



Number Systems and Number Representation

Q: Why do computer programmers
confuse Christmas and Halloween?

A: Because 25 Dec = 31 Oct



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Goals of this Lecture



Help you learn (or refresh your memory) about:

- The binary, hexadecimal, and octal number systems
- Finite representation of unsigned integers
- Finite representation of signed integers
- Finite representation of rational (floating-point) numbers

Why?

- A power programmer must know number systems and data representation to fully understand C's **primitive data types**

Primitive values and
the operations on them

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Agenda



Number Systems

Finite representation of unsigned integers

Finite representation of signed integers

Finite representation of rational (floating-point) numbers

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The Decimal Number System



Name

- "decem" (Latin) ⇒ ten

Characteristics

- Ten symbols
 - 0 1 2 3 4 5 6 7 8 9
- Positional
 - $2945 \neq 2495$
 - $2945 = (2 \cdot 10^3) + (9 \cdot 10^2) + (4 \cdot 10^1) + (5 \cdot 10^0)$

(Most) people use the decimal number system

Why?

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The Binary Number System



binary

adjective: being in a state of one of two mutually exclusive conditions such as on or off, true or false, molten or frozen, presence or absence of a signal.
From Late Latin *binārius* ("consisting of two").

Characteristics

- Two symbols: 0 1
- Positional: $1010_2 \neq 1100_2$

Most (digital) computers use the binary number system

Terminology

- **Bit**: a binary digit
- **Byte**: (typically) 8 bits
- **Nibble (or nybble)**: 4 bits

Why?

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Decimal-Binary Equivalence



Decimal	Binary
0	0
1	1
2	10
3	11
4	100
5	101
6	110
7	111
8	1000
9	1001
10	1010
11	1011
12	1100
13	1101
14	1110
15	1111

Decimal	Binary
16	10000
17	10001
18	10010
19	10011
20	10100
21	10101
22	10110
23	10111
24	11000
25	11001
26	11010
27	11011
28	11100
29	11101
30	11110
31	11111
...	...

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Decimal-Binary Conversion

Binary to decimal: expand using positional notation

$$\begin{aligned} 100101_{\text{B}} &= (1 \cdot 2^5) + (0 \cdot 2^4) + (0 \cdot 2^3) + (1 \cdot 2^2) + (0 \cdot 2^1) + (1 \cdot 2^0) \\ &= 32 + 0 + 0 + 4 + 0 + 1 \\ &= 37 \end{aligned}$$

Most-significant
bit (msb)

Least-significant
bit (lsb)

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~~Integer~~ Decimal-Binary Conversion

~~Integer~~ Binary to ~~decimal~~: expand using positional notation

$$\begin{aligned} 100101_{\text{B}} &= (1 \cdot 2^5) + (0 \cdot 2^4) + (0 \cdot 2^3) + (1 \cdot 2^2) + (0 \cdot 2^1) + (1 \cdot 2^0) \\ &= 32 + 0 + 0 + 4 + 0 + 1 \\ &= 37 \end{aligned}$$

These are integers
They exist as their pure selves
no matter how we might choose
to represent them with our
fingers or toes

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Integer-Binary Conversion

Integer to binary: do the reverse

- Determine largest power of 2 that's $\leq$ number; write template

$$37 = (? \cdot 2^5) + (? \cdot 2^4) + (? \cdot 2^3) + (? \cdot 2^2) + (? \cdot 2^1) + (? \cdot 2^0)$$

- Fill in template

$$\begin{array}{r} 37 = (1 \cdot 2^5) + (0 \cdot 2^4) + (0 \cdot 2^3) + (1 \cdot 2^2) + (0 \cdot 2^1) + (1 \cdot 2^0) \\ \hline -32 \\ 5 \\ \hline -4 \\ 1 \\ \hline -1 \\ 0 \end{array} \quad 100101_{\text{B}}$$

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Integer-Binary Conversion

Integer to binary shortcut

- Repeatedly divide by 2, consider remainder

$$\begin{array}{r} 37 / 2 = 18 \text{ R } 1 \\ 18 / 2 = 9 \text{ R } 0 \\ 9 / 2 = 4 \text{ R } 1 \\ 4 / 2 = 2 \text{ R } 0 \\ 2 / 2 = 1 \text{ R } 0 \\ 1 / 2 = 0 \text{ R } 1 \end{array}$$

Read from bottom
to top: 100101_B

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The Hexadecimal Number System

Name

- "hexa-" (Ancient Greek ἑξά-) $\Rightarrow$ six
- "decem" (Latin) $\Rightarrow$ ten

Characteristics

- Sixteen symbols
 - 0 1 2 3 4 5 6 7 8 9 A B C D E F
- Positional
 - A13D₁₆ $\neq$ 3DA1₁₆

Computer programmers often use hexadecimal or "hex"

- In C: 0x prefix (0xA13D, etc.)

Why?

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Decimal-Hexadecimal Equivalence

Decimal	Hex	Decimal	Hex	Decimal	Hex
0	0	16	10	32	20
1	1	17	11	33	21
2	2	18	12	34	22
3	3	19	13	35	23
4	4	20	14	36	24
5	5	21	15	37	25
6	6	22	16	38	26
7	7	23	17	39	27
8	8	24	18	40	28
9	9	25	19	41	29
10	A	26	1A	42	2A
11	B	27	1B	43	2B
12	C	28	1C	44	2C
13	D	29	1D	45	2D
14	E	30	1E	46	2E
15	F	31	1F	47	2F
				...	...

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Integer-Hexadecimal Conversion

Hexadecimal to integer: expand using positional notation

$$\begin{aligned} 25_H &= (2 \cdot 16^1) + (5 \cdot 16^0) \\ &= 32 + 5 \\ &= 37 \end{aligned}$$

Integer to hexadecimal: use the shortcut

$$\begin{array}{l} 37 / 16 = 2 \text{ R } 5 \\ 2 / 16 = 0 \text{ R } 2 \end{array} \quad \uparrow \quad \text{Read from bottom to top: } 25_H$$

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Binary-Hexadecimal Conversion

Observation: $16^1 = 2^4$

- Every 1 hexadecimal digit corresponds to 4 binary digits

Binary to hexadecimal

1010000100111101₂
A 1 3 D₁₆

Digit count in binary number
not a multiple of 4 $\Rightarrow$
pad with zeros on left

Hexadecimal to binary

A 1 3 D₁₆
1010000100111101₂

Discard leading zeros from
binary number if appropriate

Is it clear why programmers
often use hexadecimal?

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iClicker Question

Q: Convert binary 101010 into decimal and hex

- A. 21 decimal, 1A hex
- B. 42 decimal, 2A hex
- C. 48 decimal, 32 hex
- D. 55 decimal, 4G hex

Hint: convert to hex first

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The Octal Number System

Name

- "octo" (Latin) $\Rightarrow$ eight

Characteristics

- Eight symbols
 - 0 1 2 3 4 5 6 7
- Positional
 - $1743_8 \neq 7314_{10}$



Computer programmers often use octal (so does Mickey!)

- In C: 0 prefix (01743, etc.)

Why?

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Agenda

Number Systems

Finite representation of unsigned integers

Finite representation of signed integers

Finite representation of rational (floating-point) numbers

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Integral Types in Java vs. C

	Java	C
Unsigned types	char // 16 bits	unsigned char /* Note 2 */ unsigned short unsigned (int) unsigned long
Signed types	byte // 8 bits short // 16 bits int // 32 bits long // 64 bits	signed char /* Note 2 */ (signed) short (signed) int (signed) long

- Not guaranteed by C, but on `armlab`, `char` = 8 bits, `short` = 16 bits, `int` = 32 bits, `long` = 64 bits
- Not guaranteed by C, but on `armlab`, `char` is unsigned

To understand C, must consider representation of
both unsigned and signed integers

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Representing Unsigned Integers

Mathematics

- Range is 0 to ∞

Computer programming

- Range limited by computer's **word** size
- Word size is n bits $\Rightarrow$ range is 0 to $2^n - 1$
- Exceed range $\Rightarrow$ **overflow**

Typical computers today

- $n = 32$ or 64 , so range is 0 to $2^{32} - 1$ or $2^{64} - 1$ (huge!)

Pretend computer

- $n = 4$, so range is 0 to $2^4 - 1$ (15)

Hereafter, assume word size = 4

- All points generalize to word size = 64, word size = n

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Representing Unsigned Integers

On pretend computer

Unsigned Integer	Rep
0	0000
1	0001
2	0010
3	0011
4	0100
5	0101
6	0110
7	0111
8	1000
9	1001
10	1010
11	1011
12	1100
13	1101
14	1110
15	1111

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Adding Unsigned Integers

Addition

		1
3	0011 ₂	
+ 10	+ 1010 ₂	
--	----	
13	1101 ₂	

Start at right column
Proceed leftward
Carry 1 when necessary

		111
7	0111 ₂	
+ 10	+ 1010 ₂	
--	----	
1	0001 ₂	

Beware of overflow

Results are mod 2^4

How would you
detect overflow
programmatically?

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Subtracting Unsigned Integers

Subtraction

		111
10	1010 ₂	
- 7	- 0111 ₂	
--	----	
3	0011 ₂	

Start at right column
Proceed leftward
Borrow when necessary

		1
3	0011 ₂	
- 10	- 1010 ₂	
--	----	
9	1001 ₂	

Beware of overflow

Results are mod 2^4

How would you
detect overflow
programmatically?

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Shifting Unsigned Integers

Bitwise right shift ($\gg$ in C): fill on left with zeros

10 $\gg$ 1 $\Rightarrow$ 5
1010 ₂ 0101 ₂

10 $\gg$ 2 $\Rightarrow$ 2
1010 ₂ 0010 ₂

Bitwise left shift ($\ll$ in C): fill on right with zeros

5 $\ll$ 1 $\Rightarrow$ 10
0101 ₂ 1010 ₂

3 $\ll$ 2 $\Rightarrow$ 12
0011 ₂ 1100 ₂

Results are mod 2^4

What is the effect
arithmetically?

What is the effect
arithmetically?

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Other Operations on Unsigned Ints

Bitwise NOT ($\sim$ in C)

- Flip each bit

$\sim 10 \Rightarrow 5$
1010 ₂ 0101 ₂

$\sim 5 \Rightarrow 10$
0101 ₂ 1010 ₂

Bitwise AND ($\&$ in C)

- Logical AND corresponding bits

10	1010 ₂
& 7	& 0111 ₂
--	----
2	0010 ₂

10	1010 ₂
& 2	& 0010 ₂
--	----
2	0010 ₂

Useful for "masking" bits to 0

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Other Operations on Unsigned Ints

Bitwise OR: (| in C)

- Logical OR corresponding bits

10	1010 _B
1	0001 _B
--	----
11	1011 _B

Useful for "masking" bits to 1

Bitwise exclusive OR (^ in C)

- Logical exclusive OR corresponding bits

10	1010 _B
^ 10	^ 1010 _B
--	----
0	0000 _B

$x \wedge x$ sets
all bits to 0

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iClicker Question

Q: How do you set bit "n" (counting lsb=0) of unsigned variable "u" to zero?

- A. $u \&= (0 \ll n);$
- B. $u |= (1 \ll n);$
- C. $u \&= \sim(1 \ll n);$
- D. $u |= \sim(1 \ll n);$
- E. $u = \sim u \wedge (1 \ll n);$

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Aside: Using Bitwise Ops for Arith

Can use $\ll$, $\gg$, and $\&$ to do some arithmetic efficiently

$x * 2^y = x \ll y$

- $3 * 4 = 3 * 2^2 = 3 \ll 2 \Rightarrow 12$

Fast way to **multiply**
by a power of 2

$x / 2^y = x \gg y$

- $13 / 4 = 13 / 2^2 = 13 \gg 2 \Rightarrow 3$

Fast way to **divide**
unsigned by power of 2

$x \% 2^y = x \& (2^y - 1)$

- $13 \% 4 = 13 \% 2^2 = 13 \& (2^2 - 1)$
 $= 13 \& 3 \Rightarrow 1$

Fast way to **mod**
by a power of 2

13	1101 _B
& 3	& 0011 _B
--	----
1	0001 _B

Many compilers will
do these transformations
automatically!

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Aside: Example C Program

```
#include <stdio.h>
#include <stdlib.h>
int main(void)
{
    unsigned int n;
    unsigned int count = 0;
    printf("Enter an unsigned integer: ");
    if (scanf("%u", &n) != 1)
    {
        fprintf(stderr, "Error: Expect unsigned int.\n");
        exit(EXIT_FAILURE);
    }
    while (n > 0)
    {
        count += (n & 1);
        n = n >> 1;
    }
    printf("%u\n", count);
    return 0;
}
```

What does it
write?

How could you
express this more
succinctly?

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Agenda

Number Systems

Finite representation of unsigned integers

Finite representation of signed integers

Finite representation of rational (floating-point) numbers

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Sign-Magnitude

Integer	Rep
-7	1111
-6	1110
-5	1101
-4	1100
-3	1011
-2	1010
-1	1001
-0	1000
0	0000
1	0001
2	0010
3	0011
4	0100
5	0101
6	0110
7	0111

Definition

High-order bit indicates sign

0 $\Rightarrow$ positive

1 $\Rightarrow$ negative

Remaining bits indicate magnitude

0101_B = 101_B = 5

1101_B = -101_B = -5

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Sign-Magnitude (cont.)

Integer	Rep
-7	1111
-6	1110
-5	1101
-4	1100
-3	1011
-2	1010
-1	1001
0	1000
0	0000
1	0001
2	0010
3	0011
4	0100
5	0101
6	0110
7	0111

Computing negative

$\text{neg}(x) = \text{flip high order bit of } x$

$$\text{neg}(0101_B) = 1101_B$$

$$\text{neg}(1101_B) = 0101_B$$

Pros and cons

- + easy to understand, easy to negate
- + symmetric
- two representations of zero
- need different algorithms to add signed and unsigned numbers

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Ones' Complement

Integer	Rep
-7	1000
-6	1001
-5	1010
-4	1011
-3	1100
-2	1101
-1	1110
0	1111
0	0000
1	0001
2	0010
3	0011
4	0100
5	0101
6	0110
7	0111

Definition

High-order bit has weight $-(2^{b-1})$

$$1010_B = (1 \cdot -7) + (0 \cdot 4) + (1 \cdot 2) + (0 \cdot 1) = -5$$

$$0010_B = (0 \cdot -7) + (0 \cdot 4) + (1 \cdot 2) + (0 \cdot 1) = 2$$

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Ones' Complement (cont.)

Integer	Rep
-7	1000
-6	1001
-5	1010
-4	1011
-3	1100
-2	1101
-1	1110
0	1111
0	0000
1	0001
2	0010
3	0011
4	0100
5	0101
6	0110
7	0111

Computing negative

$\text{neg}(x) = \sim x$

$$\text{neg}(0101_B) = 1010_B$$

$$\text{neg}(1010_B) = 0101_B$$

Similar pros and cons to sign-magnitude

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Two's Complement

Integer	Rep
-8	1000
-7	1001
-6	1010
-5	1011
-4	1100
-3	1101
-2	1110
-1	1111
0	0000
1	0001
2	0010
3	0011
4	0100
5	0101
6	0110
7	0111

Definition

High-order bit has weight $-(2^{b-1})$

$$1010_B = (1 \cdot -8) + (0 \cdot 4) + (1 \cdot 2) + (0 \cdot 1) = -6$$

$$0010_B = (0 \cdot -8) + (0 \cdot 4) + (1 \cdot 2) + (0 \cdot 1) = 2$$

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Two's Complement (cont.)

Integer	Rep
-8	1000
-7	1001
-6	1010
-5	1011
-4	1100
-3	1101
-2	1110
-1	1111
0	0000
1	0001
2	0010
3	0011
4	0100
5	0101
6	0110
7	0111

Computing negative

$\text{neg}(x) = \sim x + 1$

$\text{neg}(x) = \text{onescomp}(x) + 1$

$$\text{neg}(0101_B) = 1010_B + 1 = 1011_B$$

$$\text{neg}(1011_B) = 0100_B + 1 = 0101_B$$

Pros and cons

- not symmetric ("extra" negative number)
- + one representation of zero
- + same algorithm adds unsigned numbers or signed numbers

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Two's Complement (cont.)

Almost all computers today use two's complement to represent signed integers

- Arithmetic is easy!

Is it after 1980?
OK, then we're surely
two's complement



Hereafter, assume two's complement

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Adding Signed Integers

pos + pos	pos + pos (overflow)
<pre> 11 3 0011s + 3 0011s -- --- 6 0110s </pre>	<pre> 111 7 0111s + 1 0001s -- --- -8 1000s </pre>
pos + neg	
<pre> 1111 3 0011s + -1 1111s -- --- 2 0010s </pre>	
neg + neg	neg + neg (overflow)
<pre> 11 -3 1101s + -2 1110s -- --- -5 1011s </pre>	<pre> 1 1 -6 1010s + -5 1011s -- --- 5 0101s </pre>

How would you detect overflow programmatically?

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Subtracting Signed Integers

Perform subtraction with borrows

or

Compute two's comp and add

<pre> 11 3 0011s - 4 0100s -- --- -1 1111s </pre>	→	<pre> 111 3 0011s + -4 1100s -- --- -1 1111s </pre>
<pre> 111 -5 1011s - 2 0010s -- --- -7 1001s </pre>	→	<pre> 111 -5 1011s + -2 1110s -- --- -7 1001s </pre>

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Negating Signed Ints: Math

Question: Why does two's comp arithmetic work?

Answer: $[-b] \bmod 2^4 = [\text{twoscomp}(b)] \bmod 2^4$

$$\begin{aligned}
 [-b] \bmod 2^4 &= [2^4 - b] \bmod 2^4 \\
 &= [2^4 - 1 - b + 1] \bmod 2^4 \\
 &= [(2^4 - 1 - b) + 1] \bmod 2^4 \\
 &= [\text{onescomp}(b) + 1] \bmod 2^4 \\
 &= [\text{twoscomp}(b)] \bmod 2^4
 \end{aligned}$$

See Bryant & O'Hallaron book for much more info

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Subtracting Signed Ints: Math

And so:

$$[a - b] \bmod 2^4 = [a + \text{twoscomp}(b)] \bmod 2^4$$

$$\begin{aligned}
 [a - b] \bmod 2^4 &= [a + 2^4 - b] \bmod 2^4 \\
 &= [a + 2^4 - 1 - b + 1] \bmod 2^4 \\
 &= [a + (2^4 - 1 - b) + 1] \bmod 2^4 \\
 &= [a + \text{onescomp}(b) + 1] \bmod 2^4 \\
 &= [a + \text{twoscomp}(b)] \bmod 2^4
 \end{aligned}$$

See Bryant & O'Hallaron book for much more info

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Pithier Rationale: Math

Ring theory.

If $n > 0$, $\mathbb{Z}/(n)$ is a finite commutative ring, with properties:

$$\overline{a_n} + \overline{b_n} = \overline{(a + b)_n}; \overline{a_n} - \overline{b_n} = \overline{(a - b)_n}; \overline{a_n} \overline{b_n} = \overline{(ab)_n}$$

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Shifting Signed Integers

Bitwise left shift (<< in C): fill on right with zeros

$$\begin{aligned}
 3 &<< 1 \Rightarrow 6 \\
 0011s & \quad 0110s \\
 -3 &<< 1 \Rightarrow -6 \\
 1101s & \quad 1010s
 \end{aligned}$$

What is the effect arithmetically?

Results are mod 2^4

Bitwise right shift: fill on left with ???

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Shifting Signed Integers (cont.)

Bitwise **arithmetic** right shift: fill on left **with sign bit**

$6 \gg 1 \Rightarrow 3$
0110_a 0011_a

$-6 \gg 1 \Rightarrow -3$
1010_a 1101_a

What is the effect
arithmetically?

Bitwise **logical** right shift: fill on left **with zeros**

$6 \gg 1 \Rightarrow 3$
0110_a 0011_a

$-6 \gg 1 \Rightarrow 5$
1010_a 0101_a

What is the effect
arithmetically???

In C, right shift ($\gg$) could be logical or arithmetic

- Not specified by standard (happens to be arithmetic on armlab)
- Best to avoid shifting signed integers**

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Other Operations on Signed Ints

Bitwise NOT ($\sim$ in C)

- Same as with unsigned ints

Bitwise AND ($\&$ in C)

- Same as with unsigned ints

Bitwise OR ($\mid$ in C)

- Same as with unsigned ints

Bitwise exclusive OR ($\wedge$ in C)

- Same as with unsigned ints

Best to avoid with signed integers

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Agenda

Number Systems

Finite representation of unsigned integers

Finite representation of signed integers

Finite representation of rational (floating-point) numbers

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Rational Numbers

Mathematics

- A **rational** number is one that can be expressed as the **ratio** of two integers
- Unbounded range and precision

Computer science

- Finite range and precision
- Approximate using **floating point** number

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Floating Point Numbers

Like scientific notation: e.g., c is

2.99792458×10^8 m/s

This has the form

(multiplier) $\times$ (base)^(power)

In the computer,

- Multiplier is called mantissa
- Base is almost always 2
- Power is called exponent

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IEEE Floating Point Representation

Common finite representation: **IEEE floating point**

- More precisely: ISO/IEEE 754 standard

Using 32 bits (type **float** in C):

- 1 bit: sign (0 $\Rightarrow$ positive, 1 $\Rightarrow$ negative)
- 8 bits: exponent + 127
- 23 bits: binary fraction of the form 1.bbbbbbbbbbbbbbbbbbbbbbb

Using 64 bits (type **double** in C):

- 1 bit: sign (0 $\Rightarrow$ positive, 1 $\Rightarrow$ negative)
- 11 bits: exponent + 1023
- 52 bits: binary fraction of the form 1.bbbbbbbbbbbbbbbbbbbbbbbbbbbbbbbbbbbbbbb

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Floating Point Example

Sign (1 bit):

- 1 $\Rightarrow$ negative

32-bit representation

11000001110110110000000000000000

Exponent (8 bits):

- $10000011_2 = 131$
- $131 - 127 = 4$

Mantissa (23 bits):

- $1.10110110000000000000000_2$
- $1 + (1 \cdot 2^{-1}) + (0 \cdot 2^{-2}) + (1 \cdot 2^{-3}) + (1 \cdot 2^{-4}) + (0 \cdot 2^{-5}) + (1 \cdot 2^{-6}) + (1 \cdot 2^{-7}) = 1.7109375$

Number:

- $-1.7109375 \cdot 2^4 = -27.375$

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When was floating-point invented?

Answer: long before computers!

mantissa

noun

decimal part of a logarithm, 1865, from Latin *mantisa* "a worthless addition, makeweight," perhaps a Gaulish word introduced into Latin via Etruscan (cf. Old Irish *meit*, Welsh *maint* "size").

COMMON LOGARITHMS $\log_{10} x$												
x	0	1	2	3	4	5	6	7	8	9	Δ_m	Δ
50	6990	6998	7007	7016	7024	7033	7042	7050	7059	7067	9	1 2 3
51	7076	7084	7093	7101	7110	7118	7126	7135	7143	7152	8	1 2 2
52	7160	7168	7177	7185	7193	7202	7210	7218	7226	7235	8	1 2 2
53	7243	7251	7259	7267	7275	7284	7292	7300	7308	7316	8	1 2 2
54	7324	7332	7340	7348	7356	7364	7372	7380	7388	7396	8	1 2 2
55	7404	7412	7419	7427	7435	7443	7451	7459	7466	7474	8	1 2 2

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Floating Point Consequences

"Machine epsilon": smallest positive number you can add to 1.0 and get something other than 1.0

For float: $\epsilon \approx 10^{-7}$

- No such number as 1.000000001
- Rule of thumb: "almost 7 digits of precision"

For double: $\epsilon \approx 2 \times 10^{-16}$

- Rule of thumb: "not quite 16 digits of precision"

These are all *relative* numbers

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Floating Point Consequences, cont

Just as decimal number system can represent only some rational numbers with finite digit count...

- Example: $1/3$ *cannot* be represented

Decimal Approx.	Rational Value
.3	3/10
.33	33/100
.333	333/1000
...	

Binary number system can represent only some rational numbers with finite digit count

- Example: $1/5$ *cannot* be represented

Binary Approx.	Rational Value
0.0	0/2
0.01	1/4
0.010	2/8
0.0011	3/16
0.00110	6/32
0.001101	13/64
0.0011010	26/128
0.00110011	51/256
...	

Beware of **roundoff error**

- Error resulting from inexact representation
- Can accumulate
- Be careful when comparing two floating-point numbers for equality

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iClicker Question

Q: What does the following code print?

```
double sum = 0.0;
int i;
for (i = 0; i < 10; i++)
    sum += 0.1;
if (sum == 1.0)
    printf("All good!\n");
else
    printf("Yikes!\n");
```

- A. All good!
- B. Yikes!
- C. Code crashes
- D. Code enters an infinite loop

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Summary

- The binary, hexadecimal, and octal number systems
- Finite representation of unsigned integers
- Finite representation of signed integers
- Finite representation of rational (floating-point) numbers

Essential for proper understanding of

- C primitive data types
- Assembly language
- Machine language

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