

Introducing Assignment 2: Mesh Processing & Half Edges

COS 426: Computer Graphics (Fall 2022)

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Agenda

- Brief overview of A2
- Half-edge data structure
 - Definition
 - Traversal
 - Modification

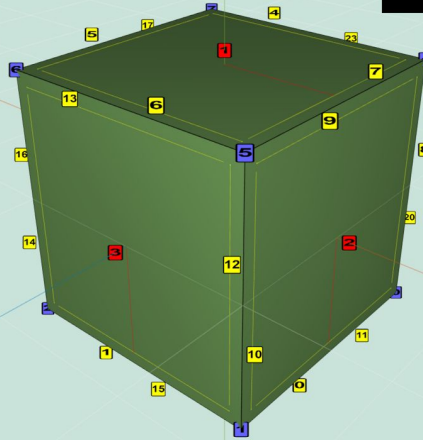
Setup

Same as in A0 and A1:

- Run `python3 -m http.server` (or similar) inside the assignment directory
- Open `http://localhost:8000` in web browser

GUI

COS426 Assignment 2
Mesh Processing
Student Name <NetID>



Batch Mode

▸ Transformations

▸ Warps

▸ Filters

▸ Topology

▸ Subdivision

Close Controls

▼ History

▼ 1: Base Mesh

mesh cube.obj ▼

▼ 2: Display Settings

show labels ☒

show halfedge ☒

shading flat ▼

vert normals ☐

face normals ☐

show grid ☒

show all verts ☐

show axes ☒

vert colors ☐

Close Controls

10 FPS (0-60)

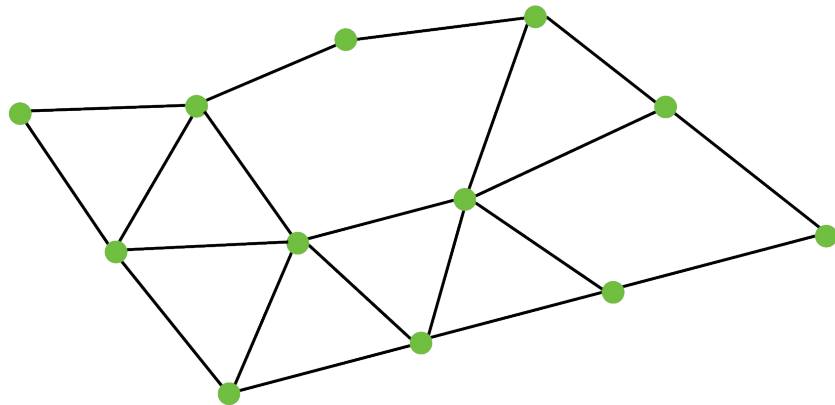


Tips for Three.js and A2

- For A2 you will be using the Three.js library
 - Simple and efficient primitives for working in 3D
- You should **read the docs!**
 - [Vector3](#)
 - [Euler](#) (for rotations)
- Modularity is your friend!
 - You will be writing helper functions. Use them!

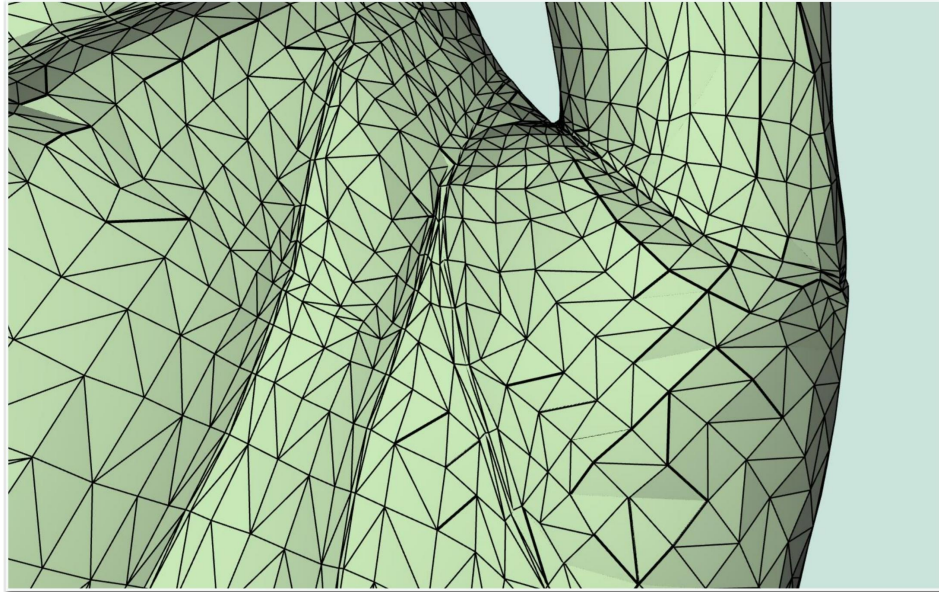
Meshes vs. Images

- Images have implicit adjacency information
 - Window around a pixel
 - Easy to express local operations
 - (e.g. convolution)
- What about meshes?
 - How to apply smoothing?



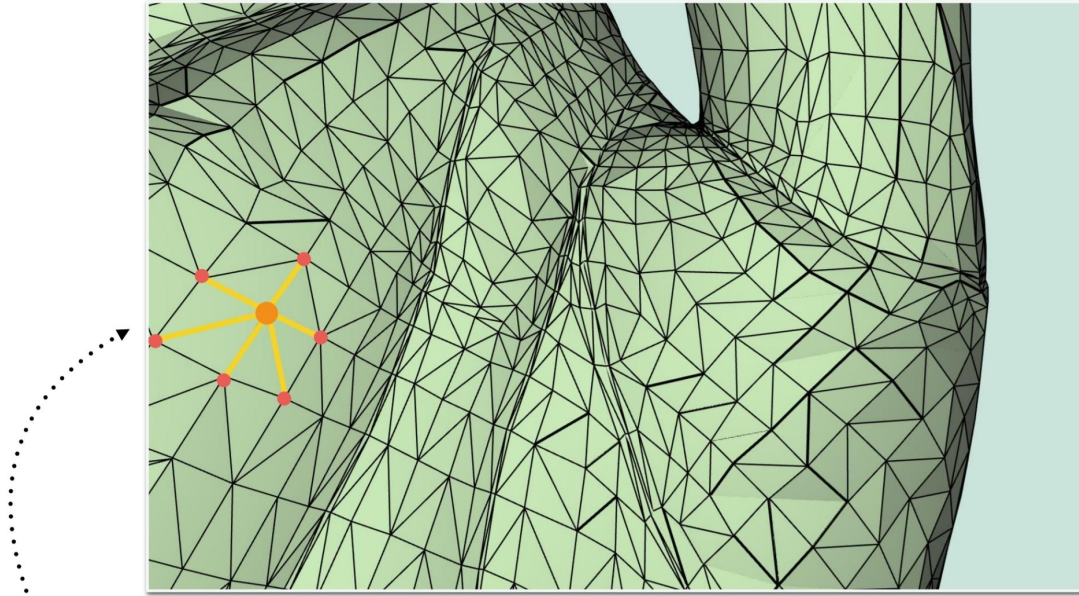
Meshes

- Meshes can be quite dense



Meshes

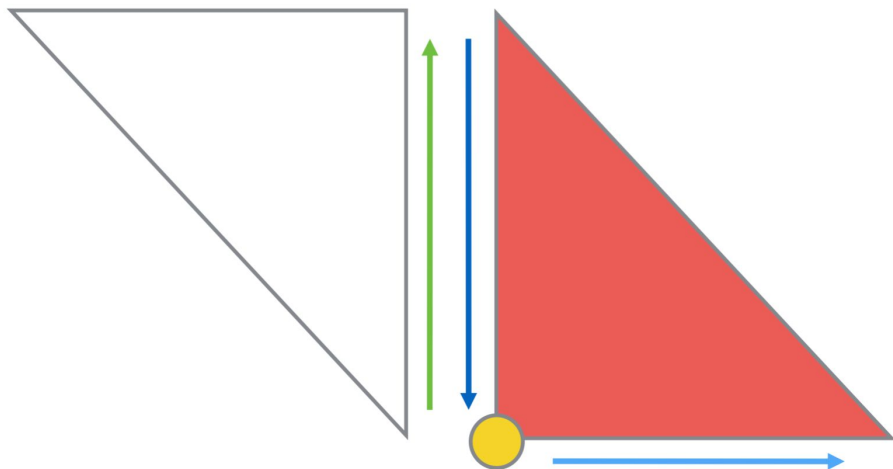
- How can we efficiently access adjacency information?



One - Ring Neighborhood

What is a Half-Edge?

- Imagine splitting each edge in two
 - Each half gets one of the edge's faces
 - Each face, vertex, and half-edge stores some state
 - Conceptually very similar to doubly linked list



Half-Edge: What State is Stored?

Half Edge	Vertex	Face
Vertex	Position	Half-Edge
Opposite Half-Edge	Outgoing Half-Edge	
Face		
Next Half-Edge		

Half-Edge Data Structure

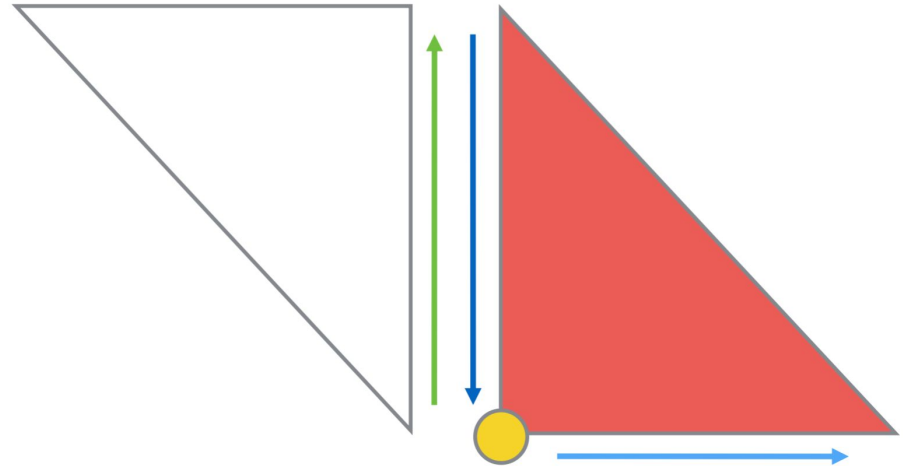
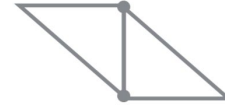
Half Edge

Vertex

Opposite
Half-Edge

Face

Next
Half-Edge

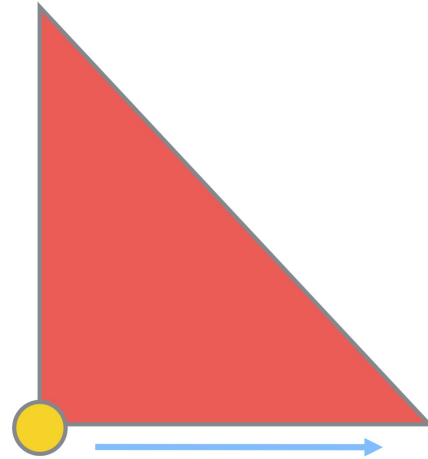


Half-Edge Data Structure

Vertex

Location

Outgoing
Half-Edge



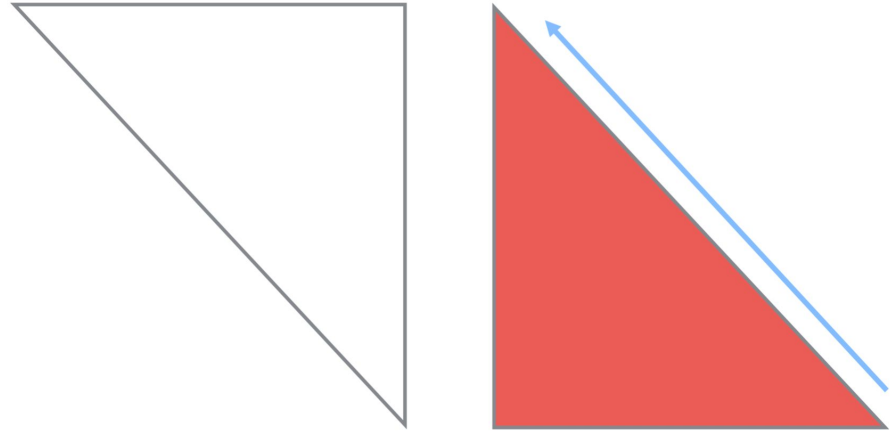
Q: Which half-edge to choose?

A: Pick one arbitrarily

Half-Edge Data Structure

Face

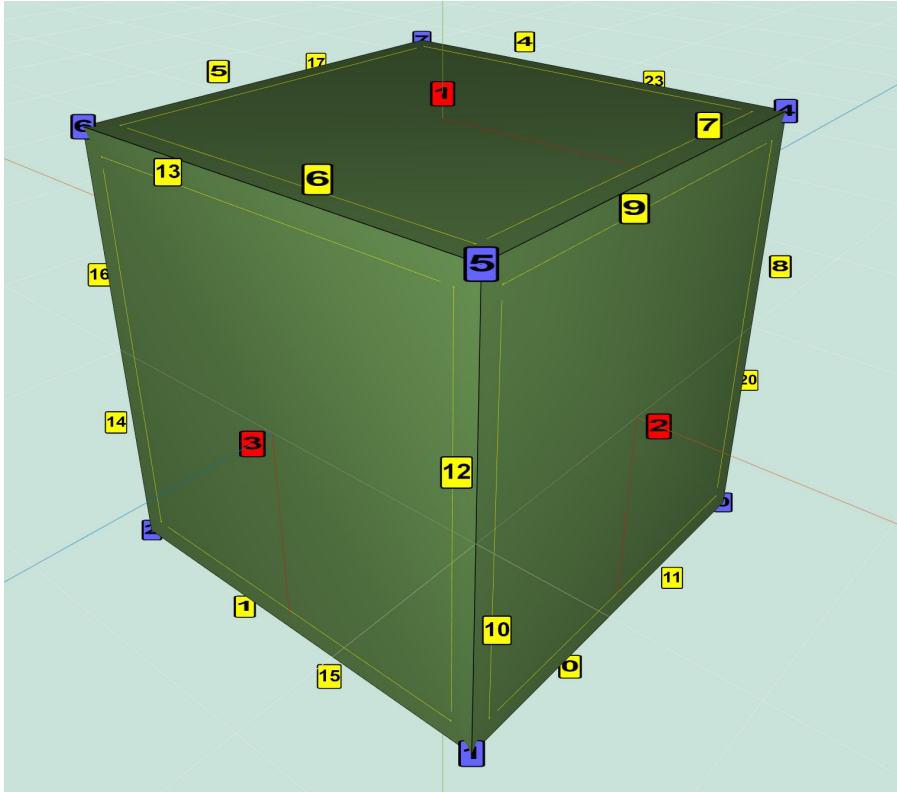
Half-Edge



Q: Which half-edge to choose?

A: Pick one arbitrarily

Half-Edge Visualization



- Faces:
- Half-edges:
- Vertices:

id

id

id

Features

Transformations

- Translation
- Rotation
- Scale

Traversal

- **Various edge/vertex/face helpers**

Analysis

- Face Area
- Per-vertex Normals
- Average Edge Lengths

Warps

- Twist
- Inflate
- Wacky

Filters

- Noise
- Smoothing
- Sharpening
- Curvature

Topology

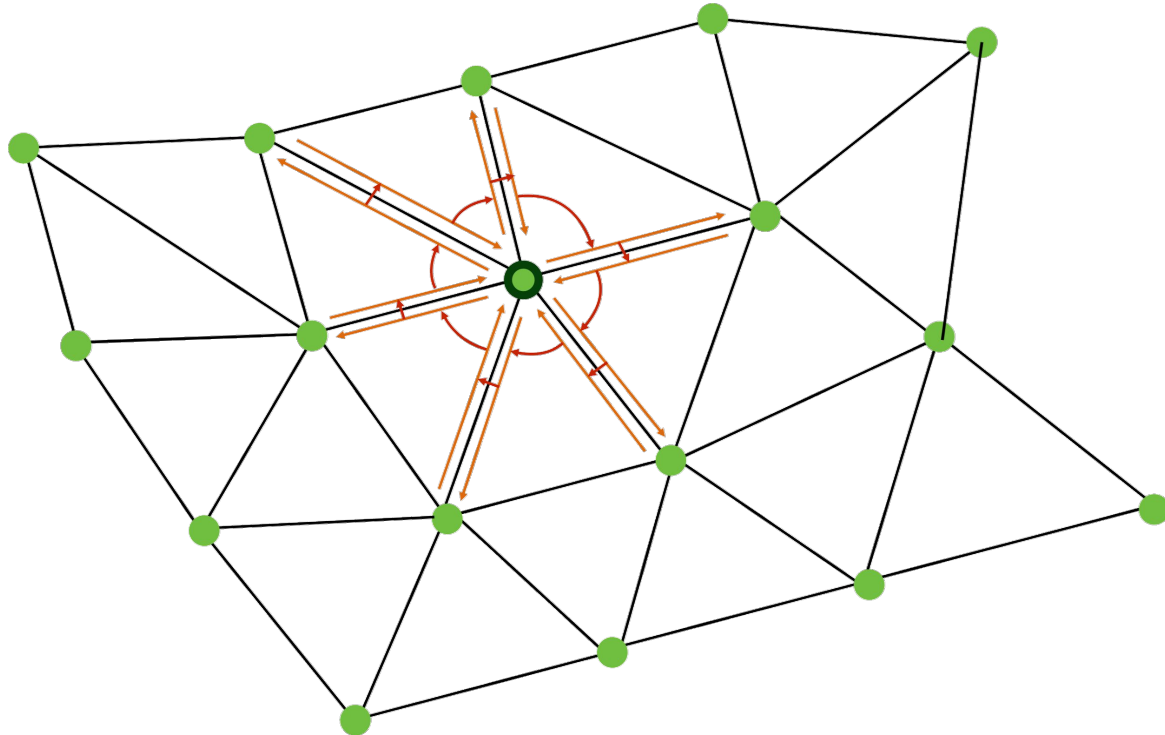
- Triangulate
- Truncate
- Extrude
- Split Long Edges

Subdivision

- Triangle Topology
- Loop
- Quad Topology
- Catmull-Clark

Traversal (Vertices on vertex)

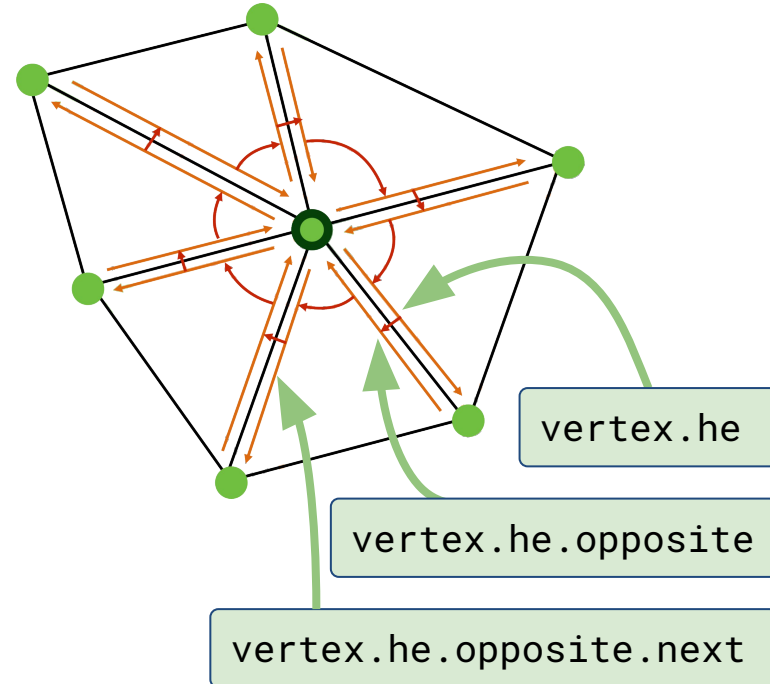
- How do we get one-ring neighbors of a vertex?



Traversal (Vertices on vertex)

- How do we get one-ring neighbors of a vertex?

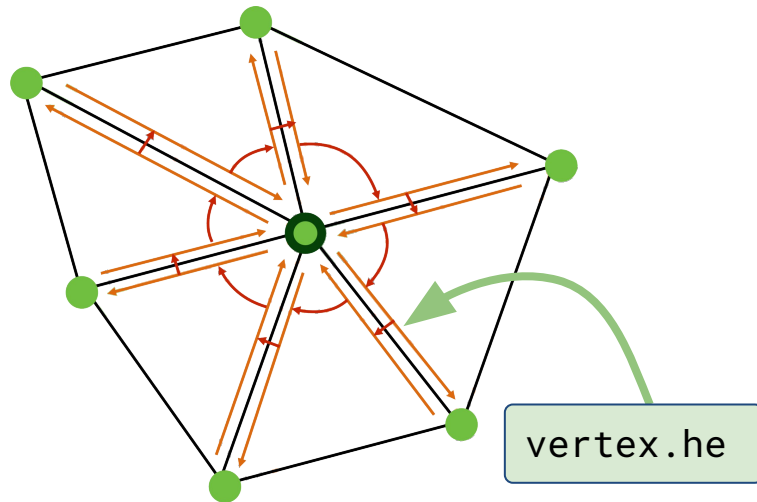
```
original_he = vertex.he;  
he = original_he;  
do {  
    // some calculations  
    he = he.opposite.next  
} while (he != original_he)
```



Traversal (Vertex Normals)

- Vertex Normals are defined as a weighted average of the normals of adjacent faces (weighted by face area)
- How would you compute vertex normals given face normals and areas?

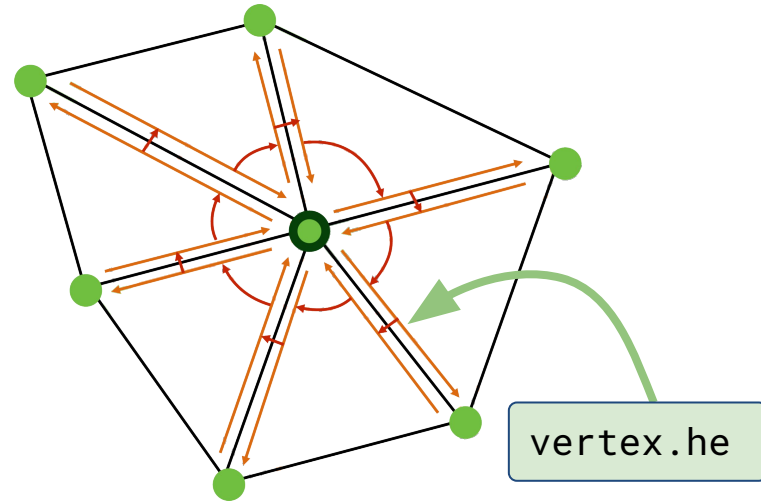
```
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```



Traversal (Vertex Normals)

- Vertex Normals are defined as a weighted average of the normals of adjacent faces (weighted by face area)
- How would you compute vertex normals given face normals and areas?

```
original_he = vertex.he;  
he = original_he;  
v_normal.set(0,0,0);  
do {  
    f_normal = he.face.normal;  
    area = he.face.area;  
    v_normal.add(f_normal*area);  
    he = he.opposite.next  
} while (he != original_he)  
v_normal.normalize()
```

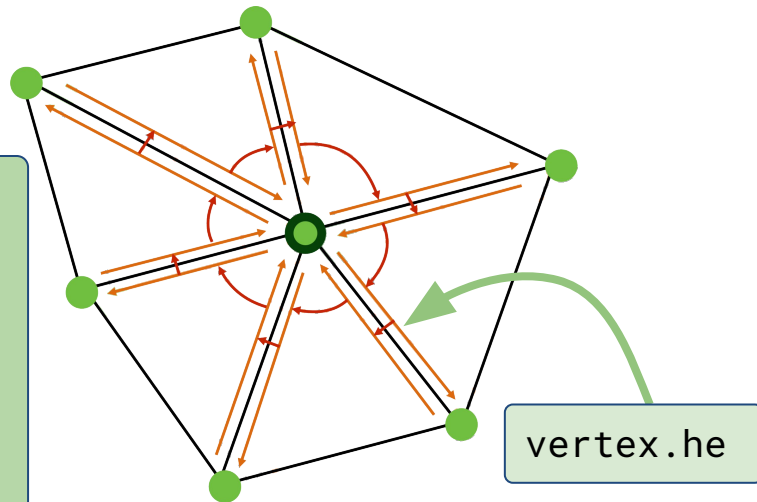


Traversal (Vertex Normals)

- Vertex Normals are defined as a weighted average of the normals of adjacent faces (weighted by face area)
- How would you compute vertex normals given face normals and areas?

Easier way: use `facesOnVertex()`!

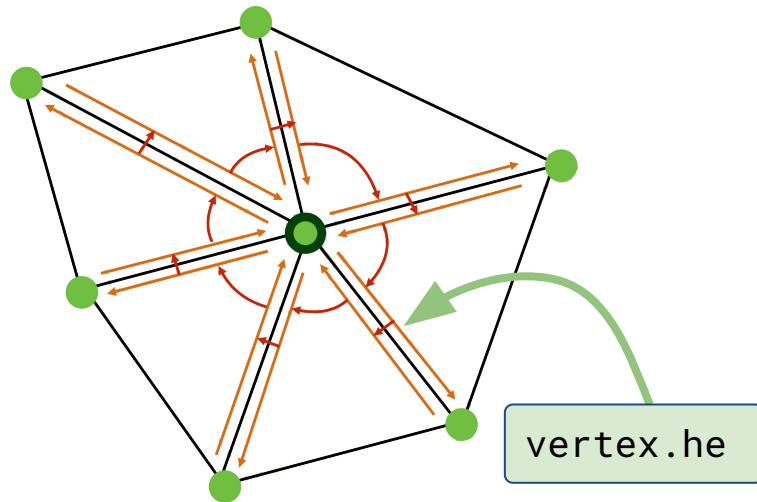
```
fs = mesh.facesOnVertex(v);  
v_normal.set(0,0,0);  
for (let f of fs) {  
    v_normal.add(f.normal * f.area);  
}  
v_normal.normalize()
```



Traversal (Laplacian Smoothing)

- Similarly, in uniform Laplacian smoothing, each vertex moves towards the average of it and its neighbors.

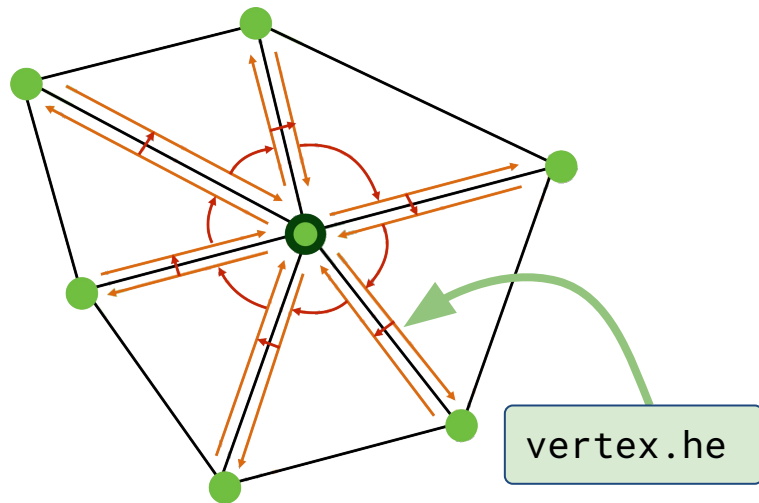
```
original_he = vertex.he;  
he = original_he;  
do {  
    // some calculations  
    he = he.opposite.next  
} while (he != original_he)
```



Traversal (Laplacian Smoothing)

- Similarly, in uniform Laplacian smoothing, each vertex moves towards the average of it and its neighbors.

```
original_he = vertex.he;  
he = original_he;  
avg_pos.set(0,0,0);  
do {  
    avg_pos.add(he.vertex.pos);  
    he = he.opposite.next  
} while (he != original_he)  
avg_pos.add(-vertex*num_neigh);  
new_pos = vertex + avg_pos * delta;
```



Traversal (Laplacian Smoothing)

- Some tips for uniform Laplacian smoothing:
 - You can use `verticesOnVertex()` to simplify your code!
 - Be careful not to modify your mesh before you've computed offsets for all vertices!
 - (Similar to filters in A1 that modified the image)

Traversal (Cotan Laplacian Smoothing)

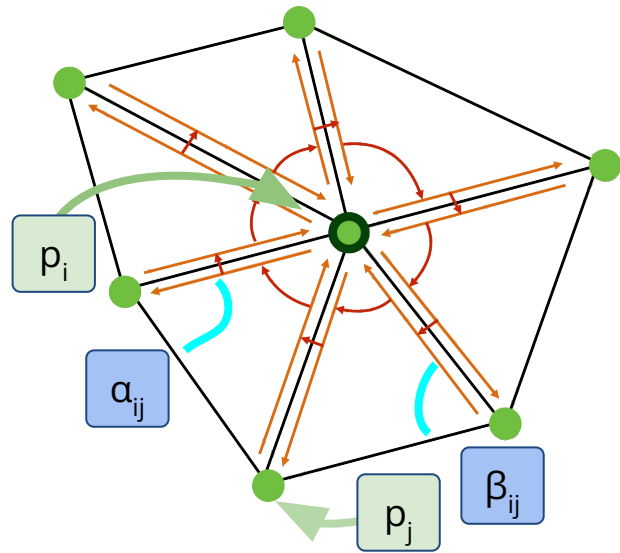
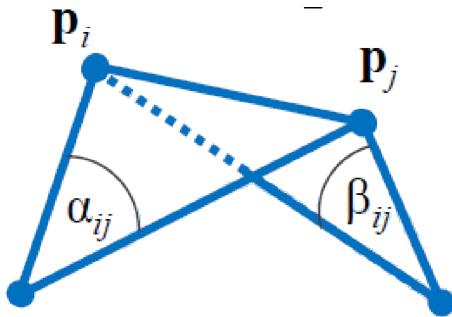
- Cotangent Laplacian smoothing

```
avg_pos.add(he.vertex.pos);  
num_neigh  
⇒ avg_pos.add(w*he.vertex.pos);  
⇒ total_w
```

- Notes:

- p_i = center vert
- Iterate over all neighboring p_j
- p_i, p_j will share two faces
- α_{ij}, β_{ij} are the far angles on these faces

$$w = \frac{\cot(\alpha_{ij}) + \cot(\beta_{ij})}{2}$$



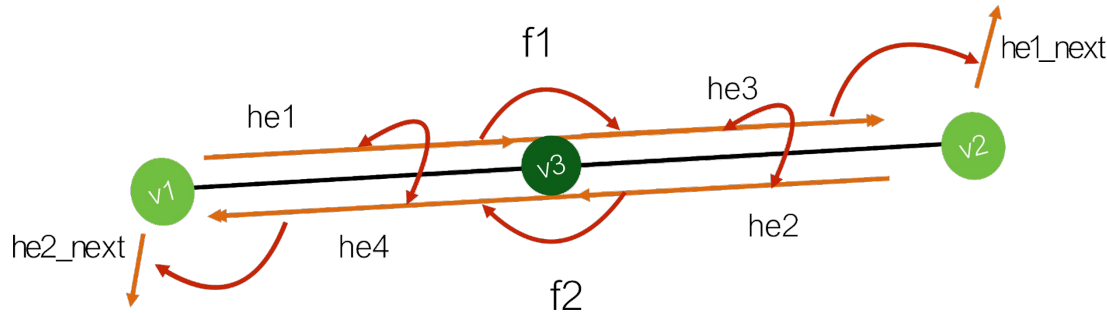
Data Structure Modification

- Take a look meshUtils.js for the all the primitives
 - splitEdgeMakeVert()
 - joinEdgeKillVert()
 - splitFaceMakeEdge()
 - joinFaceKillEdge()

Data Structure Modification (splitEdge)

How to add new vertices to an existing half-edge data structure?

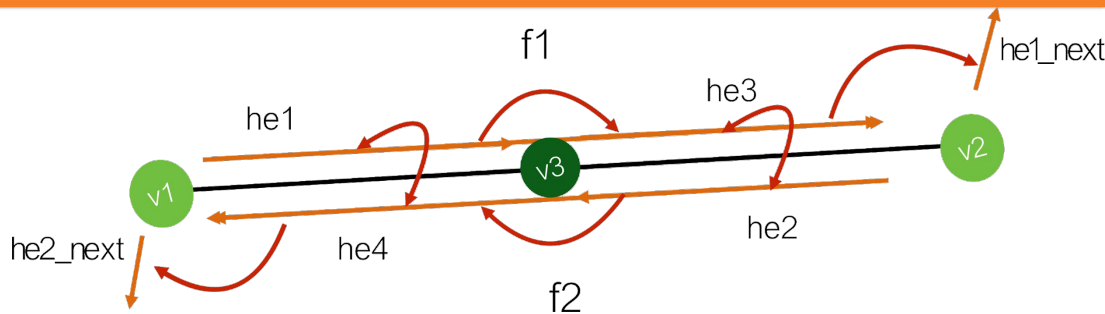
`splitEdgeMakeVert(v1,v2,factor):`



Data Structure Modification (splitEdge)

splitEdgeMakeVert(v1,v2,factor):

- addVertex
- addHalfEdge
- he.vertex, he.opposite



```
v3 = addVertex(v1.pos.lerp(v2.pos, factor));
```

```
he3 = addHalfEdge(v3,v2,f1);
```

```
he4 = addHalfEdge(v3,v1,f2);
```

```
he1.vertex = v3;
```

```
he2.vertex = v2;
```

```
he1.next = he3;
```

```
he2.next = he4;
```

```
he3.next = he1_next;
```

```
he4.next = he2_next;
```

```
he1.opposite = he4;
```

```
he4.opposite = he1;
```

```
he2.opposite = he3;
```

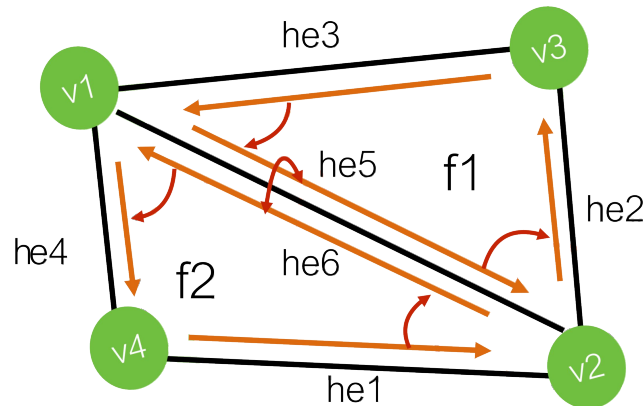
```
he3.opposite = he2;
```

Data Structure Modification (splitFace)

How to add new edges to an existing half-edge data structure?

splitFaceMakeEdge(f, v1, v2, vertOnF, switchFaces)

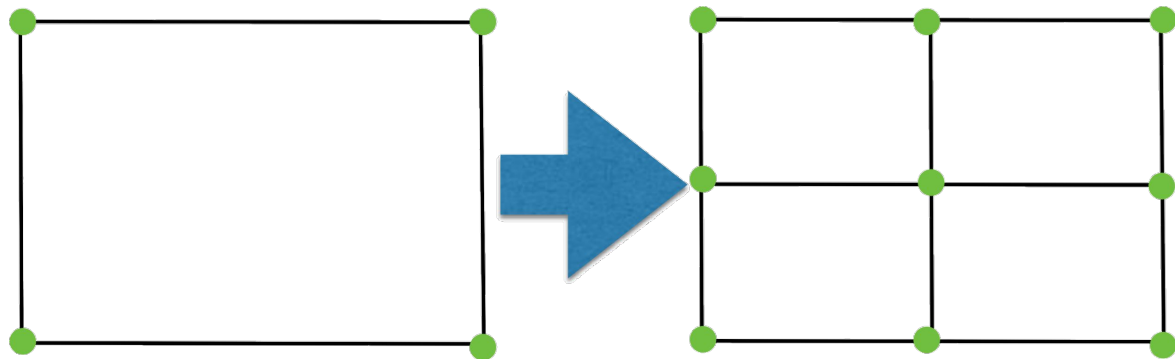
```
f2 = addFace();  
he5 = addHalfEdge(v1,v2,f1);  
he6 = addHalfEdge(v2,v1,f2);  
he5.opposite = he6;  
he6.opposite = he5;  
he5.next = he2;  
he3.next = he5;  
he1.next = he6;  
he6.next = he4;  
f1.halfedge = he5;  
f2.halfedge = he6;
```



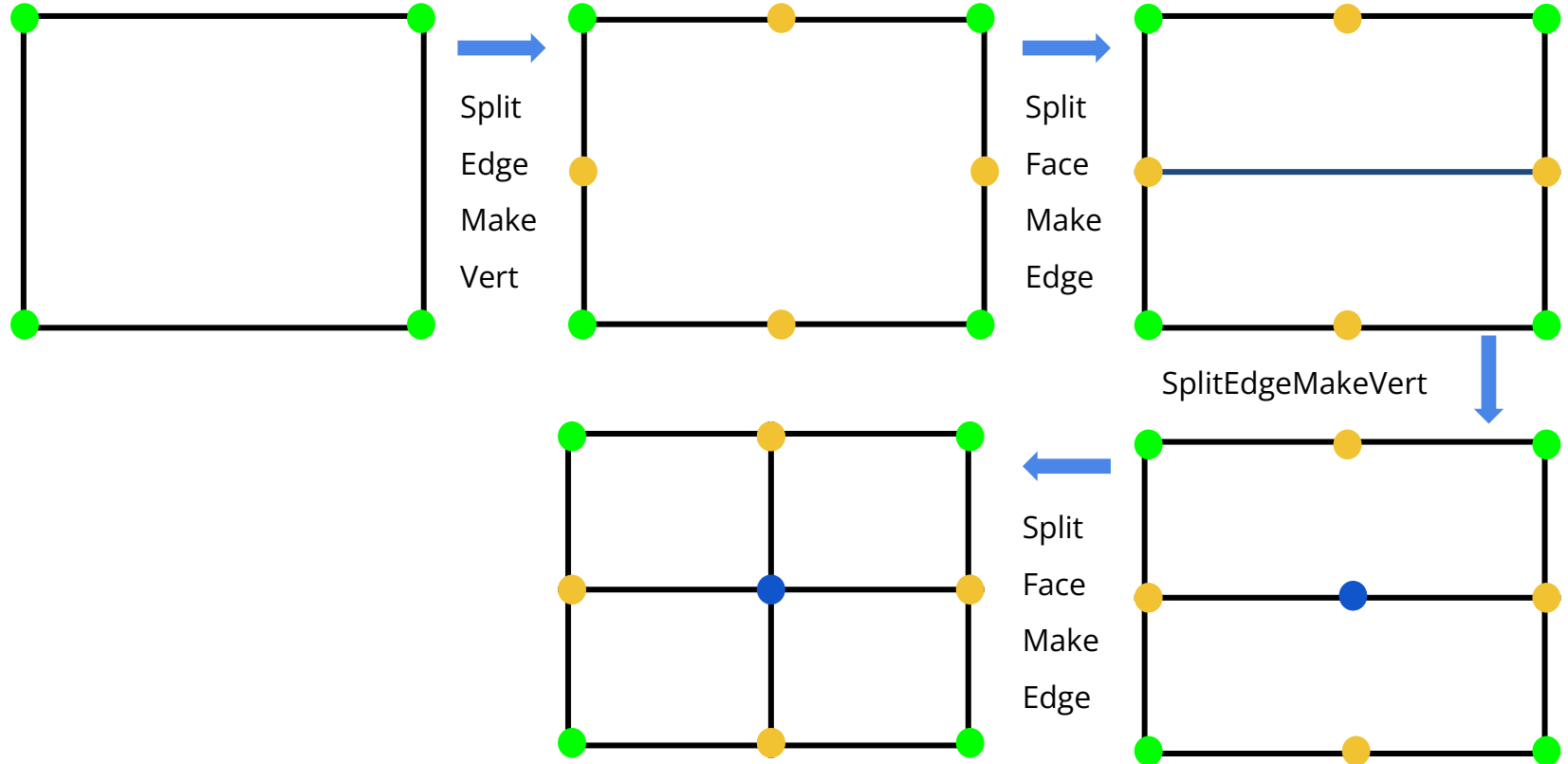
- Optional args: (for advanced filters, like Extrude)
 - vertOnF: if provided, this vert will still be on the original face
 - switchFaces: if true, vertOnF is placed on the new face instead

Data Structure Modification (subdividing)

- How would you go about subdividing a quad face?
 - You're given *split edge* and *split face*
 - Just use those - guaranteed validity of mesh after use!



Data Structure Modification(subdividing)



Q&A
