Computer Science

input and output

arrays

 von Neumann architecture TOY emulator

OMPUTER CIENCE

An Interdisciplinary Approach

ROBERT SEDGEWICK KEVIN WAYNE

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6. TOY MACHINE II

conditionals and loops

Last updated on 4/13/25 12:55PM





TOY machine.

- Arithmetic logic unit (ALU).
- Memory and registers.
- Program counter (PC) and instruction register (IR).
- Lights and switches.

TOY programming.

- Move data between memory and registers.
- Arithmetic/logic operations.
- Conditionals and loops.
- Arrays.
- Standard input and output.
- Functions.
- Linked structures.







this lecture/precept





Add two integers.

- Load operands from memory into two registers.
- Add the two registers.
- Store the result in memory.

MEMORY			
:	• •		
10:	8A15	R[A] = M[15]	
11:	8B16	R[B] = M[16]	
12:	1CAB	R[C] = R[A] + R[B]	
13:	9C17	M[17] = R[C]	
14:	0000	halt	
15:	8000	input 1	
16:	0005	input 2	
17:	0000	output	
•	•		



REGISTERS : : R[A] 0 0 0 R[B] 0 0 0 0 R[C] 0 0 0 0 : : : : :

PC 1 0



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6. TOY MACHINE II

conditionals and loops

+ input and output

array

- von Neumann architecture
- TOY emulator



Conditionals and loops

To control the flow of instruction execution.

- Test a register's value.
- Change the PC, depending on the value.

Ex 1. Typical if statement.



replace R[A] with absolute value of R[A]

opcode	instruction	pseudocode
С	branch if zero	if (R[d] == 0) PC = a
D	branch if positive	if (R[d] > 0) PC = a

skips line 16 if R[A] > 0

replace a with |a|



Conditionals and loops

To control the flow of instruction execution

- Test a register's value.
- Change the PC, depending on the value.

Ex 2. Typical while loop.



line 14 is repeated R[A] times (assuming R[A] is non-negative)

opcode	instruction	pseudocode
С	branch if zero	if (R[d] == 0) PC = a
D	branch if positive	if (R[d] > 0) PC = a

skip lines 14 *to* 17 *if* R[A] *is* 0

goto line 13 (R[0] is always 0)

repeat a times (assuming a is non-negative)





Goal. Compute product of two positive integers: c = Algorithm. Initialize c = 0; then, add b to c, a times.

	10.	2 Λ1Λ	ΡΓΛΊ - ΜΓΊΛΊ
	10.		N[A] - M[1A]
	11:	8 R T R	K[R] = M[TR]
	12:	7C00	R[C] = 0
$\square \rightarrow$	13:	CA18	if (R[A] == 0) goto 18
	14:	1CCB	R[C] = R[C] + R[B]
	15:	7101	R[1] = 1
	16:	2AA1	R[A] = R[A] - 1
	17:	C013	goto 13
	18:	9C1A	M[1C] = R[C]
	19:	0000	halt
	1A:	0007	input a
	1B:	0009	input b
	1C:	0000	output c = a * b

$a \times b$

opcode	instruction	pseudocode
С	branch if zero	if (R[d] == 0) PC = a
D	branch if positive	if (R[d] > 0) PC = a

loop template from previous slide

multiplication: $c = a \times b$ (via repeated addition)

input and output





Upon termination, which value is stored in R[A] **?**





Upon termination, which value is stored in R[B] **?**



L01	R[1] = 1
04	R[A] = 4
801	R[B] = 1
AA1	R[A] = R[A] - 1
B B B	R[B] = R[B] + R[B]
13	if (R[A] > 0) goto 13
000	halt



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6. TOY MACHINE II

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 TOY emulator



Standard input and output

An immediate problem. Can't address real-world problems with just switches and lights for I/O.



Punched paper tape.

- Encode each 16-bit word in two 8-bit rows.
- To *write* a word, punch a hole for each 1.
- To *read* a word, shine a light behind the tape and sense the holes.

TOY mechanism.

- Connect hardware to memory address FF.
- To write the contents of a register to stdout, store to M[FF].
- To read from stdin into a register, load from M[FF].





Standard input and output: absolute value

Goal. Read integers from standard input (stop on 000 write absolute value to standard output.

	10: 8AFF 11: CA16 12: DA14 13: 2A0A 14: 9AFF 15: C010 16: 0000	<pre>Read R[A] from stdin ← if (R[A] == 0) goto 16 if (R[A] > 0) goto 14 R[A] = -R[A] write R[A] to stdout ← goto 10 halt</pre>
--	--	--

00);	opcode	operation	pseudocode
	8	load	R[d] = M[add
	9	store	M[addr] = R[d

read from standard input (since address is FF)

write to standard output (since address is FF) while (true) {
 a = StdIn.readInt();
 if (a == 0) break;
 if (a <= 0) a = -a;
 StdOut.println(a);
}</pre>



Standard input and output trace

Goal. Read integers from standard input (stop on 000 write absolute value to standard output.

10: 8AFF	Read R[A] from stdin
11: CA16	if (R[A] == 0) goto 16
12: DA14	if (R[A] > 0) goto 14
13: 2A0A	R[A] = -R[A]
14: 9AFF	write R[A] to stdout
15: C010	goto 10
16: 0000	halt

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6. TOY MACHINE II

- conditionals and loops
- + input and output

► arrays

- von Neumann architecture
- TOY emulator



Upon termination, which value is stored in R[C] **?**

- **A.** 000A
- **B.** 0011
- **C.** 8B12
- D. ACOA

10: 7A11	R[A] = 11
11: 8B12	R[B] = M[12]
12: ACOA	$R[C] = M[R[A]] \leftarrow$
13: 0000	halt

opcode	operation	pseudocode
7	load address	R[d] = addı
8	load	R[d] = M[add
A	load indirect	R[d] = M[R[t]















































To implement an array:

- Keep array elements contiguous in memory, say, s
- Access array element i at M[80 + i]. using load/sto

Goal. Print elements in an array of length n > 0 to star



	opcode	operation	pseudocode
starting at 80.	7	load address	R[d] = add
ore indirect.	Α	load indirect	R[d] = M[R[t]
ndard output.	В	store indirect	M[R[t]] = R[

array starts at	R[A]	= 80
and has length	R[B]	= 9

load next array element into R[C]

"array" of length 9

80:	CODE
81:	CAFE
82:	ABBA
83:	8BAD
84:	FOOD
85:	FACE
86:	1377
87:	D1CE
88:	C1A0





Suppose that we execute the same program, but initialize R[A] to 10. What is the result?

- A. Prints 0010, 0011, 0012, ..., 0017, 0018.
- **B.** Prints 7A10, 7B09, 7101, ..., CB13, 0000.
- C. Crashes when R[A] is 0013.
- **D.** Infinite loop.

	10: 11:	7A10 7B09	R[A] R[B]
	12:	7101	R[1]
\rightarrow	13:	ACOA	R[C]
	14:	9CFF	write
	15:	1AA1	R[A]
	16:	2BB1	R[B]
	17:	CB13	if (R
	18:	0000	halt





array now starts at R[A] = 10



Pointers



https://imgs.xkcd.com/comics/pointers.png



Direct addressing.Specify memory address to access.Indirect addressing.Specify register containing memory address to access.

Pointer. Variable/register that stores a memory address.

Indirection. Manipulating a value through its memory address.

- TOY arrays.
- Java references.
- C pointers.
- ...

SIMPLY EXPLAINED





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TOY vs. your laptop

Two different computing machines.

- Both implement basic data types, conditionals, loops, and other low-level constructs.
- Both can have arrays, functions, linked structures, and other high-level constructs.
- Both have unbounded input and output streams.



A few key differences.

- Performance: 1Hz vs. 3.5 GHz.
- Memory: 512 bytes vs. 32GB.
- Input/output devices: display, keyboard, trackpad, speakers, webcam, ...



An early computer

Electronic Numerical Integrator and Calculator (ENIAC).

- First widely-known general-purpose electronic computer.
- "Programmable", but no memory.
- **Programming**: change switches and cable connections.
- Data: enter numbers using punch cards.



two programmers "programming" the ENIAC (1946)





J. Presper Eckert



John W. Mauchly

facts and figures

30 *tons*

 $30 \times 50 \times 8.5$ feet

17,468 vacuum tubes

300 multiply/sec



one bit (vacuum tube)



Von Neumann architecture

First Draft of a Report on the EDVAC (1945).

- Brilliant summation of a stored-program machine.
- Written by John von Neumann on a train.
- Based upon EDVAC design of Eckert–Mauchly; influenced by Turing.



Keys elements.

- Data and instructions encoded in binary.
- ALU, control, memory, registers, and input/output.



What does the following program print to standard output?

1

- **A.** 0000
- **B.** 0088
- **C.** 0088,0088,0088,0088,...
- **D.** Nothing.

.0:	7202	R[2] = 2	
1:	7A88	R[A] = 88	
.2:	AB16	R[B] = M[16] ←	R[B] <i>stores</i> C017
.3:	2BB1	$R[B] = R[B] - 2 \longleftarrow$	R[B] <i>stores</i> C015
.4:	BB16	M[16] = R[B]	
.5:	9AFF	write R[A] to stdout	
.6:	C013	goto 13	
.7:	0000	halt	



Stored-program (von Neumann) architecture is the basis of nearly all computers since the 1950s.

Practical implications.

- Programming: develop programs without rewiring.
- Download apps: load programs, not just data, into memory.
- Compilers:
- Code-injection attacks: trick program into treating input data as code.





write programs that take programs as input (and produce programs as output).









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von Neumann architecture

TOY emulator

array.



TOY emulator

- **Q.** How did we debug all our TOY programs?
- A. We wrote a Java program to emulate a TOY machine.

Emulator. Hardware or software that enables one computer system to behave like another.



Remarks.

- YOU could write a TOY emulator (ahead).
- We designed TOY by refining this code.
- All computers are designed in this way.

estimated number of Android devices: 1 billion+



estimated number of TOY devices: 1 billion+





TOY emulator in Java: high-level design

Goal. Write a Java program that emulates the TOY machine.









and produces same output



TOY emulator: fetch and increment

Fetch. Get instruction from memory location indexed by PC. Increment. Increment PC by 1.

int ir = M[pc]; // fetch
pc++; // increment



TOY emulator: decode instruction

Decode. Extract relevant components from instruction register (IR).

- Call String.format() to get 4 hex digits as a String.
- Call substring() to extract relevant hex digit(s).
- Call Integer.parseInt() to convert from hex string.

Alternative. Use shift-and-mask technique.

```
int ir = M[pc]; // fetch
      // increment
pc++;
                                       hex
String hex = String.format("%04X", ir);
int op = Integer.parseInt(hex.substring(0,
        = Integer.parseInt(hex.substring(1,
int d
        = Integer.parseInt(hex.substring(2,
int s
int t
      = Integer.parseInt(hex.substring(3,
int addr = Integer.parseInt(hex.substring(2,
```

0	1	2	3
1	С	Α	В
ор	d	S	t
$\begin{array}{c} 1)), \ 16);\\ 2)), \ 16);\\ 3)), \ 16);\\ 4)), \ 16);\\ 4)), \ 16);\\ \end{array}$	// o // d // s // s // s	pcode estinati ource s ource t ddress	on d

TOY emulator: execute instruction

Execute. Use Java switch statement to implement state change for each of 16 instructions.

if (op == 0)	break; // halt	
switch (op)	{	
case 1:	R[d] = R[s] + R[t];	k
case 2:	R[d] = R[s] - R[t];	k
case 3:	R[d] = R[s] & R[t];	k
case 4:	$R[d] = R[s] \wedge R[t];$	k
case 5:	$R[d] = R[s] \ll R[t];$	k
case 6:	R[d] = R[s] >> R[t];	k
case 7:	R[d] = addr;	k
case 8:	R[d] = M[addr];	k
case 9:	M[addr] = R[d];	k
case 10:	R[d] = M[R[t]];	k
case 11:	M[R[t]] = R[d];	k
case 12:	if $(R[d] == 0)$ pc = addr;	k
case 13:	if $(R[d] > 0)$ pc = addr;	k
case 14:	pc = R[d];	k
case 15:	R[d] = pc; pc = addr;	k
}		

- break;
- break;
- break; break;
- break;
- break;
- break;
- break;
 break;
- break;
- break;
- break;
 break;
- break;
- break;

A few missing details.

- R[0] is always 0000.
- TOY standard input/output.
- 16-bit TOY word vs. 32-bit Java int.
- More flexible TOY program input format.

Full implementation. See booksite.

Implications.

- Can run any TOY program!
- Can develop TOY code on another machine.
- Easy to change TOY design.

```
public class TOYLite {
   public static void main(String[] args) {
     int pc = 0x10;
                               // program counter
                                                                    state of machine
     int[] R = new int[16];
                               // registers
     int[] M = new int[256];
                              // main memory
     In in = new In(args[0]);
     for (int i = pc; !in.isEmpty(); i++)
        M[i] = Integer.parseInt(in.readString(), 16);
                                                                    parse input file
     while (true) {
        int ir = M[pc++];
                             // fetch
                                                                    fetch, increment
                             // increment
         pc++;
         int op = (ir >> 12) \& 0xF;
                                        // opcode
                 = (ir >> 8) & 0xF;
                                        // destination d
         int d
                                                                      decode
                = (ir >> 4) & 0xF;
                                        // source s
         int s
               = (ir >> 0) & 0xF;
                                                                    instruction
                                        // source t
         int t
        int addr = (ir >> 0) \& 0xFF;
                                        // address
        if (op == 0) break;
         switch (op)
            case 1: R[d] = R[s] +
                                    R[t];
                                                break;
            case 2: R[d] = R[s] -
                                                break;
                                    R[t];
            case 3: R[d] = R[s] \& R[t];
                                                break;
            case 4: R[d] = R[s] \wedge R[t];
                                                break;
            case 5: R[d] = R[s] \ll R[t];
                                                break;
                                                                      execute
            case 6: R[d] = R[s] >> R[t];
                                                break;
                                                                    instruction
            case 7: R[d] = addr;
                                                break;
            case 8: R[d] = M[addr];
                                                break;
            case 9: M[addr] = R[d];
                                                break;
            case 10: R[d] = M[R[t]];
                                                break;
            case 11: M[R[t]] = R[d];
                                                break;
            case 12: if (R[d] == 0) pc = addr;
                                                break;
            case 13: if (R[d] > 0) pc = addr;
                                                break;
            case 14: pc = R[d];
                                                break;
            case 15: R[d] = pc; pc = addr;
                                                break;
```







Visual X-TOY

Visual X–TOY. A Java IDE that emulates the TOY machine.

- GUI, text editor, auto-comments, debugger, many other features.
- Written by Brian Tsang '04 (using Java 1.3). *and still works* 20+ years later!
- Available on the booksite.

Same approach used for all new systems.

- Build simulator and development environment.
- Develop and test software.
- Build and sell hardware.

Edit Mode	Workspace Too	ils	20			Crazy 8 - Visu	al X-TOY		
								Memory Stdin St	dout Stdin' Stdout
Load	Look	Step	Run	Enter	Stop		Reset	00: 0000	10: 7101
					IWAIT	0	READY	01: 0000	11: 7A00
PC				STDOL	JT			02: 0000	12: 7B00
o o (Addr	٥ ()	00	00					03: 0000	13: 8CFF
								04: 0000	14: CC19
88	88	88	88					05: 0000	15: 16AB
								06: 0000	16: BC06
		00	0	00	00		000	07: 0000	17: 1BB1
DATA								08: 0000	18: C013
						0		09: 0000	19: CB20
ð ð	Ö Ö	ð ð	õ õ	ŏ ŏ	õ õ	Ő	5 5 5	0A: 0000	1A: 16AB
				~				OB: 0000	1B: 2661
R[0]	R[1] 0000	R[2] 0000	R[3] 0000	R[4] 0000	R[5] 0000	R[6] 0000	R[7] 0000	0C: 0000	1C: AC06
	DIQ1	D []]		RICI	PIDI	DIEI	DIEJ	0D: 0000	1D: 9CFF
0000	0000	0000	0000	0000	0000	0000	0000	0E: 0000	1E: 2BB1
PC/INSTR 10: 7101 R[1] <- 0	: 0001			ADDR/DATA 00: 0000 halt	A:			OF: 0000	1F: C019



Backward compatibility

Q. How to run old software on a new machine architecture?

Approach 1. Rewrite it all: time-consuming, expensive, error-prone.Approach 2. Write an emulator for old computer on the new one.

- Ex 1. Pac-Man.
- Ex 2. Rosetta 2. ← run 64-bit Intel on Apple Silicon



64-bit Intel

Apple Silicon

Impact. Old software remains available.





Pac-Man 1980s (arcade machine)

Pac-Man 2020s (Android phone)



Virtual machines

Virtual machine. Software-based emulation of a physical computer.

- Can run/develop software without having physical computer.
- Provides portability, scalability, flexibility, and security.

TOY virtual machine. Java program that can execute any TOY .toy file.

Java virtual machine (JVM). Abstract machine that can execute any Java .class file.

Mobile app IDEs. Provide emulator for Android, iPhone, Apple watch, ...

Cloud computing. Virtual CPU, memory, storage, OS, and network.





"write once, run anywhere"





Microsoft Azure



Computer systems are built by accumulating layers of abstraction.

Ex. Running a TOY program.



TOY program TOY emulator Java

Java virtual machine

Machine language

Processor

Digital computers. Encode "everything" in binary, including programs and data.

von Neumann machine. Store programs and data in same memory.

Indirection. Manipulate a value through its memory address.

Emulation. Make one system imitate another.



Credits

image

Microprocessor and Binary

David Wheeler

<u>C</u>(

Simply Explained Indirection

Pointers

J. Presper Eckert

John Mauchly

Programming ENIAC

Vacuum Tube

John von Neumann

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Credits

image

Apollo 11

Integrated Circuit

Margaret Hamilton

Light Bulb

EDSAC

Old Personal Computer

Sprint Phone

Google Data Center

Pac-Man Arcade Machine

Pac-Man on Android

Rosetta Stone

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