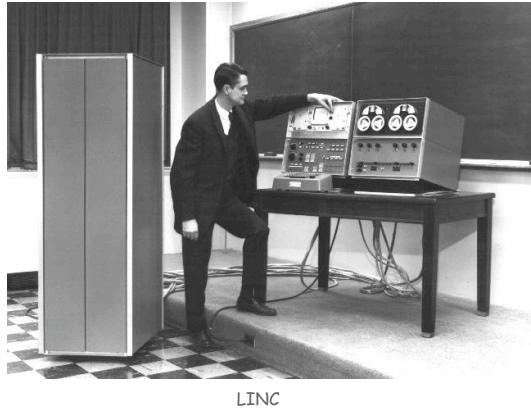


TOY II



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Data representation. Binary and hex.

TOY.

- Box with switches and lights.
- 16-bit memory locations, 16-bit registers, 8-bit pc.
- $4,328 \text{ bits} = (255 \times 16) + (15 \times 16) + (8) = 541 \text{ bytes!}$
- von Neumann architecture.

TOY instruction set architecture. 16 instruction types.

TOY machine language programs. Variables, arithmetic, loops.



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What We Do Today

Data representation. Negative numbers.

Input and output. Standard input, standard output.

Manipulate addresses. References (pointers) and arrays.

TOY simulator in Java.

Negative Numbers



Adding and Subtracting Binary Numbers

Decimal and binary addition.

$$\begin{array}{r}
 & \text{carries} \\
 & \swarrow \quad \searrow \\
 \begin{array}{r} 1 \\ 013 \\ + 092 \\ \hline 105 \end{array} & \begin{array}{r} 0\ 0\ 0\ 0\ 1\ 1\ 0\ 1 \\ + 0\ 1\ 0\ 1\ 1\ 1\ 0\ 0 \\ \hline 0\ 1\ 1\ 0\ 1\ 0\ 0\ 1 \end{array}
 \end{array}$$

Subtraction. Add a negative integer.

$$\begin{array}{c}
 \nearrow \\
 \text{e.g., } 6 - 4 = 6 + (-4)
 \end{array}$$

Q. How to represent negative integers?

Representing Negative Integers

TOY words are 16 bits each.

- We could use 16 bits to represent 0 to $2^{16} - 1$.
- We want negative integers too.
- Reserving half the possible bit-patterns for negative seems fair.

Highly desirable property. If x is an integer, then the representation of $-x$, when added to x , is zero.

$$\begin{array}{r}
 x \quad \begin{array}{r} 0\ 0\ 1\ 1\ 0\ 1\ 0\ 0 \\ + ?\ ?\ ?\ ?\ ?\ ?\ ? \\ \hline 0 \end{array} \\
 +(-x) \quad \begin{array}{r} 1\ 1\ 1\ 0\ 0\ 1\ 0\ 1 \\ + 1\ 1\ 0\ 0\ 1\ 0\ 1\ 1 \\ \hline 1 \end{array} \\
 \hline
 \begin{array}{r} 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \\ + 1 \\ \hline 0 \end{array}
 \end{array}$$

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Two's Complement Integers

To compute $-x$ from x :

- Start with x .

$$\begin{array}{r}
 \text{leading bit} \\
 +4 \quad \boxed{0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 1\ 0\ 0\ 0}
 \end{array}$$

- Flip bits.

$$\begin{array}{r}
 -5 \quad \boxed{1\ 1\ 1\ 1\ 1\ 1\ 1\ 1\ 1\ 1\ 1\ 1\ 1\ 1\ 0\ 1\ 1}
 \end{array}$$

- Add one.

$$\begin{array}{r}
 -4 \quad \boxed{1\ 1\ 1\ 1\ 1\ 1\ 1\ 1\ 1\ 1\ 1\ 1\ 1\ 1\ 0\ 0}
 \end{array}$$

Two's Complement Integers

dec	hex	15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0	
+32767	7FFF	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	
+4	0004	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	
+3	0003	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	
+2	0002	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0
+1	0001	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1
+0	0000	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
-1	FFFF	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
-2	FFFE	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
-3	FFFD	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1
-4	FFFC	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0
...																		
-32768	8000	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	

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Properties of Two's Complement Integers

Properties.

- Leading bit (bit 15) signifies sign.
- 0000000000000000 represents zero.
- Negative integer $-x$ represented by $2^{16} - x$.
- Addition is easy.
- Checking for arithmetic overflow is easy.

Standard Input and Output

Not-so-nice property. Can represent one more negative integer than positive integer.

$$32,768 = 2^{15}$$

$$-32,768 = -2^{15}$$

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Standard Output

Standard output.

- Writing to memory location FF sends one word to TOY stdout.
- Ex. 9AFF writes the integer in register A to stdout.

```

00: 0000 0
01: 0001 1

10: 8A00 RA ← mem[00]      a = 0
11: 8B01 RB ← mem[01]      b = 1
12: 9AFF write RA to stdout    print a
13: 1AAB RA ← RA + RB      a = a + b
14: 2BAB RB ← RA - RB      b = a - b
15: DA12 if (RA > 0) goto 12
16: 0000 halt

fibonacci.toy
  
```

```

0000
0001
0001
0002
0003
0005
0008
000D
0015
0022
0037
0059
0090
00E9
0179
0262
03DB
063D
0A18
1055
1A6D
2AC2
452F
6FFF1
  
```

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Standard Input

Standard input.

- Loading from memory address FF loads one word from TOY stdin.
- Ex. 8AFF reads an integer from stdin and store it in register A.

Ex: read in a sequence of integers and print their sum.

- In Java, stop reading when EOF.
- In TOY, stop reading when user enters 0000.

```

while (!StdIn.isEmpty()) {
    a = StdIn.readInt();
    sum = sum + a;
}
StdOut.println(sum);
  
```

```

00: 0000 0
10: 8C00 RC ← mem[00]
11: 8AFF read RA from stdin
12: CA15 if (RA == 0) pc ← 15
13: 1CCA RC ← RC + RA
14: C011 pc ← 11
15: 9CFF write RC
16: 0000 halt
  
```

```

00AE
0046
0003
0000
00F7
  
```

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Standard Input and Output: Implications

Standard input and output enable you to:

- Get information out of machine.
- Put information from real world into machine.
- Process more information than fits in memory.
- Interact with the computer while it is running.

Pointers

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Load Address (a.k.a. Load Constant)

Load address. [opcode 7]

- Loads an 8-bit integer into a register.
- `7A30` means load the value `30` into register `A`.

Applications.

- Load a small **constant** into a register.
- Load a 8-bit **memory address** into a register.

register stores "pointer" to a memory cell

```
a = 0x30;
```

Java code

15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
0	1	1	1	1	0	1	0	0	0	1	1	0	0	0	0
7 ₁₆				A ₁₆				3 ₁₆				0 ₁₆			
opcode		dest d		addr											

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Arrays in TOY

TOY main memory is a giant array.

- Can access memory cell `30` using load and store.
- `8C30` means load `mem[30]` into register `C`.
- Goal: access memory cell `i` where `i` is a variable.

...	...
30	0000
31	0001
32	0001
33	0002
34	0003
35	0005
36	0008
37	000D
...	...

TOY memory

Load indirect. [opcode A]

- `AC06` means load `mem[R6]` into register `C`.

a variable index

Store indirect. [opcode B]

- `BC06` means store contents of register `C` into `mem[R6]`.

a variable index

```
for (int i = 0; i < N; i++)
    a[i] = StdIn.readInt();

for (int i = 0; i < N; i++)
    StdOut.println(a[N-i-1]);
```

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TOY Implementation of Reverse

TOY implementation of reverse.

- Read in a sequence of integers and store in memory 30, 31, 32, ...
- Stop reading if 0000.
- Print sequence in reverse order.

```

10: 7101 R1 ← 0001           constant 1
11: 7A30 RA ← 0030          a[]
12: 7B00 RB ← 0000          n

13: 8CFF read RC
14: CC19 if (RC == 0) goto 19
15: 16AB R6 ← RA + RB
16: BC06 mem[R6] ← RC
17: 1BB1 RB ← RB + R1
18: C013 goto 13
}

read in the data

```

TOY Implementation of Reverse

TOY implementation of reverse.

- Read in a sequence of integers and store in memory 30, 31, 32, ...
- Stop reading if 0000.
- Print sequence in reverse order.

```

19: CB20 if (RB == 0) goto 20
1A: 16AB R6 ← RA + RB
1B: 2661 R6 ← R6 - R1
1C: AC06 RC ← mem[R6]
1D: 9CFF write RC
1E: 2BB1 RB ← RB - R1
1F: C019 goto 19
20: 0000 halt
}

while (n > 0) {
    address of a[n]
    address of a[n-1]
    c = a[n-1];
    StdOut.println(c);
    n--;
}

print in reverse order

```

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Unsafe Code at any Speed

Q. What happens if we make array start at 00 instead of 30?

A. Self modifying program; can overflow buffer and run arbitrary code!

```

10: 7101 R1 ← 0001           constant 1
11: 7A00 RA ← 0000          a[]
12: 7B00 RB ← 0000          n

13: 8CFF read RC
14: CC19 if (RC == 0) goto 19
15: 16AB R6 ← RA + RB
16: BC06 mem[R6] ← RC
17: 1BB1 RB ← RB + R1
18: C013 goto 13
}

% more crazy8.txt
1 1 1 1 1 1 1
1 1 1 1 1 1 1
8888 8810
98FF C011

```

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What Can Happen When We Lose Control (in C or C++)?

Buffer overrun.

- Array `buffer[]` has size 100.
- User might enter 200 characters.
- Might lose control of machine behavior.

```

#include <stdio.h>
int main(void) {
    char buffer[100];
    scanf("%s", buffer);
    printf("%s\n", buffer);
    return 0;
}

```

unsafe C program

Consequences. Viruses and worms.

Java enforces security.

- Type safety.
- Array bounds checking.
- Not foolproof.



shine 50W bulb at DRAM
[Appel-Govindavajala '03]

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Buffer Overrun Example: JPEG of Death

Microsoft Windows JPEG bug. [September, 2004]

- Step 1. User views malicious JPEG in IE or Outlook.
- Step 2. Machine is Owned.
- Data becomes code by exploiting buffer overrun in GDI+ library.



Fix. Update old library with patched one.



but many applications install independent copies of GDI library

Moral.

- Not easy to write error-free software.
- Embrace Java security features.
- Don't try to maintain several copies of the same file.
- Keep your OS patched.

Dumping

Q. Work all day to develop operating system. How to save it?

A. Write short program `dump.toy` and run it to dump contents of memory onto tape.

```
00: 7001 R1 ← 0001
01: 7210 R2 ← 0010
02: 73FF R3 ← 0OFF
03: AA02 RA ← mem[R2]
04: 9AFF write RA
05: 1221 R2 ← R2 + R1
06: 2432 R4 ← R3 - R2
07: D403 if (R4 > 0) goto 03
08: 0000 halt
```

`dump.toy`

Booting

Q. How do you get it back?

A. Write short program `boot.toy` and run it to read contents of memory from tape.

TOY Simulator

```
00: 7001 R1 ← 0001
01: 7210 R2 ← 0010
02: 73FF R3 ← 0OFF
03: 8AFF read RA
04: BA02 mem[R2] ← RA
05: 1221 R2 ← R2 + R1
06: 2432 R4 ← R3 - R2
07: D403 if (R4 > 0) goto 03
08: 0000 halt
```

`boot.toy`

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TOY Simulator

Goal. Write a program to "simulate" the behavior of the TOY machine.

- TOY simulator in Java.
- TOY simulator in TOY!

```
public class TOY {
    public static void main(String[] args) {
        int pc = 0x10; // program counter
        int[] R = new int[16]; // registers
        int[] mem = new int[256]; // main memory

        // READ IN .toy FILE

        while (true) {
            // FETCH INSTRUCTION and DECODE
            ...
            // EXECUTE
            ...
        }
    }
}
```

```
% java TOY add-stdin.toy
A012
002B
A03D
```

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TOY Simulator: Fetch

Fetch. Extract destination register of 1_{CAB} by shifting and masking.

	inst
	inst >> 8
	15
	(inst >> 8) & 15

```
int inst = mem[pc++]; // fetch and increment
int op = (inst >> 12) & 15; // opcode (bits 12-15)
int d = (inst >> 8) & 15; // dest d (bits 08-11)
int s = (inst >> 4) & 15; // source s (bits 04-07)
int t = (inst >> 0) & 15; // source t (bits 00-03)
int addr = (inst >> 0) & 255; // addr (bits 00-07)
```

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TOY Simulator: Execute

```
if (op == 0) break; // halt

switch (op) {
    case 1: R[d] = R[s] + R[t]; break;
    case 2: R[d] = R[s] - R[t]; break;
    case 3: R[d] = R[s] & R[t]; break;
    case 4: R[d] = R[s] ^ R[t]; break;
    case 5: R[d] = R[s] << R[t]; break;
    case 6: R[d] = R[s] >> R[t]; break;
    case 7: R[d] = addr; break;
    case 8: R[d] = mem[addr]; break;
    case 9: mem[addr] = R[d]; break;
    case 10: R[d] = mem[R[t]]; break;
    case 11: mem[R[t]] = R[d]; break;
    case 12: if (R[d] == 0) pc = addr; break;
    case 13: if (R[d] > 0) pc = addr; break;
    case 14: pc = R[d]; break;
    case 15: R[d] = pc; pc = addr; break;
}
```

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TOY Simulator: Omitted Details

Omitted details.

- Register 0 is always 0.
 - reset $R[0]=0$ after each fetch-execute step
- Standard input and output.
 - if $addr$ is FF and opcode is load (indirect) then read in data
 - if $addr$ is FF and opcode is store (indirect) then write out data
- TOY registers are 16-bit integers; program counter is 8-bit.
 - Java int is 32-bit; Java short is 16-bit
 - use casts and bit-whacking

Complete implementation. See `TOY.java` on booksite.

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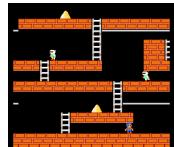
Simulation

Consequences of simulation.

- Test out new machine or microprocessor using simulator.
 - cheaper and faster than building actual machine
- Easy to add new functionality to simulator.
 - trace, single-step, breakpoint debugging
 - simulator more useful than TOY itself
- Reuse software from old machines.

Ancient programs still running on modern computers.

- Ticketron.
- Lode Runner on Apple IIe.



Backwards Compatibility

Q. Why is standard US rail gauge 4 feet, 8.5 inches?

