Programming exam information

In-class programming exam.

- Monday November 24; 1:20–2:40pm.
- See Ed for room assignments.
- Covers all Java programming material.
- Develop program in IntelliJ on your laptop; submit via TigerFile.

including associated precepts, readings, and assignments

charge battery (no outlets)

partial autograder

Rules. [see Ed post for full details]

- Subject to honor code.
- No collaboration or communication.
- No electronic devices or software (beyond what's needed).
- Allowed resources: only course materials (textbook, lecture slides, …).
- You must exclusively use Princeton wireless network *eduroam*.

no VPN or hotspots

Programming exam preparation.

- Exam archive on course website.
- Practice by taking old exam in 80-minute block.

COS 126 Princeton University Programming Exam Fall 2025

Before you begin. Read through this page of instructions. Do not start the exam (or access the next page) until instructed to do so.

Duration. You have 80 minutes to complete this exam.

Advice. Review the entire exam before starting to write code. Implement the constructor and methods in the order given, one at a time, testing in main() after you complete each method.

Submission. Submit your solutions on TigerFile using the link from the Exams page. You may submit multiple times (but only the last version will be graded).

Check Submitted Files. You may click the ***Check Submitted Files*** button to receive partial feedback on your submission. We will attempt to provide this feature during the exam, but you should not rely on it.

Grading. Your program will be graded *primarily* on correctness. However, efficiency and clarity will also be considered. You will receive partial credit for a program that implements some of the required functionality. You will receive a substantial penalty for a program that does not compile.

Allowed resources. This exam is open-book but not open-internet. During the exam you may use only the following resources: course textbook; companion booksite; lecture slides; course website; your course notes; your code from the programming assignments or precept; course Ed; course codePost, Java visualizer, and Oracle Javadoc. Accessing other websites or resources is prohibited. For example, you may not use Google, Google Docs, StackOverflow, or ChatGPT (or any other GenAI platform/assistant).

No collaboration or communication. During the exam, collaboration and communication (including sharing files) are prohibited, except with course staff members. A staff member will be outside the exam room to answer clarification questions.

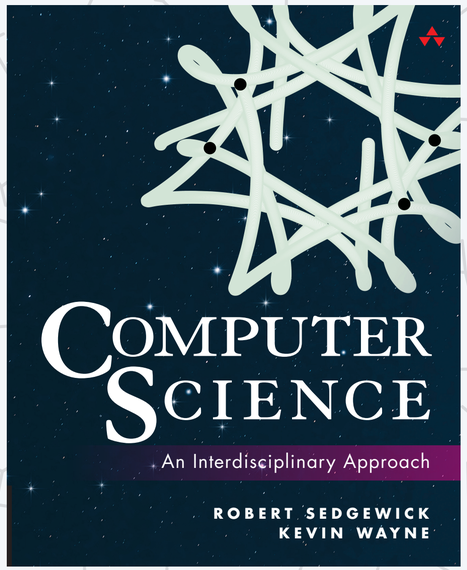
No electronic devices or software. Software and computational/communication devices are prohibited, except to the extent needed for taking this exam (such as a laptop, browser, and IntelliJ). For example, you must close all unnecessary virtual desktops, applications, and browser tabs; disable notifications; and power off all other devices (such as cell phones, tablets, smart watches, and earbuds). *You must use only the Princeton wireless network eduroam, not a VPN, mobile hotspot or other network.*

Honor Code pledge. Write and sign the Honor Code pledge by typing the text below in the file `acknowledgments.txt`. Submit to TigerFile.

I pledge my honor that I have not violated the Honor Code during this examination.
Electronically sign it by typing `/s/` followed by your name.

After the exam. Discussing or communicating the contents of this exam before solutions have been posted is a violation of the Honor Code.

Robert Sedgewick | Kevin Wayne



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6. TOY Machine I

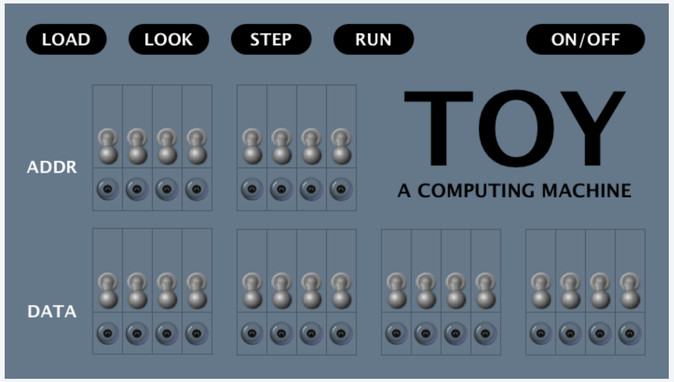
- *overview*
- *data types*
- *instructions*
- *operating the machine*

The TOY computing machine

TOY is an imaginary machine invented for this course.

It is similar in design to:

- Ancient computers.
- Today's microprocessors.
- Countless other devices designed and built over the past 60 years.



TOY machine

PDP-8, 1970s

smartphone processor, 2020s

Reasons to study TOY

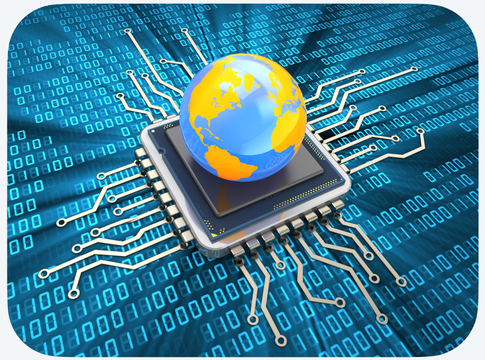
Learn about machine language programming.

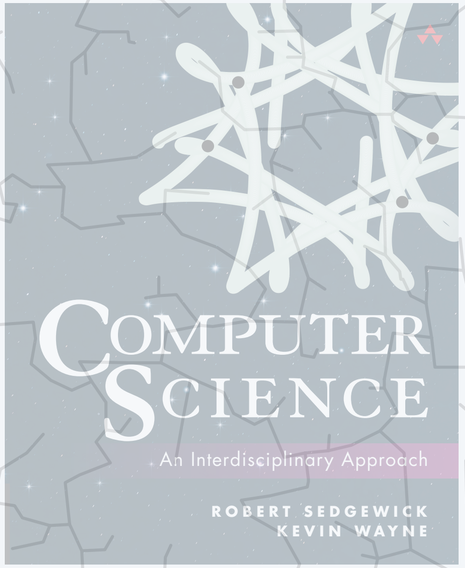
- How do Java programs relate to your computer? ⟵ *see* COS 320
- Key to understanding Java references (and C pointers). ⟵ *see* COS 217
- Still necessary in some modern applications.

multimedia, computer games, embedded devices, scientific computing, …

Prepare to learn about computer architecture. ⟵ *see* COS 375 / ECE 375

- How does your computer's processor work?
- What are its basic components?
- How do they interact?





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6. TOY Machine I

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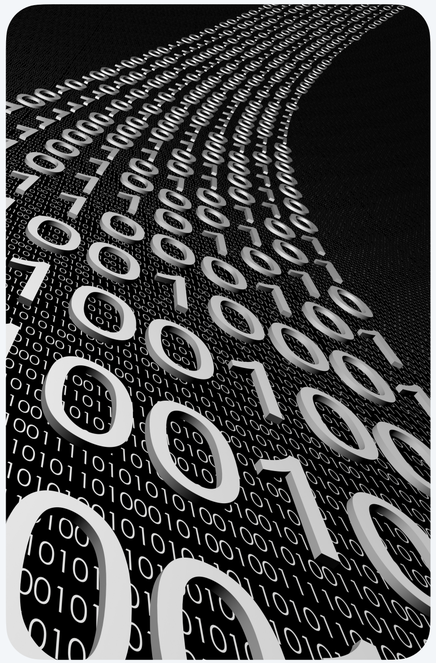
Data and programs are encoded in binary

Bit (binary digit). Basic unit of information in computing: either 0 or 1.

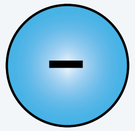
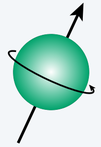
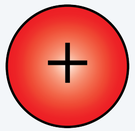
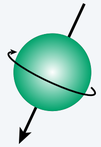


Everything stored in a computer is a sequence of bits.

- Data and programs.
- Numbers, text, pictures, songs, movies, biometrics, 3D objects, …

Q. Why binary?

A. Easy to represent two states in physical world.

0					
1					

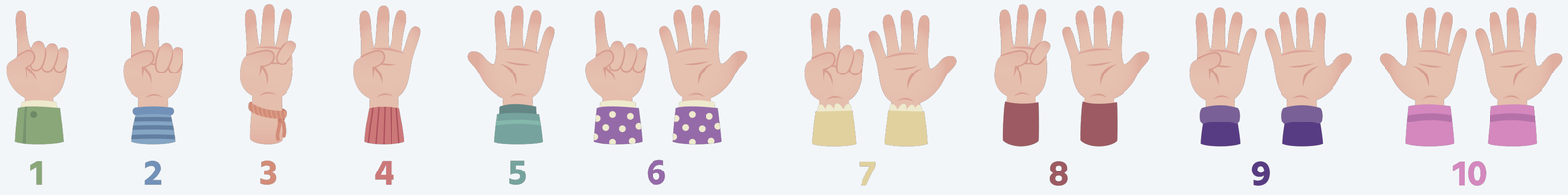
Decimal number system

Decimal number. A number expressed in base 10.

- Place-value notation with ten symbols (0–9).
- Used by most modern cultures.

	3	2	1	0
decimal	6	3	7	5

$$6 \cdot 10^3 + 3 \cdot 10^2 + 7 \cdot 10^1 + 5 \cdot 10^0 = 6375_{10}$$

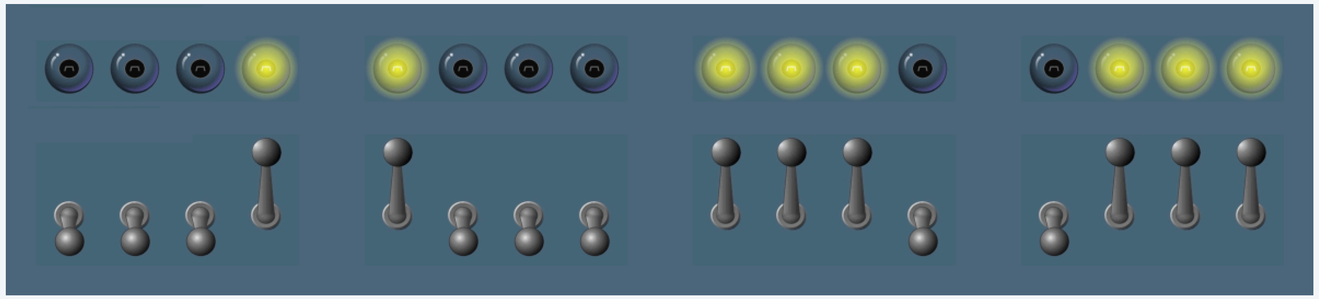


decimal
0
1
2
3
4
5
6
7
8
9
10
11
12
13
14
15

Binary number system

Binary number. A number expressed in base 2.

- Place-value notation with two symbols (0 and 1).
- Used by all modern computers.



15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
binary	0	0	0	1	1	0	0	0	1	1	1	0	0	1	1	1

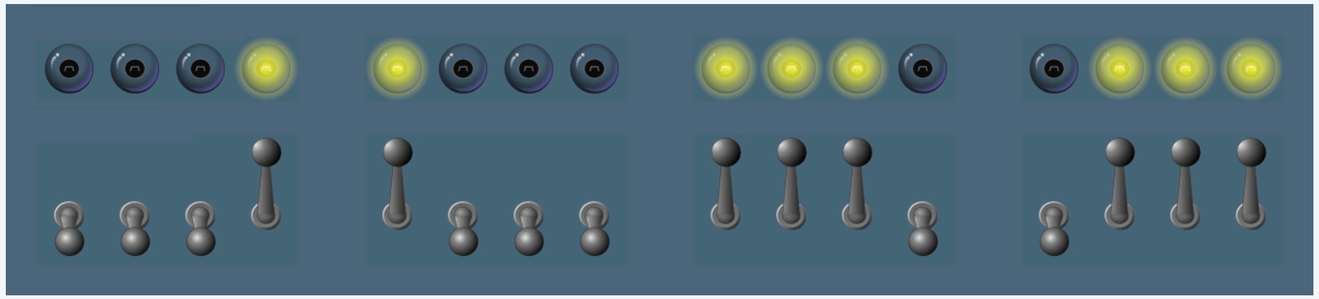
$2^{12} + 2^{11} + 2^{7} + 2^{6} + 2^{5} + 2^{2} + 2^{1} + 2^{0} = 6375_{10}$

decimal	binary
0	0000
1	0001
2	0010
3	0011
4	0100
5	0101
6	0110
7	0111
8	1000
9	1001
10	1010
11	1011
12	1100
13	1101
14	1110
15	1111

Hexadecimal number system

Hexadecimal number. A number expressed in base 16.

- Place-value notation with 16 symbols (0–9, A–F).
- Easy to convert from binary to hex (and vice versa). ← *4 bits per hex digit (because $2^4 = 16$)*
- More convenient for programmers.



	15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
binary	0	0	0	1	1	0	0	0	1	1	1	0	0	1	1	1
hex	1				8				E				7			

$1 \cdot 16^3$ $8 \cdot 16^2$ $14 \cdot 16^1$ $7 \cdot 16^0$ $= 6375_{10}$

decimal	binary	hex
0	0000	0
1	0001	1
2	0010	2
3	0011	3
4	0100	4
5	0101	5
6	0110	6
7	0111	7
8	1000	8
9	1001	9
10	1010	A
11	1011	B
12	1100	C
13	1101	D
14	1110	E
15	1111	F

TOY I: quiz 1

What is 101011101011101 in hexadecimal?

A. 2BAD

B. AEB1

C. EBAD

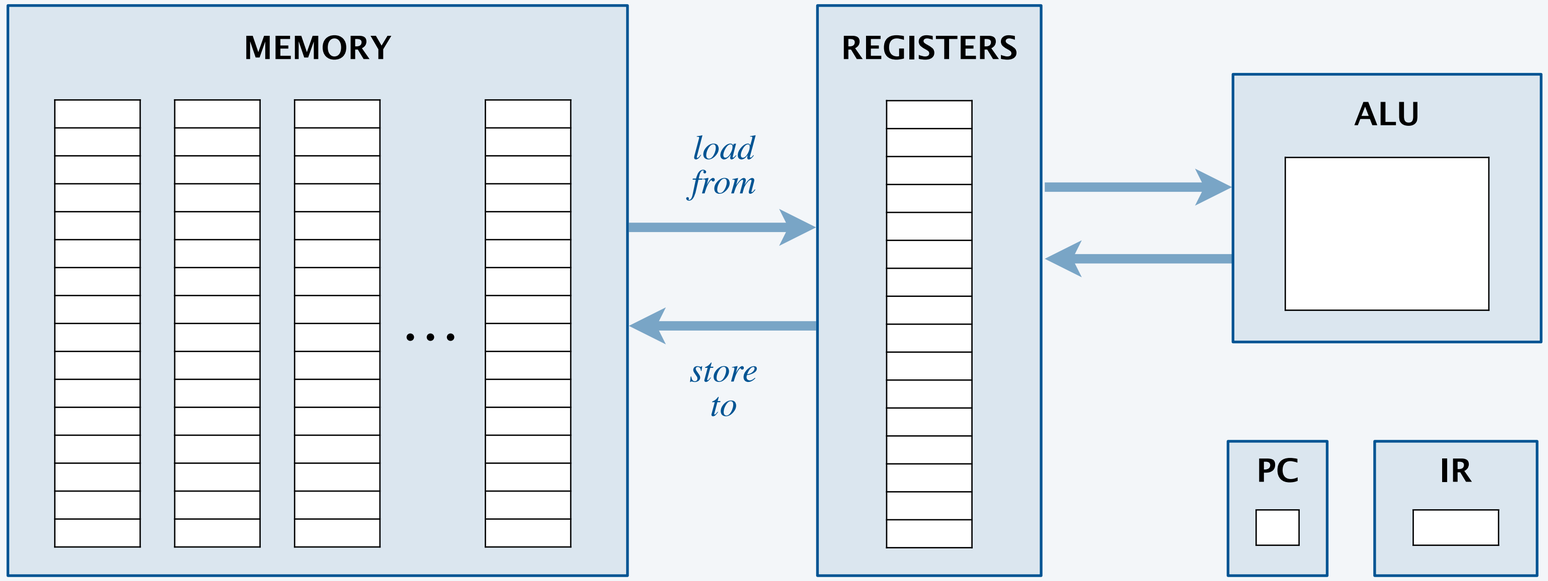
D. DAB2

decimal	binary	hex
0	0000	0
1	0001	1
2	0010	2
3	0011	3
4	0100	4
5	0101	5
6	0110	6
7	0111	7
8	1000	8
9	1001	9
10	1010	A
11	1011	B
12	1100	C
13	1101	D
14	1110	E
15	1111	F

Inside the box

TOY machine components.

- 256 memory cells.
- 16 registers.
- 1 arithmetic logic unit (ALU).
- 1 program counter (PC).
- 1 instruction register (IR).



Memory

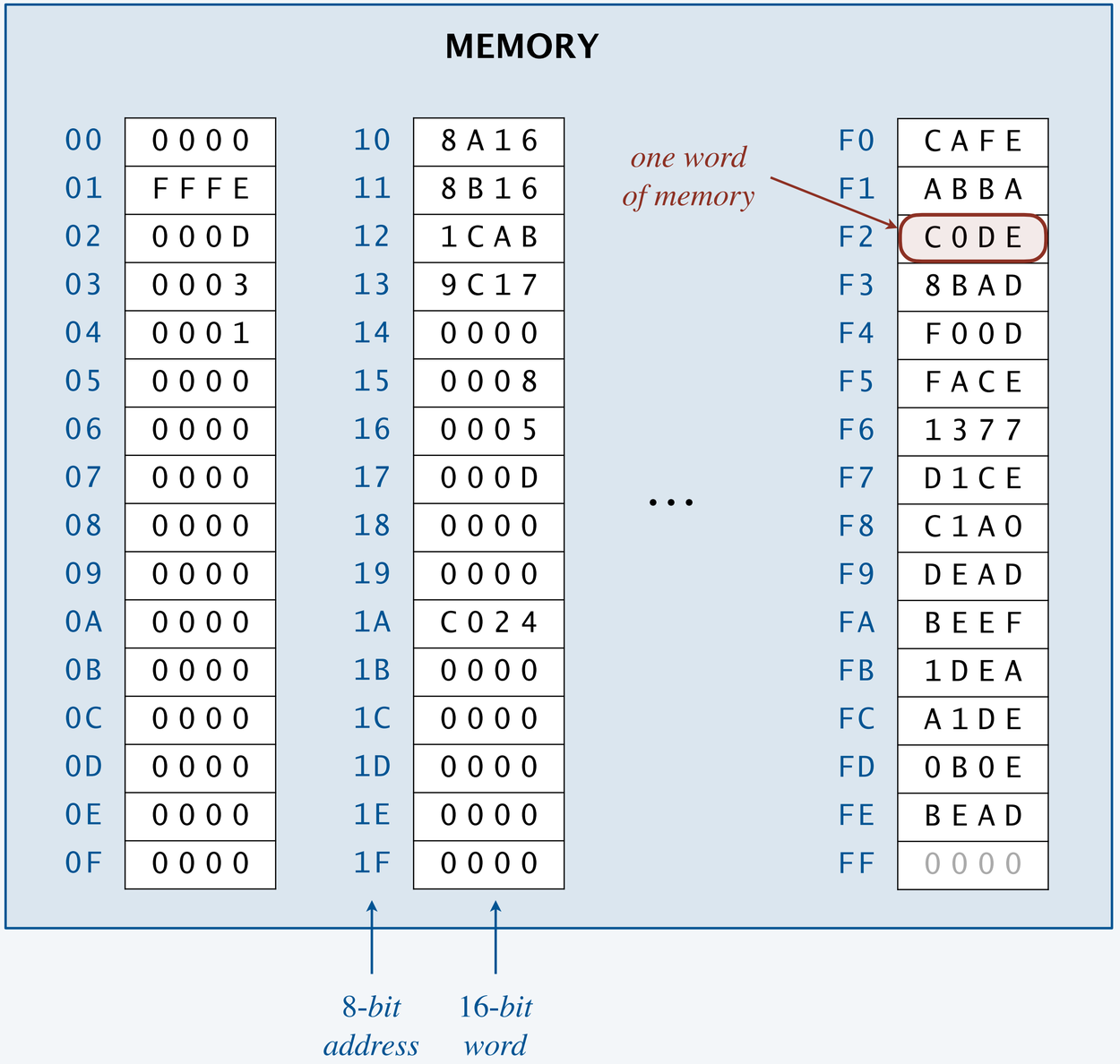
Memory.

- Holds data and instructions.
- 256 words of memory.
- 16 bits per word.

Memory is addressable.

- Specify individual word using array notation.
- Use hexadecimal for addresses: 00 to FF.
- Ex: `M[F2] = C0DE`.

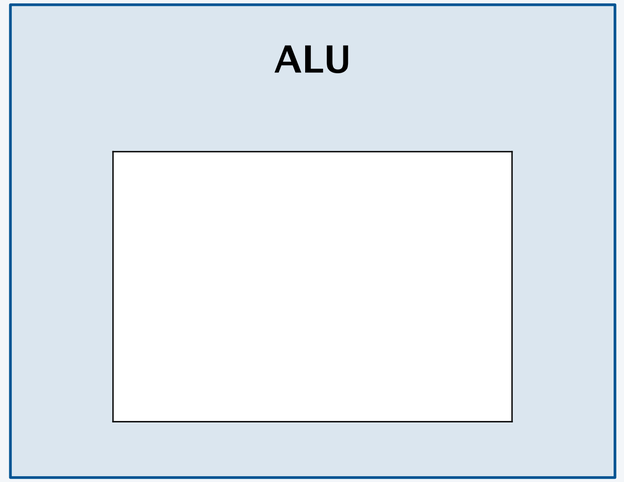
start thinking in hexadecimal

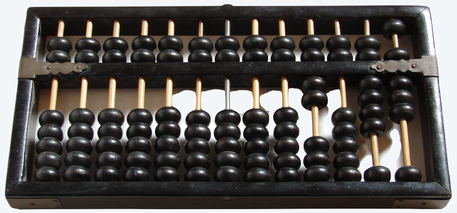


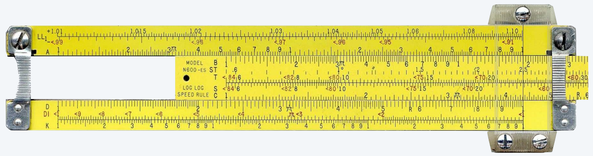
Arithmetic logic unit

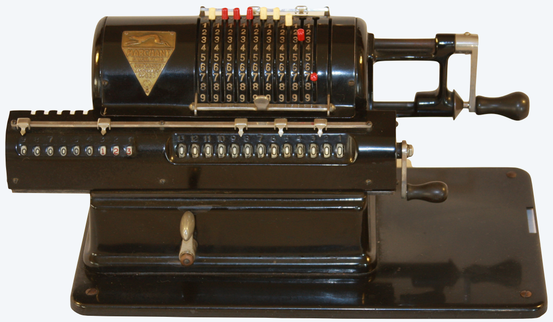
Arithmetic logic unit (ALU).

- TOY's computational engine.
- A calculator, not a computer.
- Hardware that implements *all* data-type operations (e.g., add and subtract).









Registers

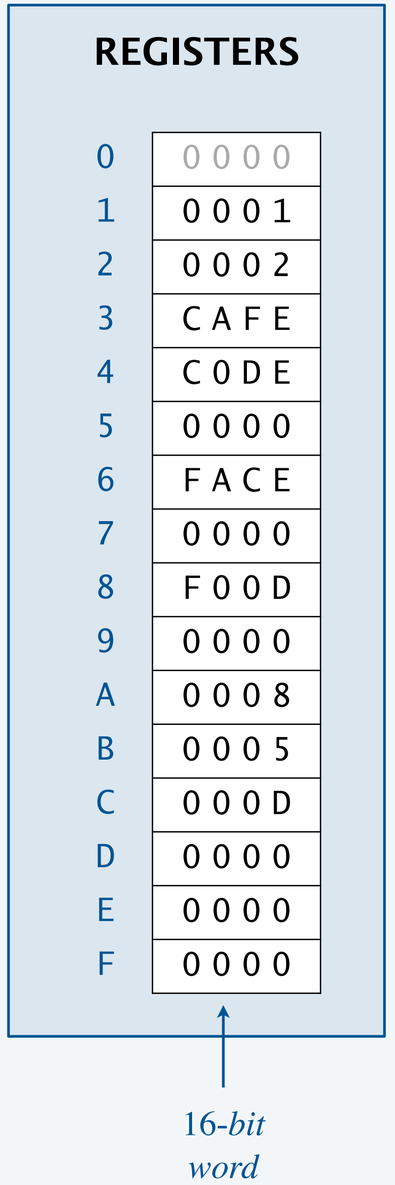
Registers.

- Scratch space for calculations and data movement.
- 16 registers, each storing one 16-bit word.
- Addressable as `R[0]` through `R[F]`.
- `R[0]` always stores `0000`.

Q. What's the difference between registers and main memory?

A. Registers are connected directly with ALU.

- faster than main memory
- more expensive than main memory

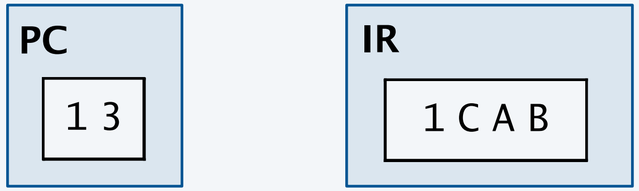


Control

TOY operates by executing a sequence of instructions.

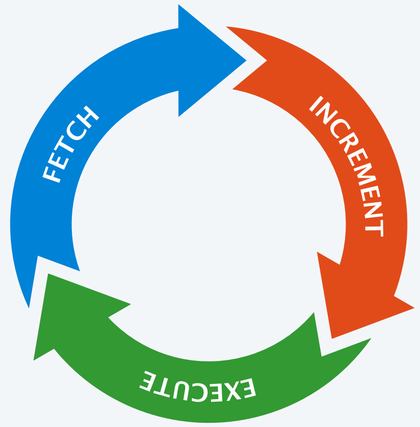
Program counter (PC). Stores memory address (8 bits) of *next* instruction to be executed.

Instruction register (IR). Stores instruction (16 bits) being executed.



Fetch-increment-execute cycle.

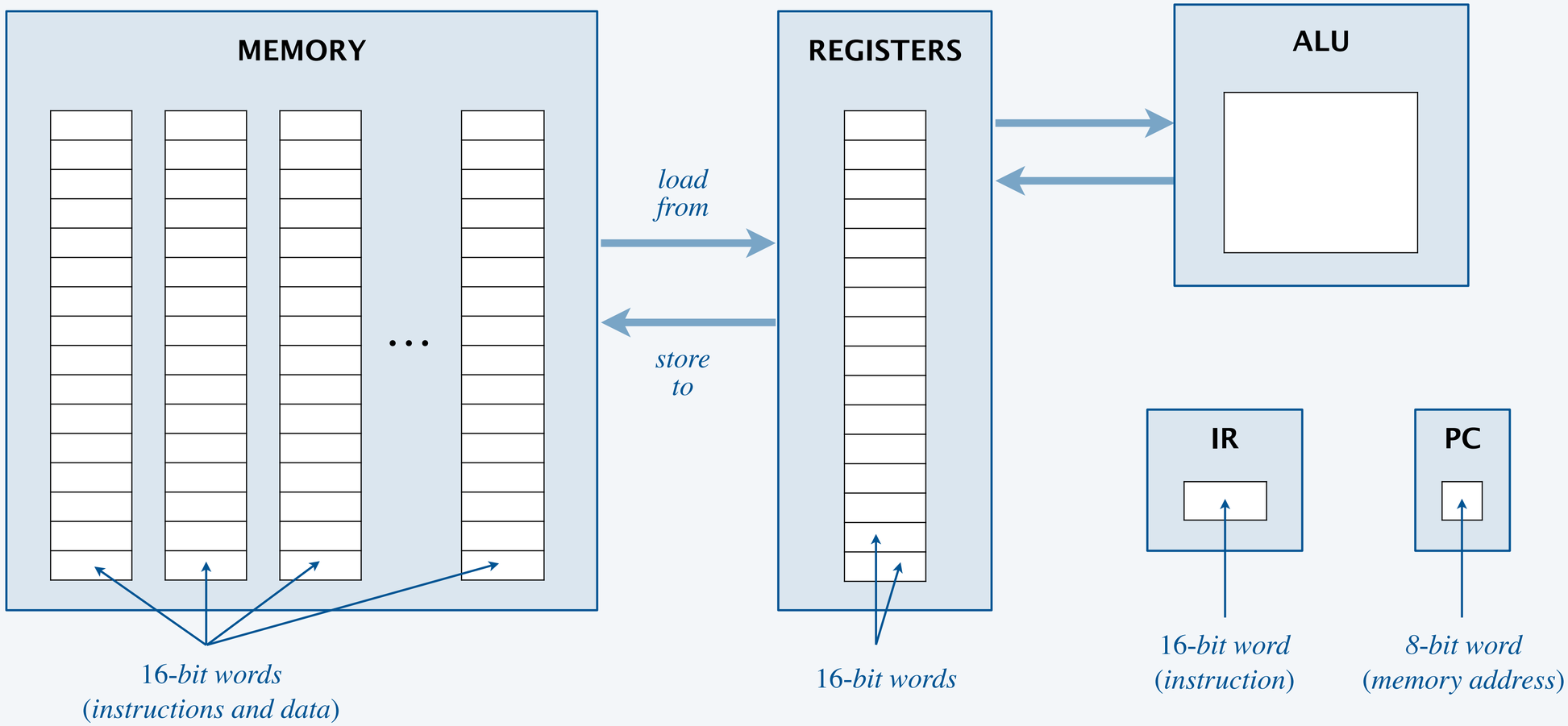
- Fetch: Get instruction (indexed by PC) from memory and store in IR.
- Increment: Update PC to point to next instruction.
- Execute: Move data to (or from) memory; change PC; or perform calculations.



The state of the machine

Contents of memory, registers, and PC at a particular time.

- Provide a record of what a program has done.
- Completely determines the machine will do.



TOY I: quiz 2

Approximate how many bytes of main memory does TOY machine have?

A. 250 bytes

B. 500 bytes

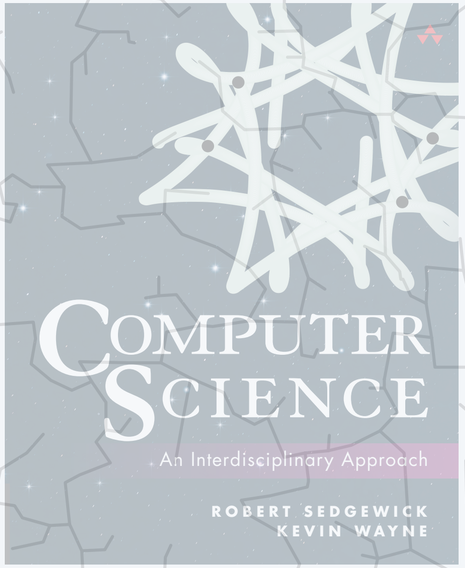
C. 4000 bytes

D. 250 MB

E. 500 GB

term	symbol	quantity
bit	b	1 bit
byte	B	8 bits
kilobyte	KB	1000 bytes
megabyte	MB	1000^2 bytes
gigabyte	GB	1000^3 bytes
terabyte	TB	1000^4 bytes
⋮	⋮	⋮

some define using powers of 2
(MB = 2^{10} *bytes*)



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6. TOY Machine I

- *overview*
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- *instructions*
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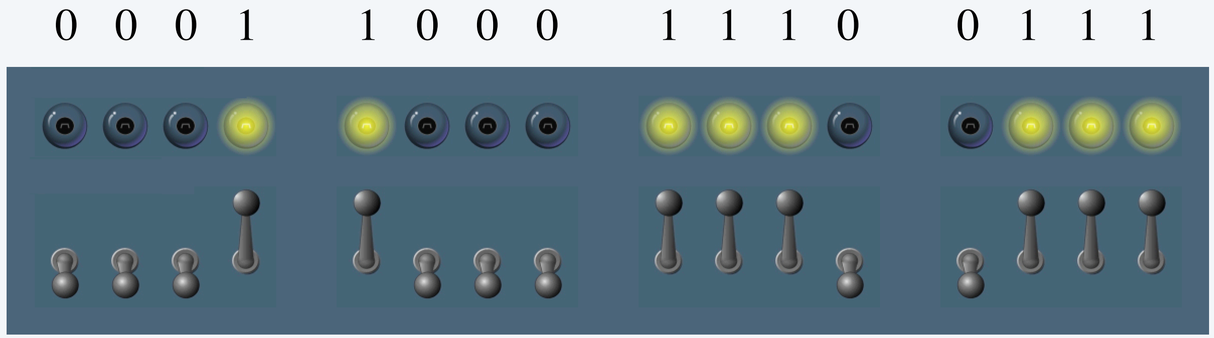
TOY data type

A data type is a set of values and a set of operations on those values.

TOY's data type.

- Value: 16-bit two's complement integer.
- Operations: arithmetic (add, subtract) and bitwise (AND, XOR, shift).

Representation. Each value is represented using one 16-bit word.



Note. All other types of data must be implemented with software. ← *32-bit integers, floating-point numbers, booleans, characters, strings, …*

Unsigned integers (16 bit)

Values. Integers 0 to $2^{16} - 1$. ← *only non-negative integers*

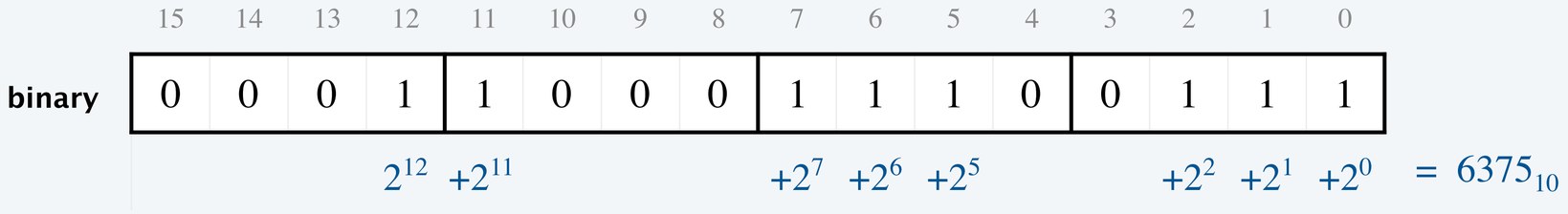
Operations.

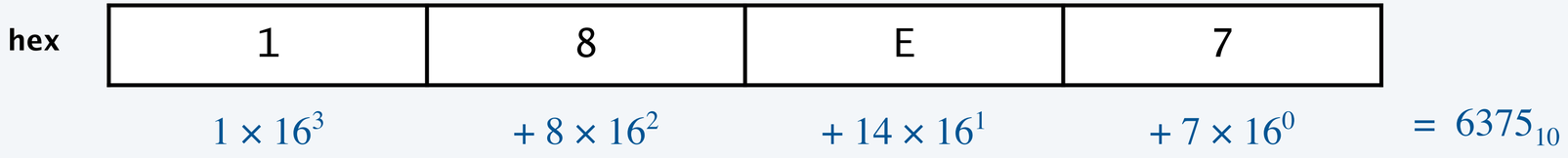
- Arithmetic: add, subtract.
- Bitwise: AND, XOR, left shift, right shift.

Representation. 16 bits.

decimal	hex	binary
0	0000	0000000000000000
1	0001	0000000000000001
2	0002	0000000000000010
3	0003	0000000000000011
4	0004	0000000000000100
⋮	⋮	⋮
65,533	FFFD	1111111111111101
65,534	FFFE	1111111111111110
65,535	FFFF	1111111111111111

largest integer $(2^{16} - 1)$





Signed integers (16-bit two's complement)

Values. Integers -2^{15} to $2^{15} - 1$. ← *includes negative integers!*

Operations.

- Arithmetic: add, subtract.
- Bitwise: AND, XOR, left shift, right shift.
- Comparison: test if positive, test if zero.

Representation. 16-bit two's complement.

- For $0 \le x < 2^{15}$, 16-bit unsigned representation of x.
- For $-2^{15} \le x < 0$, 16-bit unsigned representation of $2^{16} - |x|$.

"complement" of 2^{16}

decimal	hex	binary
−32,768	8000	1000000000000000
−32,767	8001	1000000000000001
−32,766	8002	1000000000000010
⋮	⋮	⋮
−3	FFFD	1111111111111101
−2	FFFE	1111111111111110
−1	FFFF	1111111111111111
0	0000	0000000000000000
+1	0001	0000000000000001
+2	0002	0000000000000010
+3	0003	0000000000000011
⋮	⋮	⋮
+32,765	7FFD	0111111111111101
+32,766	7FFE	0111111111111110
+32,767	7FFF	0111111111111111

smallest integer (-2^{15})

representation for 0 is 0000000000000000

largest integer ($2^{15} - 1$)

sign bit

Calculations with two's complement integers

Addition. To compute $x + y$:

- Add as unsigned integers.
- Ignore any overflow.

```
  1111111110000010      −126₁₀
+ 0000001111101000     1,000₁₀
------------------
  0000001101101010       874₁₀
```


ignore carry bit
out sign bit

Negation. To convert from x to $-x$ (or vice versa):

- Flip all bits.
- Add 1.

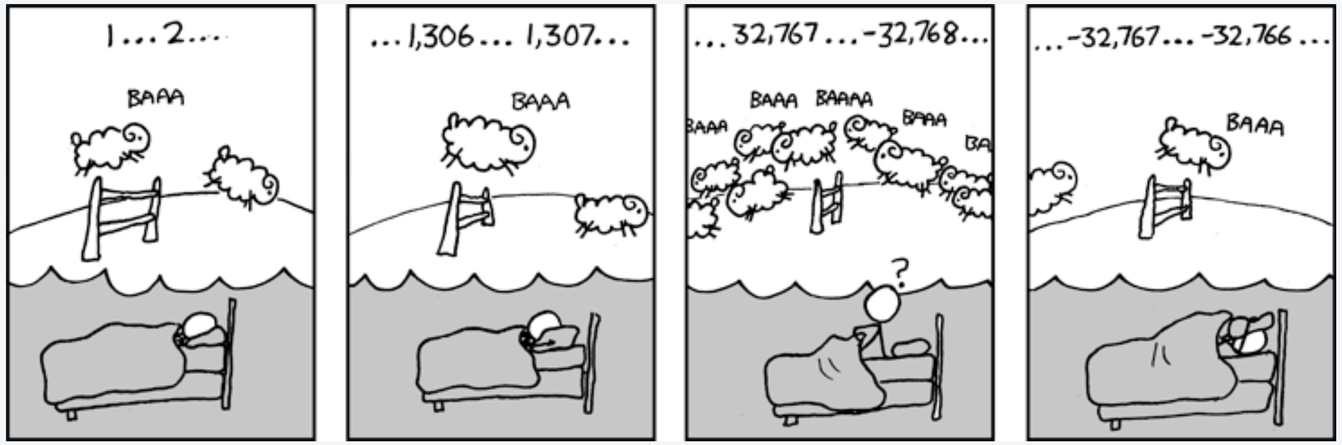
```
  0000000001111110      126₁₀
  1111111110000001      flip bits
+ 0000000000000001      add 1
------------------
  1111111110000010      −126₁₀
```

Overflow with two's complement integers

Integer overflow. Result of arithmetic operation is outside prescribed range (too large or small).

	0111111111111111	$32{,}767_{10}$	← *largest integer* $(2^{15} - 1)$
+	0000000000000001	1_{10}	
	1000000000000000	$-32{,}768_{10}$	← *smallest integer* (-2^{15})

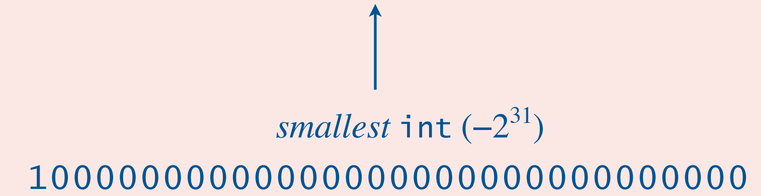
overflow (*carry into sign bit*)



https://xkcd.com/571

TOY I: quiz 3

Java's `int` data type is a 32-bit two's complement integer. What is `Math.abs(-2147483648)` ?



A. `-2147483648`

B. `2147483647`

C. `2147483648`

D. `ArithmeticOverflowError`

TOY data type: bitwise operations

Bitwise AND. Apply *and* operation to corresponding bits.

	0	1	0	1	1	0	0	1	0	1	0	0	1	0	0	0
&	0	0	0	1	1	1	1	1	0	0	0	0	0	1	0	1
	0	0	0	1	1	0	0	1	0	0	0	0	0	0	0	0

x	*y*	*x* & *y*
0	0	0
0	1	0
1	0	0
1	1	1

AND

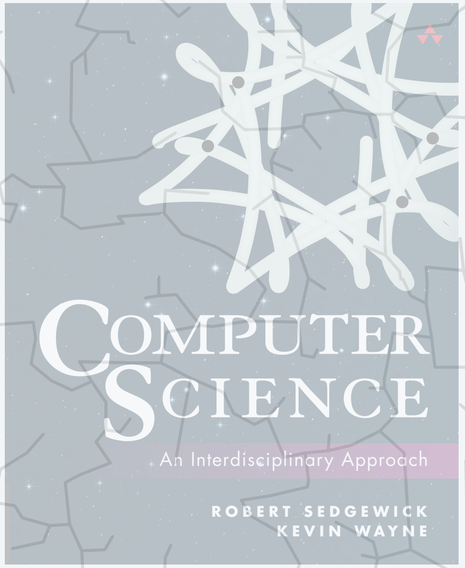
Bitwise XOR. Apply *xor* operation to corresponding bits.

	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1
^	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	1
	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	0

x	*y*	*x* ^ *y*
0	0	0
0	1	1
1	0	1
1	1	0

XOR

```
~/toy/toy1> jshell
jshell> int a = 3 ^ 5;
a ==> 6
```



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6. TOY Machine I

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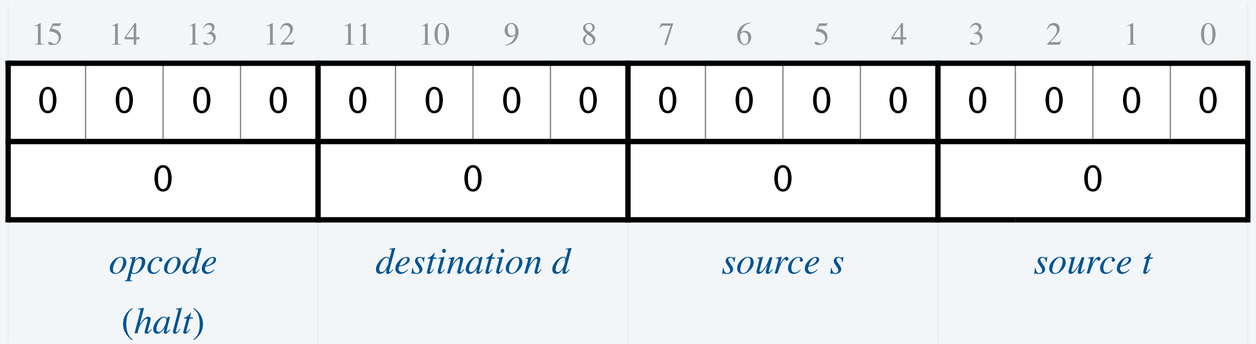
TOY instructions: halt

TOY program. A TOY program is a sequence of TOY instructions.

Instructions. Any 16-bit value can be interpreted as a TOY instruction.

Halt. Stop executing the program.

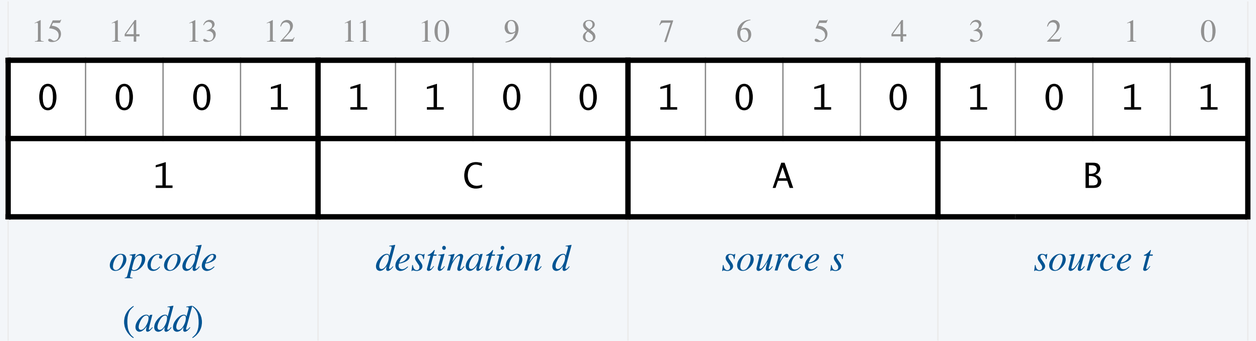


TOY instructions: add

TOY program. A TOY program is a sequence of TOY instructions.

Instructions. Any 16-bit value can be interpreted as a TOY instruction.

Add. Add two 16-bit integers from registers and store the sum in a register.



Pseudocode. `R[C] = R[A] + R[B]` ← *add* `R[A]` *and* `R[B]`; *put result in* `R[C]`

Registers

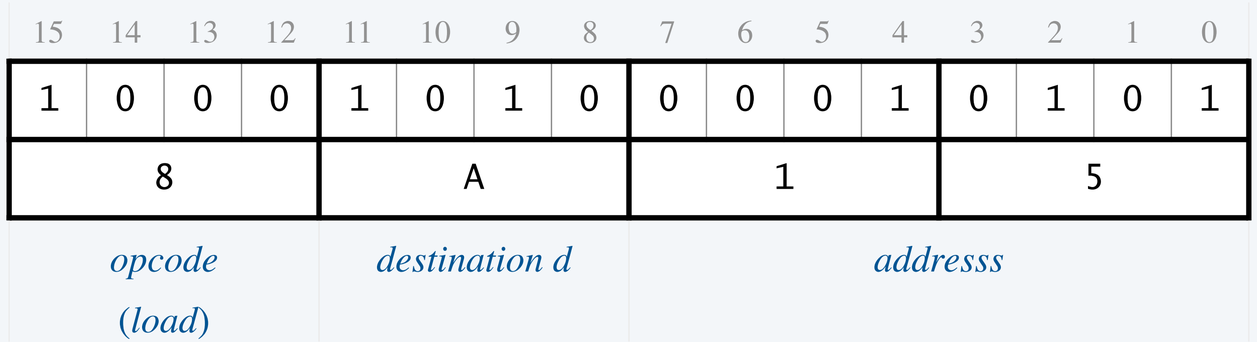
R[0]	0 0 0 0
R[1]	0 0 0 1
R[2]	0 0 1 0
R[3]	C A F E
R[4]	0 0 0 1
R[5]	0 0 0 0
R[6]	C 0 D E
R[7]	0 0 0 0
R[8]	F 0 0 D
R[9]	0 0 0 0
R[A]	0 0 0 8
R[B]	0 0 0 5
R[C]	0 0 0 D
R[D]	0 0 0 0
R[E]	0 0 0 0
R[F]	0 0 0 0

TOY instructions: load and store

TOY program. A TOY program is a sequence of TOY instructions.

Instructions. Any 16-bit value can be interpreted as a TOY instruction.

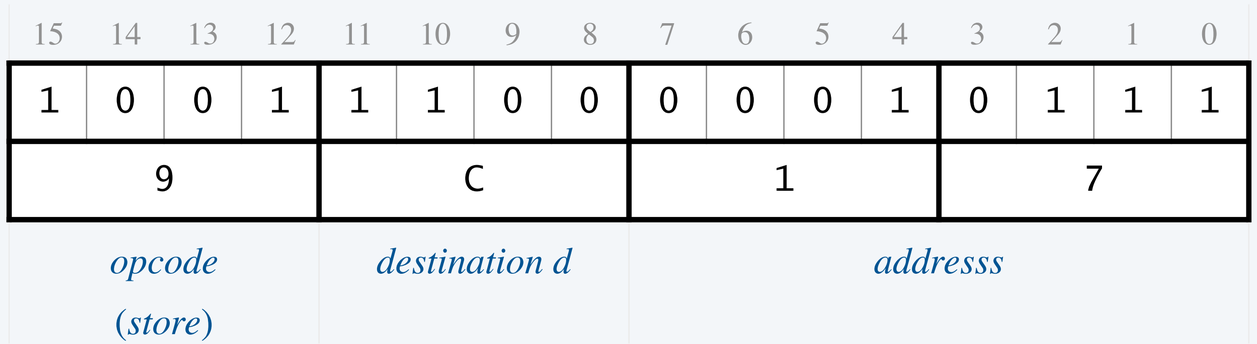
Load. Copy a 16-bit integer from a memory cell to a register.



load data from `M[15]` *into* `R[A]`

```
R[A] = M[15]
```

Store. Copy a 16-bit integer from a register to a memory cell.



store contents of `R[C]` *into* `M[17]`

```
M[17] = R[C]
```

Your first TOY program

Add two integers.

- Load operands from memory into two registers.
- Add the 16-bit integers in the two registers.
- Store the result in memory.

MEMORY

```
 ⋮    ⋮
10: 8A15   R[A] = M[15]
11: 8B16   R[B] = M[16]
12: 1CAB   R[C] = R[A] + R[B]
13: 9C17   M[17] = R[C]
14: 0000   halt
15: 0008   input 1
16: 0005   input 2
17: 0000   output
 ⋮    ⋮
```

REGISTERS

```
   ⋮      ⋮
R[A]   0 0 0 0
R[B]   0 0 0 0
R[C]   0 0 0 0
   ⋮      ⋮
```

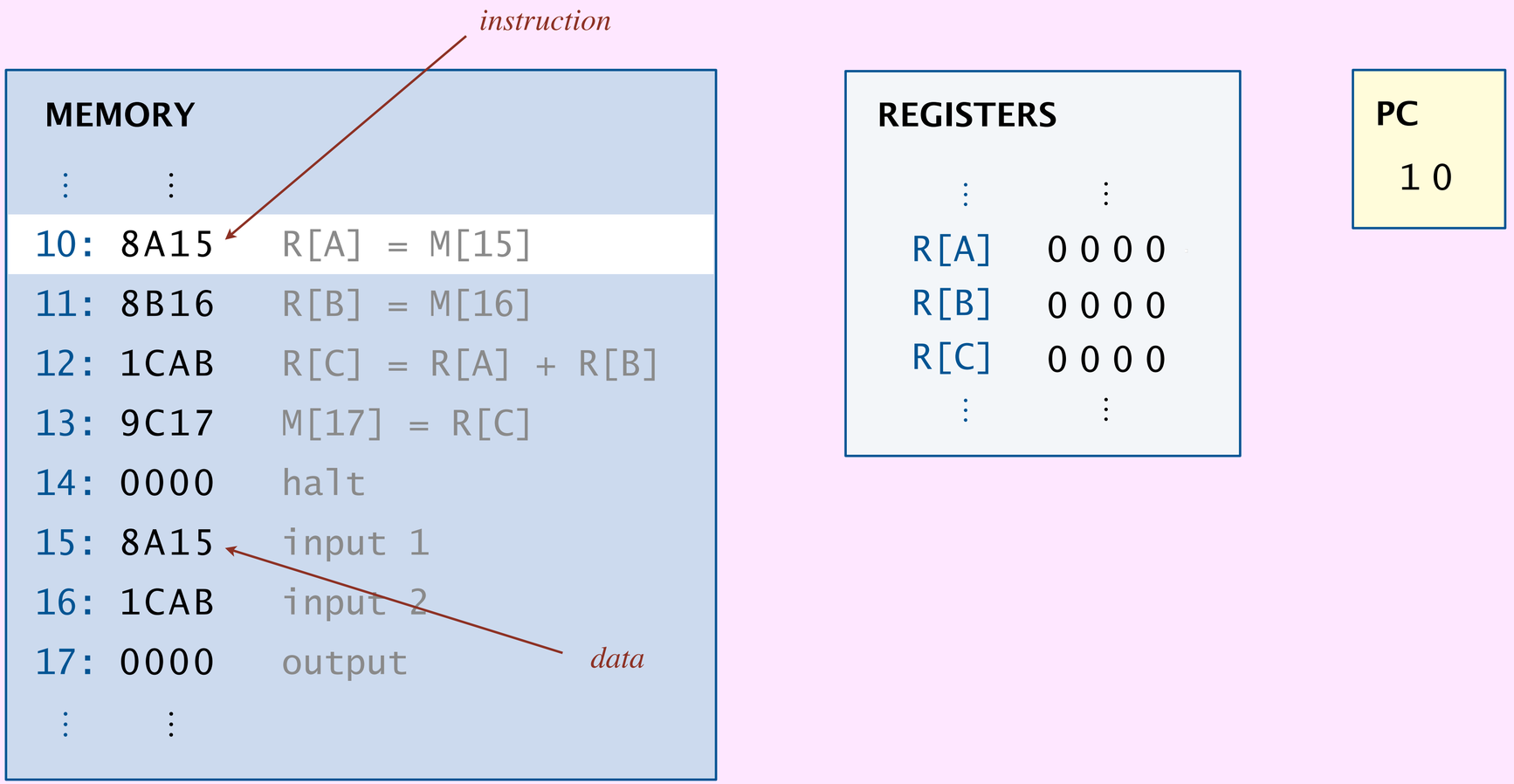
PC

1 0

Your first TOY program (with different data)

Q. How can you tell whether a word is an instruction or data?

A. If the PC has its address, it is an instruction.



Instruction set

Instruction set. Complete list of machine instructions.

- First hex digit (opcode) specifies which instruction.
- Each instruction changes machine in well-defined way.

category	opcodes	implements	changes
arithmetic and logic operations	1 2 3 4 5 6	data-type operations	registers
data movement	7 8 9 A B	data moves between registers and memory	registers, memory
flow of control	0 C D E F	conditionals, loops, and functions	program counter

opcode	instruction
0	*halt*
1	*add*
2	*subtract*
3	*bitwise and*
4	*bitwise xor*
5	*shift left*
6	*shift right*
7	*load address*
8	*load*
9	*store*
A	*load indirect*
B	*store indirect*
C	*branch if zero*
D	*branch if positive*
E	*jump register*
F	*jump and link*

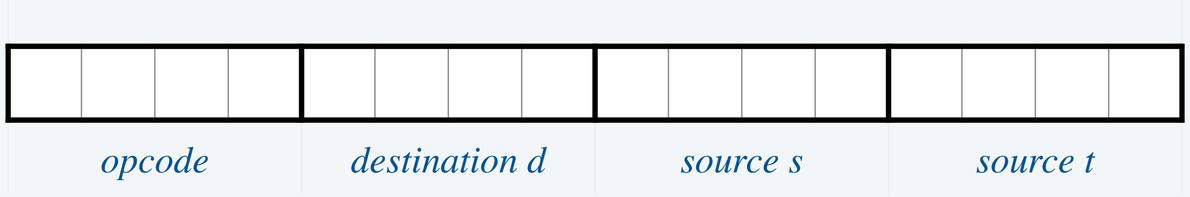
Instruction set

Instruction set. Complete list of machine instructions.

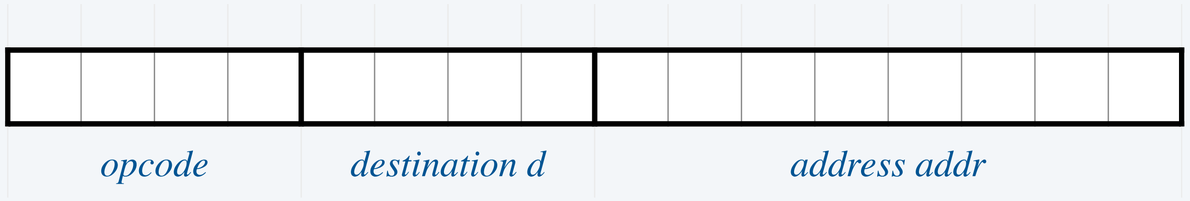
- First hex digit (opcode) specifies which instruction.
- Each instruction changes machine in well-defined way.

Instruction formats. How to interpret a 16-bit instruction?

- Format *RR*: opcode and three registers.



- Format *A*: opcode, one register, and one memory address.



opcode	format	instruction
0	—	*halt*
1	*RR*	*add*
2	*RR*	*subtract*
3	*RR*	*bitwise and*
4	*RR*	*bitwise xor*
5	*RR*	*shift left*
6	*RR*	*shift right*
7	*A*	*load address*
8	*A*	*load*
9	*A*	*store*
A	*RR*	*load indirect*
B	*RR*	*store indirect*
C	*A*	*branch if zero*
D	*A*	*branch if positive*
E	*RR*	*jump register*
F	*A*	*jump and link*

TOY I: quiz 4

Which instruction copies the values in `R[A]` to `R[B]` ?

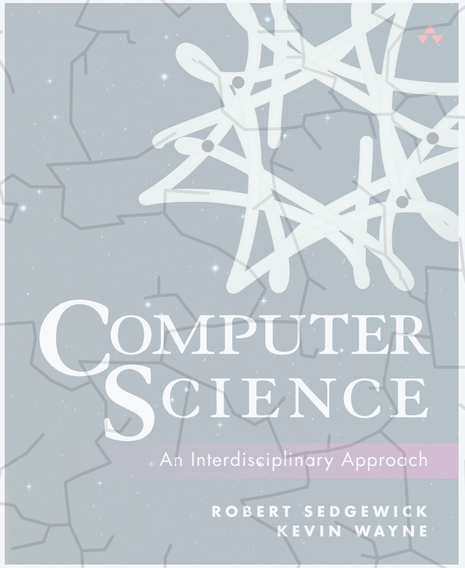
A. `1BA0` `R[B] = R[A] + R[0]`

B. `2BA0` `R[B] = R[A] - R[0]`

← `R[0]` *is always* 0000

C. `3BAA` `R[B] = R[A] & R[A]`

D. All of the above.



https://introcs.cs.princeton.edu

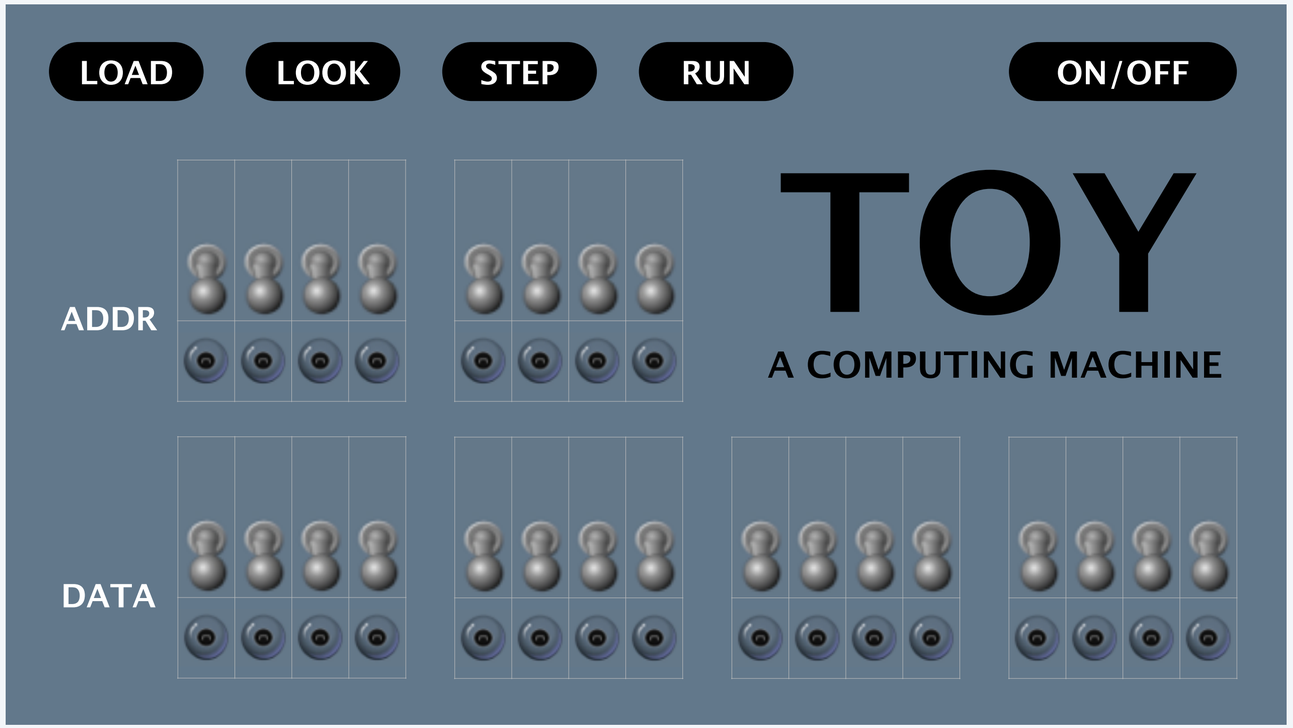
6. TOY Machine I

- *overview*
- *data types*
- *instructions*
- *operating the machine*

Outside the box

User interface

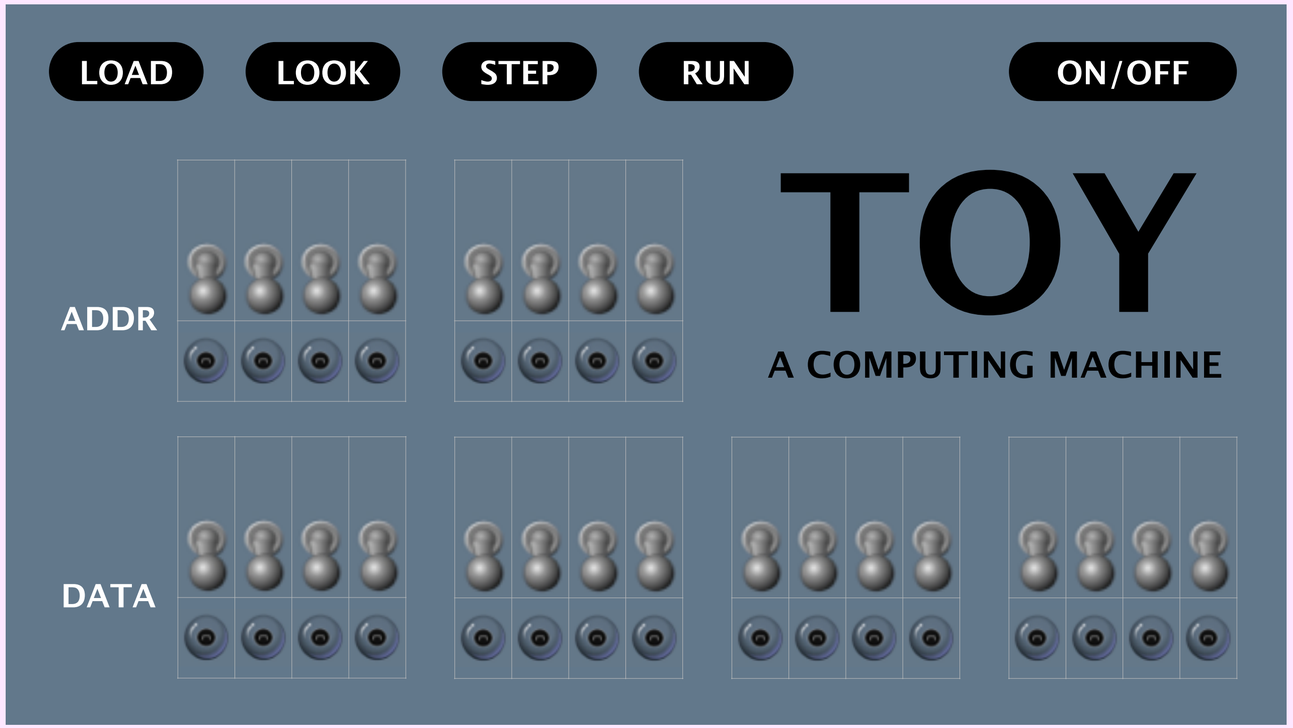
- Switches.
- Lights.
- Control buttons.



TOY machine demo

To load an instruction or data into memory:

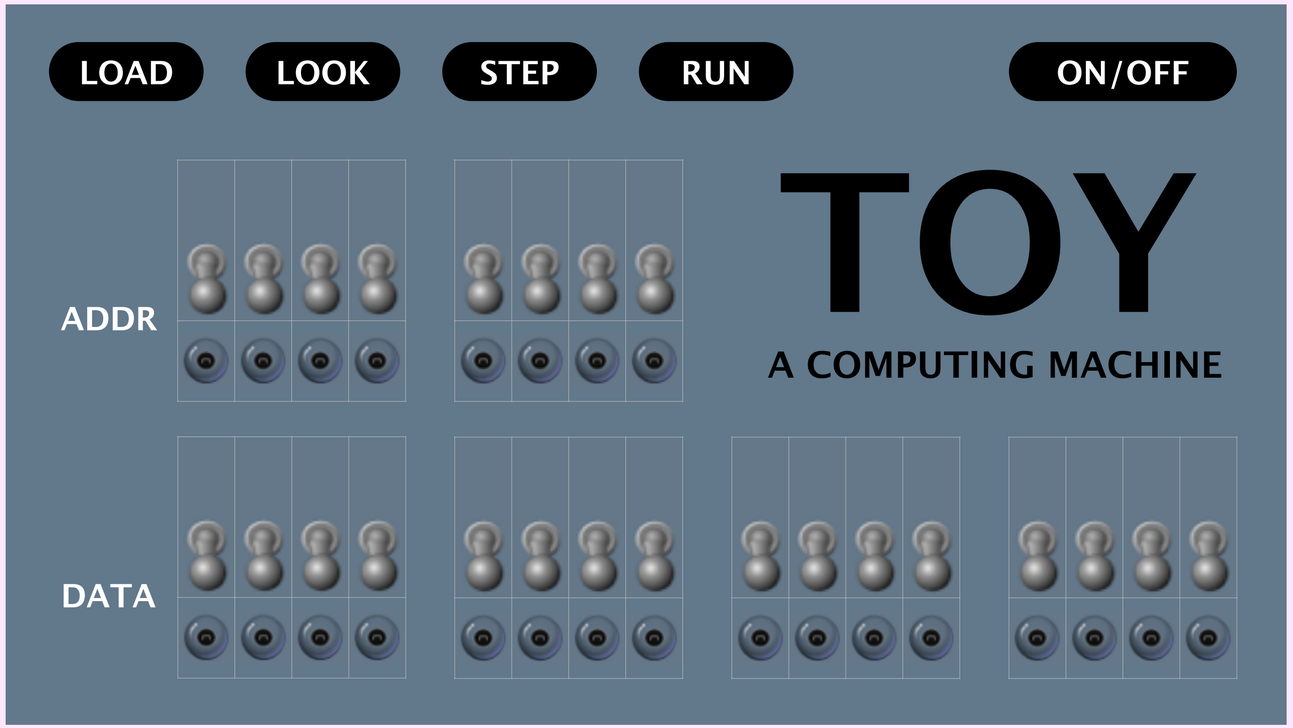
- Set the 8 memory address switches.
- Set the 16 data switches.
- Press LOAD.



TOY machine demo

To view the data in memory:

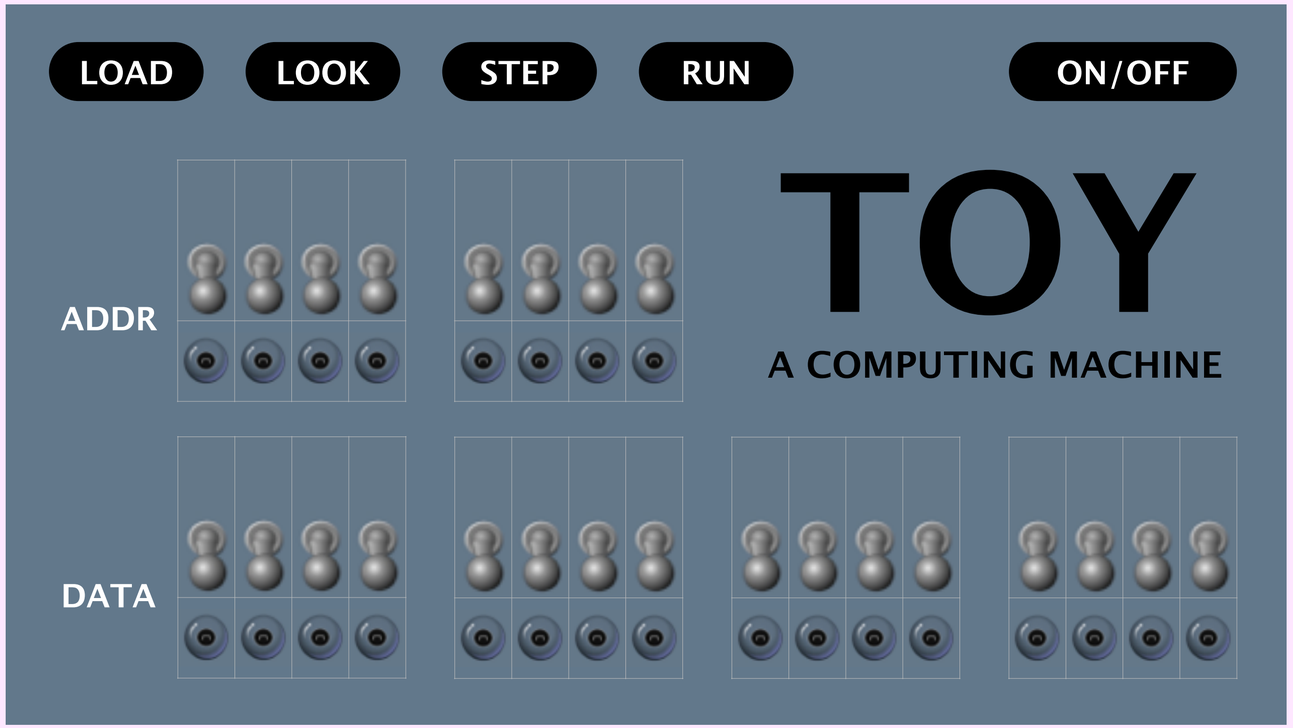
- Set the 8 address switches.
- Press LOOK.



TOY machine demo

To run a program:

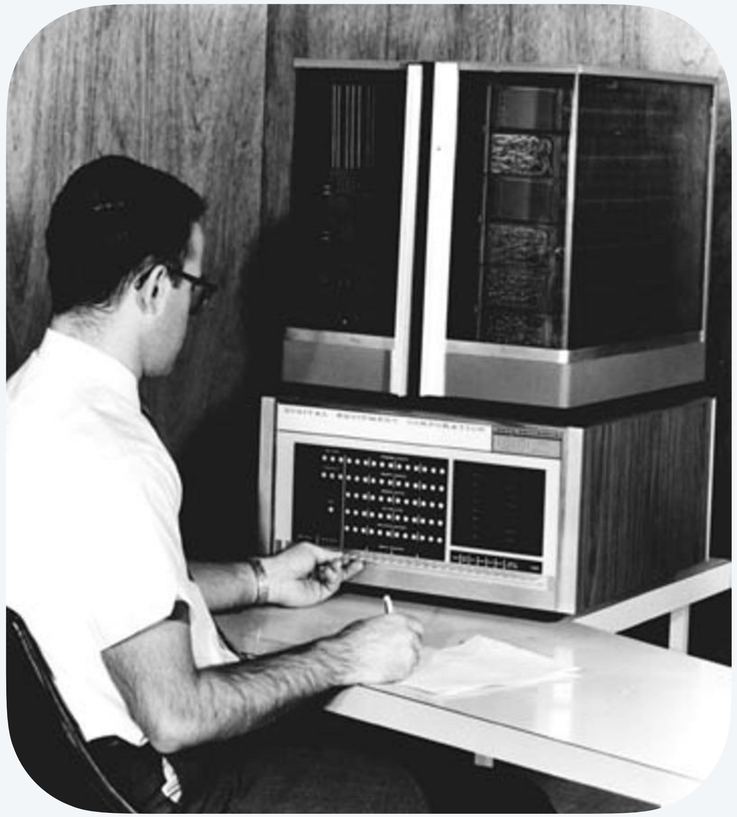
- Set the 8 address switches to the address of first instruction.
- Press RUN.



Switches and lights

Q. Did people really program this way?

A. Yes! We have it good.

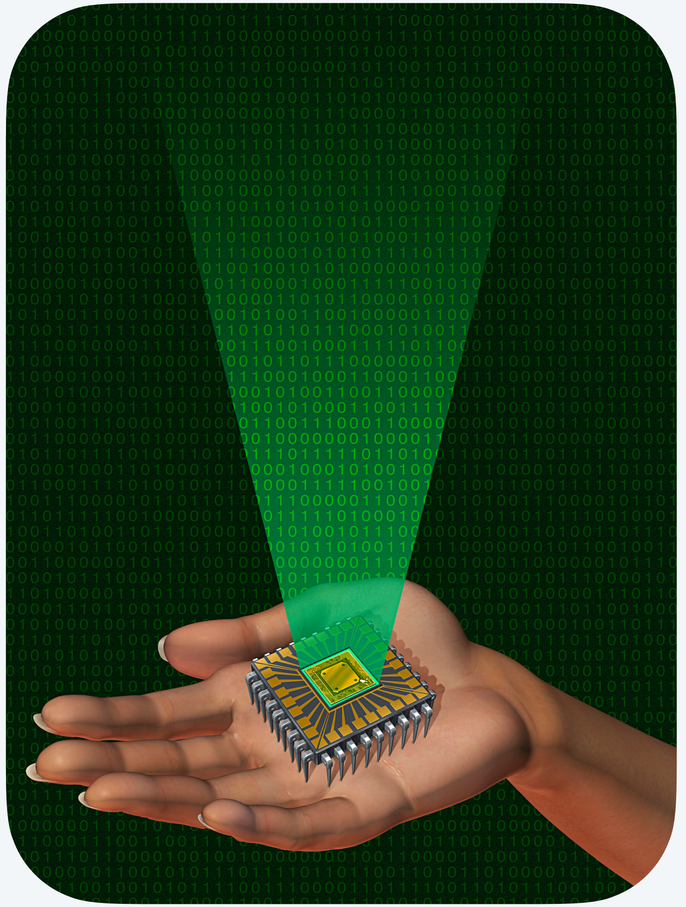


DEC PDP-8 (1964)

TOY summary

TOY machine has same basic architecture as modern CPUs:

- Arithmetic logic unit (ALU).
- Memory and registers.
- Program counter (PC) and instruction register (IR).
- Input and output.



TOY supports same basic programming constructs as Java:

- Primitive data types.
- Arithmetic/logic operations.
- Conditionals and loops.
- Input and output.
- Arrays.
- Functions.
- Linked structures.

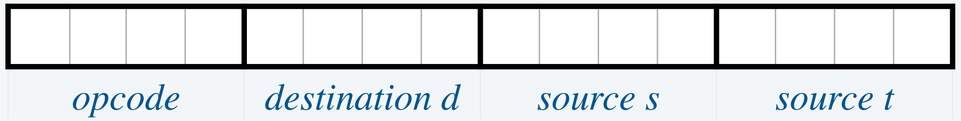
next lecture

see textbook

TOY reference sheet

opcode	operation	format	pseudo-code
0	*halt*	—	`halt`
1	*add*	*RR*	`R[d] = R[s] + R[t]`
2	*subtract*	*RR*	`R[d] = R[s] - R[t]`
3	*bitwise and*	*RR*	`R[d] = R[s] & R[t]`
4	*bitwise xor*	*RR*	`R[d] = R[s] ^ R[t]`
5	*shift left*	*RR*	`R[d] = R[s] << R[t]`
6	*shift right*	*RR*	`R[d] = R[s] >> R[t]`
7	*load address*	*A*	`R[d] = addr`
8	*load*	*A*	`R[d] = M[addr]`
9	*store*	*A*	`M[addr] = R[d]`
A	*load indirect*	*RR*	`R[d] = M[R[t]]`
B	*store indirect*	*RR*	`M[R[t]] = R[d]`
C	*branch zero*	*A*	`if (R[d] == 0) PC = addr`
D	*branch positive*	*A*	`if (R[d] > 0)  PC = addr`
E	*jump register*	*RR*	`PC = R[d]`
F	*jump and link*	*A*	`R[d] = PC; PC = addr`

format RR



format A

zero `R[0]` *is always* `0000`.

standard input *Load from* `M[FF]`.

standard output *Store to* `M[FF]`.

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