

### 2.2 Libraries and Clients

- random number library
- designing libraries
- sound synthesis
- synthesizer library


## Basic building blocks for programming




### 2.2 Libraries and Clients

- random number library
- designíng librariés
- sound synthesis
- synthesizer library
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```
int getRandomNumber()
    return 4; // chosen by fair dice roll.
        // guaranteed to be random
```

Standard random library

Goal. Design a library to generate pseudo-random numbers.

| public class StdRandom |  |
| :--- | :--- |
| static double uniformDouble() | real number between 0 and 1 |
| static double uniformDouble(double 1o, double hi) | real number between lo and hi |
| static boolean bernoulli(double p) | true with probability p, fal se otherwise |
| static int $\quad$ uniformInt(int n) | integer between 0 and $\mathrm{n}-1$ |
| static double gaussian() | normal with mean 0 and stddev 1 |
| static double gaussian(double mu, double sigma) | normal with mean mu and stddev sigma |
| static void | shuffle(String[] a) |
| static int | discrete(int[] freq) |

## Standard random implementation: random numbers from various distributions



## Standard random implementation: random numbers from a Gaussian distribution


\}

## Standard random implementation: shuffling the elements in an array



## Calling a library function

Calling from a client. Specify library name, dot operator, function name, and arguments.


Note. Must use fully qualified name if calling a function from another file.

## Standard random clients

## StdRandom client 1

```
public class Shuffle {
    public static void main(String[] args) {
        StdRandom.shuffle(args);
        for (int i = 0; i < args.length; i++) {
            StdOut.print(args[i] + " ");
        }
        StdOut.println();
    }
}
```

~/cos126/libraries> java-introcs Shuffle A B C D E
E A D B C
~/cos126/libraries> java-introcs Shuffle A B C D E
C A E B D
~/cos126/libraries> java-introcs Shuff1e 2C 2D 2H ... AS
4S 2D AC 9H QH 8C ... JS 4H 2S

```

\section*{StdRandom client 2}
```

public class RandomPoints {
public static void main(String[] args) {
int n = Integer.parseInt(args[0]);
for (int i = 0; i < n; i++) {
double x = StdRandom.gaussian(0.5, 0.1);
double y = StdRandom.gaussian(0.5, 0.1);
StdDraw.point(x, y);
}
}
}

```
~/cos126/7ibraries> java-introcs RandomPoints 100000


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\section*{Libraries}

Def. A module is a set of functions stored in a single file.
Def. A library is a module whose primary purpose is for use by other programs.
\begin{tabular}{|c|c|c|c|c|}
\hline library & description & example method call & source & logo \\
\hline StdRandom & generate random numbers & StdRandom.uniformInt(6) & \multirow{2}{*}{textbook} & \multirow[t]{2}{*}{} \\
\hline StdDraw & draw geometric shapes & StdDraw.circle(0.5, 0.5, 0.25) & & \\
\hline Math & compute mathematical functions & Math.sqrt(2.0) & \multirow{2}{*}{Java system} & \multirow[t]{2}{*}{\[
\stackrel{(5}{5}
\]} \\
\hline java.util.Arrays & manipulate arrays & Arrays.sort(a) & & \\
\hline Gaussian & compute Gaussian pdf and cdf & Gaussian.pdf(3.0) & \multirow{3}{*}{user-defined} & \multirow[t]{3}{*}{\[
\langle 1\rangle
\]} \\
\hline & & & & \\
\hline SayNumber & speak numbers & SayNumber.sayInteger (126) & & \\
\hline
\end{tabular}

\section*{API, client, and implementation}

Application programming interface (API). Specifies method headers and behavior for a library. Implementation. Program that implements the methods in an API.
Client. Program that uses a library through its API.

\section*{client}


\section*{implementation}


\section*{API, client, and implementation}

Application programming interface (API). Specifies method headers and behavior for a library. Implementation. Program that implements the methods in an API.
Client. Program that uses a library through its API.


API

implementation


\section*{Encapsulation}

Encapsulation. Separating clients from implementation details by hiding information.

Principle. A client does not need to know how a method is implemented in order to use it.

Benefits.
- Can develop client code and implementation code independently.
- Can change implementation details without breaking clients.

Private access modifier. Designates a method as not for use by a client.
- API does not list private methods.
- Compile-time error for client to call a private method.
- Advantage: implementation can add/remove private methods without impacting clients.

\section*{Accessing a library}

Java classpath. Places where Java looks for user-defined libraries (and other resources).
- Simplest: put library .class file in same directory as client program.
- Best practice: bundle library .class files in a .jar file; add .jar file to Java classpath.
std7ib.jar contains:
StdRandom.class
StdIn.class
StdOut.class
StdDraw.class
StdPicture.class
StdAudio.class
```

~/cos126/libraries> javac Shuff1e.java
Shuffle.java:3: error: cannot find symbol
StdRandom.shuffle(args);
adds stdlib.jar
to Java classpath
~/cos126/1 ibraries> javac-introcs Shuffle,java
~/cos126/7ibraries> java-introcs Shuffle A B C D E
C A E B D

```

\section*{Unit testing}

Best practice. Include a main() method in each class as a test client.
- Call each public method at least once.
- Use result to check behavior.
\(\qquad\) minimum requirements
(in this course)
- Identify failed tests programmatically.
```

public class StdRandom {
public static void main(String[] args) {
int n = Integer.parseInt(args[0]);
for (int i = 0; i < n; i++) {
StdOut.printf("%8.5f ", uniformDouble(10.0, 99.0));
StdOut.printf("%5b " , bernoulli(0.5));
StdOut.printf("%2d " , uniformInt(100));
StdOut.printf("%7.5f ", gaussian(9.0, 0.2));
StdOut.print7n();
}

```
\(\qquad\) unit tests for shuffle() and other methods
    \}
\}


\section*{Method header comments}

Best practice. Every method should include a comment before the method header.
- Describe it purpose. \(\qquad\) minimum requirements
- Use names of parameter variables in description. (in this course)
- Identify parameters, return value, and exceptions using Javadoc tags.
```

/**
* Returns a random integer uniform7y in [0, n).
* @param n number of possible integers
* @return a random integer uniform7y between 0 (inc7usive) and n (exc7usive)
public static int uniformInt(int n) {
return (int) (Math.random() * n);
}

```

Javadoc

\section*{Javadoc. Automatically generates API and documentation from Javadoc comments.}

\section*{Class StdRandom}

Object
StdRandom
public final class StdRandom
extends Object
Overview. The StdRandom class provides static methods for generating random number from various discrete and continuous distributions, including uniform, Bernoulli, geometric, Gaussian, exponential, Pareto, Poisson, and Cauchy. It also provides method for shuffling an array or subarray and generating random permutations.

Conventions. By convention, all intervals are half open. For example, uniformDouble ( \(-1.0,1.0\) ) returns a random number between -1.0 (inclusive) and 1.0 (exclusive). Similarly, shuffle (a, lo, hi) shuffles the hi - lo elements in the array a[], starting at index lo (inclusive) and ending at index hi (exclusive).

Performance. The methods all take constant expected time, except those that involve arrays. The shuffle method takes time linear in the subarray to be shuffled; the discrete methods take time linear in the length of the argument array.

Additional information. For additional documentation, see Section 2.2 of Computer Science: An Interdisciplinary Approach by Robert Sedgewick and Kevin Wayne.

\section*{Author:}

Robert Sedgewick, Kevin Wayne

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\section*{Review: digital audio}

Sound is the perception the vibration of our eardrums.

Audio signal. Real-valued (between -1 and +1 ) function of time.

Pure tone. Sound wave defined by the sine function of given frequency, amplitude and duration.
\[
y(t)=\sin (2 \pi \cdot 2048 \cdot t) \quad 0 \leq t \leq T
\]

\section*{Review: audio sampling}

Goal. Convert a continuous-time signal into a discrete-time signal.
- A sample is a signal value at specific point in time.
- Take samples at evenly spaced points.
real numbers between -1 and +1 (using 44,100 samples per second)

\section*{amplitude}
\(\mathrm{a}(\mathrm{t})\)

\[
\begin{aligned}
& y(t)=\sin (2 \pi \cdot 2048 \cdot t), \quad 0 \leq t \leq T \\
& a(t)=\sin (2 \pi \cdot 2048 \cdot t), \quad t=\frac{0}{44100}, \frac{1}{44100}, \frac{2}{44100}, \ldots
\end{aligned}
\]

\section*{Review: standard audio API}

StdAudio. Our library for playing, reading, and saving digital audio.
public class StdAudio
\begin{tabular}{lll}
\hline static int & SAMPLE_RATE & 44,100 (CD quality audio) \\
static void & play (String filename) & play the audio file \\
static void & playInBackground (String filename) & play the audio file in the background \\
static void & play (double sample) & play the sample \\
static void & play (double[] samples) & play the samples \\
static double[] read(String filename) & read the samples from an audio file \\
static void & save(String filename, double[] samples) & save the samples to an audio file
\end{tabular}
```

public class Synth {
implementation
public static int numberOfSamples(double duration) {
return (int) (StdAudio.SAMPLE_RATE * duration);
}
private static double sine(doub7e freq, double t) {
return Math.sin(2 * Math.PI * freq * t);
}
public static double[] sineWave(double freq, double amplitude, double duration) {
int n = numberOfSamples(duration);
doub7e[] a = new double[n];
for (int i = 0; i < n; i++) {
doub1e t = 1.0 * i / StdAudio.SAMPLE_RATE;
a[i] = amplitude * sine(freq, t);
}
return a;
}
double[] a = Synth.sineWave(2048.0, 0.5, 3.0);
StdAudio.play(a);
\}

$$
a(t)=A \sin (2 \pi \cdot f \cdot t), \quad t=\frac{0}{44100}, \frac{1}{44100}, \frac{2}{44100}, \ldots
$$

```

Libraries and clients: quiz 1

\section*{What sound will the following code fragment produce?}
```

doub7e freq = 17400.0;
double amplitude = 0.5
double duration = 10.0;
double[] a = Synth.sineWave(freq, amplitude, duration);
StdAudio.play(a);

```
A. Extremely high-pitched sound.
B. Inaudible.
C. Ultrasonic weapon.
D. All of the above.
- Concert A is 440 Hz .
- An octave is the interval between a note and one with twice its frequency.
- Octave is divided into 12 notes on a logarithmic scale. \(\qquad\) "twelve-tone equal temperament"

\[
\begin{array}{llllllll}
\mathrm{A}_{4} & \mathrm{~B} & \mathrm{C} & \mathrm{D} & \mathrm{E} & \mathrm{~F} & \mathrm{G} & \mathrm{~A}_{5}
\end{array}
\]


Libraries and clients: quiz 2

Which of the following converts from MIDI note number to frequency?
A.
```

private static double midiToFrequency(int midi) {
return 440 * Math.pow(2, (midi - 69) / 12);
}

```
\[
\text { frequency }=440 \times 2^{(m i d i-69)} / 12
\]
B.
```

private static double midiToFrequency(int midi) {
return 440.0 * 2.0 ^ ((midi - 69.0) / 12.0);
}

```
C. Both A and B.
D. Neither A nor B.

Goal. Add methods (and constants) to library that many clients might want to use.

Musical Instrument Digital Interface (MIDI). Digital music standard.

Class constant.
- Declare and initialize "variable" outside of any method, using fina 7 and static modifiers.
- Access modifier can be public or private.
- Java naming convention: use SCREAMING_SNAKE_CASE.
```

public class Synth {
public static final double CONCERT_A = 440.0; \longleftarrow
private static doub7e midiToFrequency(int midi) {
return CONCERT_A * Math.pow(2, (midi - 69) / 12.0);
}
} frequency = 440 < 2 (midi-69)/12
implementation

```

\section*{Musical scales}

Major scale. Sequence of 8 notes in a specific interval pattern, starting with a root note and ending with the same note one octave higher.

Ex 1. C major scale.


Ex 2. A major scale.


Major scale. Sequence of 8 notes in a specific interval pattern, starting with a root note and ending with the same note one octave higher.
```

public class MajorScale {
public static void main(String[] args) {
int root = Integer.parseInt(args[0]);
doub7e duration = 0.5;
doub7e amplitude = 0.5;
int[] pattern = { 0, 2, 4, 5, 7, 9, 11, 12 };
for (int i = 0; i < pattern.length; i++) {
int midi = root + pattern[i];
double freq = Synth.midiToFrequency(midi);
double[] a = Synth.sineWave(freq, amplitude, duration);
StdAudio.play(a);
}
}
}

```
```

~/cos126/7ibraries> java-introcs MajorScale 60

```
~/cos126/7ibraries> java-introcs MajorScale 60
4)) [plays A major scale]
4)) [plays A major scale]
~/cos126/libraries> java-introcs MajorScale 69
~/cos126/libraries> java-introcs MajorScale 69
4)) [plays C major scale]
```

4)) [plays C major scale]

```

\section*{Play that tune}

Goal. Read in a sequence of MIDI note numbers and durations from standard input, and play the synthesized results to standard audio.
```

~/cos126/libraries> more MajorScaleC.txt
60 0.5
6 2 0 . 5 ~ \longleftarrow . ~ d u r a t i o n ~ ( s e c o n d s )
64 0.5
655
MMDI note number
~/cos126/libraries> java-introcs PlayThatTune < MajorScaleC.txt
4)) [plays C major scale]

```

\section*{Play that tune}

Goal. Read in a sequence of MIDI note numbers and durations from standard input, and play the synthesized results to standard audio.
```

                    client
    public class PlayThatTune {
public static void main(String[] args) {
doub7e amplitude = 0.5;
while (!StdIn.isEmpty()) {
int midi = StdIn.readInt();
double duration = StdIn.readDoub7e();
double freq = Synth.midiToFrequency(midi);
doub7e[] a = Synth.sineWave(freq, amplitude, duration);
StdAudio.play(a);
}
}
}

```
```

~/cos126/7ibraries> java-introcs PlayThatTune < Arpeggio.txt

```
~/cos126/7ibraries> java-introcs PlayThatTune < Arpeggio.txt
-\)) [plays arpeggio]
~/cos126/7ibraries> java-introcs PlayThatTune < LooneyTunes.txt
4)) [plays Looney Tunes theme]
~/cos126/libraries> java-introcs PlayThatTune < FurElise.txt
G)) [plays beginning of Fur Elise]
```


### 2.2 Libraries and Clients

- random number tibrary
$\checkmark$ designing librariés
- sound synthesis
- synthesizer library

[^0]Digital synth. Electronic musical instrument that generates audio signals digitally.

- Sound effects.
- Film and television soundtracks.
- Diverse genres of music (rock, jazz, pop, disco, hip-hop, electronic music, ...).
- ...



R2-D2
(Star Wars)


Axel F (Harold Faltemeyer)

## Synthesizer API

## Synth. A library for synthesizing sound.

| public class Synth |
| :--- |
| static int |
| CONCERT_A |


| static double | sineWave(double freq, double amplitude, double duration) | sine wave |  |
| :--- | ---: | :--- | :--- | :--- |
| static double | squareWave(double freq, double amplitude, double duration) | square wave |  |
| static double | sawWave(double freq, double amplitude, double duration) | saw wave |  |
| static double | supersawWave(double freq, double amplitude, double duration) | supersaw wave |  |
| static double | whiteNoise( | double amplitude, double duration) | white noise |


| static double[] superpose(double[] a, double[] b) | add the two waves |  |
| :--- | ---: | :--- |
| static double[] | modulate(double[] a, double[] b) | multiply the two waves |
| static double[] | fadeIn(double[] a, double lambda) | exponential fade in |
| static double[] | fadeOut (double[] a, double lambda) | exponential fade out waves |

Square wave. Alternates between +1 and -1 with frequency $f$, half the time at each value.


$$
a(t)=\operatorname{sgn}(\sin (2 \pi \cdot 440 \cdot t)), \quad 0 \leq t \leq T \quad \operatorname{sgn}(x)=\left\{\begin{aligned}
-1 & \text { if } x<0 \\
0 & \text { if } x=0 \\
+1 & \text { if } x>0
\end{aligned}\right.
$$

private static doub7e square(double freq, double t) {
private static doub7e square(double freq, double t) {
return Math.signum(sine(freq, t));
return Math.signum(sine(freq, t));
}
}
public static doub7e[] squareWave(doub7e freq, doub7e amplitude, doub7e duration) {
public static doub7e[] squareWave(doub7e freq, doub7e amplitude, doub7e duration) {
/* similar to sineWave() */
/* similar to sineWave() */
}
}

Sawtooth wave. Rises from -1 to +1 linearly, then drops back to -1 , and repeats with frequency $f$.


```
private static double saw(double freq, doub7e t) {
implementation
    return 2 % (freq*t - Math.floor(freq*t + 0.5));
}
public static doub7e[] sawWave(double freq, double amplitude, double duration) {
    /* similar to sineWave() %/
}
```


## Exponential fade

Sound envelope. Defines how a sound changes over time.
Exponential fade. A sound envelope whose amplitude decays according to exponential function.
sine wave ( 30 Hz )

sine wave ( 30 Hz ) with exponential fade ( $\lambda=10$ )


```
public class Synth {
implementation
    public static doub7e[] fadeOut(doub1e[] a, doub7e lambda) {
    int n = a.length;
    double[] result = new double[n];
    for (int i = 0; i < n; i++) {
        double t = 1.0 * i / StdAudio.SAMPLE_RATE;
        result[i] = a[i] * Math.pow(2.0, -1ambda* t);
        }
        return result;
    }
}
```


## client

```
doub7e[] a = Synth.sineWave(440.0, 0.5, 1.0);
doub7e[] b = Synth.fadeOut(a, 10.0);
StdAudio.play(b);
```

```
doub7e[] a = Synth.squareWave(55.0, 0.25, 1.0);
doub7e[] b = Synth.fadeOut(a, 5.0);
StdAudio.play(b);
```

Libraries and clients: quiz 3

What sound does StdAudio.p7ay(mystery(5.0)) produce?
A. 5 seconds of concert $A(440 \mathrm{~Hz})$.
B. 5 seconds of a random frequency.
C. 5 seconds of silence.
D. 5 seconds of static.

```
public static doub7e[] mystery(doub7e duration) {
    int n = numberOfSamples(duration);
    double[] a = new double[n];
    for (int i = 0; i < n; i++) {
        a[i] = StdRandom.uniformDoub7e(-0.5, 0.5);
    }
    return a;
}
```


## White noise. Samples are uniformly random values.


implementation

```
public static doub7e[] whiteNoise(double amplitude, double duration) {
    int n = numberOfSamples(duration);
    doub7e[] a = new doub7e[n];
    for (int i = 0; i < n; i++) {
            a[i] = StdRandom.uniformDouble(-amplitude, +amplitude);
    }
    return a;
}
```

Superposition. To combine two (or more) audio signals, add the corresponding samples.

## Ex 1. Harmonics.

```
doub7e duration = 5.0;
doub7e[] a4 = Synth.sineWave(440.0, 0.50, duration);
doub7e[] a3 = Synth.sineWave(220.0, 0.25, duration);
doub7e[] a5 = Synth.sineWave(880.0, 0.25, duration);
doub7e[] harmonics = Synth.superpose(a4, a3, a5);
StdAudio.play(harmonics);
```


concert A with harmonics
Mrn rnsurns

Superposition. To combine two (or more) audio signals, add the corresponding samples.

## Ex 1. Harmonics.

Ex 2. Chord.

```
doub7e duration = 5.0;
doub7e[] a = Synth.sineWave(440.00, 0.33, duration);
doub7e[] c = Synth.sineWave(554.37, 0.33, duration);
doub7e[] e = Synth.sineWave(659.26, 0.33, duration);
doub7e[] chord = Synth.superpose(a, c, e);
StdAudio.play(chord);
```

Superposition. To combine two (or more) audio signals, add the corresponding samples.

## Ex 1. Harmonics.

Ex 2. Chord.
Ex 3. Supersaw.

```
double freq = 220.0;
doub7e amplitude = 0.05;; "detuned" frequencies
double duration = 10.0;
doub7e[] a0 = Synth.sawWave(freq, \downarrow amplitude, duration);
doub7e[] a1 = Synth.sawWave(freq - 0.191, amplitude, duration);
doub7e[] a2 = Synth.sawWave(freq - 0.109, amplitude, duration);
doub7e[] a3 = Synth.sawWave(freq - 0.037, amplitude, duration);
doub7e[] a4 = Synth.sawWave(freq + 0.031, amplitude, duration);
doub7e[] a5 = Synth.sawWave(freq + 0.107, amplitude, duration);
doub7e[] a6 = Synth.sawWave(freq + 0.181, amplitude, duration);
doub7e[] supersaw = Synth.superpose(a0, a1, a2, a3, a4, a5, a6);
StdAudio.play(supersaw);
```

Goal. Play that tune, but with a supersaw.

```
client
public class SlayThatTune {
    public static void main(String[] args) {
        doub7e amplitude = 0.5;
                            transpose one
        while (!StdIn.isEmpty()) {
                                octave lower
                int midi = StdIn.readInt();
                double duration = StdIn.readDoub7e();
            double freq = Synth.midiToFrequency(midi - 12);
            double[] a = Synth.supersawWave(freq, amplitude, duration);
            StdAudio.play(a);
        }
    }
}
```



## Synth library

```
public class Synth {
    public static final double CONCERT_A = 440.0;
```


## implementation

```
    public static double midiToFrequency(int midi) { ... }
    private static double sine(double freq, double t) { ... }
    private static doub7e square(double freq, doub7e t) { ...} < «
    private static double saw(double freq, double t) { ... }
    public static doub7e[] sineWave(doub7e freq, double amplitude, double duration) { ... }
    public static double[] squareWave(doub7e freq, doub7e amplitude, double duration) {... }
    public static double[] sawWave(double freq, double amplitude, double duration) {... }
    public static doub7e[] supersawWave(double freq, double amplitude, double duration) { ... }
    public static double[] whiteNoise( double amplitude, double duration) { ... }
\begin{tabular}{|c|c|c|}
\hline pub7ic static double[] & superpose (doub7e[] a, double[] b) & \{ ... \} \\
\hline public static double[] & modulate(double[] a, doub7e[] b) & \{ ... \} \\
\hline public static double[] & fadeIn (double[] a, double lambda) & \{ ... \} \\
\hline pub7ic static double[] & fadeOut(double[] a, double 1ambda) & \{ ... \} \\
\hline
\end{tabular}
}
```


## Summary

API. Defines method headers and behavior for a library.
Client. Program that calls a library's methods.
Implementation. Program that implements the library's functionality.

Encapsulation. Separating clients from implementation details by hiding information.

## Benefits.

- Reusable libraries.
- Independent development of small programs.
- Collaboration with a team of programmers.

Sound synthesis. You can write programs to synthesize sound.


Credits

| media | source | license |
| :---: | :---: | :---: |
| Zhongshuge bookstore | Feng Shao / X+Living |  |
| Random Number | xkcd | CC BY-NC 2.5 |
| Coin Toss | Adobe Stock | education license |
| Ten-Sided Die | Adobe Stock | education license |
| Normal Distribution | Adobe Stock | education license |
| Shuffle Icon | Adobe Stock | education license |
| Client Avatars | Adobe Stock | education license |
| Cloud Coding Icon | Adobe Stock | education license |
| Contract Icon | Adobe Stock | education license |
| Implementation Icon | Adobe Stock | education license |
| Family 1 Watching TV | Adobe Stock | education license |
| Family 2 Watching TV | Adobe Stock | education license |
| Family 3 Watching TV | Adobe Stock | education license |

## Credits

| media | source | license |
| :---: | :---: | :---: |
| TV Remote Control | $\underline{\text { Adobe Stock }}$ | $\underline{\text { education license }}$ |
| Pink Vintage TV | $\underline{\text { Adobe Stock }}$ | $\underline{\text { education license }}$ |
| Bravia TV | $\underline{\text { Sony }}$ |  |
| Pharmacy Pills | $\underline{\text { Adobe Stock }}$ | $\underline{\text { education license }}$ |
| Private Sign on a Door | $\underline{\text { Adobe Stock }}$ | $\underline{\text { education license }}$ |
| Sound Waves and the Ear | $\underline{\text { Wikimedia }}$ | $\underline{\text { CC BY 4.0 }}$ |
| Piano Keys | $\underline{\text { Adobe Stock }}$ | $\underline{\text { education license }}$ |
| Yamaha DX7 | $\underline{\text { Wikimedia }}$ | public domain |
| R2-D2 Sound Effects | $\underline{\text { Star Wars }}$ |  |
| Axel F | $\underline{\text { Harold Faltemeyer }}$ |  |
| Piano Keys | $\underline{\text { Adobe Stock }}$ | $\underline{\text { education license }}$ |
| Human Hands with Puzzle | $\underline{\text { Adobe Stock }}$ | education license |


[^0]:    https://introcs.cs.princeton.edu

