Topic 12: Acyclic Instruction Scheduling

COS 320

Compiling Techniques

Princeton University Spring 2018

Prof. David August

Scheduling

Multiply instruction takes 2 cycles...

```
r1 = r0 + 0
                                  r1 = r0 + 0
   r2 = M[FP + A]
                                  r2 = M[FP + A]
   r3 = r0 + 4
                                  r3 = r0 + 4
   r4 = M[FP + X]
                                   r4 = M[FP + X]
 LOOP:
                                 LOOP:
    r5 = r3 * r1
                                  r5 = r3 * r1
2
                                  r1 = r1 + 1
    r5 = r2 + r5
                                  r5 = r2 + r5
                              3
   M[r5] = r4
                                  M[r5] = r4
    r1 = r1 + 1
                                  BR r1 <= 10, LOOP
   BR r1 <= 10, LOOP
```

Optimization Register Allocation Scheduling Control Flow Analysis Dataflow Analysis

The Back End:

- Maps infinite number of virtual registers to finite number of real registers → register allocation
- 2. Removes inefficiencies introduced by front-end \rightarrow optimizer
- 3. Removes inefficiencies introduced by programmer \rightarrow optimizer
- Adjusts pseudo-assembly composition and order to match target machine → scheduler

Scheduling

Multiply instruction takes 2 cycles...

Machine executes 2 instructions per cycle...

```
r1 = r0 + 0
  r2 = M[FP + A]
                          r1 = r0 + 0
                                        r2 = M[FP + A]
                          r3 = r0 + 4
  r3 = r0 + 4
                                        r4 = M[FP + X]
  r4 = M[FP + X]
LOOP:
                        LOOP:
  r5 = r3 * r1
                          r5 = r3 * r1   r1 = r1 + 1
  r1 = r1 + 1
  r5 = r2 + r5
                          r5 = r2 + r5
  M[r5] = r4
                          M[r5] = r4
                                        BR r1 <= 10, LOOP
 BR r1 <= 10, LOOP
```

Instruction Level Parallelism

- Instruction-Level Parallelism (ILP), the concurrent execution of independent assembly instructions.
- ILP is a cost effective way to extract performance from programs.
- Exploiting ILP requires global optimization and scheduling.
- Processors are becoming increasingly dependent on the ability of compilers to expose ILP.
 - Current state-of-the-art machines can execute 3 to 6 instructions per cycle if available. (i.e. Pentium III, DEC Alpha 21264)
 - Some processors rely on compiler for guidance. (i.e. Itanium)
- Current state-of-the-art compilers cannot expose this level of ILP in integer programs.

Data Dependence

$$r1 = r2 + r3$$

Branch r1 <= 10, TRUE

r4 = r2 * r5

r5 = r4 + 1

TRUE:

$$r4 = r5 - 1$$

Data Dependence

- A *data dependence* is a constraint on scheduling arising from the flow of data between two instructions. Types:
 - RAW: An instruction u is *flow-dependent* on a preceding instruction d if u consumes a value computed by d.
 - WAR: An instruction d is *anti-dependent* on a preceding instruction u if d writes to a location read by u.
 - WAW: An instruction d_2 is *output-dependent* on a preceding instruction d_1 if d_1 writes to a location also written by d_2 .
- Types of data:
 - Register dependence
 - Memory dependence

False Dependence

Eliminate WAW dependences

r1 =

branch

r1 =

= r1

Eliminate WAR dependences

= r1 r1 =

= r1

- Eliminate RAW dependences?
- Register allocation vs. splitting live ranges

Control Dependence

• A *control dependence* is a constraint on scheduling arising from the control flow of the program.

```
Branch r1 <= 10, TARGET1

Branch r2 <= 10, TARGET2

r4 = r3 + 5

TARGET1:

r5 = r4 - 1

TARGET2: (Assume: r4 not live here)
```

Dependences

Latency

- Amount of time after the execution of an instruction that its result is ready.
- An instruction can have more than one latency!

Data Dependence Graph

- A *data dependence graph* consists of instructions and a set of directed data dependence edges among them in which each edge is labeled with its latency and type of dependence.
- Scheduling (code motion) must respect dependence graph.

Control Dependences

Sources of Control Dependence

- Liveness
- Side-effects
 - Potentially Excepting Instructions (PEIs)
 - Memory Writes
 - Input/Output

Resources

- What does "two instructions per cycle" mean?
- *Resource* A function of the processor that can be used by only one instruction at a time.
- Examples:
 - Fetch units
 - Decode units
 - Execution units
 - Register ports

Pipelining

Scheduling

- The goal of *scheduling* is to construct a sort of the dependence graph that:
 - Produces the same result respects dependences
 - Minimizes execution time makes maximal use of machine resources
- Scheduling is NP-hard even with simple formulation of problem.
- Use Heuristics to approximate solution.
- In practice, is exhaustive search of all schedules practical in most cases?

Heuristic: List Scheduling

Resource Map

- ullet List scheduling, the most common heuristic, is $O(n_2)$.
- Create *ready queue* to hold *ready* instructions.
- An instruction is *ready* when all incoming dependences are satisfied.
- A dependence is satisfied when source of dependence are has been scheduled at least latency cycles earlier.

List Scheduling

```
build dependence graph
insert instructions with no incoming dependences into ready queue
WHILE (instruction are not scheduled) DO
current_cycle_sched = FALSE
FOREACH instruction i in ready queue DO
IF (resources exist to schedule i in cycle) THEN
schedule i, update ready queue
current_cycle_sched = TRUE
IF (NOT current_cycle_sched) THEN
cycle++
update ready queue
```

List Scheduling Priority

List Scheduling

Hardware Scheduling

Machines can also do scheduling...

- hardware schedulers process code after it has been fetched
- hardware finds independent instructions
- works with legacy architectures (found in x86; Pentium)
- program knowledge more precise at run-time memory dependence

But compiler still important.

- Hardware schedulers have a small window.
- Hardware complexity increases.
- Hardware does not benefit directly from compiler optimization.

Expression Reformulation

Loop Unrolling

$$0 r1 = 0 r2 = 0$$

$$r2 = 0$$

Loop:

$$0 r3 = M[r1 + A] r1 = r1 + 1$$

$$r1 = r1 + 1$$

1

2
$$r2 = r2 + r3$$
 BR $r1 \le 30$, Loop

BR
$$r1 < 30$$
. Loop

Renaming

$$0 r1 = 0 r2 = 0$$

Loop:

$$0 r3 = M[r1 + A] r1 = r1 + 1$$

$$r1 = r1 + 1$$

1

$$2 r2 = r2 + r3$$

$$3 \quad r3 = M[r1 + A] \quad r1 = r1 + 1$$

$$r1 = r1 + 1$$

4

$$5 r2 = r2 + r2$$

$$r2 = r2 + r3$$
 BR $r1 < 30$, Loop

Accumulator Expansion

$$0 r1 = 0 r2 = 0$$

$$r2 = 0$$

Loop:

$$0 r3 = M[r1 + A] r1 = r1 + 1$$

$$r1 = r1 + 1$$

$$1 r4 = M[r1 + A] r1 = r1 + 1$$

$$r1 = r1 + 1$$

$$2 r2 = r2 + r3$$

$$3 r2 = r2 + r4$$

$$3 r2 = r2 + r4 BR r1 < 30, Loop$$

Accumulator Expansion

0 r1 = 0r2 = 0Loop:

$$0 r3 = M[r1 + A] r1 = r1 + 1$$

$$1 r4 = M[r1 + A] r1 = r1 + 1$$

$$2 r5 = M[r1 + A] r1 = r1 + 1 r2 = r2 + r3$$

$$3 r2 = r2 + r4$$

$$4 r2 = r2 + r5 BR r1 < 30, Loop$$

Loop Unrolling and Optimization

$$0$$
 $r13 = 0$ $r14 = 1$
 1 $r15 = 2$ $r23 = 0$
 2 $r24 = 0$ $r25 = 0$

Loop:

1

0
$$r3 = M[r13 + A]$$
 $r13 = r13 + 3$ $r4 = M[r14 + A]$
 $r14 = r14 + 3$ $r5 = M[r15 + A]$ $r15 = r15 + 3$

2
$$r23 = r23 + r3$$
 $r24 = r24 + r4$ $r25 = r25 + r5$ BR r13 < 30, Loop

$$0$$
 $r2 = r23 + r24$
 1 $r2 = r2 + r25$

Induction Variable Elimination

Pipelining

0 r2 = r23 + r241 r2 = r2 + r25