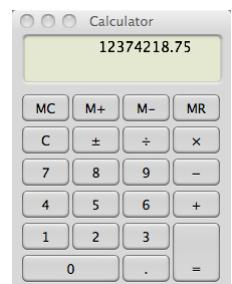
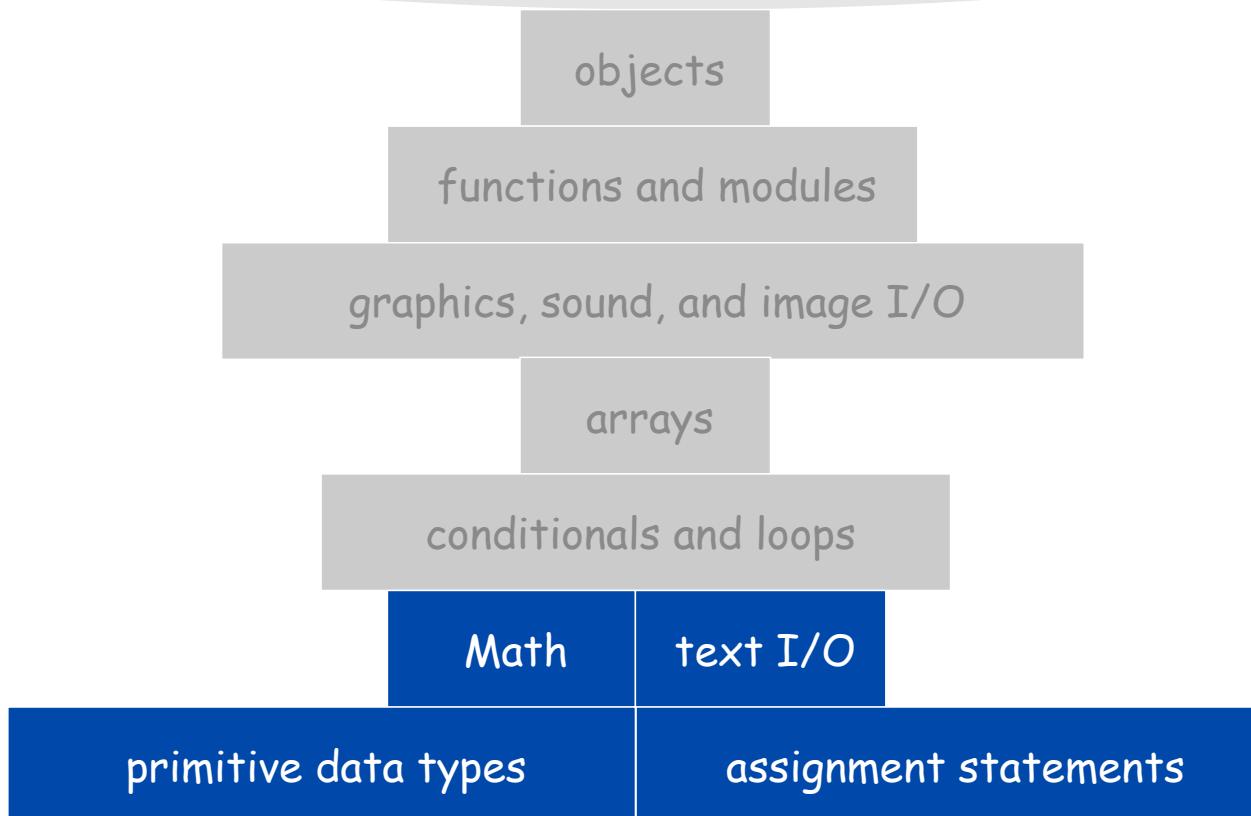


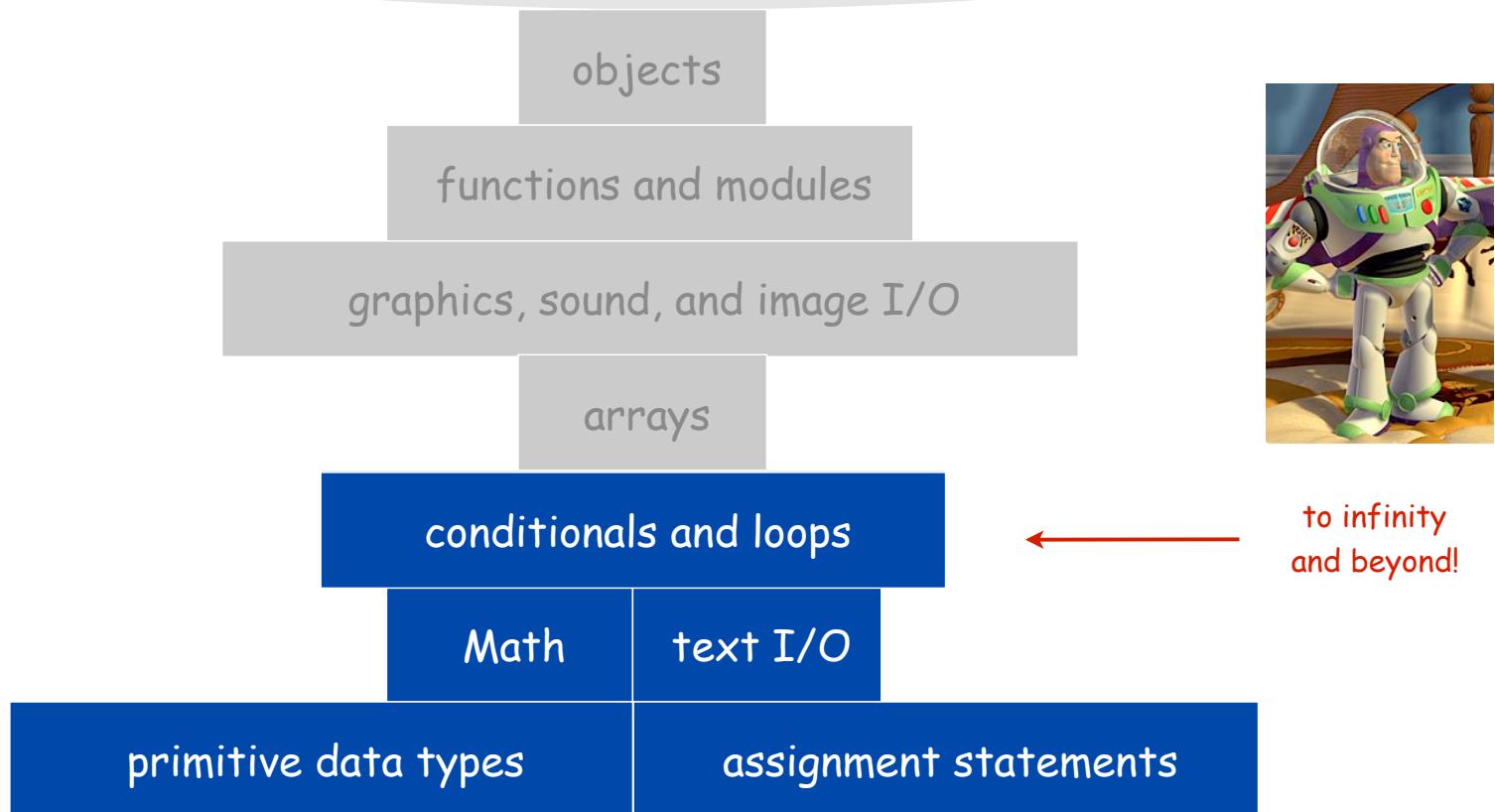
1.3 Conditionals and Loops

any program you might want to write



1.3 Conditionals and Loops

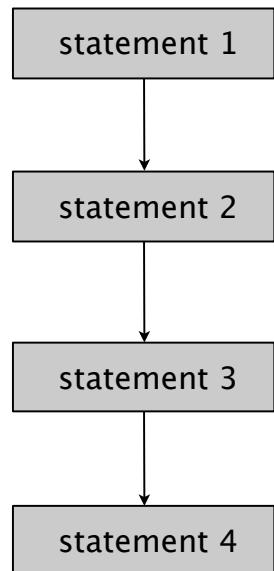
any program you might want to write



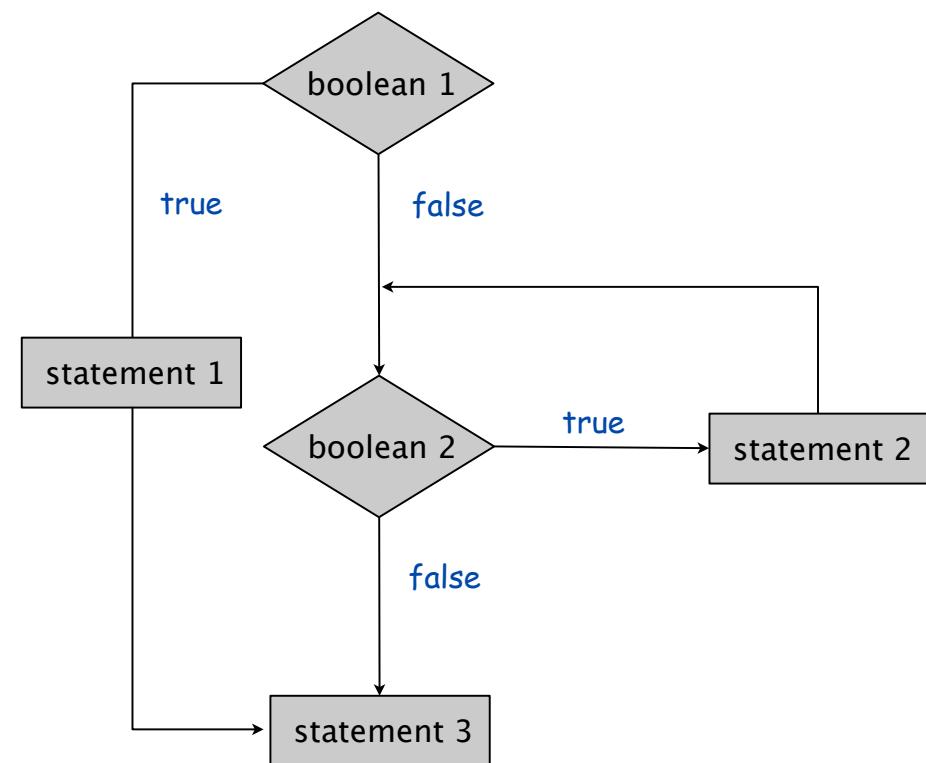
Conditionals and Loops

Control flow.

- Sequence of statements that are actually executed in a program.
- Conditionals and loops: enable us to choreograph control flow.



straight-line control flow



control flow with conditionals and loops

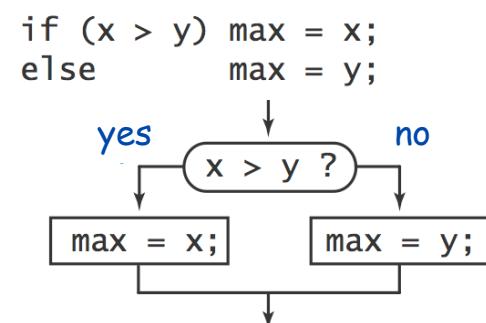
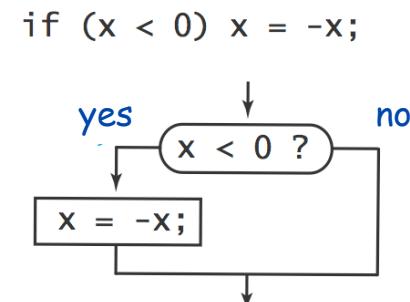
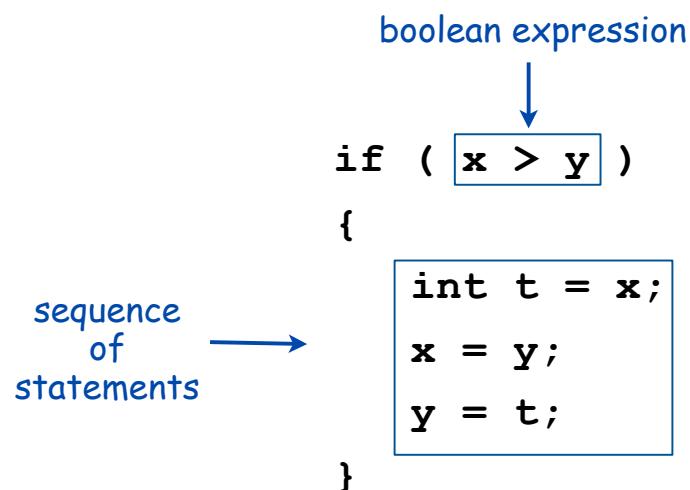
Conditionals



If Statement

The `if` statement. A common branching structure.

- Evaluate a boolean expression.
- If true, execute some statements.
- `else` option: If false, execute other statements.



If Statement

Ex. Take different action depending on value of variable.

```
public class Flip
{
    public static void main(String[] args)
    {
        if (Math.random() < 0.5)
            System.out.println("Heads");
        else System.out.println("Tails");
    }
}
```



```
% java Flip
Heads

% java Flip
Heads

% java Flip
Tails

% java Flip
Heads
```

If Statement Examples

```
if (x < 0) x = -x;
```

absolute value

```
if (x > y) max = x;  
else max = y;
```

maximum

```
if (x > y)  
{  
    int t = x;  
    x = y;  
    y = t;  
}
```

2-sort

$x > y$ before

x	y	t
1234	99	undefined
1234	99	1234
99	99	1234
99	1234	1234

$x < y$ after

```
if (den == 0) System.out.println("Division by zero");  
else System.out.println("Quotient = " + num/den);
```

error check for division operation

```
double discriminant = b*b - 4.0*c;  
if (discriminant < 0.0)  
{  
    System.out.println("No real roots");  
}  
else  
{  
    System.out.println((-b + Math.sqrt(discriminant))/2.0);  
    System.out.println((-b - Math.sqrt(discriminant))/2.0);  
}
```

error check for quadratic formula

Loops

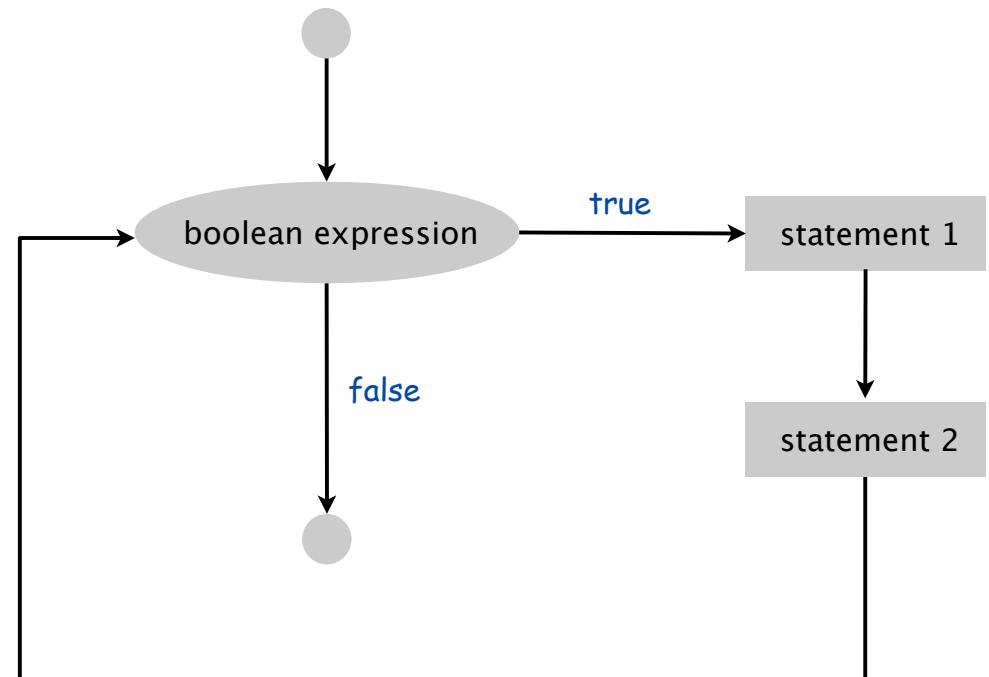


While Loop

The `while` loop. A common repetition structure.

- • Check a boolean expression.
- Execute a sequence of statements.
- Repeat.

```
loop continuation condition  
while (boolean expression)  
{  
    statement 1;  
    statement 2; ← loop body  
}
```



While Loop Example: Powers of Two

Ex. Print powers of 2 that are $\leq 2^n$.

- Increment **i** from 0 to **n**.
- Double **v** each time.

```
int i = 0;
int v = 1;
while (i <= n)
{
    System.out.println(v);
    i = i + 1;
    v = 2 * v;
}
```

i	v	i <= n
0	1	true
1	2	true
2	4	true
3	8	true
4	16	true
5	32	true
6	64	true
7	128	false

```
1
2
4
8
16
32
64
```

n = 6

Powers of Two (full program)

```
public class PowersOfTwo
{
    public static void main(String[] args)
    {

        // last power of two to print
        int n = Integer.parseInt(args[0]);

        int i = 0;    // loop control counter
        int v = 1;    // current power of two
        while (i <= n)
        {
            System.out.println(v);
            i = i + 1;
            v = 2 * v;
        }
    }
}
```

```
% java PowersOfTwo 3
```

```
1  
2  
4  
8
```

```
% java PowersOfTwo 6
```

```
1  
2  
4  
8  
16  
32  
64
```

While Loop Challenge

Anything wrong with the following code?

```
public class PowersOfTwo {  
    public static void main(String[] args) {  
        int N = Integer.parseInt(args[0]);  
        int i = 0; // loop control counter  
        int v = 1; // current power of two  
        while (i <= N)  
            System.out.println(v);  
            i = i + 1;  
            v = 2 * v;  
    }  
}
```

While Loop Example: Square Root

Goal. Implement `Math.sqrt()`.

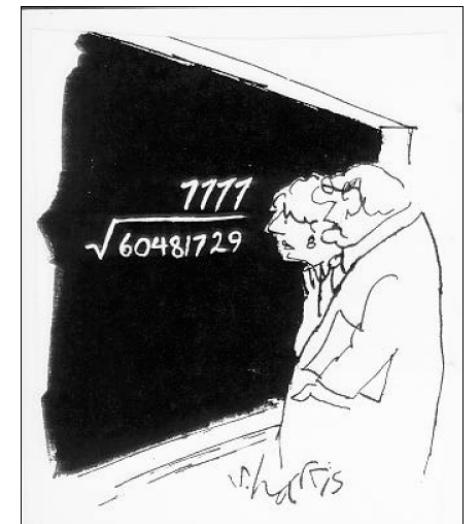
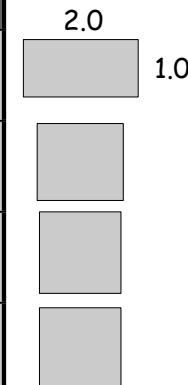
```
% java Sqrt 60481729  
7777.0
```

Newton-Raphson method to compute the square root of c :

- Initialize $t_0 = c$.
- Repeat until $t_i = c / t_i$, up to desired precision:
set t_{i+1} to be the average of t_i and c / t_i .

i	t_i	$2/t_i$	average
0	2.0	1.0	1.5
1	1.5	1.3333333	1.4166667
2	1.4166667	1.4117647	1.4142157
3	1.4142157	1.4142114	1.4142136
4	1.4142136	1.4142136	

computing the square root of 2 to seven places



"A wonderful square root. Let's hope it can be used for the good of mankind."

Copyright 2004, Sidney Harris
<http://www.sciencecartoonsplus.com>

While Loop Example: Square Root

Goal. Implement `Math.sqrt()`.

Newton-Raphson method to compute the square root of c :

- Initialize $t_0 = c$.
- Repeat until $t_i = c / t_i$, up to desired precision:
set t_{i+1} to be the average of t_i and c / t_i .

```
public class Sqrt
{
    public static void main(String[] args)
    {
        double EPS = 1E-15;
        double c = Double.parseDouble(args[0]);
        double t = c;
        while (Math.abs(t - c/t) > t*EPS)
        {   t = (c/t + t) / 2.0;   }
        System.out.println(t);
    }
}
```

% java Sqrt 2.0

1.414213562373095

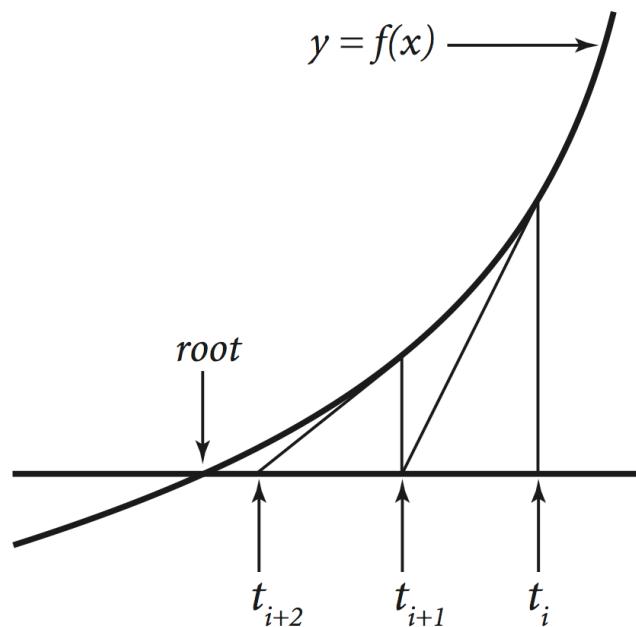
error tolerance

15 decimal digits of accuracy in 5 iterations

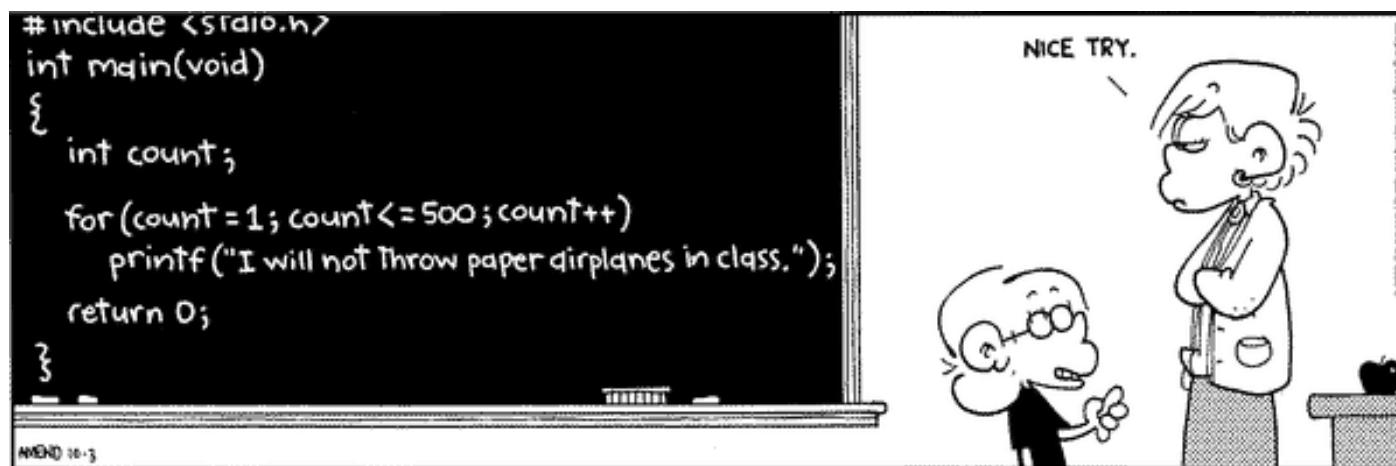
Newton-Raphson Method

Square root method explained (some math omitted).

- Goal: find root of function $f(x)$.
- Start with estimate t_0 .
- Draw line tangent to curve at $x = t_i$.
- Set t_{i+1} to be x -coordinate where line hits x -axis.
- Repeat until desired precision.



The For Loop



Copyright 2004, FoxTrot by Bill Amend
www.ucomics.com/foxtrot/2003/10/03

The For Loop

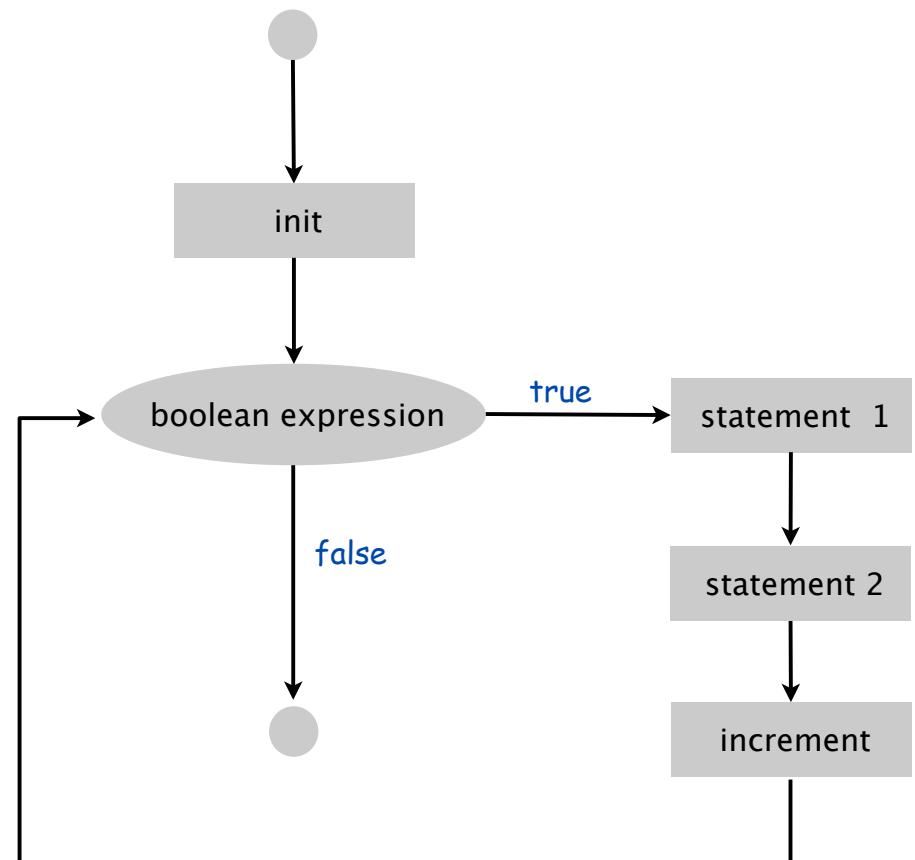
The **for** loop. Another common repetition structure.

- Execute initialization statement.
- Check boolean expression.
- Execute sequence of statements.
- Execute increment statement.
- Repeat.

```
for (init; boolean expression; increment)
{
    statement 1;
    statement 2;
}
```

loop continuation condition

body



Anatomy of a for Loop

```
int v = 1;  
for ( int i = 0; i <= N; i++ )  
{  
    System.out.println( i + " " + v );  
    v = 2*v;  
}
```

initialize another variable in a separate statement → `int v = 1;`

declare and initialize a loop control variable → `int i = 0`

loop continuation condition → `i <= N`

increment → `i++`

body → `System.out.println(i + " " + v);
v = 2*v;`

prints table of powers of two

Anatomy of a for Loop

```
int v = 1;
for ( int i = 0; i <= N; i++ )
{
    System.out.println( i + " " + v );
    v = 2*v;
}
```

v	i	output
1		
1	0	
1	0	0 1
2	0	
2	1	
2	1	1 2
4	1	
4	2	
4	2	2 4
8	2	
8	3	
8	3	3 8

Every **for** loop has an equivalent **while** loop

```
int v = 1;
int i = 0;
while ( i <= N; )
{
    System.out.println( i + " " + v );
    v = 2*v;
    i++;
}
```

Why **for** loops? Can provide more compact and understandable code.

For Loops: Subdivisions of a Ruler

Create subdivision of a ruler.

- Initialize `ruler` to **single space**.
- For each value `i` from 1 to `N`:
sandwich two copies of `ruler` on either side of `i`.

```
public class Ruler
{
    public static void main(String[] args)
    {
        int N = Integer.parseInt(args[0]);
        String ruler = " ";
        for (int i = 1; i <= N; i++)
            ruler = ruler + i + ruler;
        System.out.println(ruler);
    }
}
```

i	ruler
1	" 1 "
2	" 1 2 1 "
3	" 1 2 1 3 1 2 1 "

end-of-loop trace

For Loops: Subdivisions of a Ruler

```
% java Ruler 1  
1  
  
% java Ruler 2  
1 2 1  
  
% java Ruler 3  
1 2 1 3 1 2 1  
  
% java Ruler 4  
1 2 1 3 1 2 1 4 1 2 1 3 1 2 1  
  
% java Ruler 5  
1 2 1 3 1 2 1 4 1 2 1 3 1 2 1 5 1 2 1 3 1 2 1 4 1 2 1 3 1 2 1  
  
% java Ruler 100  
Exception in thread "main"  
java.lang.OutOfMemoryError
```

$$2^{100} - 1 = 1,267,650,600,228,229,401,496,703,205,375 \text{ integers in output}$$

Observation. Loops can produce a huge amount of output!

Loop Examples

```
int sum = 0;  
for (int i = 1; i <= N; i++)  
    sum += i;  
System.out.println(sum);
```

compute sum $(1 + 2 + 3 + \dots + N)$

<u>sum</u>	<u>i</u>
1	1
3	2
6	3
10	4

← trace at end of loop for $N = 4$

```
int product = 1;  
for (int i = 1; i <= N; i++)  
    product *= i;  
System.out.println(product);
```

compute $N!$ $(1 * 2 * 3 * \dots * N)$

<u>product</u>	<u>i</u>
1	1
2	2
6	3
24	4

$N = 4$

```
for (int i = 0; i <= N; i++)  
    System.out.println(i + " " + 2*Math.PI*i/N);
```

print a table of function values

0	0.0
1	1.57079632...
2	3.14159265...
3	4.71238898...
4	6.28318530...

```
int v = 1;  
while (v <= N/2)  
    v = 2*v;  
System.out.println(v);
```

print largest power of 2 less than or equal to N

<u>v</u>
2
4
8
16

← trace at end of loop for $N = 23$

Nesting



Nesting Conditionals and Loops

Nesting. Use a conditional or a loop within a conditional or a loop

- Enables complex control flows.
- Adds to challenge of debugging.

Any "statement" within a conditional or loop
may itself be a conditional or a loop statement

```
for (int i = 0; i < trials; i++)
{
    int t = stake;
    while (t > 0 && t < goal)
        if (Math.random() < 0.5) t++;
        else                         t--;
    if (t == goal) wins++;
}
```

if-else statement
within a while loop
within a for loop

Nested If Statements

Ex. Pay a certain tax rate depending on income level.

Income	Rate
0 - 47,450	22%
47,450 - 114,650	25%
114,650 - 174,700	28%
174,700 - 311,950	33%
311,950 -	35%

5 mutually exclusive
alternatives

Nested If-Else Statements

Need all those braces? Not always:

```
if      (income < 47450) rate = 0.22;
else if (income < 114650) rate = 0.25;
else if (income < 174700) rate = 0.28;
else if (income < 311950) rate = 0.33;
else                      rate = 0.35;
```

is shorthand for

```
if (income < 47450) rate = 0.22;
else
{
    if (income < 114650) rate = 0.25;
    else
    {
        if (income < 174700) rate = 0.28;
        else
        {
            if (income < 311950) rate = 0.33;
            else                  rate = 0.35;
        }
    }
}
```

but BE CAREFUL when nesting if-else statements (see Q&A p. 75).

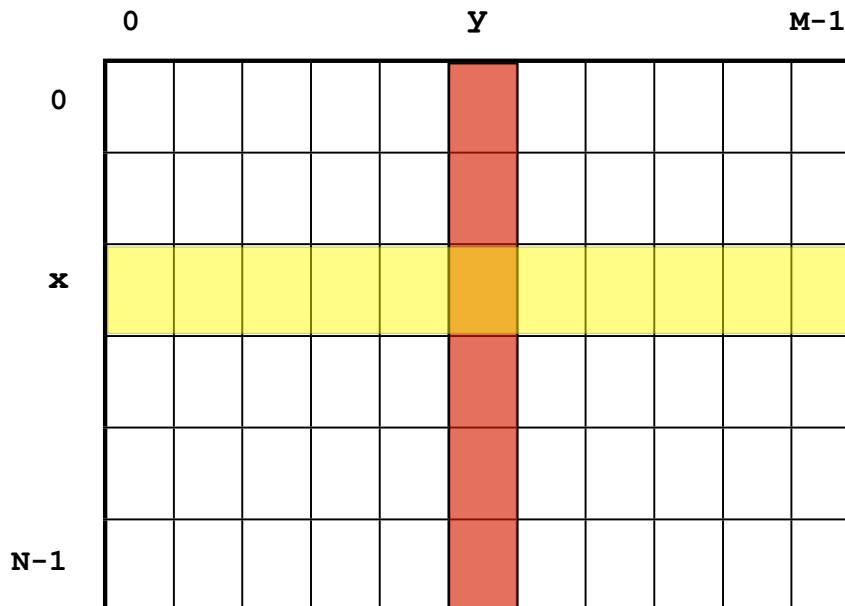
Nested If Statement Challenge

Anything wrong with the following code?

```
double rate = 0.35;  
if (income < 47450) rate = 0.22;  
if (income < 114650) rate = 0.25;  
if (income < 174700) rate = 0.28;  
if (income < 311950) rate = 0.33;
```

Nested for loops

Ex. Visit each location in a two-dimensional table (stay tuned for arrays).



```
for (x = 0; x < N; x++)
    for (y = 0; y < M; y++)
        Do something at entry (x,y);
```

Nesting Example: Gambler's Ruin

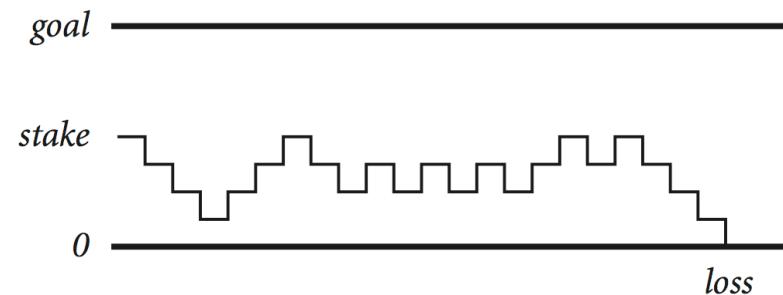
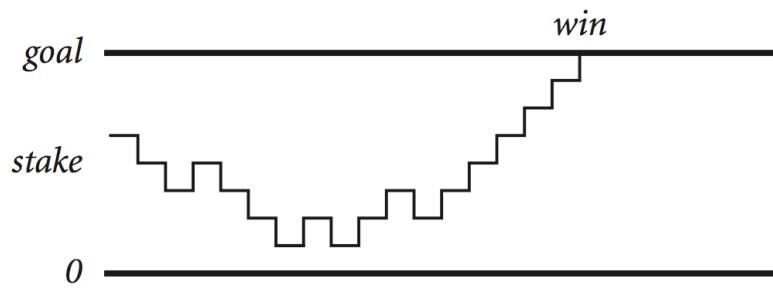
Gambler's ruin. Gambler starts with \$stake and places \$1 fair bets until going broke or reaching \$goal.

- What are the chances of winning?
- How many bets will it take?



One approach. Monte Carlo simulation.

- Flip digital coins and see what happens.
- Repeat and compute statistics.



Nesting Example: Gambler's Ruin Simulation

```
public class Gambler
{
    public static void main(String[] args)
    {
        // Get parameters from command line.
        int stake = Integer.parseInt(args[0]);
        int goal = Integer.parseInt(args[1]);
        int trials = Integer.parseInt(args[2]);

        // Count wins among args[2] trials.
        int wins = 0;
        for (int i = 0; i < trials; i++)
        {
            // Do one gambler's ruin experiment.
            int t = stake;
            while (t > 0 && t < goal)
            {
                // flip coin and update
                if (Math.random() < 0.5) t++;
                else t--;
            }
            if (t == goal) wins++;
        }
        System.out.println(wins + " wins of " + trials);
    }
}
```

if statement
within a while loop
within a for loop

Digression: Simulation and Analysis

```
      stake   goal   trials  
      ↴     ↴     ↴  
% java Gambler 5 25 1000  
191 wins of 1000  
  
% java Gambler 5 25 1000  
203 wins of 1000  
  
% java Gambler 500 2500 1000  
197 wins of 1000
```

after a substantial wait....

Fact. Probability of winning = $\text{stake} \div \text{goal}$.

Fact. Expected number of bets = $\text{stake} \times \text{desired gain}$.

Ex. 20% chance of turning \$500 into \$2500, $500/2500 = 20\%$

but expect to make one million \$1 bets. $500 * (2500 - 500) = 1,000,000$

Remark. Both facts can be proved mathematically.

For more complex scenarios, computer simulation
is often the best plan of attack.



Debugging

Debugging Example

Factor. Given an integer $N > 1$, compute its prime factorization.

$$3,757,208 = 2^3 \times 7 \times 13^2 \times 397$$

$$98 = 2 \times 7^2$$

$$17 = 17$$

Note: 1 is not prime.
(else it would have to
be in every
factorization)

$$11,111,111,111,111,111 = 2,071,723 \times 5,363,222,357$$

Application. Break RSA cryptosystem (factor 200-digit numbers).

Debugging: 99% of Program Development

Programming. A **process** of finding and fixing mistakes.

- Compiler error messages help locate **syntax** errors.
- Run program to find **semantic** and **performance** errors.

Check whether
i is a factor.

```
public class Factors
{
    public static void main(String[] args)
    {
        long N = Long.parseLong(args[0])
        for (i = 0; i < N; i++)
        {
            while (N % i == 0)
                System.out.print(i + " ")
                N = N / i
        }
    }
}
```

if i is a factor
print it and
divide it out

This program has bugs!



Debugging: Syntax Errors

Syntax error. Illegal Java program.

- Compiler error messages help locate problem.
- Goal: no errors and a file named Factors.class.

```
public class Factors
{
    public static void main(String[] args)
    {
        long N = Long.parseLong(args[0])
        for (i = 0; i < N; i++)
        {
            while (N % i == 0)
                System.out.print(i + " ")
            N = N / i
        }
    }
}
```



Debugging: Syntax Errors

Syntax error. Illegal Java program.

- Compiler error messages help locate problem.
- Goal: no errors and a file named Factors.class.

```
public class Factors
{
    public static void main(String[] args)
    {
        long N = Long.parseLong(args[0])
        for (i = 0; i < N; i++)
        {
            while (N % i == 0)
                System.out.print(i + " ")
            N = N / i
        }
    }
}
```

```
% javac Factors.java
Factors.java:6: ';' expected
      for (i = 2; i < N; i++)
      ^
1 error ← the FIRST error
```



Debugging: Syntax Errors

Syntax error. Illegal Java program.

- Compiler error messages help locate problem.
- Goal: no errors and a file named `Factors.class`.

```
public class Factors
{
    public static void main(String[] args)
    {
        long N = Long.parseLong(args[0]) ;
        for ( int i = 0; i < N; i++ )
        {
            while (N % i == 0)
                System.out.print(i + " ") ;
            N = N / i ;
        }
    }
}
```

need to declare variable i

need terminating semicolons

Syntax (compile-time) errors



Debugging: Semantic Errors

Semantic error. Legal but wrong Java program.

- Run program to identify problem.
- Add print statements if needed to produce **trace**.

```
public class Factors
{
    public static void main(String[] args)
    {
        long N = Long.parseLong(args[0]);
        for (int i = 0; i < N; i++)
        {
            while (N % i == 0)
                System.out.print(i + " ");
            N = N / i;
        }
    }
}
```

```
% javac Factors.java
% java Factors ← oops, need argument
Exception in thread "main"
java.lang.ArrayIndexOutOfBoundsException: 0
    at Factors.main(Factors.java:5)
```

you will see this message!



Debugging: Semantic Errors

Semantic error. Legal but wrong Java program.

- Run program to identify problem.
- Add print statements if needed.

```
public class Factors
{
    public static void main(String[] args)
    {
        long N = Long.parseLong(args[0]);
        for (int i = 0; i < N; i++)
        {
            while (N % i == 0)
                System.out.print(i + " ");
            N = N / i;
        }
    }
}
```

```
% javac Factors.java
% % java Factors 98
Exception in thread "main"
java.lang.ArithmetricException: / by zero
at Factors.main(Factors.java:8)
```



Debugging: Semantic Errors

Semantic error. Legal but wrong Java program.

- Run program to identify problem.
- Add print statements if needed.

```
public class Factors
{
    public static void main(String[] args)
    {
        long N = Long.parseLong(args[0]);
        for (int i = 2; i < N; i++)
        {
            while (N % i == 0)
                System.out.print(i + " ");
            N = N / i;
        }
    }
}
```

need to start at 2 since
0 and 1 cannot be factors



Debugging: Semantic Errors

Semantic error. Legal but wrong Java program.

- Run program to identify problem.
 - Add print statements if needed.



Debugging: Semantic Errors

Semantic error. Legal but wrong Java program.

- Run program to identify problem.
- Add print statements if needed.

```
public class Factors
{
    public static void main(String[] args)
    {
        long N = Long.parseLong(args[0]);
        for (int i = 2; i < N; i++)
        {
            while (N % i == 0)
                { System.out.print(i + " ");
                  N = N / i;  }
        }
    }
}
```

Semantic (run-time) error:
indents do not imply braces



Debugging: The Beat Goes On

Success? Program factors $98 = 2 \ 7 \ 7$.

- Time to try it for other inputs.
- Add **trace** to find and fix (minor) problems.

```
public class Factors
{
    public static void main(String[] args)
    {
        long N = Long.parseLong(args[0]);
        for (int i = 2; i < N; i++)
        {   // Check whether i is a factor.
            while (N % i == 0)
            {   // If so, print and divide.
                System.out.print(i + " ");
                N = N / i;
            }
        }
    }
}
```

```
% java Factors 98
2 7 7 % ← need newline
% java Factors 5
%           ← ??? no output
% java Factors 6
2 %       ← ??? where's the 3?
```



Debugging: The Beat Goes On

Success? Program factors $98 = 2 \cdot 7^2$.

- Time to try it for other inputs.
- Add `trace` to find and fix (minor) problems.

```
public class Factors
{
    public static void main(String[] args)
    {
        long N = Long.parseLong(args[0]);
        for (int i = 2; i < N; i++)
        {
            while (N % i == 0)
            {
                System.out.println(i + " ");
                N = N / i;
            }
            System.out.println("TRACE " + i + " " + N);
        }
    }
}
```

```
% javac Factors.java
% java Factors 5
TRACE 2 5
TRACE 3 5
TRACE 4 5
% java Factors 6
2
TRACE 2 3
```

AHA!
Print out N
after for loop
(if it is not 1)



Debugging: Success?

Success? Program seems to work

- Add code for corner case, add comments.
- Remove trace to try larger inputs

```
public class Factors
{
    public static void main(String[] args)
    {
        long N = Long.parseLong(args[0]);
        for (int i = 2; i < N; i++)
        {   // Check whether i is a factor.
            while (N % i == 0)
            {   // If so, print and divide.
                // System.out.print(i + " ");
                N = N / i;
            }
            // System.out.println("TRACE " + i + " " + N);
        }
        if (N > 1) System.out.println(N);
        else        System.out.println();
    }
}
```

"Comment out"
trace code
(may need it later)

Corner case:
print largest factor
(and new line)

Time to document code
(if not earlier).

???
%\$%@\$#!
forgot to recompile

```
% java Factors 5
TRACE 2 5
TRACE 3 5
TRACE 4 5
% javac Factors.java
% java Factors 5
5
% java Factors 6
2 3
% java Factors 98
2 7 7
% java Factors 3757208
2 2 2 7 13 13 397
```

Debugging: Performance Errors

Performance error. Correct program, but too slow.

- Are all iterations of inner loop necessary?
- Improve or change underlying **algorithm**.

```
public class Factors
{
    public static void main(String[] args)
    {
        long N = Long.parseLong(args[0]);
        for (int i = 2; i < N; i++)
        {   // Check whether i is a factor.
            while (N % i == 0)
            {   // If so, print and divide.
                System.out.print(i + " ");
                N = N / i;
            }
        }
        if (N > 1) System.out.println(N);
        else        System.out.println();
    }
}
```

```
% java Factors 11111111
11 73 101 137
% java Factors 111111111111
21649 513239
% java Factors 11111111111111
11 239 4649 909091
% java Factors 1111111111111111
2071723
```

very long wait

Debugging: Performance Errors

Performance error. Correct program, but too slow.

- Are all iterations of inner loop necessary?
- Improve or change underlying algorithm.

```
public class Factors
{
    public static void main(String[] args)
    {
        long N = Long.parseLong(args[0]);
        for (int i = 2; i * i < N; i++)
        {   // Check whether i is a factor.
            while (N % i == 0)
                {   // If so, print and divide.
                    System.out.print(i + " ");
                    N = N / i;
                }
        }
        if (N > 1) System.out.println(N);
        else        System.out.println();
    }
}
```

Fixes performance error:
terminate when $i^2 > N$
since no larger factors left

```
% java Factors 11111111
11 73 101 137
% java Factors 111111111111
21649 513239
% java Factors 11111111111111
11 239 4649 909091
% java Factors 1111111111111111
2071723 5363222357
%
```

Debugging: Back to Semantic Errors!

Fresh semantic error. Fast program (now), but new error.

- Was performance fix exactly right?
- Again, consider (possibly new) corner cases.

```
public class Factors
{
    public static void main(String[] args)
    {
        long N = Long.parseLong(args[0]);
        for (int i = 2; i * i < N; i++)
        {   // Check whether i is a factor.
            while (N % i == 0)
            {   // If so, print and divide.
                System.out.print(i + " ");
                N = N / i;
            }
        }
        if (N > 1) System.out.println(N);
        else       System.out.println();
    }
}
```

```
% java Factors 24
2 2 2 3
% java Factors 25
25
% java Factors 49
49
%
```

Can't handle perfect squares!

Debugging: Back to Semantic Errors!

Fresh semantic error. Fast program (now), but new error.

- Was performance fix exactly right?
- Again, consider (possibly new) corner cases.

```
public class Factors
{
    public static void main(String[] args)
    {
        long N = Long.parseLong(args[0]);
        for (int i = 2; i * i <= N; i++)
        {   // Check whether i is a factor.           Execute loop body if i * i == N
            while (N % i == 0)
            {   // If so, print and divide.
                System.out.print(i + " ");
                N = N / i;
            }
        }
        if (N > 1) System.out.println(N);
        else       System.out.println();
    }
}
```

```
% java Factors 24
2 2 2 3
% java Factors 25
5 5
% java Factors 49
7 7
%
```

Program Development: Analysis

Q. How large an integer can I factor?

```
% java Factors 3757208  
2 2 2 7 13 13 397
```

```
% java Factors 920111169755555703  
920111169755555703
```

after a few minutes of computing....

in largest factor →

digits	($i < N$)	($i*i \leq N$)
3	instant	instant
6	0.15 seconds	instant
9	77 seconds	instant
12	21 hours [†]	0.16 seconds
15	2.4 years [†]	2.7 seconds
18	2.4 millennia [†]	92 seconds

[†] estimated, using analytic number theory

Note. Can't break RSA this way (experts are still trying)

Debugging Your Program

Debugging Your Program. [summary]

1. **Edit** the program (type in code).

2. **Compile** it.

Compiler says: That's not a legal program?

Back to step 1 to fix your **syntax** errors.

3. **Run** it.

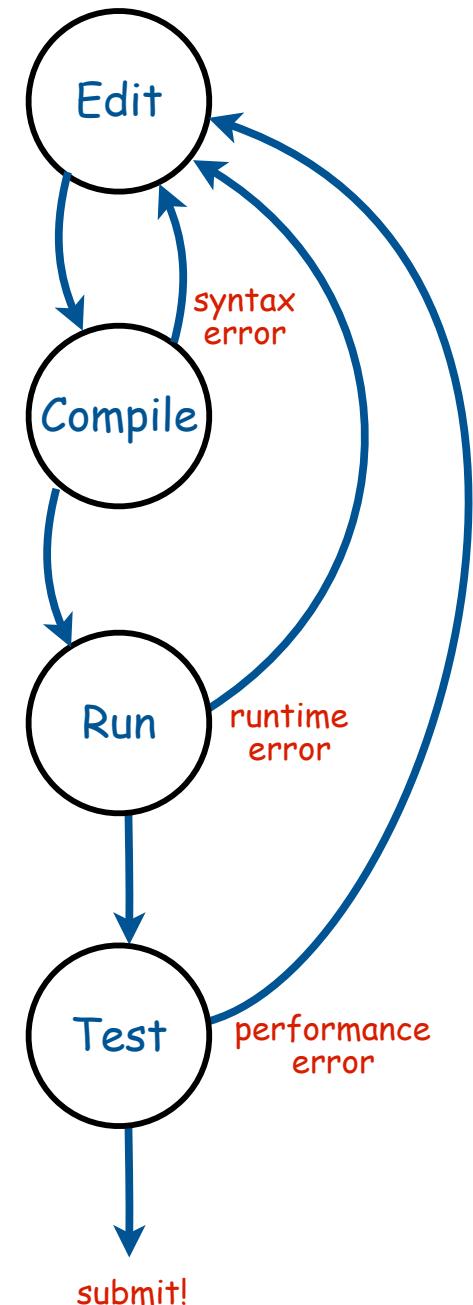
Result is bizarrely (or subtly) wrong?

Back to step 1 to fix your **runtime** (semantic) errors.

4. **Test** it.

Too slow?

Back to step 1 to try a different **algorithm**.



99% of program development

Debugging. Cyclic process of editing, compiling, and fixing errors.

- Always a logical explanation.
- What would the machine do?
- Explain it to the teddy bear.



You will make many mistakes as you write programs. It's normal.

"As soon as we started programming, we found out to our surprise that it wasn't as easy to get programs right as we had thought. I can remember the exact instant when I realized that a large part of my life from then on was going to be spent in finding mistakes in my own programs."



Sir Maurice Wilkes

Good news: Can use computer to test program.

Bad news: Conditionals/loops open up huge number of possibilities.

Really bad news: Cannot use computer to automatically find all bugs. ← stay tuned

The First Bug?

92

Photo # NH 96566-KN First Computer "Bug", 1945

9/9	
0800	Auton started
1000	" stopped - auton ✓
13'00 (033)	MP - MC
(033)	PRO 2
	convct
	Relays 6-2 in 033 failed special speed test
	in relay
	Relays changed
1100	Started Cosine Tape (Sine check)
1525	Started Multi Adder Test.
1545	Relay #70 Panel F (moth) in relay.
1625/00	First actual case of bug being found. auton starts.
1700	closed down.

<http://www.history.navy.mil/photos/images/h96000/h96566kc.htm>

Lieutenant Grace Murray Hopper

