

# Lecture A2: X-TOY Programming and Simulation



DEC PDP 12

## Useful X-TOY Idioms

### Jump absolute.

- Jump to a fixed memory address.
  - branch if zero with destination
  - register 0

```
Jump absolute
17: C014  pc ← 14
```

### Register assignment.

- No instruction that transfers contents of one register into another.
- Pseudo-instruction that simulates assignment:
  - add with register 0 as one of two source registers

```
Register assignment
17: 1230  R[2] ← R[3]
```

### No-op.

- Instruction that does nothing.
- Plays the role of whitespace in C programs.
  - numerous other possibilities!

```
No-op
17: 1000  no-op
```

## How to represent negative integers

X-TOY integers occupy 16 bits each.

- We can represent 0 to  $2^{16}-1$  if we like.
- But what about negative integers?
- Reserving half the possible bit-patterns for negative seems fair.

Highly desirable property:

- If X is a positive integer, then the representation of -X, when added to X, had better yield zero.

$$\begin{array}{r} X \\ +(-X) \\ \hline 0 \end{array} \quad \begin{array}{r} 00110100 \\ + \text{????????} \\ \hline 00000000 \end{array}$$

$$\begin{array}{r} X \\ +(-X) \\ \hline 0 \end{array} \quad \begin{array}{r} 00110100 \\ + 11001011 \\ \hline 11111111 \\ + \\ \hline 00000000 \end{array}$$

## Two's Complement Integers

Properties:

- Leading bit (bit 15) signifies sign.
- Negative integer -N represented by  $2^{16} - N$ .
- Trick to compute -N:

1. Start with N.

	15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
+4	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0

2. Flip bits.

	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1
--	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

3. Add 1.

-4	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0
----	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

## Two's Complement Integers

		15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
Dec	Hex	Binary															
+32767	7FFF	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
...																	
+4	0004	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0
+3	0003	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1
+2	0002	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0
+1	0001	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1
+0	0000	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
-1	FFFF	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
-2	FFFE	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
-3	FFFD	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1
-4	FFFC	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0
...																	
-32768	8000	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0

## Properties of Two's Complement Integers

### Nice properties:

- 0000000000000000 represents 0.
- -0 and +0 are the same.
- Addition is easy (see next slide).
- Checking for arithmetic overflow is easy.

$$-N = \sim N + 1$$

### Not-so-nice properties.

- Can represent one more negative integer than positive integer (-32,768 =  $-2^{15}$  but not  $32,768 = 2^{15}$ ).

## Two's Complement Arithmetic

Addition is carried out as if all integers were positive.

- It usually works:

-3	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	
+																		
4	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0
=																		
1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1

## Two's Complement Arithmetic

Addition is carried out as if all integers were positive.

- It usually works.
- But overflow can occur:

+32,767	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
+																		
2	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0
=																		
-32,767	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1

## Representing Other Primitive Data Types

### Negative integers.

- X-TOY uses two's complement integers.

### Big integers.

- Can use "multiple precision."
- Use two 16-bit words per integer.

### Real numbers.

- Can use "floating point" (like scientific notation).
- Double word for extra precision.

### Characters.

- Can use ASCII code (8 bits / character).
- Can pack two characters into one 16-bit word.

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## Memory Indirection

### Static addressing.

- Until now, all load/store addresses hardwired in instruction.
- Ex. 8A34:  $R[A] \leftarrow \text{mem}[34]$
- More flexibility needed to implement arrays.

### Indirect (dynamic) addressing.

- Work with **names** of data.
- Want to access variable memory location like  $x$ , instead of hardwiring 34.

### Solution.

- Put memory address in register. (**C "pointer"**)
- Use **CONTENTS** of register as address.
- Use store indirect, load indirect instructions to access.

### array3.c

```
int i = 0;
int N = 33;

while (i < N) {
    a[i] += 3;
    i++;
}
```

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## Array3

### array3.toy

```
10: 7101 R[1] ← 0001    constant 1
11: 7202 R[2] ← 0003    constant 3
12: 7A20 R[A] ← 0020    a[]
13: 7300 R[4] ← 0033    N ← 33
14: 7500 R[5] ← 0000    i ← 0

15: 17A5 R[7] ← R[A] + R[5] address of a[i]
16: A907 R[9] ← mem[R[7]] t ← a[i]
17: 1993 R[9] ← R[9] + R[2] t += 3
18: B907 mem[[R[7]]] ← R[9] a[i] ← t
19: 1551 R[5] ← R[5] + R[1] i++
1A: 2C45 R[C] ← R[4] - R[5] N - i
1B: DC15 if (R[C] > 0) goto 15
1C: 0000 halt
```

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## Standard Input, Standard Output

### Standard input.

- Loading from memory address FF loads one (hexadecimal) integer from X-TOY stdin.

- 8AFF means:

- read an integer from standard input, and store it in register A
- `scanf("%hX", &a);`

### stdin-stdout.toy

```
10: 8AFF read R[A]
11: 9AFF write R[A]
12: 0000 halt
```

### Standard output.

- Writing to memory location FF.

15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
1	0	0	0	1	0	1	0	1	1	1	1	1	1	1	1
8 <sub>16</sub>				A <sub>16</sub>				F <sub>16</sub>				F <sub>16</sub>			
opcode				dest d				addr							

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## Standard Input, Standard Output

Enables computer to process more information than fits in memory.

- Arbitrary amounts of input.

```

max.c

int x, max = 0;

while (scanf("%d", &x) != EOF) {
    if (x > max)
        max = x;
}

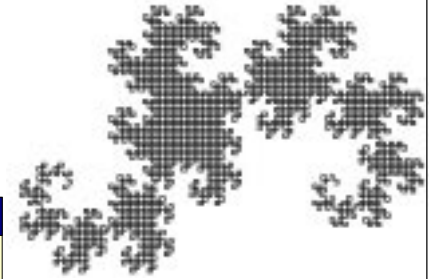
printf("Maximum = %d\n", max);
    
```

- Arbitrary amounts of output.
  - dragon curve

## Bitwise Operations

Bitwise AND. (opcode 3)

Bitwise XOR. (opcode 4)



```

dragon-nonrecursive.c

void dragon(int m) {
    int k;
    F();
    for (k = 1; k <= m-1; k++) {
        if (k & ((k^(k-1))+1))
            R();
        else
            L();
        F();
    }
}
    
```

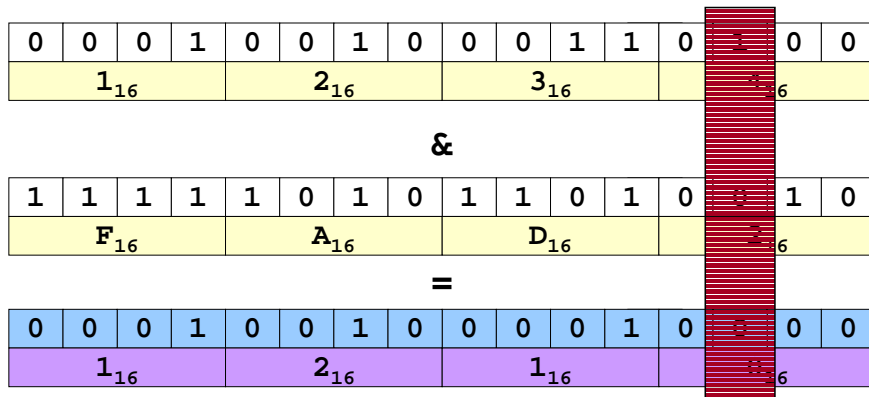
check bit to the left of rightmost 1

## Bitwise AND

Logic operations are BITWISE:

- $1234_{16} \& \text{FAD}2_{16} = 1210_{16}$

x	y	AND
0	0	0
0	1	0
1	0	0
1	1	1

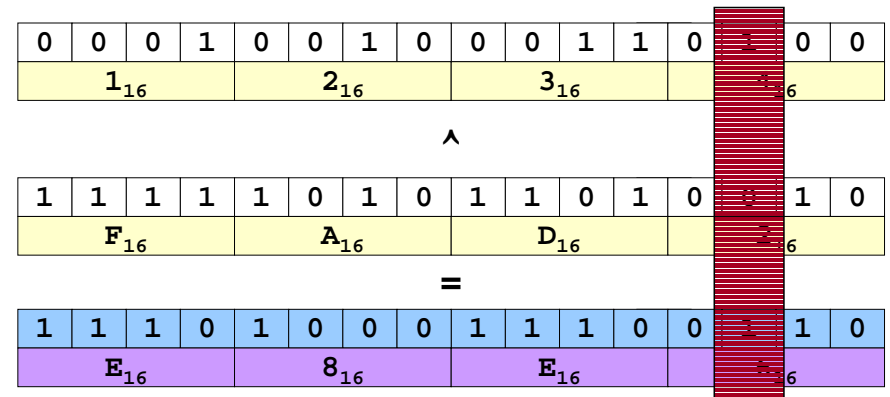


## Bitwise XOR

Logic operations are BITWISE:

- $1234_{16} \wedge \text{FAD}2_{16} = \text{E8E}6_{16}$

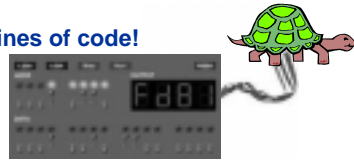
x	y	XOR
0	0	0
0	1	1
1	0	1
1	1	0



# Dragon in XTOY

Impress your Yale friends with these 10 lines of code!

- Connect stdout to turtle.
  - L if zero
  - R if nonzero
- Keeps going until turtle runs out of energy.



```

dragon.toy
10: 7101  R[1] <- 0001
11: 7201  R[2] <- 0001      k
12: 2321  R[3] <- R[2] - R[1]  k - 1
13: 4423  R[4] <- R[2] ^ R[3]  k ^ (k-1)
14: 1541  R[5] <- R[4] + R[1]  (k^(k-1))+1
15: 3552  R[5] <- R[5] & R[2]  k & ((k^(k-1))+1)
16: 95FF  write R[5]
17: 1221  R[2] <- R[2] + R[1]
18: C012  goto 12
19: 0000  halt
    
```



# Function Call: A Failed Attempt

Goal:  $x \times y \times z$ .

- Need two multiplications:  $x \times y$ ,  $(x \times y) \times z$ .

A failed attempt:

- Write multiply loop at 30-36.
- Calling program agrees to store arguments in registers A and B.
- Function agrees to leave result in register C.
- Call function with jump absolute to 30.
- Return from function with jump absolute.

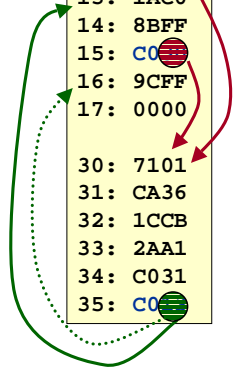
Reason for failure.

function?

```

10: 8AFF
11: 8BFF
12: C0
13: 1AC0
14: 8BFF
15: C0
16: 9CFF
17: 0000

30: 7101
31: CA36
32: 1CCB
33: 2AA1
34: C031
35: C0
    
```



# Multiplication Function

Calling convention.

- Jump to line 30.
- Store a and b in registers A and B.
- Return address in register F.
- Put result  $c = a \times b$  in register C.
- Register 1 is scratch.
- Overwrites registers A and B.

```

function.toy
30: 7C00  R[C] <- 00
31: 7101  R[1] <- 01
32: CA36  if (R[A] == 0) goto 36
33: 1CCB  R[C] += R[B]
34: 2AA1  R[A]--
35: C032  goto 32
36: EF00  pc <- R[F]
    
```

```

function
10: 8AFF
11: 8BFF
12: FF
13: 1AC0
14: 8BFF
15: FF
16: 9CFF
17: 0000

30: 7C00
31: 7101
32: CA36
33: 1CCB
34: 2AA1
35: C032
36: EF00
    
```

opcode E  
jump register

return



# Multiplication Function Call

Client program to compute  $x \times y \times z$ .

- Read x, y, z from standard input.
- Note: PC is incremented before instruction is executed.
  - value stored in register F is correct return address

```

function.toy (cont)
10: 82FF  read R[2]      x
11: 83FF  read R[3]      y
12: 84FF  read R[4]      z
13: 1A20  R[A] <- R[2]    x
14: 1B30  R[B] <- R[3]    y
15: FF30  R[F] <- pc; goto 30  x * y
16: 1AC0  R[A] <- R[C]    (x * y)
17: 1B40  R[B] <- R[4]    z
18: FF30  R[F] <- pc; goto 30  (x * y) * z
19: 9CFF  write R[C]
1A: 0000  halt
    
```

opcode F  
jump and link

R[F] <- 16



## Function Call: One Solution

### Contract between calling program and function:

- Calling program stores function parameters in specific registers.
- Calling program stores return address in a specific register.
  - jump-and-link
- Calling program sets PC to address of function.
- Function stores return value in specific register.
- Function sets PC to return address when finished.
  - jump register

### What if you want a function to call another function?



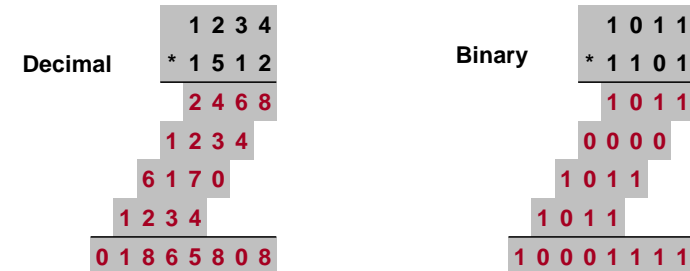
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## An Efficient Multiplication Algorithm

### Inefficient multiply.

- Load in integers a and b, and store  $c = a \times b$ .
- Brute-force algorithm:
  - initialize  $c = 0$
  - add b to c, a times

### "Grade-school" multiplication.



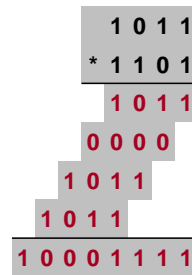
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## Binary Multiplication

### Grade school binary multiplication algorithm to compute $c = a \times b$ .

- Initialize  $c = 0$ .
- Loop over i bits of b.
  - if  $b_i = 0$ , do nothing
  - if  $b_i = 1$ , shift a left i bits and add to c

←  $b_i = i^{\text{th}}$  bit of b



### Implement with built-in TOY shift instructions.

#### multiply-fast.c

```

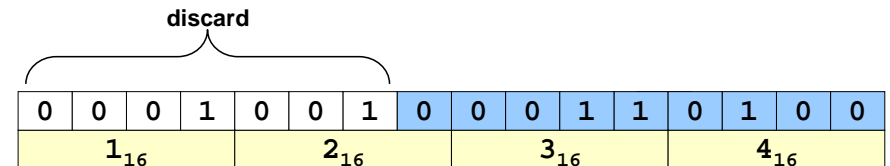
int c = 0;
for (i = 15; i >= 0; i--) {
    if ((b >> i) & 1)
        c += (a << i);
}
  
```

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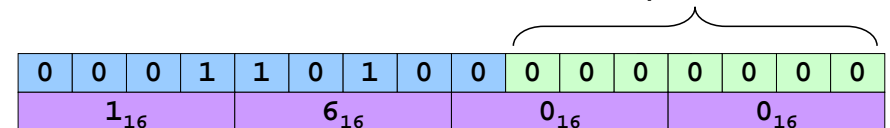
## Shift Left

### Shift left. (opcode 5)

- Move bits to the left, padding with zeros as needed.
- $1234_{16} \ll 7 = 1600_{16}$



$\ll 7 =$  pad with 0's

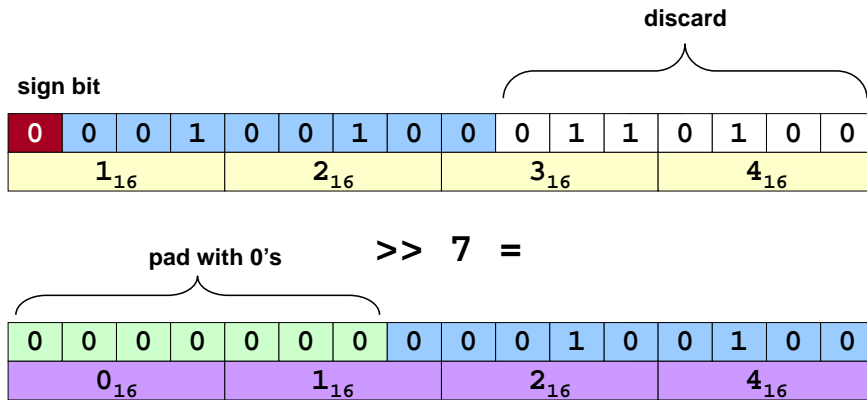


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## Shift Right

### Shift left. (opcode 6)

- Move bits to the right, padding with sign bit as needed.
- $1234_{16} \gg 7_{16} = 0124_{16}$



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## Fast Multiplication Function

```

multiply-fast.toy
// Input: R[A] contains a, R[B] contains b
// Output: R[C] contains a * b

30: 7101  R[1] <- 0001
31: 7210  R[2] <- 0010
32: 7C00  R[C] <- 0000

33: C23B  if (R[2] == 0) goto 3B
34: 2221  R[2]--
35: 53A2  R[3] <- R[A] << R[2]
36: 64B2  R[4] <- R[B] >> R[2]
37: 3441  R[4] <- R[4] & R[1]

38: C43A  if (R[4] == 0) goto 3A
39: 1CC3  R[C] += R[3]

3A: C033  goto 33
3B: EF00  goto R[F]
    
```

*i = 16* ← 16-bit integers  
*result*

*while (i > 0) {*  
    *i--*  
    *a left shifted i*  
    *b\_i = i<sup>th</sup> bit of b*  
*}*

*add to result*  
*return*

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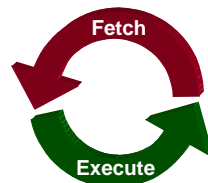
## How To Build a TOY Machine

### Implement fetch-execute cycle in hardware.

- See Lecture A4-A6.

```

X-TOY Machine
DO {
  fetch instruction
  execute instruction
} UNTIL (halt signal)
    
```



### Implement fetch-execute cycle in software.

- Write a program to "simulate" the behavior of the TOY machine.
- TOY simulator in Java.
- TOY simulator in C.
- TOY simulator in TOY! (It has been done.)

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## TOY Simulator in C

```

TOY SIMULATOR: toy.c
int main(int argc, char *argv[]) {
  short R[16] = {0}; // registers
  short mem[256] = {0}; // memory
  unsigned char pc = 0x10; // pc
  unsigned int inst, addr;
  int i, op, d, s, t;

  FILE *file;
  file = fopen(argv[1], "r");
  if (file == NULL) {
    printf("Error opening %s\n", file);
    exit(EXIT_FAILURE);
  }

  while (fscanf(file, "%2hX%4hX", &i, &inst) != EOF)
    mem[i] = inst;

  . . .
}
    
```

← short = 16 bit 2's complement integer (on arizona)

← open file for reading

```

Unix
% gcc toy.c
% a.out dragon.toy
    
```

← read TOY code from file

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## X-TOY Simulator

xtoy.c: parse instruction

fetch and increment

s = bits 4-7

addr = bits 0-7

execute

register 0 always 0

```
do {
    inst = mem[pc++];
    op  = (inst >> 12) & 15;
    d   = (inst >> 8)  & 15;
    s   = (inst >> 4)  & 15;
    t   = (inst >> 0)  & 15;
    addr = (inst >> 0) & 255;

    // see next slide
    . . .

    R[0] = 0;
} while (op != 0);

return 0;
}
```

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## Shifting and Masking

Extract destination register.

- Given 16 bit integer in C, isolate destination register (bits 8-11).
- Use bit operations in C.

inst = 3604<sub>16</sub>

15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
0	0	1	1	0	1	1	0	0	0	0	0	0	1	0	0

inst >> 8

0	0	0	0	0	0	0	0	1	0	1	1	0	1	1	0
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

15<sub>10</sub>

0	0	0	0	0	0	0	0	0	0	0	0	1	1	1	1
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

(inst >> 8) & 15 = 6

0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	0
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

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## TOY Simulator

toy.c: execute instruction

halt

bitwise AND

load address

load indirect

jump register

```
switch (op) {
    case 0: break;
    case 1: R[d] = R[s] + R[t]; break;
    case 2: R[d] = R[s] - R[t]; break;
    case 3: R[d] = R[s] & R[t]; break;
    case 4: R[d] = R[s] ^ R[t]; break;
    case 5: R[d] = R[s] << R[t]; break;
    case 6: R[d] = R[s] >> R[t]; break;
    case 7: R[d] = addr; break;
    case 8: R[d] = mem[addr]; break;
    case 9: mem[addr] = R[d]; break;
    case 10: R[d] = mem[R[t]]; break;
    case 11: mem[R[t]] = R[d]; break;
    case 12: if (R[d] == 0) pc = addr; break;
    case 13: if (R[d] > 0) pc = addr; break;
    case 14: pc = R[d]; break;
    case 15: R[d] = pc; pc = addr; break;
}
```

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## TOY Simulator

Missing details for stdin, stdout.

- Stdin: insert following code before execute switch statement.
  - if address is FF and opcode is load or load indirect

```
if ((addr == 255 && op == 8) || (R[t] == 255 && op == 10))
    scanf("%4hX", &mem[255]);
```

- Stdout: insert following code after execute switch statement.
  - if address is FF and opcode is store or store indirect

```
if ((addr == 255 && op == 9) || (R[t] == 255 && op == 11))
    printf("%04hX\n", mem[255]);
```

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## Simulation

### Consequences of simulation.

- Test out new machine (or microprocessor) using simulator.
  - cheaper and faster than building actual machine
- Easy to add new functionality to simulator.
  - trace, single-step, breakpoint debugging
  - simulator more useful than TOY itself
- Reuse software for old machines.

### Ancient programs still running on modern computers.

- Ticketron.
- Lode Runner on Apple IIe.



Apple IIe Simulator

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## Basic Characteristics of X-TOY Machine

### TOY is a general-purpose computer.

- Sufficient power to perform any computation.
- Limited only by amount of memory (and time).

### Stored-program computer. (von Neumann memo, 1944)

- Data and instructions encoded in binary.
  - immediate applications
  - profound implications
- Data and instructions stored in SAME memory.
- Can change program (control) without rewiring.
  - first stored-program computer
- EDSAC (Wilkes 1949).
  - first stored-program computer
- Outgrowth of Turing's work.

All modern computers are general-purpose computers and have same (von Neumann) architecture.

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## Lecture A2: Supplemental Notes



## TOY Cheat Sheet

	15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
Format 1	opcode				dest d			source s				source t				
Format 2	opcode				dest d			addr								

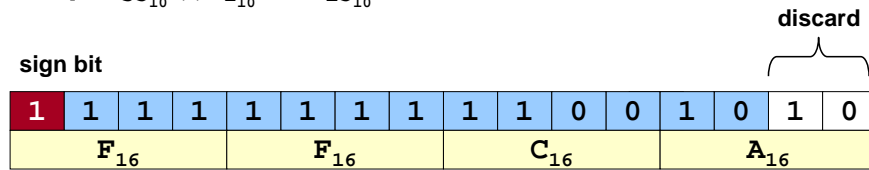
#	Operation	Fmt	Pseudocode
0:	halt	1	exit(0)
1:	add	1	$R[d] \leftarrow R[s] + R[t]$
2:	subtract	1	$R[d] \leftarrow R[s] - R[t]$
3:	and	1	$R[d] \leftarrow R[s] \& R[t]$
4:	xor	1	$R[d] \leftarrow R[s] \wedge R[t]$
5:	shift left	1	$R[d] \leftarrow R[s] \ll R[t]$
6:	shift right	1	$R[d] \leftarrow R[s] \gg R[t]$
7:	load addr	2	$R[d] \leftarrow \text{addr}$
8:	load	2	$R[d] \leftarrow \text{mem}[\text{addr}]$
9:	store	2	$\text{mem}[\text{addr}] \leftarrow R[d]$
A:	load indirect	1	$R[d] \leftarrow \text{mem}[R[t]]$
B:	store indirect	1	$\text{mem}[R[t]] \leftarrow R[d]$
C:	branch zero	2	if $(R[d] == 0)$ $\text{pc} \leftarrow \text{addr}$
D:	branch positive	2	if $(R[d] > 0)$ $\text{pc} \leftarrow \text{addr}$
E:	jump register	2	$\text{pc} \leftarrow R[d]$
F:	jump and link	2	$R[d] \leftarrow \text{pc}; \text{pc} \leftarrow \text{addr}$

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## Shift Right

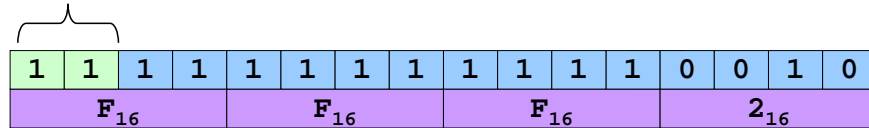
### Shift right. (opcode 6)

- Move bits to the right, padding with sign bit as needed.
- $\text{FFCA}_{16} \gg 2_{16} = \text{FFF2}_{16}$
- $-53_{10} \gg 2_{10} = -13_{10}$



pad with 1's

$\gg 2 =$



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## Other Logical Operations

Any logical operation can be implemented with AND and XOR.

- See Boolean circuit lecture.

Build OR from AND and XOR.

- $(x \& y) \vee (x \wedge y)$

		a		b	
x	y	x & y	x ^ y	a ^ b	OR
0	0	0	0	0	0
0	1	0	1	1	1
1	0	0	1	1	1
1	1	1	0	1	1

Build NOT from XOR.

- $1 \wedge x = x'$
- $\text{FFFF} \wedge x = x'$  (bitwise NOT)

x	1	x ^ 1	NOT
0	1	1	1
1	1	0	0

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