



3D Rendering

COS 426

Syllabus



I. Image processing

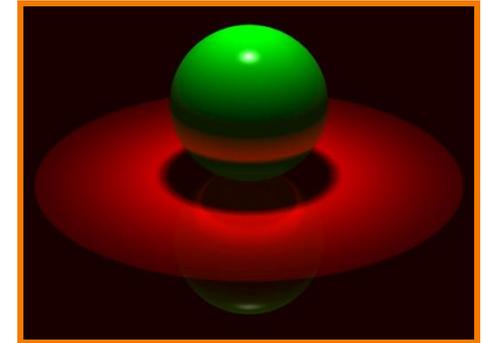
II. Modeling

III. Rendering

IV. Animation



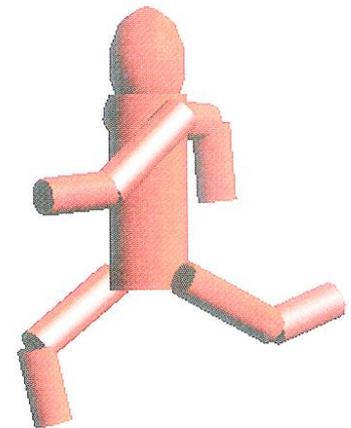
Image Processing
(Rusty Coleman, CS426, Fall99)



Rendering
(Michael Bostock, CS426, Fall99)



Modeling
(Dennis Zorin, CalTech)

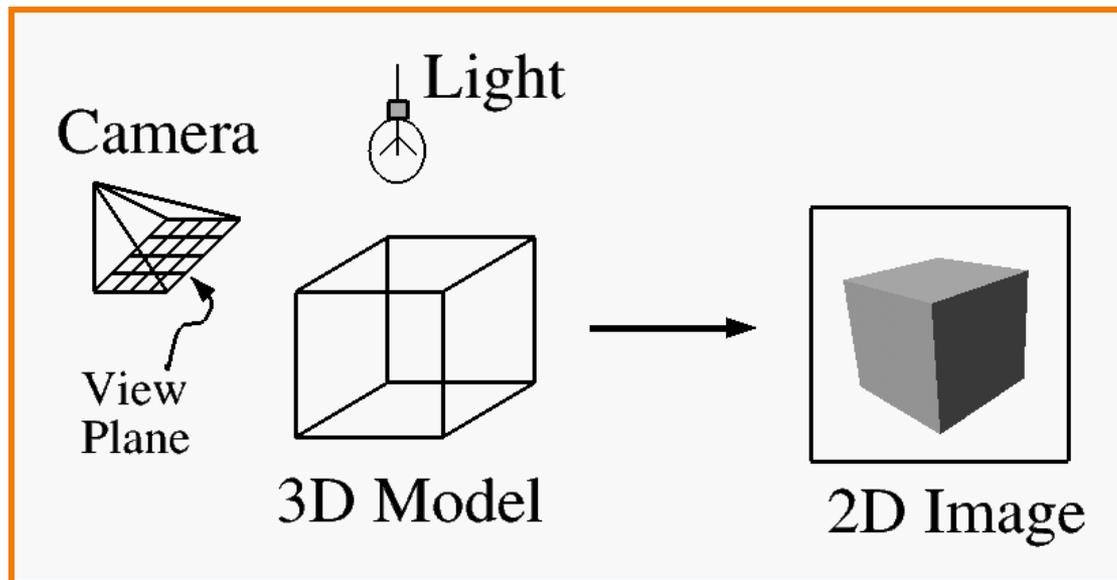


Animation
(Angel, Plate 1)



What is 3D Rendering?

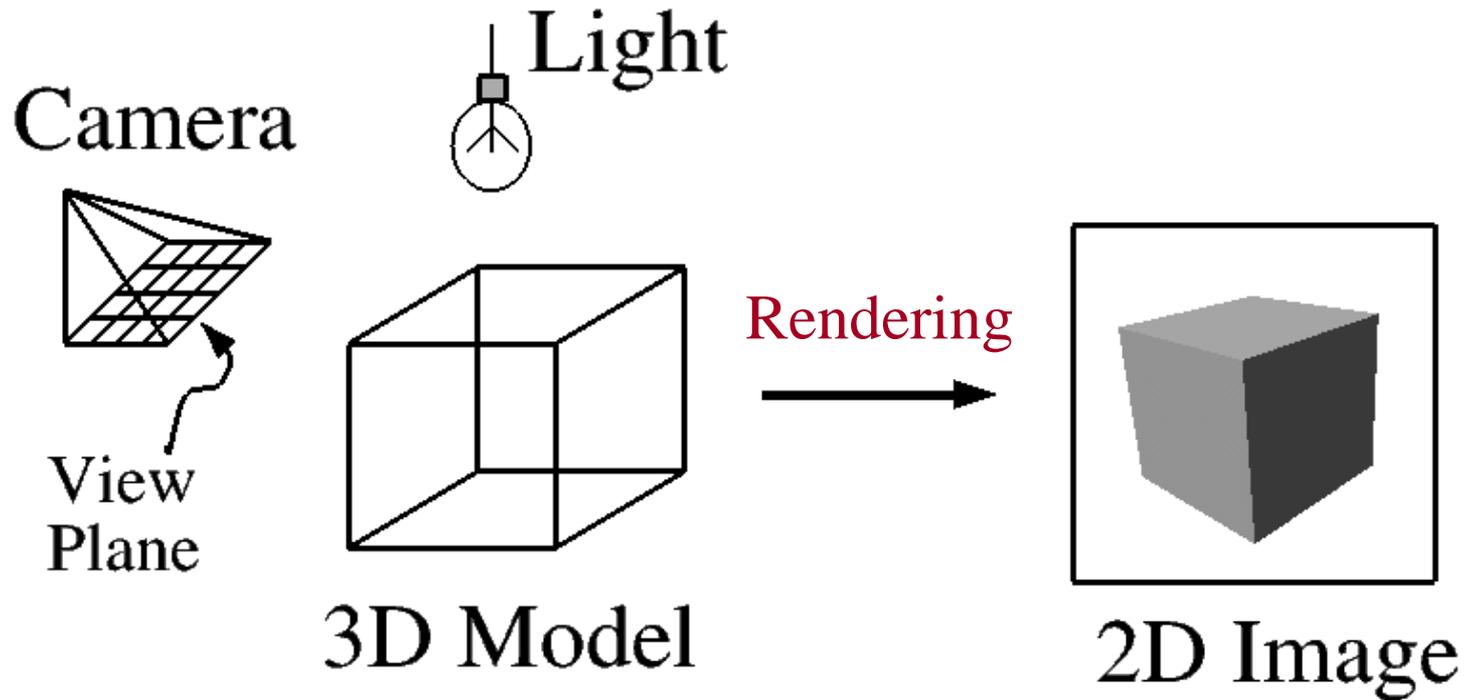
- Topics in computer graphics
 - Imaging = *representing 2D images*
 - Modeling = *representing 3D objects*
 - Rendering = *constructing 2D images from 3D models*
 - Animation = *simulating changes over time*





What is 3D Rendering?

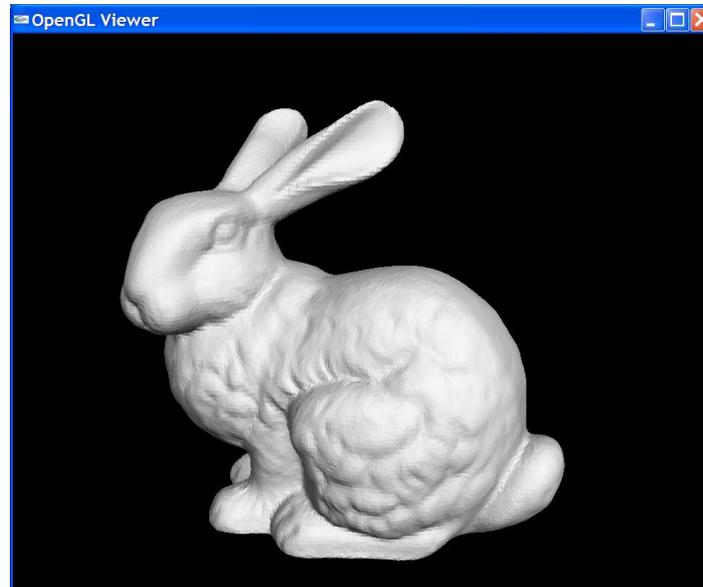
- Construct image from 3D model



3D Rendering Scenario I



- Interactive
 - Images generated in fraction of a second ($<1/10$) as user controls rendering parameters (e.g., camera)
 - Achieve highest quality possible in given time
 - Useful for visualization, games, etc.



meshview



3D Rendering Scenario II

- Offline
 - One image generated with as much quality as possible for a particular set of rendering parameters
 - Take as much time as is needed (minutes)
 - Photorealism: movies, cut scenes, etc.



Avatar

3D Rendering Issues



- What issues must be addressed by a 3D rendering system?

3D Rendering Example



3D Rendering Issues



- What issues must be addressed by a 3D rendering system?



3D Rendering Issues

- What issues must be addressed by a 3D rendering system?
 - Camera
 - Visible surface determination
 - Lights
 - Reflectance
 - Shadows
 - Indirect illumination
 - Sampling
 - etc.



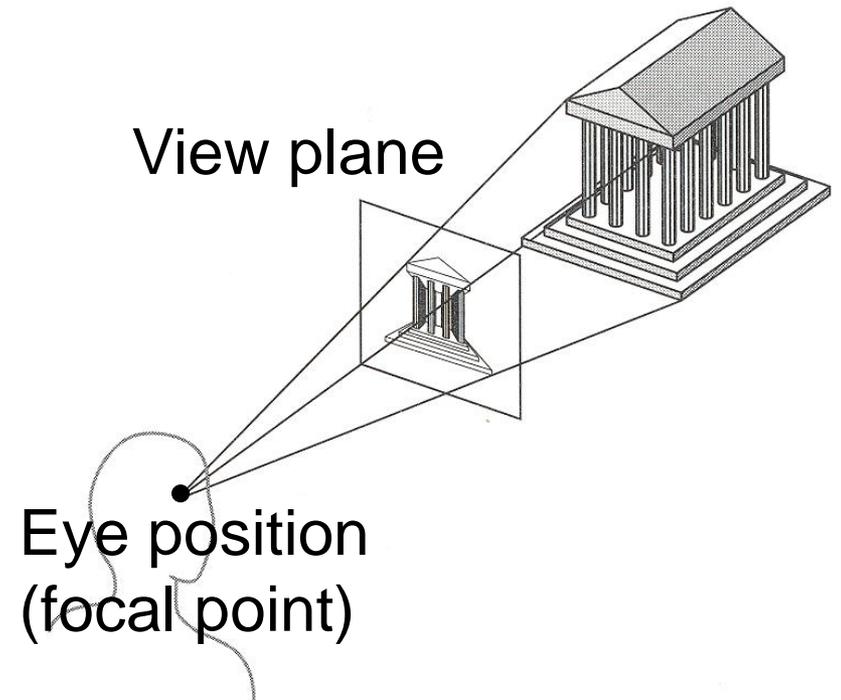
3D Rendering Issues

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 - etc.



Camera Models

- The most common model is pin-hole camera
 - Light rays arrive along paths toward focal point
 - No lens effects (e.g., everything in focus)



Other models consider ...

Depth of field

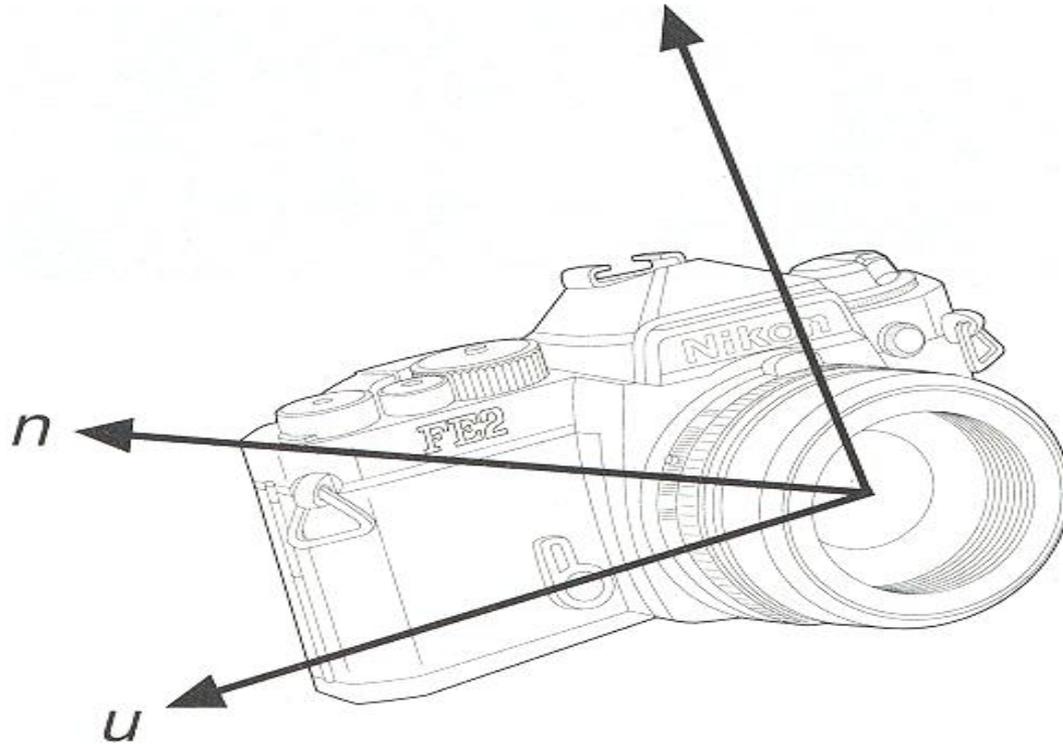
Motion blur

Lens distortion



Camera Parameters

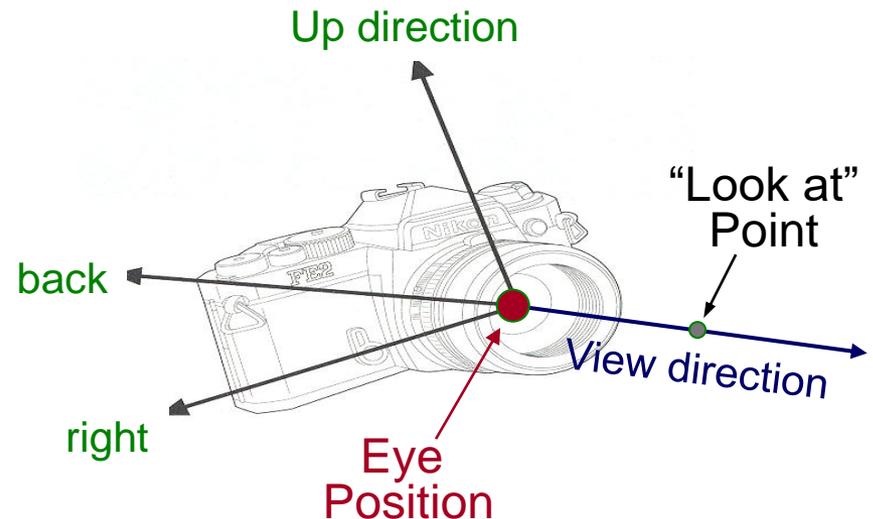
- What are the parameters of a camera?



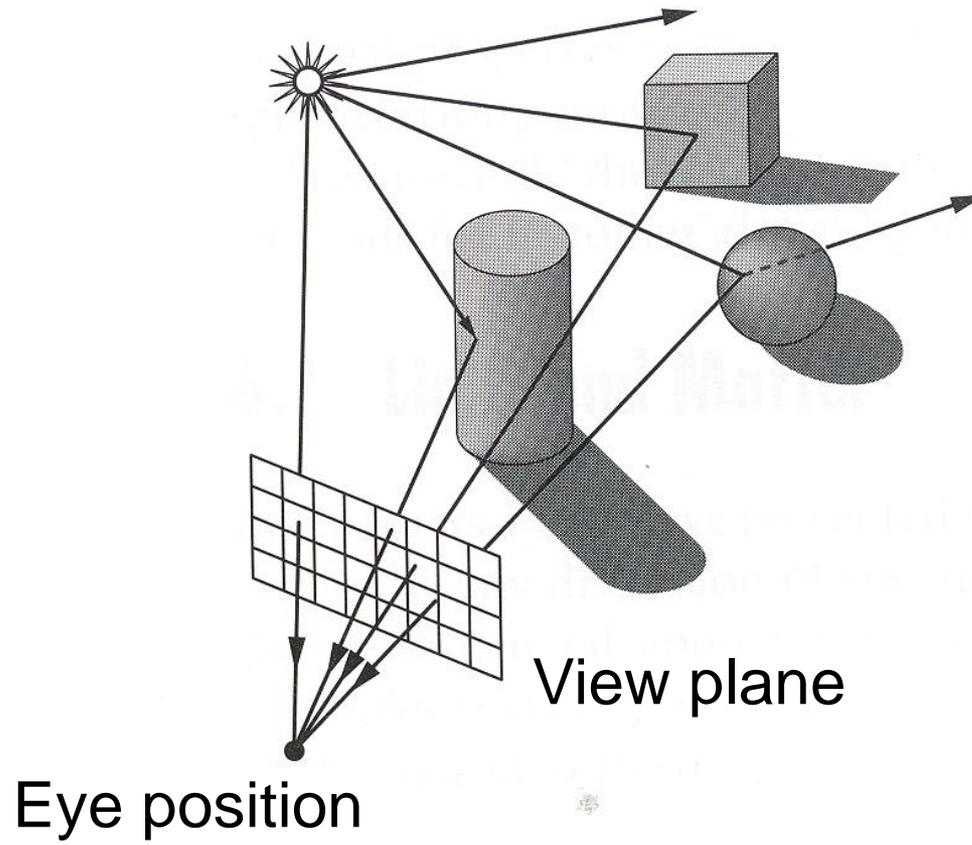


Pinhole Camera Parameters

- Position
 - Eye position (p_x, p_y, p_z)
- Orientation
 - View direction (d_x, d_y, d_z) or “look at” point
 - Up direction (u_x, u_y, u_z)
- Coverage
 - Field of view (fov_x, fov_y)
- Resolution
 - In x and y



View Plane





3D Rendering Issues

- What issues must be addressed by a 3D rendering system?
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 - etc.



Visible Surface Determination

- The color of each pixel on the view plane depends on the radiance (“amount of light”) emanating from **visible** surfaces

How find visible surfaces?

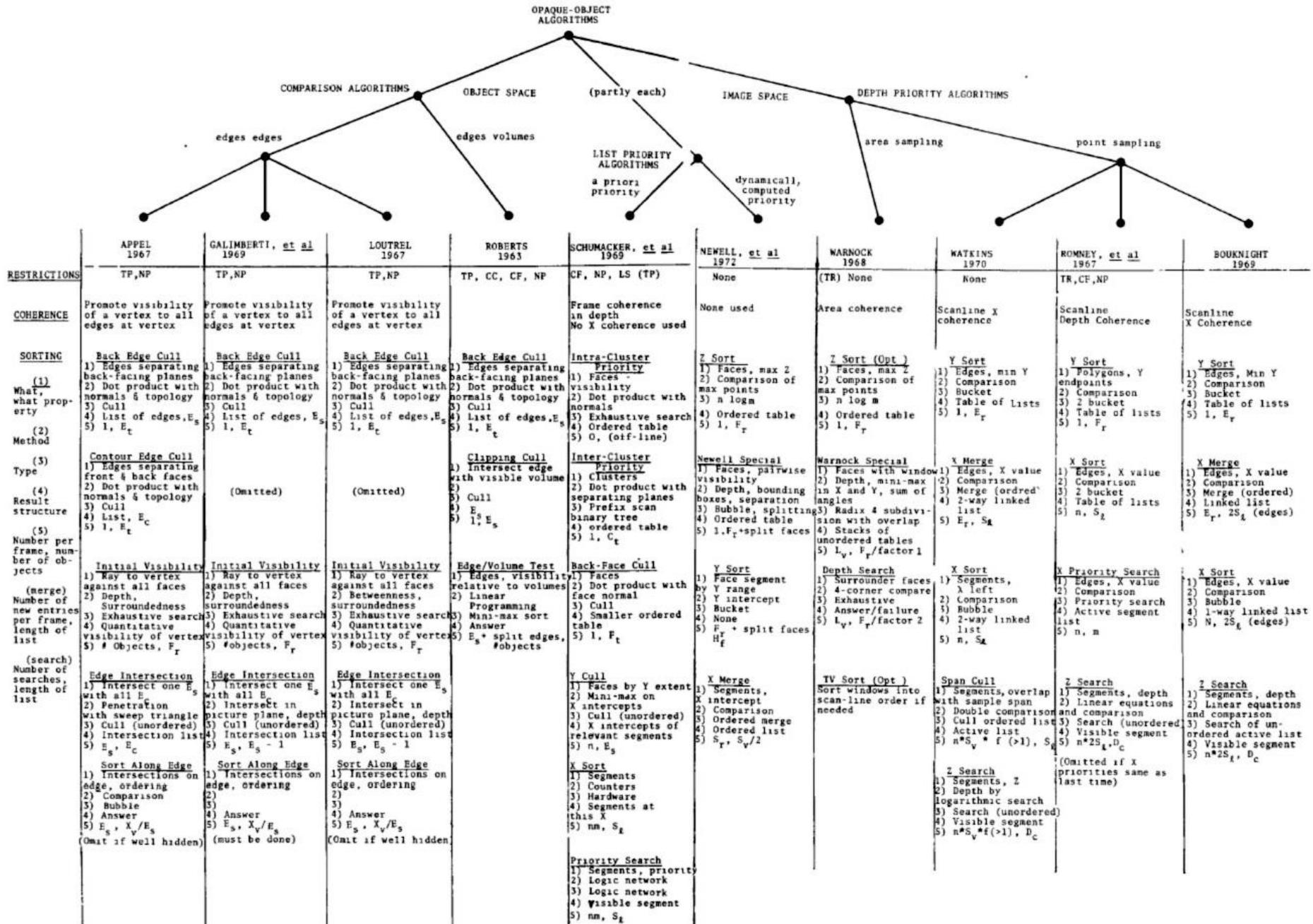


Figure 29. Characterization of ten opaque-object algorithms & Comparison of the algorithms.



In Practice... Brute Force

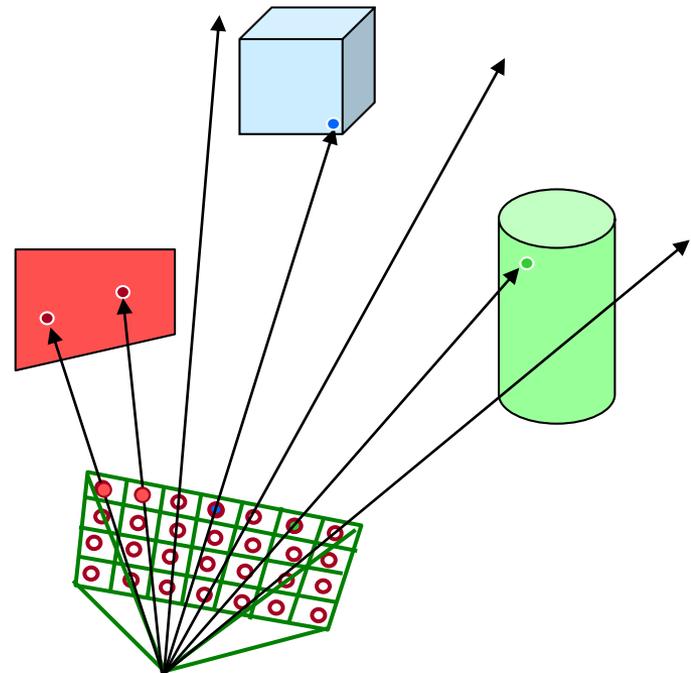
- **Ray tracing**
 - **for each** pixel: determine closest object hit by ray
 - compute color

- **Rasterization**
 - **for each** object: enumerate pixels it hits
 - keep track of color, depth of current-best surface at each pixel



Ray Casting

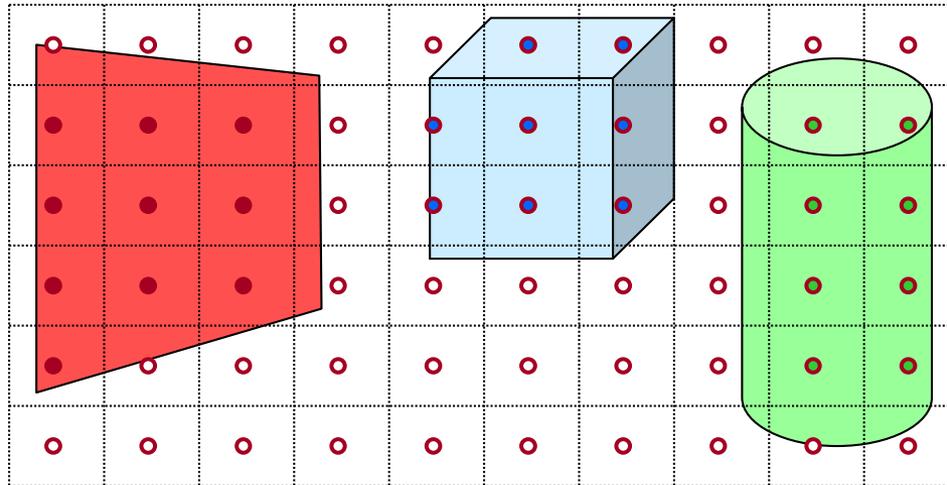
- For each sample ...
 - Construct ray from eye position through view plane
 - Find first surface intersected by ray through pixel
 - Compute color of sample based on surface radiance





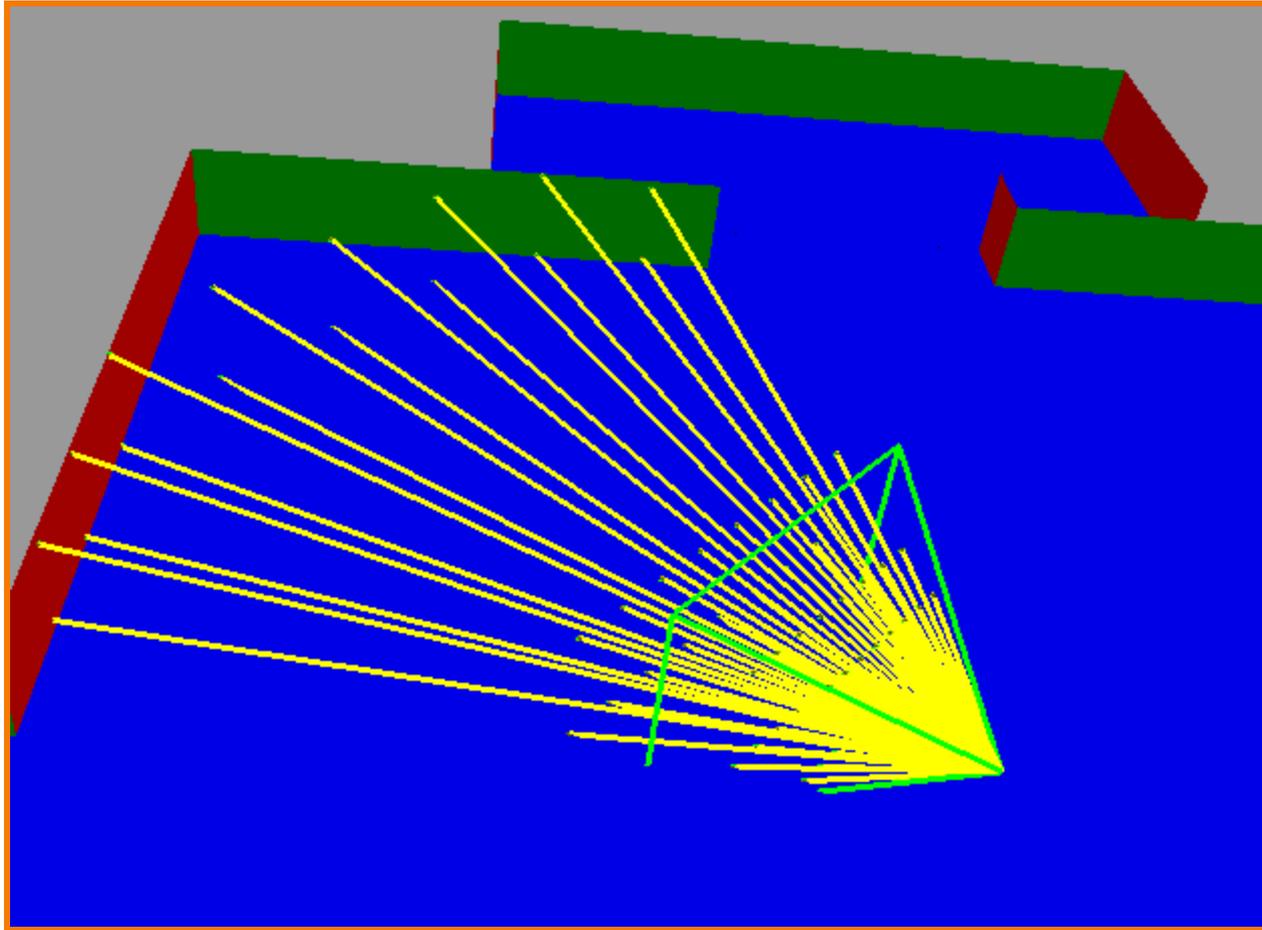
Ray Casting

- For each sample ...
 - Construct ray from eye position through view plane
 - Find first surface intersected by ray through pixel
 - Compute color of sample based on surface radiance





Ray Casting Example



Rays from camera in simple scene



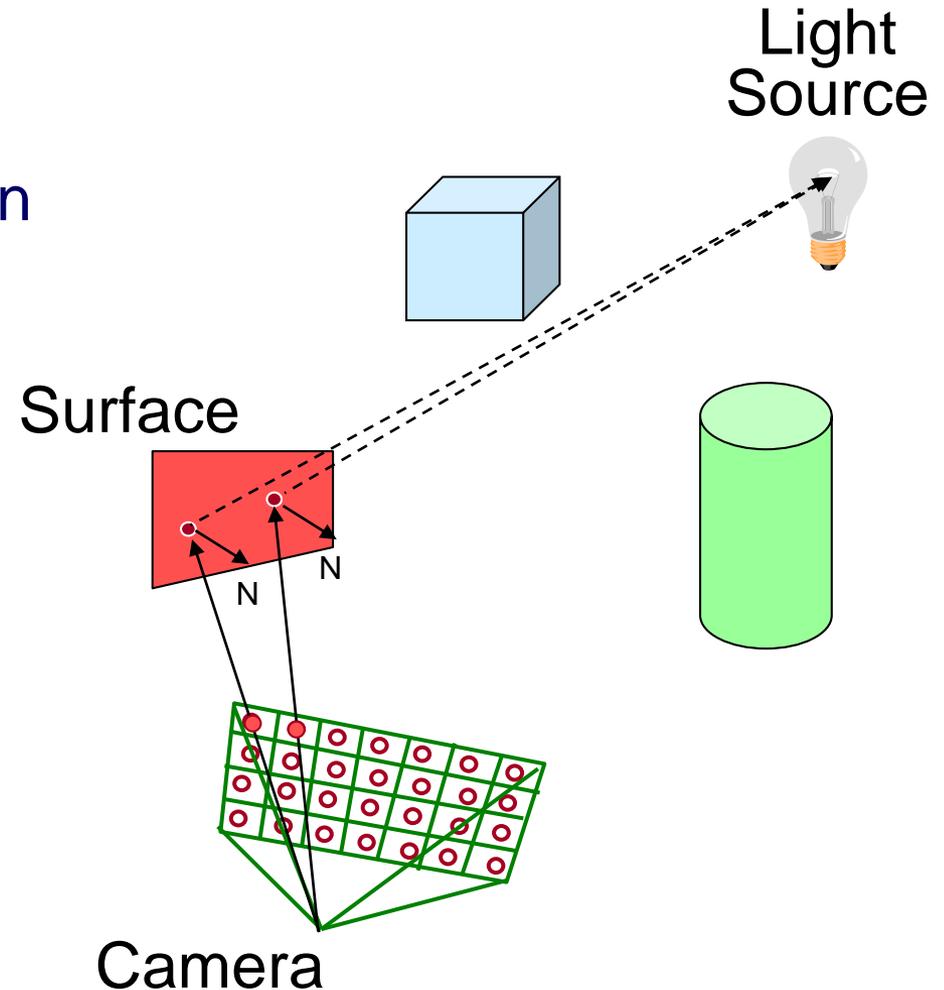
3D Rendering Issues

- What issues must be addressed by a 3D rendering system?
 - Camera
 - Visible surface determination
 - Lights
 - Reflectance
 - Shadows
 - Indirect illumination
 - Sampling
 - etc.

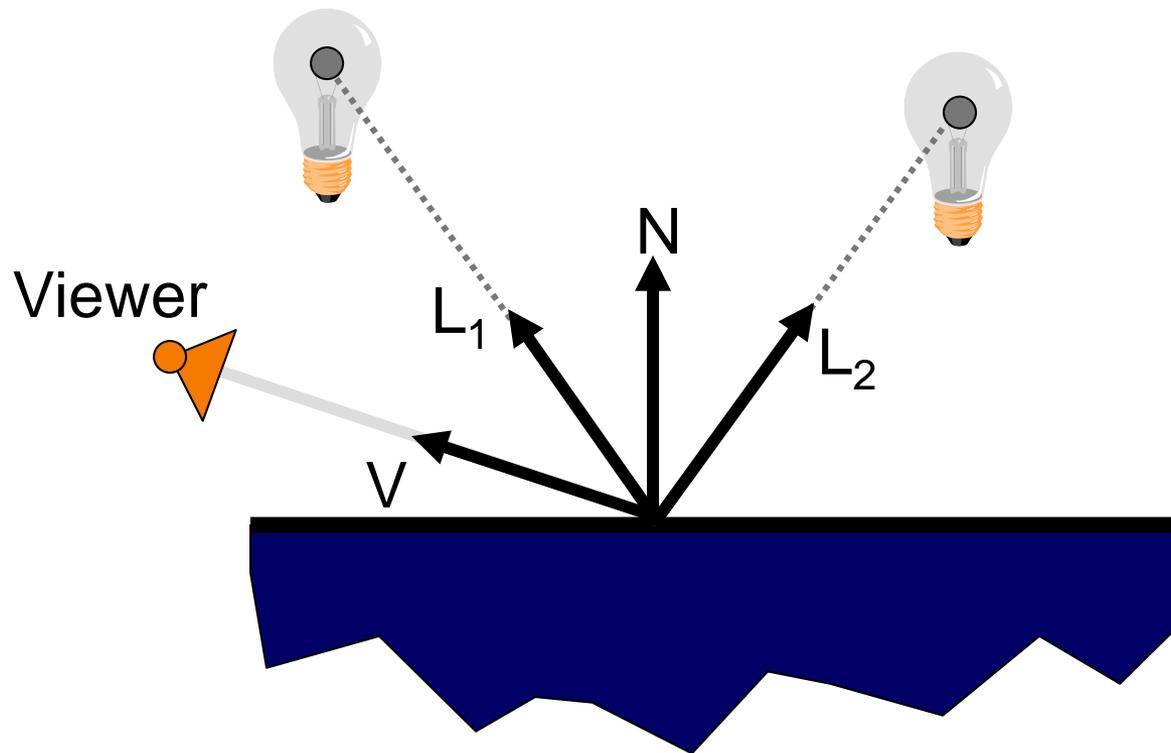


Lighting Simulation

- Lighting parameters
 - Light source emission
 - Surface reflectance
 - Atmospheric attenuation
 - Camera response



Lighting Simulation





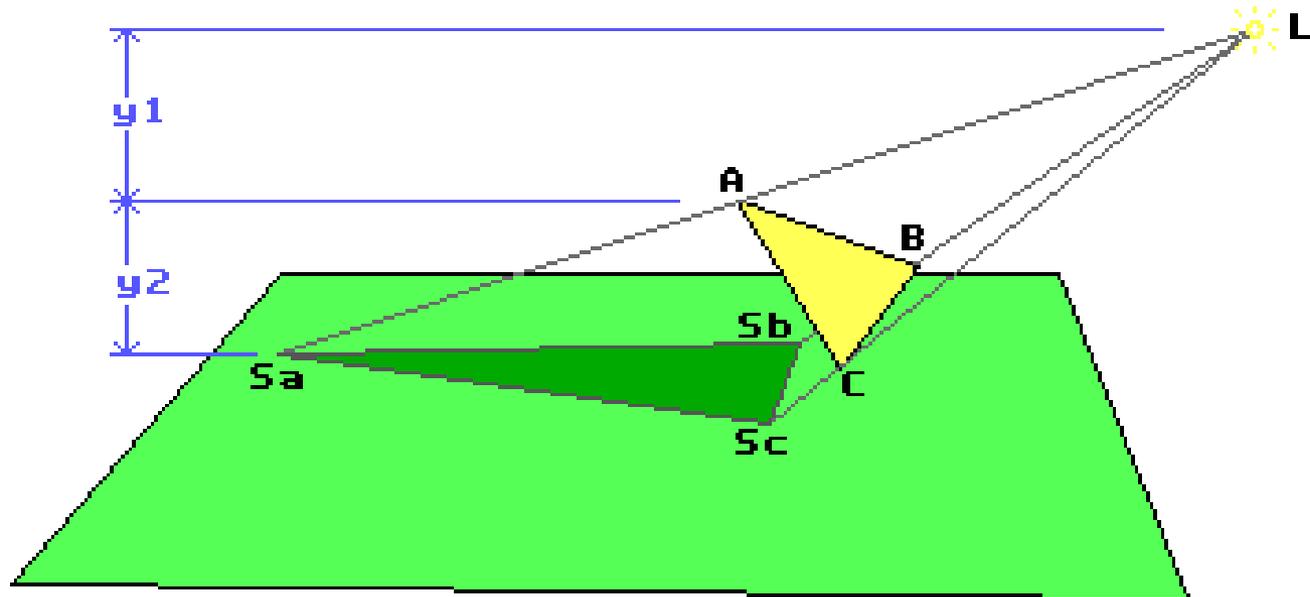
3D Rendering Issues

- What issues must be addressed by a 3D rendering system?
 - Camera
 - Visible surface determination
 - Lights
 - Reflectance
 - **Shadows**
 - Indirect illumination
 - Sampling
 - etc.



Shadows

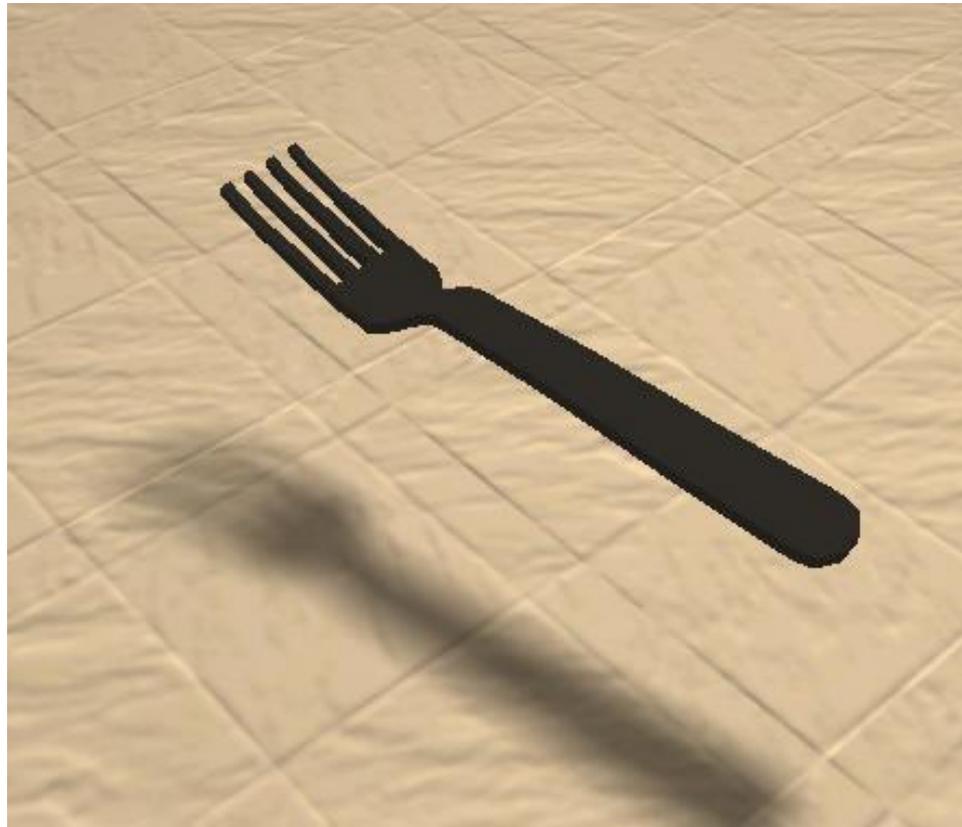
- Occlusions from light sources



Shadows



- Occlusions from light sources
 - Soft shadows with area light source



Shadows

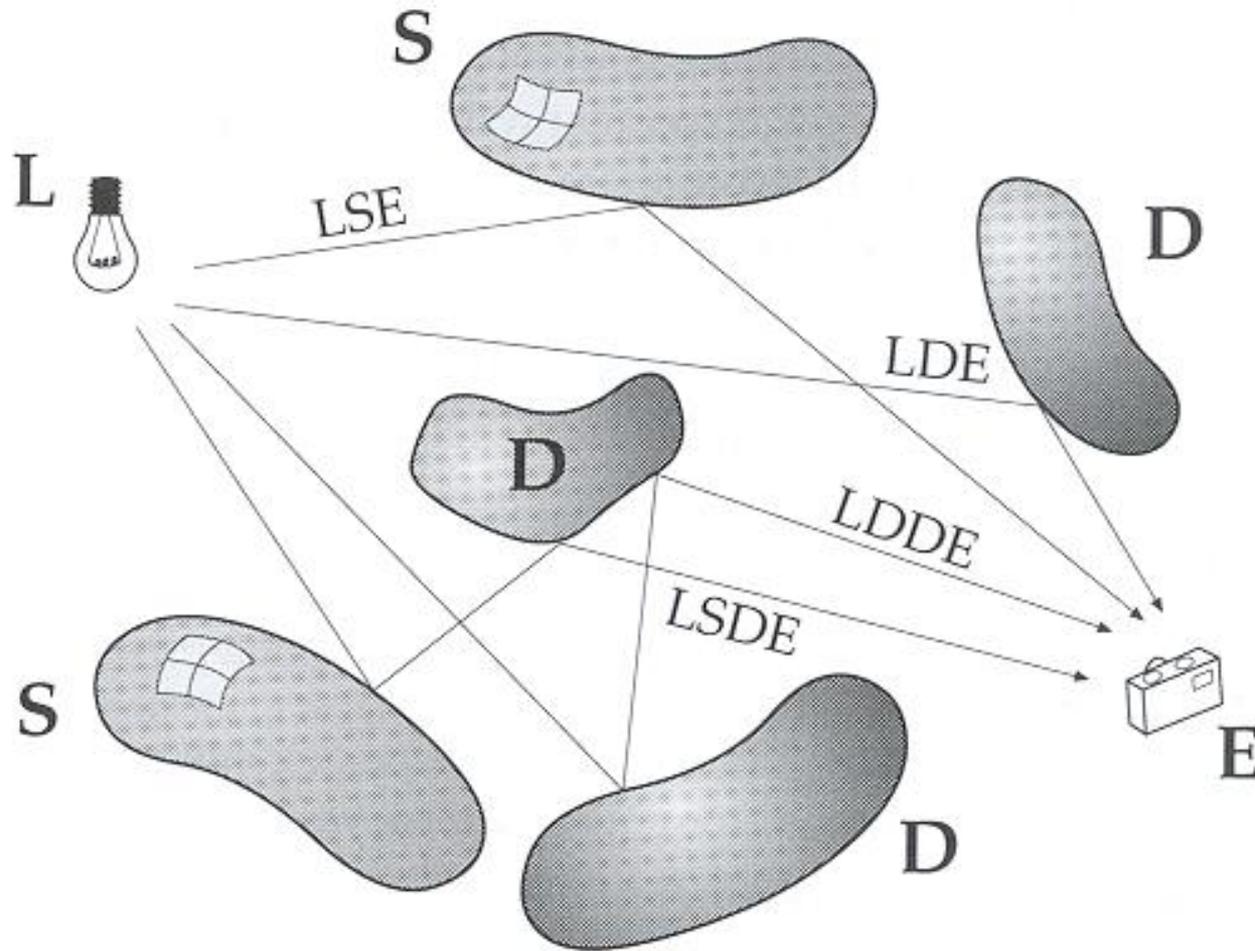




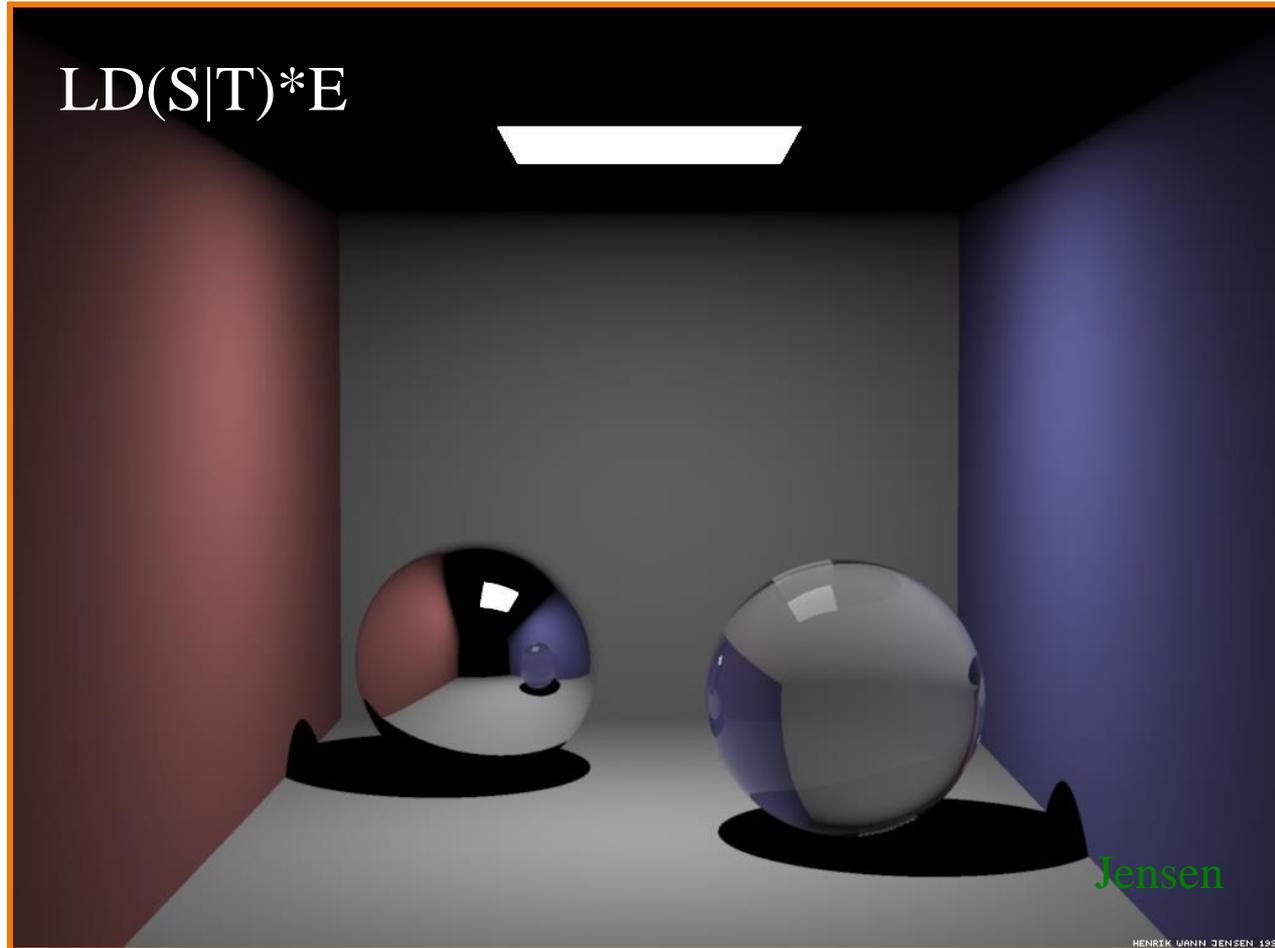
3D Rendering Issues

- What issues must be addressed by a 3D rendering system?
 - Camera
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 - etc.

Path Types



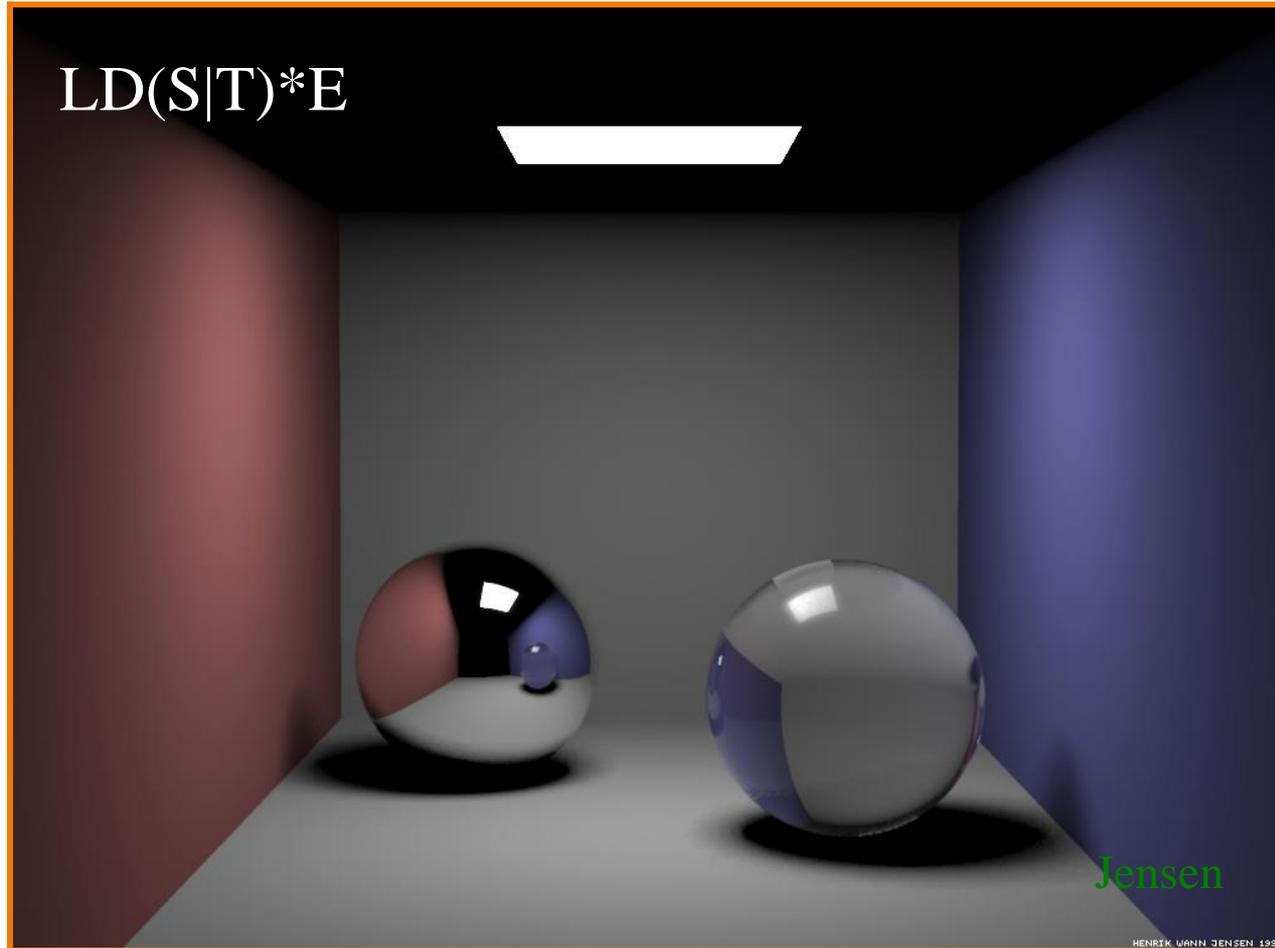
Path Types



direct diffuse + indirect specular and transmission

Henrik Wann Jensen

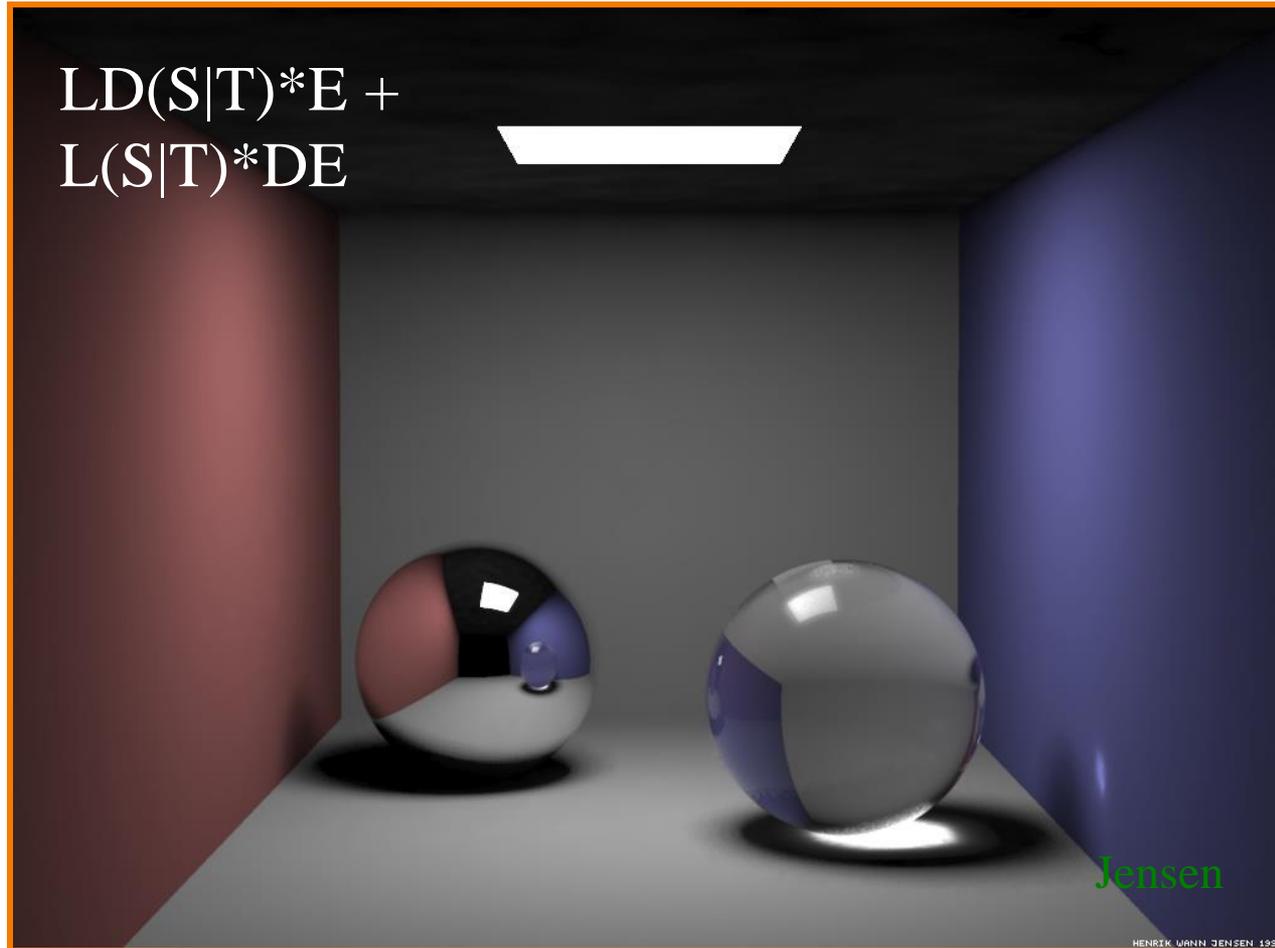
Path Types



+ soft shadows

Henrik Wann Jensen

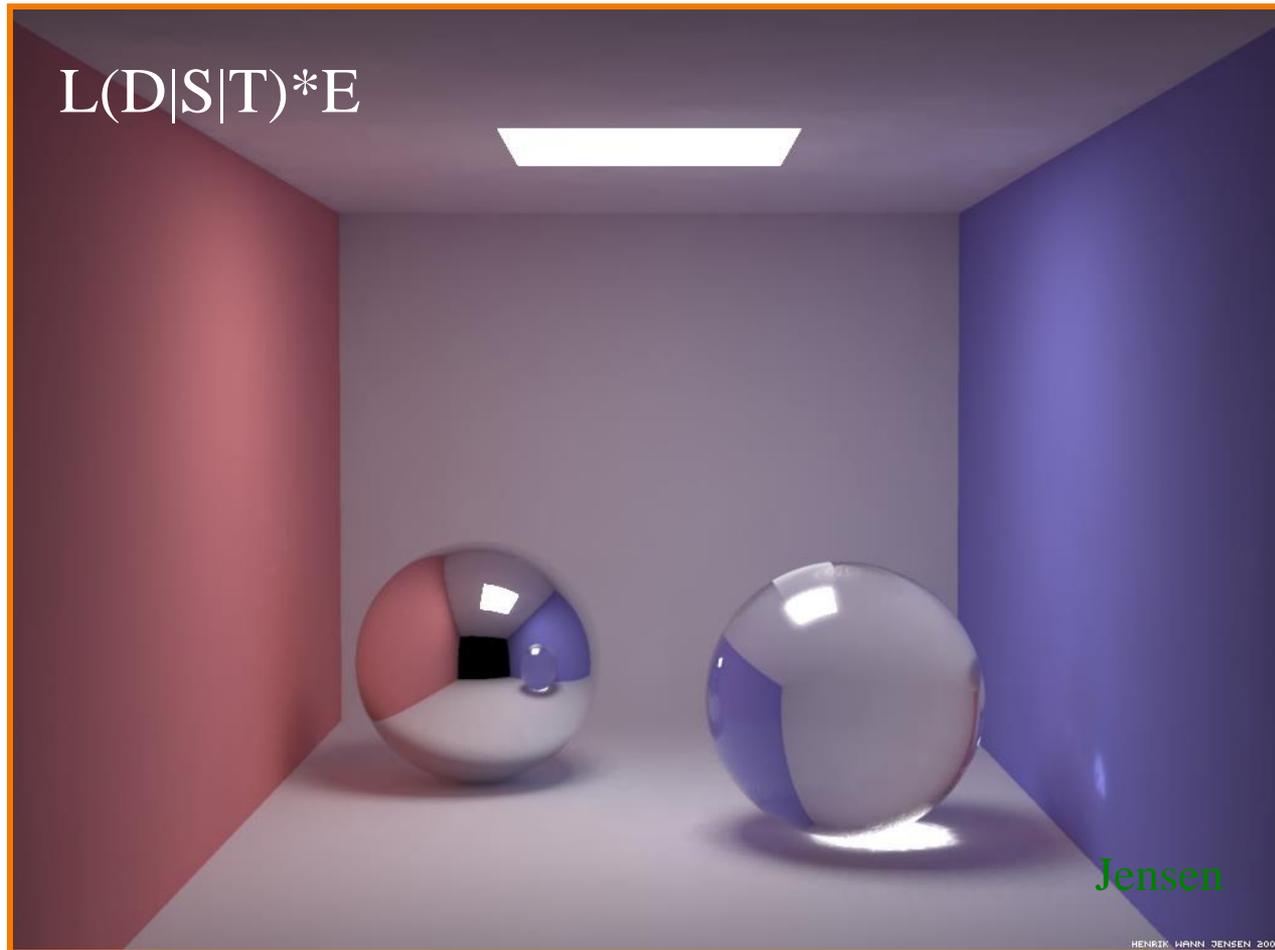
Path Types



+ caustics

Henrik Wann Jensen

Path Types



+ indirect diffuse illumination

Henrik Wann Jensen



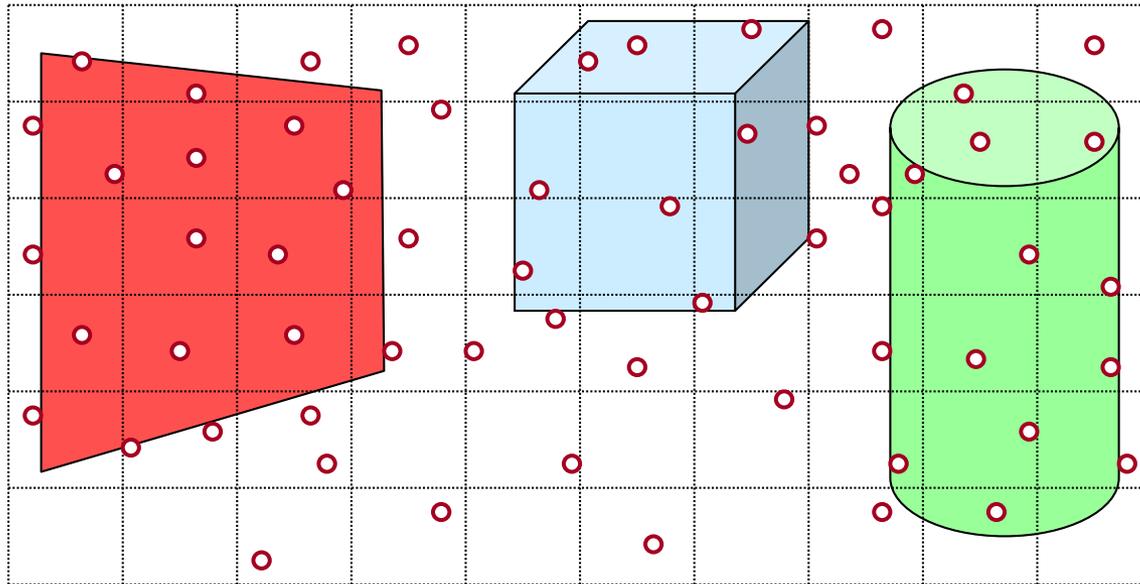
3D Rendering Issues

- What issues must be addressed by a 3D rendering system?
 - Camera
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 - Indirect illumination
 - **Sampling**
 - etc.



Sampling

- Scene can be sampled with any ray
 - Rendering is a problem in sampling and reconstruction



Summary



- Topics for upcoming lectures
 - Camera
 - Visible surface determination
 - Shadows
 - Reflectance
 - Indirect illumination
 - Sampling
 - etc.



Tricycle

(James Percy, CS 426, Fall99)

For assignment #3, you will write a ray tracer!



Ray Casting

COS 426



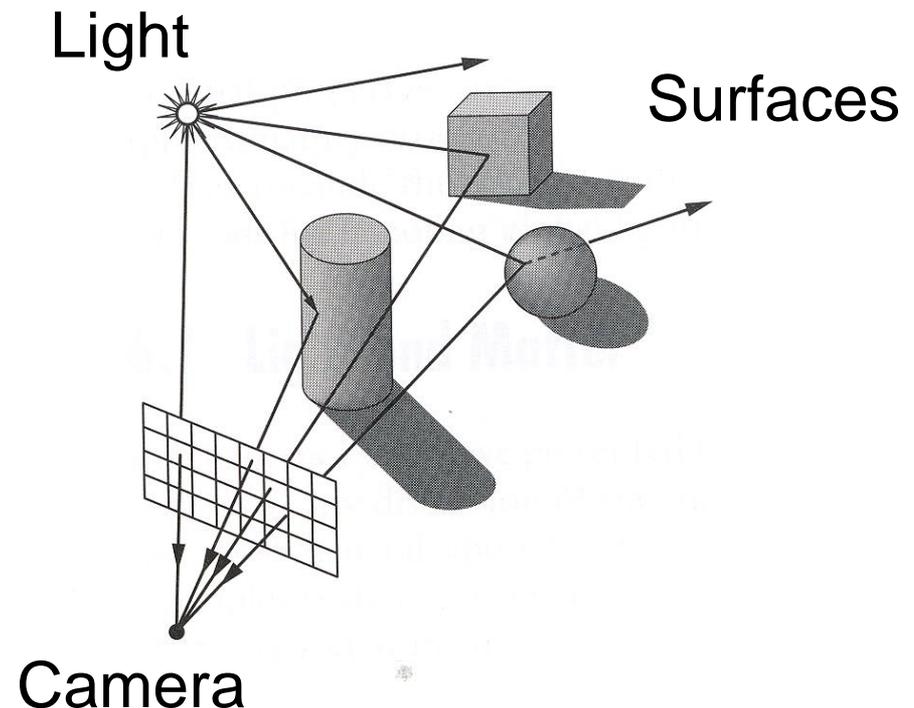
Ray Casting

- Primitive operation for one class of renderers:
 - **Given** a ray (origin, direction)
 - **Find** point of first intersection with scene
- May return:
 - Whether intersection occurs
 - Point of intersection (x,y,z)
 - Parameters of intersection on object
- Used for:
 - Camera (primary) rays: backwards ray tracing
 - Accumulate brightness from lights: forwards ray tracing
 - Shadow rays
 - Indirect illumination (path tracing)



Traditional (Backwards) Ray Tracing

- The color of each pixel on the view plane depends on the radiance emanating along rays from visible surfaces in scene

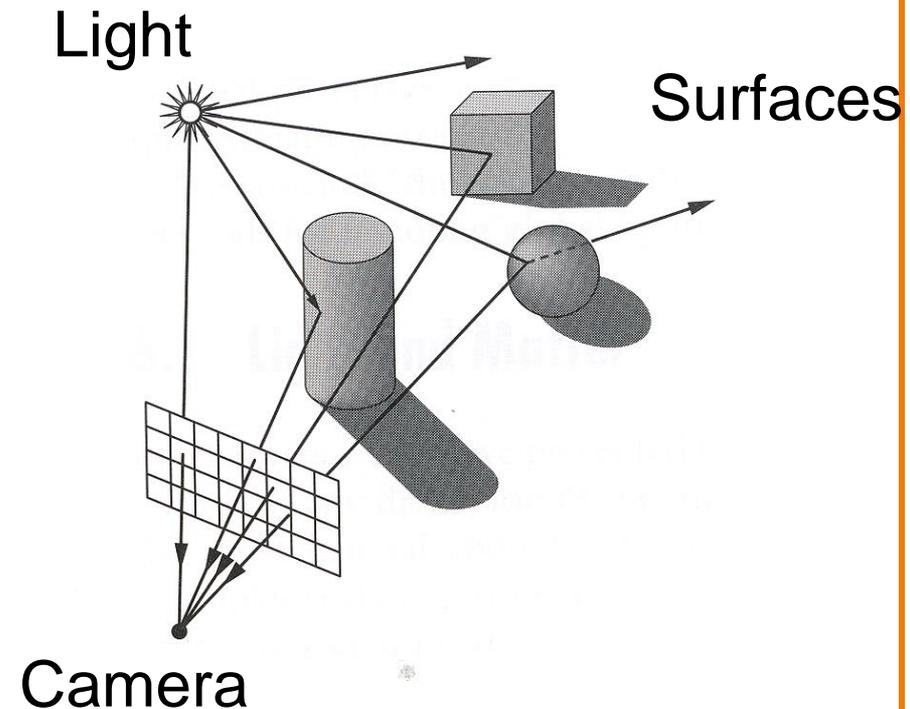


Scene



- Scene has:
 - Scene graph with surface primitives
 - Set of lights
 - Camera

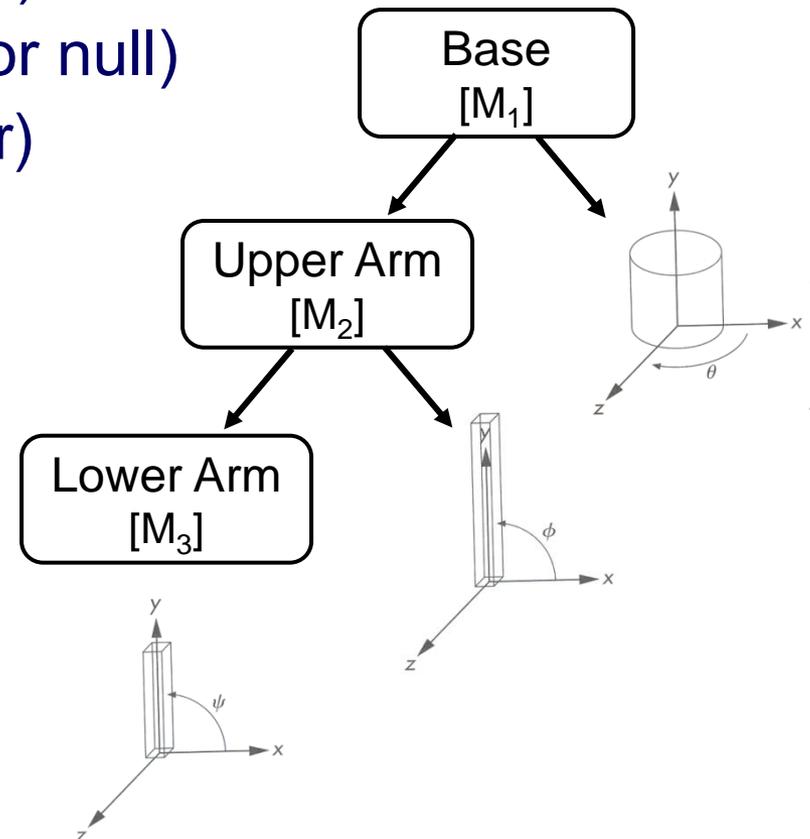
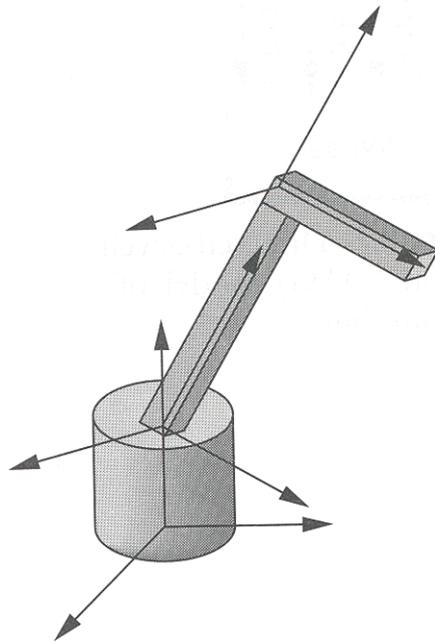
```
struct R3Scene {  
    R3Node *root;  
    vector<R3Light *> lights;  
    R3Camera camera;  
    R3Box bbox;  
    R3Rgb background;  
    R3Rgb ambient;  
};
```





Scene Graph

- Scene graph is hierarchy of nodes, each with:
 - Bounding box (in node's coordinate system)
 - Transformation (4x4 matrix)
 - Shape (mesh, sphere, ... or null)
 - Material (more on this later)





Scene Graph

- Simple scene graph implementation:

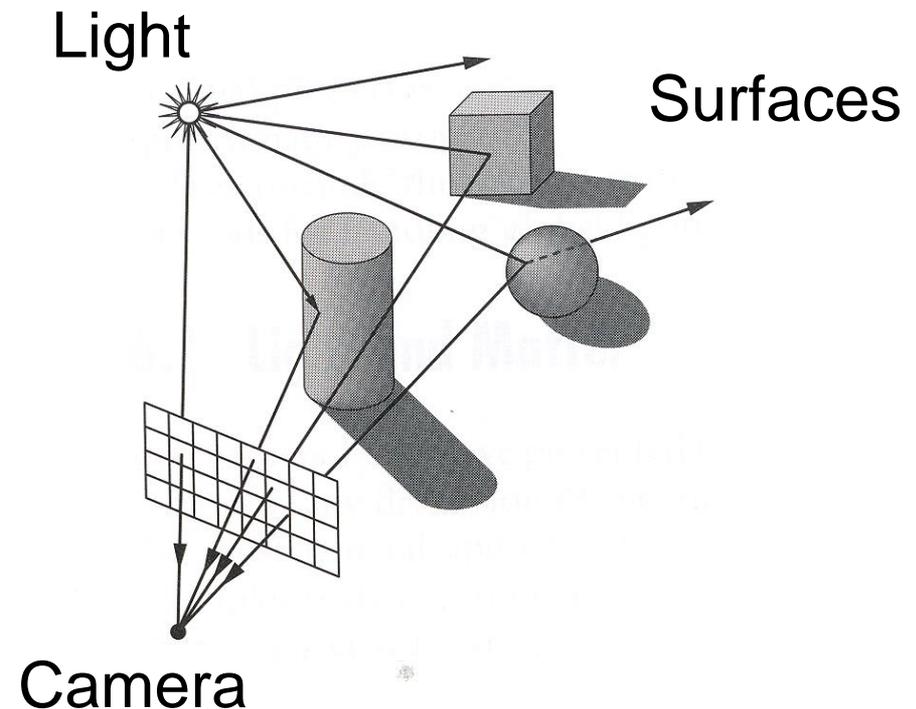
```
struct R3Node {  
    struct R3Node *parent;  
    vector<struct R3Node *> children;  
    R3Shape *shape;  
    R3Matrix transformation;  
    R3Material *material;  
    R3Box bbox;  
};
```

```
struct R3Shape {  
    R3ShapeType type;  
    R3Box *box;  
    R3Sphere *sphere;  
    R3Cylinder *cylinder;  
    R3Cone *cone;  
    R3Mesh *mesh;  
};
```



Ray Casting

- For each sample (pixel) ...
 - Construct ray from eye position through view plane
 - Compute radiance leaving first point of intersection between ray and scene



Ray Casting



- Simple implementation:

```
R2Image *RayCast(R3Scene *scene, int width, int height)
{
    R2Image *image = new R2Image(width, height);
    for (int i = 0; i < width; i++) {
        for (int j = 0; j < height; j++) {
            R3Ray ray = ConstructRayThroughPixel(scene->camera, i, j);
            R3Rgb radiance = ComputeRadiance(scene, &ray);
            image->SetPixel(i, j, radiance);
        }
    }
    return image;
}
```

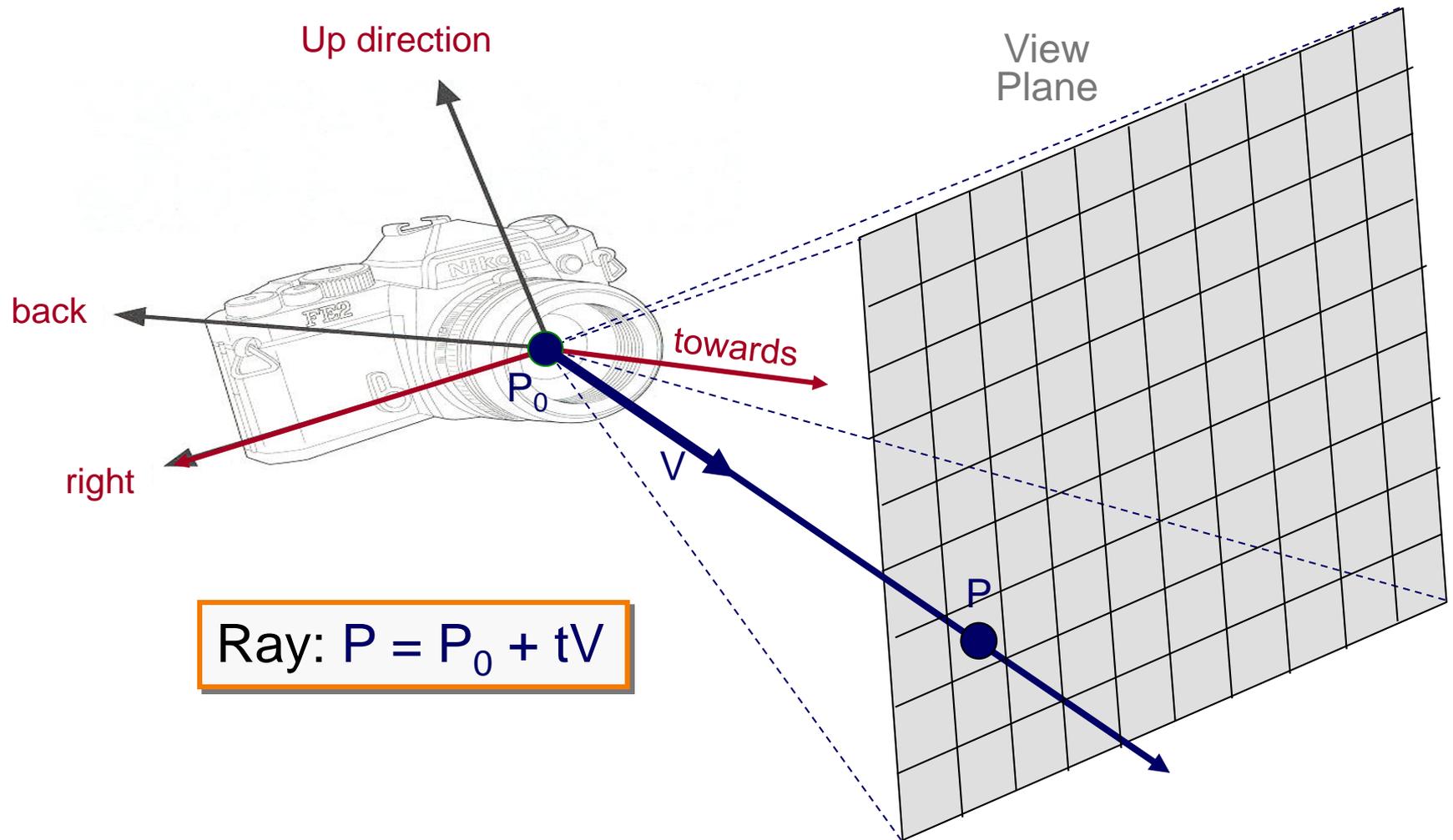


Ray Casting

- Simple implementation:

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            R3Ray ray = ConstructRayThroughPixel(scene->camera, i, j);
            R3Rgb radiance = ComputeRadiance(scene, &ray);
            image->SetPixel(i, j, radiance);
        }
    }
    return image;
}
```

Constructing Ray Through a Pixel



Constructing Ray Through a Pixel



- 2D Example

Θ = frustum **half**-angle

d = distance to view plane

$\text{right} = \text{towards} \times \text{up}$

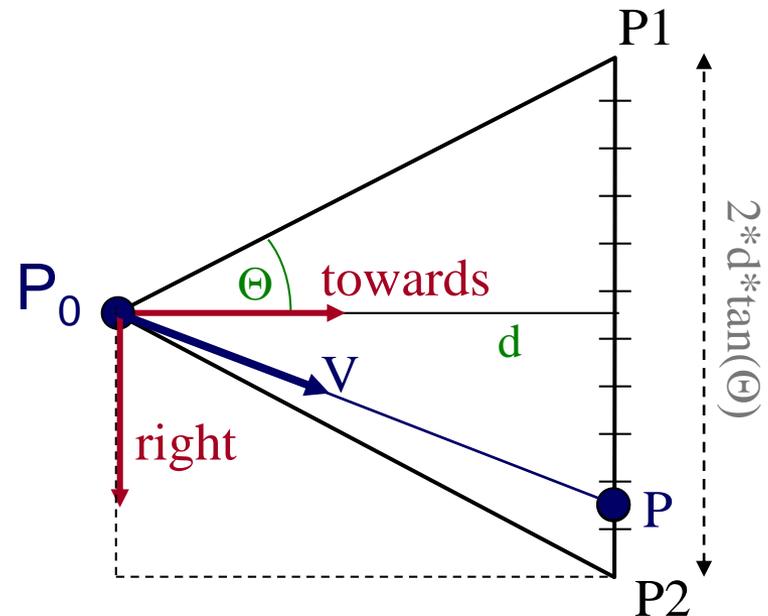
$$P_1 = P_0 + d \cdot \text{towards} - d \cdot \tan(\Theta) \cdot \text{right}$$

$$P_2 = P_0 + d \cdot \text{towards} + d \cdot \tan(\Theta) \cdot \text{right}$$

$$P = P_1 + ((i + 0.5) / \text{width}) * (P_2 - P_1)$$

$$V = (P - P_0) / \|P - P_0\|$$

(d cancels out...)



$$\text{Ray: } P = P_0 + tV$$

Ray Casting



- Simple implementation:

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R2Image *RayCast(R3Scene *scene, int width, int height)
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            image->SetPixel(i, j, radiance);
        }
    }
    return image;
}
```

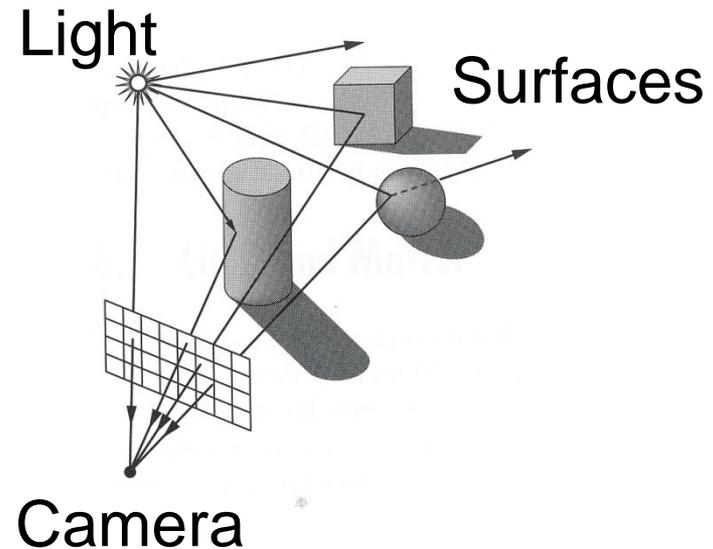


Ray Casting

- Simple implementation:

```
R3Rgb ComputeRadiance(R3Scene *scene, R3Ray *ray)
{
    R3Intersection intersection = ComputeIntersection(scene, ray);
    return ComputeRadiance(scene, ray, intersection);
}
```

```
struct R3Intersection {
    bool hit;
    R3Node *node;
    R3Point position;
    R3Vector normal;
    double t;
};
```



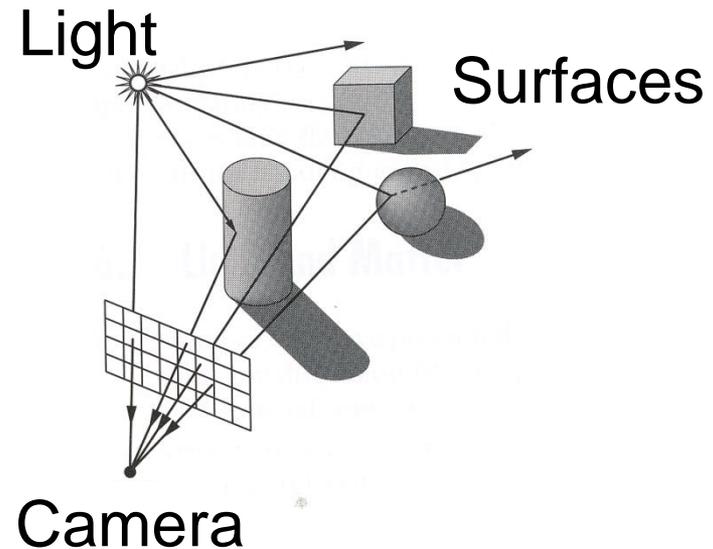


Ray Casting

- Simple implementation:

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}
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```
struct R3Intersection {
    bool hit;
    R3Node *node;
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};
```





Ray Intersection

- Ray Intersection
 - Sphere
 - Triangle
 - Box
 - Scene

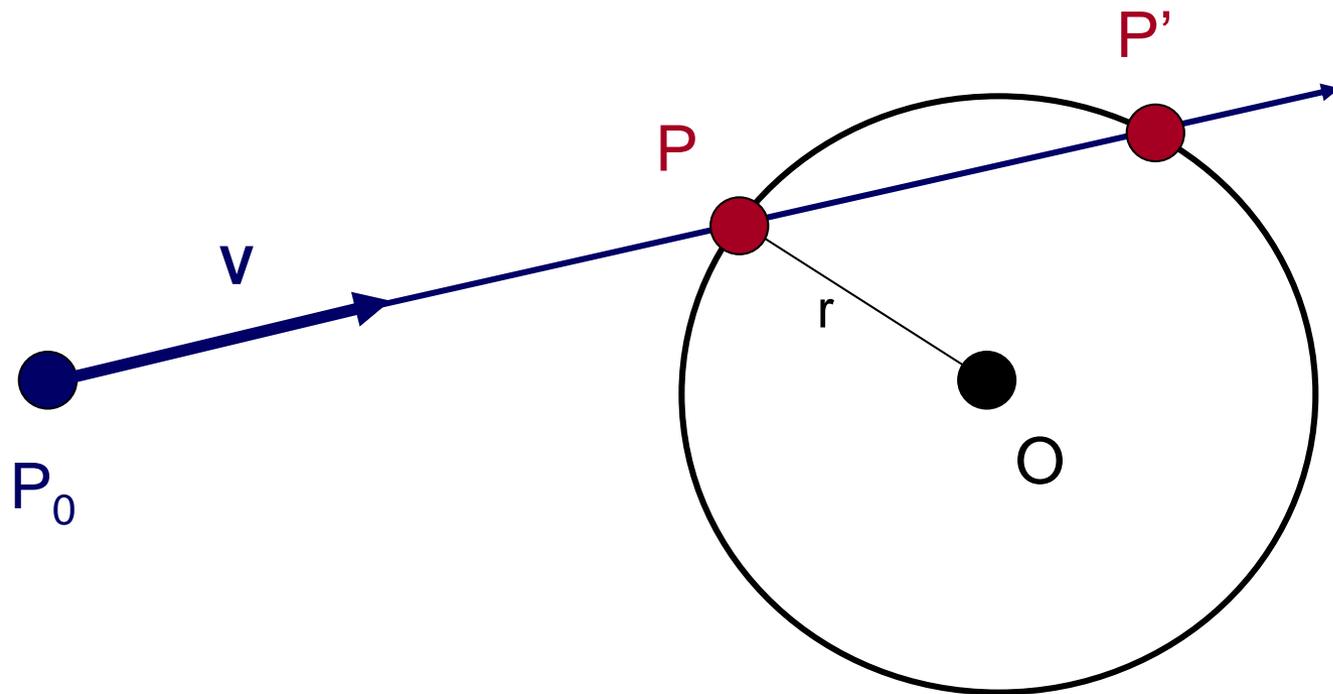
- Ray Intersection Acceleration
 - Bounding volumes
 - Uniform grids
 - Octrees
 - BSP trees



Ray Intersection

- Ray Intersection
 - Sphere
 - Triangle
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- Ray Intersection Acceleration
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Ray-Sphere Intersection

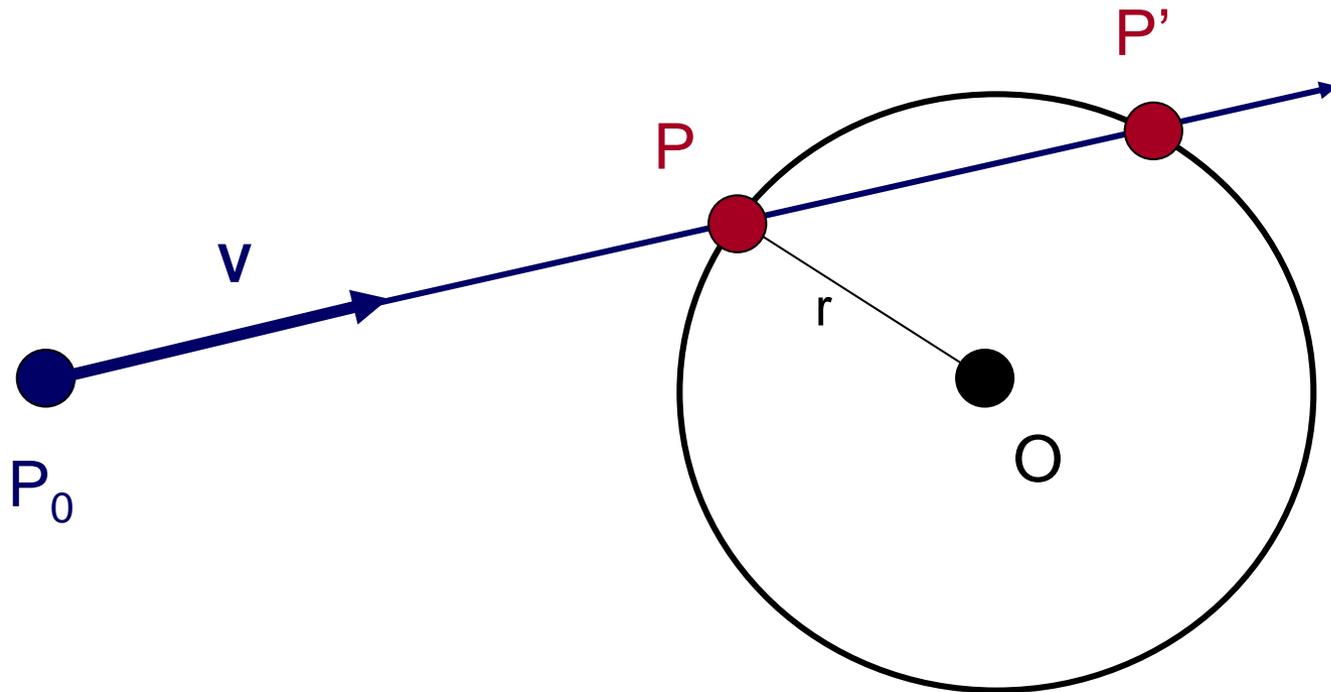




Ray-Sphere Intersection

Ray: $P = P_0 + tV$

Sphere: $|P - O|^2 - r^2 = 0$





Ray-Sphere Intersection I

Ray: $P = P_0 + tV$

Sphere: $|P - O|^2 - r^2 = 0$

Algebraic Method

Substituting for P , we get:

$$|P_0 + tV - O|^2 - r^2 = 0$$

Solve quadratic equation:

$$at^2 + bt + c = 0$$

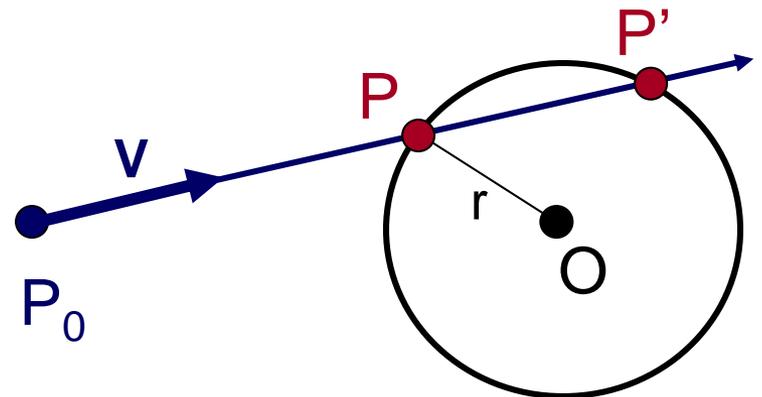
where:

$$a = 1$$

$$b = 2V \cdot (P_0 - O)$$

$$c = |P_0 - O|^2 - r^2 = 0$$

$$P = P_0 + tV$$





Ray-Sphere Intersection II

$$\text{Ray: } P = P_0 + tV$$

$$\text{Sphere: } |P - O|^2 - r^2 = 0$$

Geometric Method

$$L = O - P_0$$

$$t_{ca} = L \cdot V$$

if ($t_{ca} < 0$) return 0

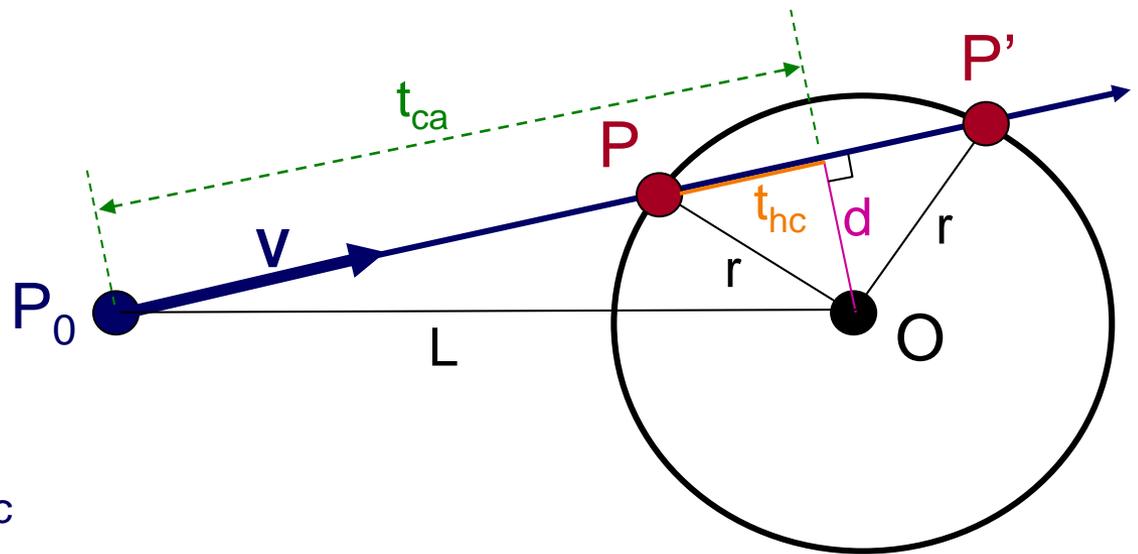
$$d^2 = L \cdot L - t_{ca}^2$$

if ($d^2 > r^2$) return 0

$$t_{hc} = \text{sqrt}(r^2 - d^2)$$

$$t = t_{ca} - t_{hc} \text{ and } t_{ca} + t_{hc}$$

$$P = P_0 + tV$$

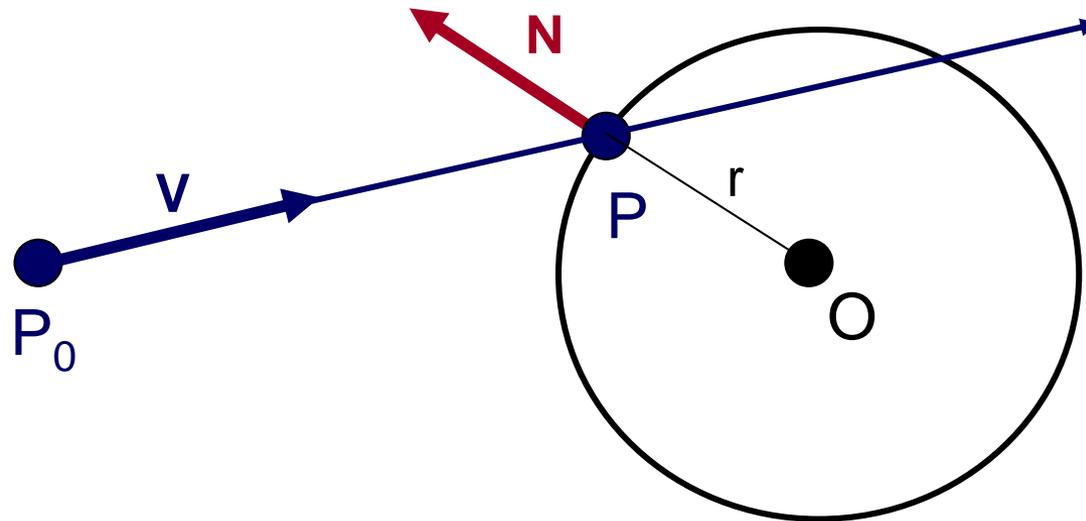




Ray-Sphere Intersection

- Need normal vector at intersection for lighting calculations

$$N = (P - O) / \|P - O\|$$



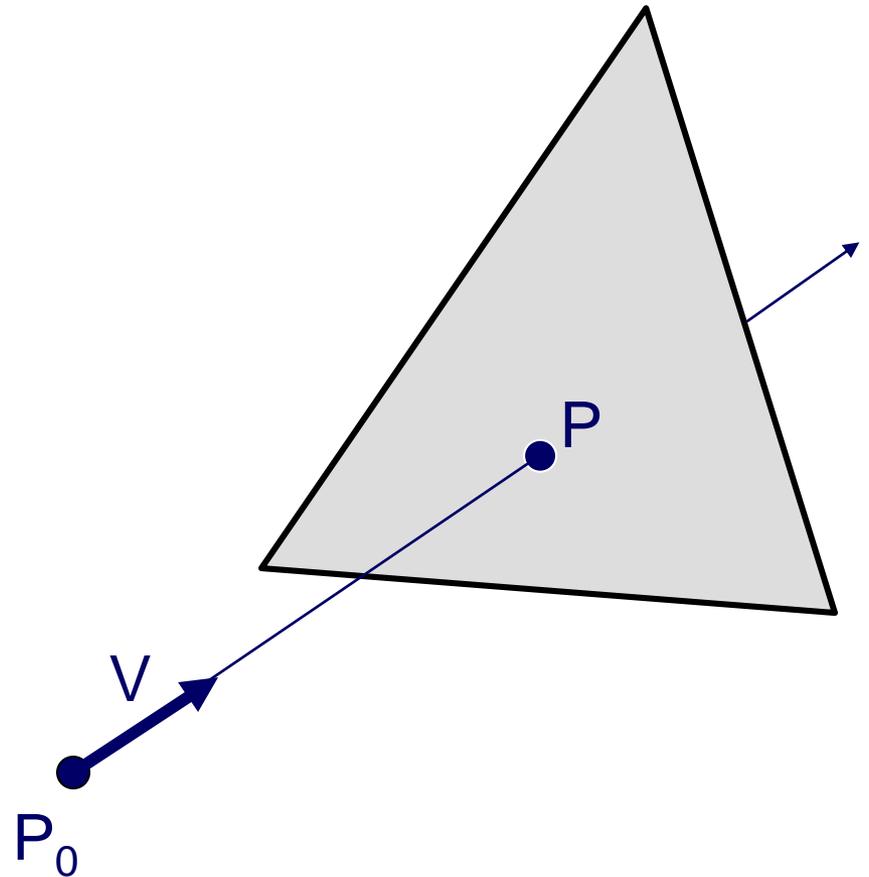


Ray Intersection

- Ray Intersection
 - Sphere
 - Triangle
 - Box
 - Scene

- Ray Intersection Acceleration
 - Bounding volumes
 - Uniform grids
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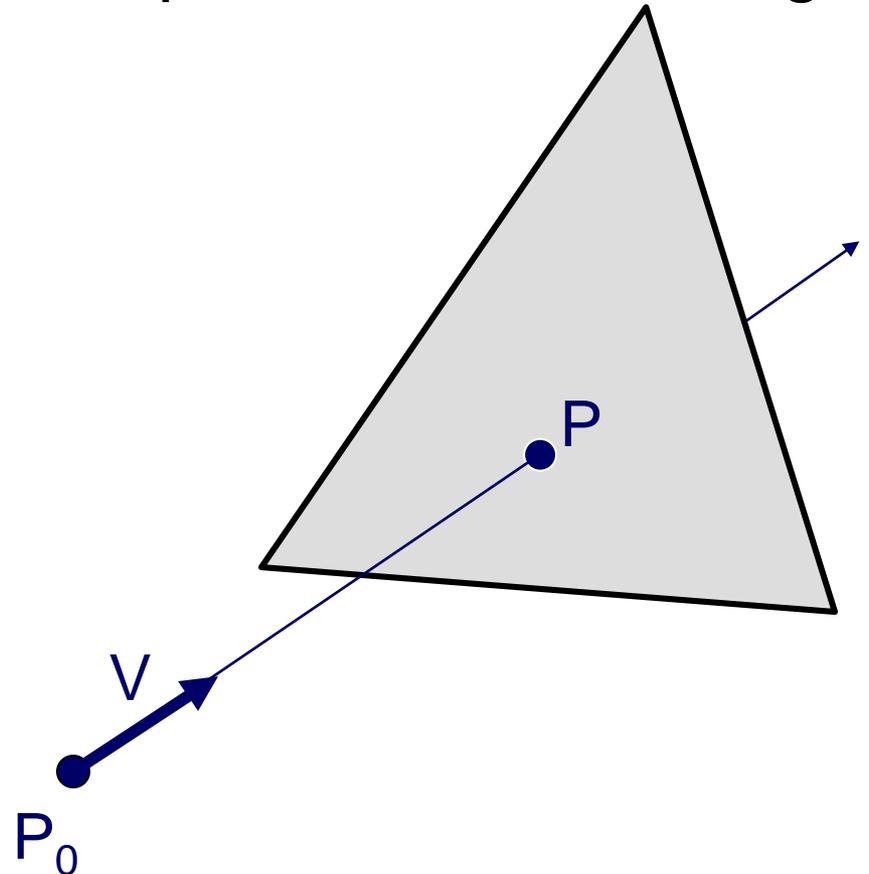
Ray-Triangle Intersection





Ray-Triangle Intersection

- First, intersect ray with plane
- Then, check if intersection point is inside triangle





Ray-Plane Intersection

$$\text{Ray: } P = P_0 + tV$$

$$\text{Plane: } P \cdot N + d = 0$$

Algebraic Method

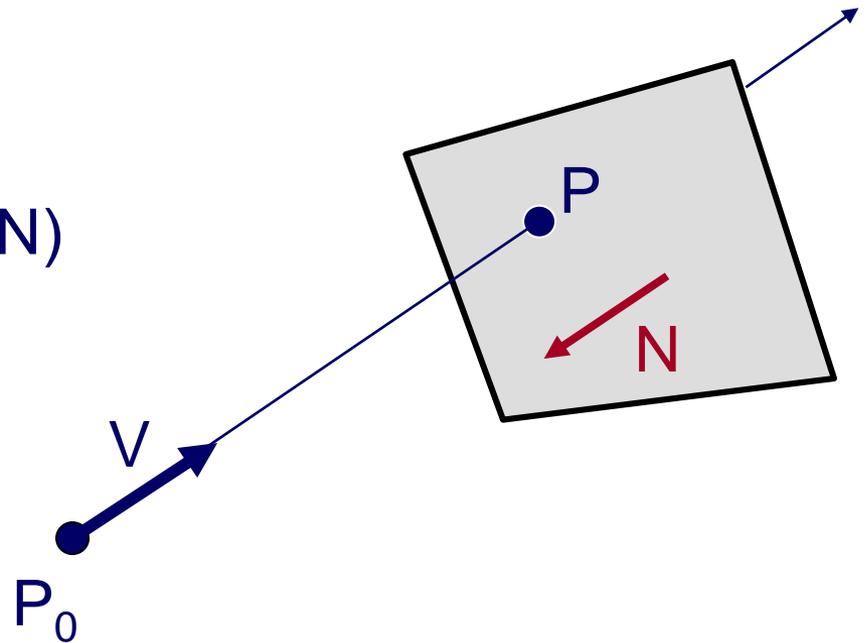
Substituting for P , we get:

$$(P_0 + tV) \cdot N + d = 0$$

Solution:

$$t = -(P_0 \cdot N + d) / (V \cdot N)$$

$$P = P_0 + tV$$





Ray-Triangle Intersection I

- Check if point is inside triangle algebraically

For each side of triangle

$$V_1 = T_1 - P_0$$

$$V_2 = T_2 - P_0$$

$$N_1 = V_2 \times V_1$$

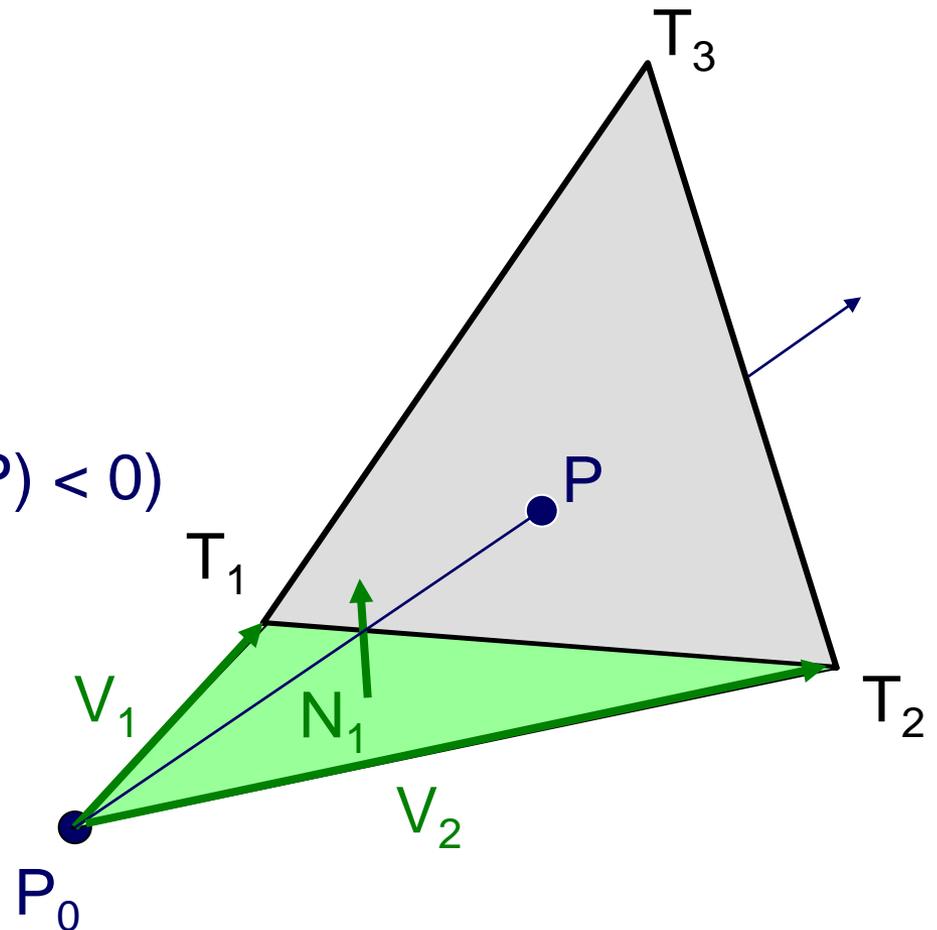
Normalize N_1

Plane $p(P_0, N_1)$

if (SignedDistance(p , P) < 0)

return FALSE;

end





Ray-Triangle Intersection II

- Check if point is inside triangle algebraically

For each side of triangle

$$V_1 = T_1 - P$$

$$V_2 = T_2 - P$$

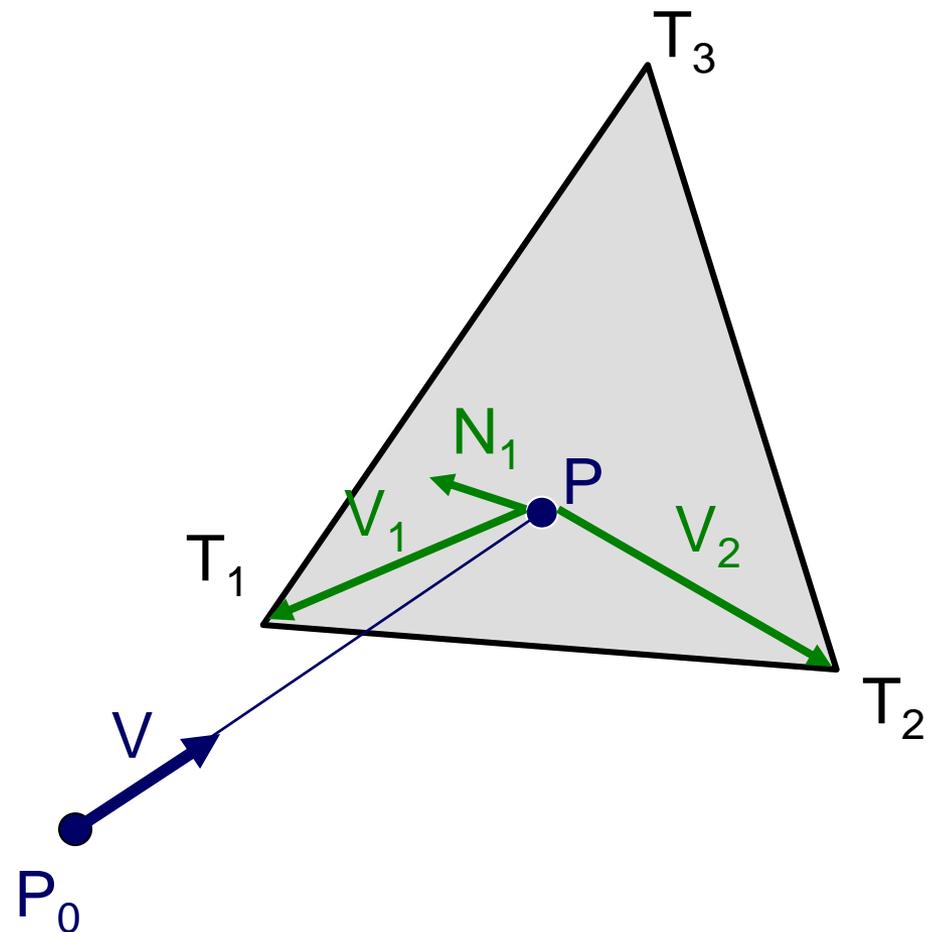
$$N_1 = V_2 \times V_1$$

Normalize N_1

if $(V \cdot N_1 < 0)$

return FALSE;

end





Ray-Triangle Intersection II

- Check if point is inside triangle algebraically

For each side of triangle

$$V_1 = T_1 - P$$

$$V_2 = T_2 - P$$

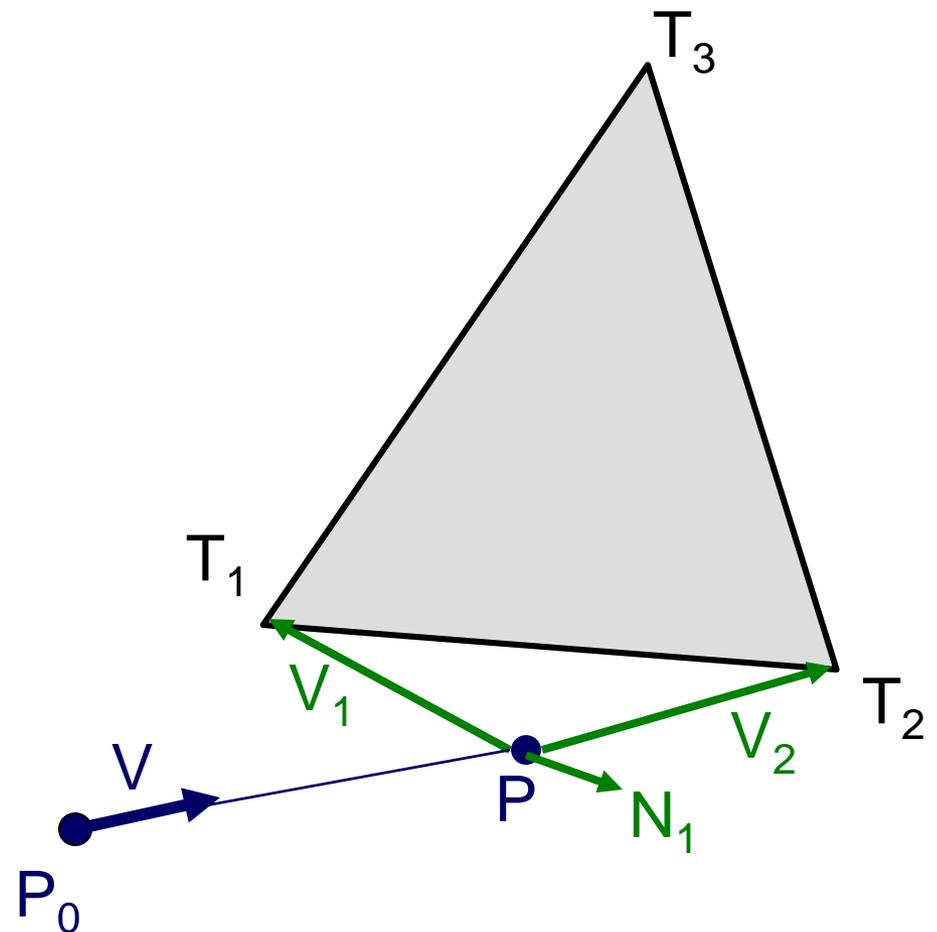
$$N_1 = V_2 \times V_1$$

Normalize N_1

if $(V \cdot N_1 < 0)$

return FALSE;

end





Ray-Triangle Intersection III

- Check if point is inside triangle parametrically

“Barycentric coordinates” α, β, γ :

$$P = \alpha T_3 + \beta T_2 + \gamma T_1$$

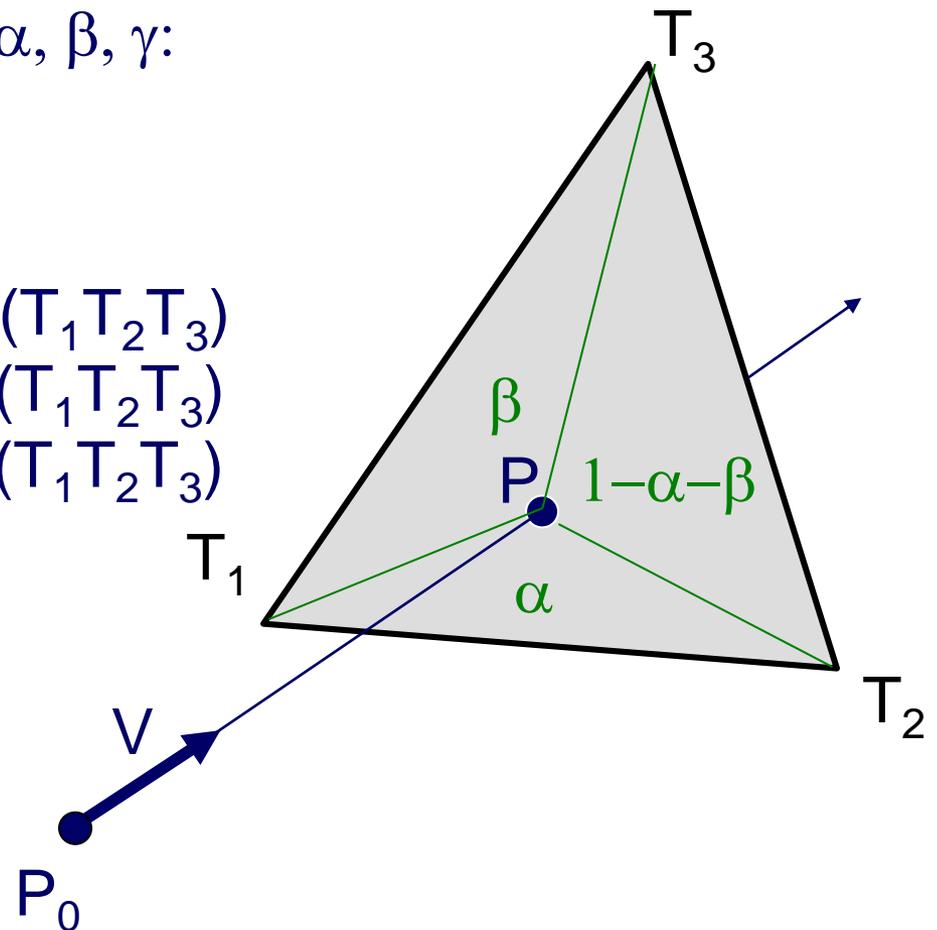
where $\alpha + \beta + \gamma = 1$

$$\alpha = \text{Area}(T_1 T_2 P) / \text{Area}(T_1 T_2 T_3)$$

$$\beta = \text{Area}(T_1 P T_3) / \text{Area}(T_1 T_2 T_3)$$

$$\gamma = \text{Area}(P T_2 T_3) / \text{Area}(T_1 T_2 T_3)$$

$$= 1 - \alpha - \beta$$





Ray-Triangle Intersection III

- Check if point is inside triangle parametrically

Compute “barycentric coordinates” α, β :

$$\alpha = \text{Area}(T_1T_2P) / \text{Area}(T_1T_2T_3)$$

$$\beta = \text{Area}(T_1PT_3) / \text{Area}(T_1T_2T_3)$$

$$\text{Area}(T_1T_2T_3) = \frac{1}{2} \|\ (T_2 - T_1) \times (T_3 - T_1) \|\$$

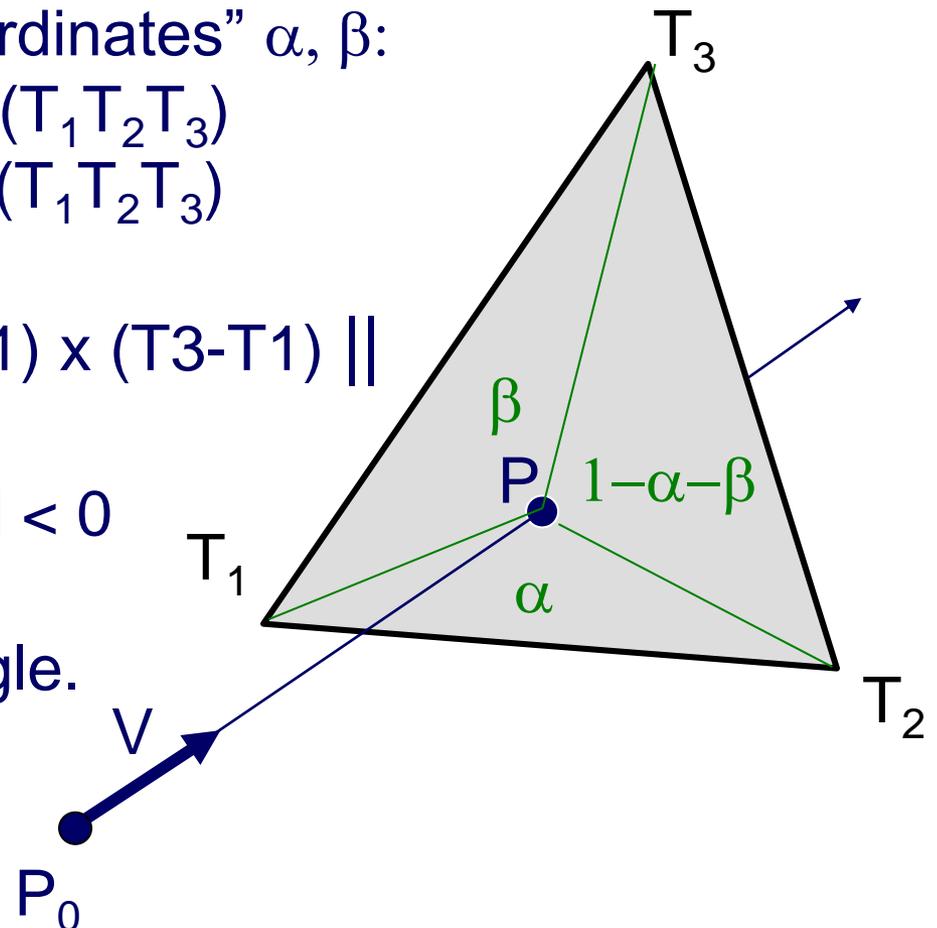
check if backfacing:

$$\left((T_2 - T_1) \times (T_3 - T_1) \right) \cdot N < 0$$

Check if point inside triangle.

$$0 \leq \alpha \leq 1 \text{ and } 0 \leq \beta \leq 1$$

$$\text{and } \alpha + \beta \leq 1$$





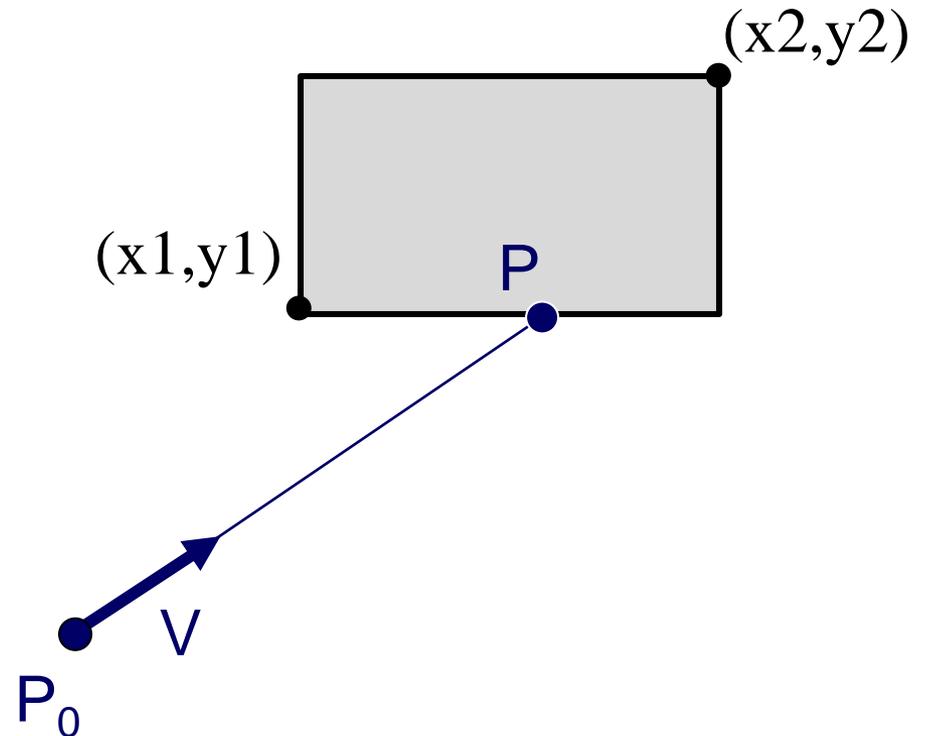
Ray Intersection

- Ray Intersection
 - Sphere
 - Triangle
 - **Box**
 - Scene
- Ray Intersection Acceleration
 - Bounding volumes
 - Uniform grids
 - Octrees
 - BSP trees



Ray-Box Intersection

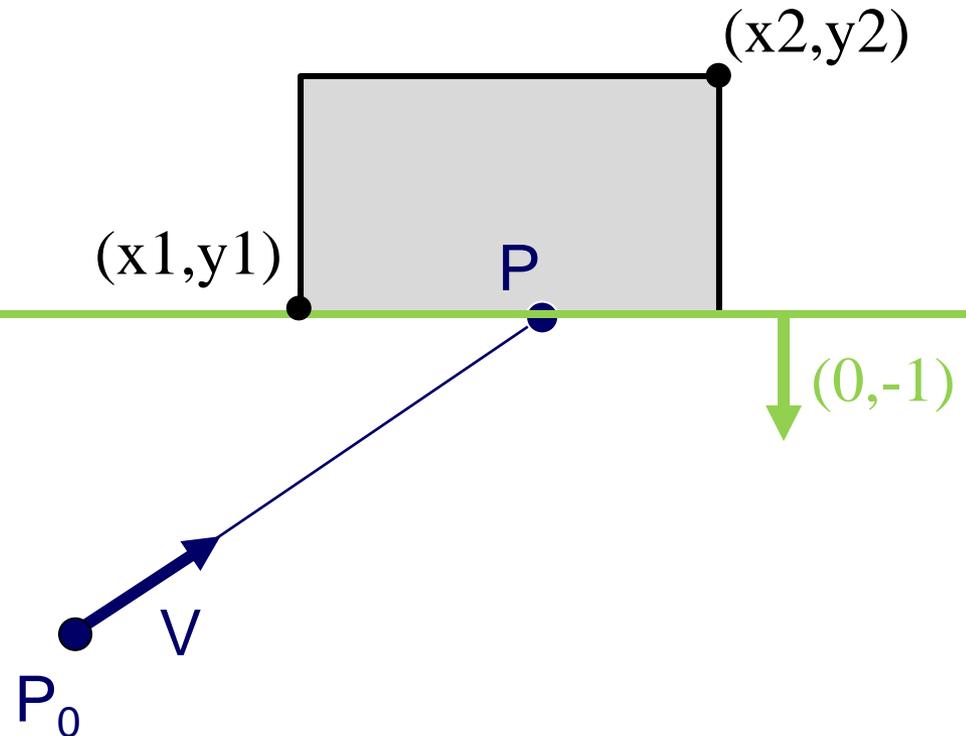
- Check front-facing sides for intersection with ray and return closest intersection (least t)





Ray-Box Intersection

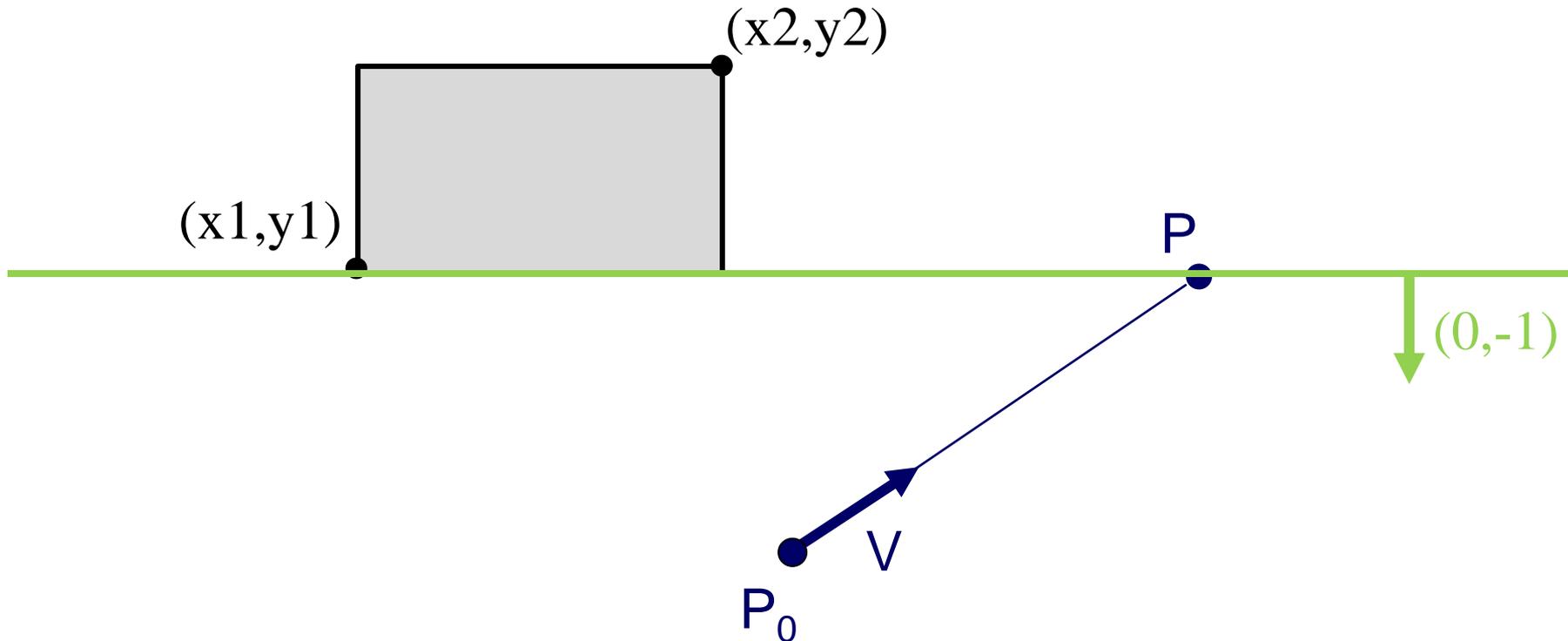
- Check front-facing sides for intersection with ray and return closest intersection (least t)
 - Find intersection with plane
 - Check if point is inside rectangle





Ray-Box Intersection

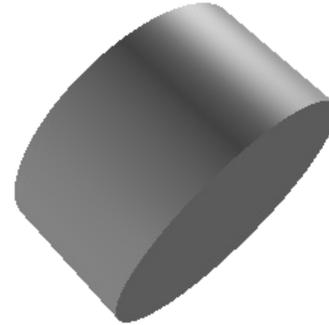
- **Check** front-facing sides for intersection with ray and return closest intersection (least t)
 - Find intersection with plane
 - Check if point is inside rectangle



Other Ray-Primitive Intersections



- Cone, cylinder:
 - Similar to sphere
 - Must also check end caps
- Convex polygon
 - Same as triangle (check point-in-polygon algebraically)
 - Or, decompose into triangles, and check all of them
- Mesh
 - Compute intersection for all polygons
 - Return closest intersection (least t)





Ray Intersection

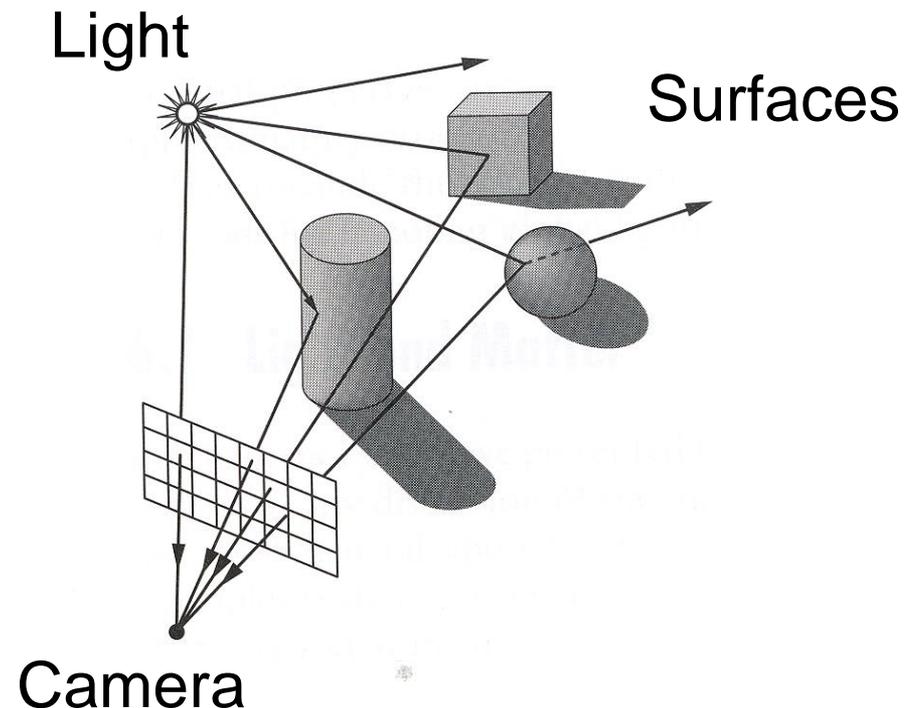
- Ray Intersection
 - Sphere
 - Triangle
 - Box
 - Scene

- Ray Intersection Acceleration
 - Bounding volumes
 - Uniform grids
 - Octrees
 - BSP trees



Ray-Scene Intersection

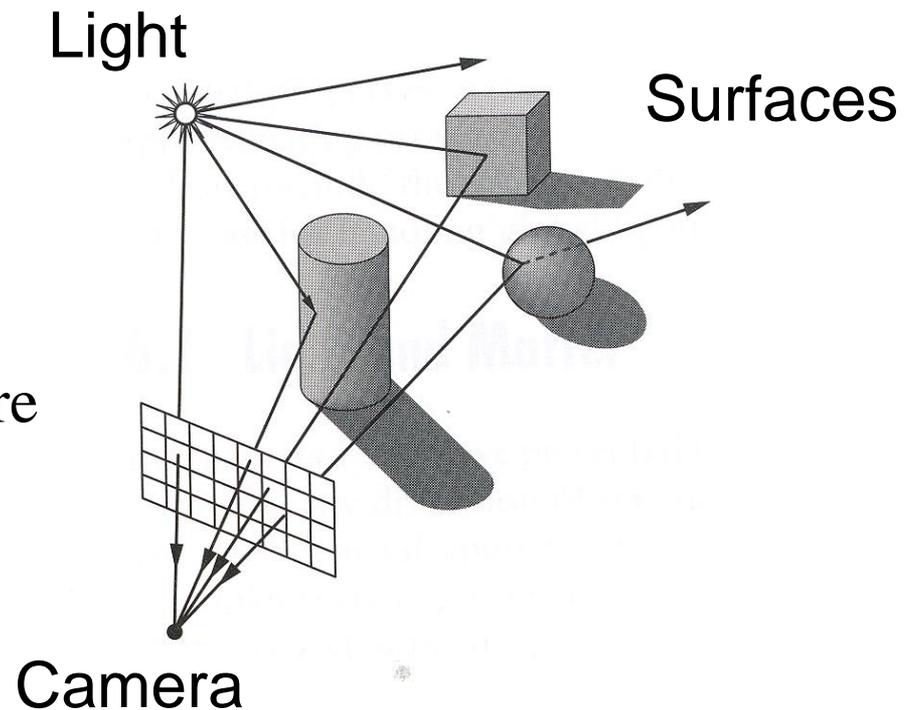
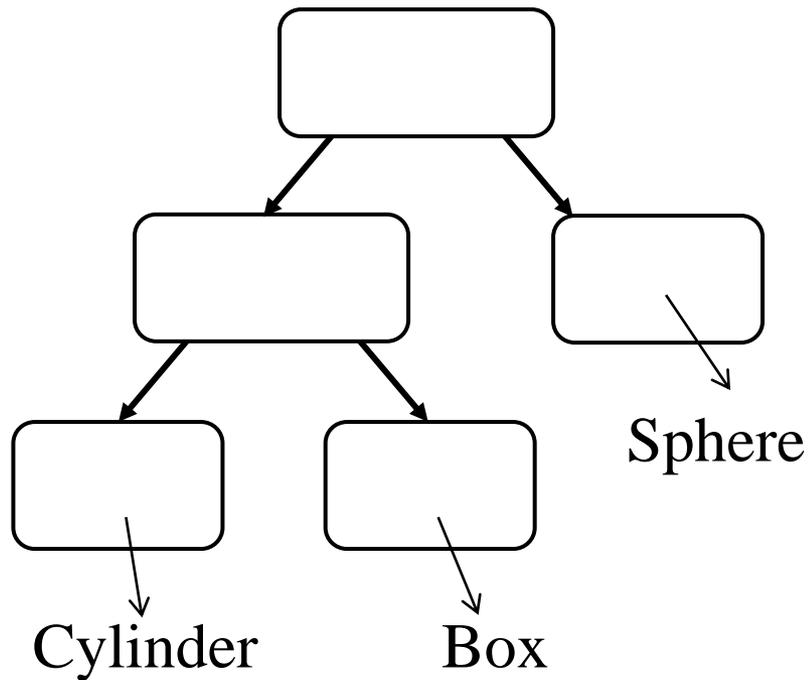
- Intuitive method
 - Compute intersection for all nodes of scene graph
 - Return closest intersection (least t)





Ray-Scene Intersection

- Scene graph is a DAG
 - Traverse with recursion



Ray-Scene Intersection I



```
R3Intersection ComputeIntersection(R3Scene *scene, R3Node *node, R3Ray *ray)
{
    // Check for intersection with shape
    shape_intersection = Intersect node's shape with ray
    if (shape_intersection is a hit) closest_intersection = shape_intersection
    else closest_intersection = infinitely far miss

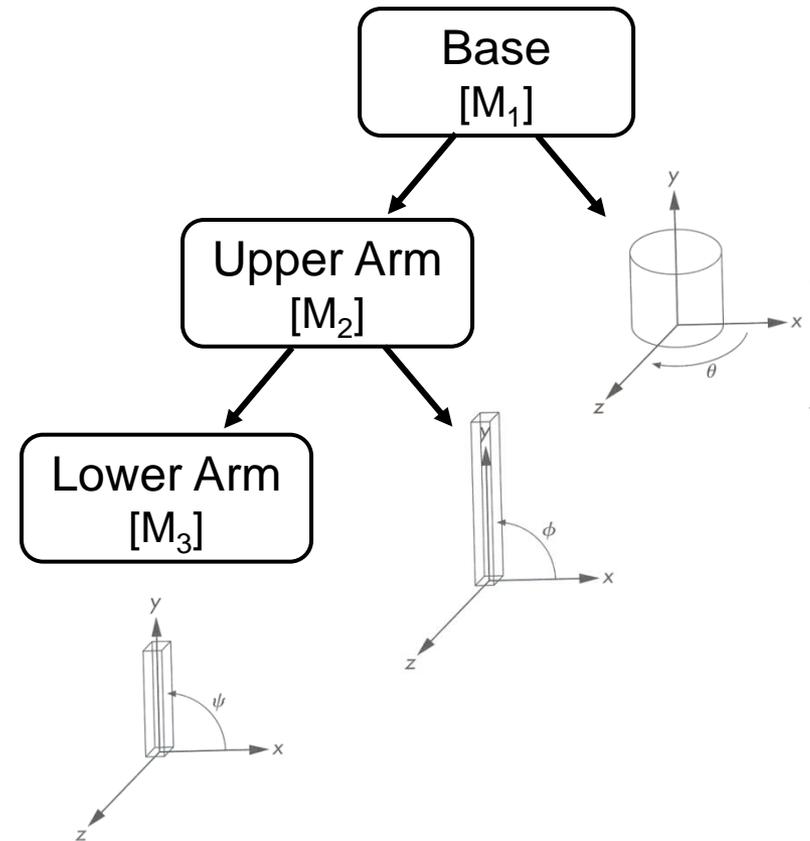
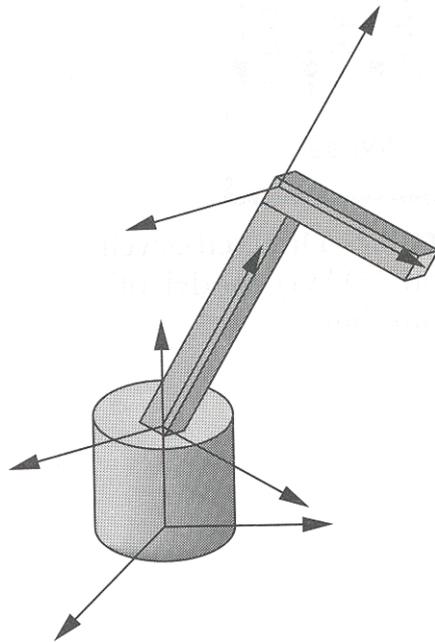
    // Check for intersection with children nodes
    for each child node
        // Check for intersection with child contents
        child_intersection = ComputeIntersection(scene, child, ray);
        if (child_intersection is a hit and is closer than closest_intersection)
            closest_intersection = child_intersection;

    // Return closest intersection in tree rooted at this node
    return closest_intersection
}
```



Ray-Scene Intersection

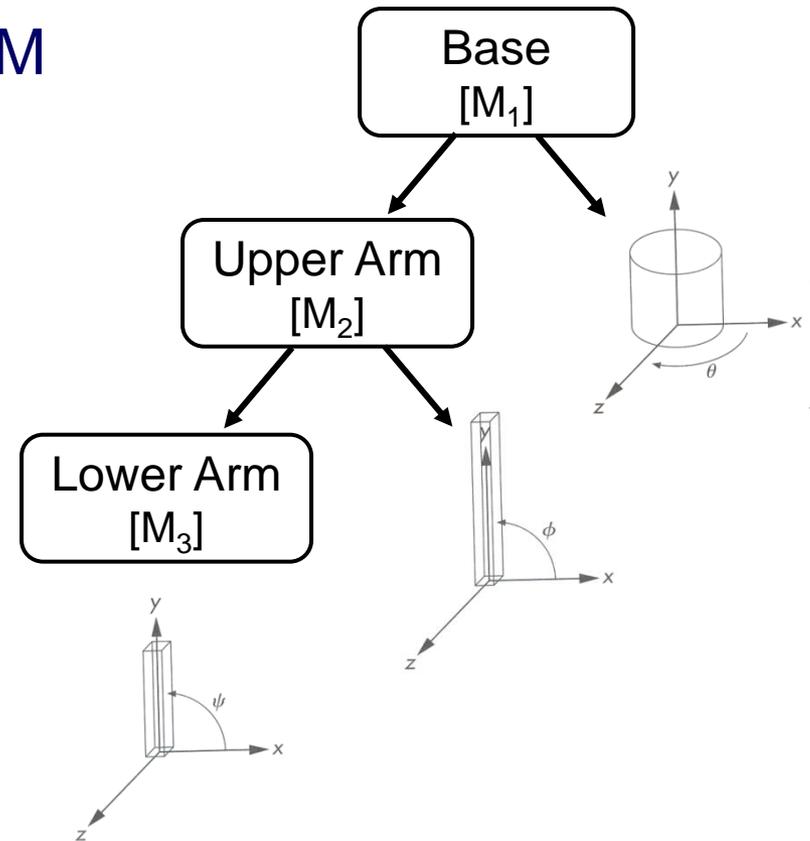
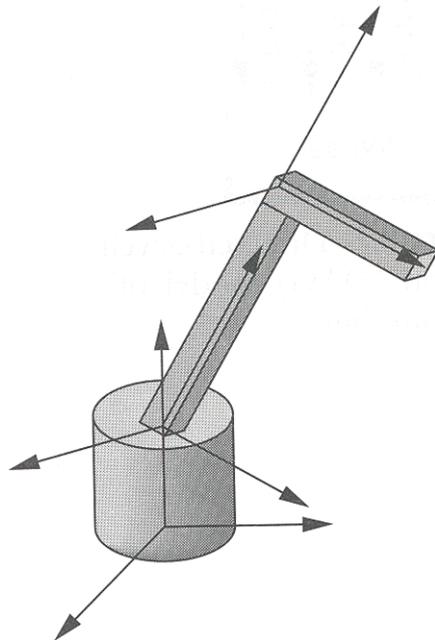
- Scene graph can have transformations





Ray-Scene Intersection

- Scene graph node can have transformations
 - Transform **ray** (not primitives) by **inverse** of M
 - Intersect in coordinate system of node
 - Transform intersection by M



Ray-Scene Intersection II



```
R3Intersection ComputeIntersection(R3Scene *scene, R3Node *node, R3Ray *ray)
{
    // Transform ray by inverse of node's transformation

    // Check for intersection with shape

    // Check for intersection with children nodes

    // Transform intersection by node's transformation

    // Return closest intersection in tree rooted at this node
}
```



Ray-Scene Intersection II

```
R3Intersection ComputeIntersection(R3Scene *scene, R3Node *node, R3Ray *ray)
{
    // Transform ray by inverse of node's transformation

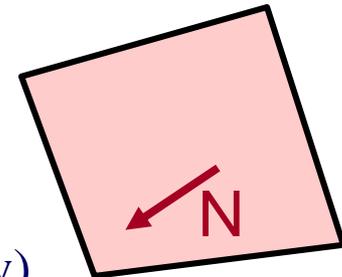
    // Check for intersection with shape

    // Check for intersection with children nodes

    // Transform intersection by node's transformation

    // Return closest intersection in tree rooted at this node
}
```

Recall: directions (including ray direction and surface normal N) must be transformed by inverse transpose of M (or M^{-1} for ray)





Ray Intersection

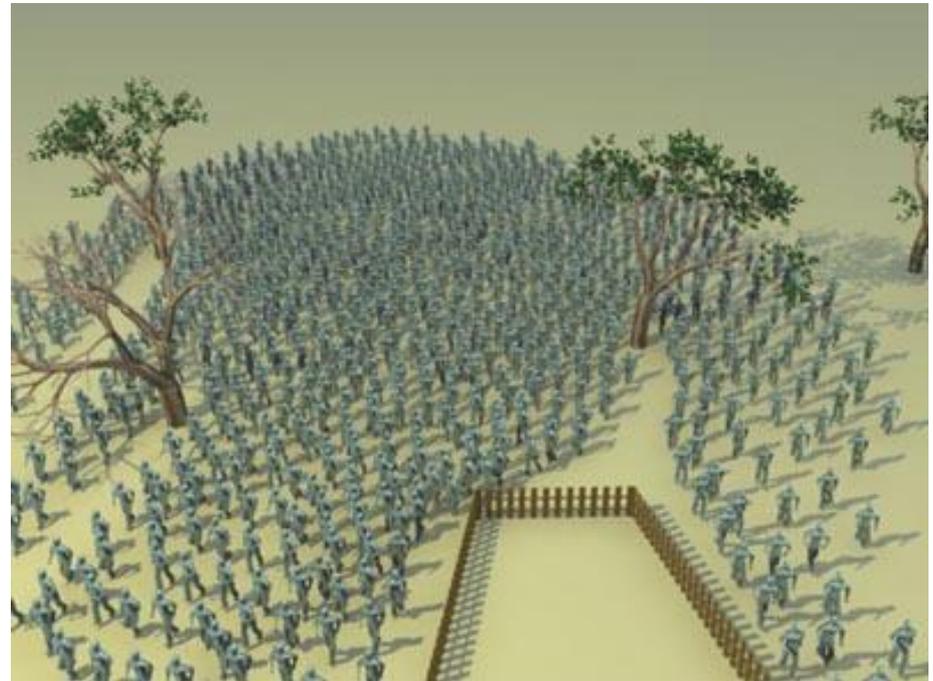
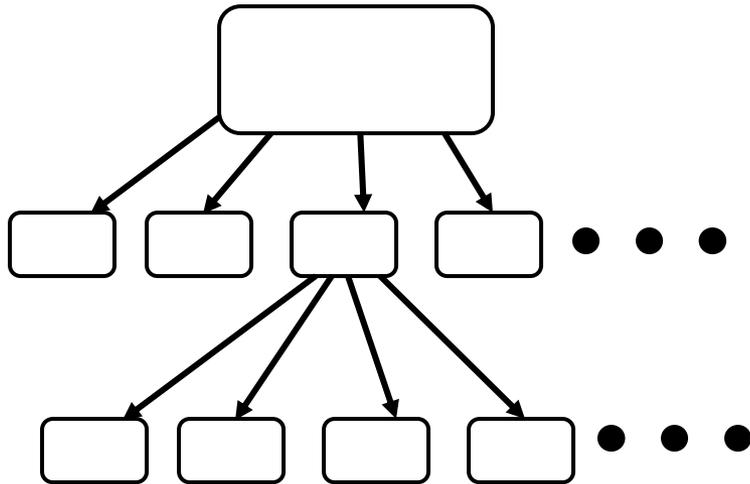
- Ray Intersection
 - Sphere
 - Triangle
 - Box
 - Scene

- Ray Intersection Acceleration
 - Bounding volumes
 - Uniform grids
 - Octrees
 - BSP trees



Ray Intersection Acceleration

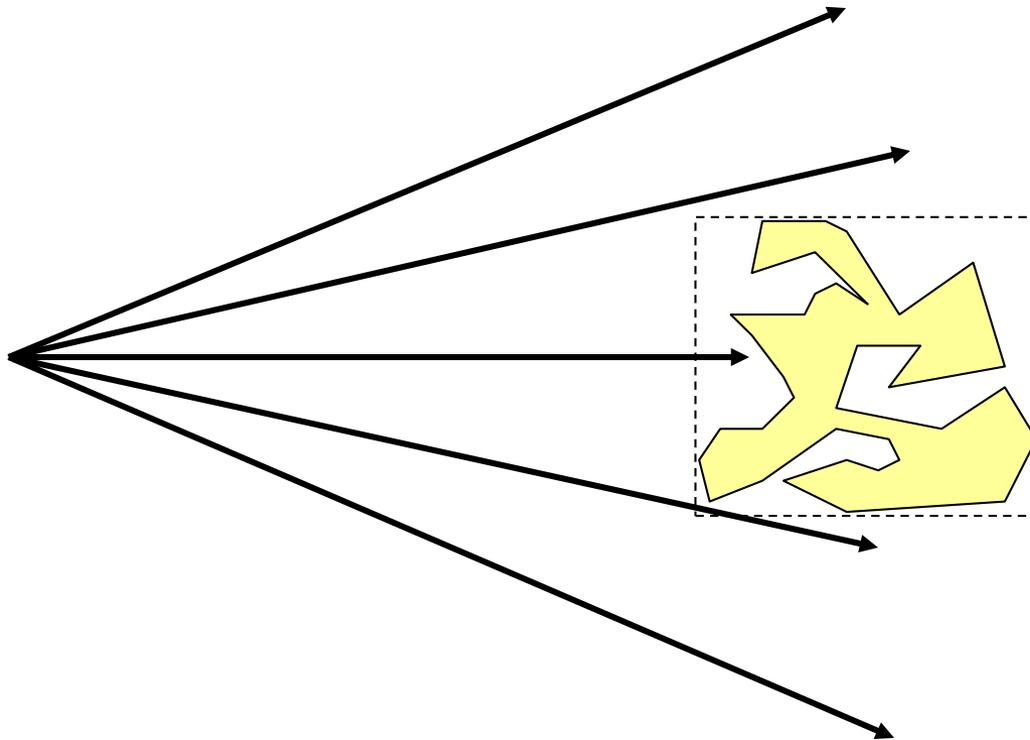
- What if there are a lot of nodes?





Bounding Volumes

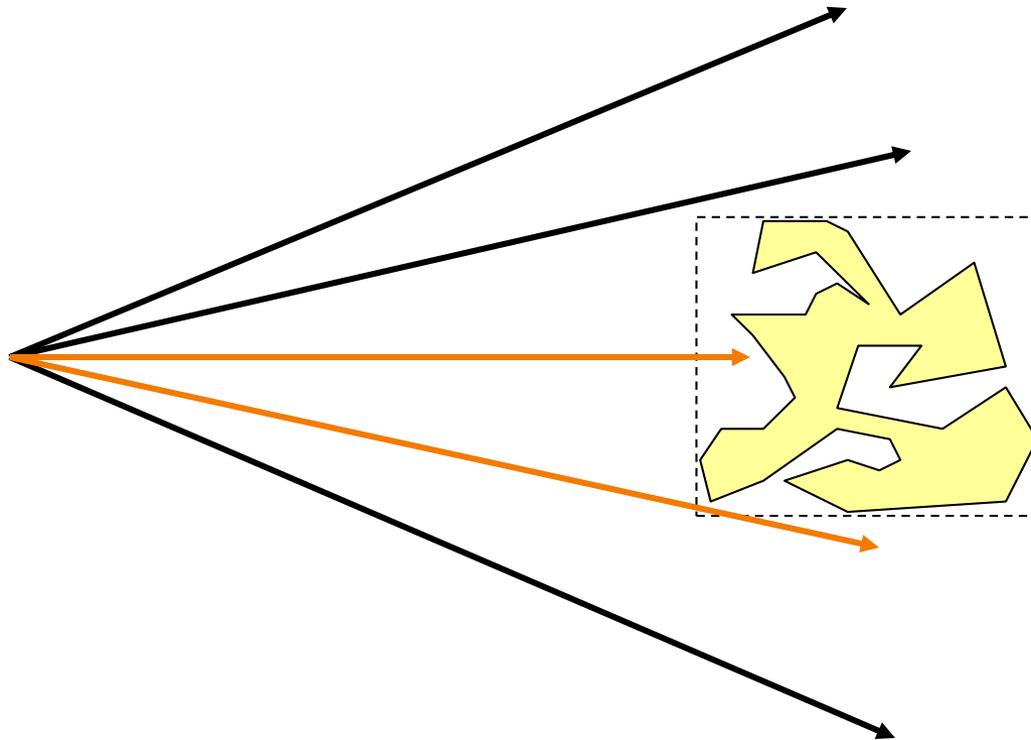
- Check for intersection with simple bounding volume first





Bounding Volumes

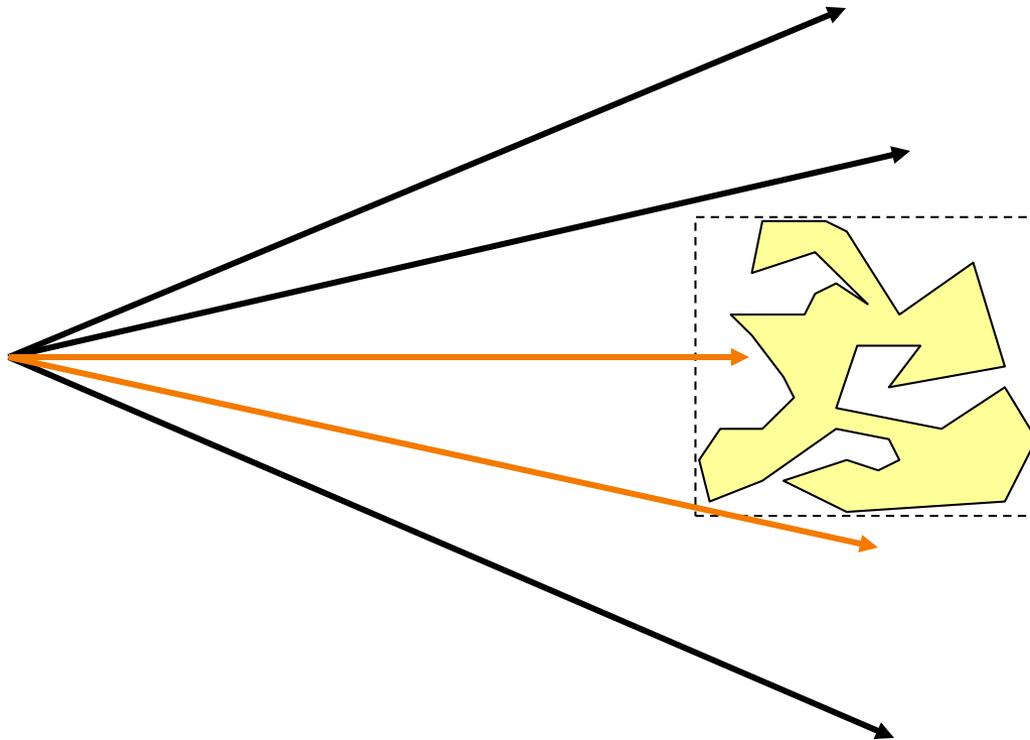
- Check for intersection with bounding volume first





Bounding Volumes

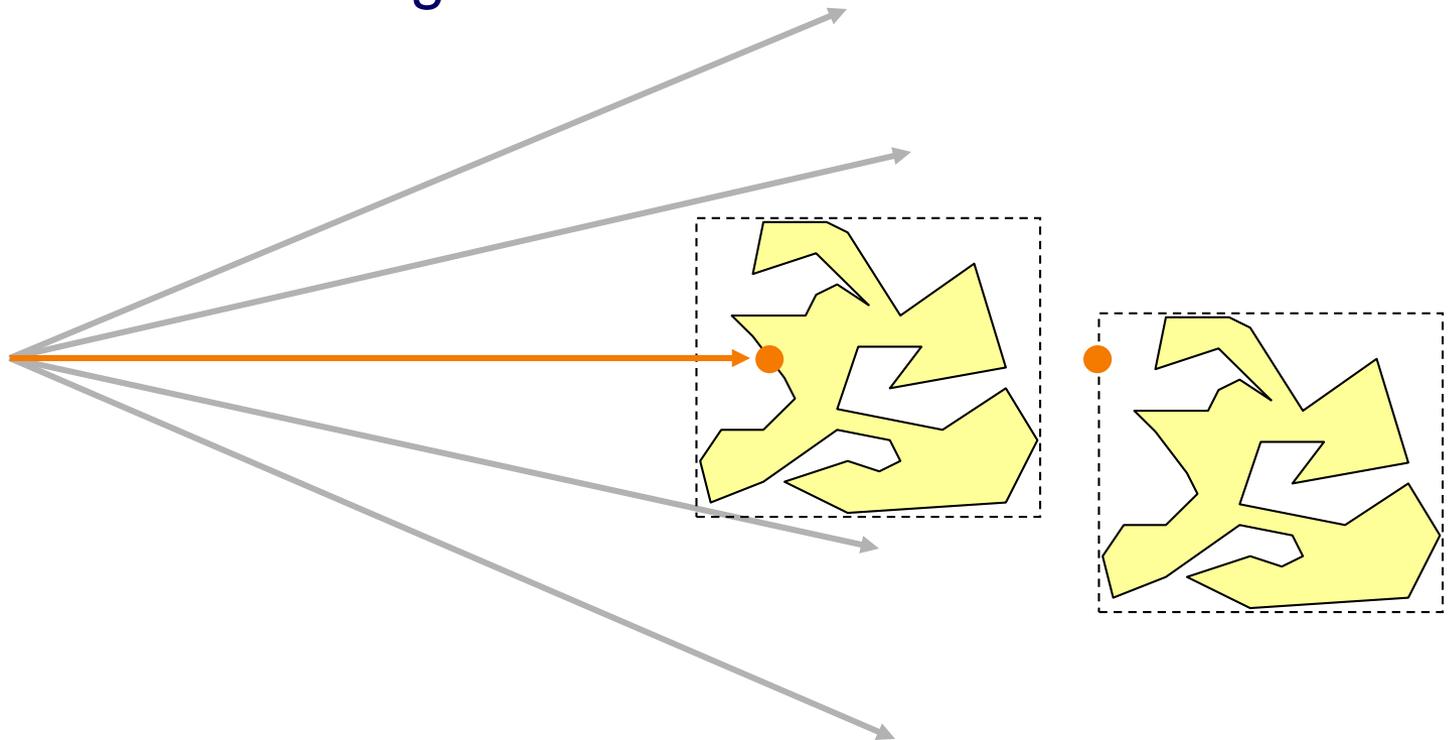
- Check for intersection with bounding volume first
 - If ray doesn't intersect bounding volume, then it can't intersect its contents





Bounding Volumes

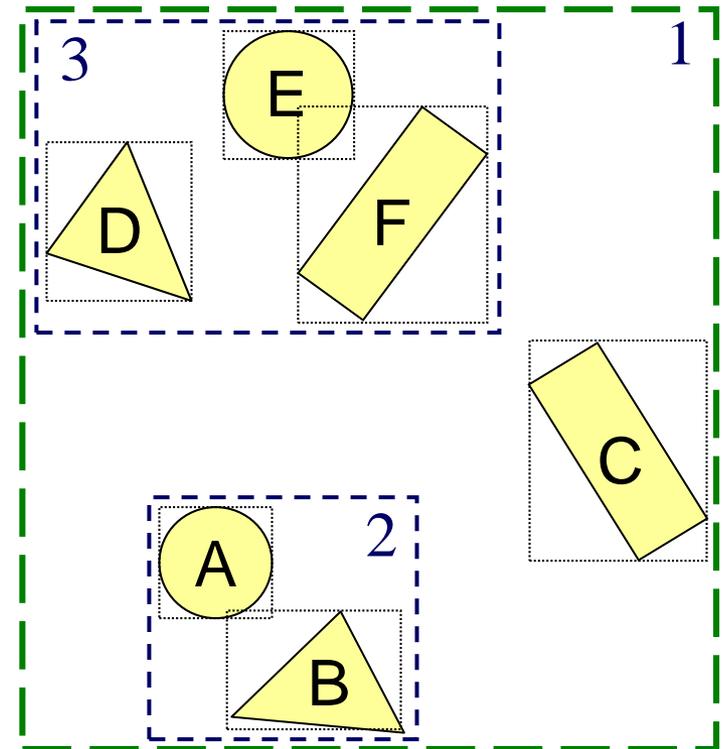
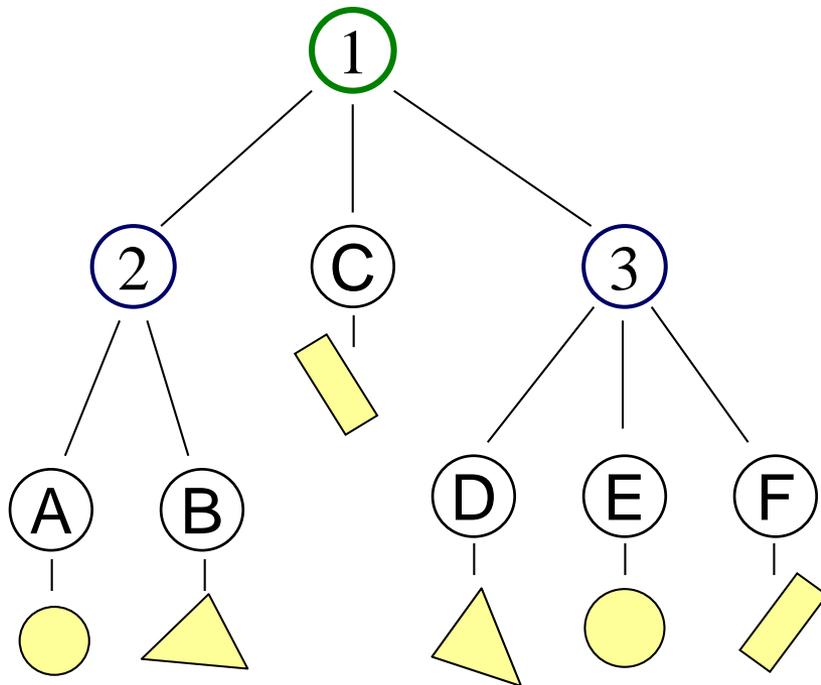
- Check for intersection with bounding volume first
 - If already found a primitive intersection closer than intersection with bounding box, then skip checking contents of bounding box





Bounding Volume Hierarchies

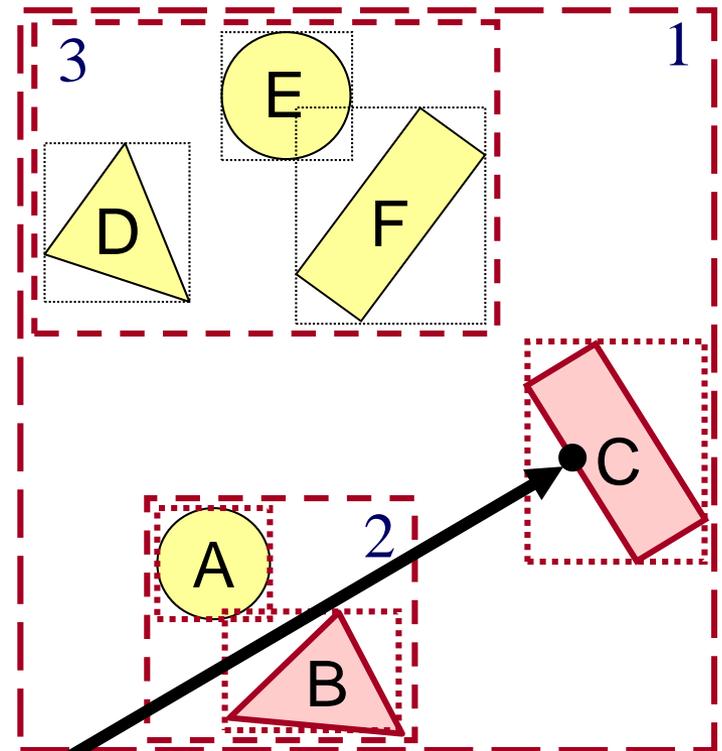
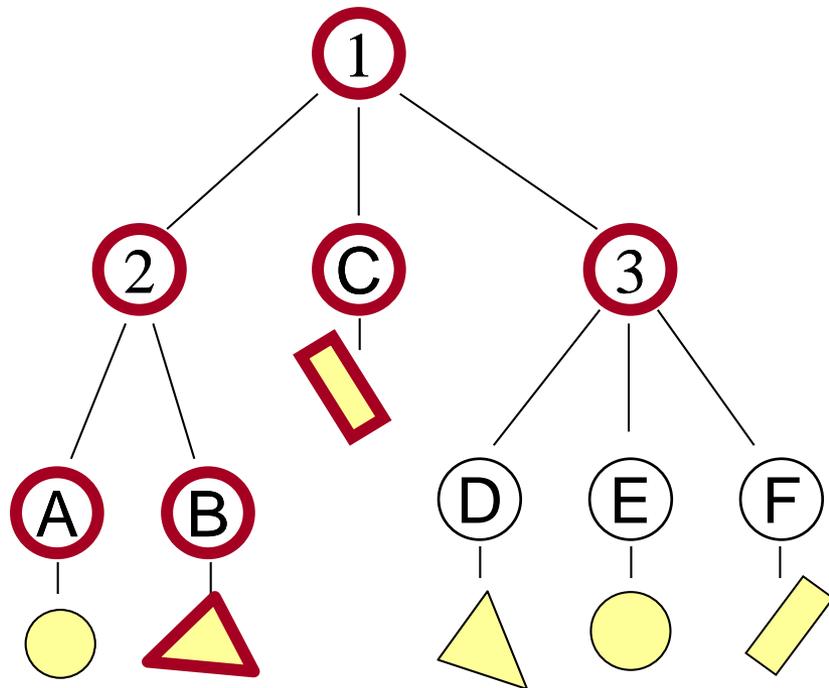
- Scene graph has hierarchy of bounding volumes
 - Bounding volume of interior node contains all children





Bounding Volume Hierarchies

- Checking bounding volumes hierarchically (within each node) can greatly accelerate ray intersection



Bounding Volume Hierarchies



```
R3Intersection ComputeIntersection(R3Scene *scene, R3Node *node, R3Ray *ray)
{
    // Transform ray by inverse of node's transformation
    // Check for intersection with shape

    // Check for intersection with children nodes
    for each child node
        // Check for intersection with child bounding box first
        bbox_intersection = Intersect child's bounding box with ray
        if (bbox_intersection is a miss or further than closest_intersection) continue

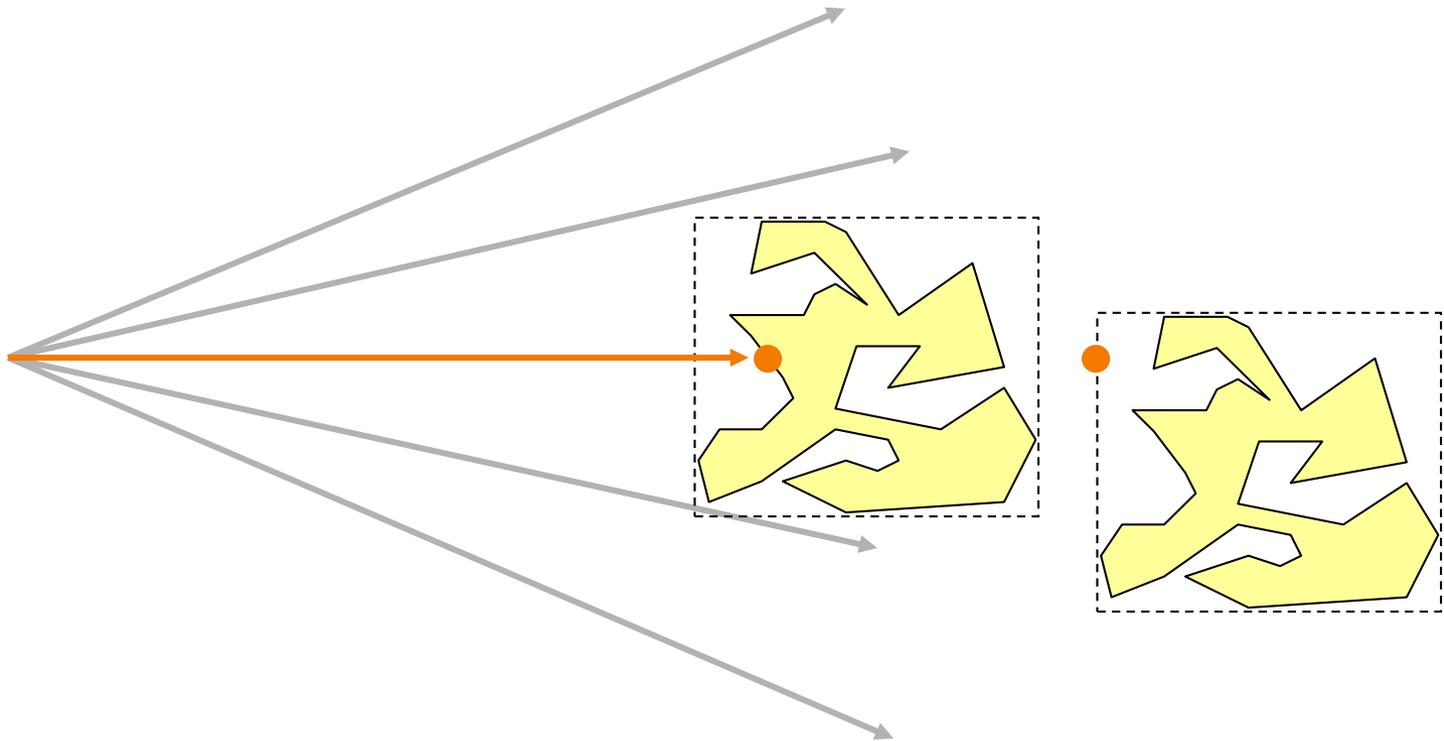
        // Check for intersection with child contents
        child_intersection = ComputeIntersection(scene, child, ray);
        if (child_intersection is a hit and is closer than closest_intersection)
            closest_intersection = child_intersection;

    // Transform intersection by node's transformation
    // Return closest intersection in tree rooted at this node
}
```

Sort Bounding Volume Intersections



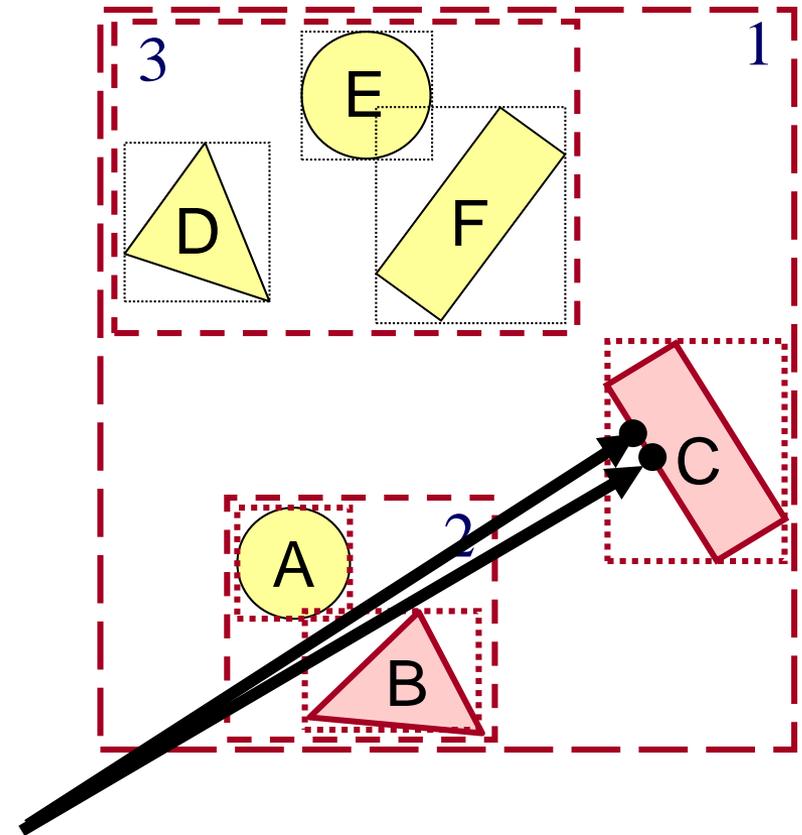
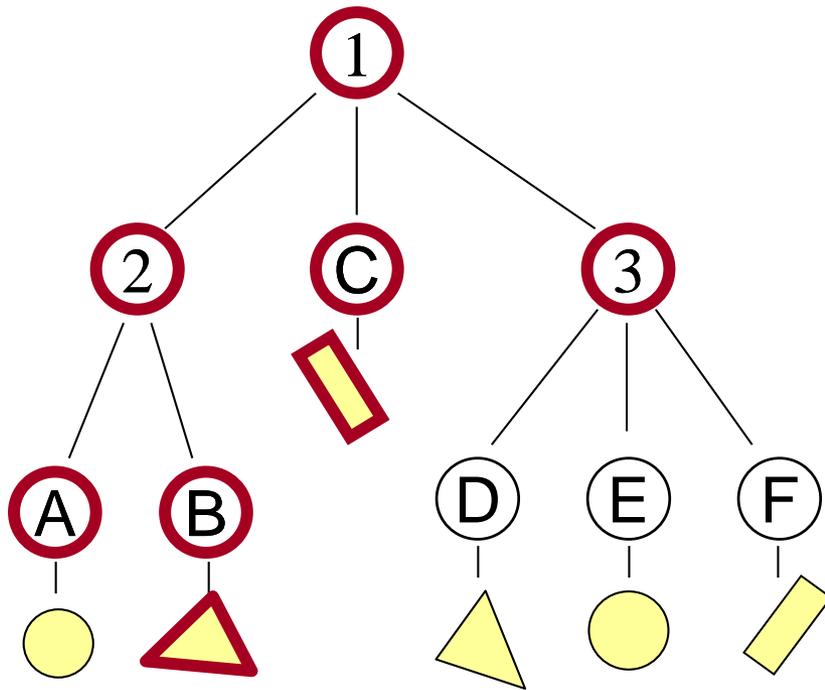
- Sort child bounding volume intersections and then visit child nodes in front-to-back order





Cache Node Intersections

- For each node, store closest child intersection from previous ray and check that node first





Ray Intersection

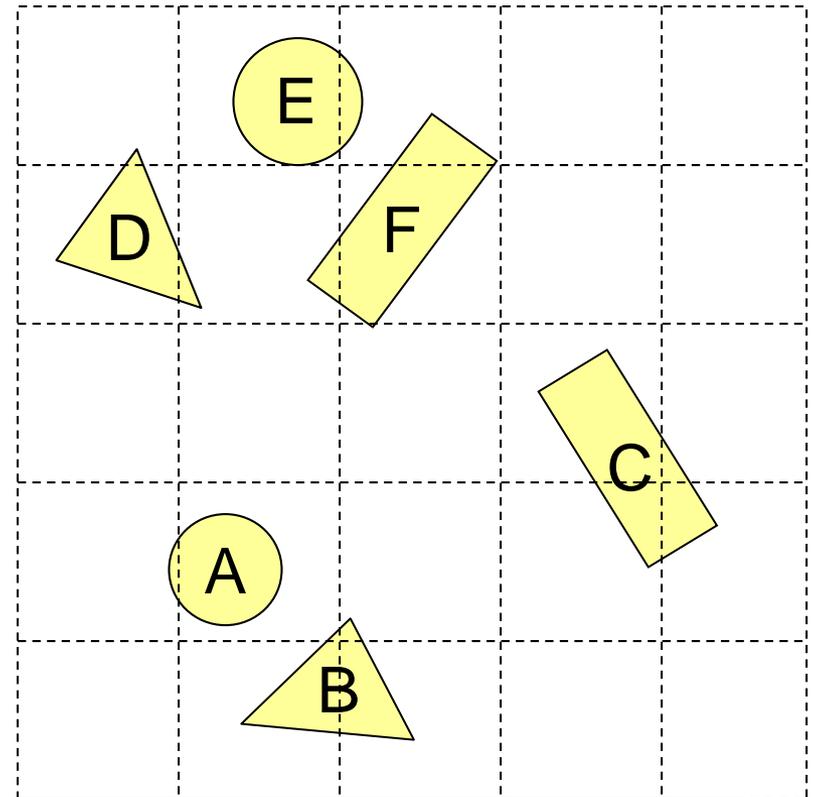
- Ray Intersection
 - Sphere
 - Triangle
 - Box
 - Scene

- Ray Intersection Acceleration
 - Bounding volumes
 - Uniform grids
 - Octrees
 - BSP trees



Uniform Grid

- Construct uniform grid over scene
 - Index primitives according to overlaps with grid cells

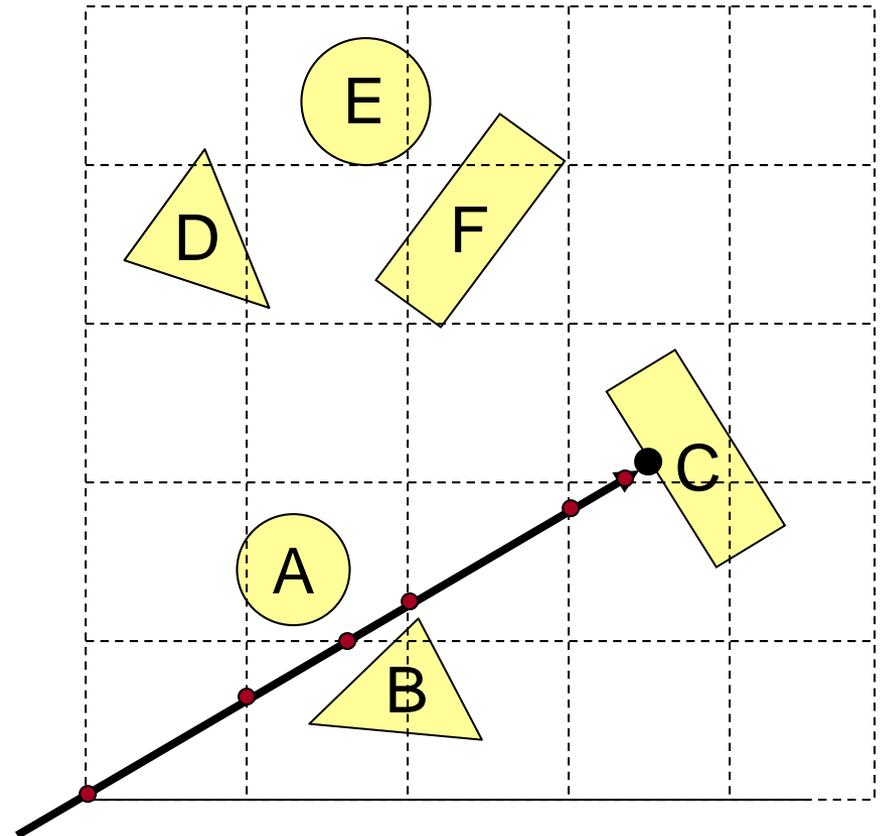




Uniform Grid

- Trace rays through grid cells
 - Fast
 - Incremental

Only check primitives in intersected grid cells



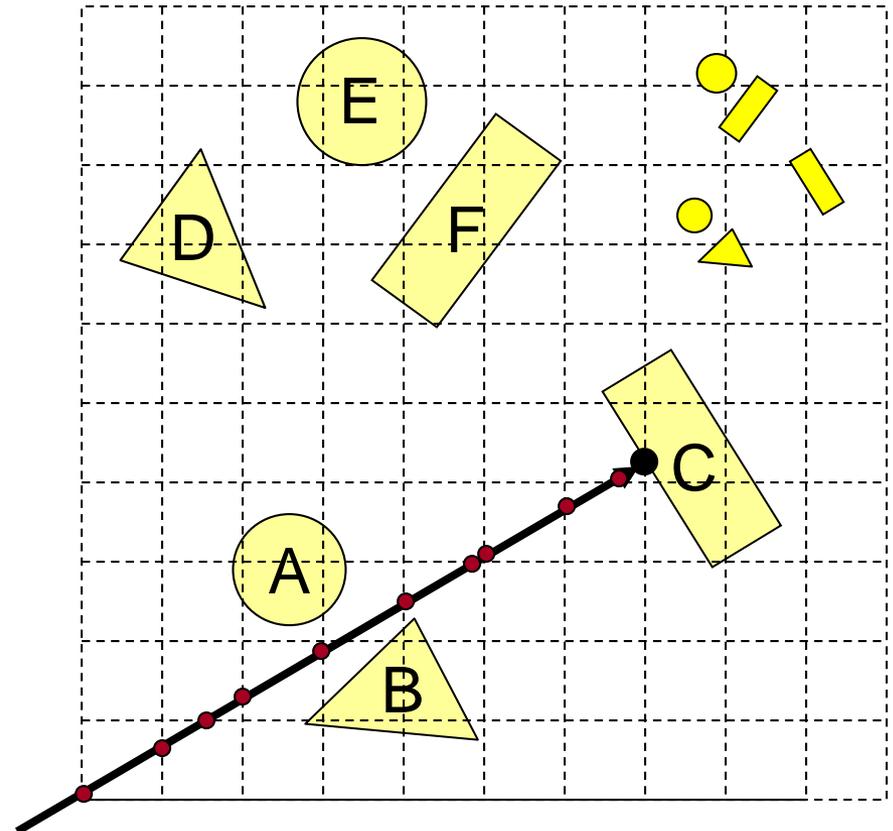


Uniform Grid

- Potential problem:
 - How choose suitable grid resolution?

Too little benefit
if grid is too coarse

Too much cost
if grid is too fine





Ray Intersection

- Ray Intersection
 - Sphere
 - Triangle
 - Box
 - Scene

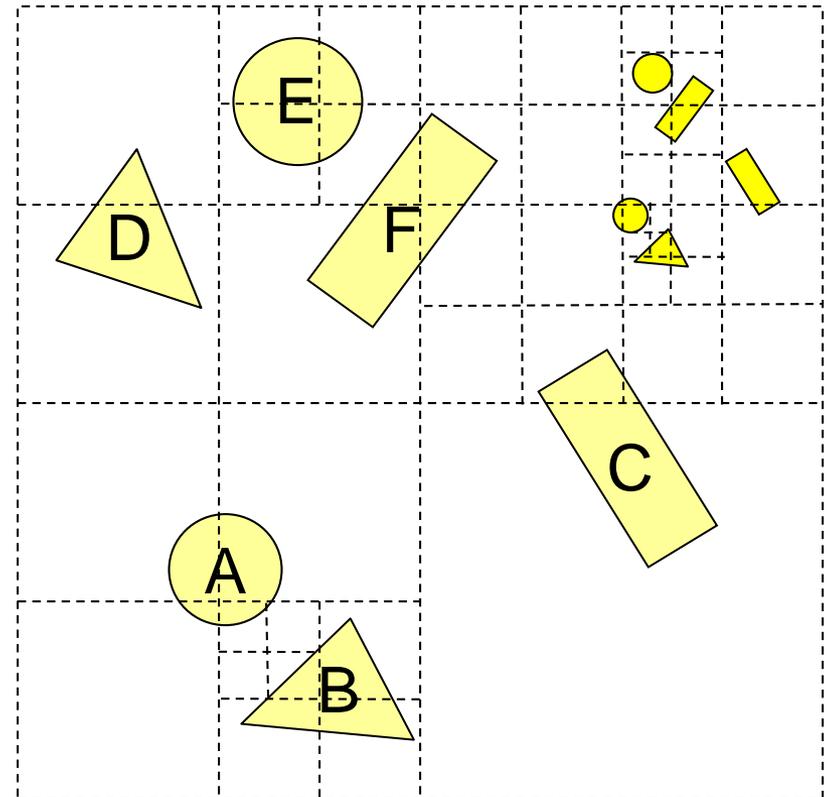
- Ray Intersection Acceleration
 - Bounding volumes
 - Uniform grids
 - Octrees
 - BSP trees



Octree

- Construct adaptive grid over scene
 - Recursively subdivide box-shaped cells into 8 octants
 - Index primitives by overlaps with cells

Generally fewer cells

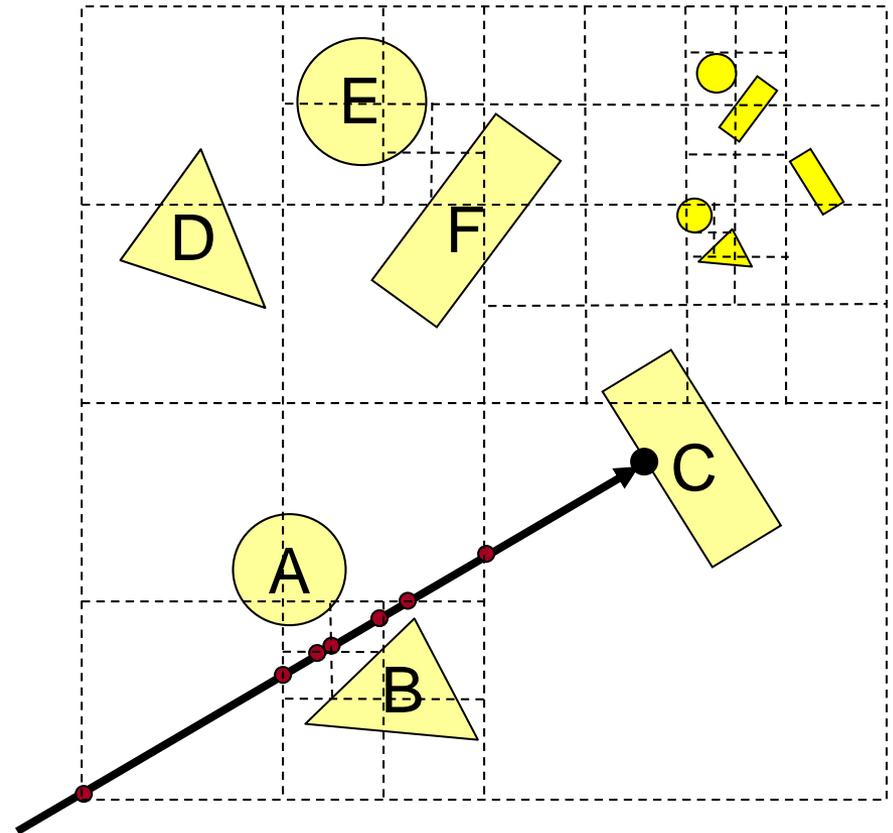




Octree

- Trace rays through neighbor cells
 - Fewer cells

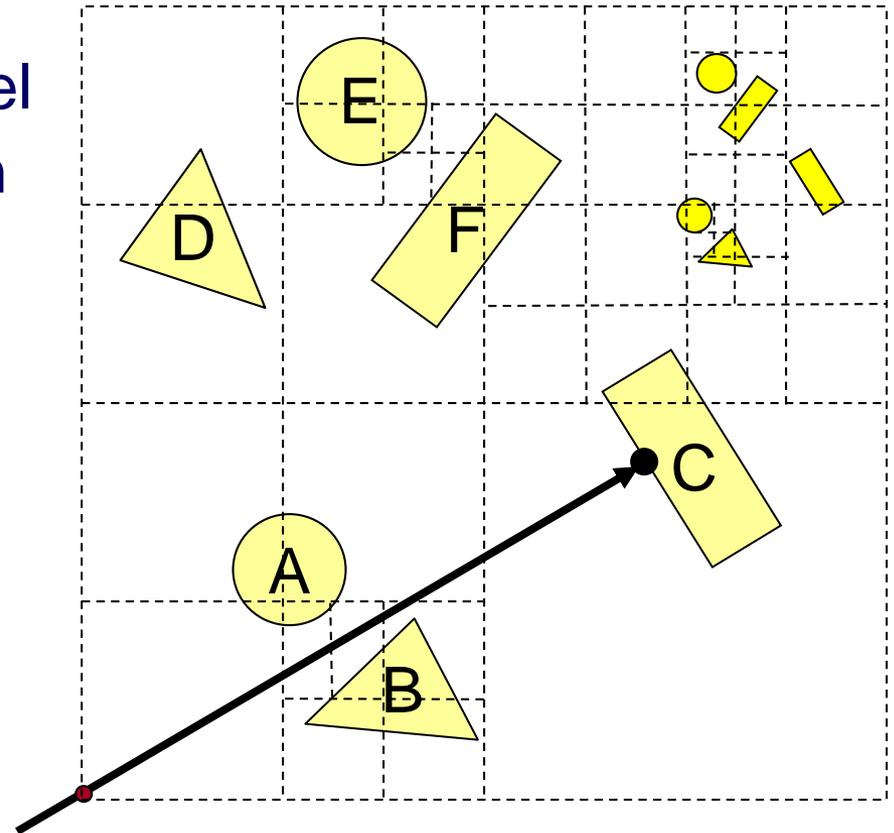
Trade-off fewer cells for more expensive traversal





Octree

- Or, check rays versus octree boxes hierarchically
 - Computing octree boxes while descending tree
 - Sort eight boxes front-to-back at each level
 - Check primitives/children inside box





Ray Intersection

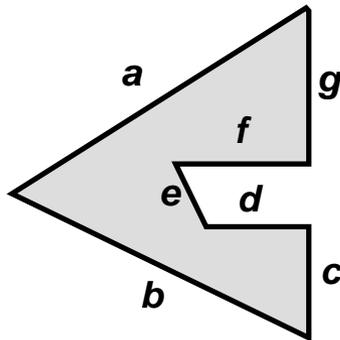
- Ray Intersection
 - Sphere
 - Triangle
 - Box
 - Scene

- Ray Intersection Acceleration
 - Bounding volumes
 - Uniform grids
 - Octrees
 - **BSP trees**

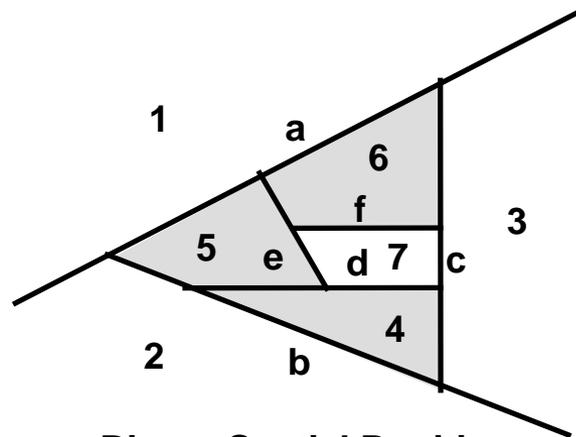


Binary Space Partition (BSP) Tree

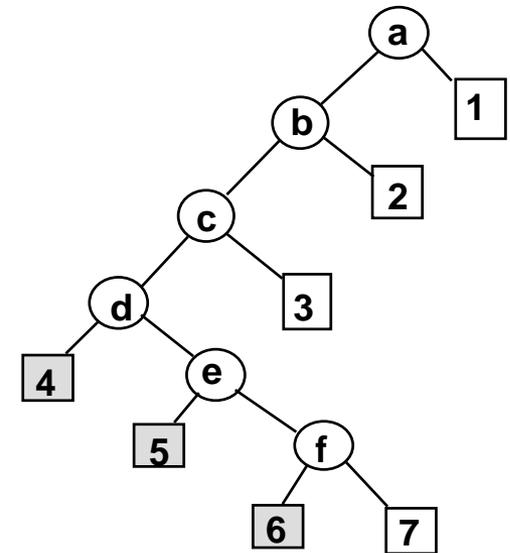
- Recursively partition space by planes
 - BSP tree nodes store partition plane and set of polygons lying on that partition plane
 - Every part of every polygon lies on a partition plane



Object



Binary Spatial Partition

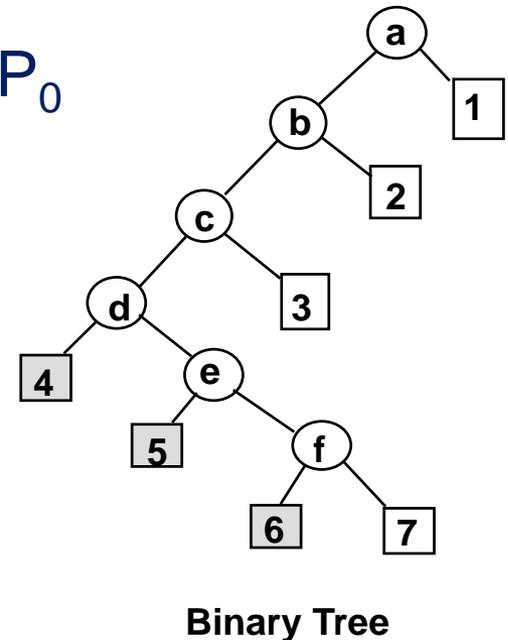
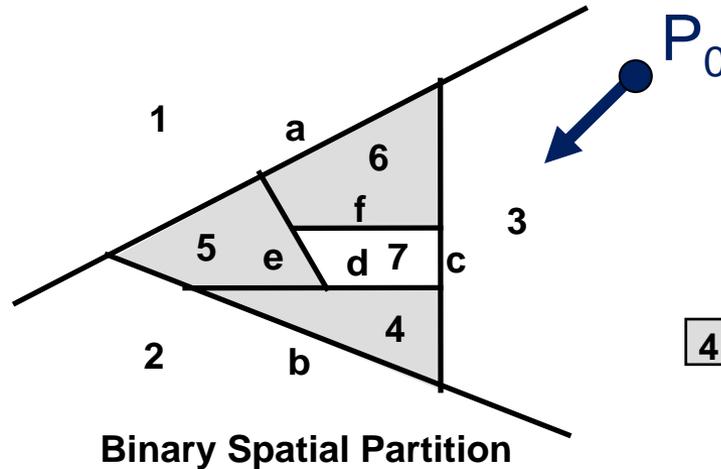
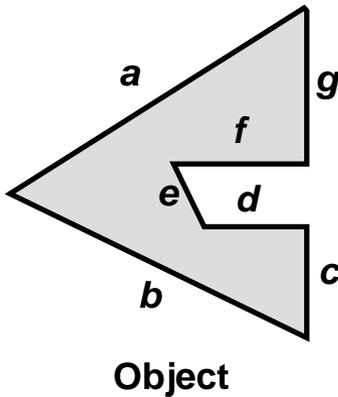


Binary Tree



Binary Space Partition (BSP) Tree

- Traverse nodes of BSP tree front-to-back
 - Visit halfspace (child node) containing P_0
 - Intersect polygons lying on partition plane
 - Visit halfspace (other child node) not containing P_0



Binary Space Partition (BSP) Tree



R3Intersection

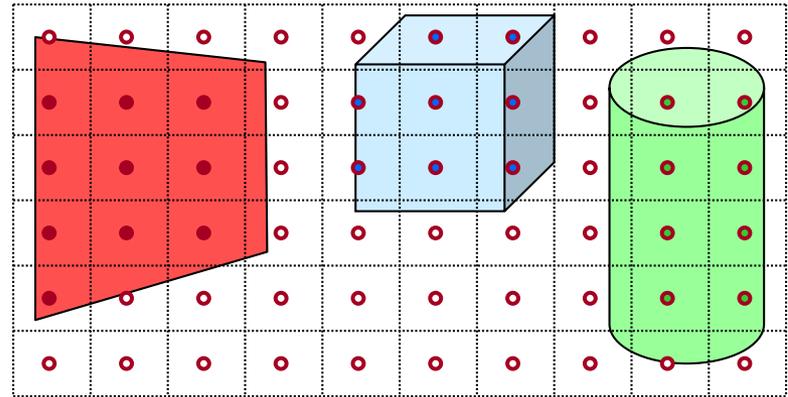
```
ComputeBSPIntersection(R3Ray *ray, BspNode *node, double min_t, double max_t)
{
    // Compute parametric value of ray-plane intersection
    t = ray parameter for intersection with split plane of node
    if (t < min_t) || (t < max_t) return no_intersection;

    // Compute side of partition plane that contains ray start point
    int side = (SignedDistance(node->plane, ray.Start()) < 0) ? 0 : 1;
    intersection1 = ComputeBSPIntersection(ray, node->child[side], min_t, t);
    if (intersection1 is a hit) return intersection1;
    intersection2 = ComputePolygonsIntersection(ray, node->polygons);
    if (intersection2 is a hit) return intersection2;
    intersection3 = ComputeBSPIntersection(ray, node->child[1-side], t, max_t);
    return intersection 3;
}
```



Other Accelerations

- Screen space coherence – check > 1 ray at once
 - Beam tracing
 - Pencil tracing
 - Cone tracing
- Memory coherence
 - Large scenes
- Parallelism
 - Ray casting is “embarrassingly parallelizable”
- etc.





Acceleration

- Intersection acceleration techniques are important
 - Bounding volume hierarchies
 - Spatial partitions
- General concepts
 - Sort objects spatially
 - Make trivial rejections quick
 - Perform checks hierarchically
 - Utilize coherence when possible

Expected time is sub-linear in number of primitives

Summary



- Writing a simple ray casting renderer is easy
 - Generate rays
 - Intersection tests
 - Lighting calculations

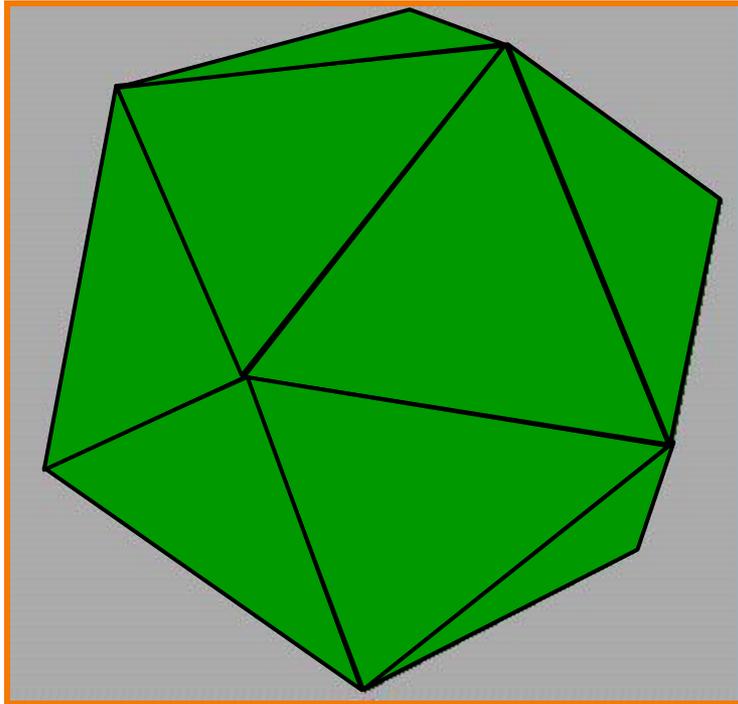
```
R2Image *RayCast(R3Scene *scene, int width, int height)
{
    R2Image *image = new R2Image(width, height);
    for (int i = 0; i < width; i++) {
        for (int j = 0; j < height; j++) {
            R3Ray ray = ConstructRayThroughPixel(scene->camera, i, j);
            R3Rgb radiance = ComputeRadiance(scene, &ray);
            image->SetPixel(i, j, radiance);
        }
    }
    return image;
}
```



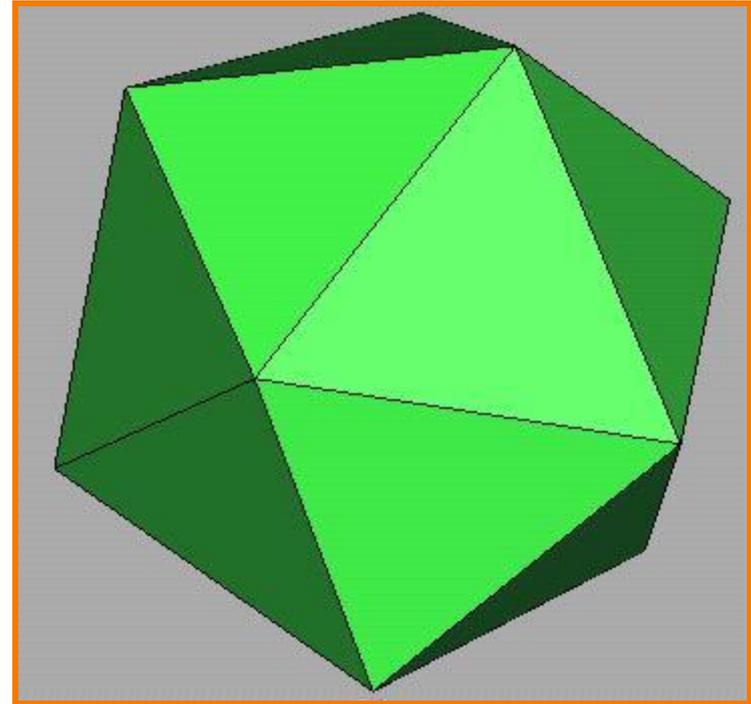
Heckbert's Business Card Ray Tracer

- ```
typedef struct{double x,y,z}vec;vec U,black,amb={.02,.02,.02};struct sphere{ vec cen,color;
double rad,kd,ks,kt,kl,ir}*s,*best,sph[]={0.,6.,.5,1.,1.,1.,.9, .05,.2,.85,0.,1.7,-1.,8.,-.5,1.,.5,.2,1.,
.7,.3,0.,.05,1.2,1.,8.,-.5,1.,.8,.8, 1.,.3,.7,0.,0.,1.2,3.,-6.,15.,1.,.8,1.,7.,0.,0.,0.,.6,1.5,-3.,-3.,12.,
.8,1., 1.,5.,0.,0.,0.,.5,1.5,};yx;double u,b,tmin,sqrt(),tan();double vdot(A,B)vec A ,B;{return A.x
*B.x+A.y*B.y+A.z*B.z;}vec vcomb(a,A,B)double a;vec A,B;{B.x+=a* A.x;B.y+=a*A.y;B.z+=a*A.z;
return B;}vec vunit(A)vec A;{return vcomb(1./sqrt(vdot(A,A)),A,black);}struct sphere*intersect
(P,D)vec P,D;{best=0;tmin=1e30;s= sph+5;while(s-->sph)b=vdot(D,U=vcomb(-1.,P,s->cen)),
u=b*b-vdot(U,U)+s->rad*s ->rad,u=u>0?sqrt(u):1e31,u=b-u>1e-7?b-u:b+u,tmin=u>=1e-7&&
u<tmin?best=s,u: tmin;return best;}vec trace(level,P,D)vec P,D;{double d,eta,e;vec N,color;
struct sphere*s,*l;if(!level--)return black;if(s=intersect(P,D));else return amb;color=amb;eta=
s->ir;d= -vdot(D,N=vunit(vcomb(-1.,P=vcomb(tmin,D,P),s->cen)));if(d<0)N=vcomb(-1.,N,black),
eta=1/eta,d= -d;l=sph+5;while(l-->sph)if((e=l ->kl*vdot(N,U=vunit(vcomb(-1.,P,l->cen))))>0&&
intersect(P,U)==l)color=vcomb(e ,l->color,color);U=s->color;color.x*=U.x;color.y*=U.y;color.z
=U.z;e=1-eta eta*(1-d*d);return vcomb(s->kt,e>0?trace(level,P,vcomb(eta,D,vcomb(eta*d-
sqrt(e),N,black)):black,vcomb(s->ks,trace(level,P,vcomb(2*d,N,D)),vcomb(s->kd, color,vcomb
(s->kl,U,black))));}main(){printf("%d %d\n",32,32);while(yx<32*32) U.x=yx%32-32/2,U.z=32/2-
yx++/32,U.y=32/2/tan(25/114.5915590261),U=vcomb(255., trace(3,black,vunit(U)),black),printf
("%%.0f %.0f %.0f\n",U);}/*minray!*/
```

# Next Time is Illumination!



Without Illumination



With Illumination