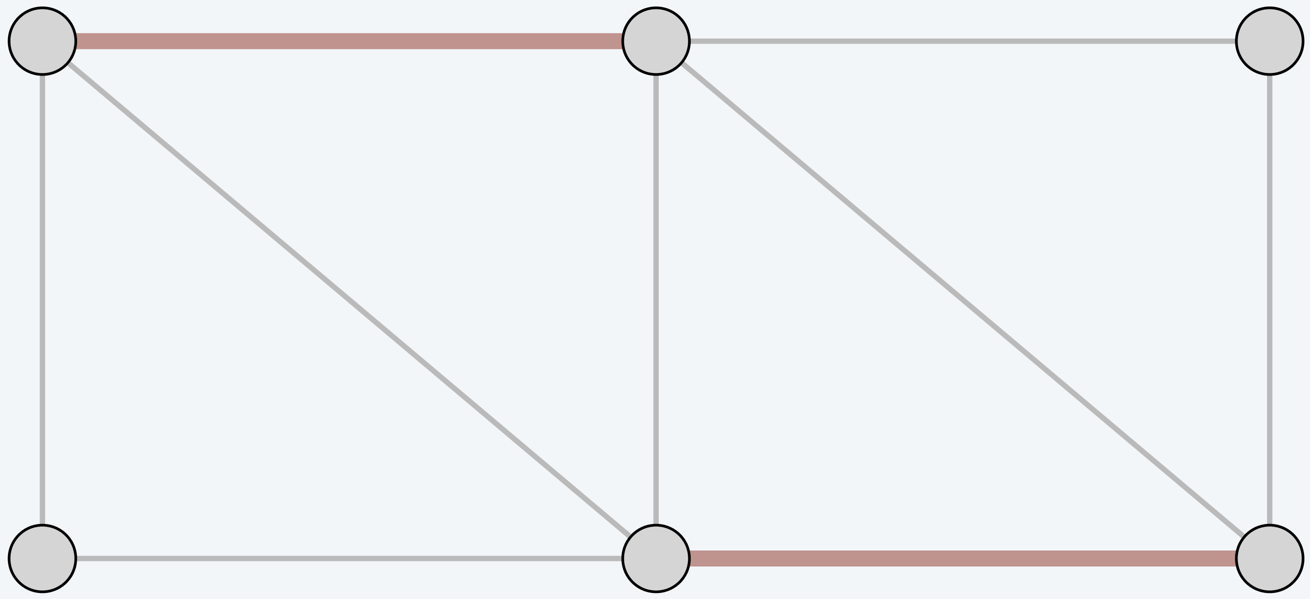
apply the red rule to the cycle



Red-rule blue-rule demo

Red rule. Let C be a cycle with no red edges. Select an uncolored edge of C of max weight and color it red.

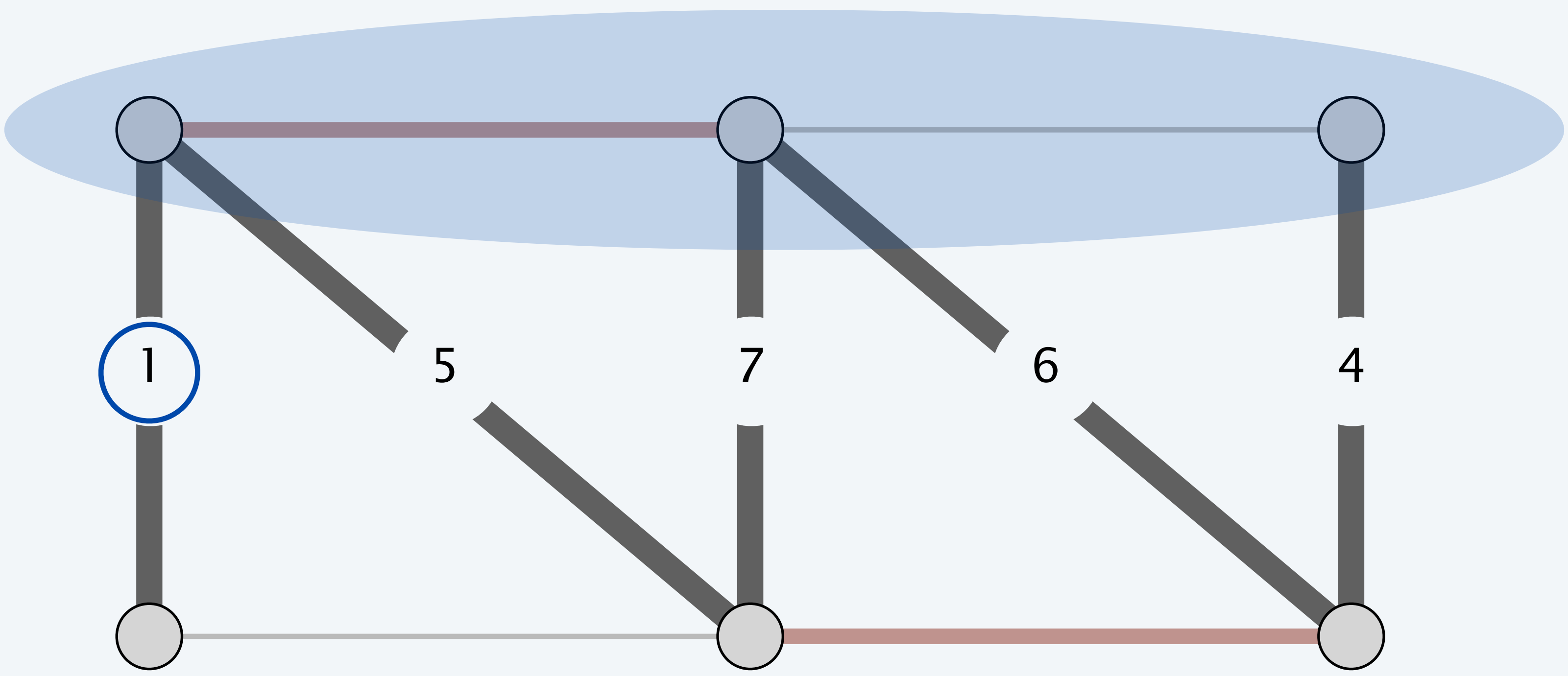
current set of red and blue edges



Red-rule blue-rule demo

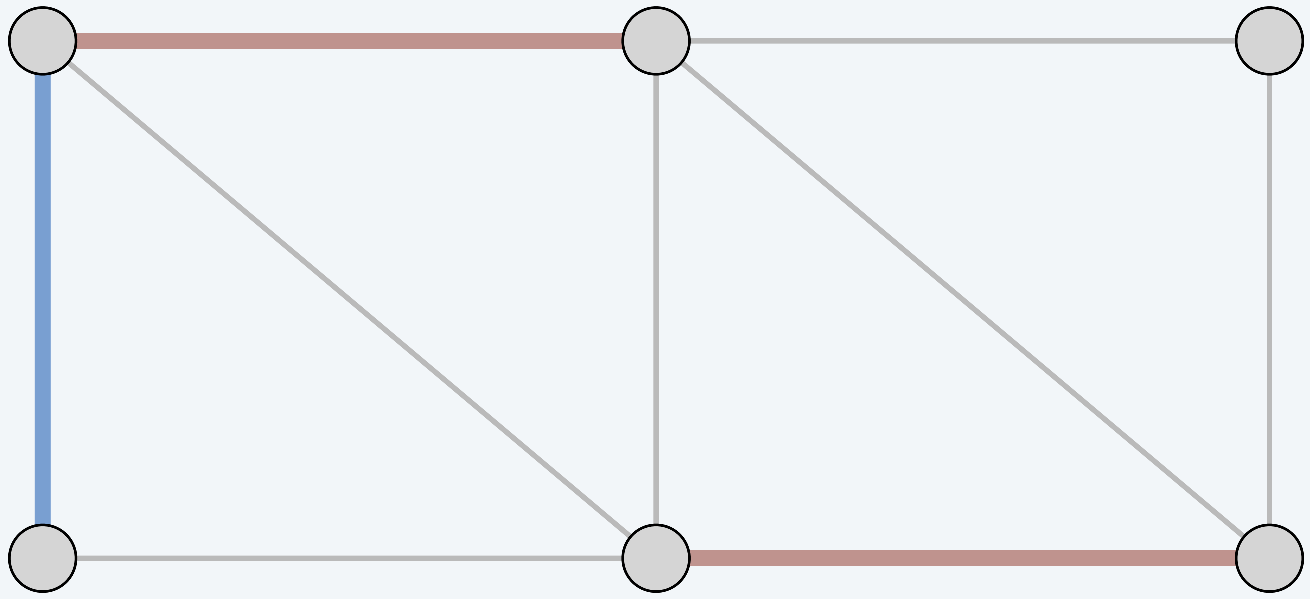
Blue rule. Let D be a cutset with no blue edges. Select an uncolored edge in D of min weight and color it blue.

apply the blue rule to the cutset



Red-rule blue-rule demo

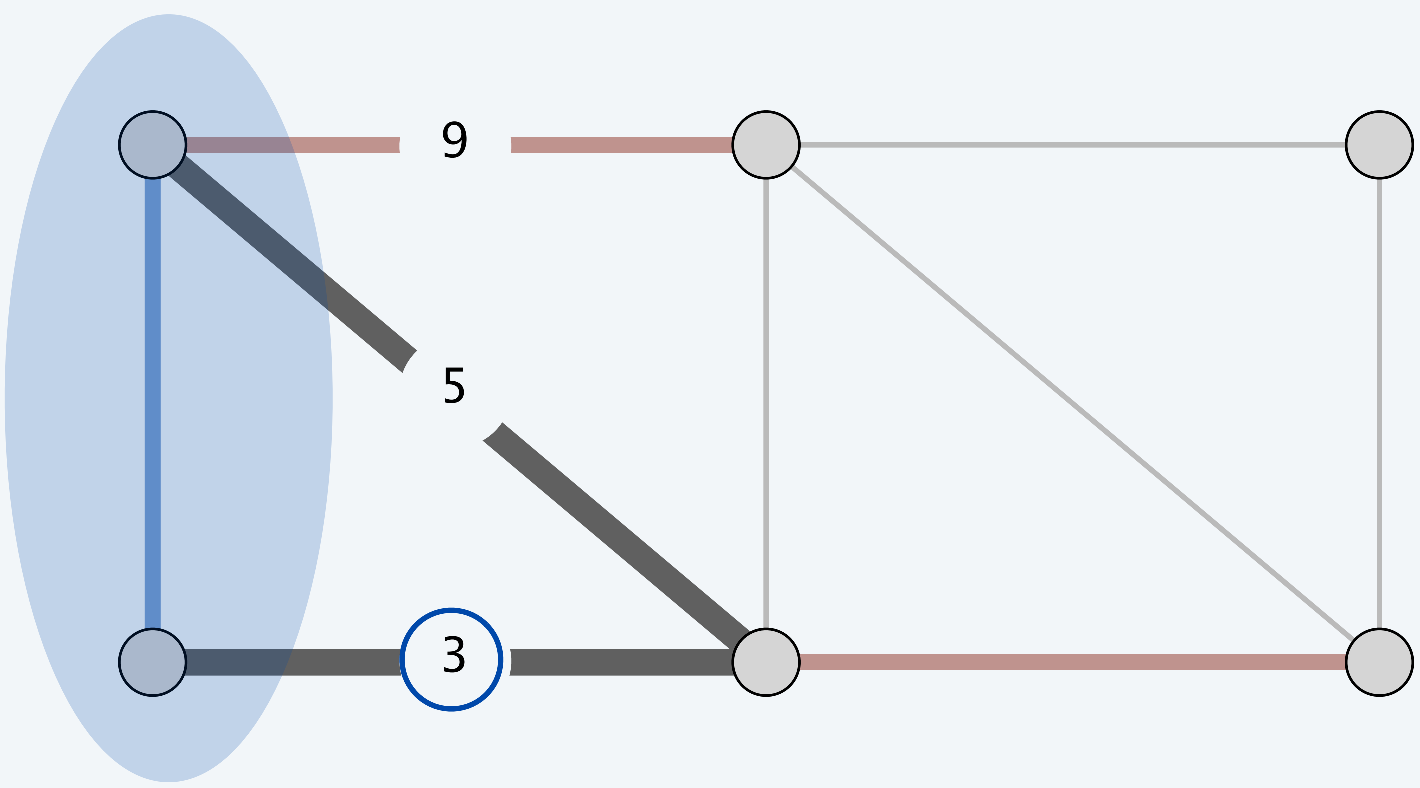
current set of red and blue edges



Red-rule blue-rule demo

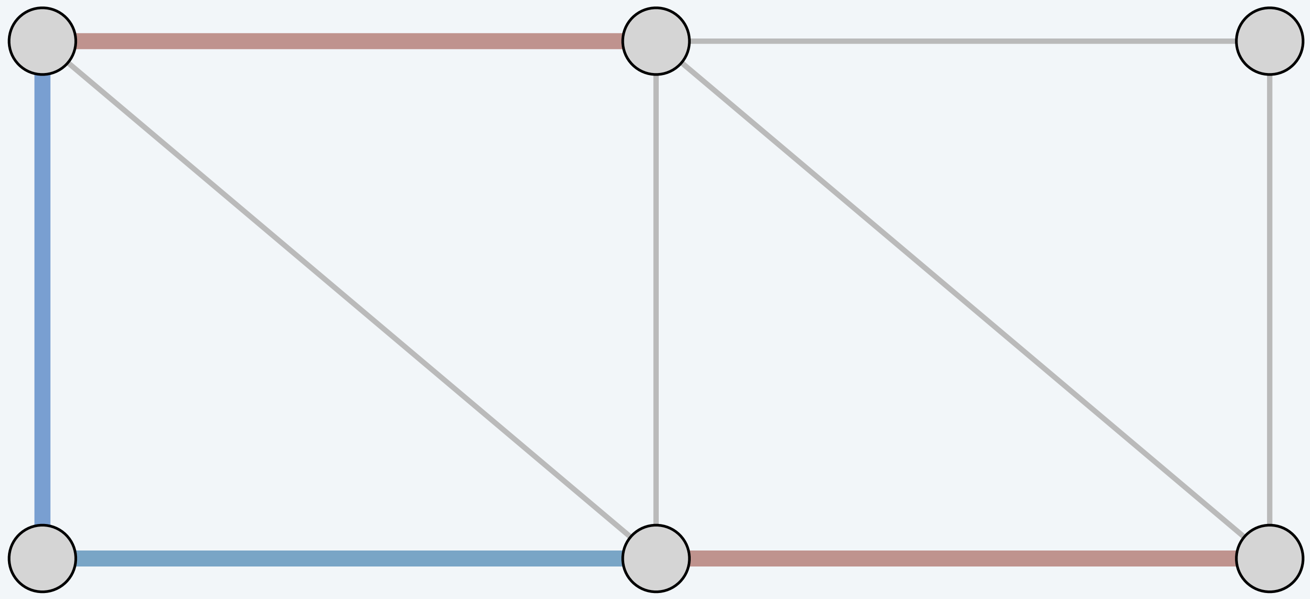
Blue rule. Let D be a cutset with no blue edges. Select an uncolored edge in D of min weight and color it blue.

apply the blue rule to the cutset



Red-rule blue-rule demo

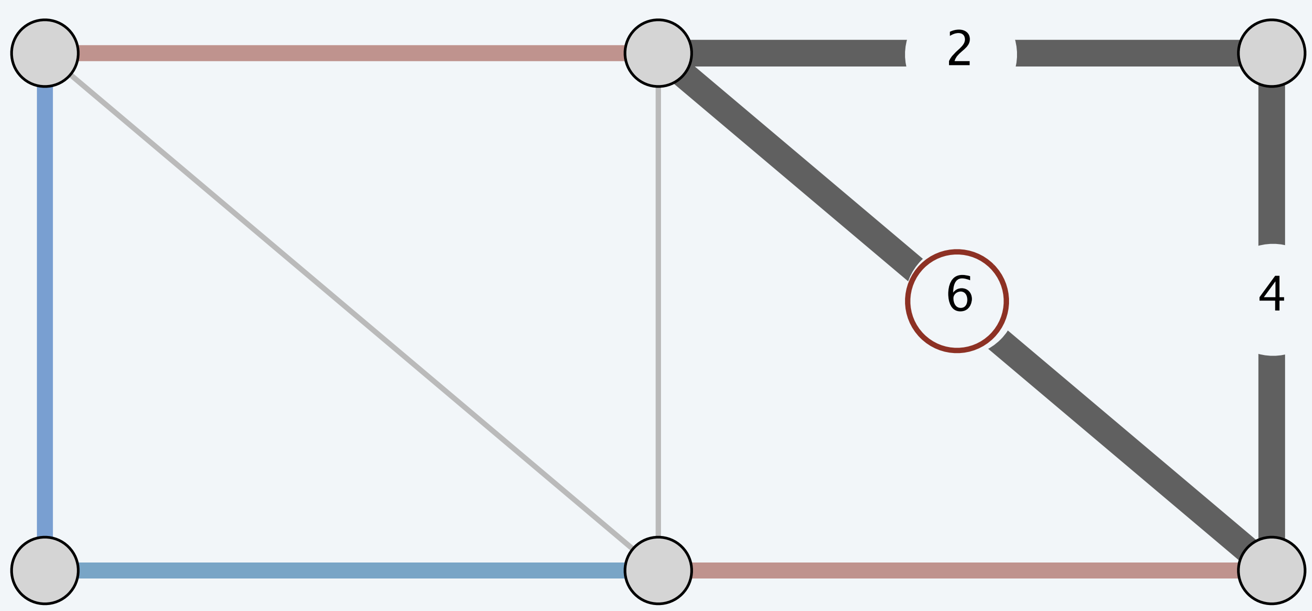
current set of red and blue edges



Red-rule blue-rule demo

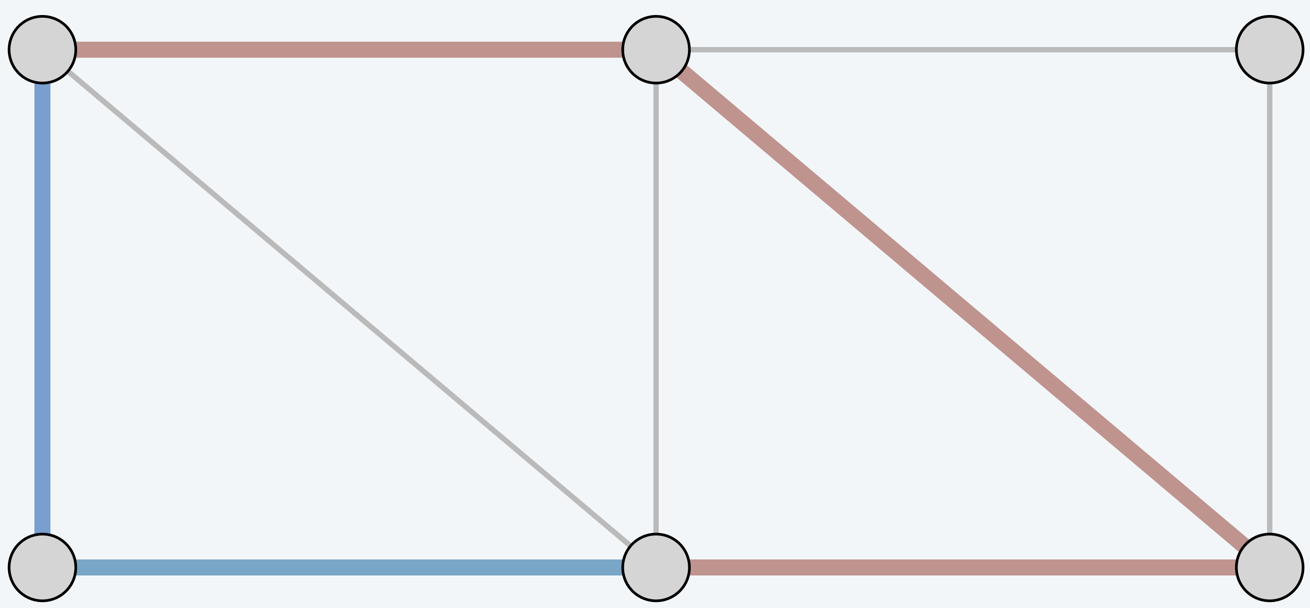
Red rule. Let C be a cycle with no red edges. Select an uncolored edge of C of max weight and color it red.

apply the red rule to the cycle



Red-rule blue-rule demo

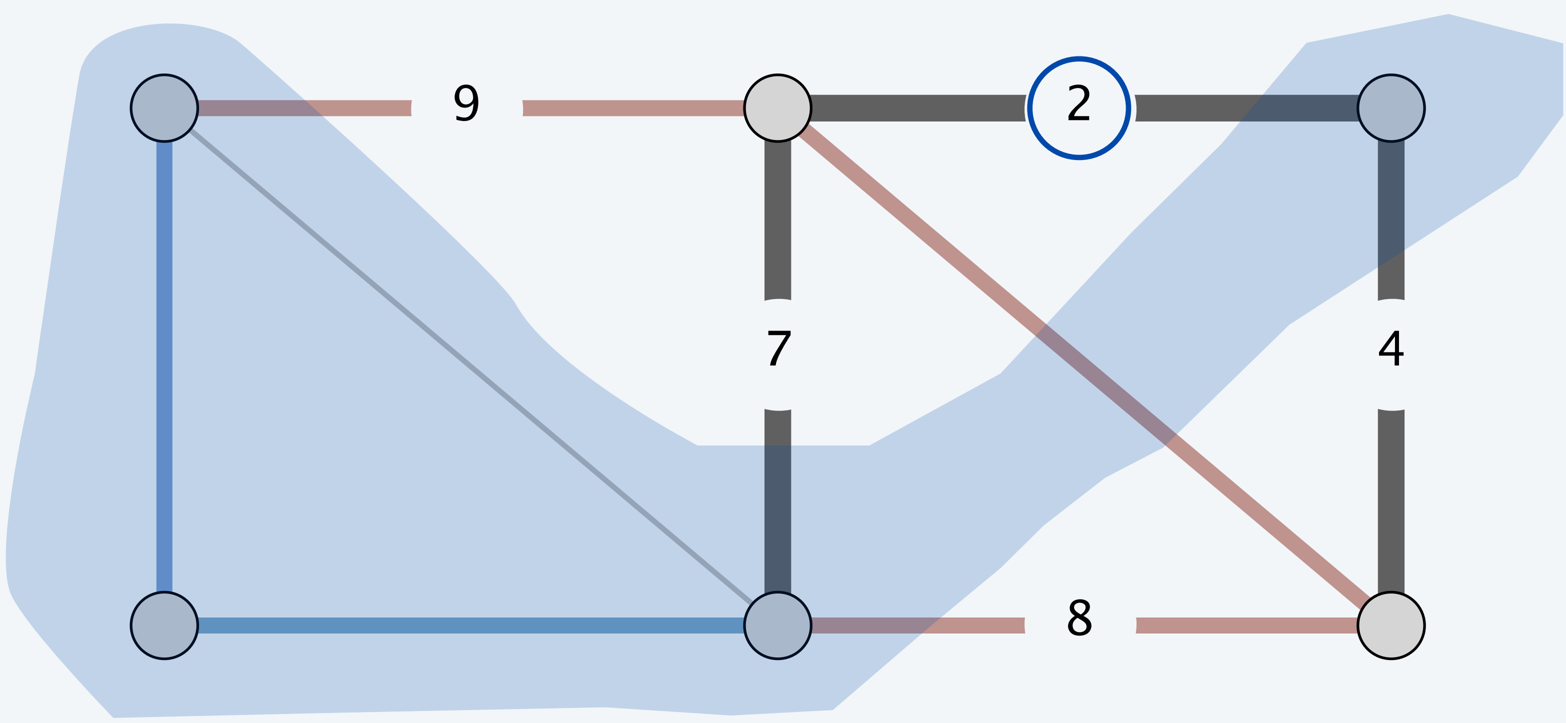
current set of red and blue edges



Red-rule blue-rule demo

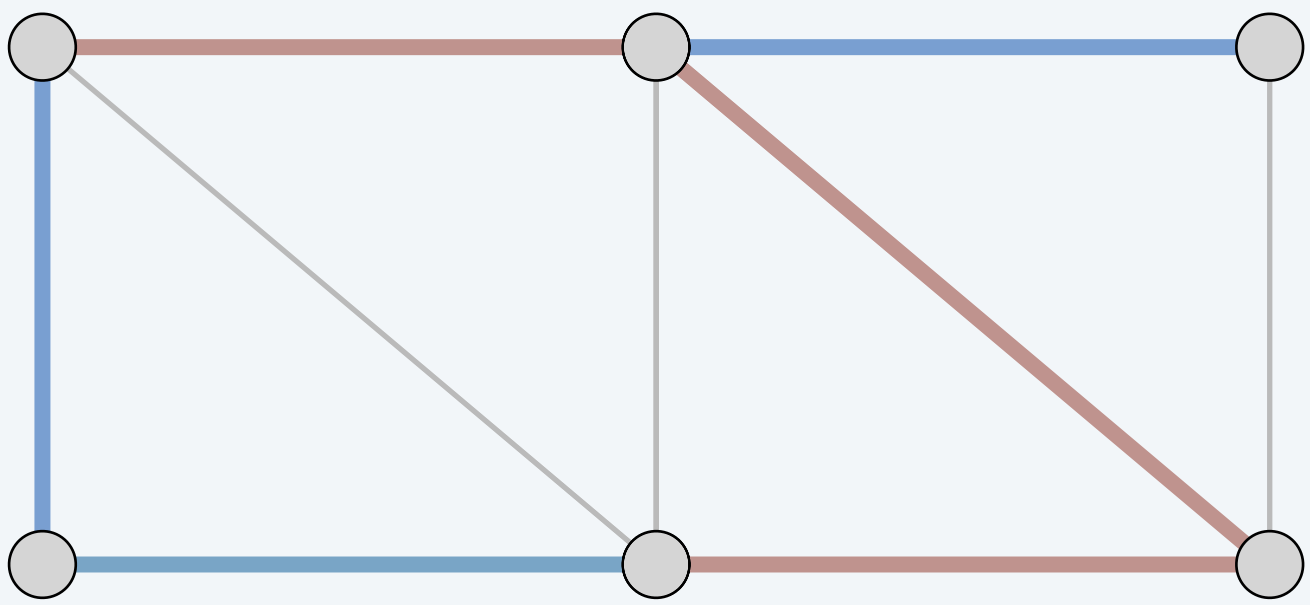
Blue rule. Let D be a cutset with no blue edges. Select an uncolored edge in D of min weight and color it blue.

apply the blue rule to the cutset



Red-rule blue-rule demo

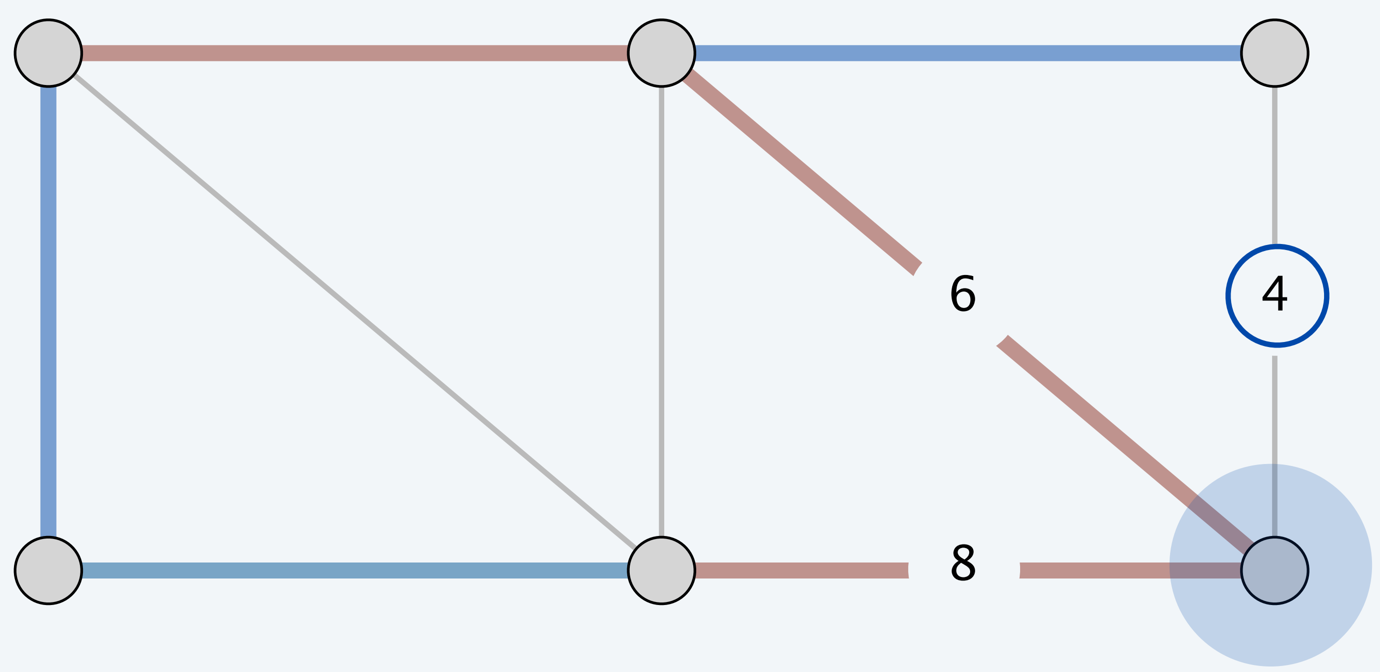
current set of red and blue edges



Red-rule blue-rule demo

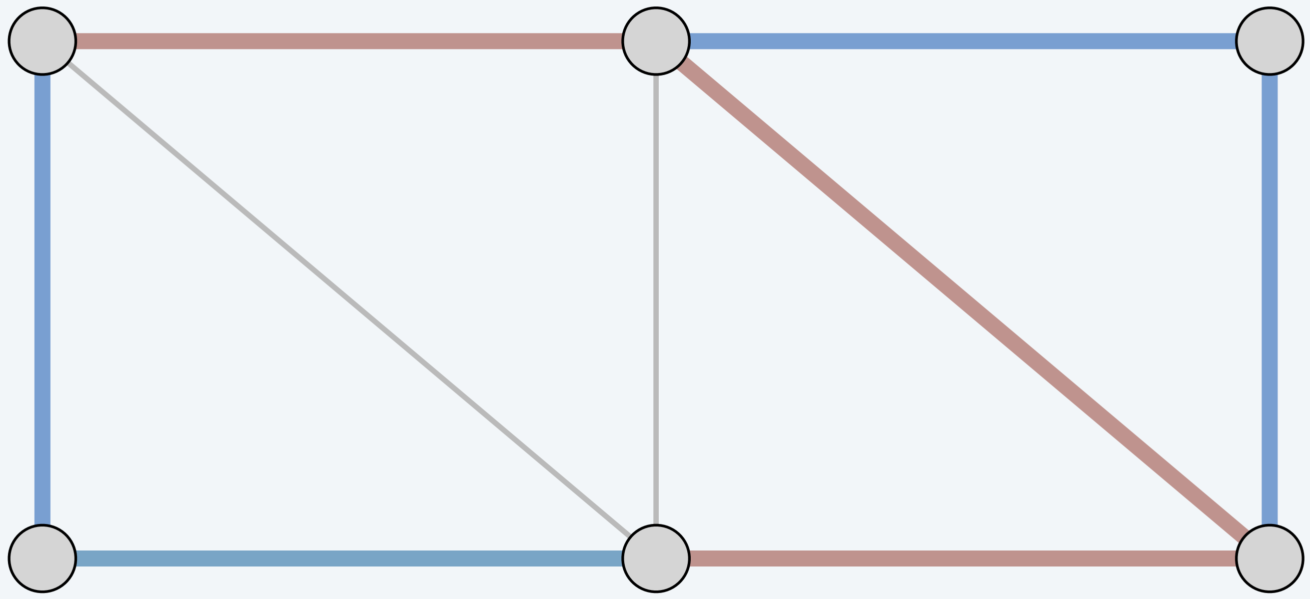
Blue rule. Let D be a cutset with no blue edges. Select an uncolored edge in D of min weight and color it blue.

apply the blue rule to the cutset



Red-rule blue-rule demo

current set of red and blue edges



Red-rule blue-rule demo

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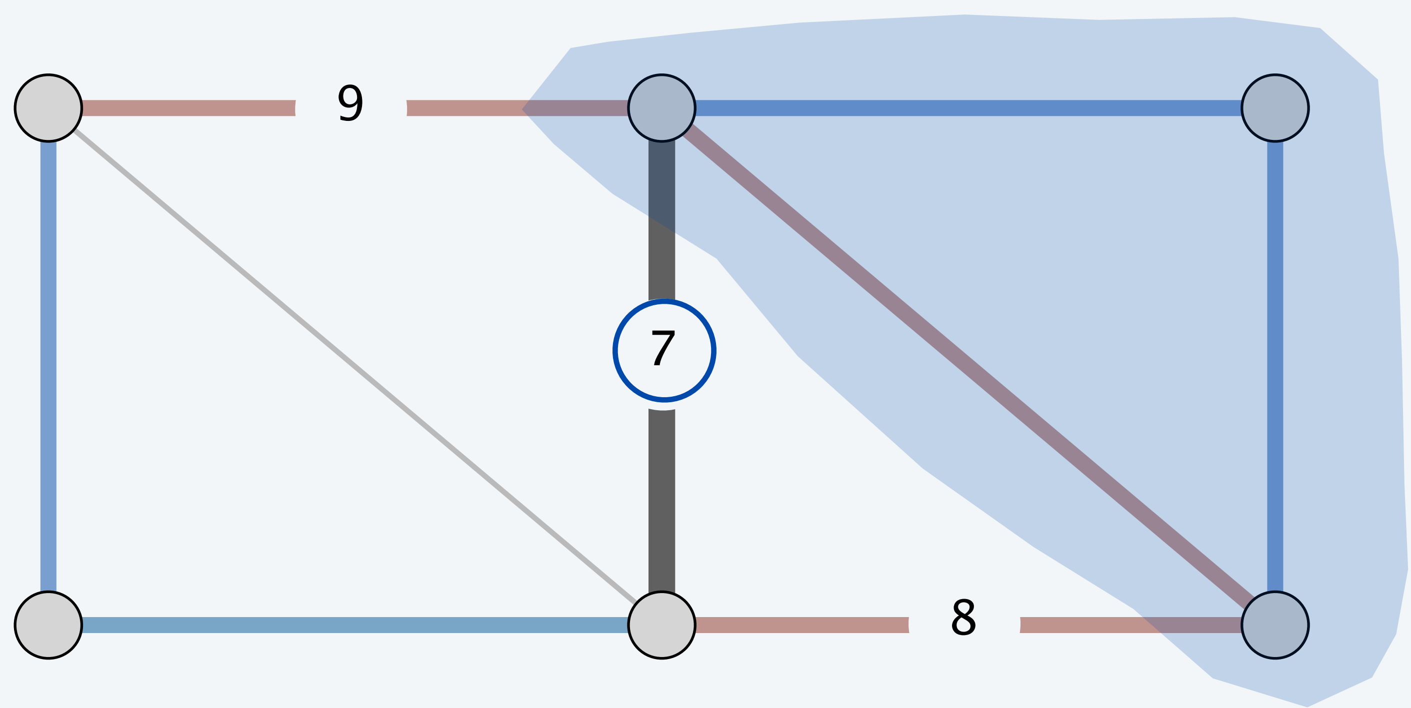
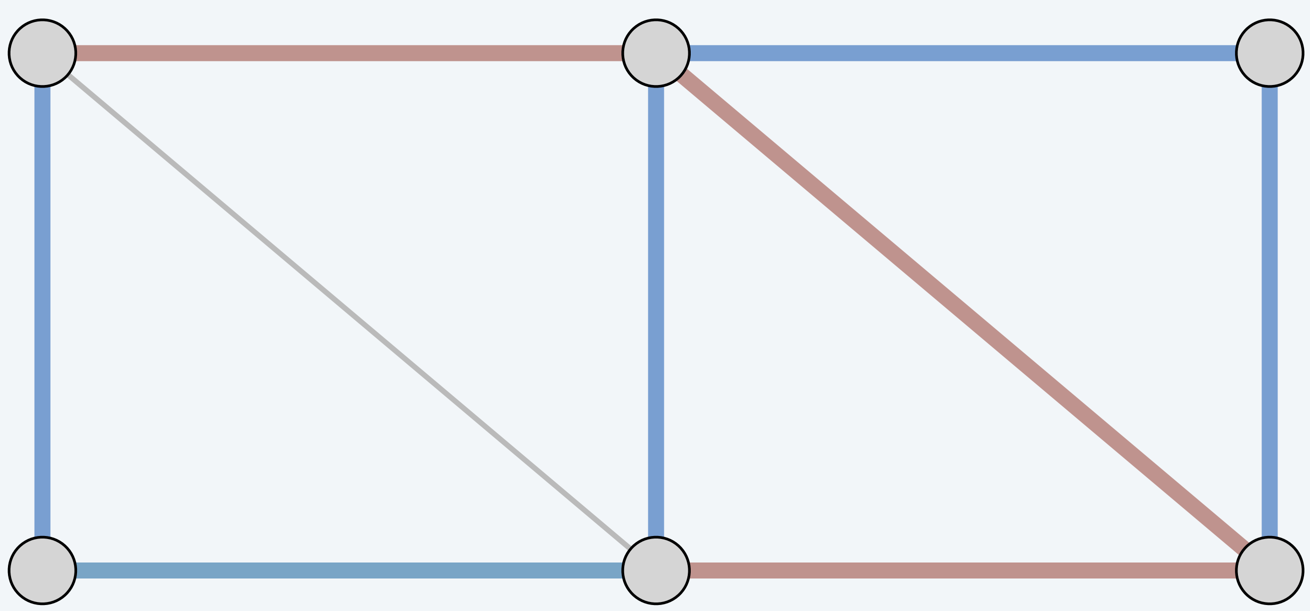
apply the blue rule to the cutset



Red-rule blue-rule demo

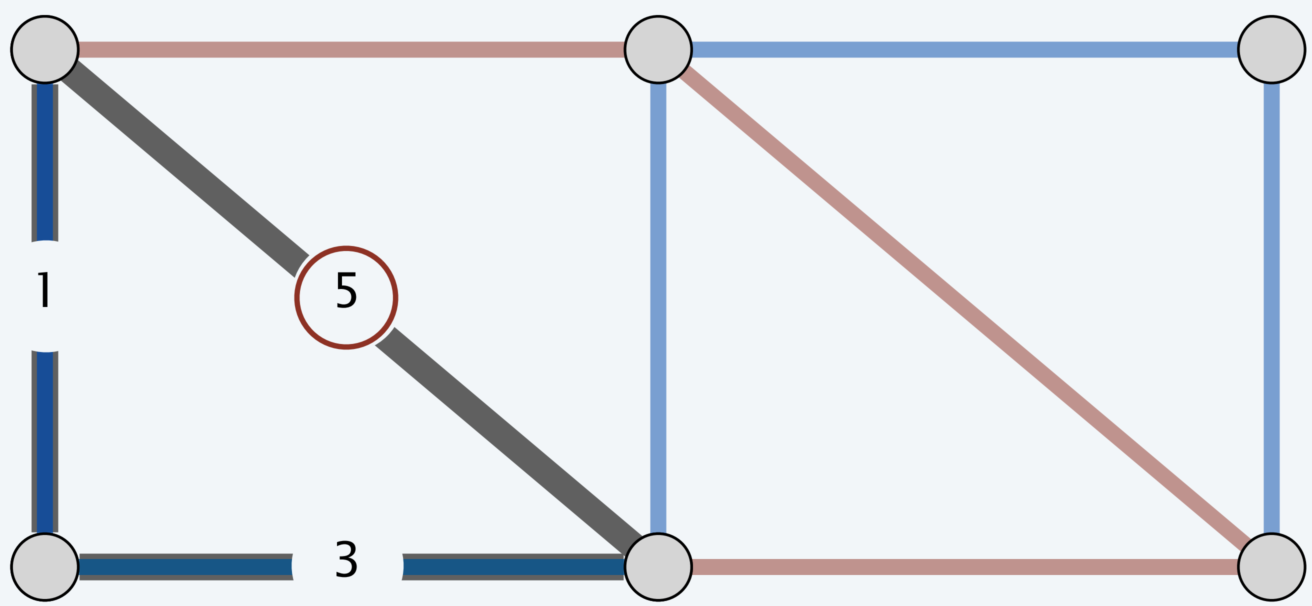
current set of red and blue edges



Red-rule blue-rule demo

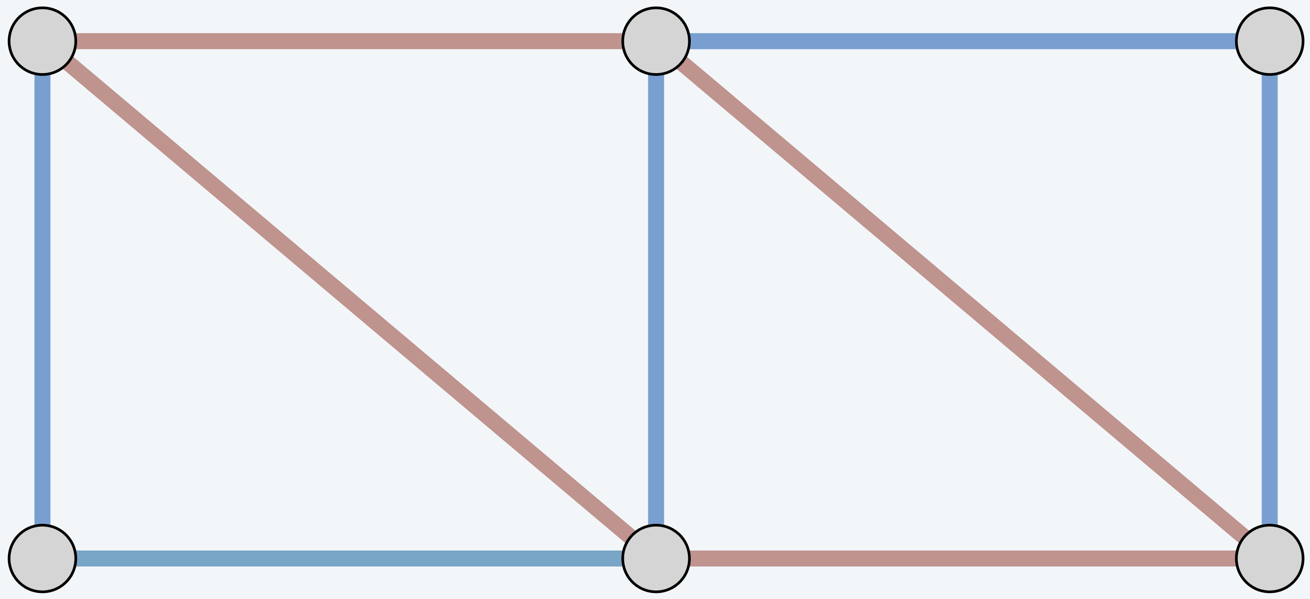
Blue rule. Let D be a cutset with no blue edges. Select an uncolored edge in D of min weight and color it blue.

apply the red rule to the cycle



Red-rule blue-rule demo

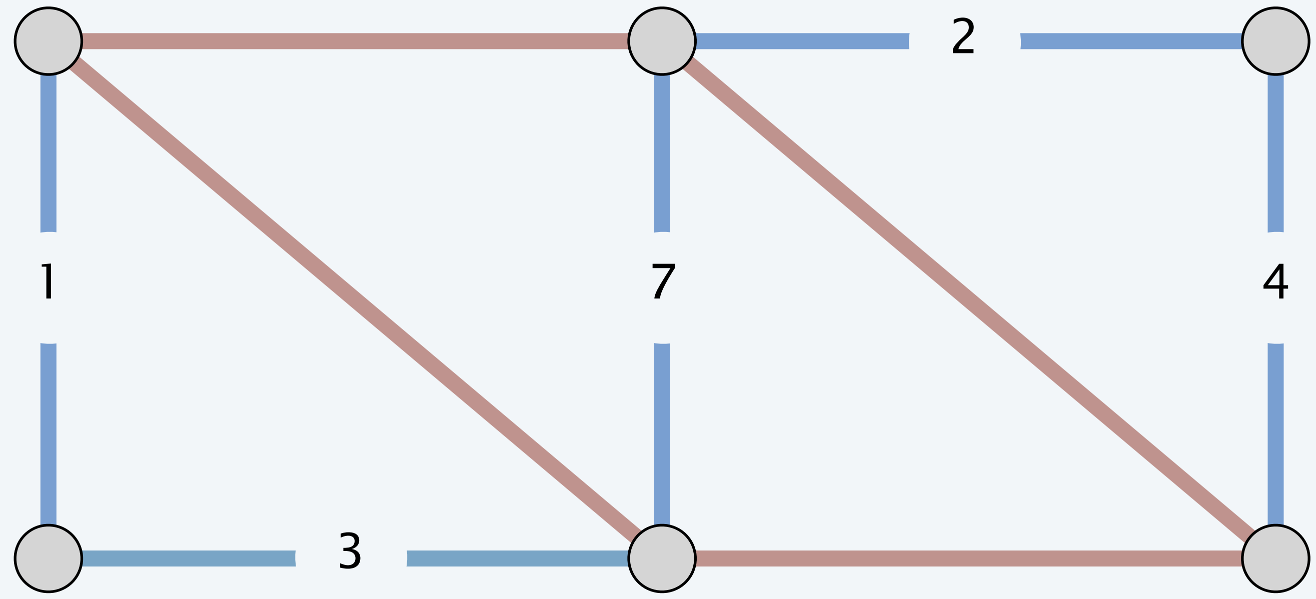
current set of red and blue edges

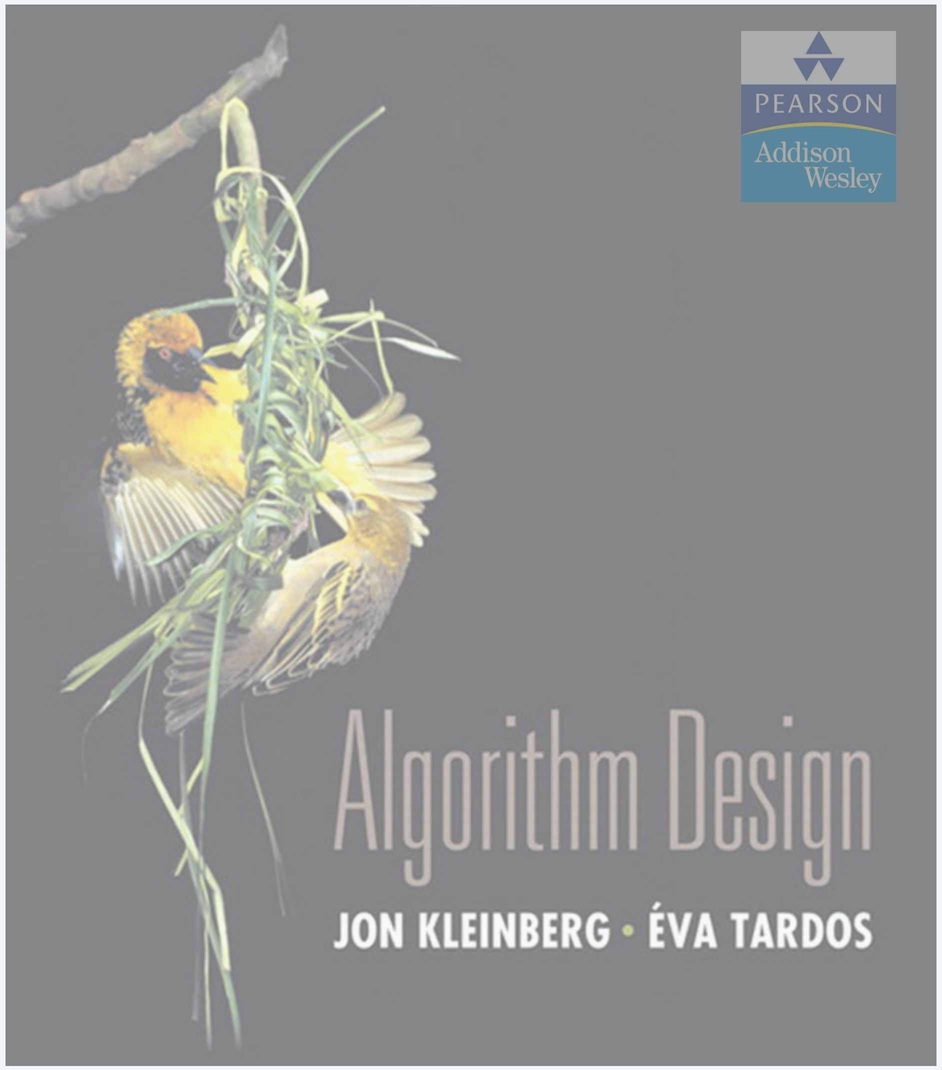


Red-rule blue-rule demo

Greedy algorithm. Upon termination, the blue edges form a MST.

a minimum spanning tree





SECTION 4.5

4. GREEDY ALGORITHMS II

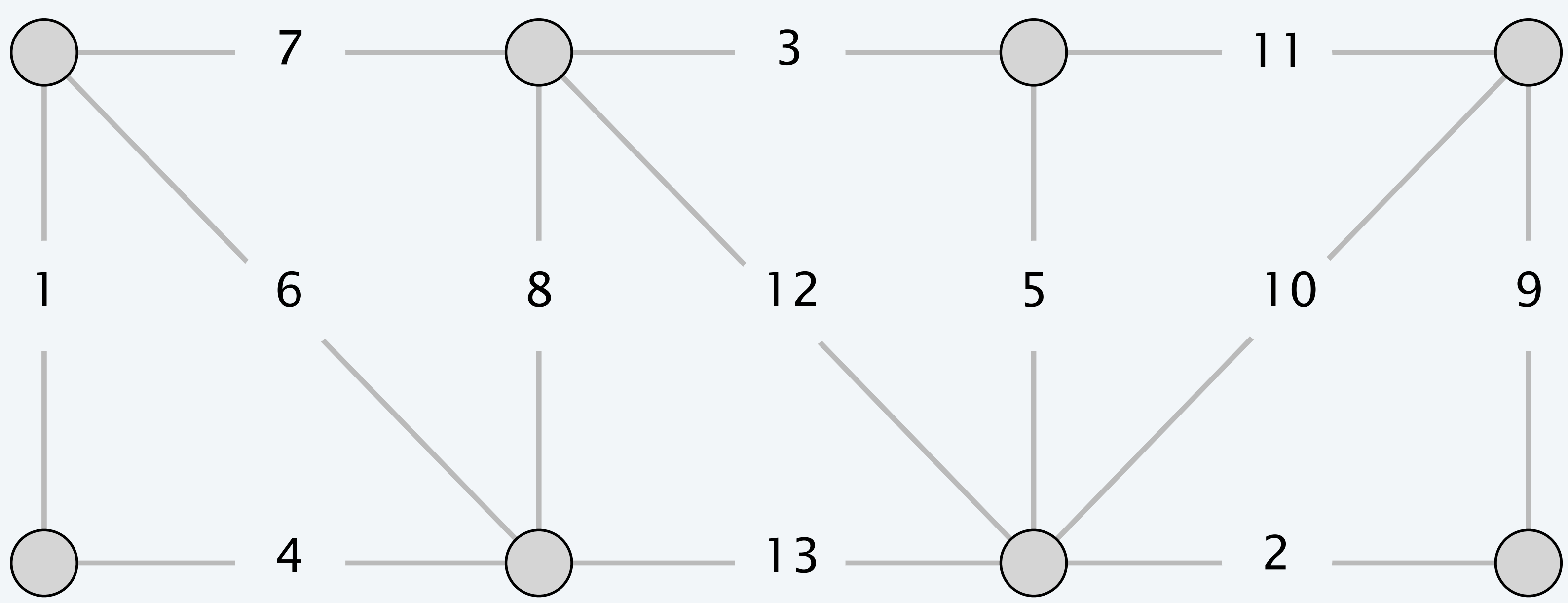
- *red-rule blue-rule demo*
- *Prim's algorithm demo*
- *Kruskal's algorithm demo*
- *reverse-delete algorithm demo*
- *Boruvka's algorithm demo*

Prim's algorithm demo

Initialize S = any node, $T = \varnothing$.

Repeat $n - 1$ times:

- Add to T a min-weight edge with one endpoint in S.
- Add new node to S.



Prim's algorithm demo

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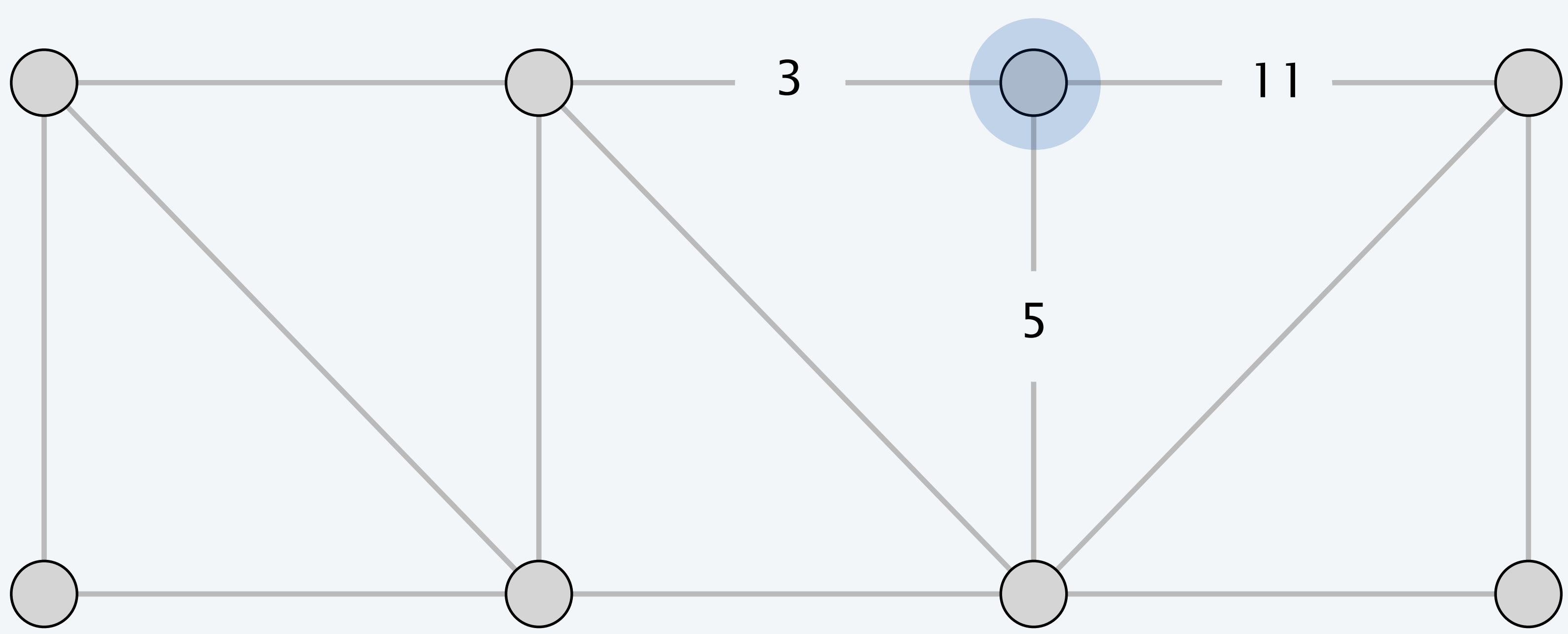

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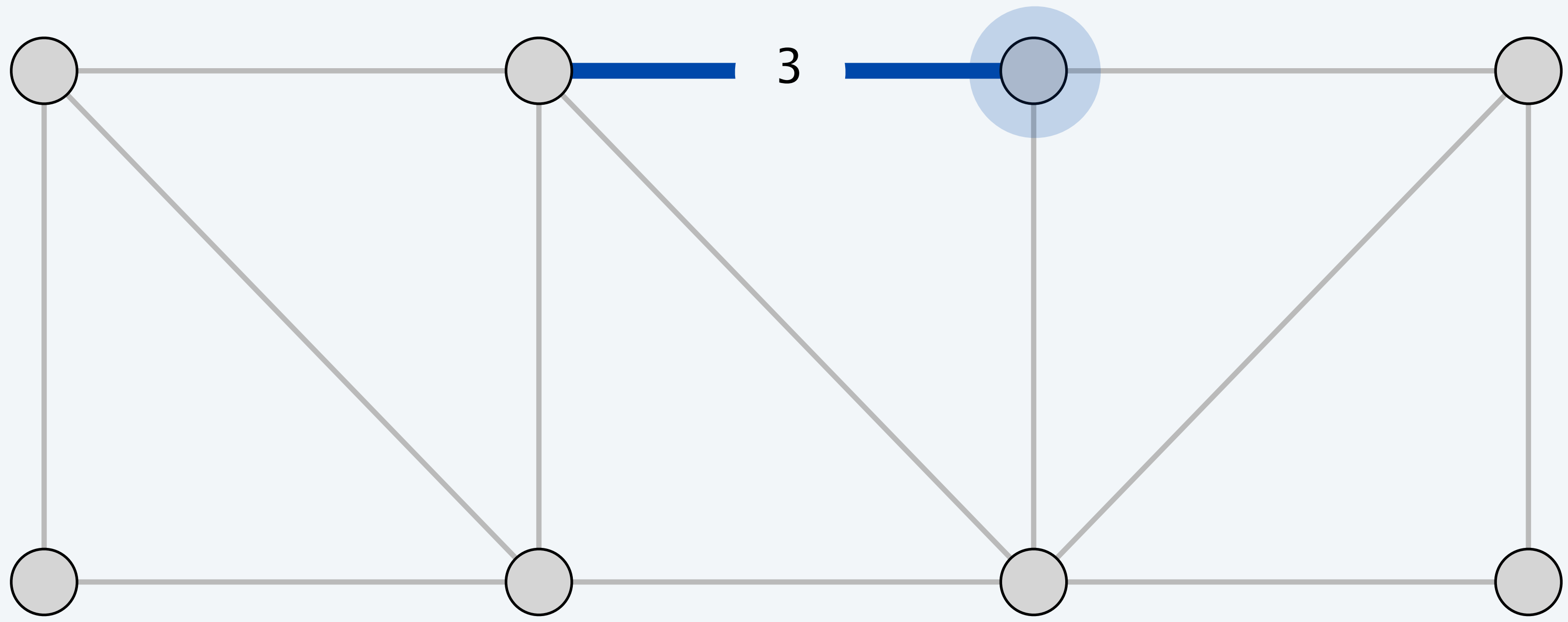

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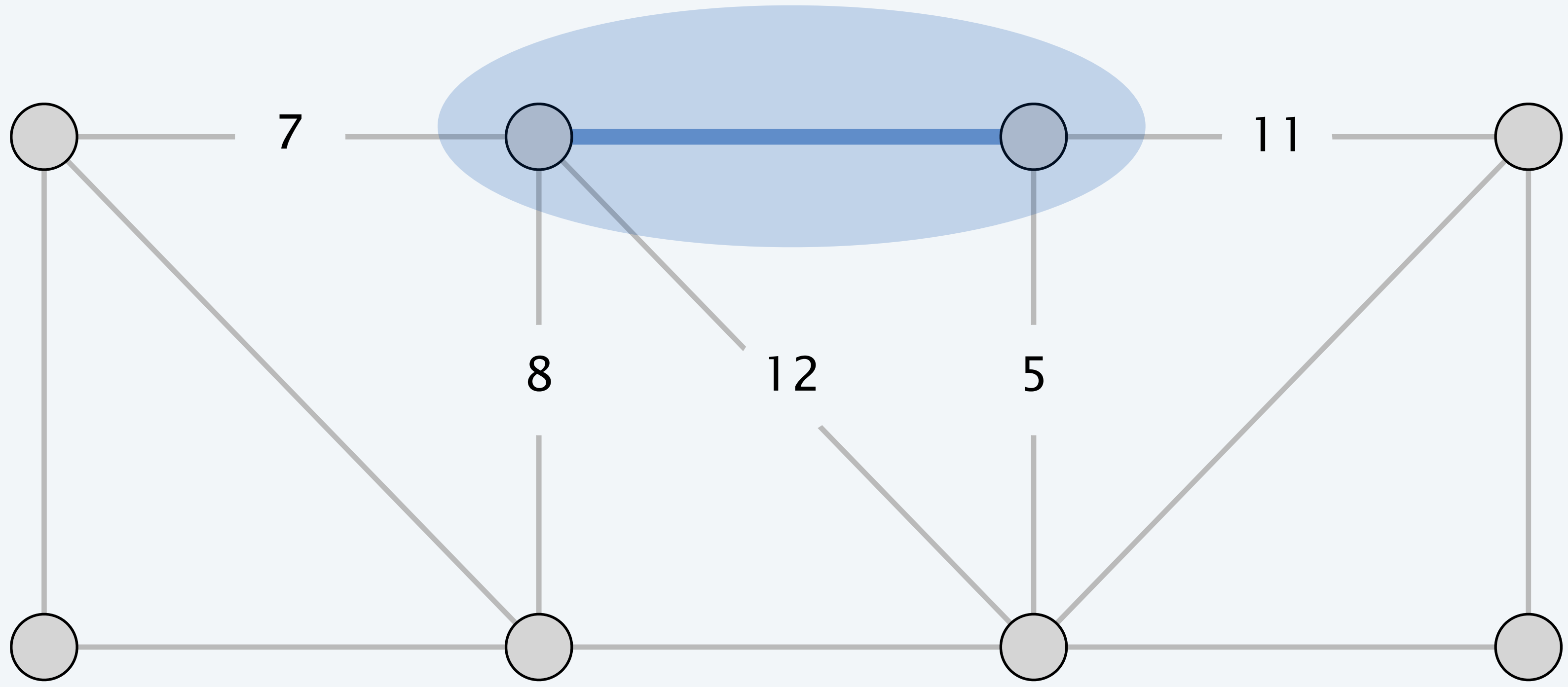

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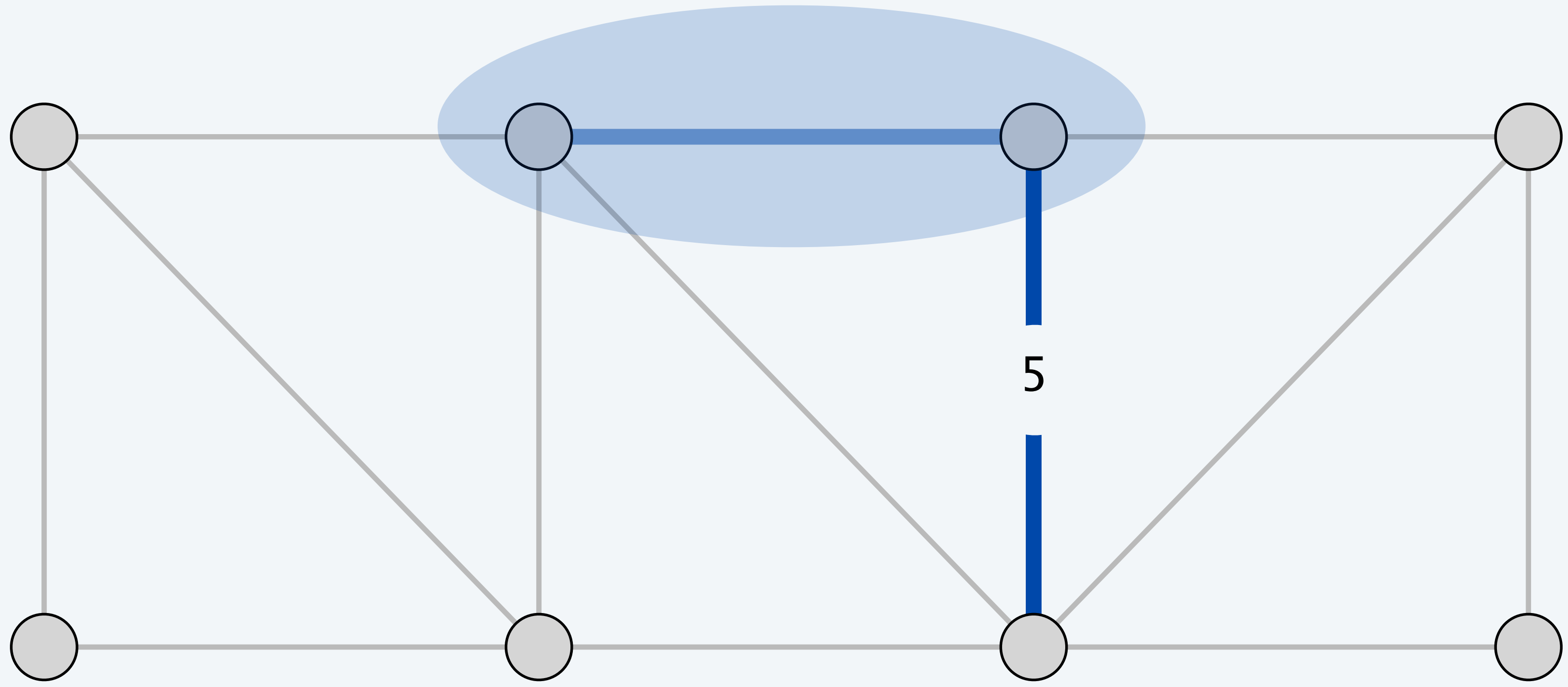

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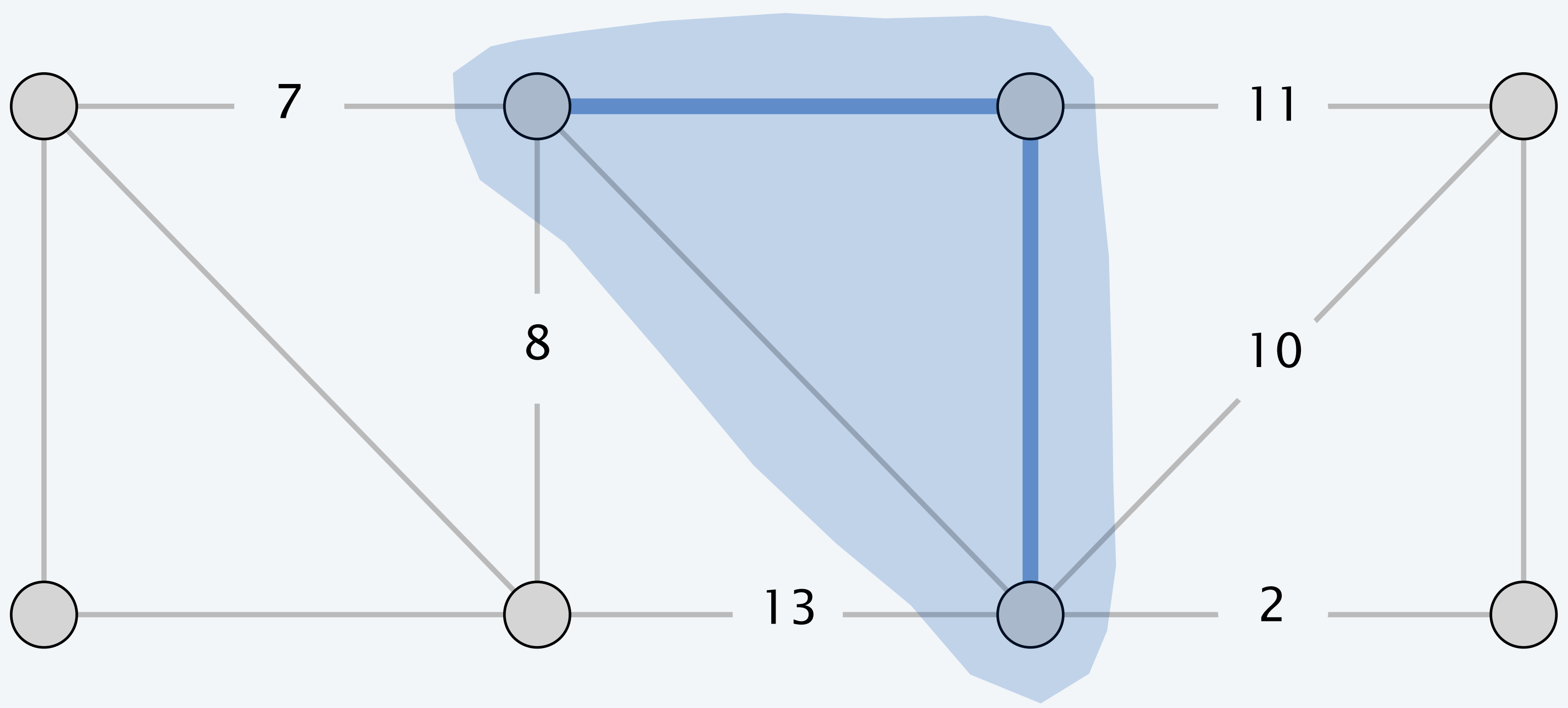

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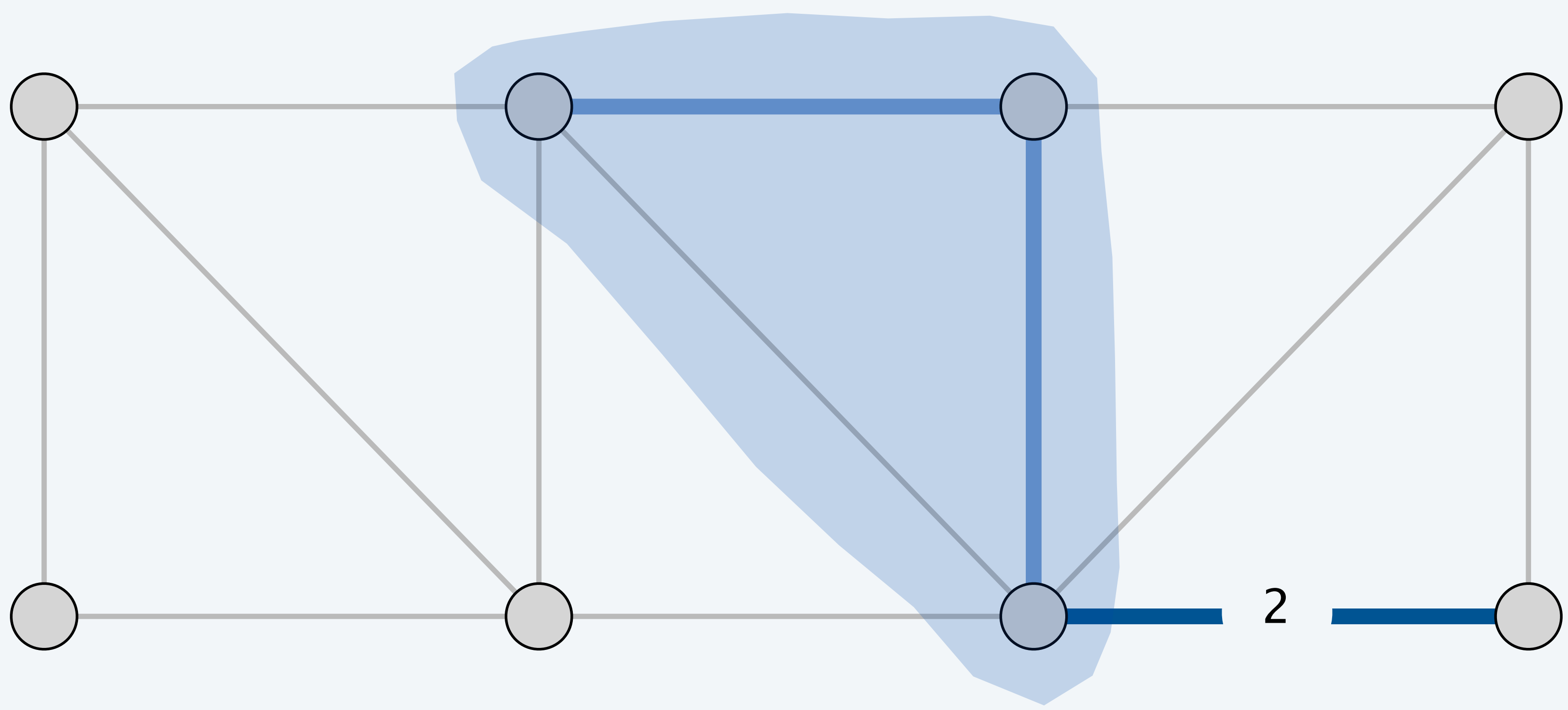

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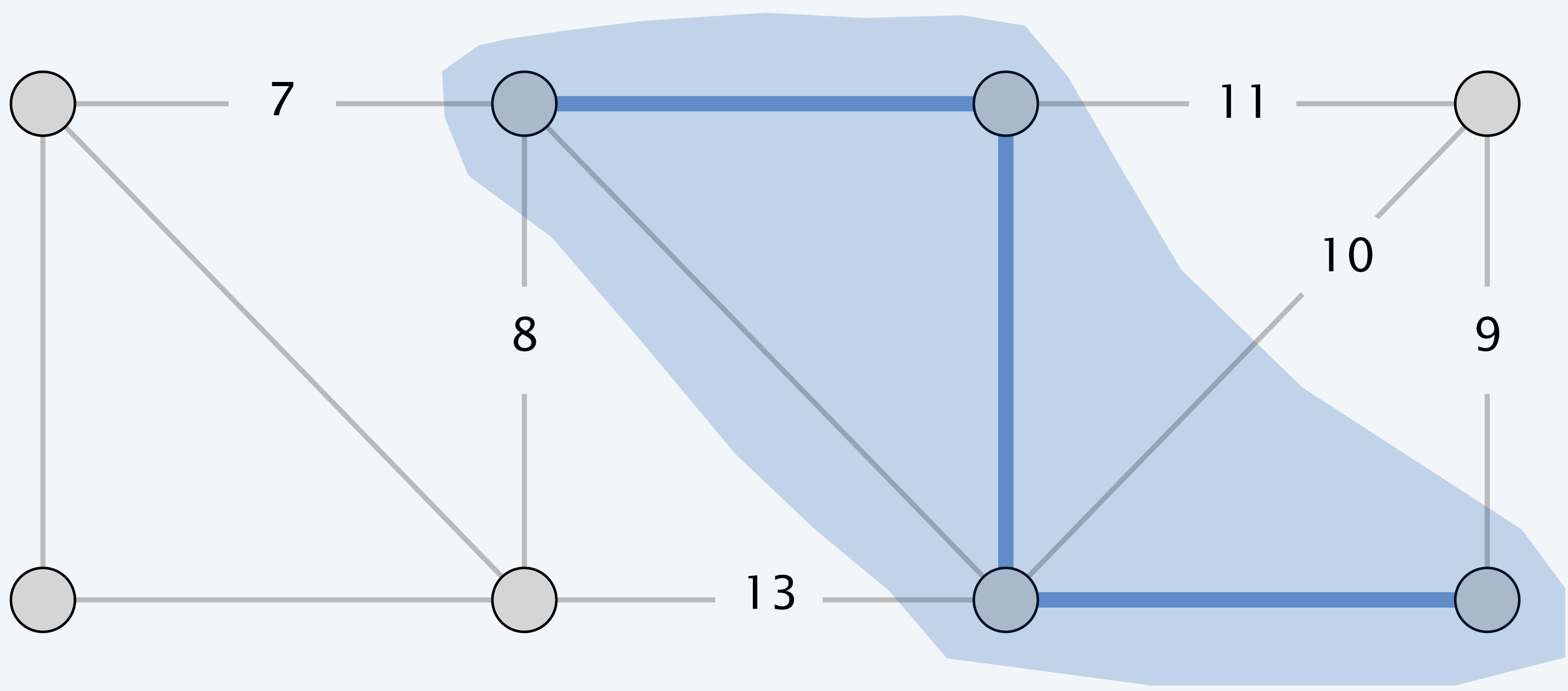

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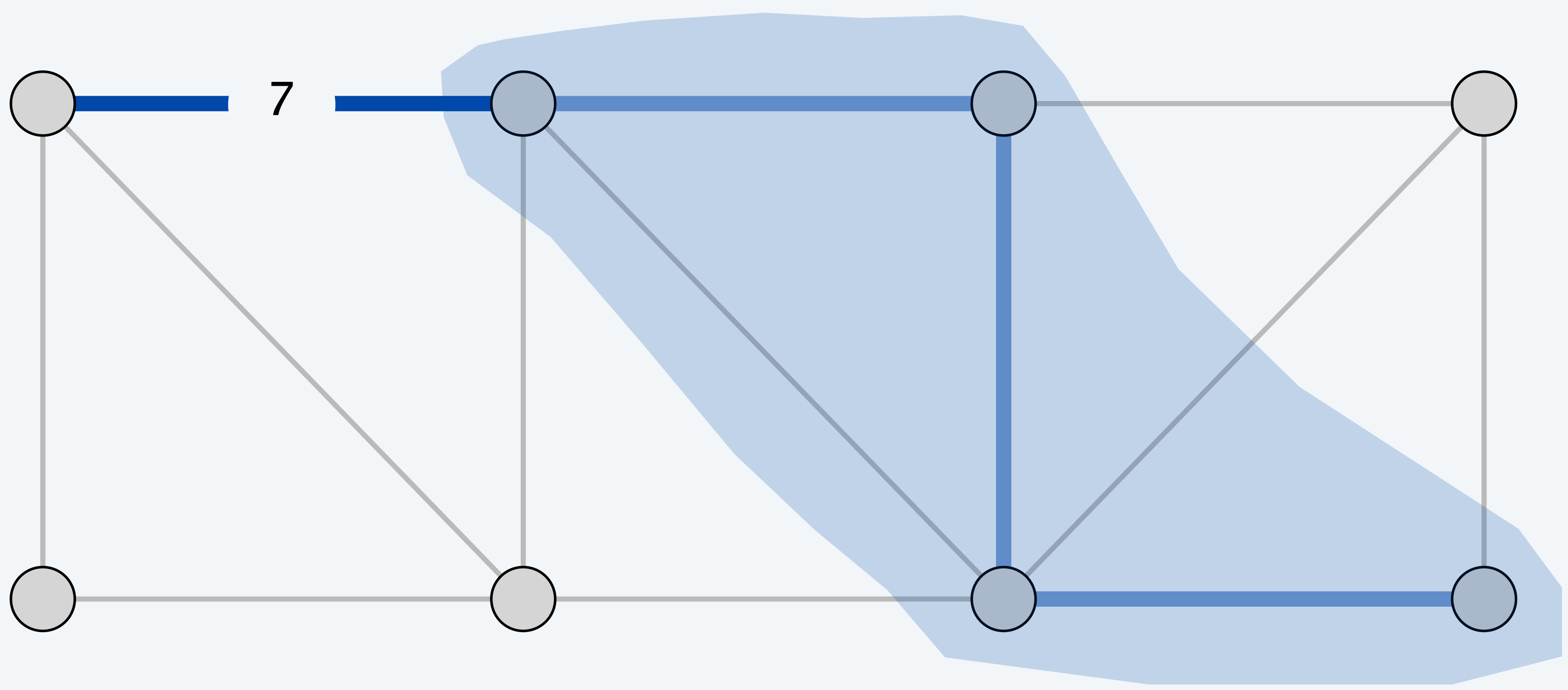

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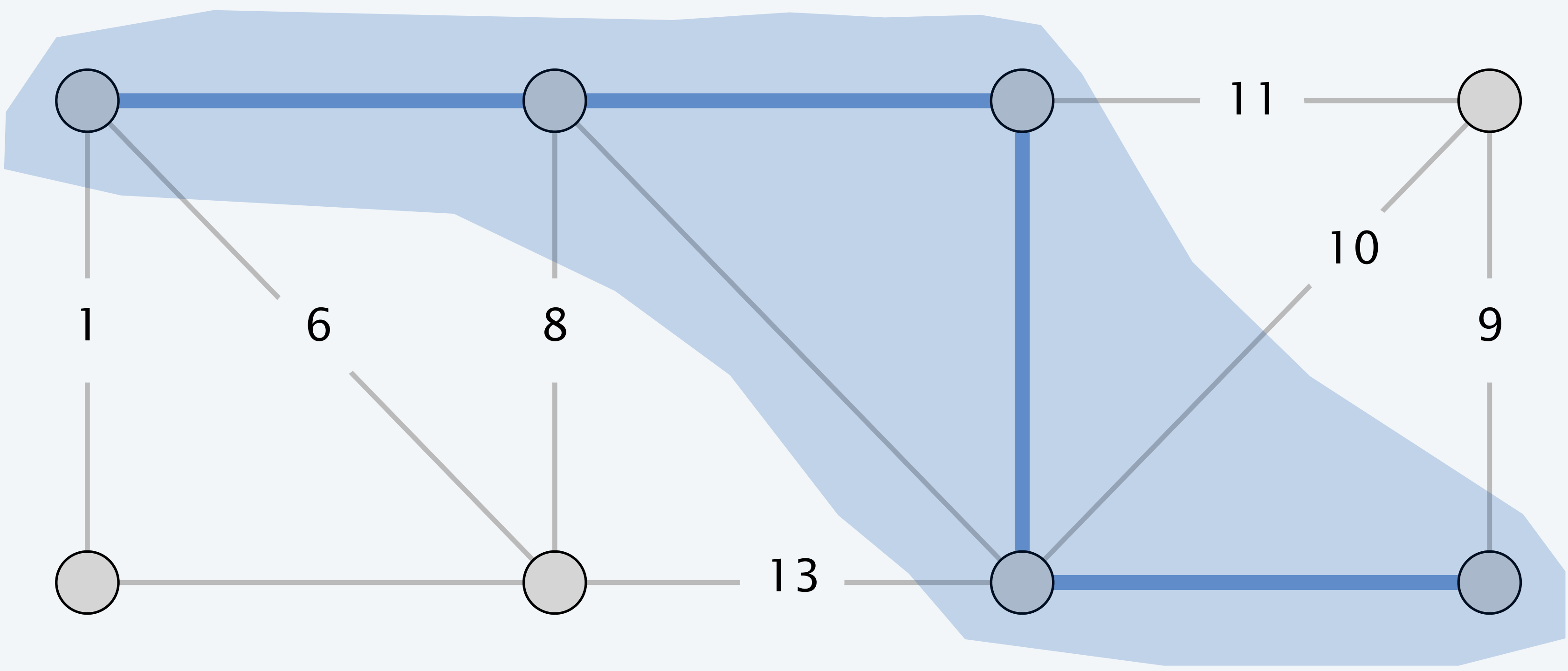

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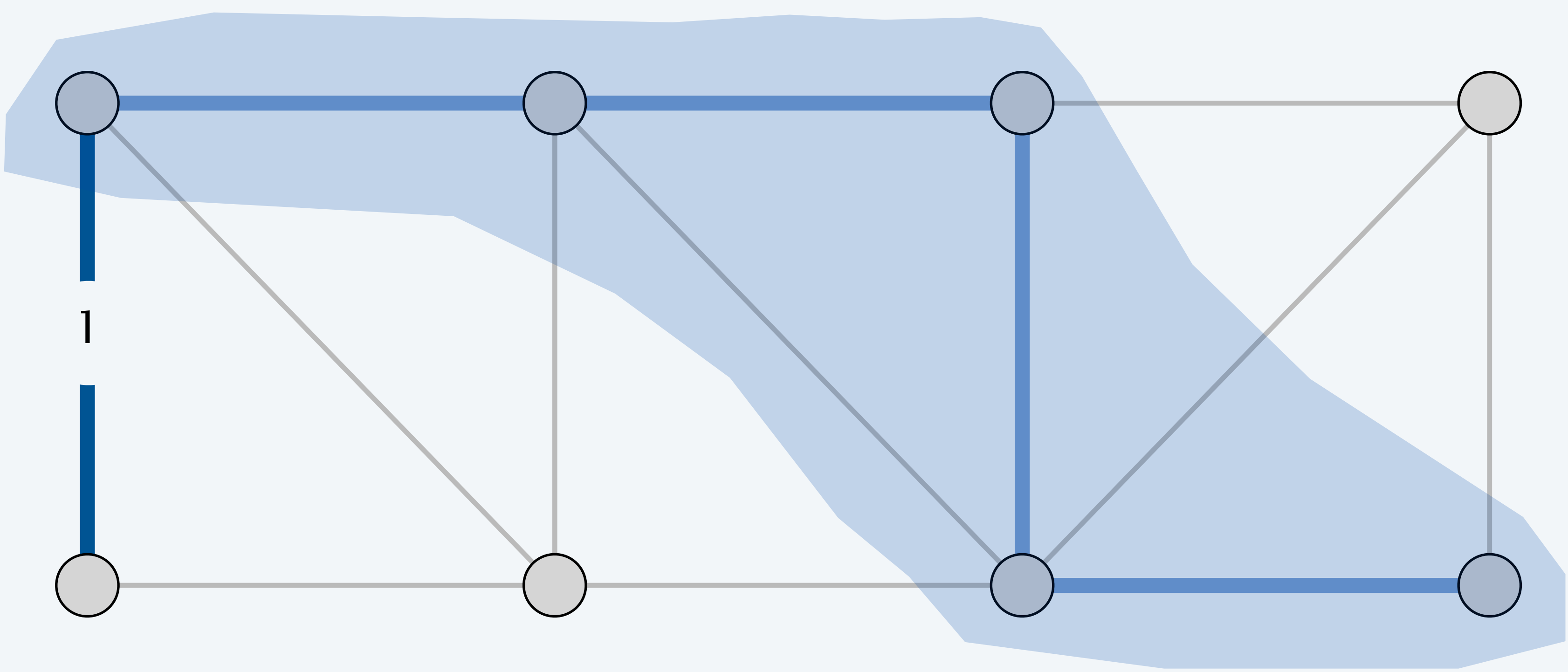

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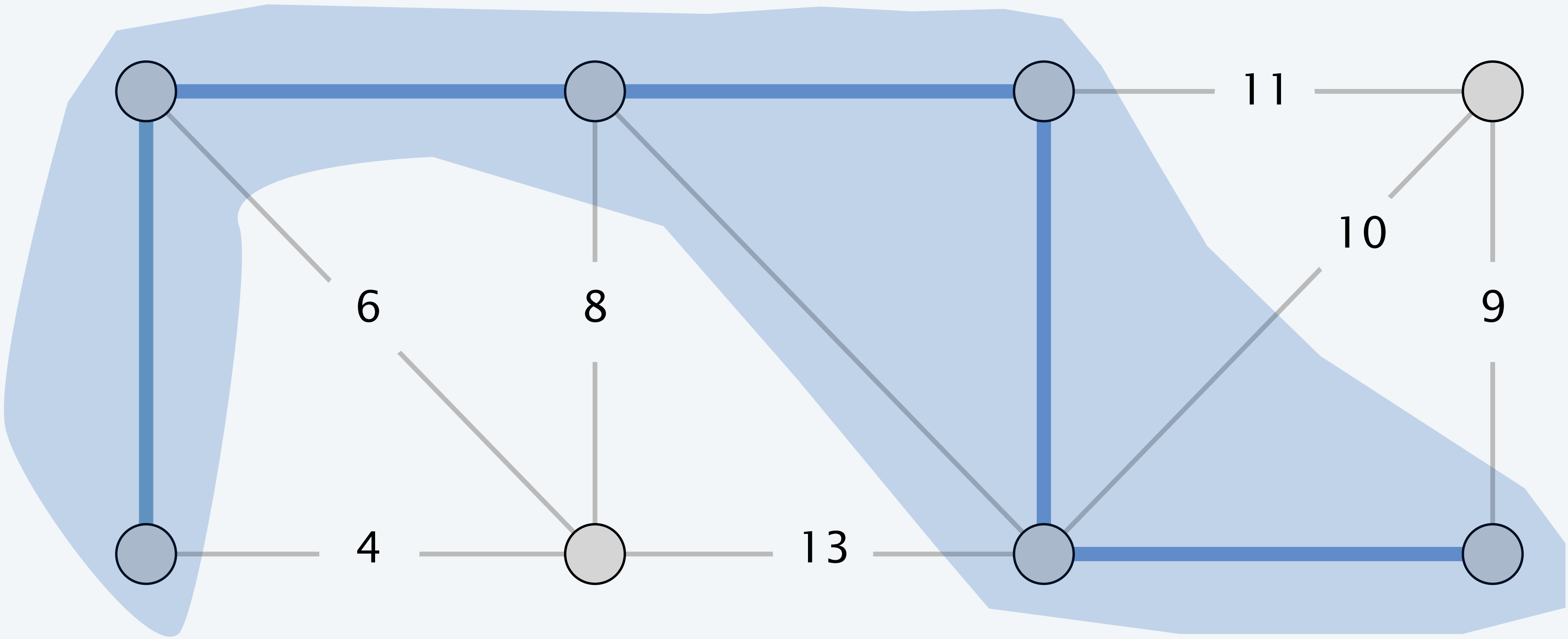

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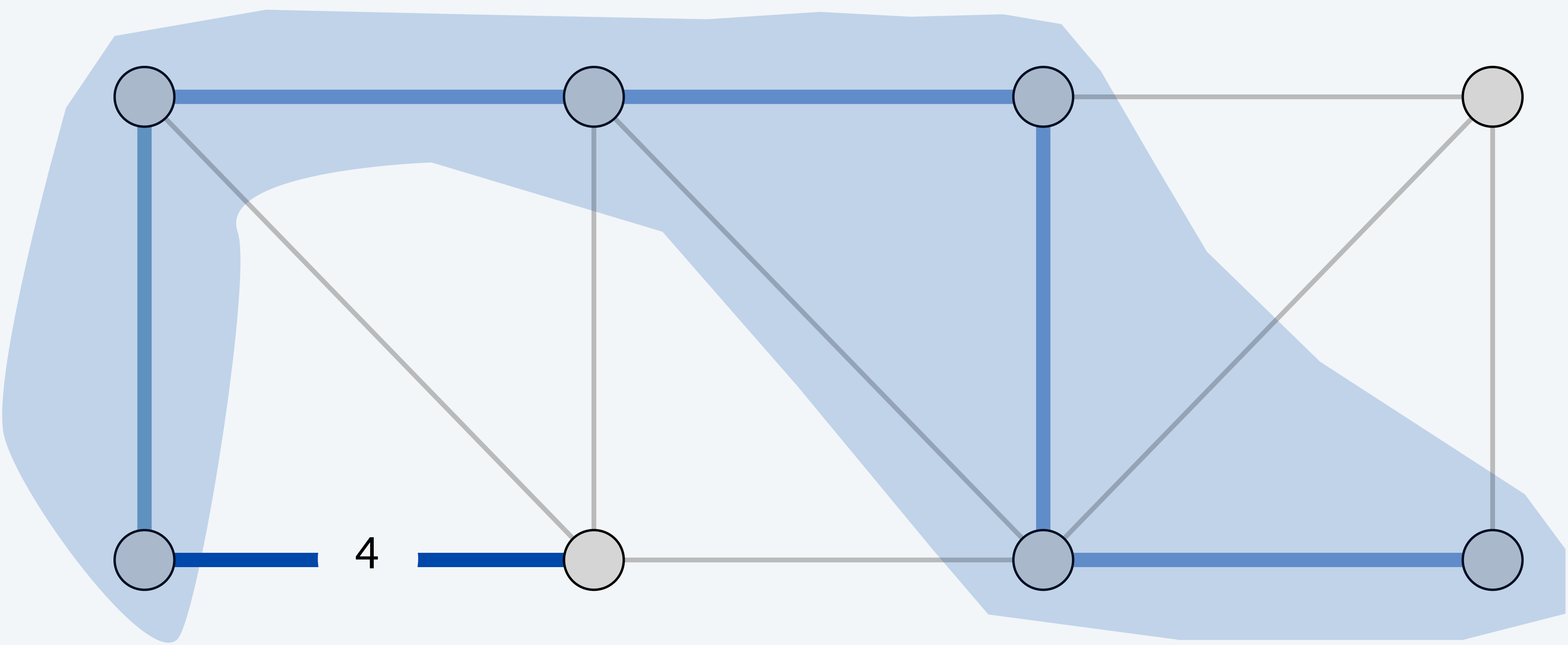

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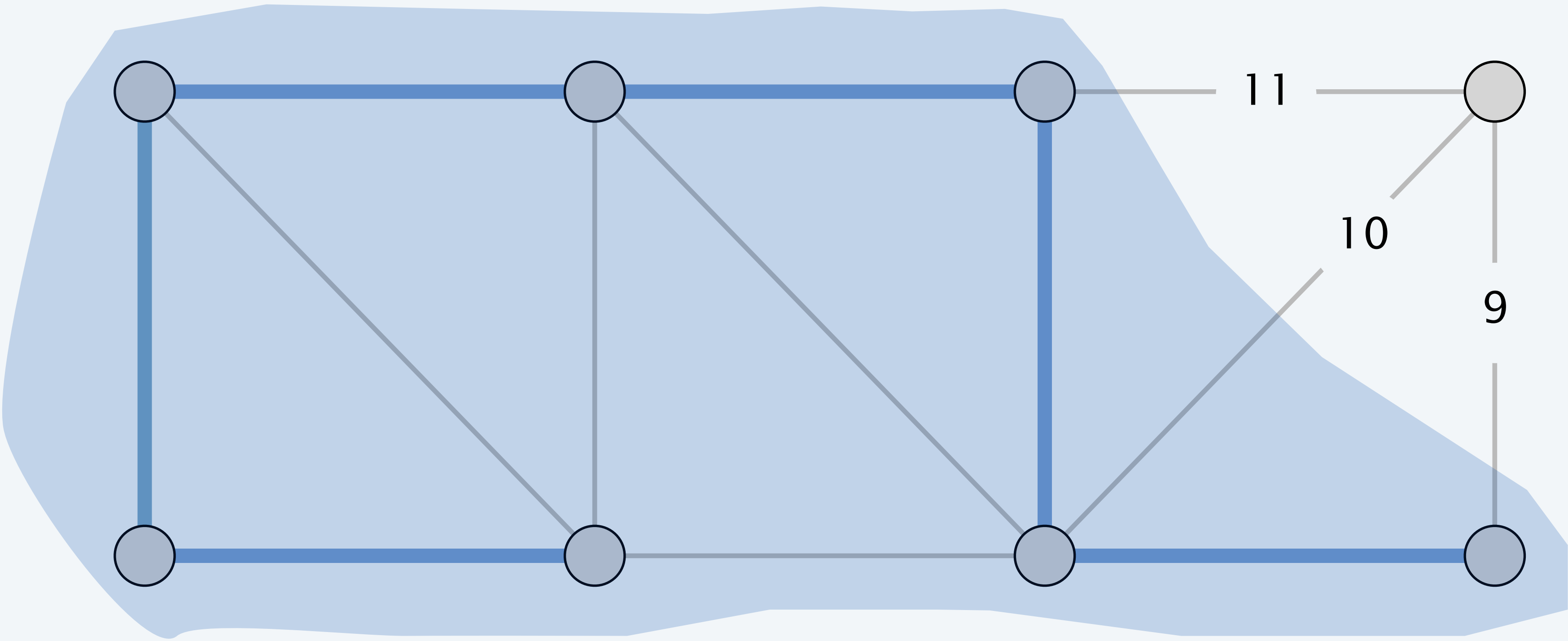

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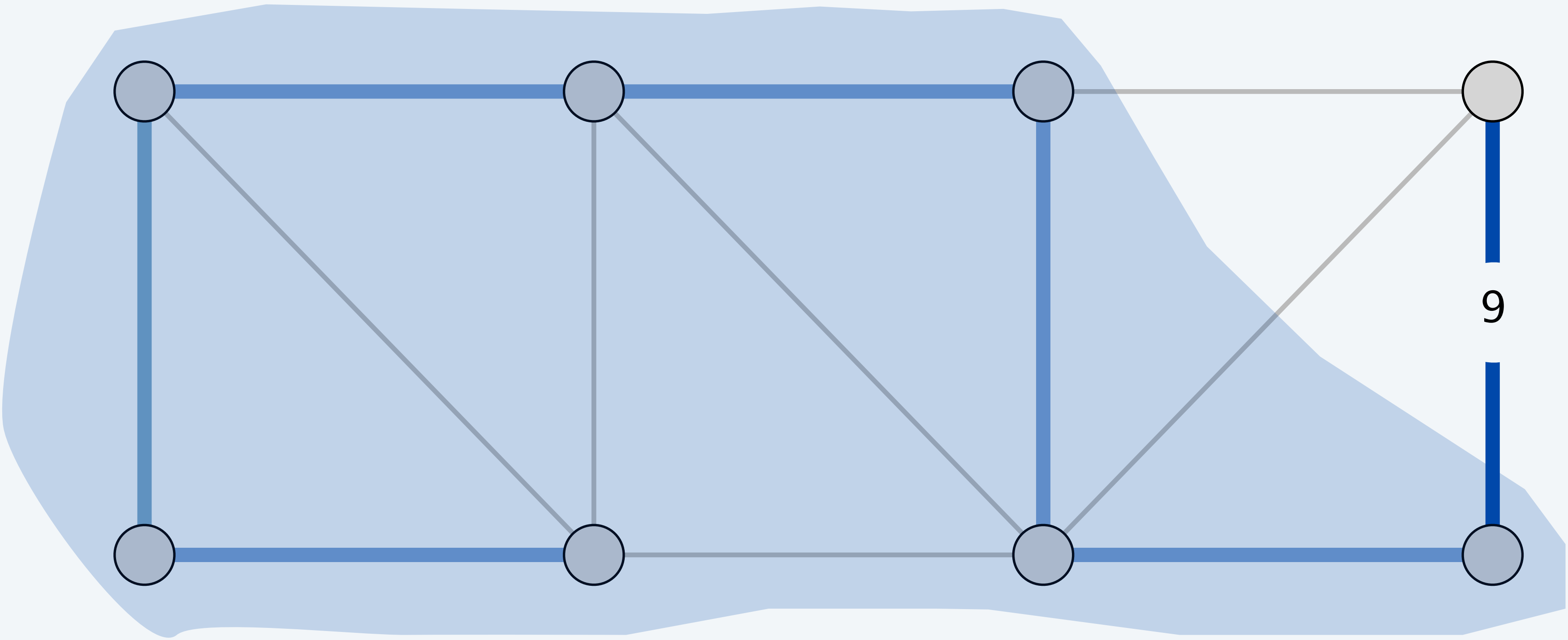

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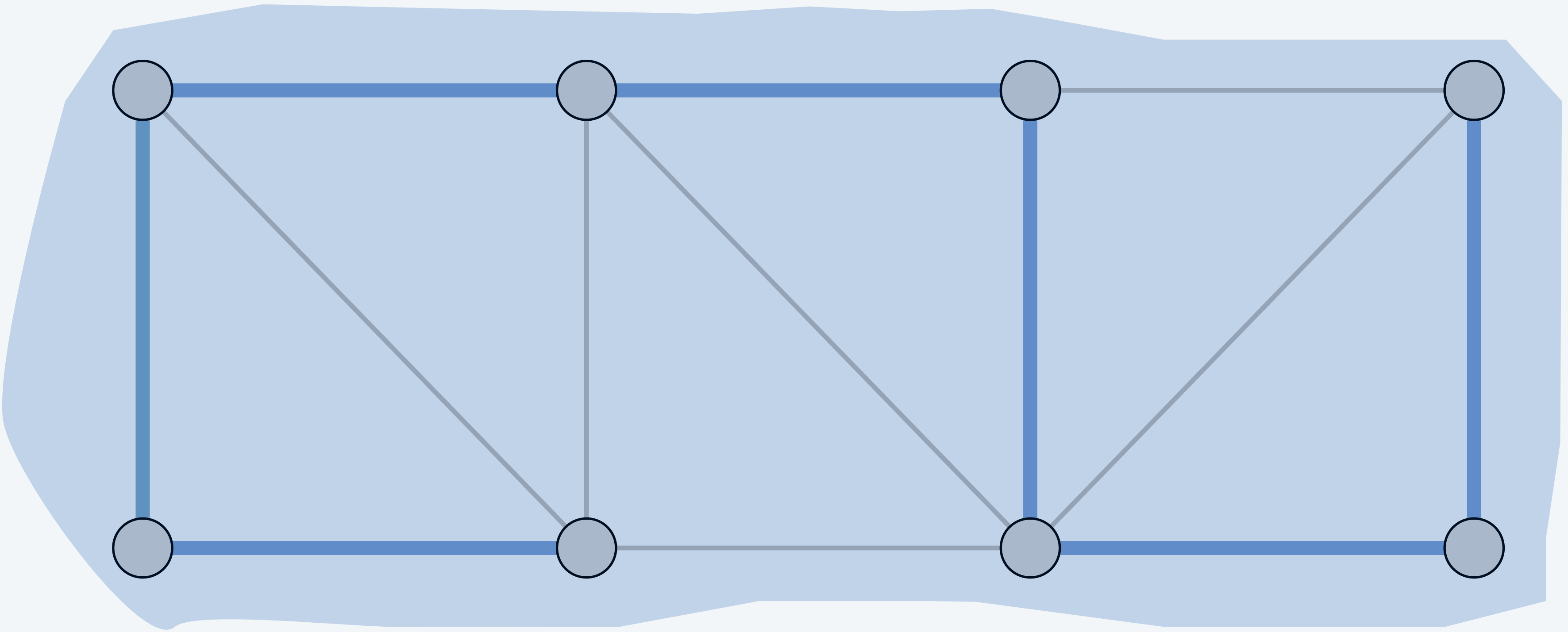

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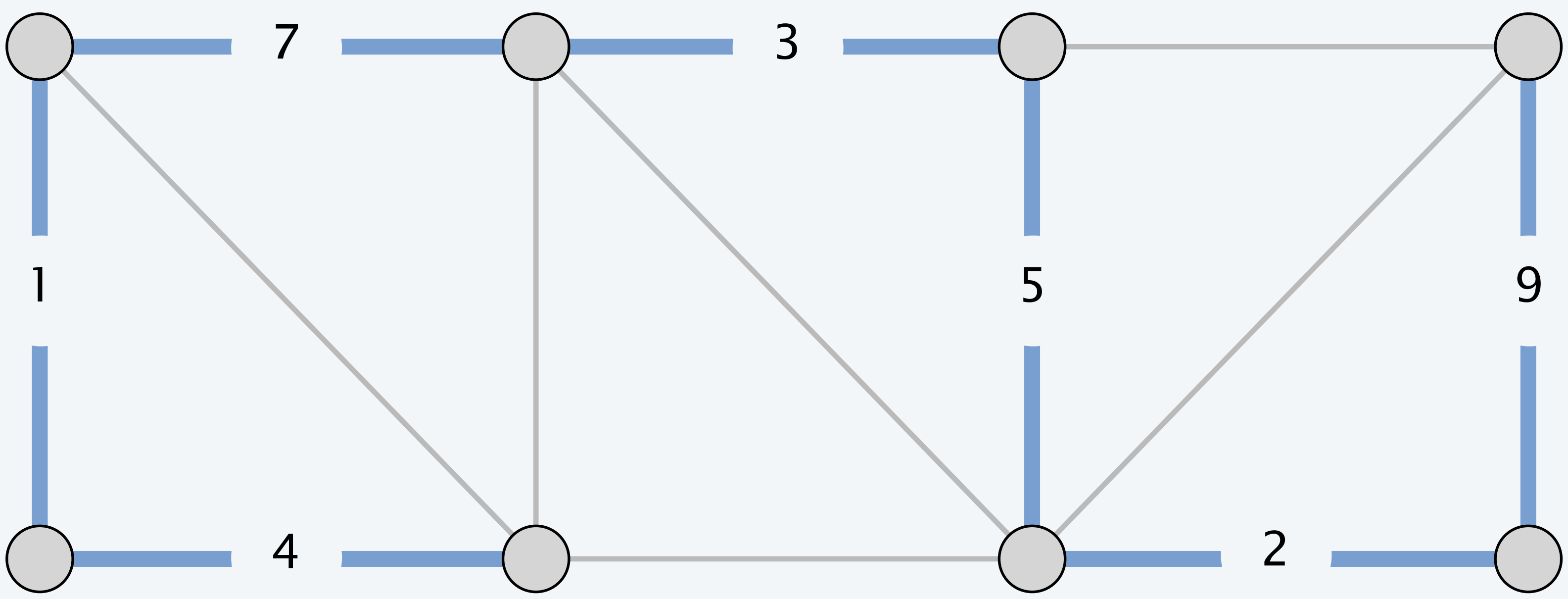
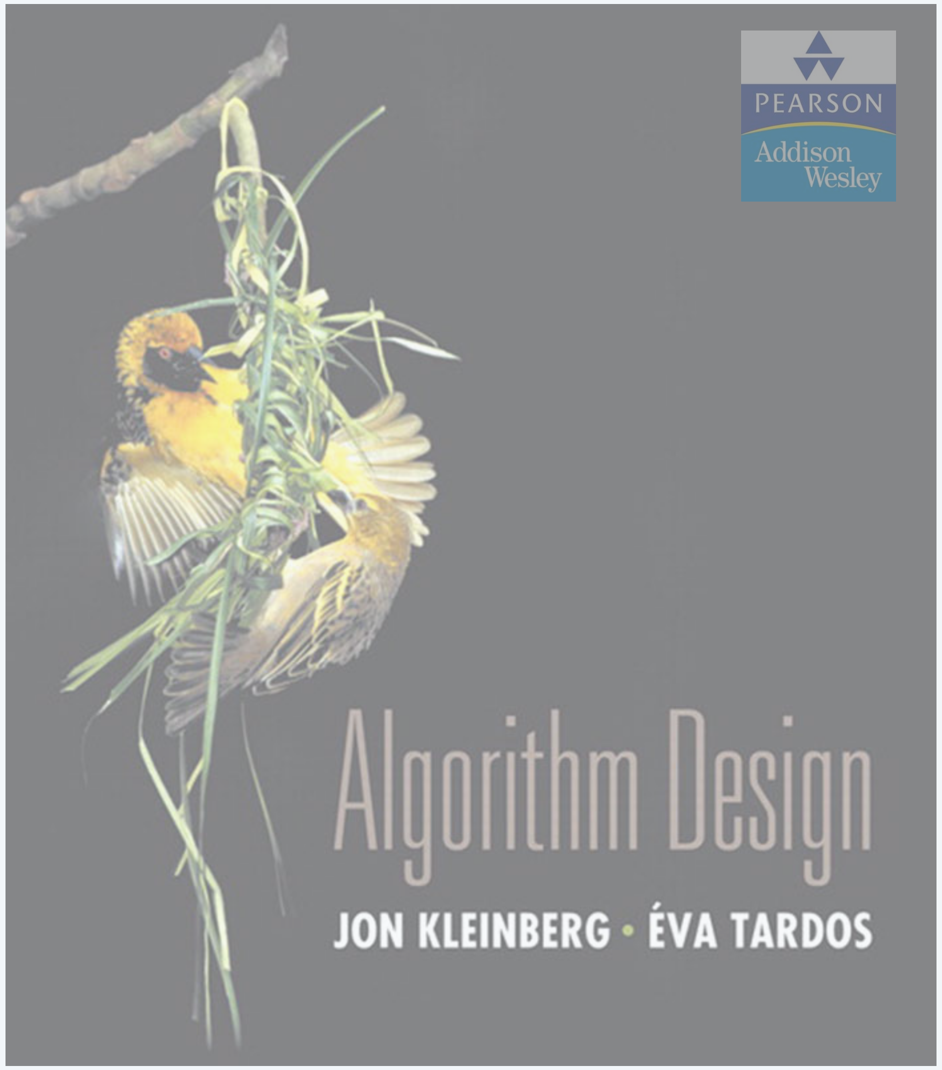




SECTION 4.5

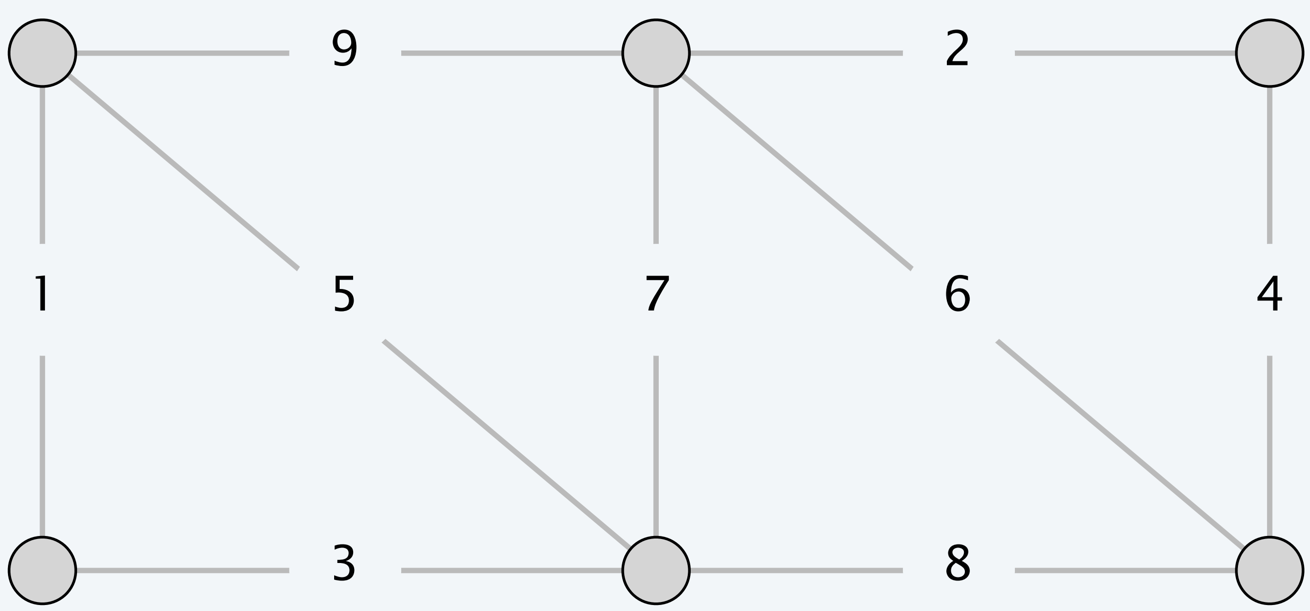
4. GREEDY ALGORITHMS II

- *red-rule blue-rule demo*
- *Prim's algorithm demo*
- *Kruskal's algorithm demo*
- *reverse-delete algorithm demo*
- *Boruvka's algorithm demo*

Kruskal's algorithm demo

Consider edges in ascending order of weight:

- Add to T unless it would create a cycle.



Kruskal's algorithm demo

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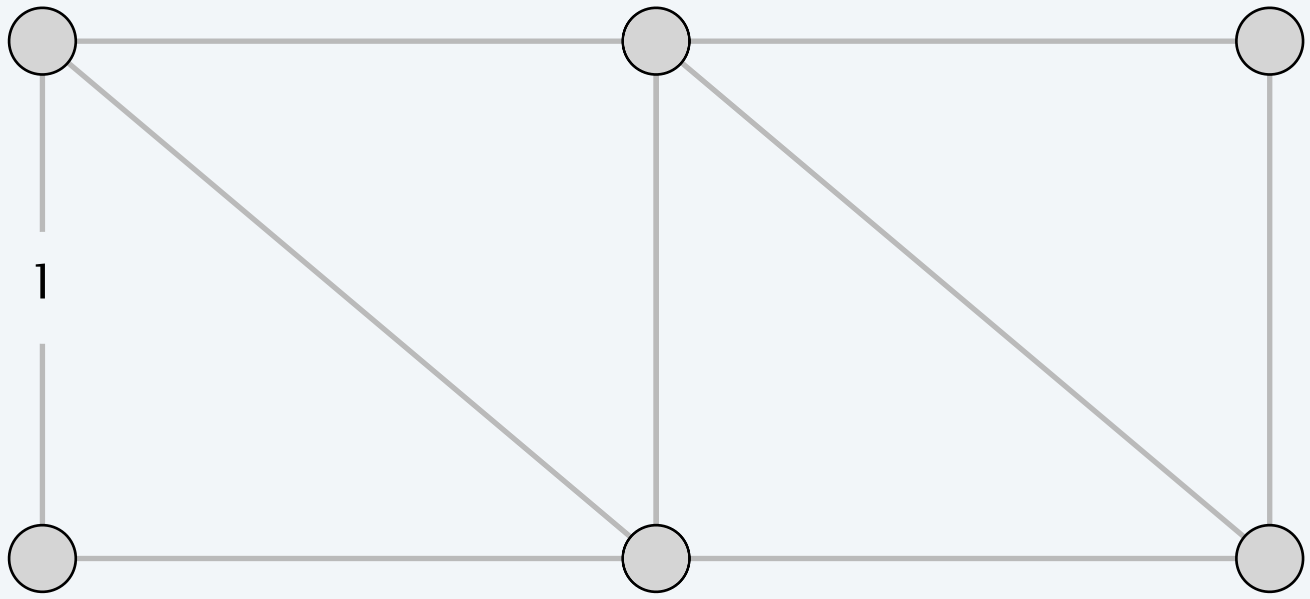

Kruskal's algorithm demo

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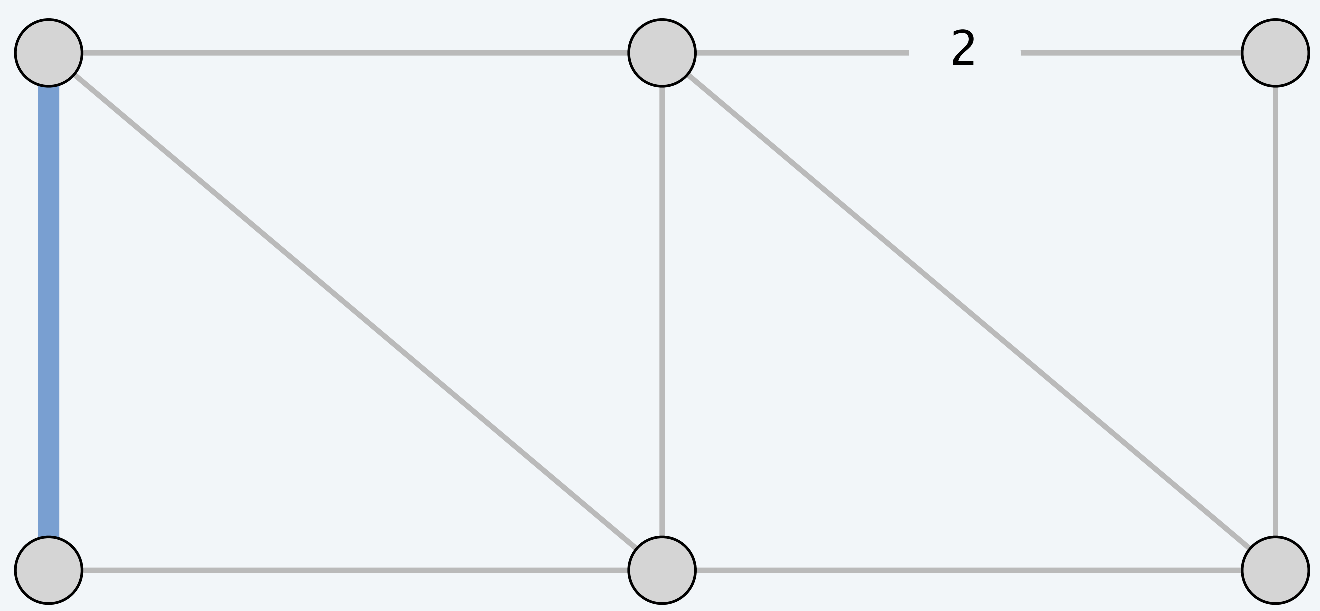

Kruskal's algorithm demo

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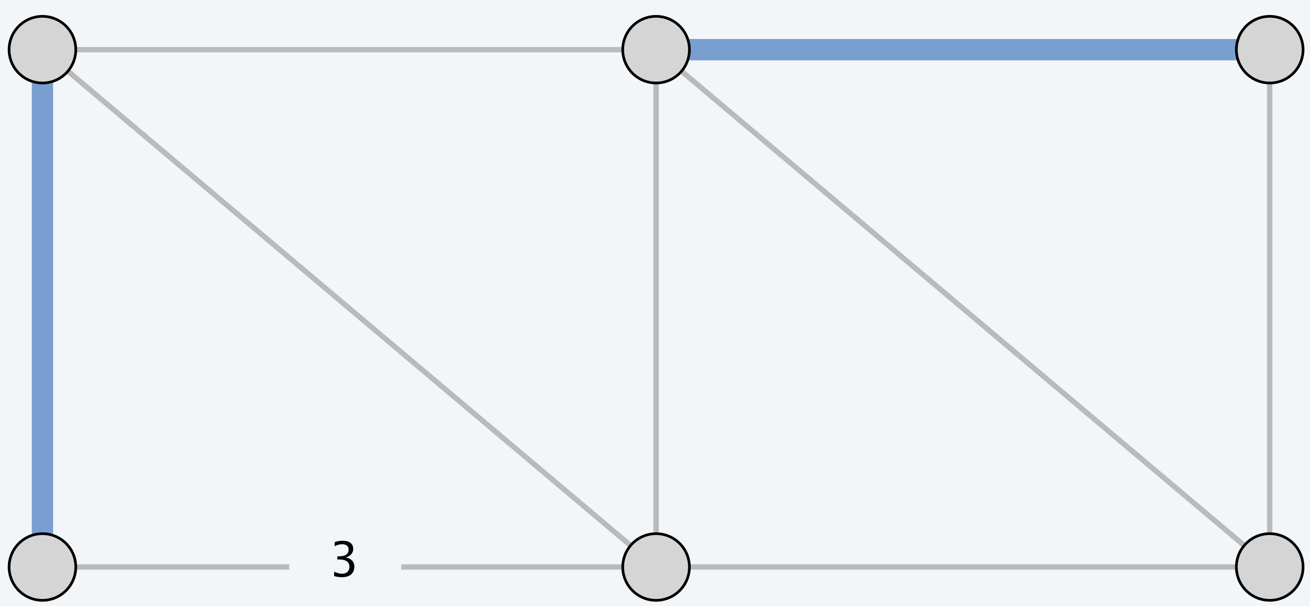

Kruskal's algorithm demo

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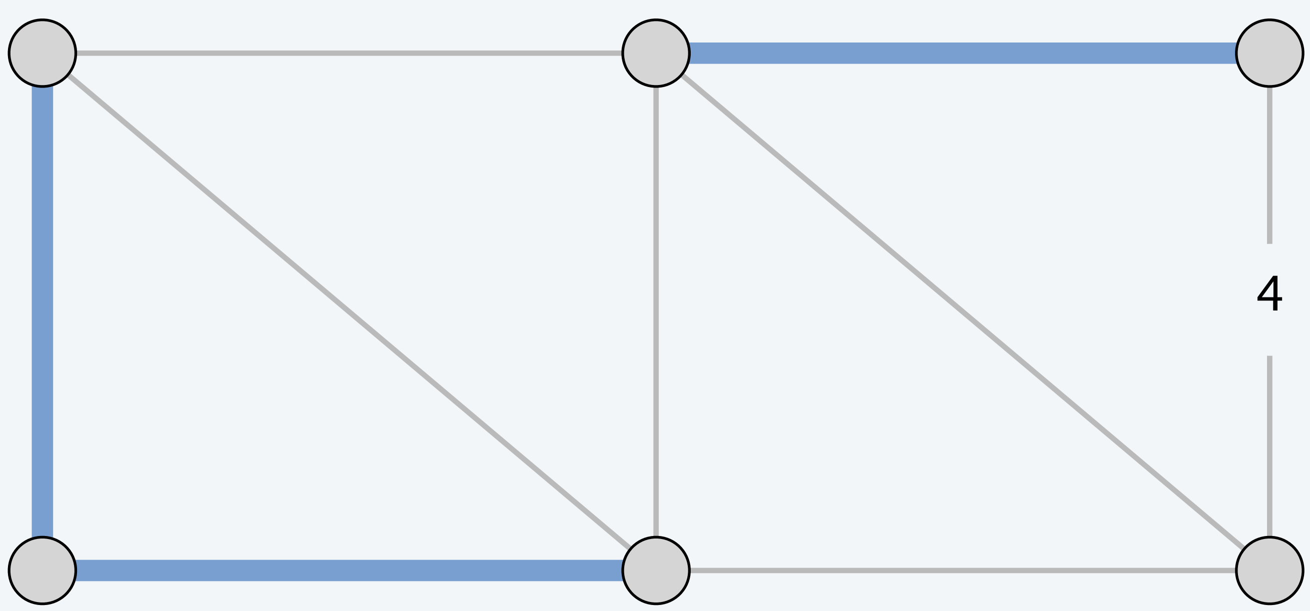

Kruskal's algorithm demo

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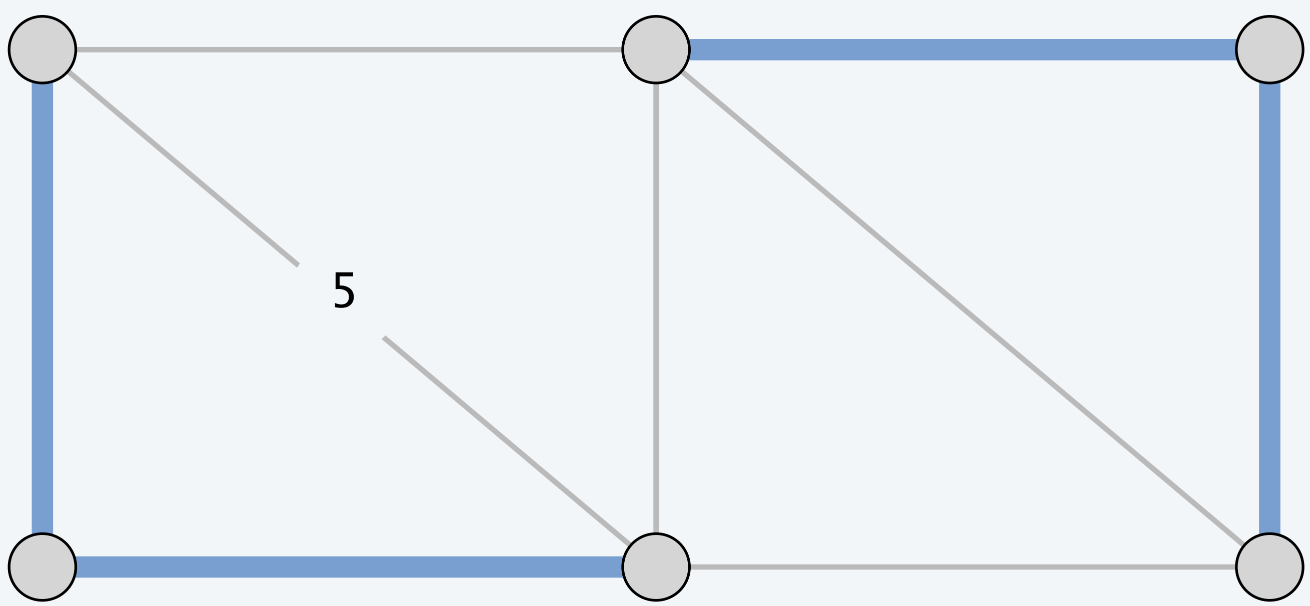

Kruskal's algorithm demo

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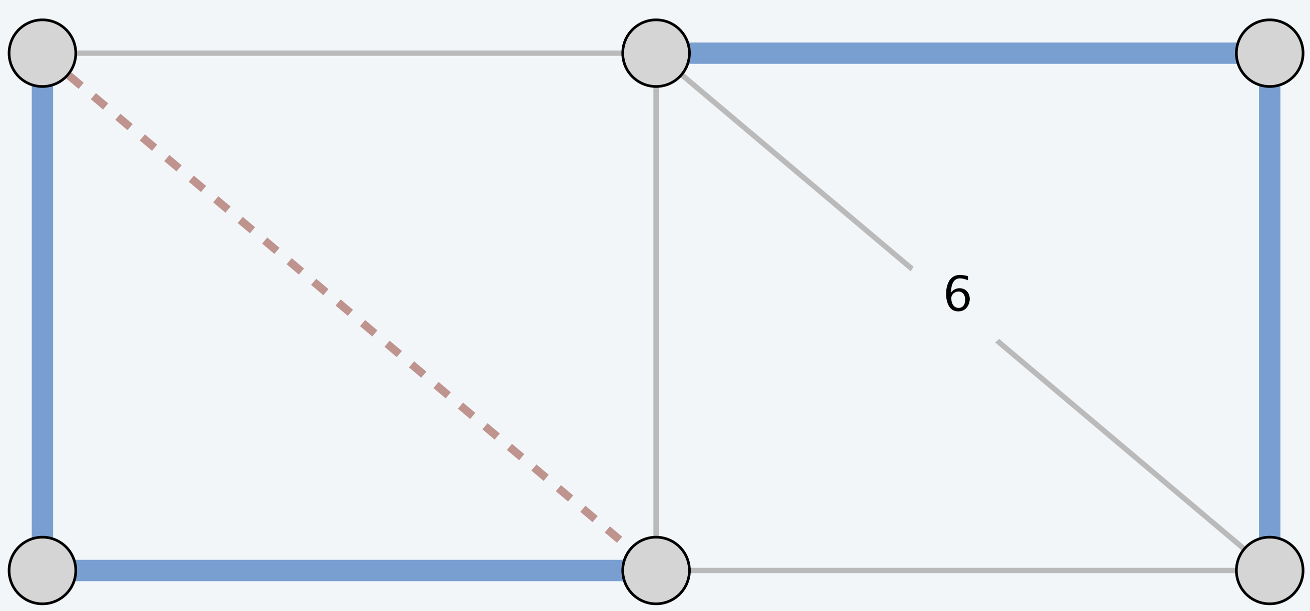

Kruskal's algorithm demo

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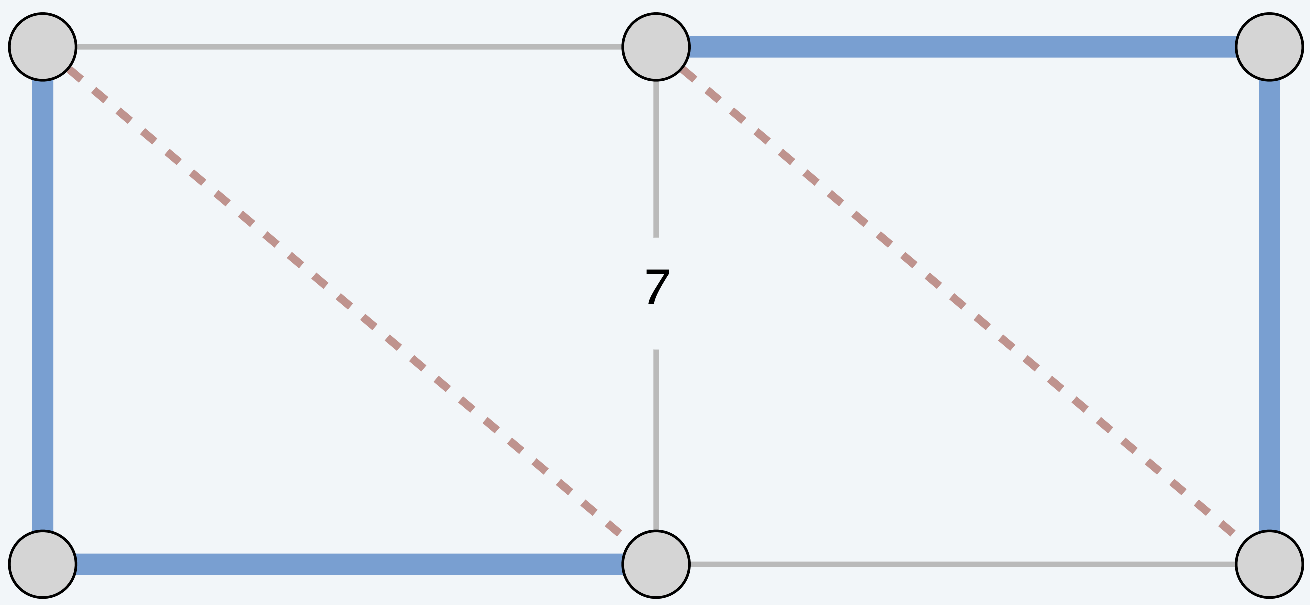

Kruskal's algorithm demo

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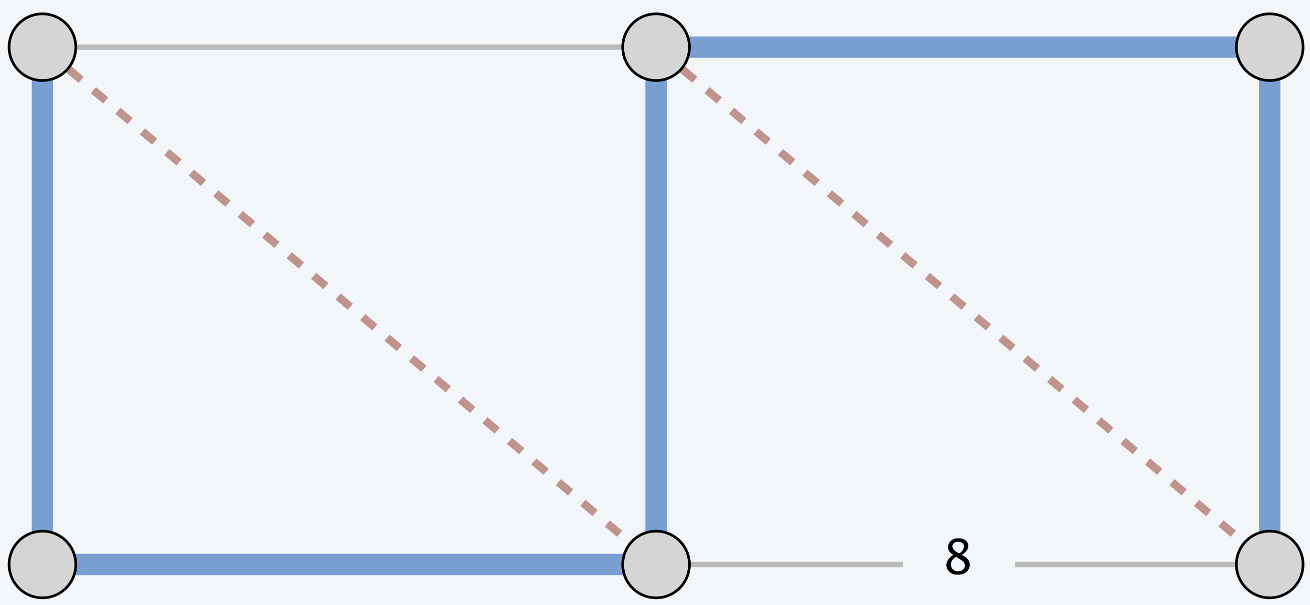

Kruskal's algorithm demo

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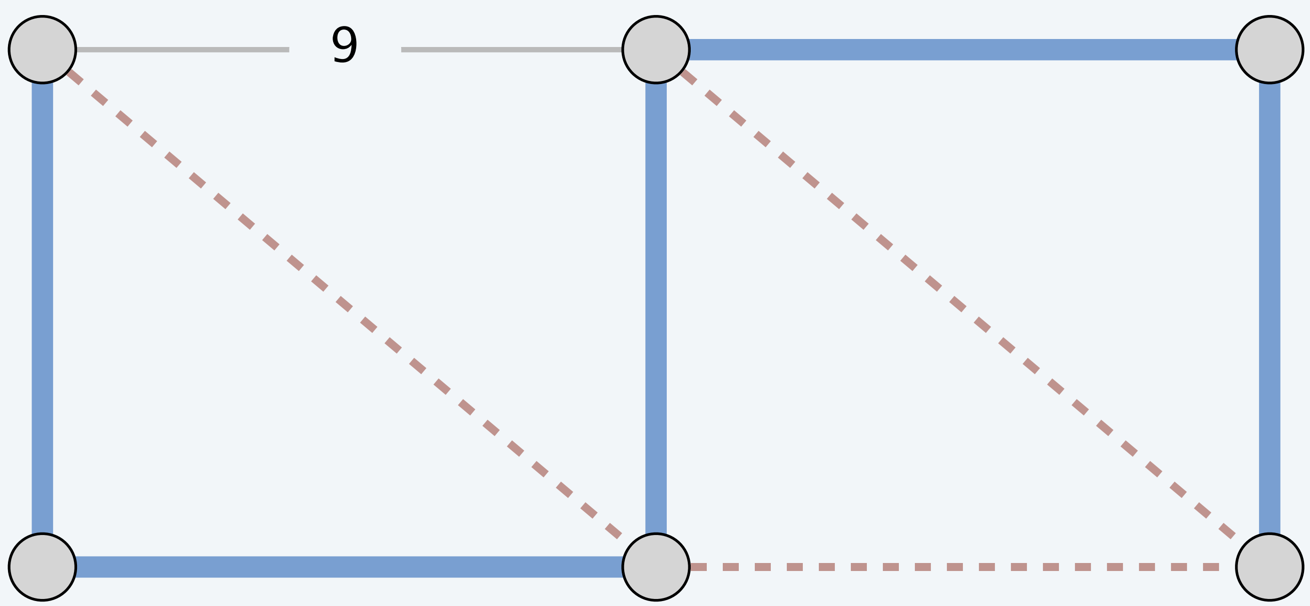

Kruskal's algorithm demo

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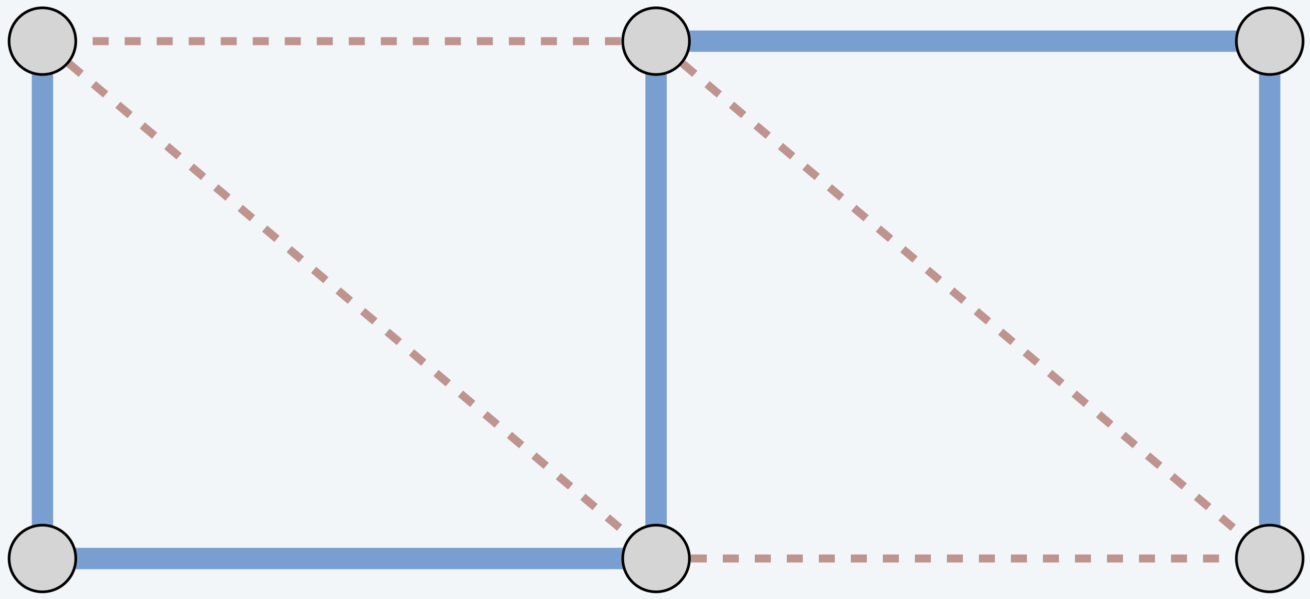

Kruskal's algorithm demo

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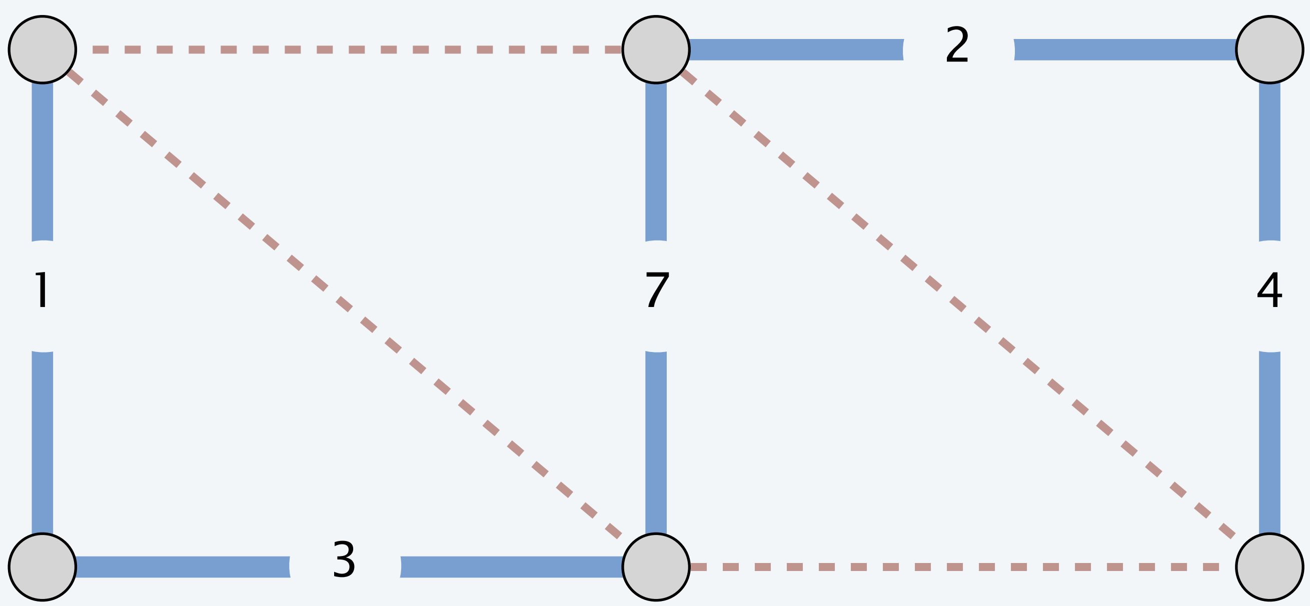
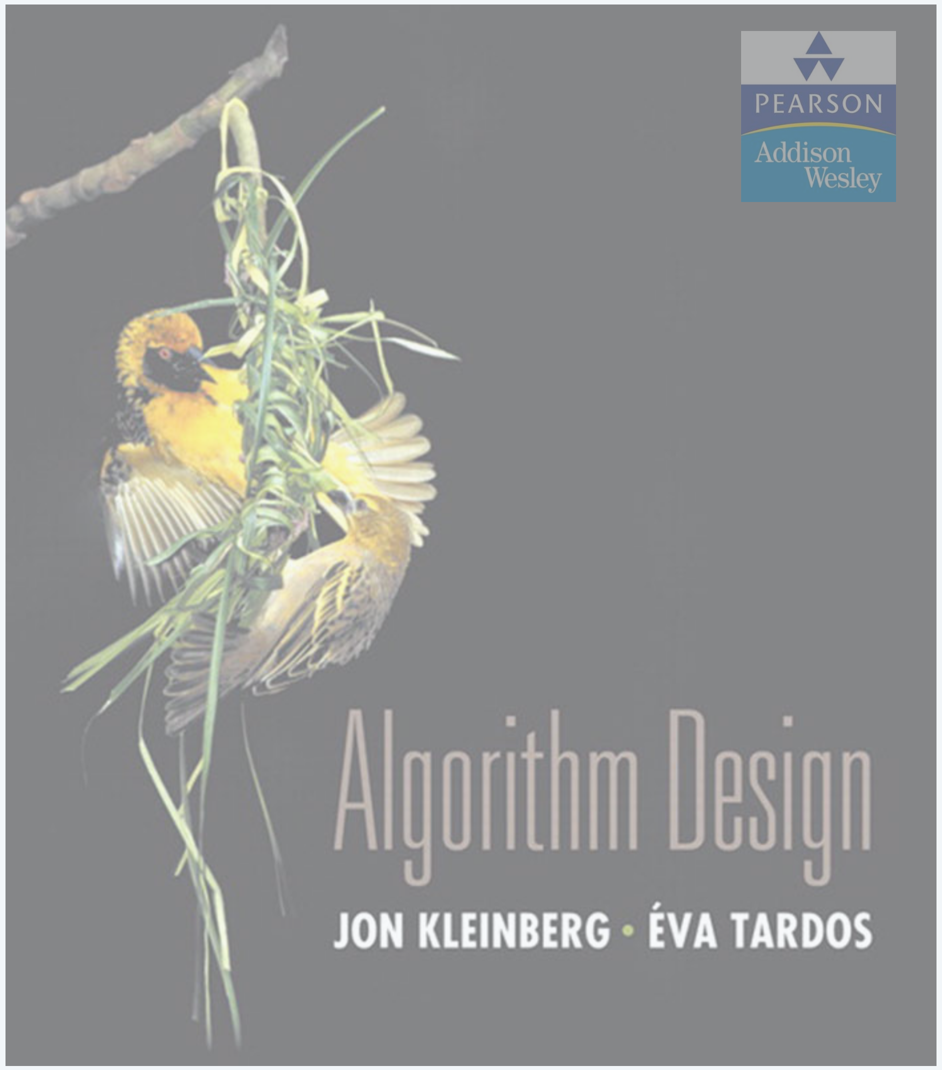




SECTION 4.5

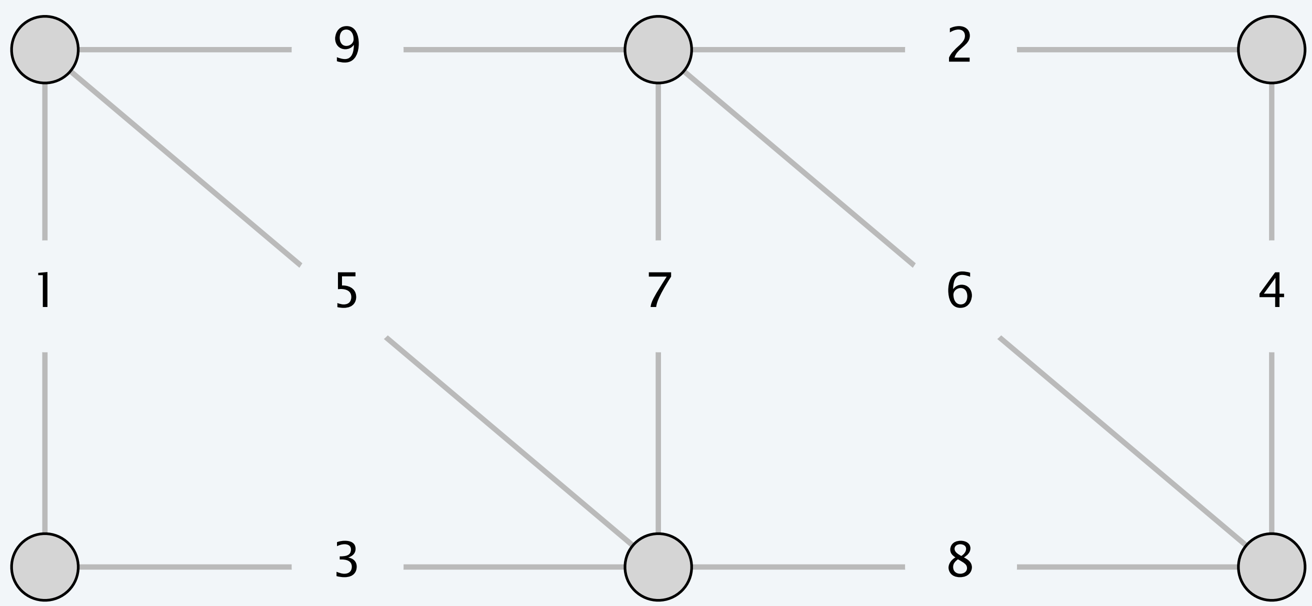
4. GREEDY ALGORITHMS II

- *red-rule blue-rule demo*
- *Prim's algorithm demo*
- *Kruskal's algorithm demo*
- *reverse-delete algorithm demo*
- *Boruvka's algorithm demo*

Reverse-delete algorithm demo

Start with all edges in T and consider them in descending order of weight:

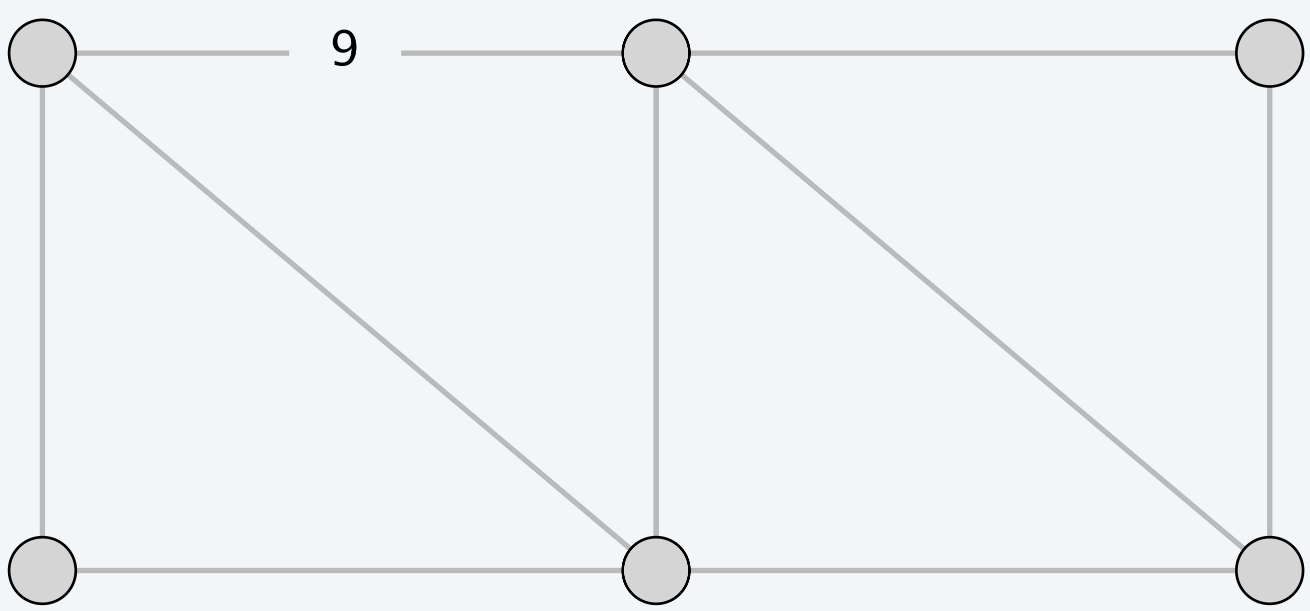
- Delete edge from T unless it would disconnect T.



Reverse-delete algorithm

Start with all edges in T and consider them in descending order of weight:

- Delete edge from T unless it would disconnect T.



Reverse-delete algorithm

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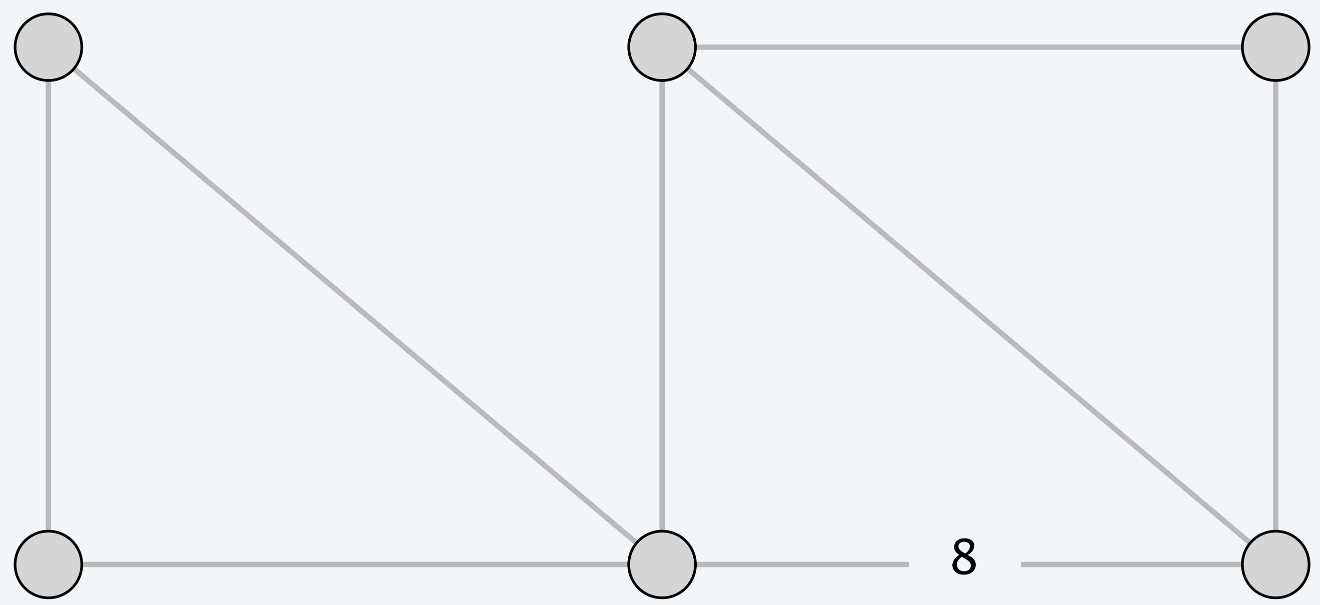

Reverse-delete algorithm

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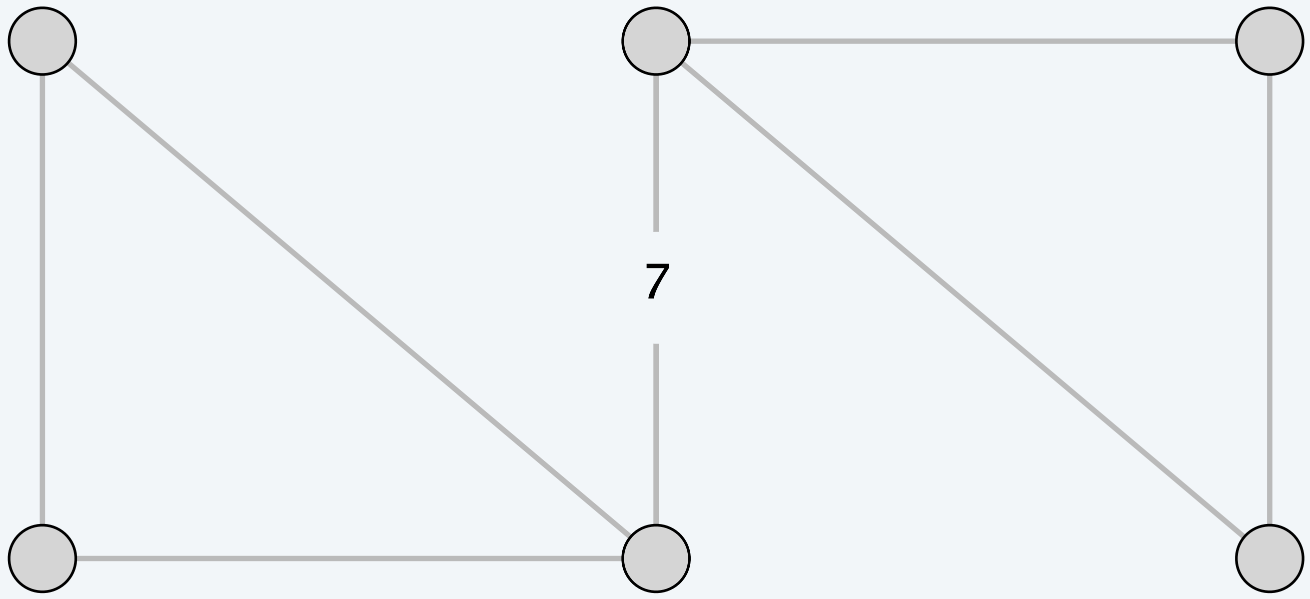

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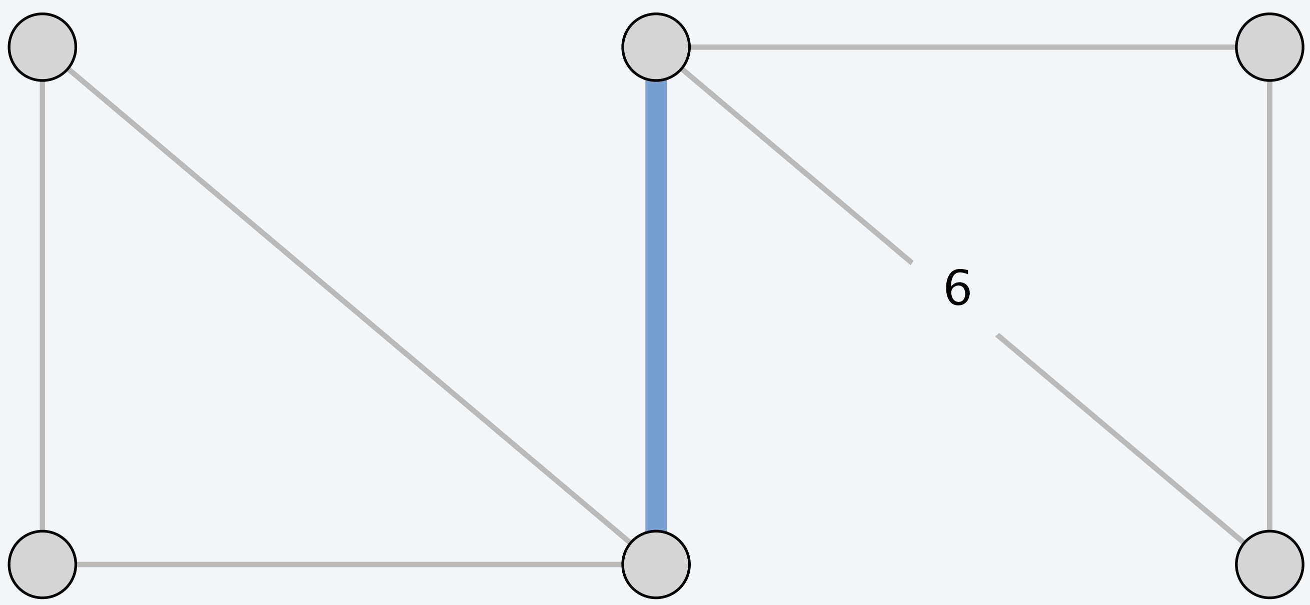

Reverse-delete algorithm

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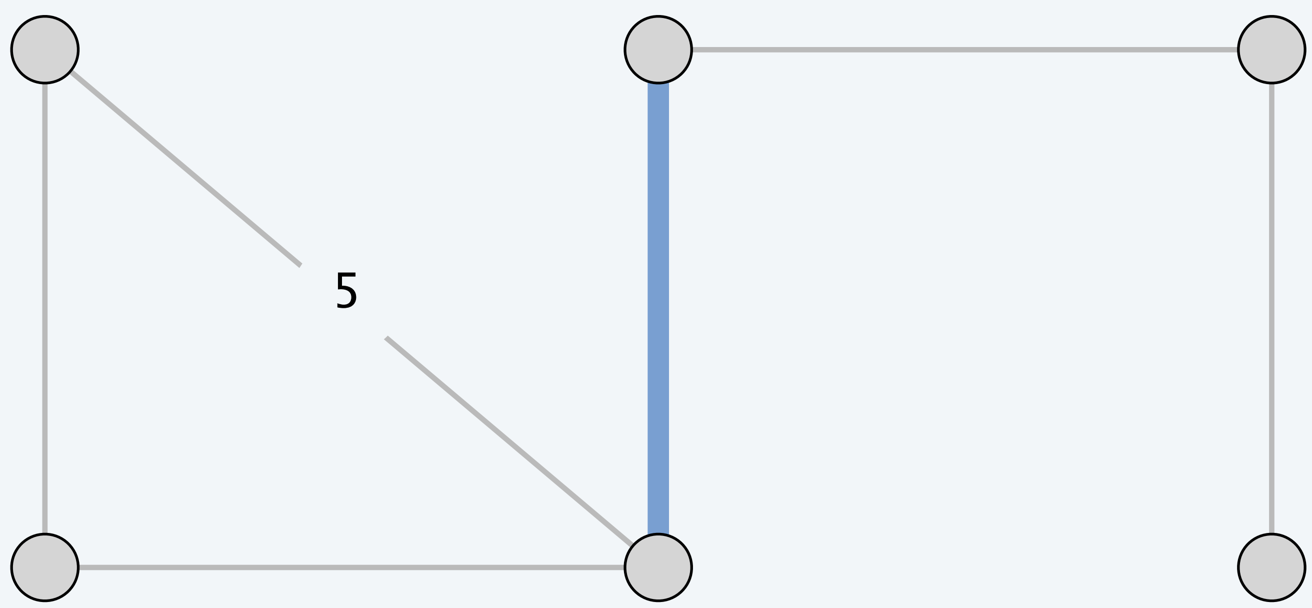

Reverse-delete algorithm

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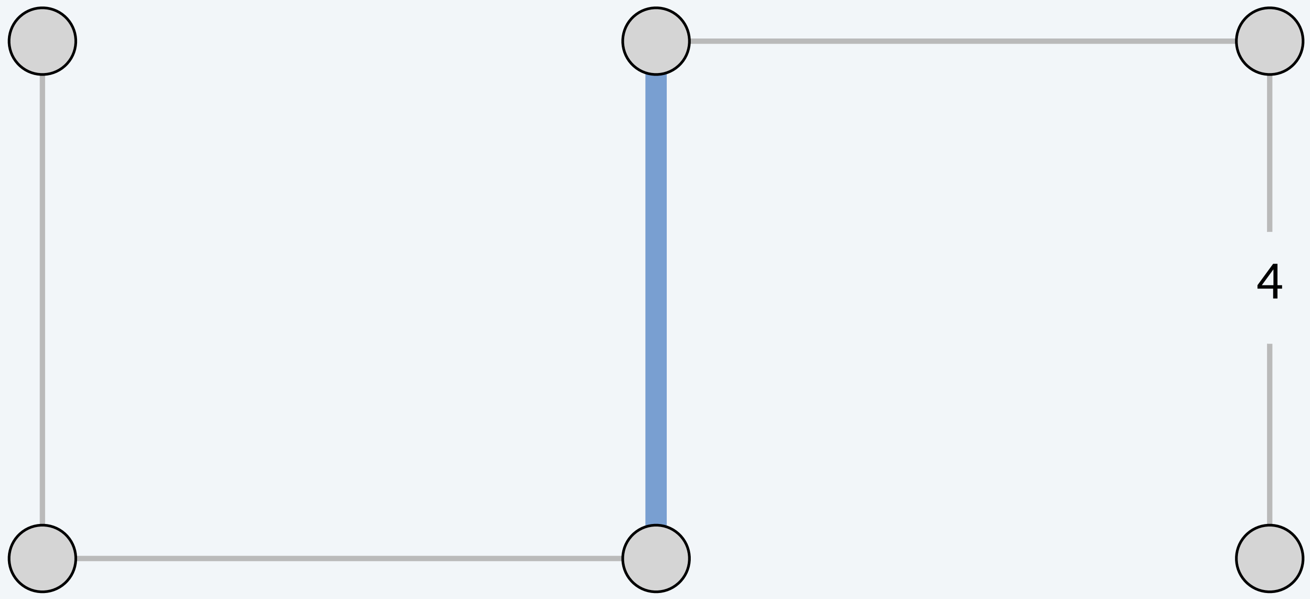

Reverse-delete algorithm

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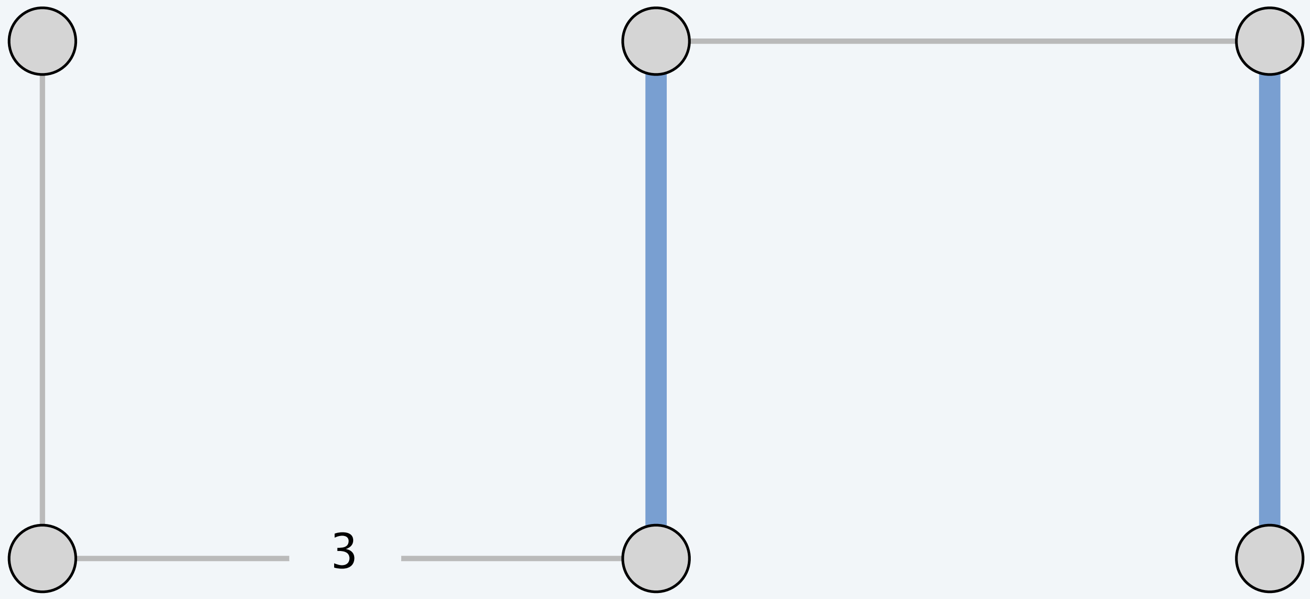

Reverse-delete algorithm

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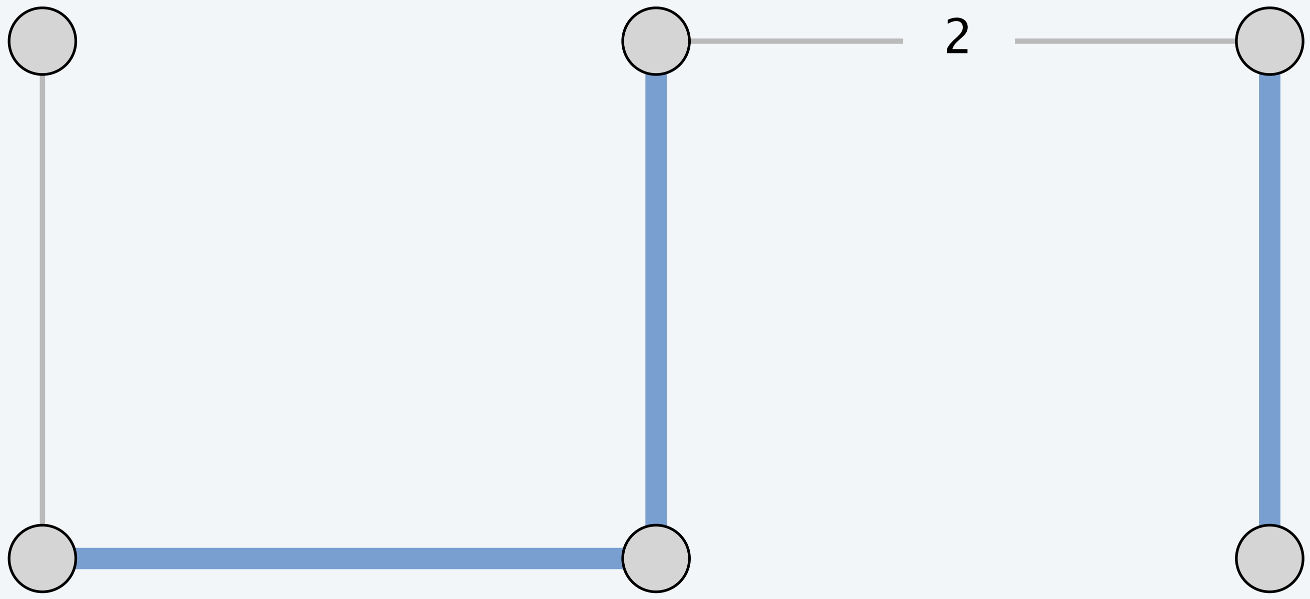

Reverse-delete algorithm

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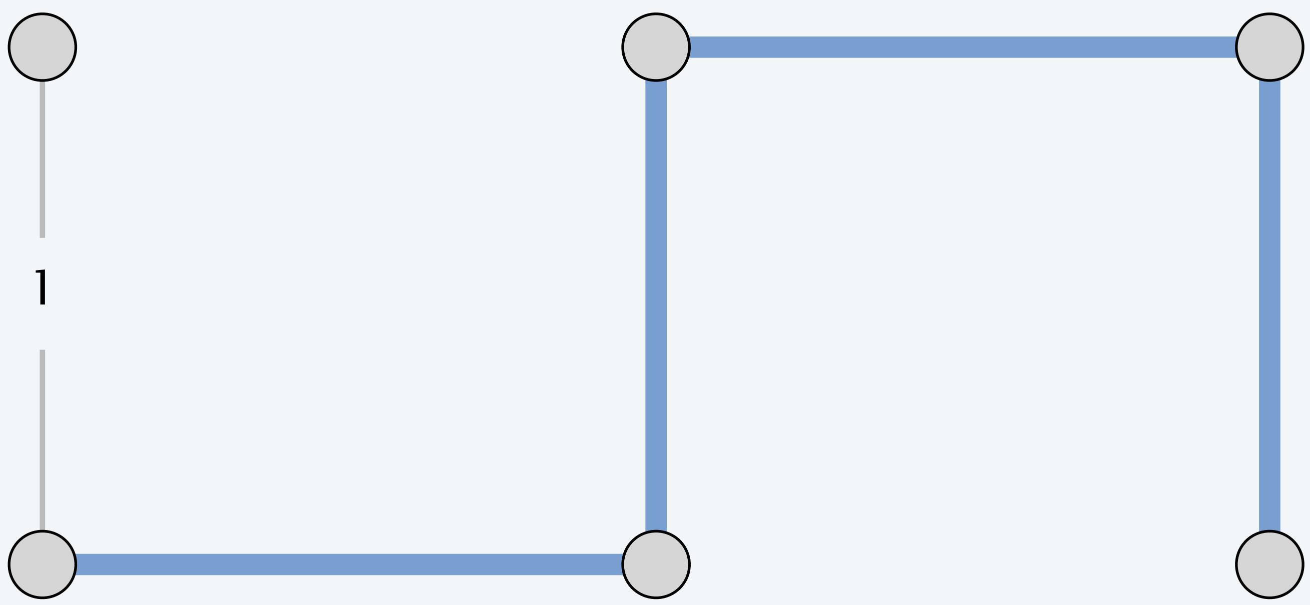

Reverse-delete algorithm

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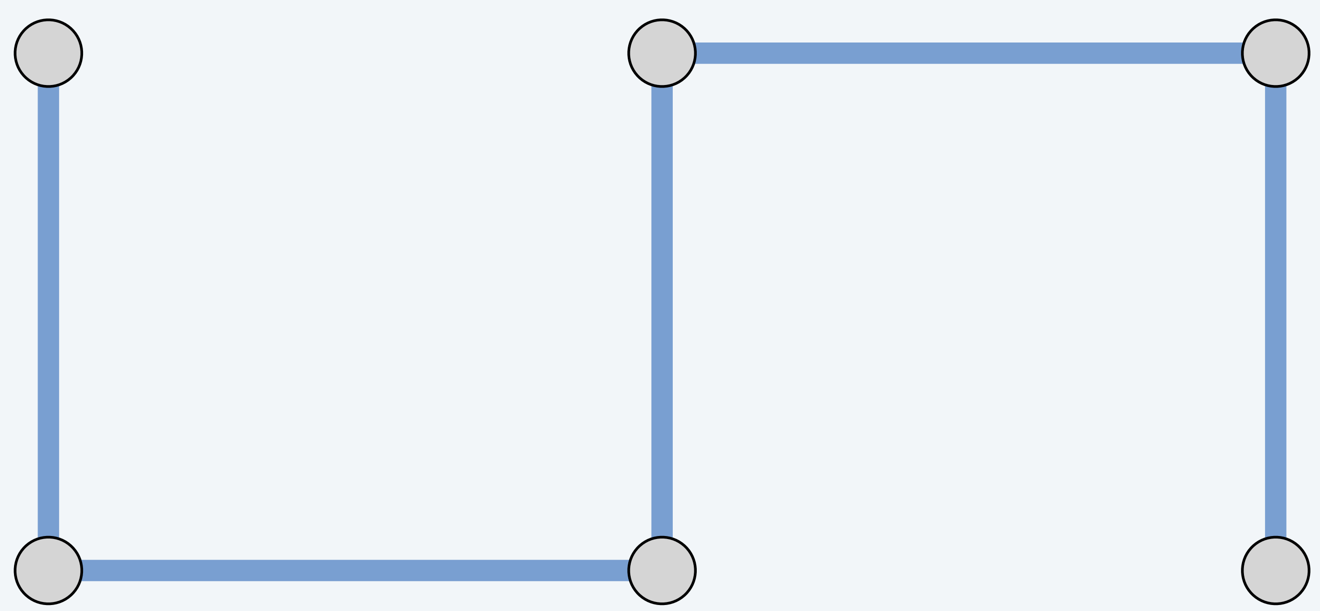

Reverse-delete algorithm

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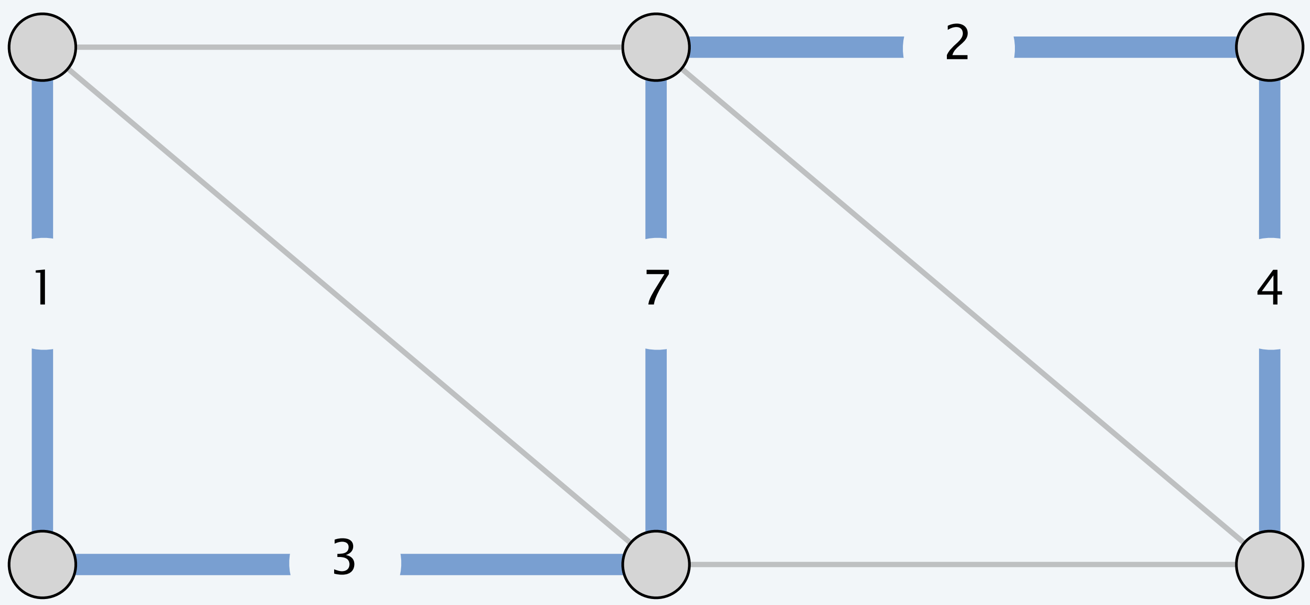
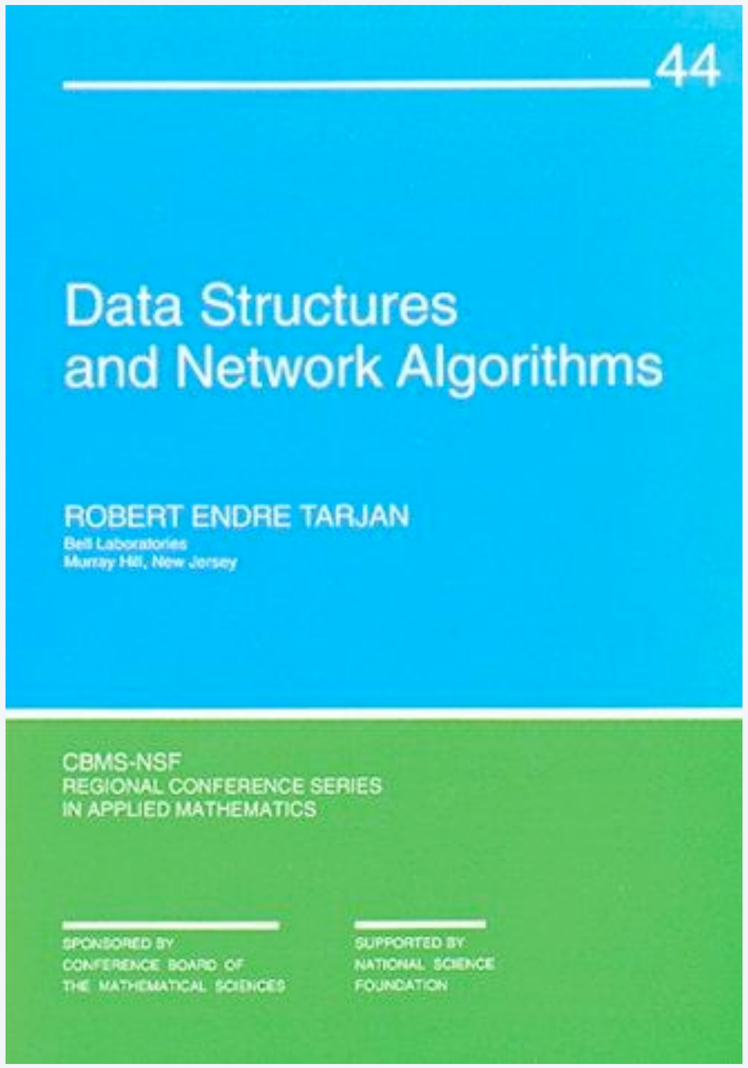




SECTION 6.2

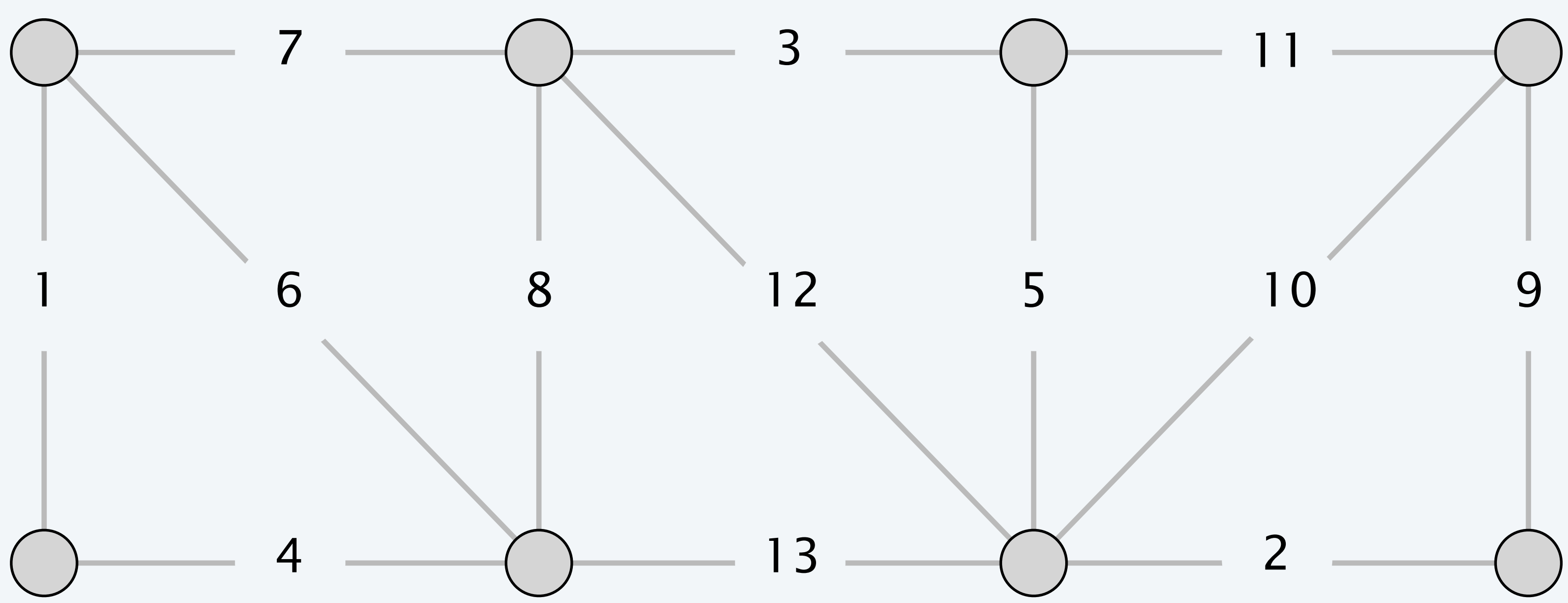
4. GREEDY ALGORITHMS II

- *red-rule blue-rule demo*
- *Prim's algorithm demo*
- *Kruskal's algorithm demo*
- *reverse-delete algorithm demo*
- *Boruvka's algorithm demo*

Borůvka's algorithm demo

Repeat until only one tree.

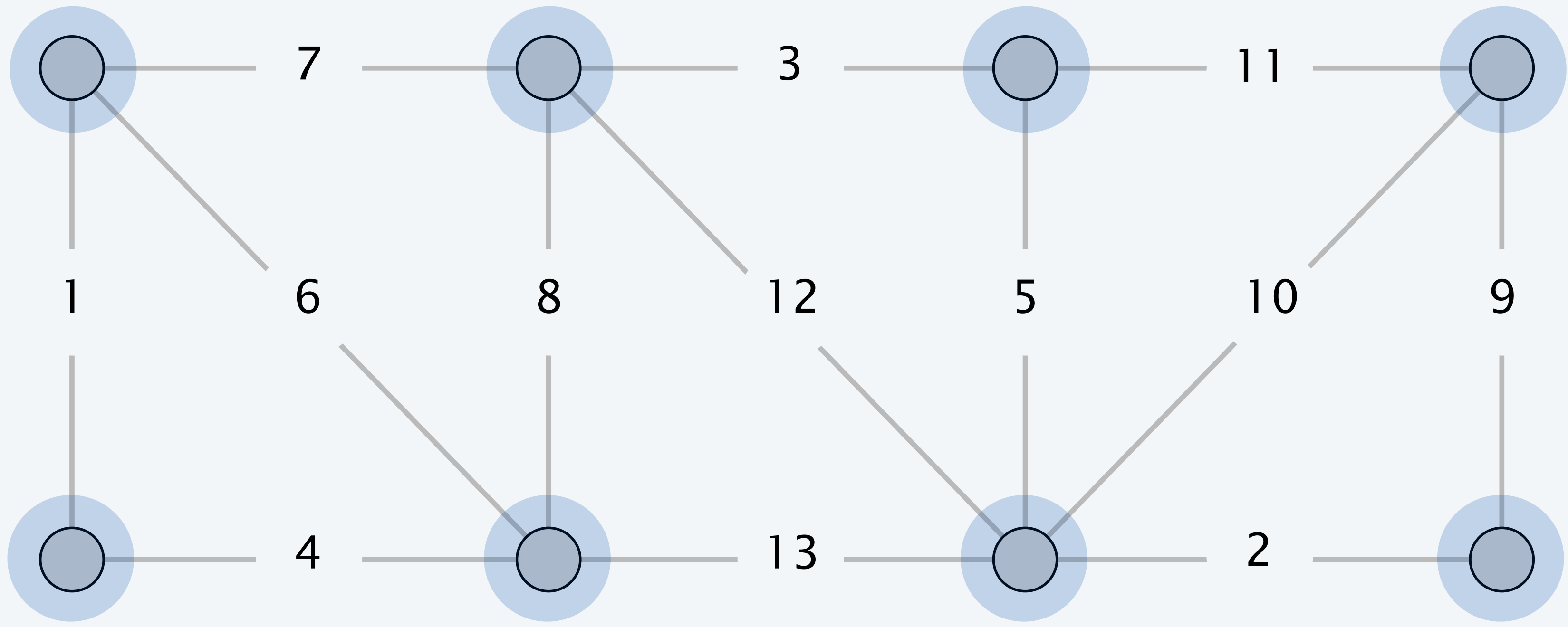
- Apply blue rule to cutset corresponding to each blue tree.
- Color all selected edges blue.



Borůvka's algorithm demo

Repeat until only one tree.

- Apply blue rule to cutset corresponding to each blue tree.
- Color all selected edges blue.



Borůvka's algorithm demo

Repeat until only one tree.

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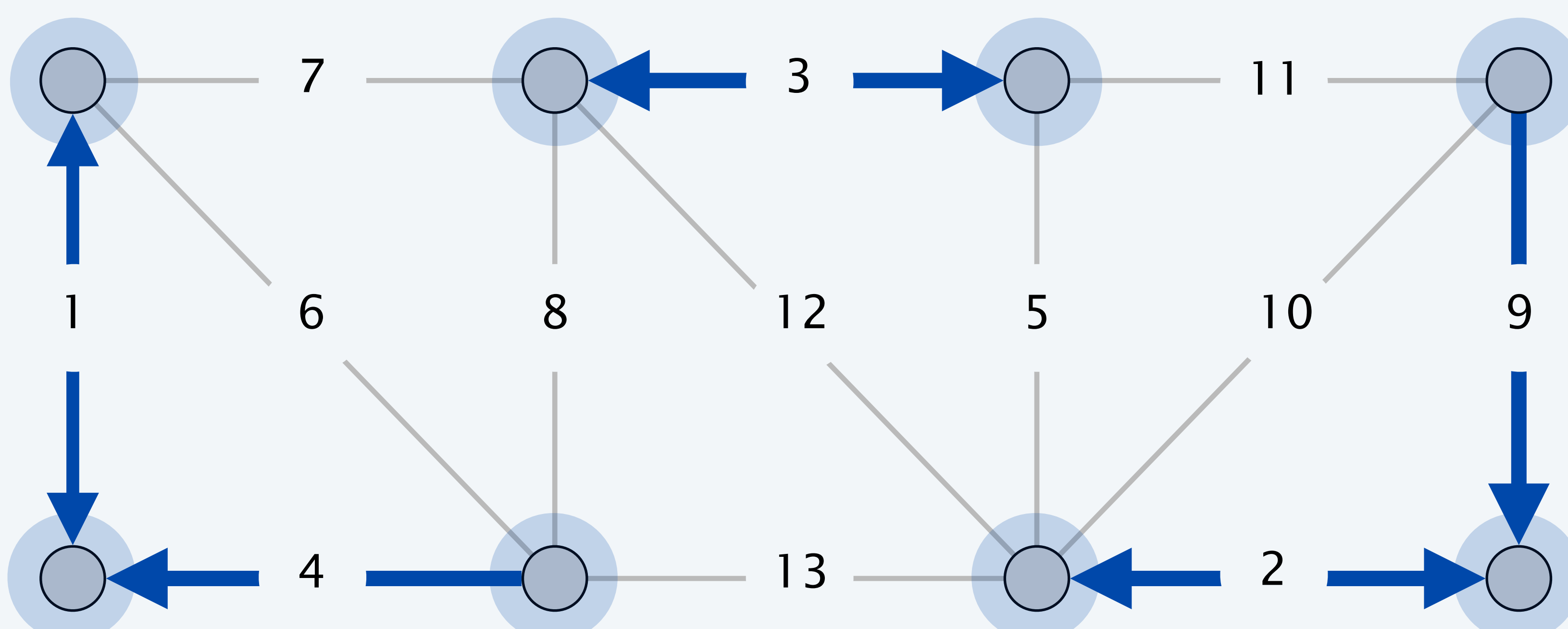

Borůvka's algorithm demo

Repeat until only one tree.

- Apply blue rule to cutset corresponding to each blue tree.
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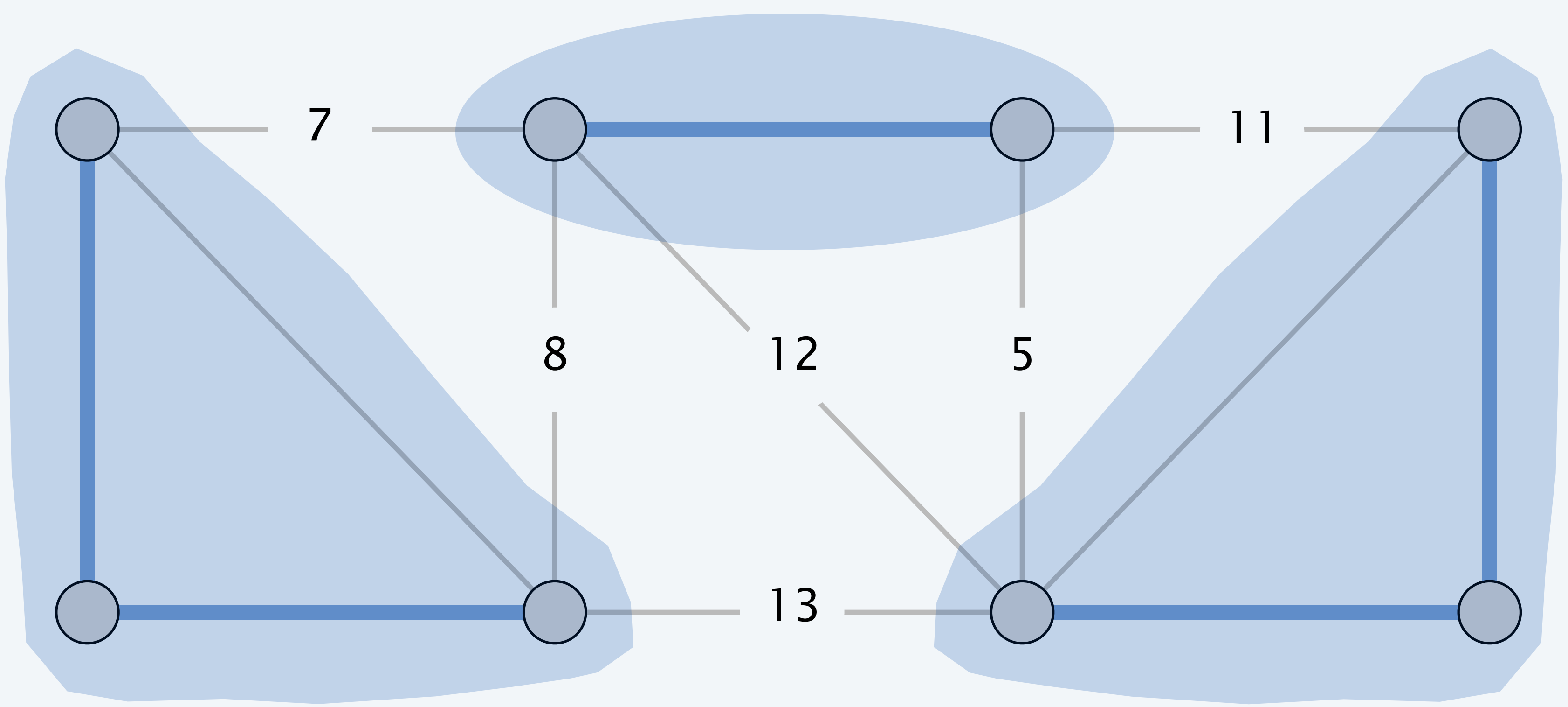
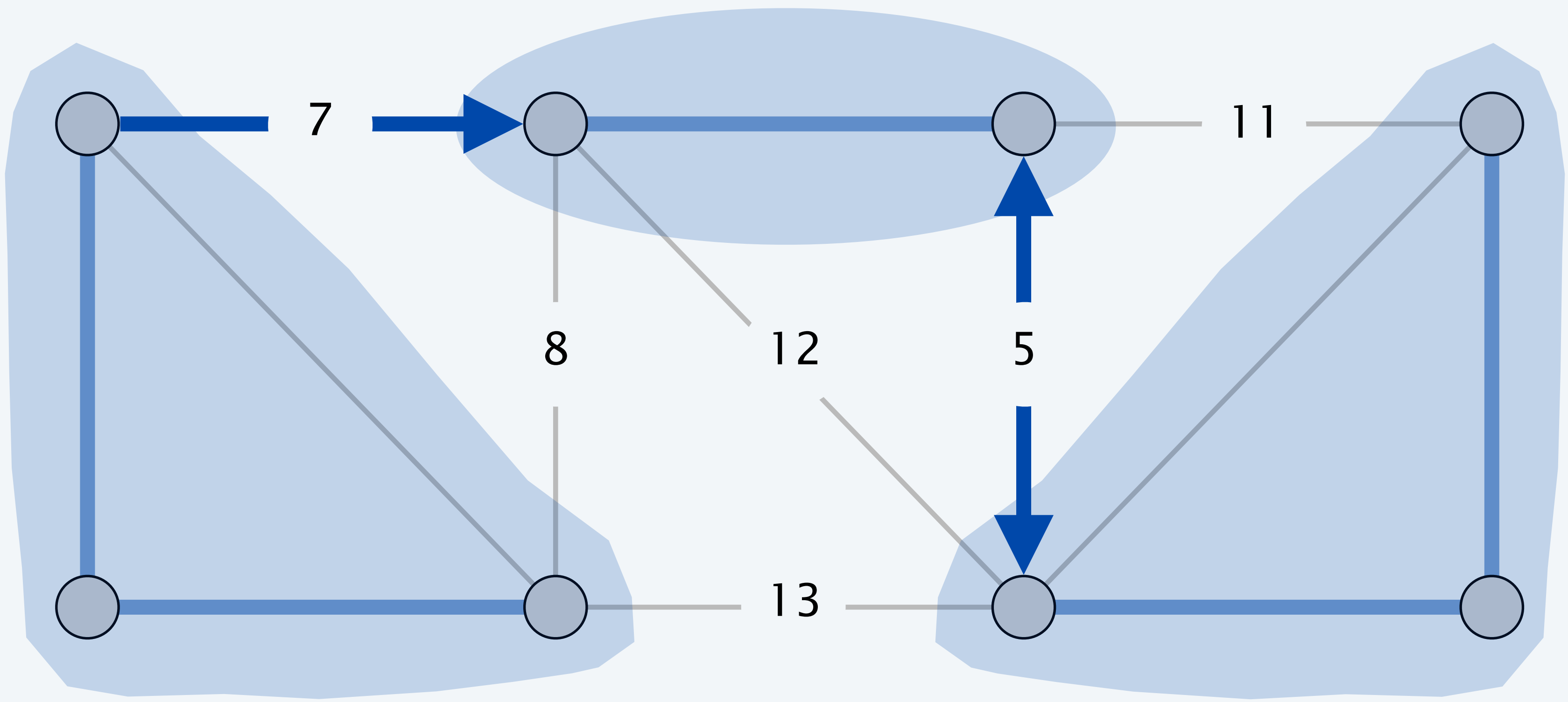


Borůvka's algorithm demo

Repeat until only one tree.

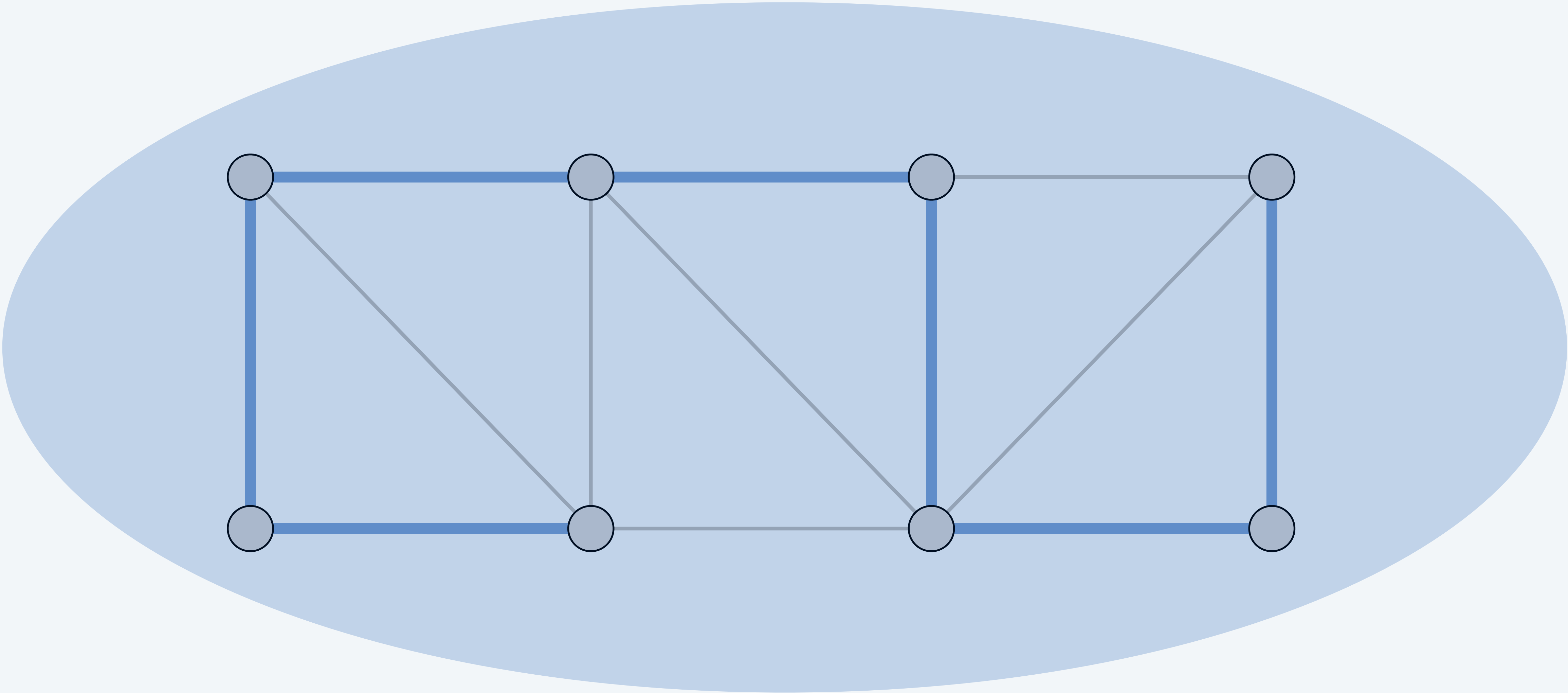
- Apply blue rule to cutset corresponding to each blue tree.
- Color all selected edges blue.



Borůvka's algorithm demo

Repeat until only one tree.

- Apply blue rule to cutset corresponding to each blue tree.
- Color all selected edges blue.



Borůvka's algorithm demo

Repeat until only one tree.

- Apply blue rule to cutset corresponding to each blue tree.
- Color all selected edges blue.