
Topic 14: Parallelism

COS 320

Compiling Techniques

Princeton University
Spring 2015

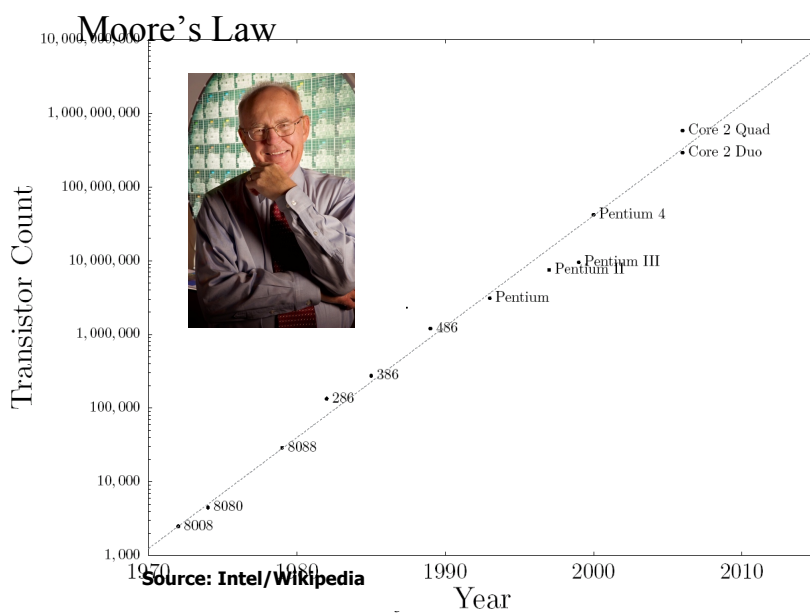
Prof. David August

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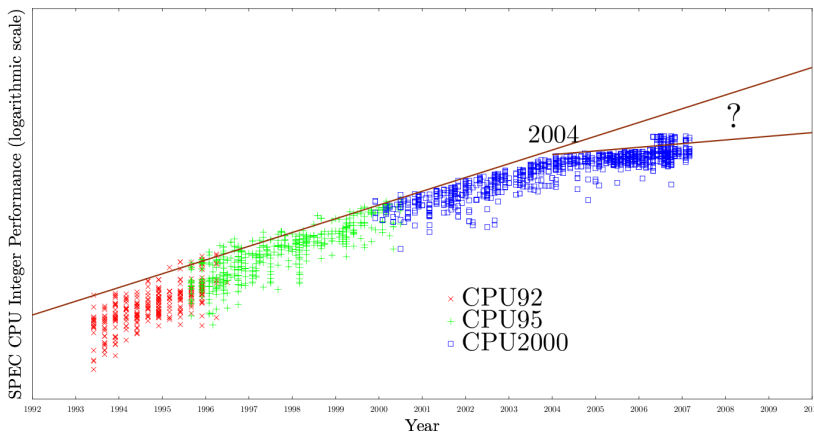
Final Exam!

- Friday May 22 at 1:30PM in FRIEND 006
- Closed book
- One Front/Back 8.5x11

2



Single-Threaded Performance Not Improving



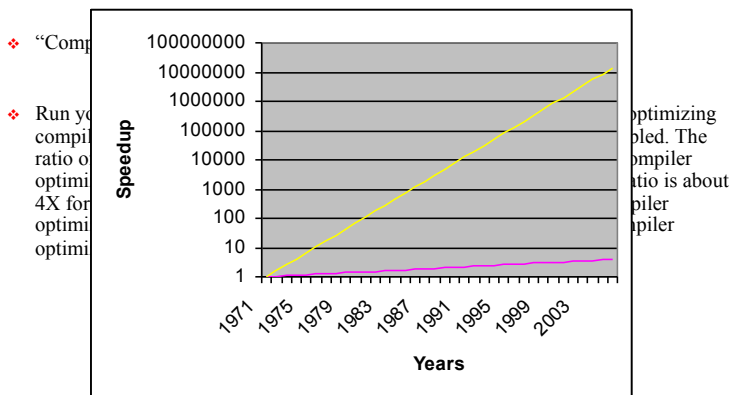
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What about Parallel Programming? –or- What is Good About the Sequential Model?

- ❖ Sequential is easier
 - » People think about programs sequentially
 - » Simpler to write a sequential program
- ❖ Deterministic execution
 - » Reproducing errors for debugging
 - » Testing for correctness
- ❖ No concurrency bugs
 - » Deadlock, livelock, atomicity violations
 - » Locks are not composable
- ❖ Performance extraction
 - » Sequential programs are portable
 - » Are parallel programs? Ask GPU developers ☺
 - » Performance debugging of sequential programs straight-forward

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Compilers are the Answer? - Proebsting's Law



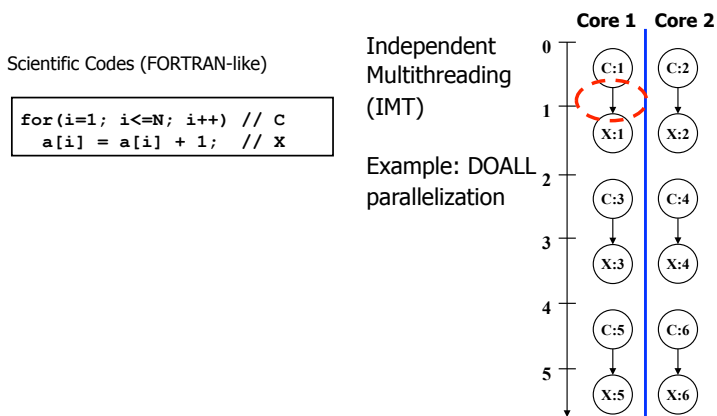
Conclusion – Compilers not about performance!

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Are We Doomed?

A Step Back in Time: Old Skool Parallelization

Parallelizing Loops In Scientific Applications



What Information is Needed to Parallelize?

- ❖ Dependences within iterations are fine
- ❖ Identify the presence of cross-iteration data-dependences
 - » Traditional analysis is inadequate for parallelization. For instance, it does not distinguish between different executions of the same statement in a loop.
- ❖ Array dependence analysis enables optimization for parallelism in programs involving arrays.
 - » Determine pairs of iterations where there is a data dependence
 - » Want to know all dependences, not just yes/no

```
for(i=1; i<=N; i++) // C
a[i] = a[i] + 1; // X
```

```
for(i=1; i<=N; i++) // C
a[i] = a[i-1] + 1; // X
```

Affine/Linear Functions

- ❖ $f(i_1, i_2, \dots, i_n)$ is affine, if it can be expressed as a sum of a constant, plus constant multiples of the variables. i.e.

$$f = c_0 + \sum_{i=1}^n c_i x_i$$

- ❖ Array subscript expressions are usually affine functions involving loop induction variables.

❖ Examples:

- » $a[i]$ affine
- » $a[i+j-1]$ affine
- » $a[i*j]$ non-linear, not affine
- » $a[2*i+1, i*j]$ linear/non-linear, not affine
- » $a[b[i]+1]$ non linear (indexed subscript), not affine

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Array Dependence Analysis

```
for (i = 1; i < 10; i++) {  
  X[i] = X[i-1]  
}
```

To find all the data dependences, we check if

1. $X[i-1]$ and $X[i]$ refer to the same location;
 2. different instances of $X[i]$ refer to the same location.
- » For 1, we solve for i and i' in
 $1 \leq i \leq 10, 1 \leq i' \leq 10$ and $i-1 = i'$
 - » For 2, we solve for i and i' in
 $1 \leq i \leq 10, 1 \leq i' \leq 10, i = i'$ and $i \neq i'$ (between different dynamic accesses)

There is a dependence since there exist integer solutions to 1. e.g. ($i=2, i'=1$), ($i=3, i'=2$). 9 solutions exist.

There is no dependences among different instances of $X[i]$ because 2 has no solutions!

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Array Dependence Analysis - Summary

- ❖ Array data dependence basically requires finding integer solutions to a system (often refers to as dependence system) consisting of equalities and inequalities.
- ❖ Equalities are derived from array accesses.
- ❖ Inequalities from the loop bounds.
- ❖ It is an integer linear programming problem.
- ❖ ILP is an NP-Complete problem.
- ❖ Several Heuristics have been developed.
 - » Omega – U. Maryland

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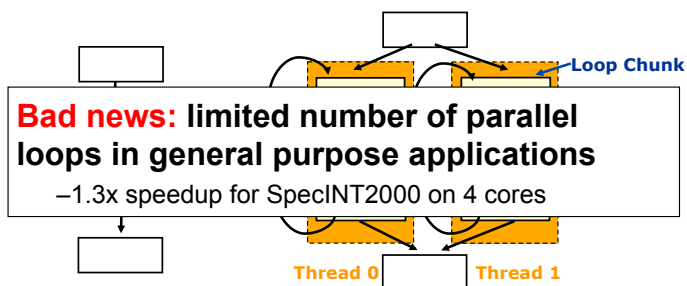
Loop Parallelization Using Affine Analysis Is Proven Technology

- ❖ DOALL Loop
 - » No loop carried dependences for a particular nest
 - » Loop interchange to move parallel loops to outer scopes
 - ❖ Other forms of parallelization possible
 - » DOAcross, DOpipeline
 - ❖ Optimizing for the memory hierarchy
 - » Tiling, skewing, etc.
 - ❖ Real compilers available – KAP, Portland Group, gcc
 - ❖ For better information, see
 - » http://gcc.gnu.org/wiki/Graphite?action=AttachFile&do=get&target=graphite_lambda_tutorial.pdf
-

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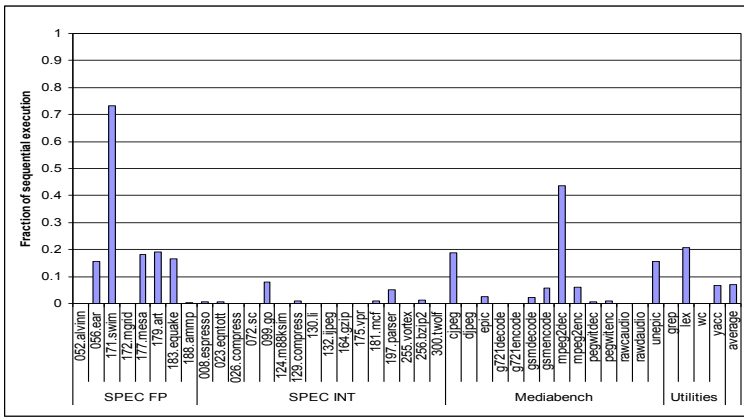
Back to the Present – Parallelizing C and C++ Programs

Loop Level Parallelization



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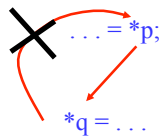
DOALL Loop Coverage



What's the Problem?

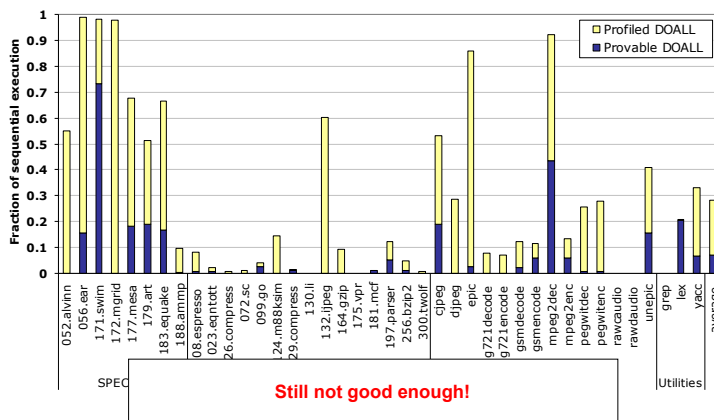
1. Memory dependence analysis

```
for (i=0; i<100; i++) {
```



Memory dependence profiling and speculative parallelization

DOALL Coverage – Provable and Profiled



What's the Next Problem?

2. Data dependences

```
while (ptr != NULL) {
```

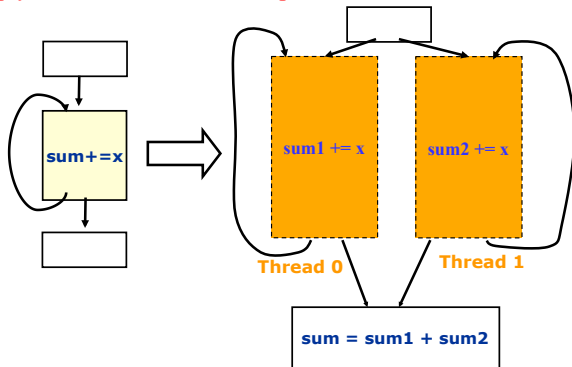
```
    ...  
    ptr = ptr->next;  
    sum = sum + foo;  
}
```

➡ Compiler transformations

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We Know How to Break Some of These Dependences – Recall ILP Optimizations

Apply accumulator variable expansion!



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Data Dependences Inhibit Parallelization

- ❖ Accumulator, induction, and min/max expansion only capture a small set of dependences
- ❖ 2 options
 - » 1) Break more dependences – New transformations
 - » 2) Parallelize in the presence of dependences – more than DOALL parallelization
- ❖ We will talk about both, but for now ignore this issue

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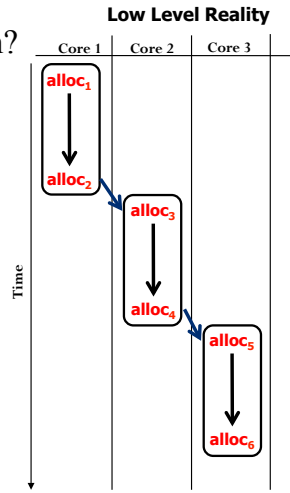
What's the Next Problem?

3. C/C++ too restrictive

```
char *memory;

void * alloc(int size);

void * alloc(int size) {
    void * ptr = memory;
    memory = memory + size;
    return ptr;
}
```

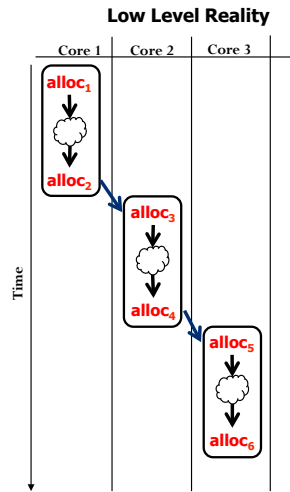


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```
char *memory;

void * alloc(int size);

void * alloc(int size) {
    void * ptr = memory;
    memory = memory + size;
    return ptr;
}
```



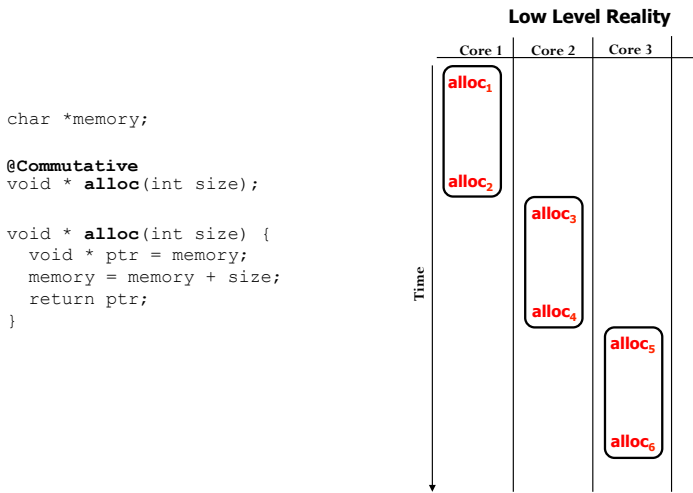
Loops cannot be parallelized even if computation is independent

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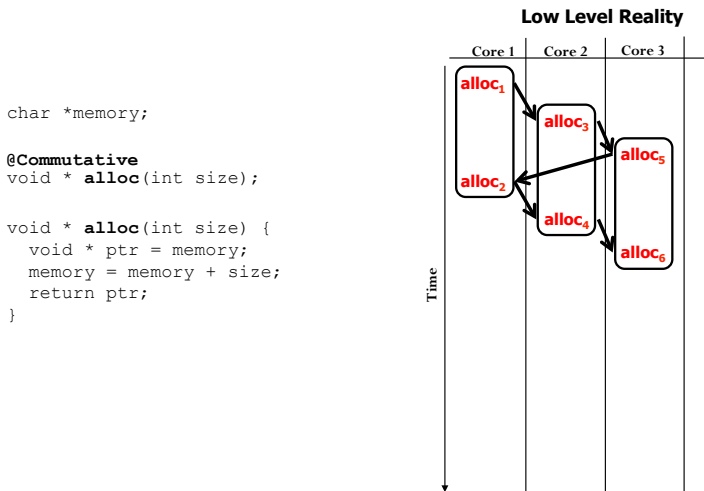
Commutative Extension

- ❖ Interchangeable call sites
 - » Programmer doesn't care about the order that a particular function is called
 - » Multiple different orders are all defined as correct
 - » Impossible to express in C
- ❖ Prime example is memory allocation routine
 - » Programmer does not care which address is returned on each call, just that the proper space is provided
- ❖ Enables compiler to break dependences that flow from 1 invocation to next forcing sequential behavior

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Implementation dependences should not cause serialization.

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What is the Next Problem?

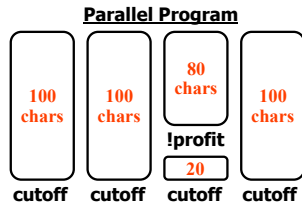
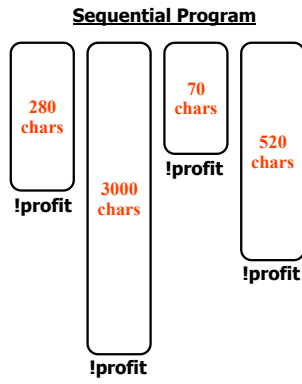
- ❖ 4. **C does not allow any prescribed non-determinism**
 - » Thus sequential semantics must be assumed even though they not necessary
 - » Restricts parallelism (useless dependences)
 - ❖ Non-deterministic branch → programmer does not care about individual outcomes
 - » They attach a probability to control how statistically often the branch should take
 - » Allow compiler to tradeoff 'quality' (e.g., compression rates) for performance
- Ÿ When to create a new dictionary in a compression scheme

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```

#define CUTOFF 100
dict = create_dict();
count = 0;
while((char = read(1))) {
    if(!profitable) {
        compress(char, dict);
        if (!profitable) {
            if(dictprefreset(dict);
            } dict=restart(dict);
        } if (count == CUTOFF){
            finish_dict(dict);
            count=0;
        }
        count++;
    }
}
finish_dict(dict);

```



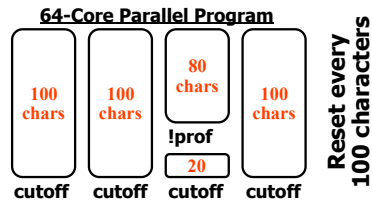
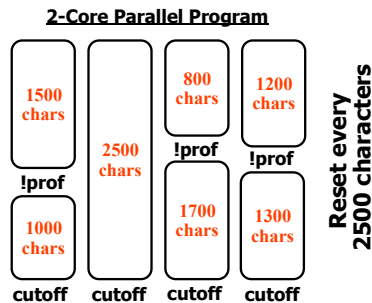
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```

dict = create_dict();
while((char = read(1))) {
    profitable =
        compress(char, dict)

    @YBRANCH(probability=.01)
    if (!profitable) {
        dict = restart(dict);
    }
}
finish_dict(dict);

```



Compilers are best situated to make the tradeoff between output quality and performance

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Capturing Output/Performance Tradeoff: Y-Branches in 164.gzip

```

dict = create_dict();
while((char = read(1))) {
    profitable =
        compress(char, dict)

    @YBRANCH(probability=.00001)
    if(dictprefreset(dict);
    } dict = restart(dict);
} }
finish_dict(dict);
finish_dict(dict);

```

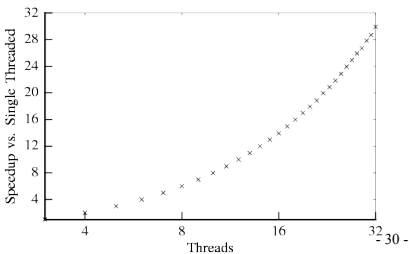
```

#define CUTOFF 100000
dict = create_dict();
count = 0;
while((char = read(1))) {
    profitable =
        compress(char, dict)

    if (!profitable)
        dict=restart(dict);
    if (count == CUTOFF){
        dict=restart(dict);
        count=0;
    }

    count++;
}
finish_dict(dict);

```



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256.bzip2

```

unsigned char *block;
int last_written;

compressStream(in, out) {
  while (True) {
    loadAndRLEsource(in);
    if (!last) break;
    doReversibleTransform();
    sendMTFValues(out);
  }
}

doReversibleTransform() {
  sortIt();
  ..
}

sortIt() {
  printf(...);
  ..
}

```

Parallelization techniques must look inside function calls to expose operations that cause synchronization.

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197.parser

```

batch_process() {
  while(True) {
    sentence = read();
    if (!sentence) break;
    parse(sentence);
    print(sentence);
  }
}

char *memory;

void *xalloc(int size) {
  void *ptr = memory;
  memory = memory + size;
  return ptr;
}

```

High-Level View:

Parsing a sentence is independent of any other sentence.

Low-Level Reality:

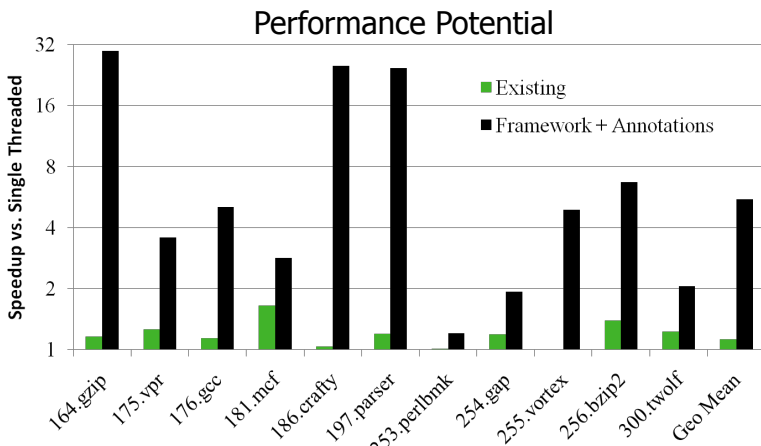
Implementation dependences inside functions called by **parse** lead to large sequential regions.

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	LoC Changed	Increased Scope	Commutative	Y-Branch	Nested Parallel	Iter. Inv. Value Spec.	Loop Alias Spec.	Programmer Mod.
164.gzip	26	x		x				x
175.vpr	1		x			x	x	
176.gcc	18	x	x				x	x
181.mcf	0				x			
186.crafty	9	x	x		x	x	x	
197.parser	3	x	x					
253.perlbnk	0	x				x	x	
254.gap	3	x	x				x	
255.vortex	0	x				x	x	
256.bzip2	0	x					x	
300.twolf	1	x	x				x	

Modified only 60 LOC out of ~500,000 LOC

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What prevents the automatic extraction of parallelism?

~~Lack of an Aggressive Compilation Framework~~

~~Sequential Programming Model~~

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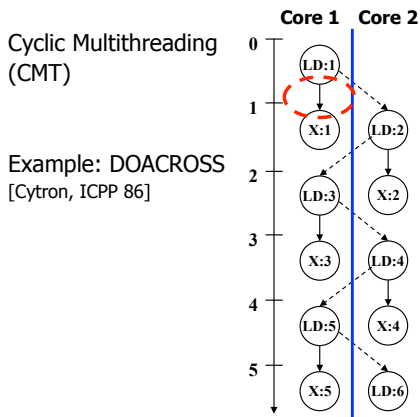
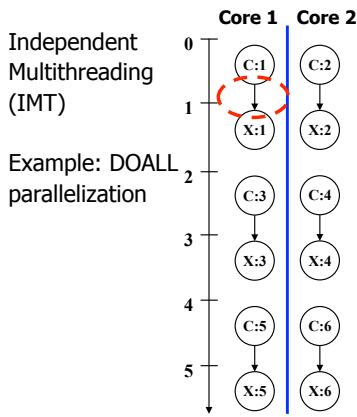
What About Non-Scientific Codes???

Scientific Codes (FORTRAN-like)

```
for (i=1; i<=N; i++) // C
  a[i] = a[i] + 1; // X
```

General-purpose Codes (legacy C/C++)

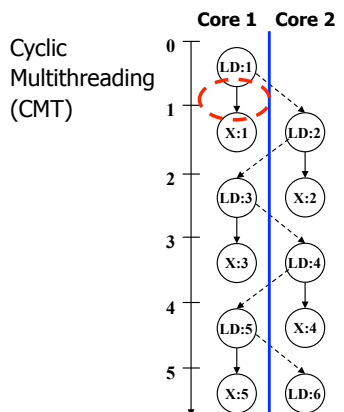
```
while (ptr = ptr->next) // LD
  ptr->val = ptr->val + 1; // X
```



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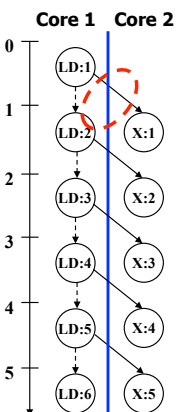
Alternative Parallelization Approaches

```
while (ptr = ptr->next) // LD
  ptr->val = ptr->val + 1; // X
```



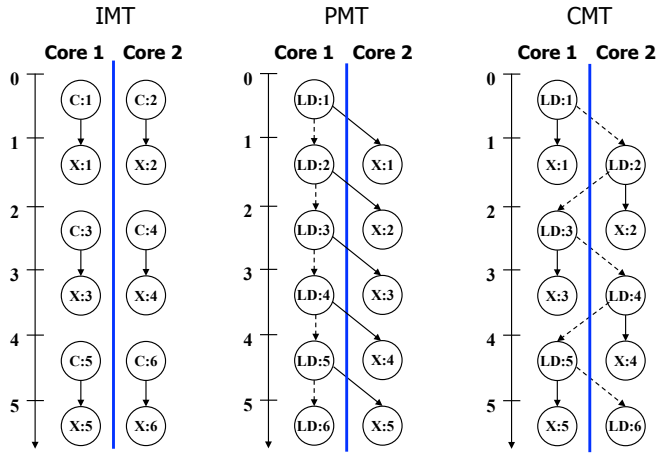
Pipelined Multithreading (PMT)

Example: DSWP [PACT 2004]



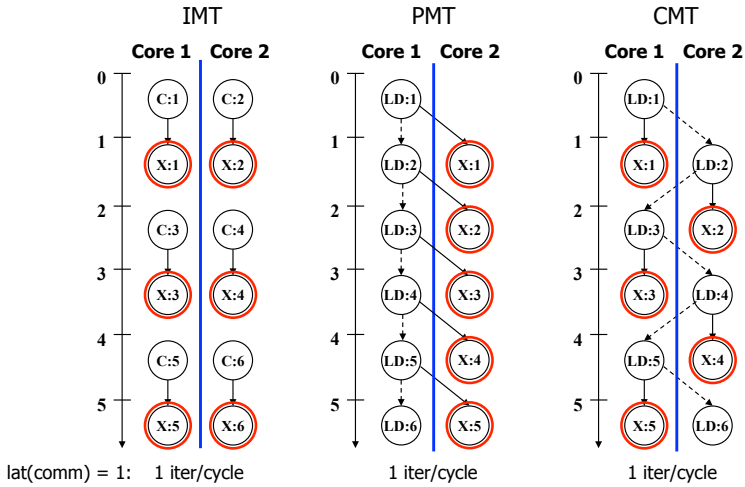
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Comparison: IMT, PMT, CMT



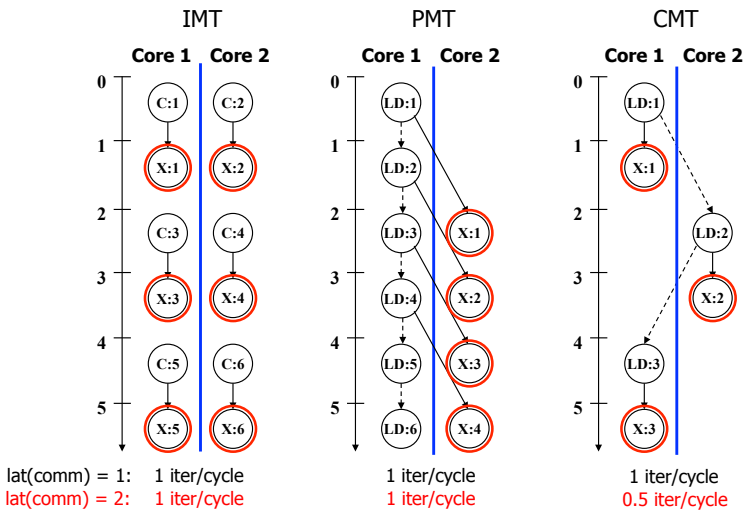
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Comparison: IMT, PMT, CMT



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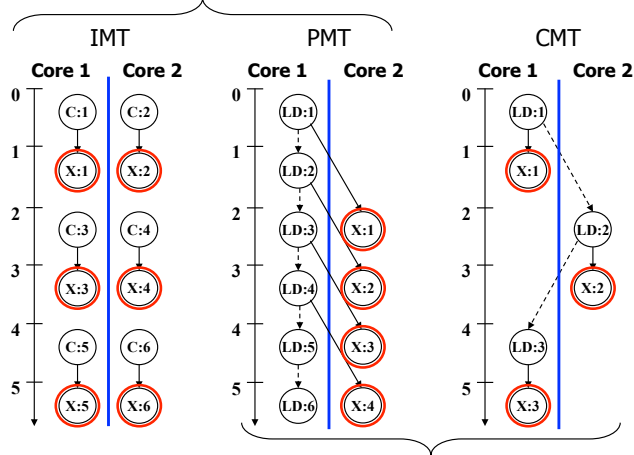
Comparison: IMT, PMT, CMT



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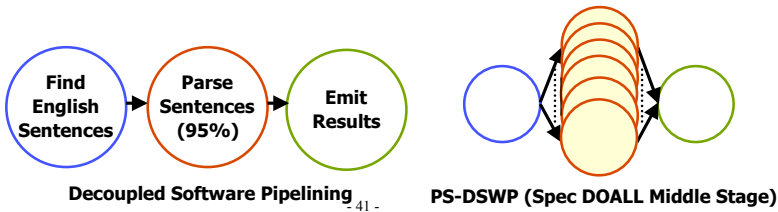
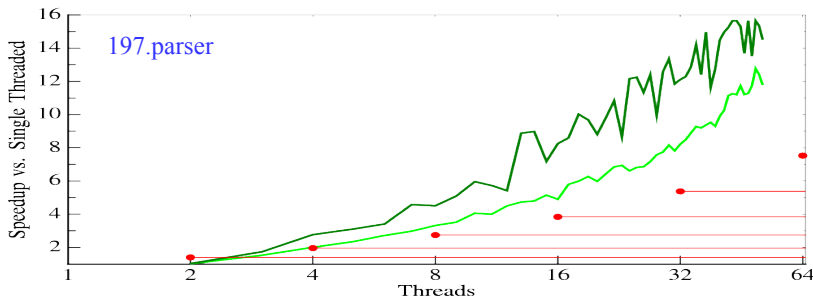
Comparison: IMT, PMT, CMT

Thread-local Recurrences → Fast Execution



Cross-thread Dependences → Wide Applicability

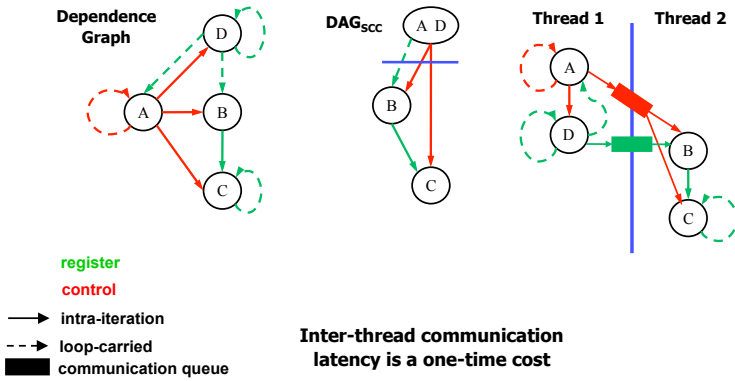
Our Objective: Automatic Extraction of Pipeline Parallelism using DSWP



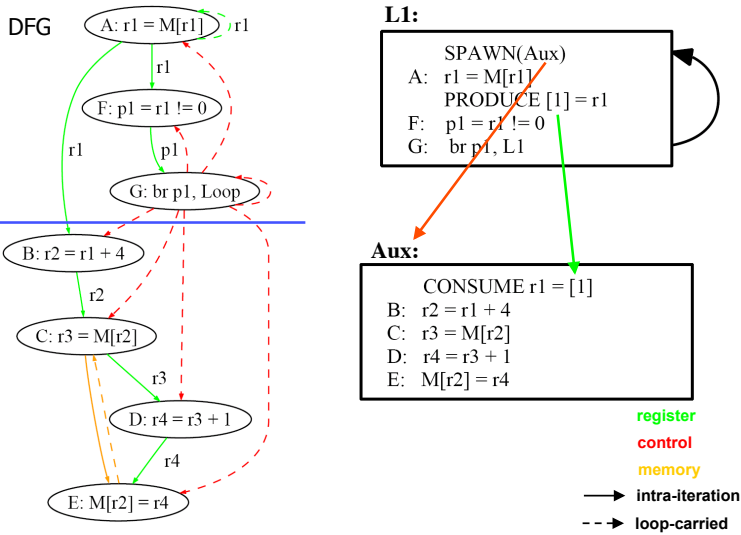
Decoupled Software Pipelining

```

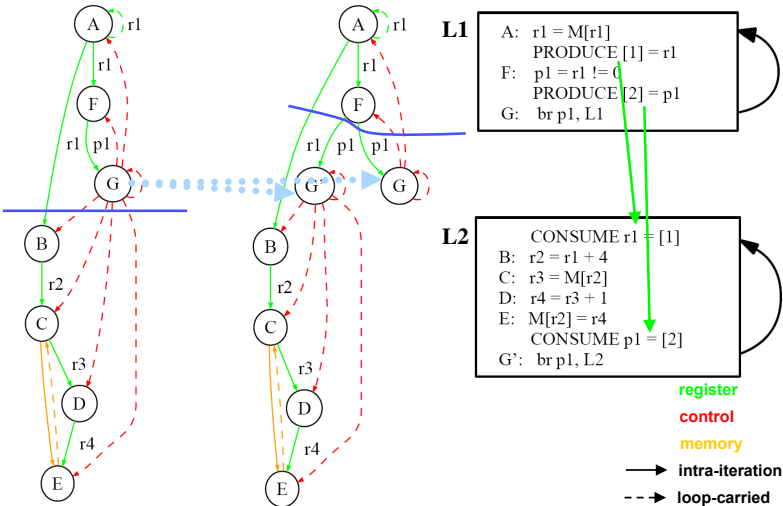
A: while (node)
B:   ncost = doit(node);
C:   cost += ncost;
D:   node = node->next;
    
```



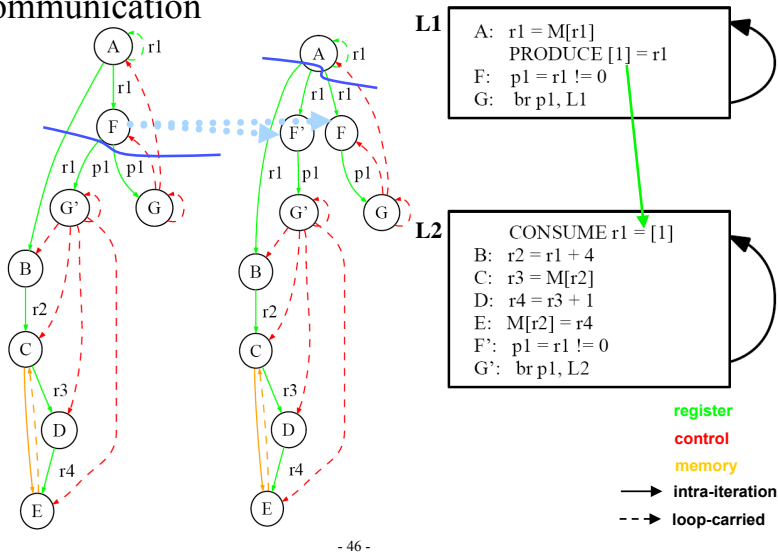
Implementing DSWP



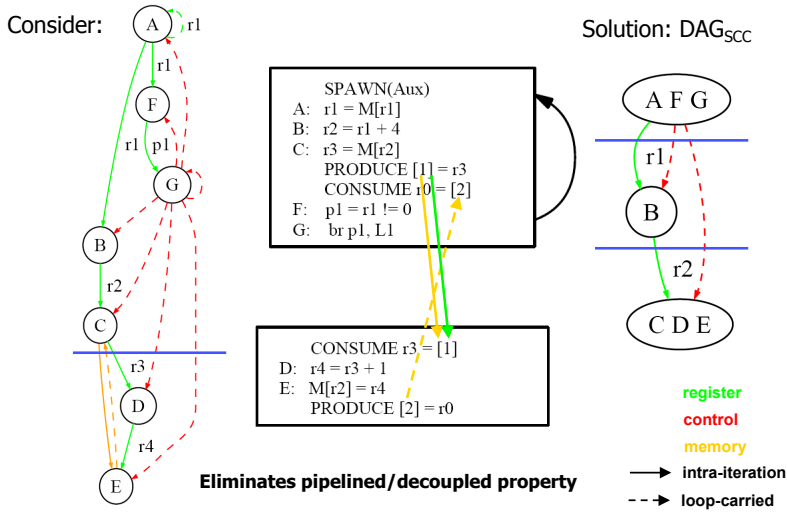
Optimization: Node Splitting To Eliminate Cross Thread Control



Optimization: Node Splitting To Reduce Communication



Constraint: Strongly Connected Components



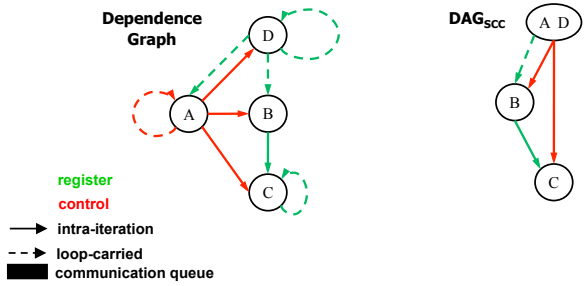
2 Extensions to the Basic Transformation

- ❖ Speculation
 - » Break statistically unlikely dependences
 - » Form better-balanced pipelines
- ❖ Parallel Stages
 - » Execute multiple copies of certain “large” stages
 - » Stages that contain inner loops perfect candidates

Why Speculation?

```

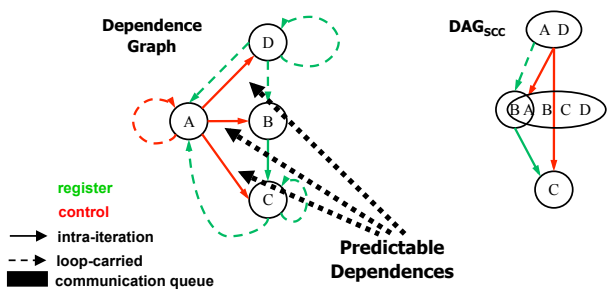
A: while (node)
B:   ncost = doit(node);
C:   cost += ncost;
D:   node = node->next;
    
```



Why Speculation?

```

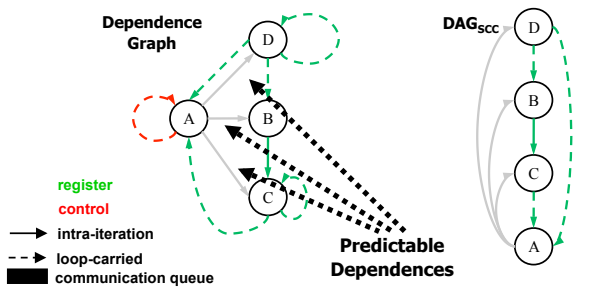
A: while (cost < T && node)
B:   ncost = doit(node);
C:   cost += ncost;
D:   node = node->next;
    
```



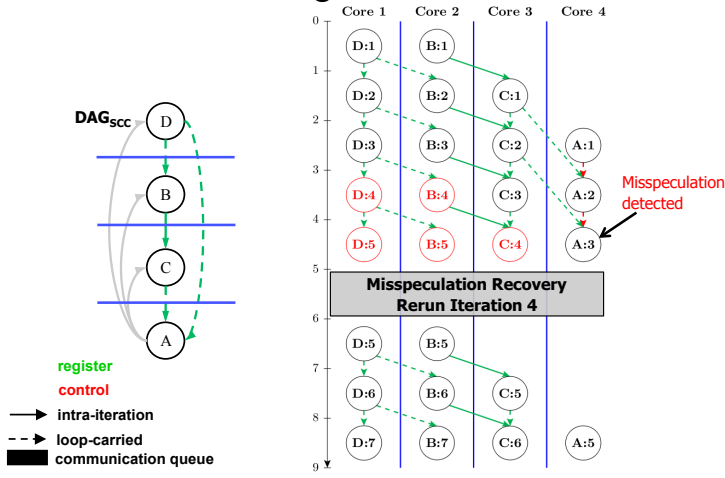
Why Speculation?

```

A: while (cost < T && node)
B:   ncost = doit(node);
C:   cost += ncost;
D:   node = node->next;
    
```

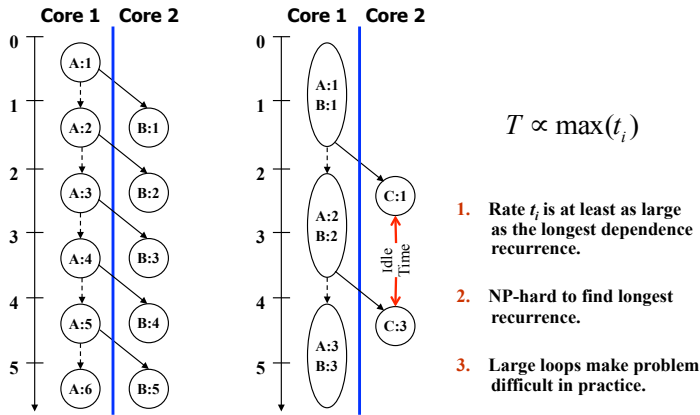


Execution Paradigm



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Understanding PMT Performance



Slowest thread: 1 cycle/iter
 Iteration Rate: 1 iter/cycle

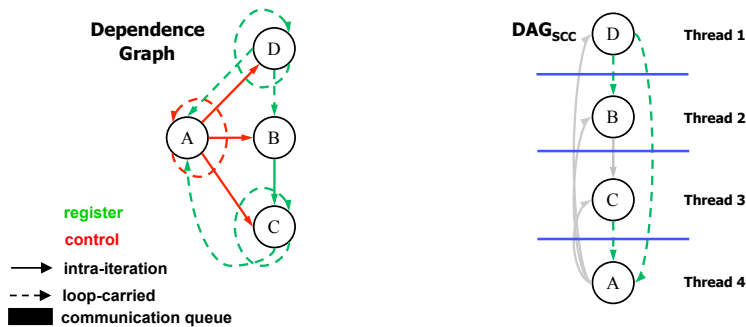
2 cycle/iter
 0.5 iter/cycle

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Selecting Dependences To Speculate

```

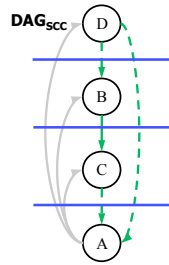
A: while(cost < T && node)
B:   ncost = doit(node);
C:   cost += ncost;
D:   node = node->next;
    
```



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Detecting Misspeculation

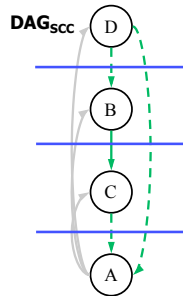
Thread 1	A ¹ : while (consume(4)) D : node = node->next produce({0,1},node);
Thread 2	A ² : while (consume(5)) B : ncost = doit(node); produce(2,ncost); D ² : node = consume(0);
Thread 3	A ³ : while (consume(6)) B ³ : ncost = consume(2); C : cost += ncost; produce(3,cost);
Thread 4	A : while (cost < T && node) B ⁴ : cost = consume(3); C ⁴ : node = consume(1); produce({4,5,6},cost < T && node);



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Detecting Misspeculation

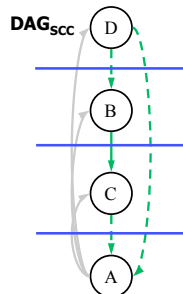
Thread 1	A ¹ : while (TRUE) D : node = node->next produce({0,1},node);
Thread 2	A ² : while (TRUE) B : ncost = doit(node); produce(2,ncost); D ² : node = consume(0);
Thread 3	A ³ : while (TRUE) B ³ : ncost = consume(2); C : cost += ncost; produce(3,cost);
Thread 4	A : while (cost < T && node) B ⁴ : cost = consume(3); C ⁴ : node = consume(1); produce({4,5,6},cost < T && node);



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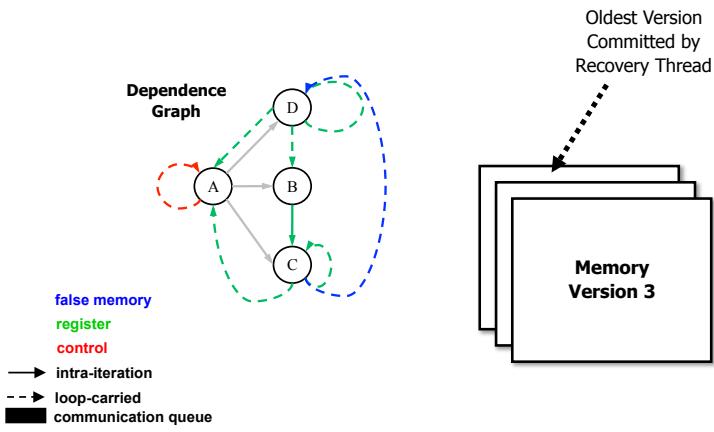
Detecting Misspeculation

Thread 1	A ¹ : while (TRUE) D : node = node->next produce({0,1},node);
Thread 2	A ² : while (TRUE) B : ncost = doit(node); produce(2,ncost); D ² : node = consume(0);
Thread 3	A ³ : while (TRUE) B ³ : ncost = consume(2); C : cost += ncost; produce(3,cost);
Thread 4	A : while (cost < T && node) B ⁴ : cost = consume(3); C ⁴ : node = consume(1); if (!(cost < T && node)) FLAG_MISSPEC();



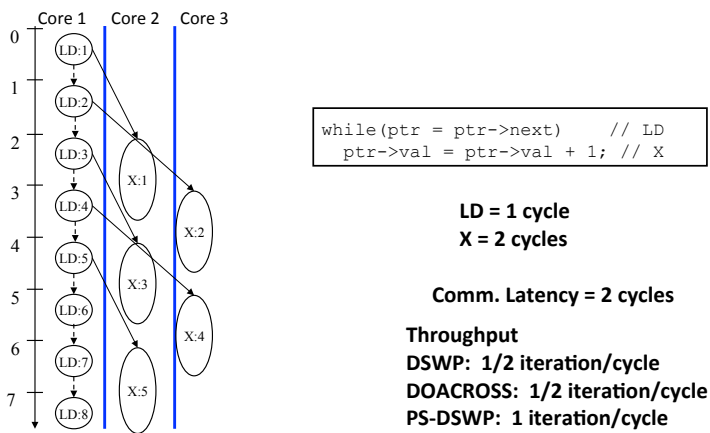
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Breaking False Memory Dependences



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Adding Parallel Stages to DSWP

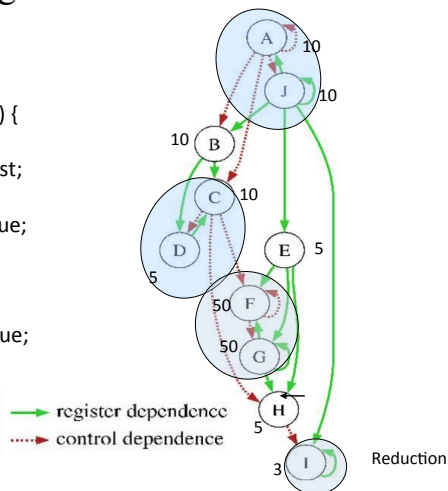


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Thread Partitioning

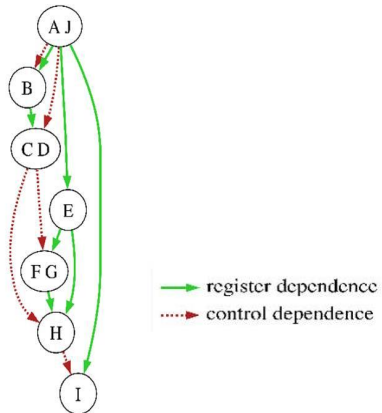
```

p = list;
sum = 0;
A: while (p != NULL) {
B:   id = p->id;
E:   q = p->inner_list;
C:   if (!visited[id]) {
D:     visited[id] = true;
F:     while (foo(q))
G:       q = q->next;
H:       if (q != NULL)
I:         sum += p->value;
      }
J:   p = p->next;
}
  
```

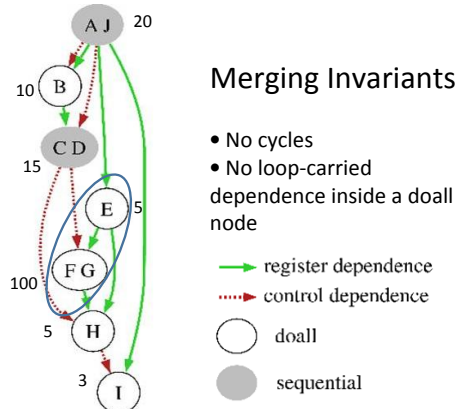


- 60 -

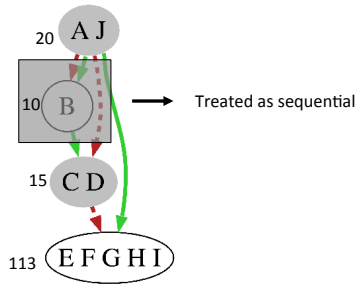
Thread Partitioning: DAG_{SCC}



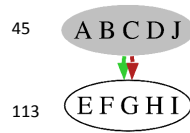
Thread Partitioning



Thread Partitioning



Thread Partitioning



- ❖ Modified MTCG[Ottoni, MICRO'05] to generate code from partition

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Discussion Point 1 – Speculation

- ❖ How do you decide what dependences to speculate?
 - » Look solely at profile data?
 - » How do you ensure enough profile coverage?
 - » What about code structure?
 - » What if you are wrong? Undo speculation decisions at run-time?
- ❖ How do you manage speculation in a pipeline?
 - » Traditional definition of a transaction is broken
 - » Transaction execution spread out across multiple cores

- 65 -

Discussion Point 2 – Pipeline Structure

- ❖ When is a pipeline a good/bad choice for parallelization?
- ❖ Is pipelining good or bad for cache performance?
 - » Is DOALL better/worse for cache?
- ❖ Can a pipeline be adjusted when the number of available cores increases/decreases?

- 66 -

CFGs, PCs, and Cross-Iteration Deps

1. $r1 = 10$

1. $r1 = r1 + 1$

2. $r2 = \text{MEM}[r1]$

3. $r2 = r2 + 1$

4. $\text{MEM}[r1] = r2$

5. Branch $r1 < 1000$

No register live outs

67

Loop-Level Parallelization: DOALL

1. $r1 = 10$

1. $r1 = r1 + 1$

2. $r2 = \text{MEM}[r1]$

3. $r2 = r2 + 1$

4. $\text{MEM}[r1] = r2$

5. Branch $r1 < 1000$

1. $r1 = 9$

1. $r1 = r1 + 2$

2. $r2 = \text{MEM}[r1]$

3. $r2 = r2 + 1$

4. $\text{MEM}[r1] = r2$

5. Branch $r1 < 999$

1. $r1 = 10$

1. $r1 = r1 + 2$

2. $r2 = \text{MEM}[r1]$

3. $r2 = r2 + 1$

4. $\text{MEM}[r1] = r2$

5. Branch $r1 < 1000$

No register live outs

68

Another Example

1. $r1 = 10$

1. $r1 = r1 + 1$

2. $r2 = \text{MEM}[r1]$

3. $r2 = r2 + 1$

4. $\text{MEM}[r1] = r2$

5. Branch $r2 == 10$

No register live outs

69

Another Example

1. r1 = 10	1. r1 = 9	1. r1 = 10
1. r1 = r1 + 1 2. r2 = MEM[r1] 3. r2 = r2 + 1 4. MEM[r1] = r2 5. Branch r2 == 10	1. r1 = r1 + 2 2. r2 = MEM[r1] 3. r2 = r2 + 1 4. MEM[r1] = r2 5. Branch r2 == 10	1. r1 = r1 + 2 2. r2 = MEM[r1] 3. r2 = r2 + 1 4. MEM[r1] = r2 5. Branch r2 == 10

No register live outs

70

Speculation

1. r1 = 9	1. r1 = 10
1. r1 = r1 + 2 2. r2 = MEM[r1] 3. r2 = r2 + 1 4. MEM[r1] = r2 5. Branch r2 == 10	1. r1 = r1 + 2 2. r2 = MEM[r1] 3. r2 = r2 + 1 4. MEM[r1] = r2 5. Branch r2 == 10

No register live outs

71

Speculation, Commit, and Recovery

1. r1 = 9	1. r2 = Receive{1} 2. Branch r2 != 10 3. MEM[r1] = r2 4. r2 = Receive{2} 5. Branch r2 != 10 6. MEM[r1] = r2 7. Jump	1. r1 = 10
1. r1 = r1 + 2 2. r2 = MEM[r1] 3. r2 = r2 + 1 4. Send{1} r2 5. Jump		1. r1 = r1 + 2 2. r2 = MEM[r1] 3. r2 = r2 + 1 4. MEM[r1] = r2 5. Jump

No register live outs

1. Kill and Continue

72

Difficult Dependences

1. r1 = Head

1. r1 = MEM[r1]

2. Branch r1 == 0

3. r2 = MEM[r1 + 4]

4. r3 = Work (r2)

5. Print (r3)

6. Jump

No register live outs

73

DOACROSS

1. r1 = Head

1. r1 = MEM[r1]

2. Branch r1 == 0

3. r2 = MEM[r1 + 4]

4. r3 = Work (r2)

5. Print (r3)

6. Jump

No register live outs

74

PS-DSWP

1. r1 = Head

1. r1 = MEM[r1]

2. Branch r1 == 0

3. r2 = MEM[r1 + 4]

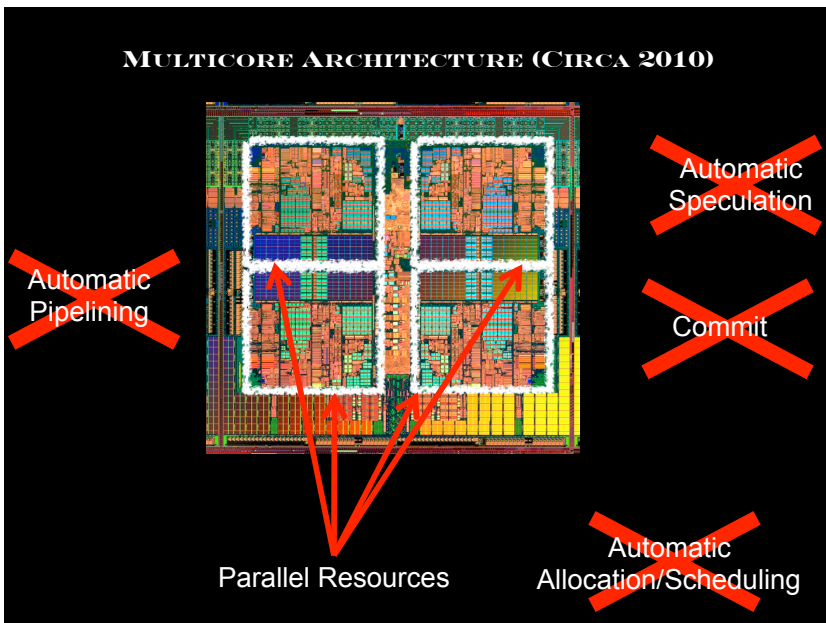
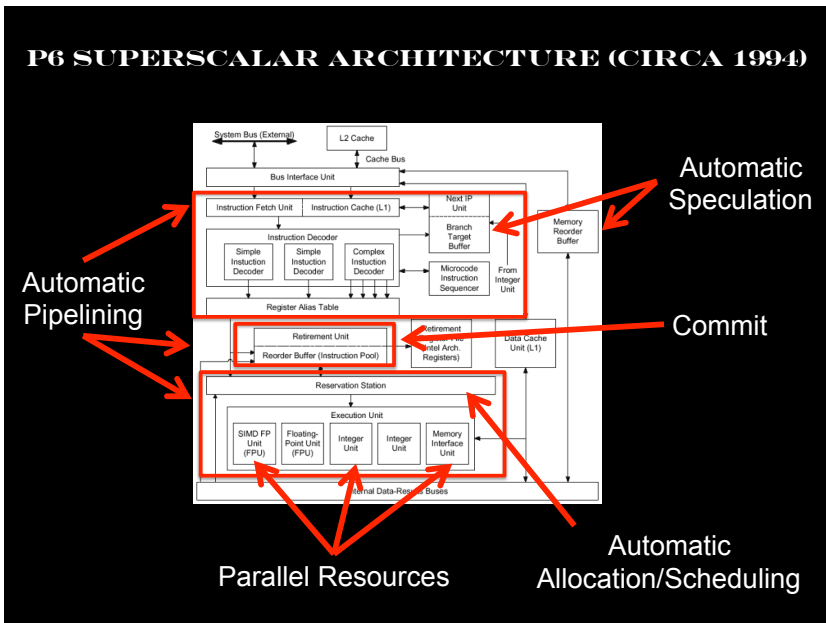
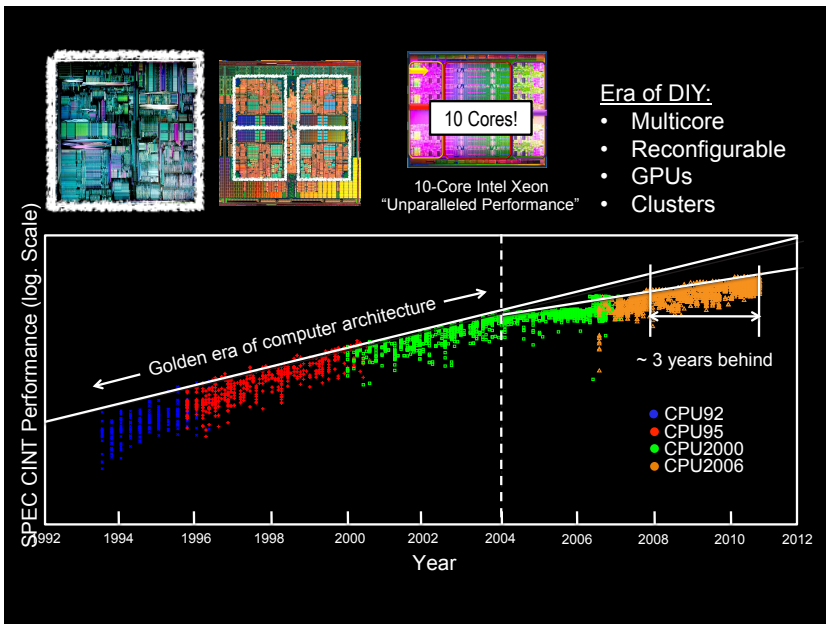
4. r3 = Work (r2)

5. Print (r3)

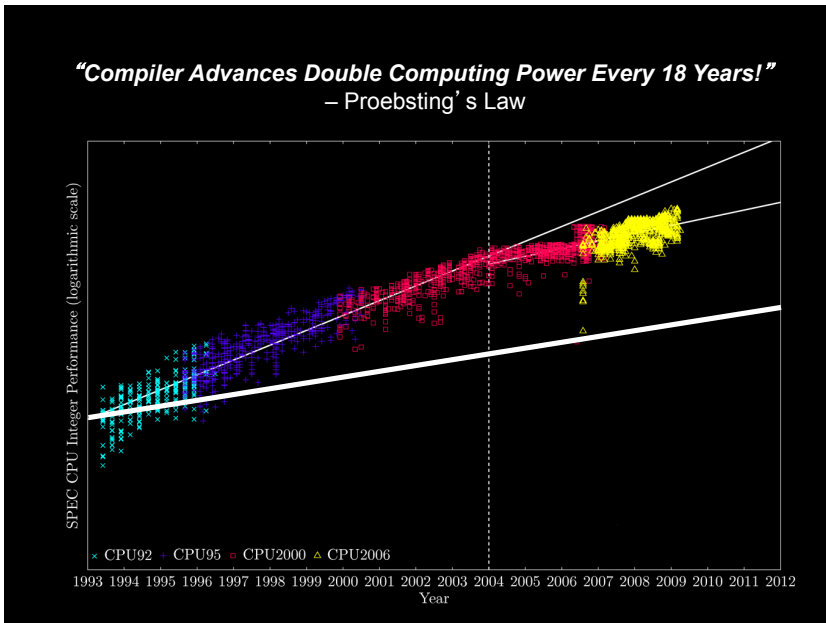
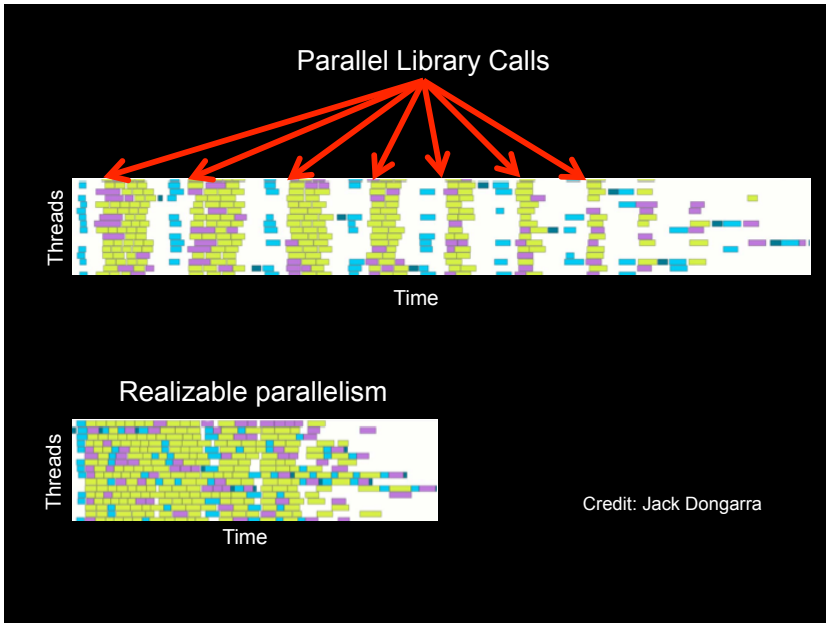
6. Jump

No register live outs

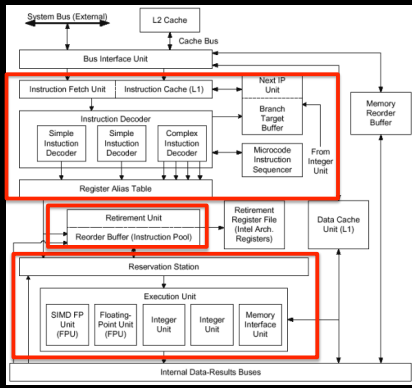
75



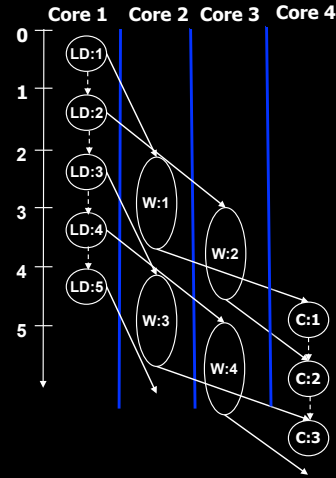
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ACE	CPS	GUARD	Legion	Paralation	SCHEDULE
ACT++	CRL	HAaL	Meta Chaos	Parallel-C++	SciTL
Active messages	CSP	Haskell	Midway	Parallaxis	POET
Adl	Cthreads	HPC++	Millipede	ParC	SDDA
Adminth	CUMULVS	JAVAR	CparPar	ParLib++	SHMEM
ADDAP	DAGGER	HORUS	Mirage	ParLin	SIMPLE
AFAPI	DAPPLE	HPC	MpC	Parmacs	Sina
ALWAN	Data Parallel C	IMPACT	MOSIX	Parh	SISAL
AM	DC++	ISIS	Modula-P	pC	distributed smalltalk
AMDC	DCE++	JAVAR	Modula-2*	pC++	SML
AppLeS	DDD	JADE	MultiPol	PCN	SONiC
Amoeba	DICE	Java RMI	MPI	PCP	Split-C
ARTS	DIPC	javaPG	MPC++	PH	SR
Athapascan-0b	DOLIB	JavaSpace	Mumin	PEACE	Sthreads
Aurora	DOIME	JIDL	Nano-Threads	PCU	Strand
Automap	DOSMOS	Joyce	NESL	PET	SUIF
bb_threads	DRL	Khoros	NetClasses++	PETSc	Synergy
Blaze	DSM-Threads	Karma	Nexus	PENNY	Telegraphos
BSP	Ease	KOAN/Fortran-S	Nimrod	Phosphorus	SuperPascal
BlockComm	ECO	LAM	NOW	POET	TCGMSG
C*	Eiffel	Lilac	Objective Linda	Polans	Threads.h++
C in C	Eilean	Linda	Occam	POOMA	TreadMarks
C++	Emerald	JADA	Omega	POOL-T	TRAPPER
CarLOS	EPL	WWWinda	OpenMP	PRESTO	uC++
Cashmere	Excalibur	ISETL-Linda	Orca	P-RIO	UNITY
C4	Express	ParLin	OOP90	Prospero	UC
CC++	Falcon	Eilean	P++	Proteus	V
Chu	Filaments	P4-Linda	P3L	QPC++	Vic*
Charlotte	FM	Gienda	p4-Linda	PVM	Viafold V-NUS
Charm	FLASH	POSYBL	Pablo	PSI	VPE
Charm++	The FORCE	Objective-Linda	PADE	PSDM	Win32 threads
Cid	Fork	LiPS	PADRE	Quake	WinPar
Cilk	Fortran-M	Locust	Panda	Quark	WWWinda
CM-Fortran	FX	Lparx	Papers	Quick Threads	XENOOFS
Converse	GA	Lucid	AFAPI	Sage++	XPC
Code	GAMMA	Masie	Para++	SCANDAL	Zounds
COOL	Glenda	Manifold	Paradigm	SAM	ZPL



P6 SUPERSCALAR ARCHITECTURE



Spec-PS-DSWP

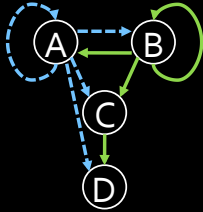


Example

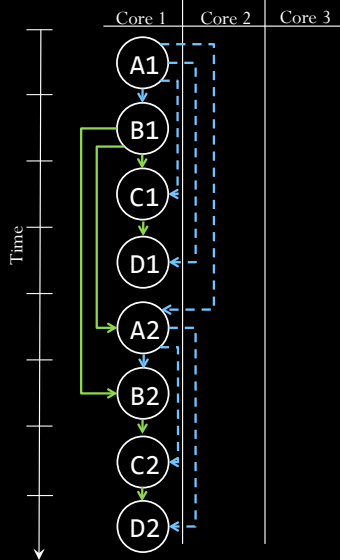
```

A: while (node) {
B:   node = node->next;
C:   res = work(node);
D:   write(res);
}
    
```

Program Dependence Graph



--- Control Dependence
 — Data Dependence



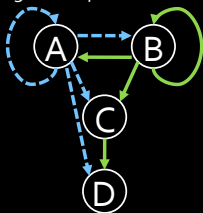
Spec-DOALL

Example

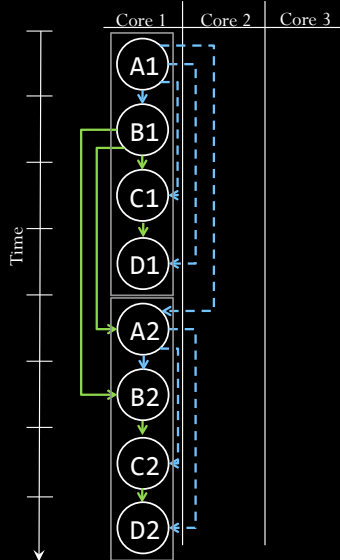
```

A: while (node) {
B:   node = node->next;
C:   res = work(node);
D:   write(res);
}
    
```

Program Dependence Graph



--- Control Dependence
 — Data Dependence

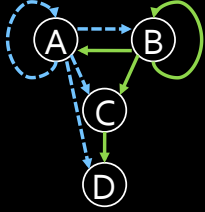


Spec-DOALL

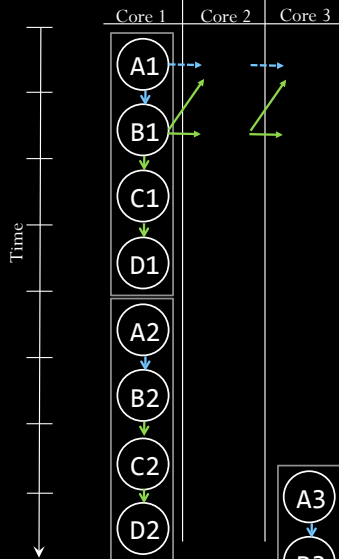
Example

```
A: while (node) {
B:   node = node->next;
C:   res = work(node);
D:   write(res);
}
```

Program Dependence Graph



--- Control Dependence
— Data Dependence

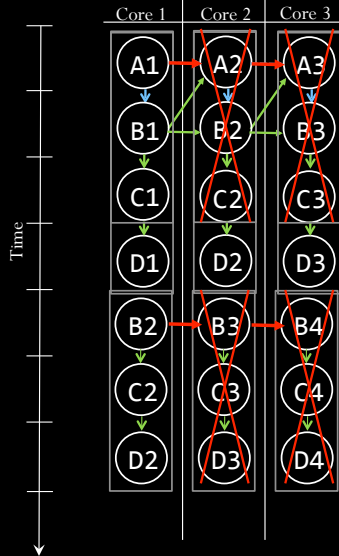
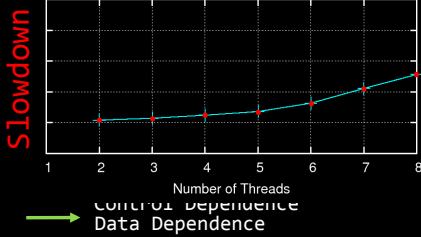


Spec-DOALL

Example

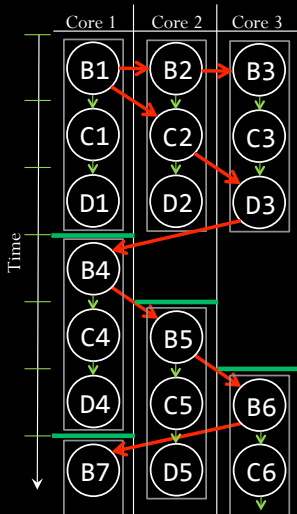
```
A: while (node) {
B:   node = node->next;
C:   res = work(node);
D:   write(res);
}
```

Program Dependence Graph



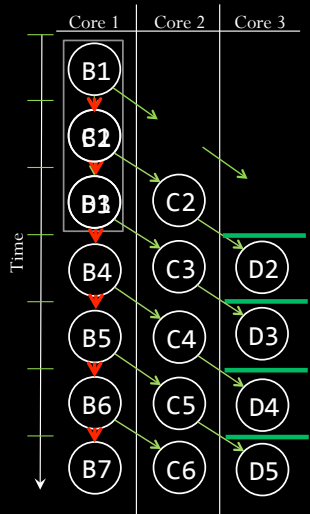
Spec-DOACROSS

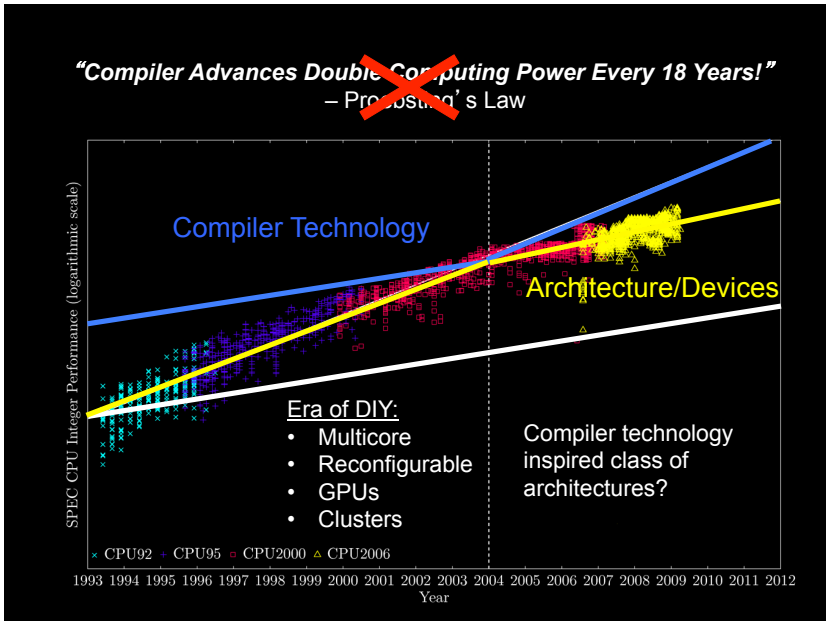
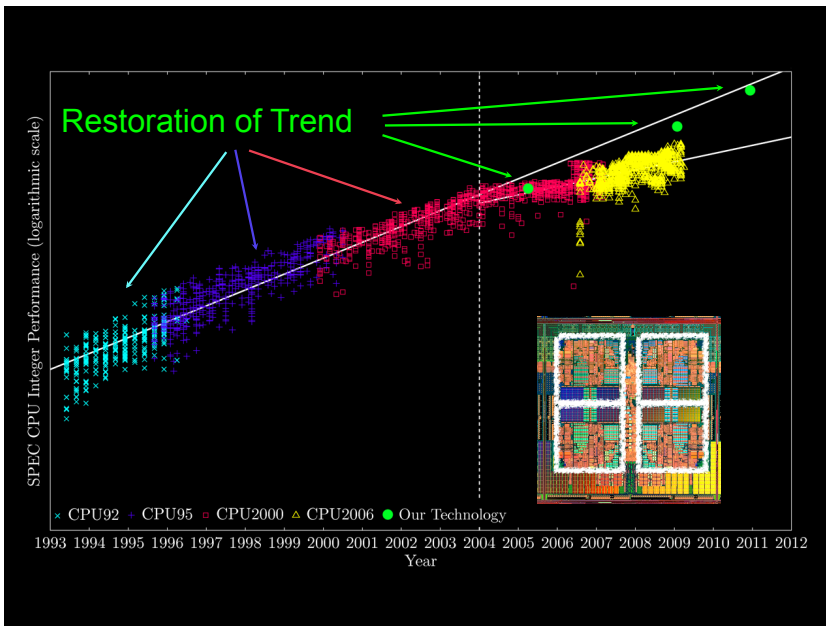
Throughput: 1 iter/cycle



Spec-DSWP

Throughput: 1 iter/cycle





CFGs and PCs

