This exam has 10 questions worth a total of 50 points. You have 70 minutes.

Instructions. This exam is preprocessed by computer. Write neatly, legibly, and darkly. Put all answers (and nothing else) inside the designated spaces. *Fill in* bubbles and checkboxes completely: \bullet and \blacksquare . To change an answer, erase it completely and redo.

Resources. The exam is closed book, except that you are allowed to use a one page reference sheet (8.5-by-11 paper, both sides, in your own handwriting). No electronic devices are permitted.

Honor Code. This exam is governed by Princeton's Honor Code. Discussing the contents of this exam before solutions have been posted is a violation of the Honor Code.

Please complete the following information now.

Name:									
NetID:									
Exam room:	O M	IcCosh 1	0) McCo	$\sinh 50$	O N	IcCosh (62	Other
Precept:	P01	P02	P03	P04	\bigcirc^{P05}	P06	P07	P08	P08A
	P10	P11	P12	P12A	P13	P14	P15		

"I pledge my honor that I will not violate the Honor Code during this examination."

1. Initialization. (1 point)

On the front of this exam, in the designated spaces, write your name and NetID (not email alias); mark the room in which you are taking the exam and your precept number; and write and sign the Honor Code pledge.

2. Java OOP properties. (7 points)

Which of the following are properties of object-oriented programming in Java?

Mark each statement as either true or false by filling in the appropriate bubble.

true	false	
	\bigcirc	Java has two kinds of types— <i>primitive types</i> and <i>reference types</i> .
\bigcirc	\bigcirc	Every reference variable has a type (such as String or Perceptron) that is known at compile time.
\bigcirc	\bigcirc	Every class has <i>exactly one</i> constructor.
\bigcirc	\bigcirc	Programmers typically declare instance variables to be public in order to make the data type easier to test, debug, and maintain.
\bigcirc	\bigcirc	If you do not explicitly initialize an instance variable, it is initialized automatically to a default value (such as 0, 0.0, or null).
\bigcirc	\bigcirc	If a and b refer to two String objects, then a == b checks whether they correspond to the same sequence of characters.
\bigcirc	\bigcirc	The String data type is <i>immutable</i> : it is not possible to change the value of a String object by calling one of its public instance methods.
\bigcirc	\bigcirc	If x is a reference variable, then, when evaluating the expression $"x = " + x$, Java automatically calls the toString() method for x, then concatenates the two strings.

3. Recursive graphics. (4 points)

Design a recursive function with the signature

public static void draw(int n, double x, double y, double length) so that the call draw(4, 0.5, 0.5, 0.5) produces the following drawing:



These are the six statements in the function body, but not necessarily in the order given:

```
if (n == 0) return;
1.
2.
    drawShadedSquare(x, y, length);
3.
    draw(n-1, x - \text{length}/2, y + \text{length}/2, length/2);
                                                          // upper left
    draw(n-1, x + length/2, y + length/2, length/2);
4.
                                                          // upper right
5.
    draw(n-1, x - length/2, y - length/2, length/2);
                                                          // lower left
    draw(n-1, x + length/2, y - length/2, length/2);
6.
                                                          // lower right
```

The helper function drawShadedSquare() draws a gray square of the specified side length, outlined in black, and centered at (x, y).

Which of the following must be true for *any* possible ordering of the six statements that produces the drawing above?

Mark all that apply.

true	false	
\bigcirc	\bigcirc	Statement 1 must appear <i>first</i> .
\bigcirc	\bigcirc	Statement 2 must appear <i>last</i> .
\bigcirc	\bigcirc	Statement 3 must appear <i>before</i> statement 4.
\bigcirc	\bigcirc	Both statements 5 and 6 must appear <i>before</i> statement 2.

4. Data-type design and debugging. (6 points)

Recall the Vector data type from lecture, precept, and the textbook. Consider the following partial implementation and client:

```
public class Vector {
    private double[] coords; // coords[i] = ith coordinate of vector
                              // length of vector
    private int n;
    // constructs a new vector using given coordinates
    public Vector(double[] coordinates) {
        // SEE IMPLEMENTATIONS ON FACING PAGE
    }
    // returns the dot product of the two vectors
    public double dot(Vector that) {
        double sum = 0.0;
        for (int i = 0; i < n; i++) {</pre>
            sum += this.coords[i] * that.coords[i];
        }
        return sum;
    }
    // a test client
    public static void main(String[] args) {
        double[] x = { 3.0, 2.0, 1.0 };
        Vector a = new Vector(x);
        x[0] = 1.0;
        Vector b = new Vector(x);
        x[0] = 2.0;
        System.out.println(a.dot(b));
    }
}
```

Suppose that you run the main() on the facing page with each of the constructor implementations on the left. What will be printed to standard output?

For each implementation on the left, write the letter of the best-matching description on the right. You may use each letter once, more than once, or not at all.

<pre>public Vector(double[] coordinates) { n = coordinates.length;</pre>	A. 0.0
<pre>coords = coordinates; }</pre>	B. 1.0
	C. 2.0
<pre>public Vector(double[] coordinates) { this.n = coordinates.length; this.coords = new double[n];</pre>	D. 6.0
<pre>for (int i = 0; i < n; i++) coords[i] = coordinates[i]; }</pre>	E. 8.0
	F. 9.0
<pre>public Vector(double[] coordinates) { int n = coordinates.length;</pre>	G. 13.0
<pre>double[] coords = new double[n]; for (int i = 0; i < n; i++) coords[i] = coordinates[i];</pre>	H. 14.0
}	I. run-time exception

5. TOY. (6 points)

For each description on the left, write the letter of the best-matching power of 2 on the right. You may use each letter once, more than once, or not at all.

Number of 1	s in the binary representation of the decimal integer 27.	А.	2^{0}	(1)
		В.	2^1	(2)
Number of 1 Assume 16-	Is in the binary representation of -1 . bit two's complement integer.	C.	2^2	(4)
		D.	2^3	(8)
Number of a	distinct integers representable by a TOY register.	E.	2^4	(16)
		F.	2^{5}	(32)
Number of $\dot{\ell}$	bytes of main memory in TOY (including FF).	G.	2^{6}	(64)
		H.	2^{7}	(128)
Value in R[3	3] after executing the TOY code, starting from 10:	I.	2^8	(256)
11: 720D 12: 1312		J.	2^{9}	(512)
13: 0000		K.	2^{10}	(1,024)
Number of t following T(imes the instruction 92FF is executed when running the DY code, starting from 10:	L.	2^{11}	(2,048)
10: 7101 11: 720F	R[1] <- 0001 B[2] <- 000F	м.	2^{12}	(4,096)
12: 92FF 13: 6221	<pre>R[2] < 0001 print R[2] R[2] <- R[2] >> 1 </pre>	N.	2^{13}	(8,192)
14: D212 15: 0000	if $(R[2] > 0)$ goto 12 halt	0.	2^{14}	(16,384)
		Р.	2^{15}	(32,768)
		Q.	2^{16}	(65, 536)

TOY REFERENCE CARD

INSTRUCTION FORMATS

```
      | . . . . | . . . . | . . . . |

      Format RR:
      | opcode
      | d
      | s
      | t
      | (1-6, A-B)

      Format A:
      | opcode
      | d
      | addr
      | (7-9, C-F)
```

ARITHMETIC and LOGICAL operations

1:	add	R[d]	<- R[s]	+	R[t]
2:	subtract	R[d]	<- R[s]	-	R[t]
3:	and	R[d]	<- R[s]	&	R[t]
4:	xor	R[d]	<- R[s]	^	R[t]
5:	shift left	R[d]	<- R[s]	<<	R[t]
6:	shift right	R[d]	<- R[s]	>>	R[t]

TRANSFER between registers and memory

7:	load address	R[d] <- addr
8:	load	R[d] <- M[addr]
9:	store	M[addr] <- R[d]
A:	load indirect	R[d] <- M[R[t]]
B:	store indirect	M[R[t]] <- R[d]

CONTROL

0:	halt	halt
C:	branch zero	if $(R[d] == 0) PC <- addr$
D:	branch positive	if $(R[d] > 0) PC <- addr$
E:	jump register	PC <- R[d]
F:	jump and link	R[d] <- PC; PC <- addr

Register O always reads O. Loads from M[FF] come from stdin. Stores to M[FF] go to stdout.

```
16-bit registers (using two's complement arithmetic)
16-bit memory locations
8-bit program counter
```

6. Linked lists. (4 points)

Suppose that the Node data type is defined as

```
private class Node {
    private int item;
    private Node next;
}
```

and that first is a variable of type Node that refers to the first node in a *circular* linked list. Assume the circular linked list contains at least two nodes.

For each code fragment on the left, write the letter of the best-matching description on the right. You may use each letter once, more than once, or not at all.

```
A. prints all items once
for (Node x = first; x != first; x = x.next)
   StdOut.println(x.item);
                                                       B. prints all items once
                                                           except the first one
for (Node x = first; x != null; x = x.next)
                                                       C. prints all items once
   StdOut.println(x.item);
                                                           except the last one
                                                       D. prints only the first item
Node x = first;
while (x.next != first) {
   StdOut.println(x.item);
                                                       E. prints only the last item
   x = x.next;
}
                                                        F. prints nothing
                                                       G. infinite printing loop
Node x = first;
do {
   StdOut.println(x.item);
   x = x.next;
} while (x != first);
```

7. Algorithms, data structures, and performance. (5 points)

Suppose that the following code fragment is used to initialize array, stack, queue, and bst:

```
int[] array = { 2, 1, 1, 3, 1, 2, 1, 1, 1 };
int n = array.length;
Stack<Integer> stack = new Stack<Integer>();
Queue<Integer> queue = new Queue<Integer>();
ST<Integer, Integer> st = new ST<Integer, Integer>();
for (int i = 0; i < n; i++) {
    stack.push(array[i]);
    queue.enqueue(array[i]);
    st.put(array[i], i);
}
```

What is the order of growth of the running time of the above for loop in the worst case as a function of the array length n? Recall that ST is implemented using a balanced BST.



For each code fragment on the left, write the letter of the best-matching output on the right. You may use each letter once, more than once, or not at all.

	<pre>while (!stack.isEmpty())</pre>	A. 0 1 2 3 4 5 6 7 8
	<pre>StdUut.print(stack.pop() + " ");</pre>	B. 1 1 1 1 1 1 2 2 3
	<pre>while (!queue.isEmpty())</pre>	C. 1 1 1 2 1 3 1 1 2
	<pre>StdOut.print(queue.dequeue() + " ");</pre>	D. 2 1 1 3 1 2 1 1 1
	for $(int kov \cdot st kovs())$	E. 5 8 8 3 8 5 8 8 8
10	StdOut.print(key + " ");	F. 1 2 3
		G. 1 2 6
	<pre>for (int i = 0; i < n; i++) StdOut.print(st.get(array[i]) + " ");</pre>	H. 6 2 1
		I. 8 5 3

8. Regular expressions and DFAs. (5 points)

Consider the following regular expressions and DFAs over the binary alphabet $\{A, B\}$.

For each regular expression or DFA on the left, write the letter of the best-matching language (set of strings) on the right. You may use each letter once, more than once, or not at all.



9. Intractability and computability. (6 points)

Suppose that PROBLEMX is a search problem (i.e., in **NP**).

Mark each statement as either true, false, or unknown by filling in the appropriate bubble.

true	false	unkna	own
	\bigcirc	\bigcirc	FACTOR poly-time reduces to SAT.
\bigcirc	\bigcirc	\bigcirc	FACTOR can be solved in exponential time.
\bigcirc	\bigcirc	\bigcirc	SAT can be solved in poly-time but TSP cannot.
\bigcirc	\bigcirc	\bigcirc	Every problem in NP poly-time reduces to SAT.
\bigcirc	\bigcirc	\bigcirc	The halting problem can be solved in exponential time with a Java program on a Macbook Pro running OS X.
\bigcirc	\bigcirc	\bigcirc	If a search problem can be solved in poly-time on a TOY machine, then it can be solved in poly-time on a Turing machine.
\bigcirc	\bigcirc	\bigcirc	$\mathbf{P} \neq \mathbf{NP}.$

10. Boolean logic and circuits. (6 points)

The 3-bit *minority* function f(x, y, z) is a boolean function that is 1 if at most one of its three inputs is 1, and 0 otherwise. Which of the following represent the minority function?

Mark all that apply.

