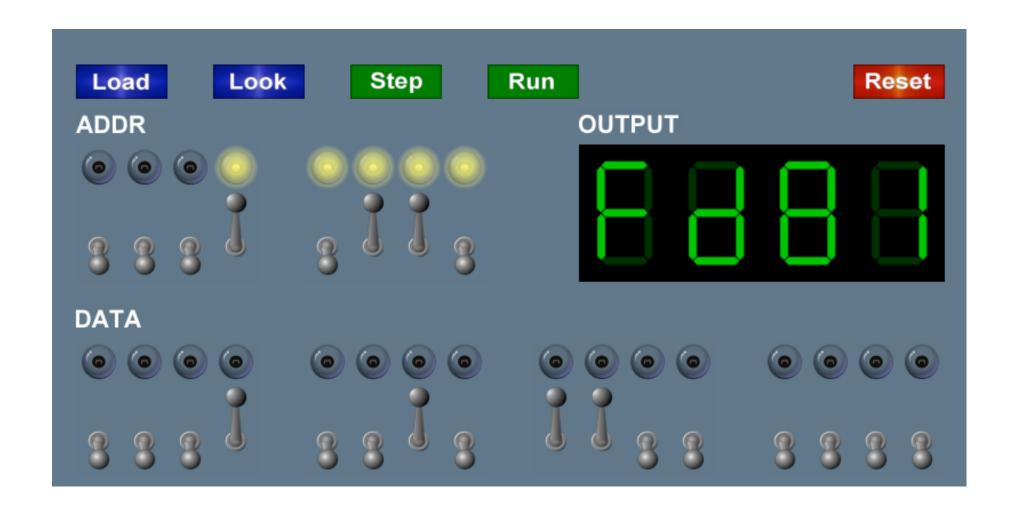


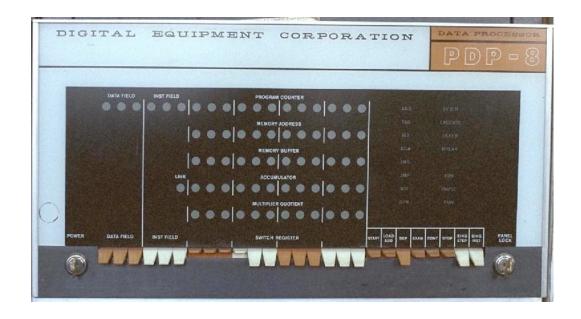
5. The TOY Machine



What is TOY?

An imaginary machine similar to:

- Ancient computers.
- Today's microprocessors.
- And practically everything in between!





Why Study TOY?

Machine language programming.

- How do Java programs relate to computer?
- Key to understanding Java references.
- Still situations today where it is really necessary.

multimedia, computer games, embedded devices, scientific computing, SSE5, AVX

Computer architecture.

- How does it work?
- How is a computer put together?

TOY machine. Optimized for simplicity, not cost or performance.

Inside the Box

Switches. Input data and programs.

Lights. View data.

Memory.

- Stores data and programs.
- 256 16-bit "words."
- Special word for stdin / stdout.

Program counter (PC).

- An extra 8-bit register.
- Keeps track of next instruction to be executed.

Registers.

- Fastest form of storage.
- Scratch space during computation.
- 16 16-bit registers.
- Register 0 is always 0.

Arithmetic-logic unit (ALU). Manipulate data stored in registers.

Standard input, standard output. Interact with outside world.

Data and Programs Are Encoded in Binary

Each bit consists of two states:

- 1 or 0; true or false.
- Switch is on or off; wire has high voltage or low voltage.

Everything stored in a computer is a sequence of bits.

- Data and programs.
- Text, documents, pictures, sounds, movies, executables, . . .



```
M = 77_{10} = 01001101_2 = 4D_{16}

O = 79_{10} = 01001111_2 = 4F_{16}

M = 77_{10} = 01001101_2 = 4D_{16}
```

Binary Encoding

How to represent integers?

- Use binary encoding.
- $Ex: 6375_{10} = 0001100011100111_2$

Dec	Bin
0	0000
1	0001
2	0010
3	0011
4	0100
5	0101
6	0110
7	0111

Dec	Bin
8	1000
9	1001
10	1010
11	1011
12	1100
13	1101
14	1110
15	1111

15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
0	0	0	1	1	0	0	0	1	1	1	0	0	1	1	1

$$6375_{10} = +2^{12} +2^{11}$$

$$+2^7 +2^6 +2^5$$

$$+2^2 +2^1 +2^0$$

Hexadecimal Encoding

How to represent integers?

- Use hexadecimal encoding.
- Binary code, four bits at a time.

• Ex: 6375₁₀ = 0001100011100111₂ = 18E7₁₆

Dec	Bin	Hex	Dec	Bin	Hex
0	0000	0	8	1000	8
1	0001	1	9	1001	9
2	0010	2	10	1010	А
3	0011	3	11	1011	В
4	0100	4	12	1100	С
5	0101	5	13	1101	D
6	0110	6	14	1110	E
7	0111	7	15	1111	F

15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
0	0	0	1	1	0	0	0	1	1	1	0	0	1	1	1
		1			(8]	Ξ				7	

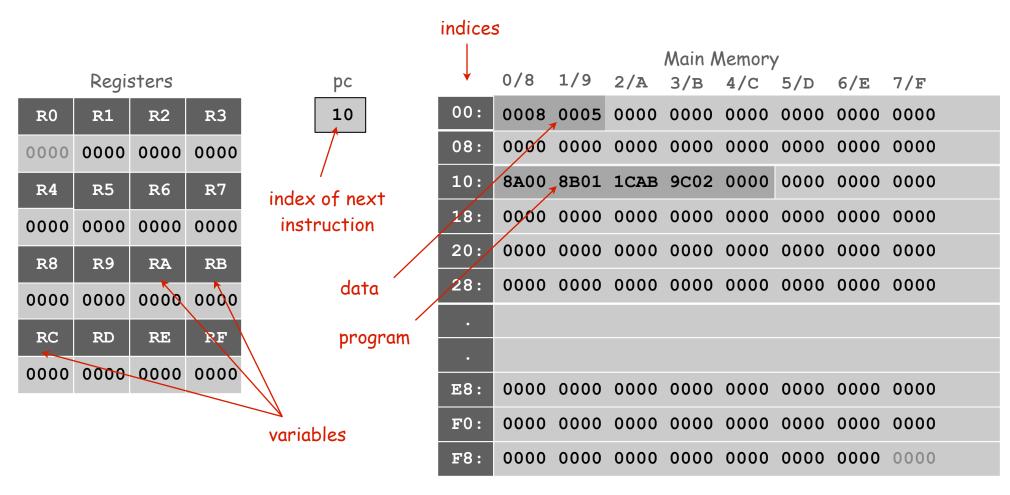
$$6375_{10} = 1 \times 16^{3} + 8 \times 16^{2} + 14 \times 16^{1} + 7 \times 16^{0}$$

$$= 4096 + 2048 + 224 + 7$$

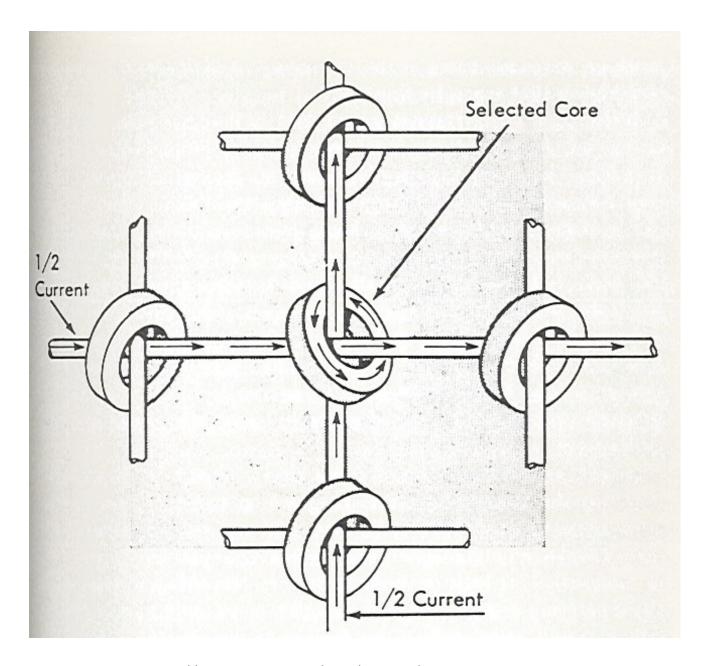
Machine "Core" Dump

Machine contents at a particular place and time.

- Record of what program has done.
- Completely determines what machine will do.



Why do They Call it "Core"?



http://www.columbia.edu/acis/history/core.html

A Sample Program

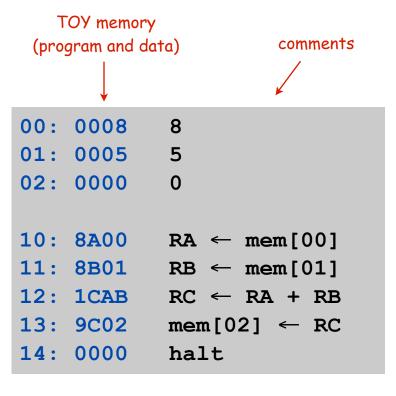
A sample program. Adds 0008 + 0005 = 000D.

RA	RB	RC
0000	0000	0000

Registers



Program counter

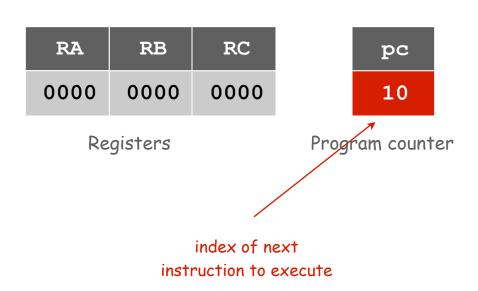


add.toy

TOY code to compute 0008₁₀ + 0005₁₀

A Sample Program

Program counter. The pc is initially 10, so the machine interprets 8A00 as an instruction.



```
00: 0008 8
01: 0005 5
02: 0000 0

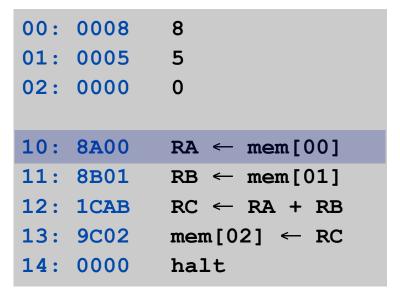
10: 8A00 RA ← mem[00]
11: 8B01 RB ← mem[01]
12: 1CAB RC ← RA + RB
13: 9C02 mem[02] ← RC
14: 0000 halt
```

Load

Load. [opcode 8]

- Loads the contents of some memory location into a register.
- 8A00 means load the contents of memory cell 00 into register A.

RA	RB	RC		pc
0000	0000	0000		10
Re	gisters		Progi	ram counter



15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
1	0	0	0	1	0	1	0	0	0	0	0	0	0	0	0
8 ₁₆ A ₁₆					00 ₁₆										
	opc	ode		dest d							ad	dr			

Load

Load. [opcode 8]

- Loads the contents of some memory location into a register.
- 8B01 means load the contents of memory cell 01 into register B.

RA	RB	RC		рc	
0008	0000	0000		11	
Re	gisters		Progr	ram count	er

00:	8000	8
01:	0005	5
02:	0000	0
10:	8 A 00	$RA \leftarrow mem[00]$
11:	8B01	$RB \leftarrow mem[01]$
12:	1CAB	$RC \leftarrow RA + RB$
13:	9C02	$mem[02] \leftarrow RC$
14:	0000	halt

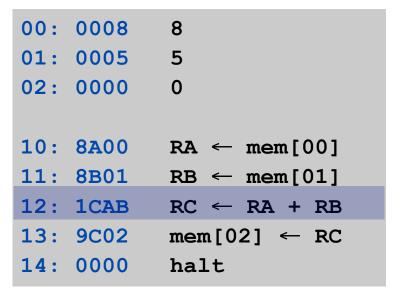
15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
1	0	0	0	1	0	1	1	0	0	0	0	0	0	0	1
8 ₁₆ B ₁₆					01 ₁₆										
	opc	code dest d								ad	dr				

Add

Add. [opcode 1]

- Add contents of two registers and store sum in a third.
- 1CAB means add the contents of registers A and B and put the result into register C.

RA	RB	RC		рc	
0008	0005	0000		12	
Re	gisters		Prog	ram count	er



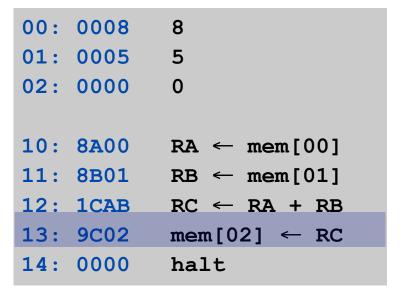
15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
0	0	0	1	1	1	0	0	1	0	1	0	1	0	1	1
	1	16			С	16			A	16			В	16	
	opc	ode			des	t d			sour	ce s			sour	ce t	

Store

Store. [opcode 9]

- Stores the contents of some register into a memory cell.
- 9C02 means store the contents of register C into memory cell 02.

RA	RB	RC		pc	
0008	0005	000D		13	
Re	gisters		Progi	ram count	er



15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0	
1	0	0	1	1	1	0	0	0	0	0	0	0	0	1	0	
	9	16			С	16		02 ₁₆								
	opc	ode			des	t d					ad	dr				

Halt

Halt. [opcode 0]

• Stop the machine.

RA	RB	RC
0008	0005	000D

рс 14

Registers

Program counter

```
00: 0008
              8
01: 0005
              5
02: 000D
              D
10: 8A00
              RA \leftarrow mem[00]
11: 8B01
              RB \leftarrow mem[01]
12: 1CAB
              RC \leftarrow RA + RB
13: 9C02
              mem[02] \leftarrow RC
14: 0000
              halt
```

add.toy

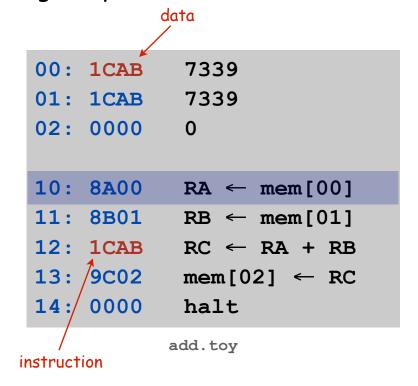
TOY code to compute 0008₁₀ + 0005₁₀

Same Program, Different Data

Program. Sequence of instructions.

Instruction addresses. 10, 11, 12, 13, and 14 (executed when pc points to it). Data addresses. 00, 01, and 02 (used and changed by instructions).

RA	RB	RC		pc	
0000	0000	0000		10	
Re	gisters	Progi	ram count	er	



$$1CAB_{16} = 1 \times 16^{3}$$
 $+ 12 \times 16^{2}$
 $+ 10 \times 16^{1}$
 $+ 11 \times 16^{0}$
 $= 4096 + 3072 + 160 + 11 = 100$

TOY code to compute 7339₁₀ + 7339₁₀

7339₁₀

Load

Load. [opcode 8]

- Loads the contents of some memory location into a register.
- 8A00 means load the contents of memory cell 00 into register A.

RA	RB	RC		рc	
0000	0000	0000		10	
Re	gisters		Prog	ram counte	er

00:	1CAB	7339
01:	1CAB	7339
02:	0000	0
10:	8 A 00	$RA \leftarrow mem[00]$
11:	8B01	$RB \leftarrow mem[01]$
12:	1CAB	$RC \leftarrow RA + RB$
13:	9C02	$mem[02] \leftarrow RC$
14:	0000	halt

15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0	
1	0	0	0	1	0	1	0	0	0	0	0	0	0	0	0	
	8	16			A	16		00 ₁₆								
	opc	ode			des	t d		addr								

Load

Load. [opcode 8]

- Loads the contents of some memory location into a register.
- 8B01 means load the contents of memory cell 01 into register B.

RA	RB	RC		рc	
1CAB	0000	0000		11	
Re	gisters		Prog	ram counte	er

00:	1CAB	7339
01:	1CAB	7339
02:	0000	0
10:	8 A 00	$RA \leftarrow mem[00]$
11:	8B01	RB ← mem[01]
12:	1CAB	RC ← RA + RB
13:	9C02	$mem[02] \leftarrow RC$
14:	0000	halt

15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0	
1	0	0	0	1	0	1	1	0	0	0	0	0	0	0	1	
	8	16			В	16		01 ₁₆								
	opc	ode			des	t d					ad	dr				

Add

Add. [opcode 1]

- Add contents of two registers and store sum in a third.
- 1CAB means add the contents of registers A and B and put the result into register C.

RA	RB	RC		рc	
1CAB	1CAB	0000		12	
Re	gisters		Progi	ram count	er

00:	1CAB	7339
01:	1CAB	7339
02:	0000	0
10:	8 A 00	$RA \leftarrow mem[00]$
11:	8B01	RB ← mem[01]
12:	1CAB	RC ← RA + RB
13:	9C02	$mem[02] \leftarrow RC$
14:	0000	halt

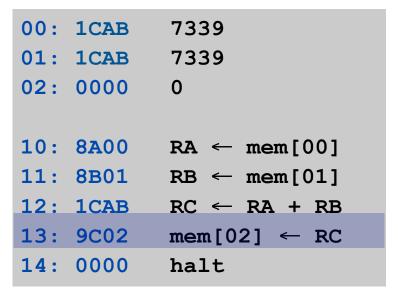
15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
0	0	0	1	1	1	0	0	1	0	1	0	1	0	1	1
	1	16			С	16			A	16			В	16	
	opc	ode			des	t d			sour	ce s			sour	ce t	

Store

Store. [opcode 9]

- Stores the contents of some register into a memory cell.
- 9C02 means store the contents of register C into memory cell 02.

RA	RB	RC		pc
1CAB	1CAB	3956		13
Re	gisters		Prog	ram counter



15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
1	0	0	1	1	1	0	0	0	0	0	0	0	0	1	0
	9	16			С	16					02	216			
opcode dest d										ad	dr				

Halt

Halt. [opcode 0]

• Stop the machine.

RA	RB	RC
1CAB	1CAB	3956

14

Registers

Program counter

```
00: 1CAB
               7339
01: 1CAB
               7339
02: 3956
              14678
10: 8A00
              RA \leftarrow mem[00]
11: 8B01
              RB \leftarrow mem[01]
12: 1CAB
              RC \leftarrow RA + RB
13: 9C02
              mem[02] \leftarrow RC
14: 0000
              halt
```

Program and Data

Program. Sequence of 16-bit integers, interpreted one way.

Data. Sequence of 16-bit integers, interpreted another way.

Program counter (pc). Holds memory address of the "next instruction" and determines which integers get interpreted as instructions.

16 instruction types. Changes contents of registers, memory, and pc in specified, well-defined ways.

Instructions

\rightarrow	0:	halt
\rightarrow	1:	add
	2:	subtract
	3:	and
	4:	xor
	5:	shift left
	6:	shift right
	7:	load address
\rightarrow	8:	load
\rightarrow	9:	store
	A:	load indirect
	в:	store indirect
	C:	branch zero
	D:	branch positive
	E:	jump register
	F:	jump and link

TOY Instruction Set Architecture

TOY instruction set architecture (ISA).

- Interface that specifies behavior of machine.
- 16 register, 256 words of main memory, 16-bit words.
- 16 instructions.

Each instruction consists of 16 bits.

- Bits 12-15 encode one of 16 instruction types or opcodes.
- Bits 8-11 encode destination register d.
- Bits 0-7 encode:

[Format 1] source registers s and t

[Format 2] 8-bit memory address or constant

15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
1	0	1	1	1	0	1	0	0	0	0	0	0	1	0	0
	opc	ode			des	t d			sour	ce s			sour	ce t	
opcode					des	t d					ad	ldr			

Format 1

Format 2

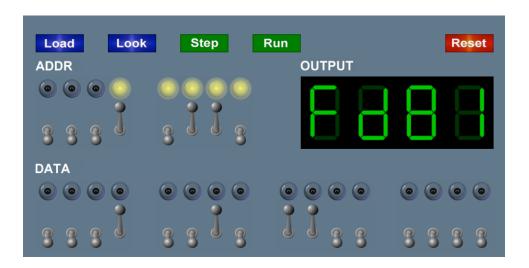
Interfacing with the TOY Machine

To enter a program or data:

- Set 8 memory address switches.
- Set 16 data switches.
- Press Load: data written into addressed word of memory.

To view the results of a program:

- Set 8 memory address switches.
- Press Look: contents of addressed word appears in lights.



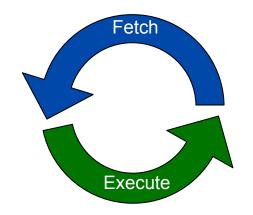
Interfacing with the TOY Machine

To execute the program:

- Set 8 memory address switches to address of first instruction.
- Press Look to set pc to first instruction.
- Press Run to repeat fetch-execute cycle until halt opcode.

Fetch-execute cycle.

- Fetch: get instruction from memory.
- Execute: update pc, move data to or from memory and registers, perform calculations.





Flow Control

Flow control.

- To harness the power of TOY, need loops and conditionals.
- Manipulate pc to control program flow.

Branch if zero. [opcode C]

- Changes pc depending on whether value of some register is zero.
- Used to implement: for, while, if-else.

Branch if positive. [opcode D]

- Changes pc depending on whether value of some register is positive.
- Used to implement: for, while, if-else.

An Example: Multiplication

Multiply. Given integers a and b, compute $c = a \times b$.

TOY multiplication. No direct support in TOY hardware.

Brute-force multiplication algorithm:

- Initialize c to 0.
- Add b to c, a times.

```
int a = 3;
int b = 9;
int c = 0;

while (a != 0) {
   c = c + b;
   a = a - 1;
}
```

brute force multiply in Java

Issues ignored. Slow, overflow, negative numbers.

Multiply

```
0A: 0003
                        ← inputs
       OB: 0009
                   0
       OC: 0000
                         output
       OD: 0000
                       ← constants
       OE: 0001
       10: 8A0A RA \leftarrow mem[0A]
                                                   a
       11: 8B0B RB \leftarrow mem[0B]
                                                   b
       12: 8COD RC \leftarrow mem[OD]
                                                  c = 0
       13: 810E R1 \leftarrow mem[0E]
                                                  always 1
       14: CA18 if (RA == 0) pc \leftarrow 18 while (a != 0) {
       15: 1CCB RC \leftarrow RC + RB
                                                     c = c + b
loop
       16: 2AA1 RA \leftarrow RA - R1
                                                     a = a - 1
       17: C014
                pc ← 14
       18: 9C0C mem[0C] \leftarrow RC
       19: 0000
                  halt
```

Step-By-Step Trace

		<u>R1</u>	_RA_	_RB_	_RC
10: 8A0A	RA ← mem[OA]		0003		
11: 8B0B	RB ← mem[OB]			0009	
12: 8COD	RC ← mem[OD]				0000
13: 810E	R1 ← mem[OE]	0001			
14: CA18	if (RA == 0) pc ← 18				
15: 1CCB	RC ← RC + RB				0009
16: 2AA1	$RA \leftarrow RA - R1$		0002		
17: C014	pc ← 14				
14: CA18	if (RA == 0) pc ← 18				
15: 1CCB	RC ← RC + RB				0012
16: 2AA1	$RA \leftarrow RA - R1$		0001		
17: C014	pc ← 14				
14: CA18	if (RA == 0) pc \leftarrow 18				
15: 1CCB	RC ← RC + RB				001B
16: 2AA1	$RA \leftarrow RA - R1$		0000		
17: C014	pc ← 14				
14: CA18	if (RA == 0) pc ← 18				
18: 9COC	mem[OC] ← RC				
19: 0000	halt				

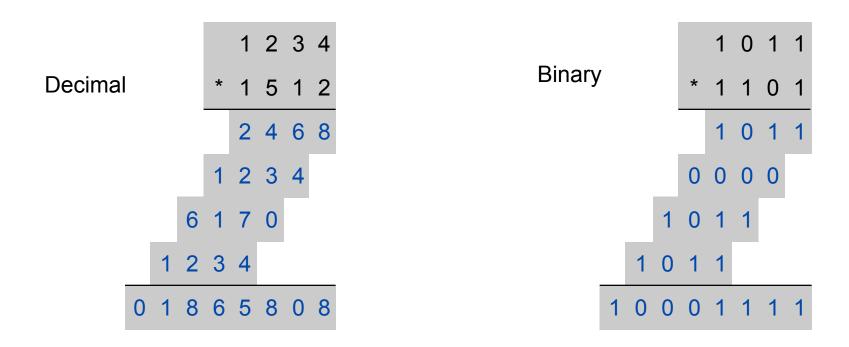
An Efficient Multiplication Algorithm

Inefficient multiply.

- Brute force multiplication algorithm loops a times.
- In worst case, 65,535 additions!

"Grade-school" multiplication.

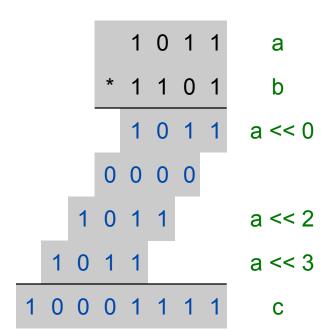
Always 16 additions to multiply 16-bit integers.



Binary Multiplication

Grade school binary multiplication algorithm to compute $c = a \times b$.

- Initialize c = 0.
- Loop over i bits of b.
 - if $b_i = 0$, do nothing $b_i = i^{th}$ bit of b
 - if $b_i = 1$, shift a left i bits and add to c



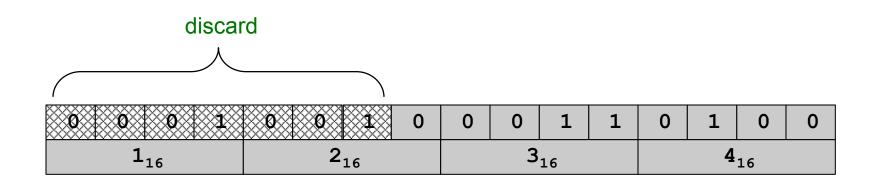
Implement with built-in TOY shift instructions.

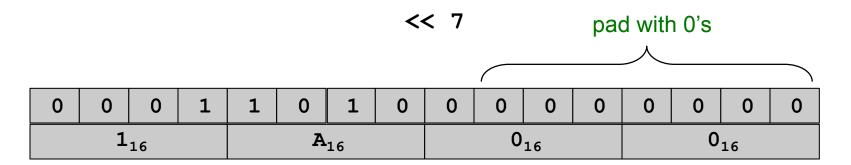
```
int c = 0;
for (int i = 15; i >= 0; i--)
  if (((b >> i) & 1) == 1)
      c = c + (a << i);</pre>
```

Shift Left

Shift left. (opcode 5)

- Move bits to the left, padding with zeros as needed.
- $-1234_{16} << 7_{16} = 1A00_{16}$

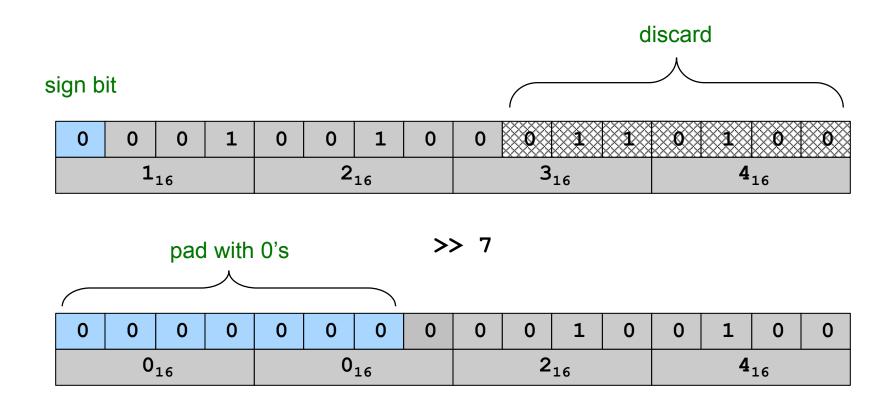




Shift Right

Shift right. (opcode 6)

- Move bits to the right, padding with sign bit as needed.
- \blacksquare 1234₁₆ >> 7₁₆ = 0024₁₆



Bitwise AND

Logical AND. (opcode B)

- Logic operations are BITWISE.
- \bullet 0024₁₆ & 0001₁₆ = 0000₁₆

x	У	&
0	0	0
0	1	0
1	0	0
1	1	1

0	0	0	0	0	0	0	0	0	0	1	0	0	1	0	0		
	0	16			0	16		2 ₁₆ 4 ₁₆									
&																	
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1		
	0	16			0	16			0	16			1	16			
							:	=									
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0		
	0 ₁₆					0 ₁₆				0 ₁₆				0 ₁₆			

Shifting and Masking

Shift and mask: get the 7th bit of 1234.

- Compute $1234_{16} >> 7_{16} = 0024_{16}$.
- Compute $0024_{16} \& 1_{16} = 0_{16}$.

0	0	0	1	0	0	1	0	0	0	1	1	0	1	0	0
1 ₁₆					2	16			3	16			4	16	

>> 7

0	0	0	0	0	0	0	0	0	0	1	0	0	1	0	0
0 ₁₆					0	16			2	16			4	16	

æ

0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1
	0	16		0 ₁₆					0	16		1 ₁₆			

=

0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	0	16			0 ₁₆				0	16		0 ₁₆			

Binary Multiplication

```
0A: 0003
                              inputs
      OB: 0009
                    0
                              output
      OC: 0000
      OD: 0000
                              constants
                        —
                    1
      OE: 0001
      OF: 0010
                   16
      10: 8A0A RA \leftarrow mem[0A]
                                                   a
      11: 8B0B RB \leftarrow mem[0B]
                                                   b
      12: 8COD RC \leftarrow mem[OD]
                                                  c = 0
      13: 810E R1 \leftarrow mem[0E]
                                               always 1
      14: 820F R2 \leftarrow mem[0F]
                                                   i = 16 \leftarrow 16 bit words
                                                   do {
 loop
       15: 2221 R2 \leftarrow R2 - R1
      16: 53A2 R3 \leftarrow RA << R2
                                                       a << i
      17: 64B2 R4 \leftarrow RB >> R2
                                                      b >> i
      18: 3441 R4 \leftarrow R4 \& R1
                                                   b_i = i^{th} bit of b
branch
       19:) C41B
                                                   if b; is 1
                if (R4 == 0) goto 1B
       1A: 1CC3 RC \leftarrow RC + R3
                                                          add a << i to sum
          D215
                   if (R2 > 0) goto 15 } while (i > 0);
      1C: 9COC mem[OC] \leftarrow RC
```

TOY Reference Card

	15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
Format 1	1 opcode				dest d					sour	ce s		source t			
Format 2	at 2 opcode				dest d				addr							

#	Operation	Fmt	Pseudocode
0:	halt	1	exit(0)
1:	add	1	$R[d] \leftarrow R[s] + R[t]$
2:	subtract	1	$R[d] \leftarrow R[s] - R[t]$
3:	and	1	$R[d] \leftarrow R[s] \& R[t]$
4:	xor	1	$R[d] \leftarrow R[s] ^ R[t]$
5:	shift left	1	$R[d] \leftarrow R[s] \ll R[t]$
6:	shift right	1	$R[d] \leftarrow R[s] \gg R[t]$
7:	load addr	2	R[d] ← addr
8:	load	2	R[d] ← mem[addr]
9:	store	2	mem[addr] ← R[d]
A:	load indirect	1	$R[d] \leftarrow mem[R[t]]$
В:	store indirect	1	$mem[R[t]] \leftarrow R[d]$
C:	branch zero	2	if $(R[d] == 0)$ pc \leftarrow addr
D:	branch positive	2	if $(R[d] > 0)$ pc \leftarrow addr
E:	jump register	2	pc ← R[d]
F:	jump and link	2	R[d] ← pc; pc ← addr

Register 0 always 0. Loads from mem[FF] from stdin. Stores to mem[FF] to stdout.

Useful TOY "Idioms"

Jump absolute.

- Always jump to a fixed memory address.
 - -branch if zero with register 0 and destination
 - -register 0 is always 0

17: C014 pc ← 14

Register copy (or move).

- No instruction that transfers contents of one register into another.
- Pseudo-instruction that simulates copy:
 - add with register 0 as one of two source registers

17: 1230 $R[2] \leftarrow R[3]$

No-op.

- Instruction that does nothing.
- Plays the role of whitespace in C programs.
 - numerous other possibilities!

17: 1000 no-op

A Little History

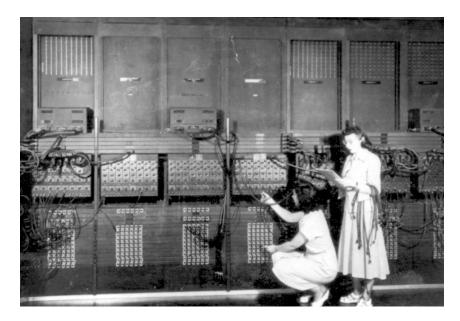
Electronic Numerical Integrator and Calculator (ENIAC).

- First widely known general purpose electronic computer.
- Conditional jumps, programmable.
- Programming: change switches and cable connections.
- Data: enter numbers using punch cards.

30 tons $30 \times 50 \times 8.5 \text{ ft}$ 17,468 vacuum tubes300 multiply/sec



John Mauchly (left) and J. Presper Eckert (right) http://cs.swau.edu/~durkin/articles/history_computing.html



ENIAC, Ester Gerston (left), Gloria Gordon (right)
US Army photo: http://ftp.arl.mil/ftp/historic-computers

ENIAC



Basic Characteristics of TOY Machine

TOY is a general-purpose computer.

- Sufficient power to perform ANY computation.
- Limited only by amount of memory and time.

Stored-program computer. [von Neumann memo, 1944]

- Data and program encoded in binary.
- Data and program stored in SAME memory.
- Can change program without rewiring.

Outgrowth of Alan Turing's work. (stay tuned)

All modern computers are general-purpose computers and have same (von Neumann) architecture.



John von Neumann



Maurice Wilkes (left)
EDSAC (right)

Harvard vs. Princeton

Harvard architecture.

- Separate program and data memories.
- Can't load game from disk (data) and execute (program).
- Used in some microcontrollers.



Von Neumann architecture.

- Program and data stored in same memory.
- Used in almost all computers.



- Q. What's the difference between Harvard and Princeton?
- A. At Princeton, data and programs are the same.