

The 3D Rasterization Pipeline

COS 426, Spring 2014
Princeton University

3D Rendering Scenarios



Batch

- One image generated with as much quality as possible for a particular set of rendering parameters
 - Take as much time as is needed (minutes)
 - Useful for photorealistism, movies, etc.

Interactive

- Images generated in fraction of a second (<1/10)
 with user input, animation, varying camera, etc.
 - Achieve highest quality possible in given time
 - Visualization, games, etc.

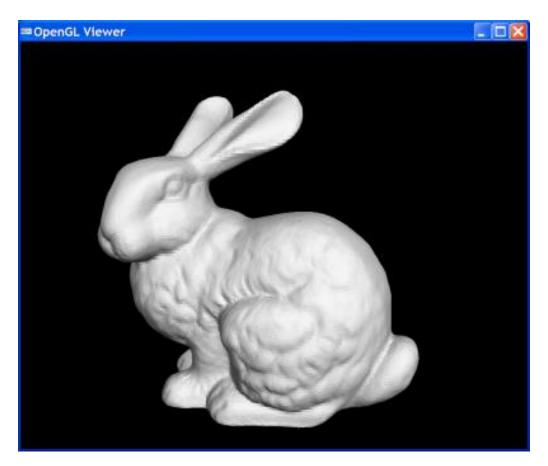


Many applications use rendering of 3D polygons with direct illumination





Many applications use rendering of 3D polygons with direct illumination

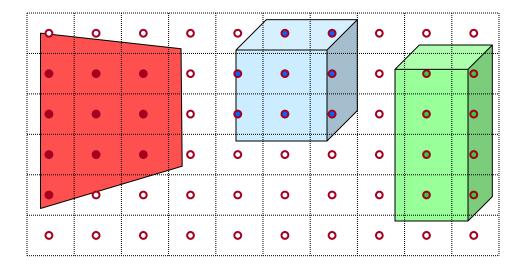


meshview

Ray Casting Revisited

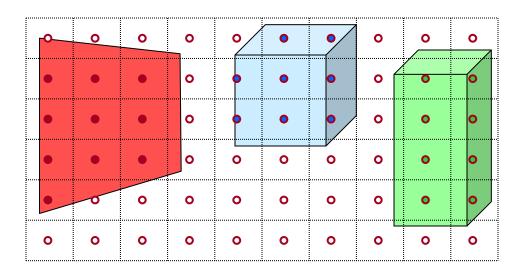


- For each sample ...
 - Construct ray from eye position through view plane
 - Find first surface intersected by ray through pixel
 - Compute color of sample based on illumination



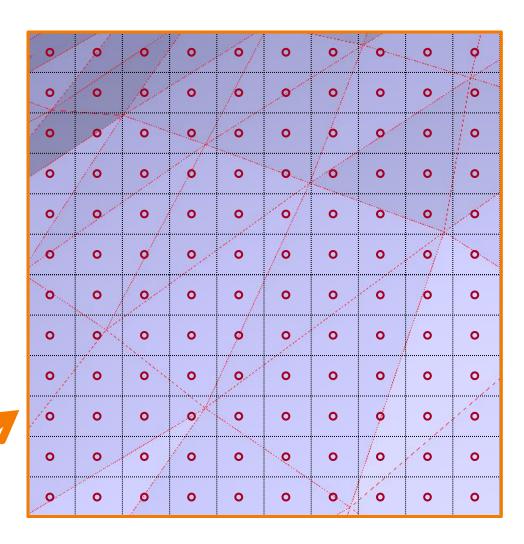


 We can render polygons faster if we take advantage of spatial coherence





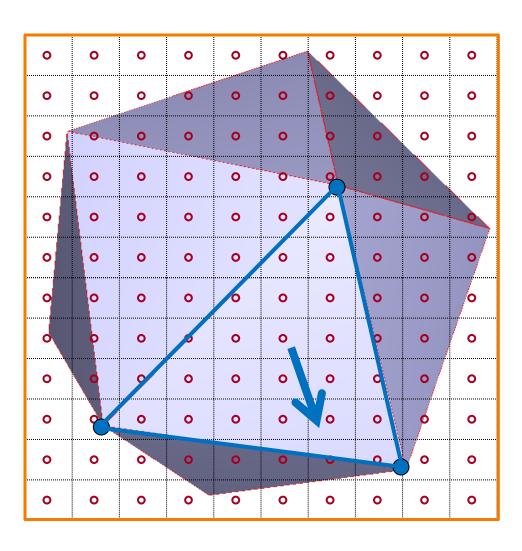
How?





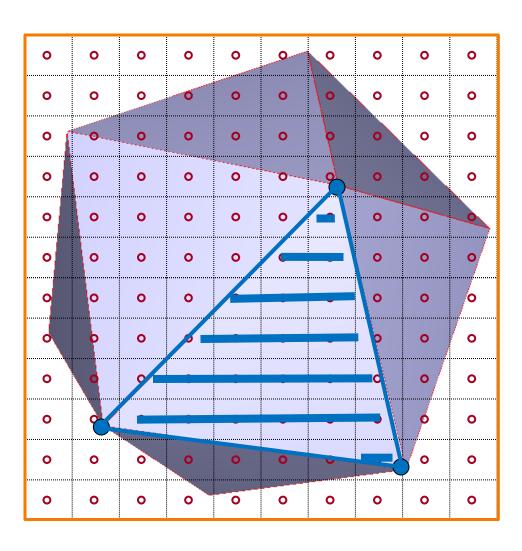


• How?

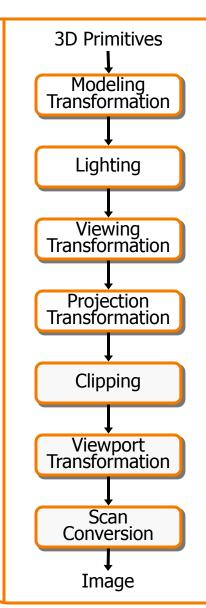




• How?

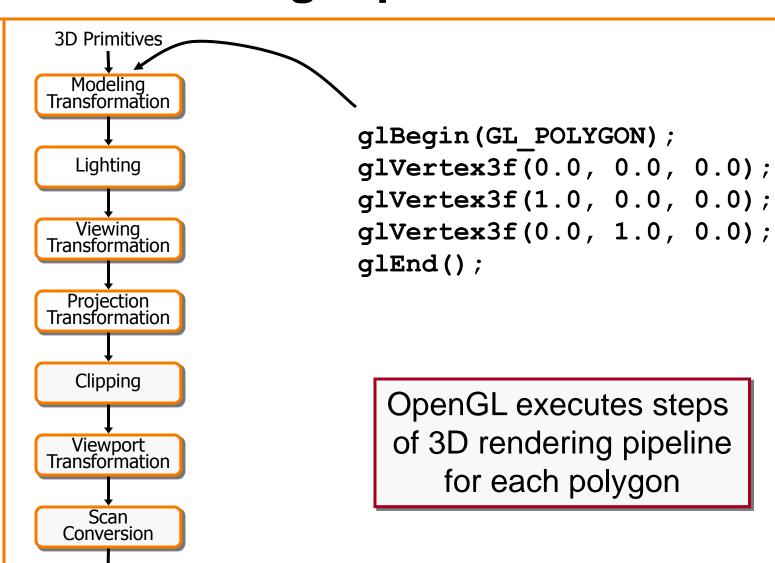






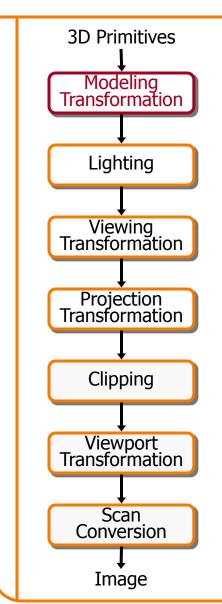
This is a pipelined sequence of operations to draw 3D primitives into a 2D image





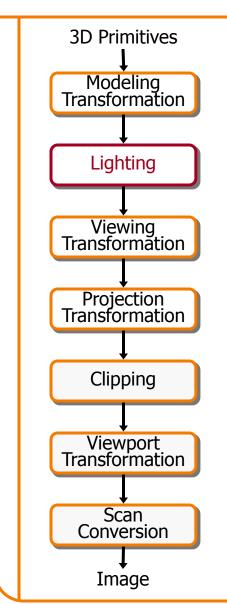
Image





Transform into 3D world coordinate system

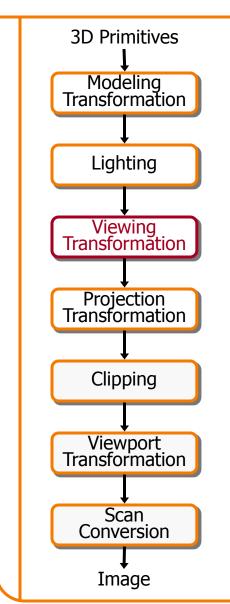




Transform into 3D world coordinate system

Illuminate according to lighting and reflectance



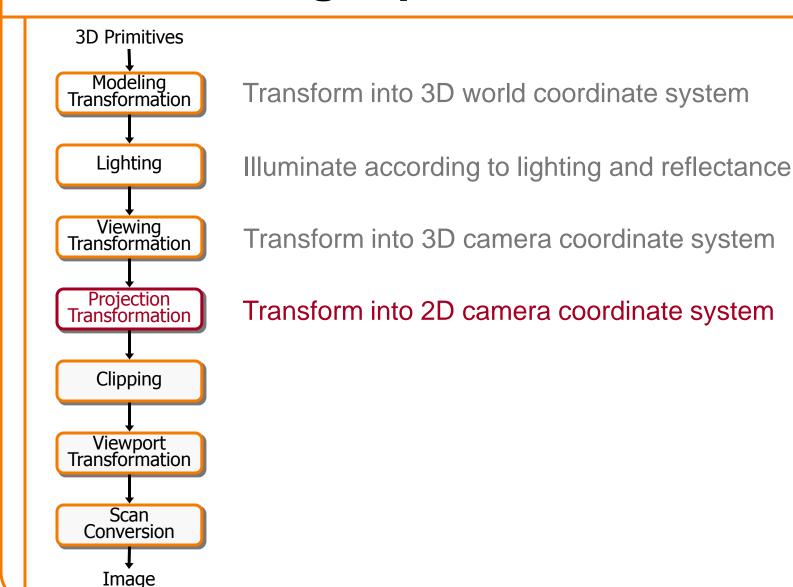


Transform into 3D world coordinate system

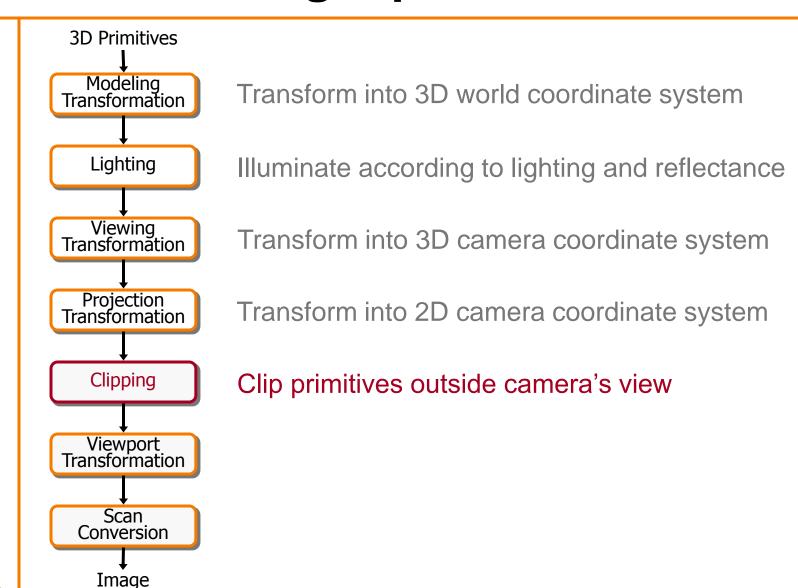
Illuminate according to lighting and reflectance

Transform into 3D camera coordinate system

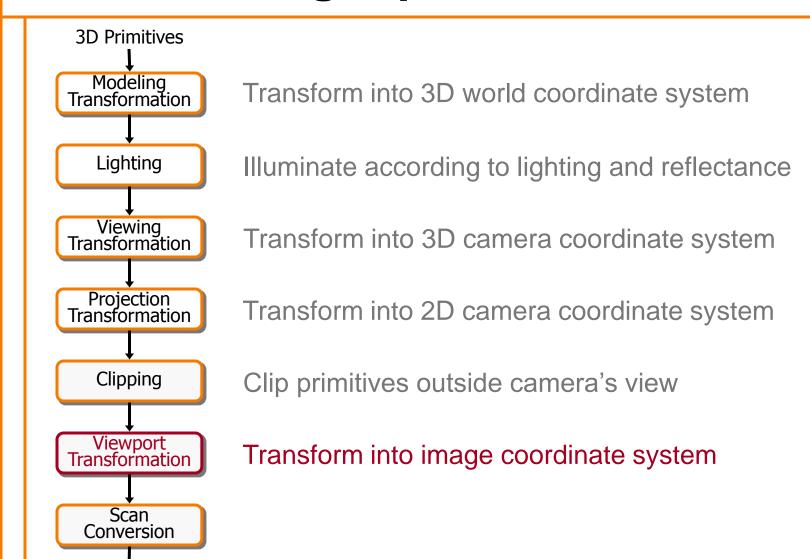






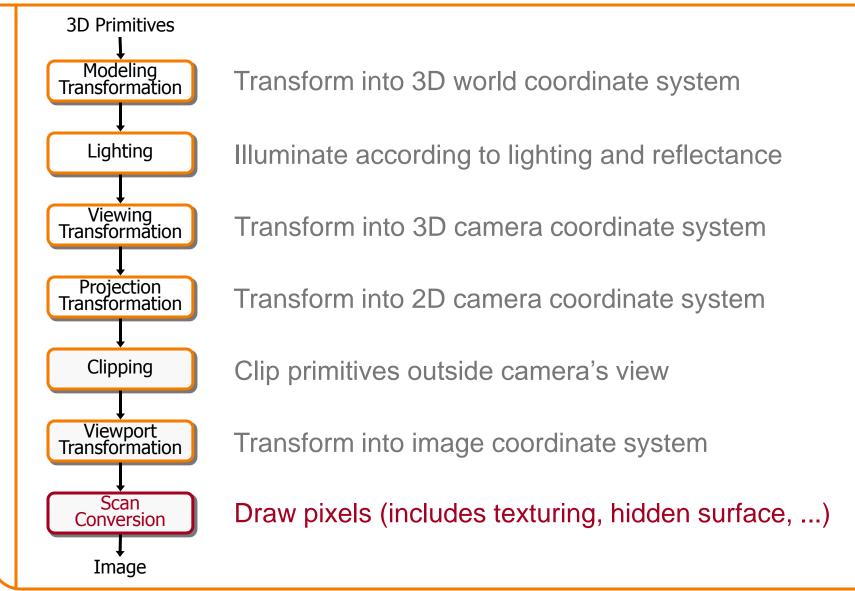




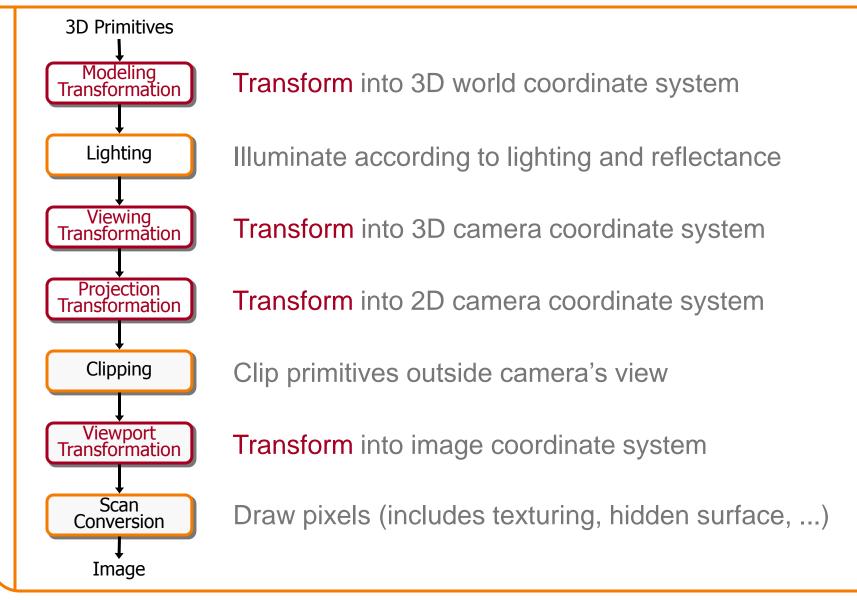


Image



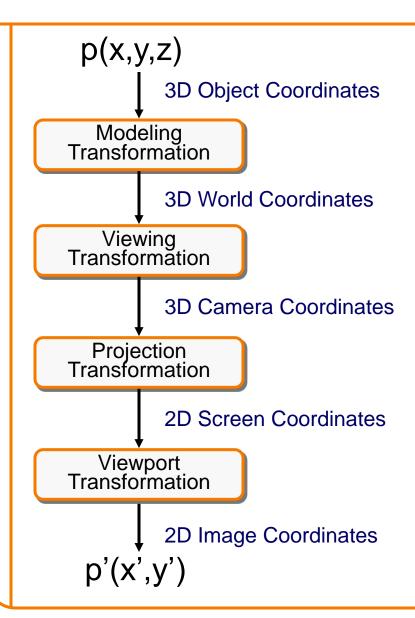




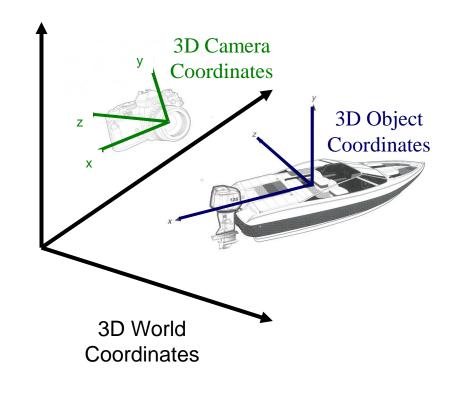


Transformations



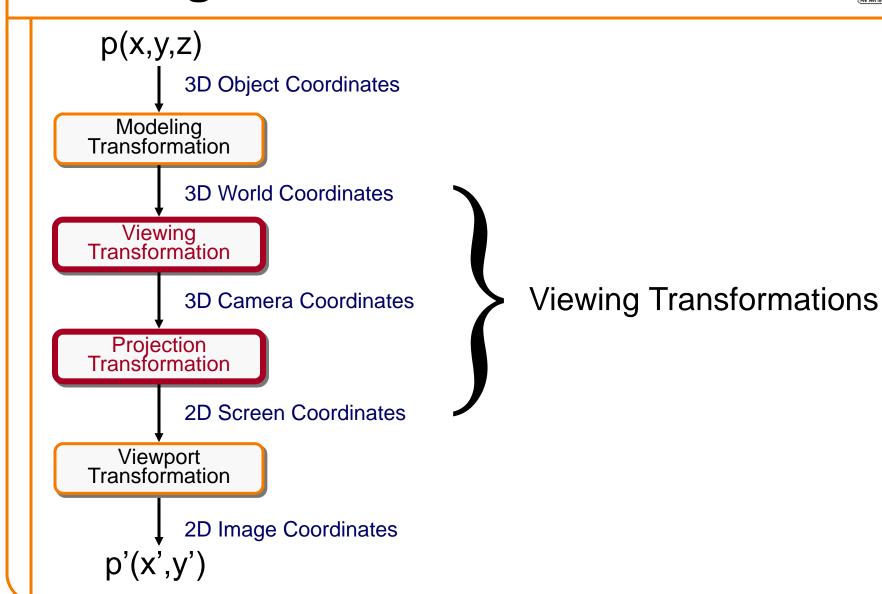


Transformations map points from one coordinate system to another



Viewing Transformations





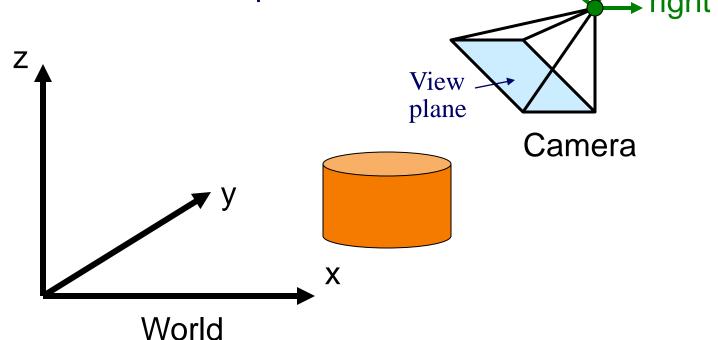
Review: Viewing Transformation



back

up

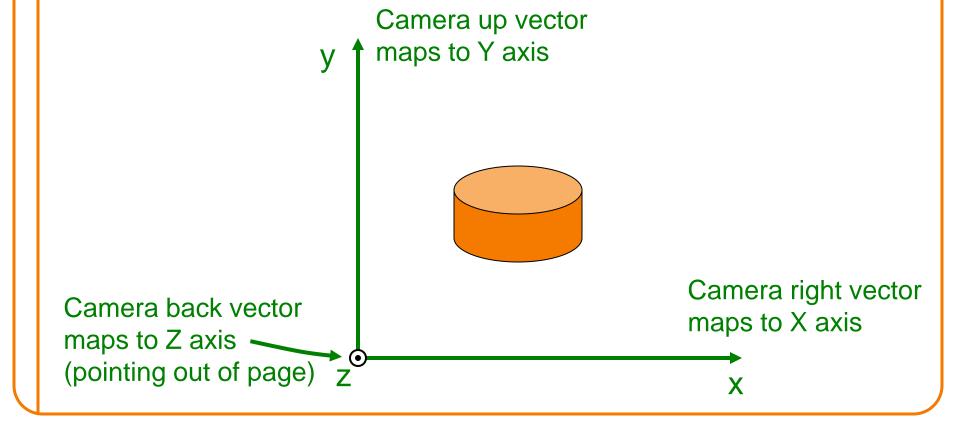
- Mapping from world to camera coordinates
 - Eye position maps to origin
 - Right vector maps to X axis
 - Up vector maps to Y axis
 - Back vector maps to Z axis



Review: Camera Coordinates



- Canonical coordinate system
 - Convention is right-handed (looking down -z axis)
 - Convenient for projection, clipping, etc.



Finding the viewing transformation



- We have the camera (in world coordinates)
- We want T taking objects from world to camera

$$p^{C} = T p^{W}$$

Trick: find T⁻¹ taking objects in camera to world

$$p^{W} = T^{-1}p^{C}$$

$$\begin{bmatrix} x' \\ y' \\ z' \\ w' \end{bmatrix} = \begin{bmatrix} a & b & c & d \\ e & f & g & h \\ i & j & k & l \\ m & n & o & p \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix}$$

Finding the Viewing Transformation

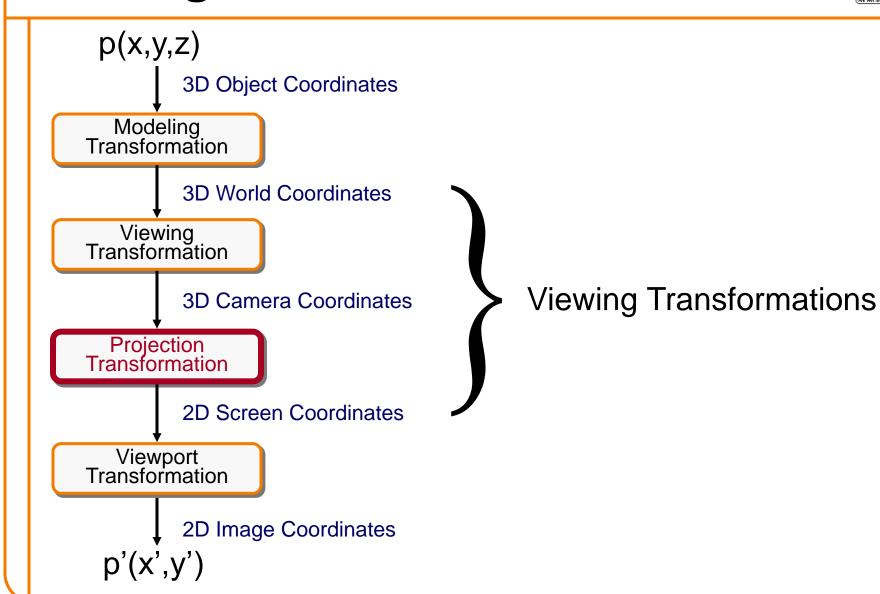
- Trick: map from camera coordinates to world
 - Origin maps to eye position
 - Z axis maps to Back vector
 - Y axis maps to Up vector
 - X axis maps to Right vector

$$\begin{bmatrix} x' \\ y' \\ z' \\ w' \end{bmatrix} = \begin{bmatrix} R_x & U_x & B_x & E_x \\ R_y & U_y & B_y & E_y \\ R_z & U_z & B_z & E_z \\ R_w & U_w & B_w & E_w \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix}$$

This matrix is T⁻¹ so we invert it to get T ... easy!

Viewing Transformations

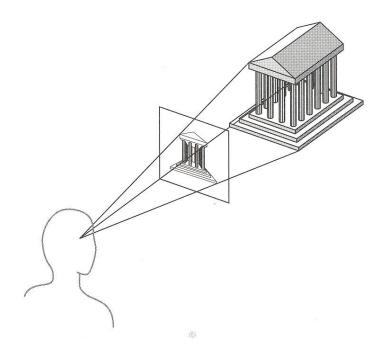




Projection

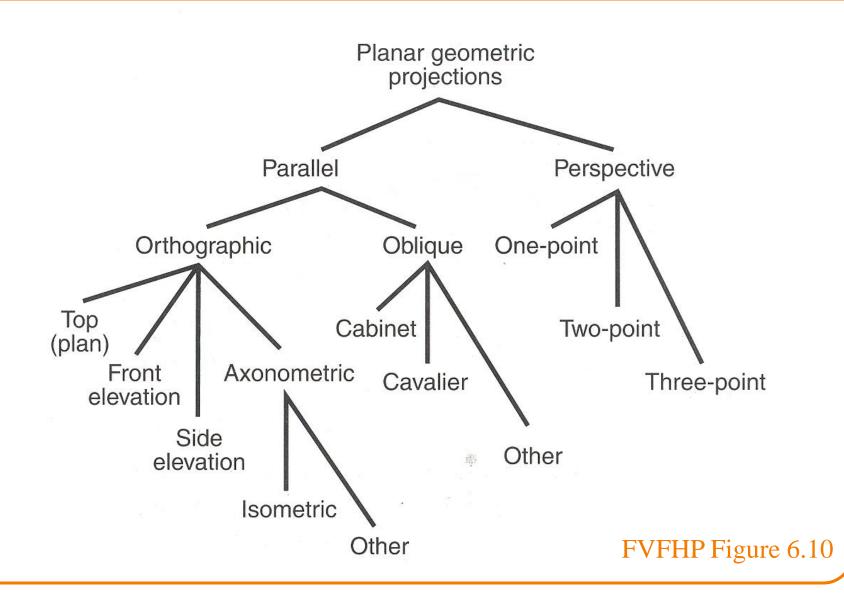


- General definition:
 - Transform points in *n*-space to *m*-space (*m*<*n*)
- In computer graphics:
 - Map 3D camera coordinates to 2D screen coordinates



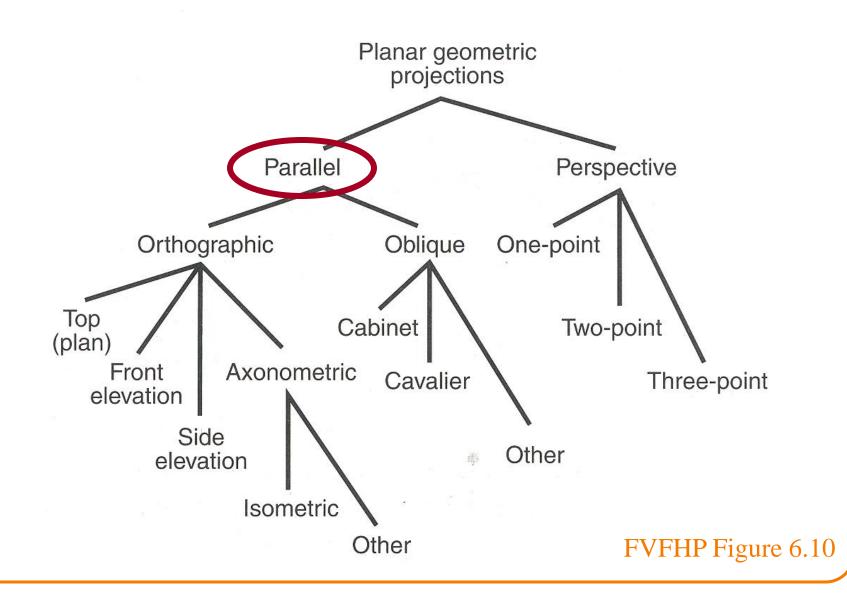
Taxonomy of Projections





Taxonomy of Projections

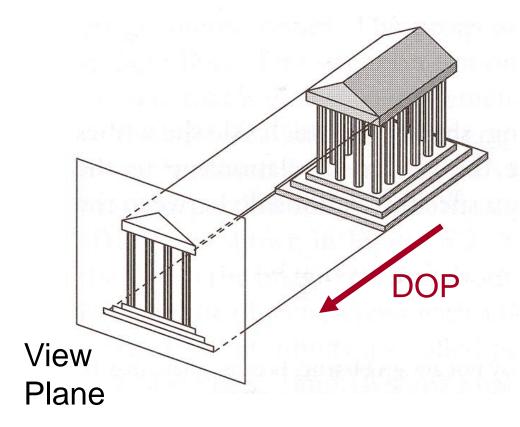




Parallel Projection



- Center of projection is at infinity
 - Direction of projection (DOP) same for all points

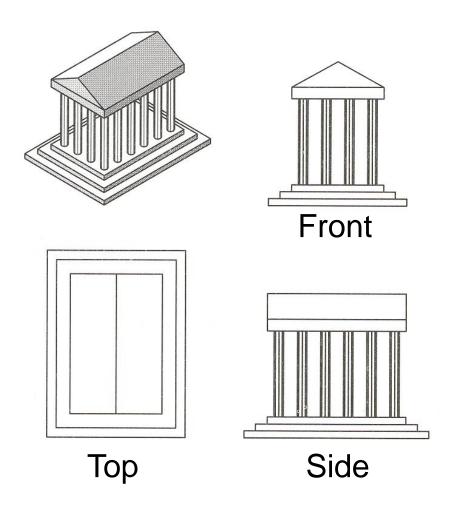


Angel Figure 5.4

Orthographic Projections



DOP perpendicular to view plane

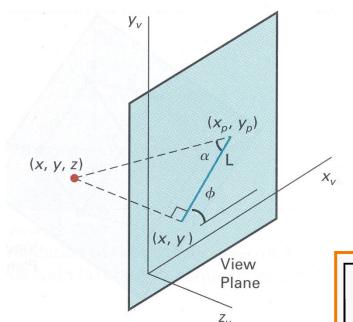


Angel Figure 5.5

Parallel Projection Matrix



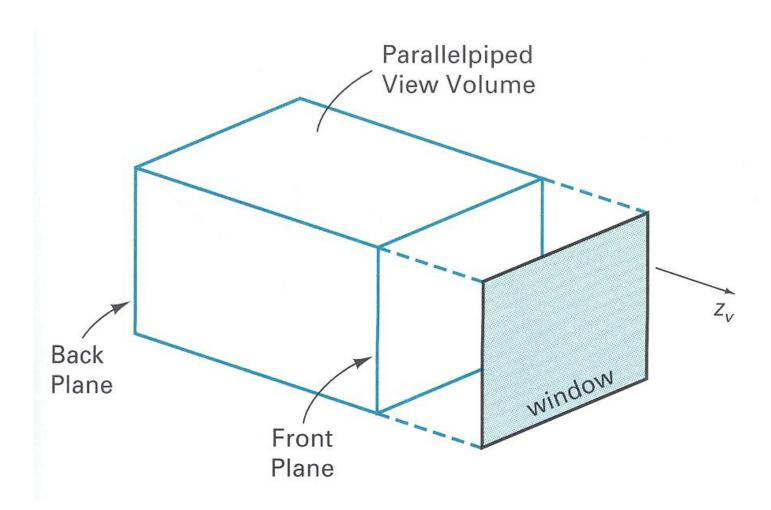
General parallel projection transformation:



$$\begin{bmatrix} x_s \\ y_s \\ z_s \\ w_s \end{bmatrix} = \begin{bmatrix} 1 & 0 & L\cos\phi & 0 \\ 0 & 1 & L\sin\phi & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x_c \\ y_c \\ z_c \\ 1 \end{bmatrix}$$

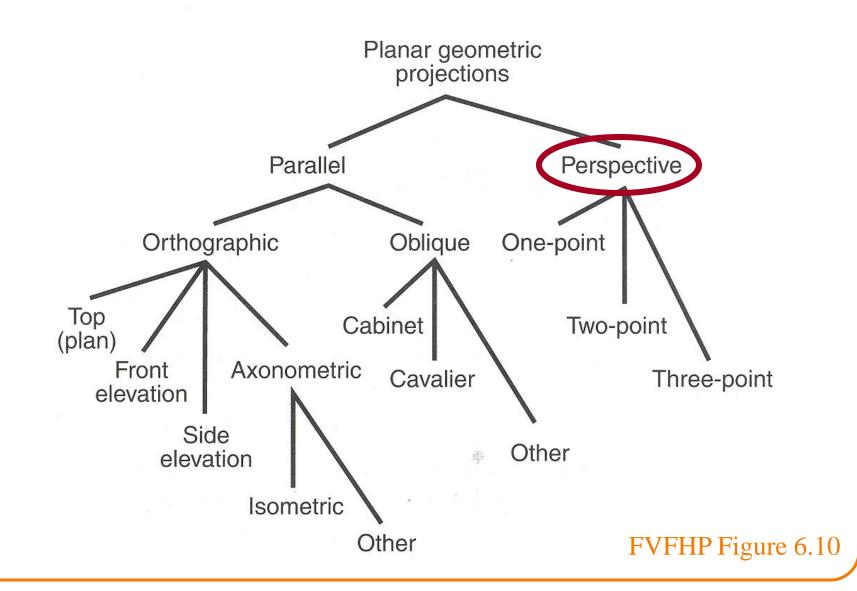
Parallel Projection View Volume





Taxonomy of Projections

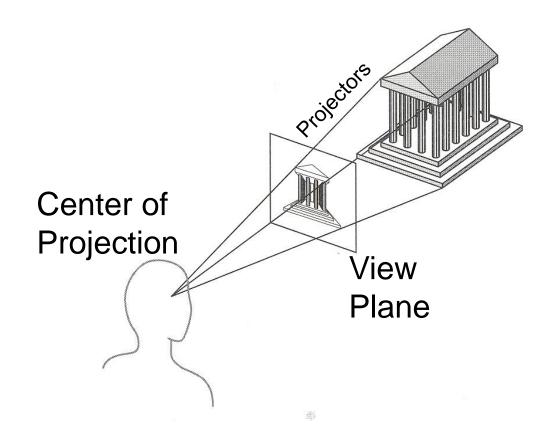




Perspective Projection

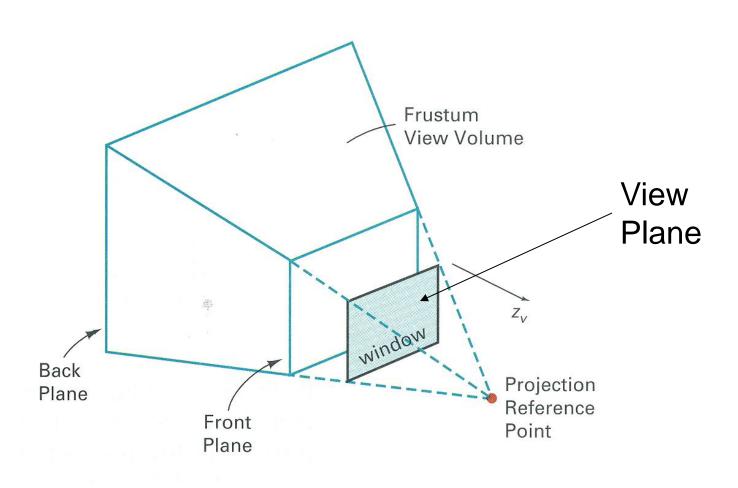


 Map points onto "view plane" along "projectors" emanating from "center of projection" (COP)



Perspective Projection View Volume

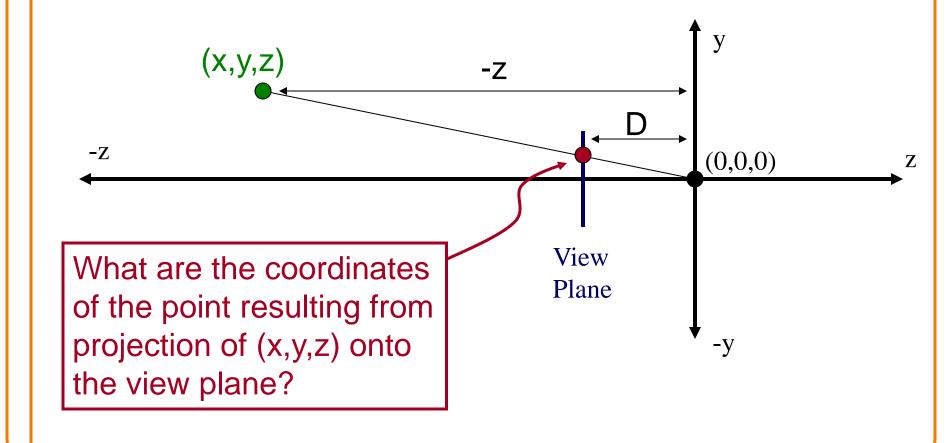




Perspective Projection



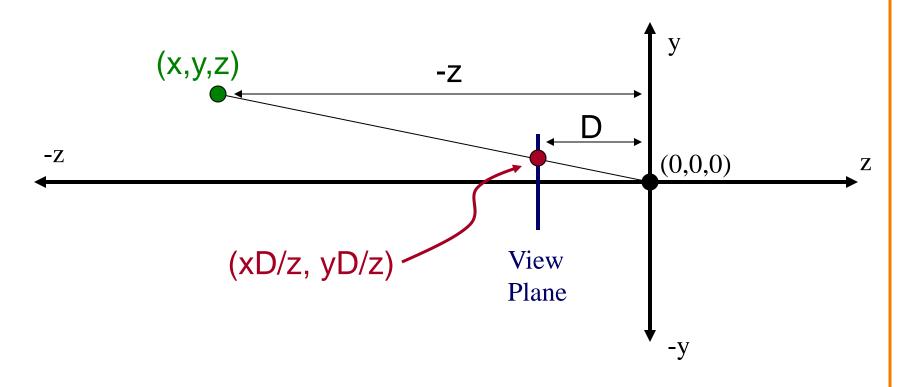
Compute 2D coordinates from 3D coordinates with similar triangles



Perspective Projection



Compute 2D coordinates from 3D coordinates with similar triangles





4x4 matrix representation?

$$x_{s} = x_{c}D/z_{c}$$

$$y_{s} = y_{c}D/z_{c}$$

$$z_{s} = D$$

$$w_{s} = 1$$



4x4 matrix representation?

$$x_s = x_c D / z_c$$
 $x_s = x' / w'$ $x' = x_c$
 $y_s = y_c D / z_c$ $y_s = y' / w'$ $y' = y_c$
 $z_s = D$ $z_s = z' / w'$ $z' = z_c$
 $w_s = 1$ $w' = z_c / D$



4x4 matrix representation?

$$x_s = x_c D / z_c$$
 $x_s = x' / w'$ $x' = x_c$
 $y_s = y_c D / z_c$ $y_s = y' / w'$ $y' = y_c$
 $z_s = D$ $z_s = z' / w'$ $z' = z_c$
 $w_s = 1$ $w' = z_c / D$

$$\begin{bmatrix} x_s \\ y_s \\ z_s \\ w_s \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 1/D & 0 \end{bmatrix} \begin{bmatrix} x_c \\ y_c \\ z_c \\ 1 \end{bmatrix}$$



 In practice, want to compute a value related to depth to include in visibility calculations

$$x_s = x_c D / z_c$$
 $x_s = x' / w'$ $x' = x_c$
 $y_s = y_c D / z_c$ $y_s = y' / w'$ $y' = y_c$
 $z_s = -D / z_c$ $z_s = z' / w'$ $z' = -1$
 $w_s = 1$ $w' = z_c / D$

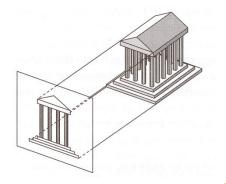
$$\begin{bmatrix} x_s \\ y_s \\ z_s \\ w_s \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & -1 \\ 0 & 0 & 1/D & 0 \end{bmatrix} \begin{bmatrix} x_c \\ y_c \\ z_c \\ 1 \end{bmatrix}$$

Perspective vs. Parallel



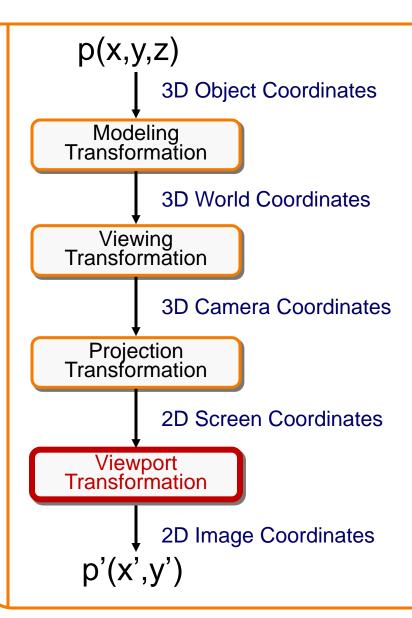
- Perspective projection
 - + Size varies inversely with distance looks realistic
 - Distance and angles are not (in general) preserved
 - Parallel lines do not (in general) remain parallel

- Parallel projection
 - + Good for exact measurements
 - + Parallel lines remain parallel
 - Angles are not (in general) preserved
 - Less realistic looking

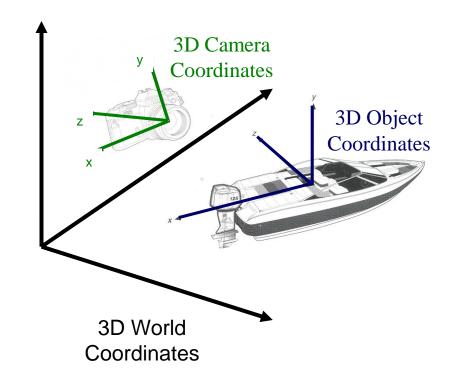


Transformations





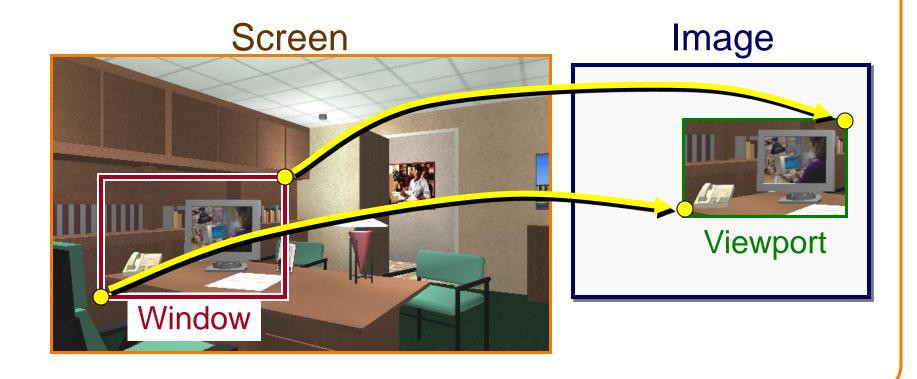
Transformations map points from one coordinate system to another



Viewport Transformation



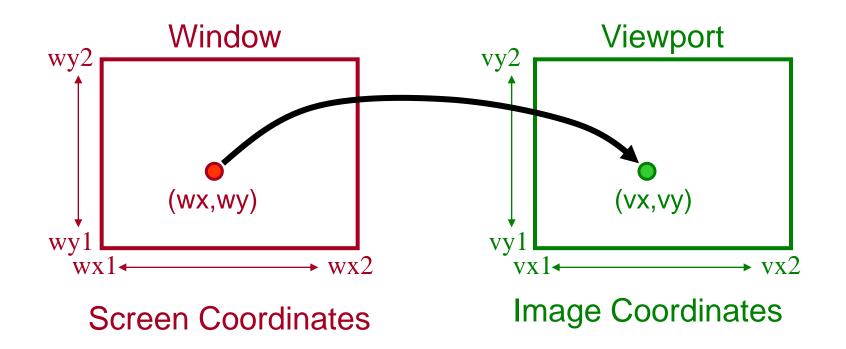
 Transform 2D geometric primitives from screen coordinate system (normalized device coordinates) to image coordinate system (pixels)



Viewport Transformation



Window-to-viewport mapping

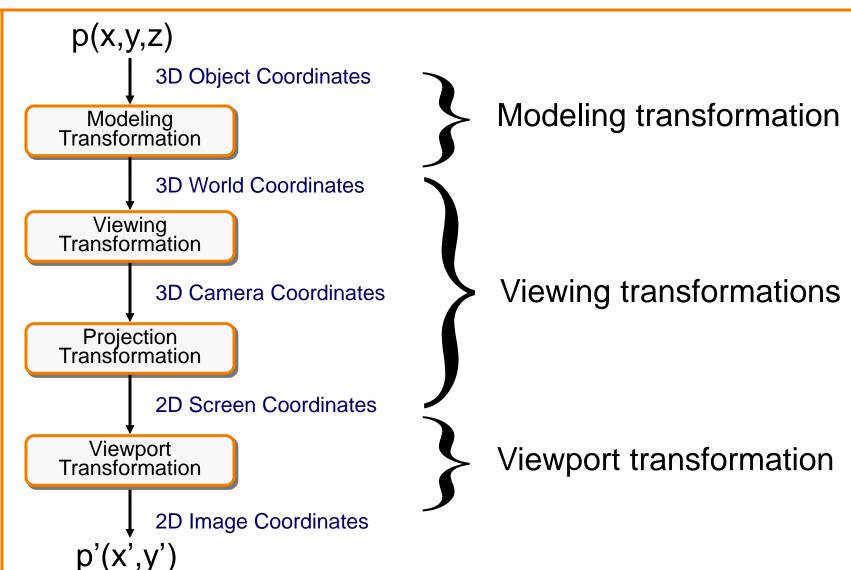


```
vx = vx1 + (wx - wx1) * (vx2 - vx1) / (wx2 - wx1);

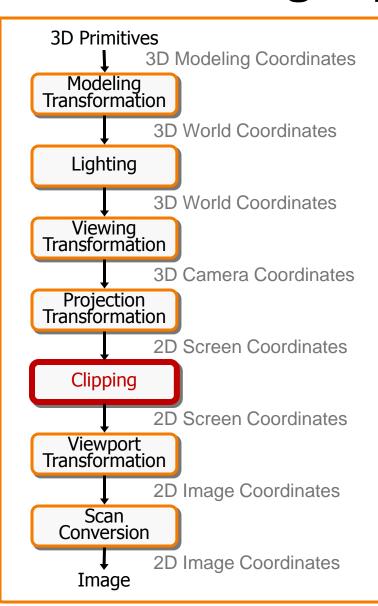
vy = vy1 + (wy - wy1) * (vy2 - vy1) / (wy2 - wy1);
```

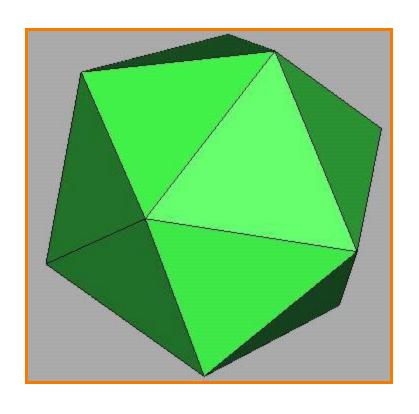
Summary of Transformations







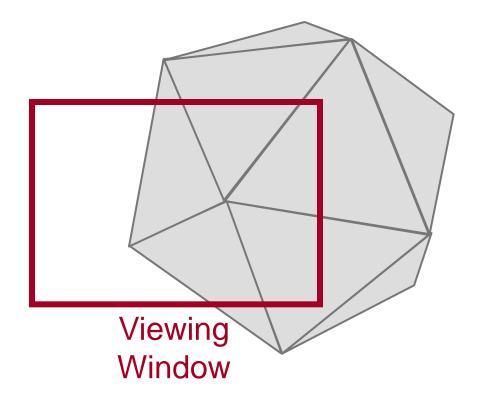




Clipping



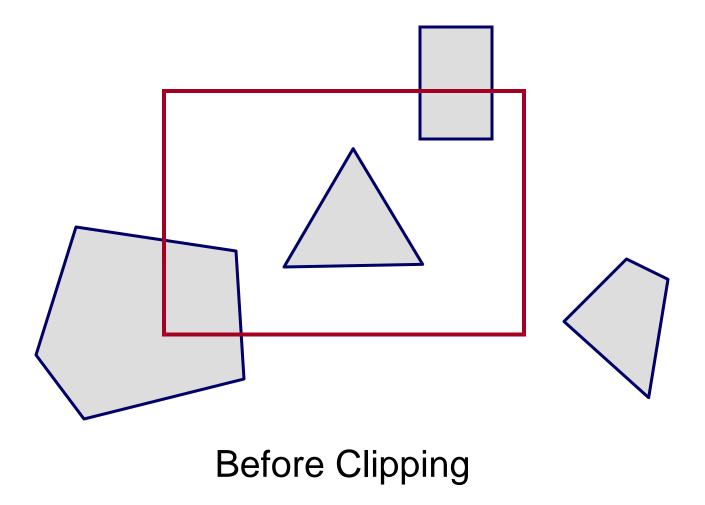
- Avoid drawing parts of primitives outside window
 - Window defines part of scene being viewed
 - Must draw geometric primitives only inside window



Polygon Clipping



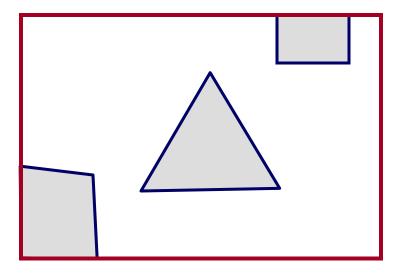
Find the part of a polygon inside the clip window?



Polygon Clipping



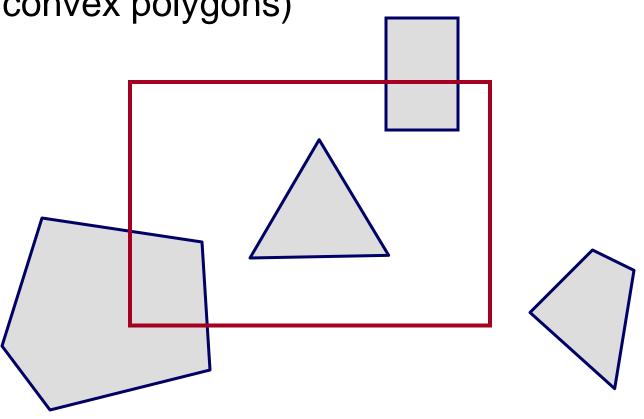
Find the part of a polygon inside the clip window?



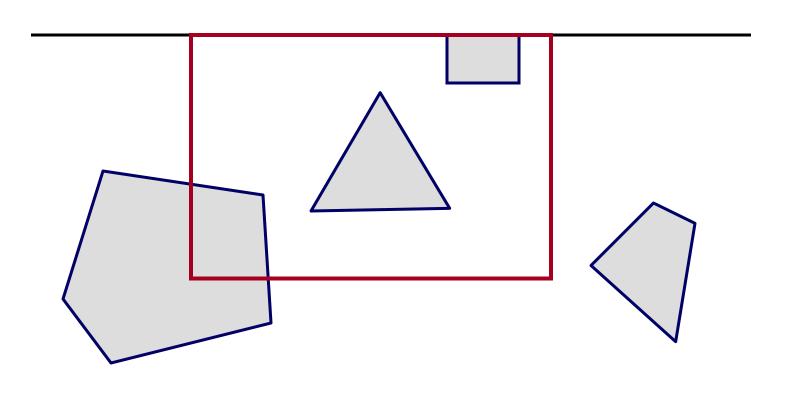
After Clipping



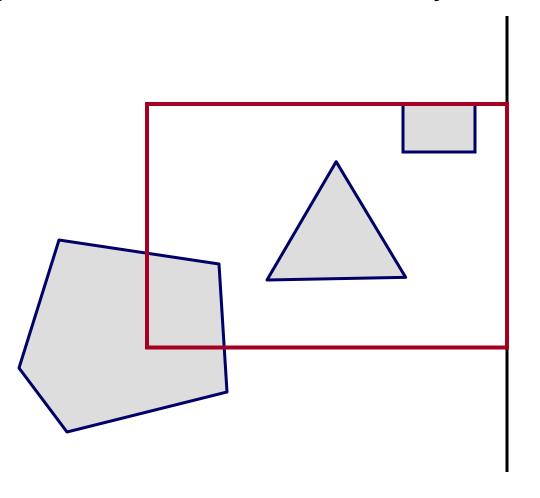
 Clip to each window boundary one at a time (for convex polygons)



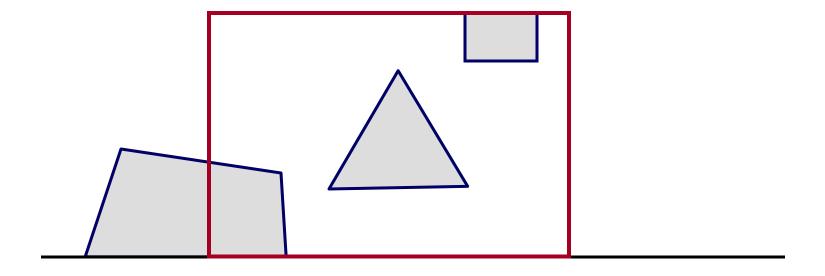




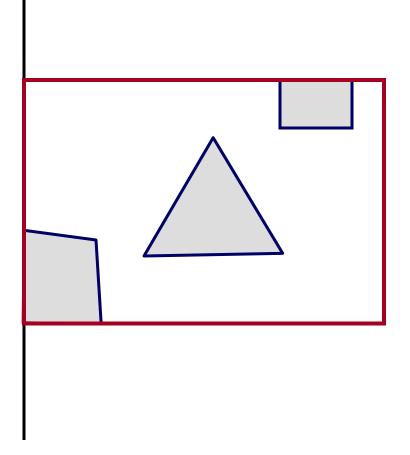




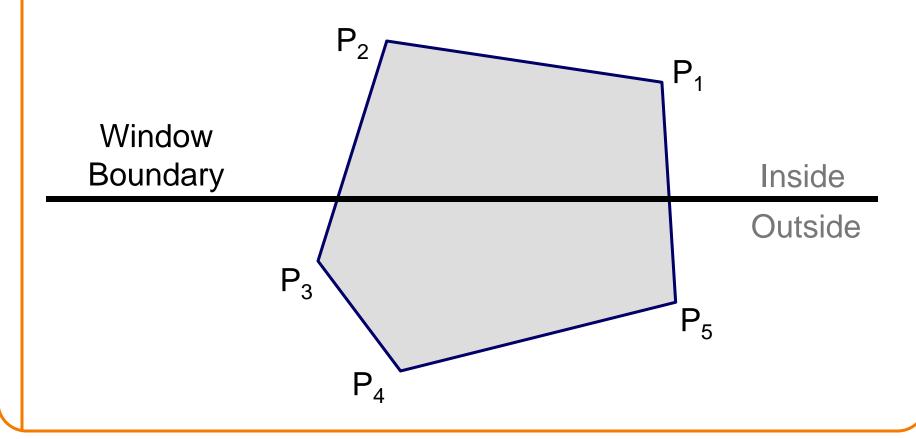




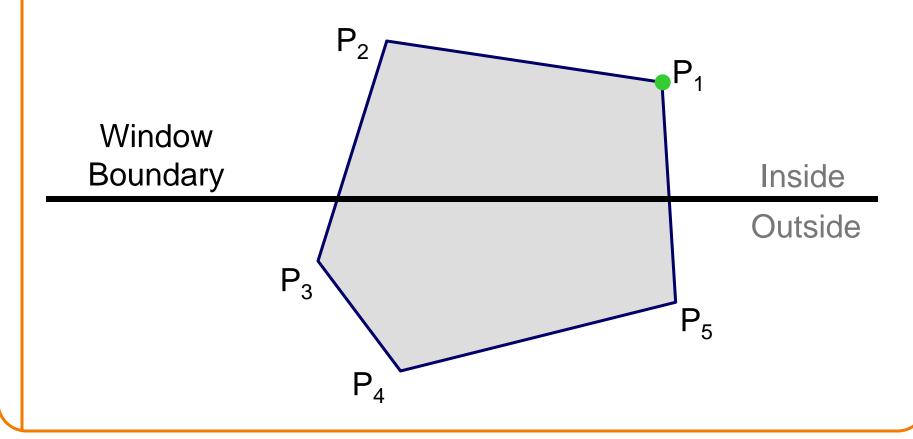




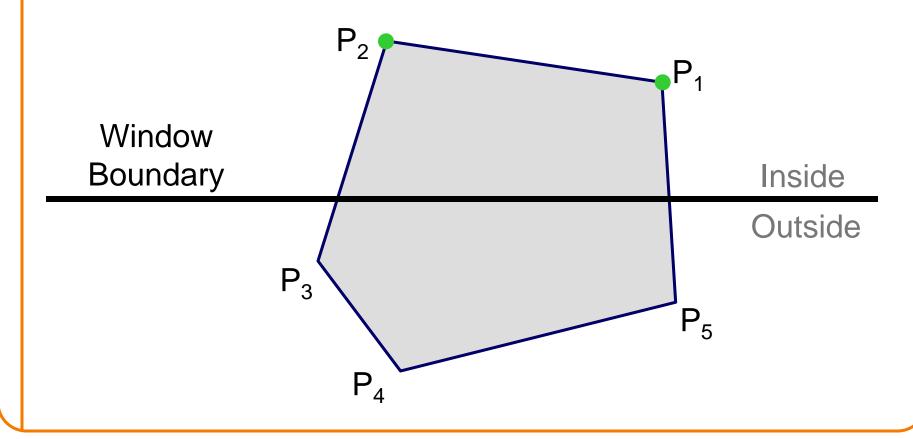




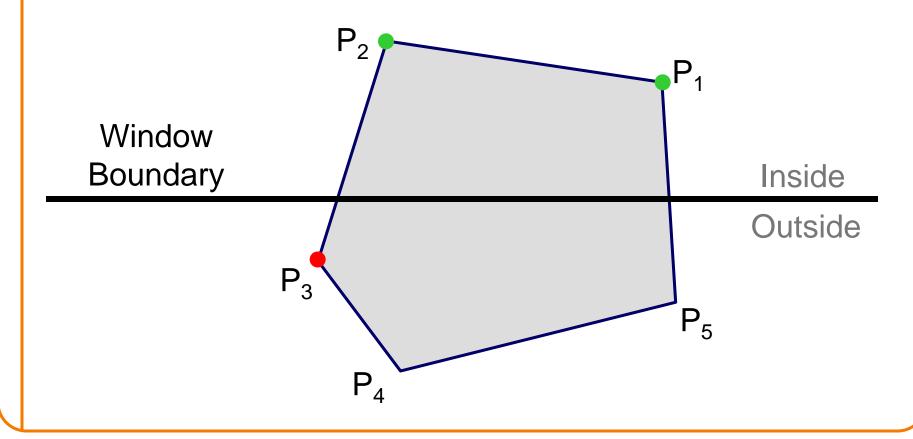




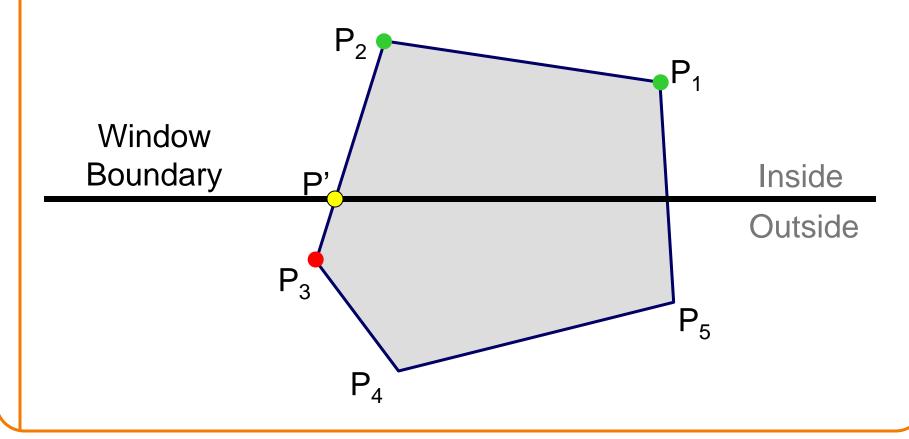




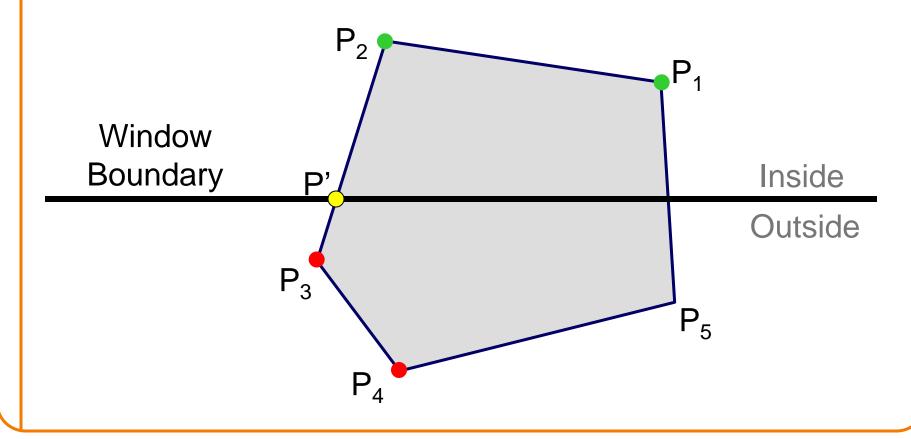




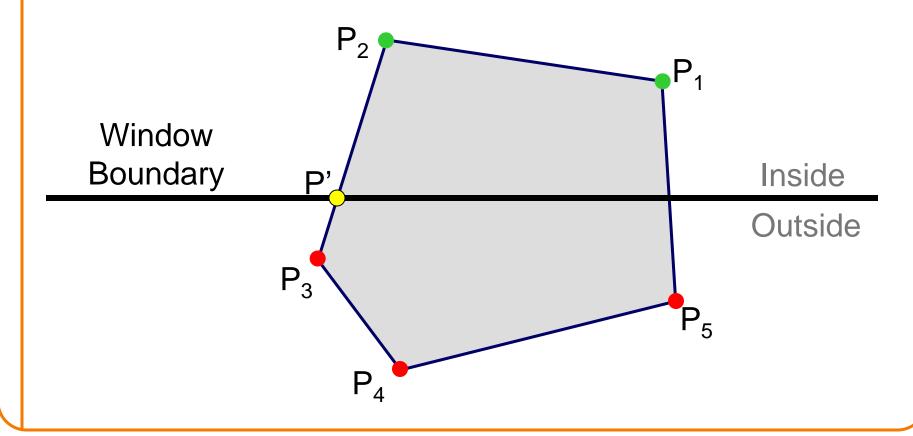




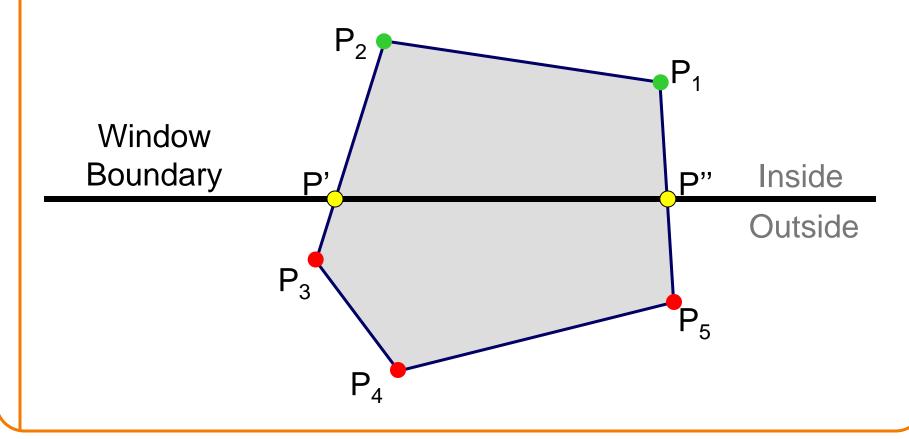




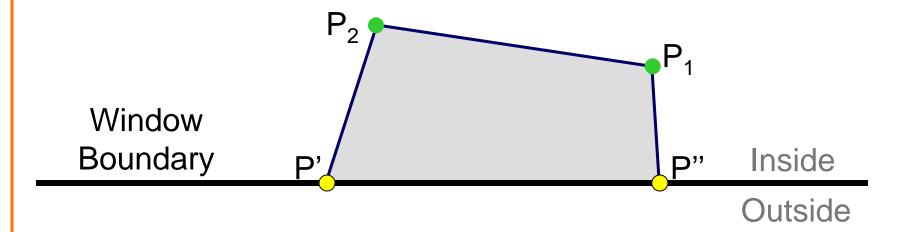




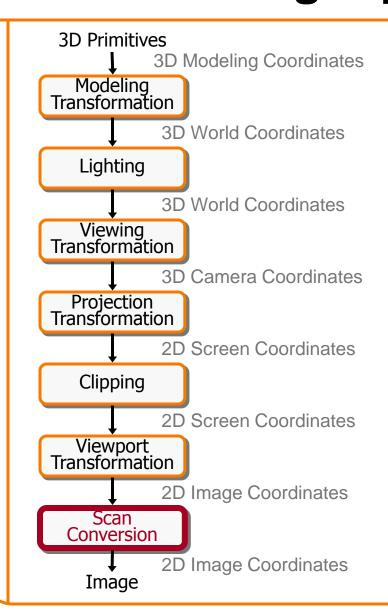


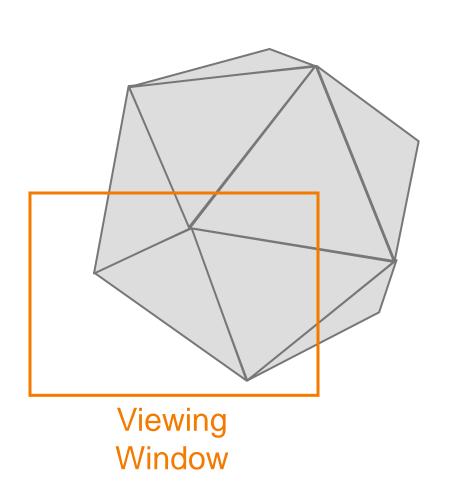






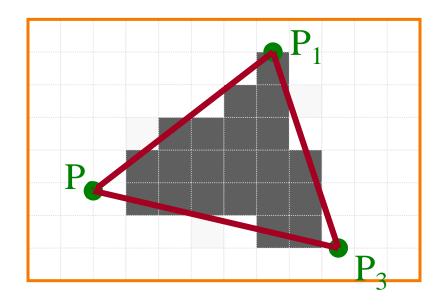








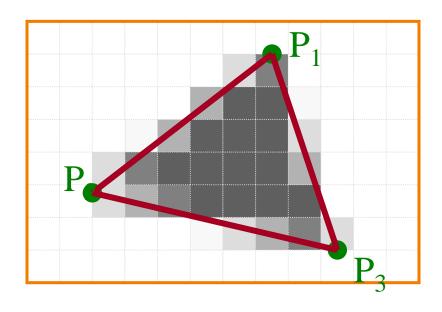




Standard (aliased)
Scan Conversion







Antialiased Scan Conversion

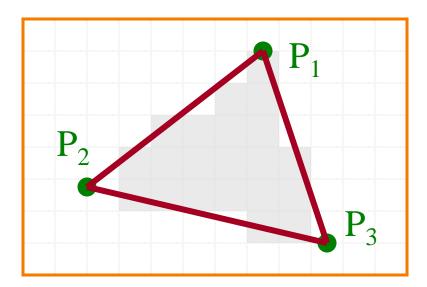
Scan Conversion



 Render an image of a geometric primitive by setting pixel colors

```
void SetPixel(int x, int y, Color rgba)
```

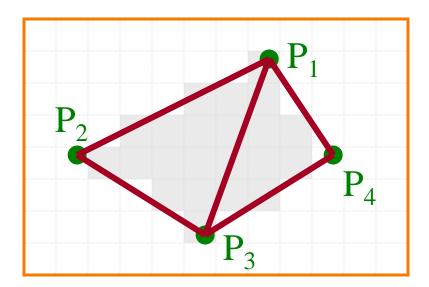
Example: Filling the inside of a triangle



Triangle Scan Conversion



- Properties of a good algorithm
 - Symmetric
 - Straight edges
 - No cracks between adjacent primitives
 - (Antialiased edges)
 - FAST!

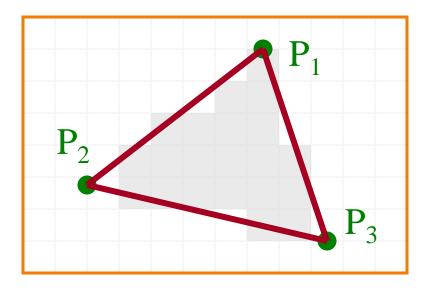


Simple Algorithm



Color all pixels inside triangle

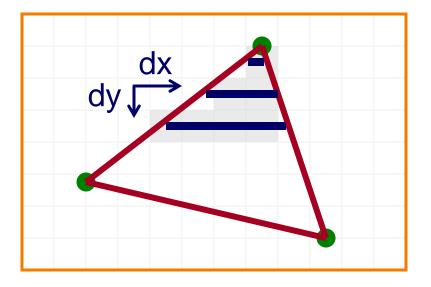
```
void ScanTriangle(Triangle T, Color rgba) {
    for each pixel P in bbox(T) {
        if (Inside(T, P))
            SetPixel(P.x, P.y, rgba);
    }
}
```



Triangle Sweep-Line Algorithm



- Take advantage of spatial coherence
 - Compute which pixels are inside using horizontal spans
 - Process horizontal spans in scan-line order
- Take advantage of edge linearity
 - Use edge slopes to update coordinates incrementally



Triangle Sweep-Line Algorithm



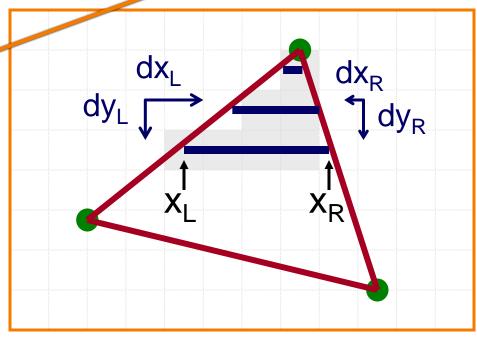
```
void ScanTriangle(Triangle T, Color rgba) {
  for each edge pair {
      initialize x_L, x_R;
      compute dx_L/dy_L and dx_R/dy_R;
      for each scanline at y
         for (int x = x_L; x \le x_R; x++)
            SetPixel(x, y, rgba);
     x_L += dx_L/dy_L;
      x_R += dx_R/dy_R;
                                  dx_{i}
                                                dx_R
```

Triangle Sweep-Line Algorithm



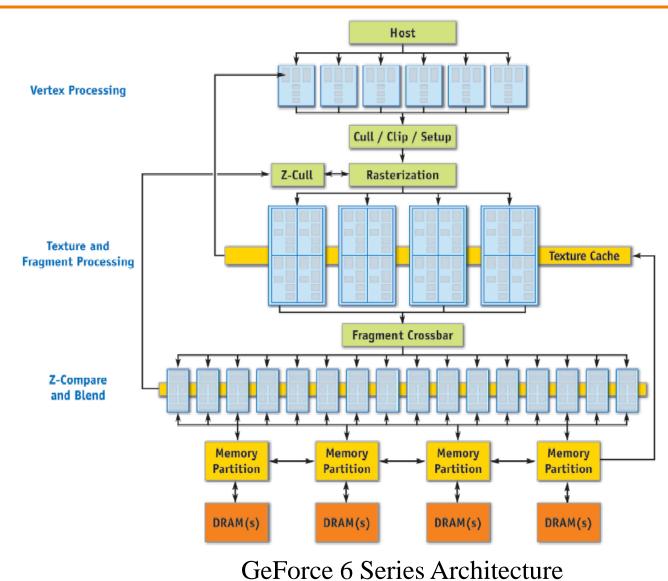
```
void ScanTriangle(Triangle T, Color rgba) {
  for each edge pair {
    initialize x<sub>L</sub>, x<sub>R</sub>;
    compute dx<sub>L</sub>/dy<sub>L</sub> and dx<sub>R</sub>/dy<sub>R</sub>;
    for each scanline at y
        for (int x = x<sub>L</sub>; x <= x<sub>R</sub>; x++)
        SetPixel(x, y, rgba);
    x<sub>L</sub> += dx<sub>R</sub>/dy<sub>L</sub>;
    x<sub>R</sub> += dx<sub>R</sub>/dy<sub>R</sub>;
}
```

Minimize computation in inner loops



GPU Architecture

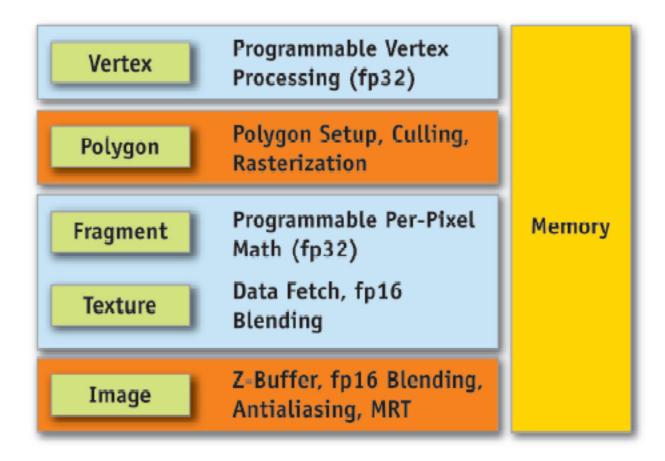




GPU Gems 2, NVIDIA

GPU Architecture





GeForce 6 Series Architecture