

3D Modeling

COS 426, Fall 2022

PRINCETON UNIVERSITY

Syllabus

I. Image processing

- II. Modeling
- **III.** Rendering
- **IV.** Animation

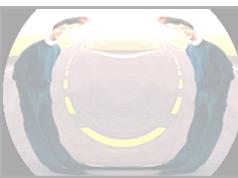
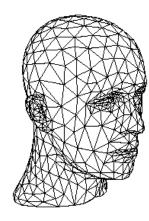


Image Processing (Rusty Coleman, CS426, Fall99)





Rendering

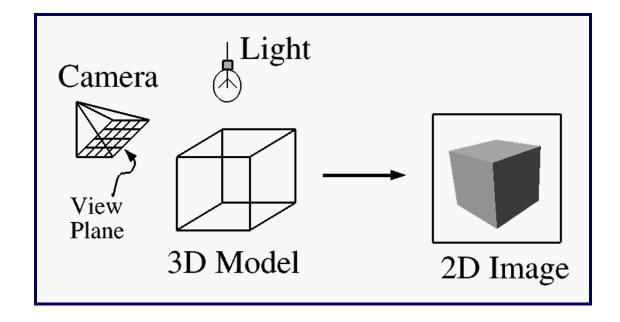
(Michael Bostock, CS426, Fall99)



Modeling (Denis Zorin, CalTech)

What is 3D Modeling?

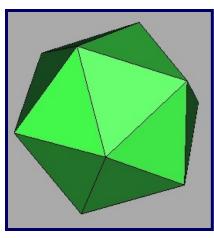
- Topics in computer graphics
 - **Imaging** = *representing 2D images*
 - Modeling = *representing 3D objects*
 - **Rendering** = *constructing 2D images from 3D models*
 - Animation = *simulating changes over time*

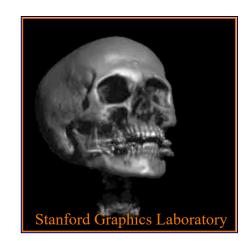


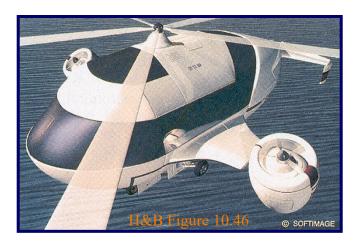


Modeling

- How do we ...
 - Represent 3D objects in a computer?
 - Acquire computer representations of 3D objects?
 - Manipulate these representations?





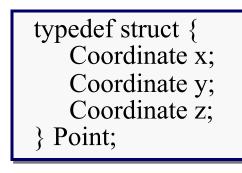


Modeling Background

- Scene is usually approximated by 3D primitives
 - Point
 - Vector
 - Line segment
 - Ray
 - Line
 - Plane
 - Polygon

3D Point

- Specifies a location
 - Represented by three coordinates
 - Infinitely small



 \bullet (x,y,z)



3D Vector



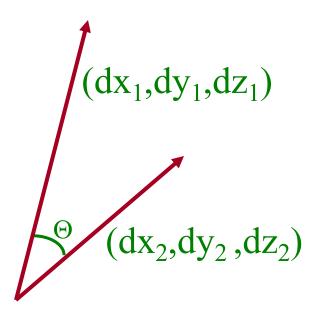
(dx,dy,dz)

- Specifies a direction and a magnitude
 - Represented by three coordinates
 - Magnitude IIvII = sqrt(dx \cdot dx + dy \cdot dy + dz \cdot dz)
 - Has no location

typedef struct {
 Coordinate dx;
 Coordinate dy;
 Coordinate dz;
} Vector;

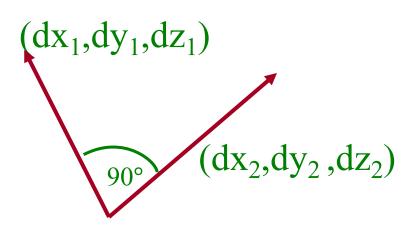
3D Vector

Dot product of two 3D vectors
 v₁·v₂ = IIv₁II IIv₂II cos(Θ)



3D Orthogonality

• Dot product of two 3D vectors • $v_1 \cdot v_2 = I |v_1| I ||v_2| I \cos(\pi/2) = 0$

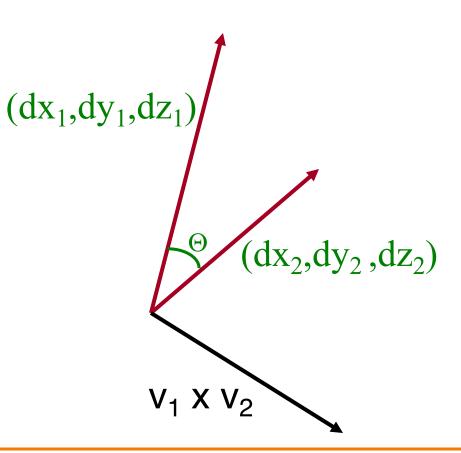




3D Vector

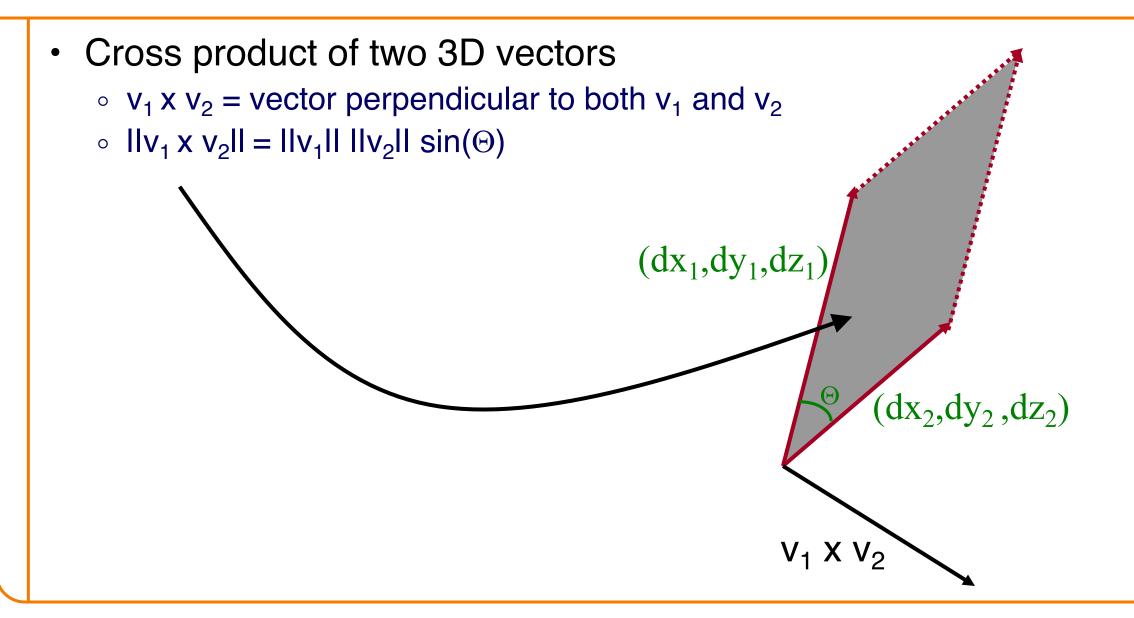


- Cross product of two 3D vectors
 - $v_1 x v_2$ = vector perpendicular to both v_1 and v_2
 - $IIv_1 x v_2II = IIv_1II IIv_2II sin(\Theta)$



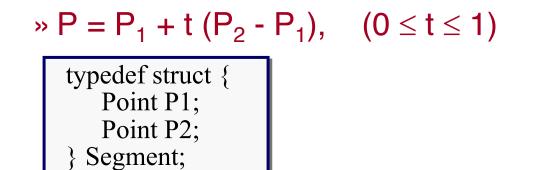
3D Vector

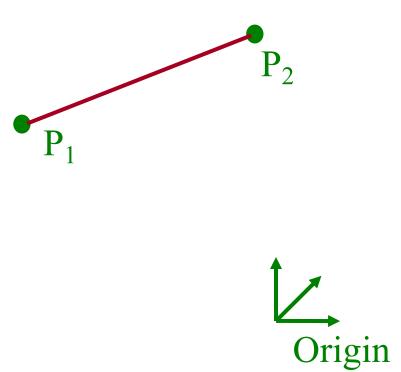




3D Line Segment

- Linear path between two points
 - Parametric representation:







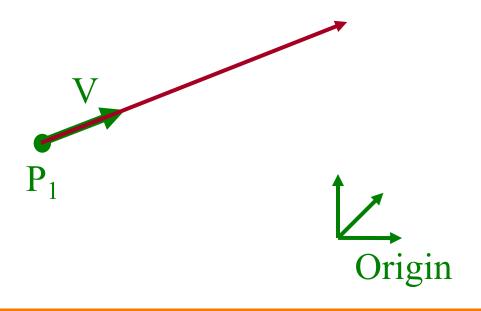
3D Ray



- Line segment with one endpoint at infinity
 - Parametric representation:

```
 P = P_1 + t V, \quad (0 \le t < \infty)
```

```
typedef struct {
    Point P1;
    Vector V;
} Ray;
```



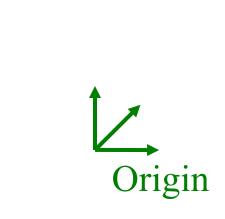
3D Line



- Line segment with both endpoints at infinity
 - Parametric representation:

```
 = P_1 + t V, \quad (-\infty < t < \infty)
```

typedef struct {
 Point P1;
 Vector V;
} Line;

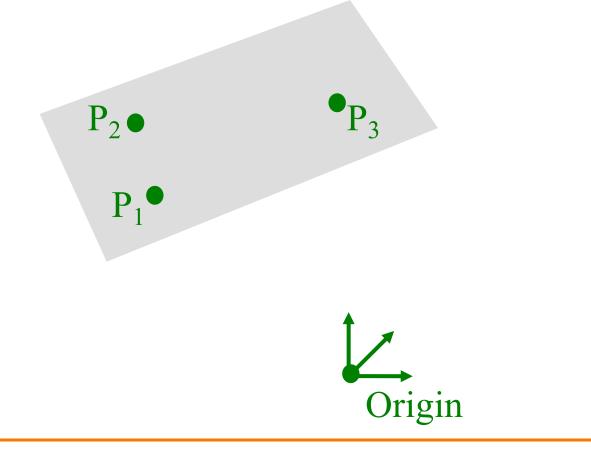


 \mathbf{P}_1

3D Plane



• Defined by three points in 3D space



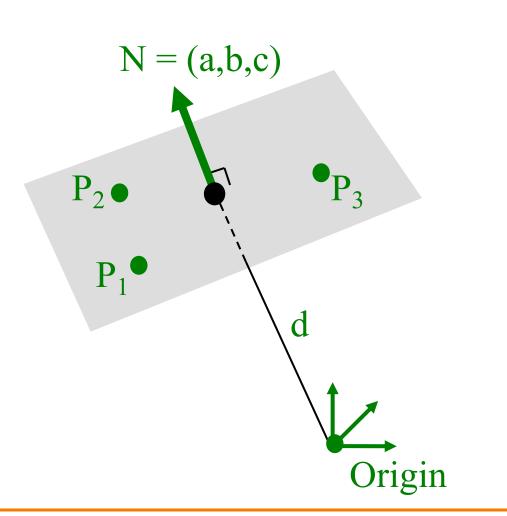
3D Plane



- A linear combination of three points
 - Implicit representation:
 - $P \cdot N d = 0, or$
 - » N· (P P₁)= 0, or
 - ax + by + cz + d = 0

typedef struct { Vector N; Distance d; } Plane;

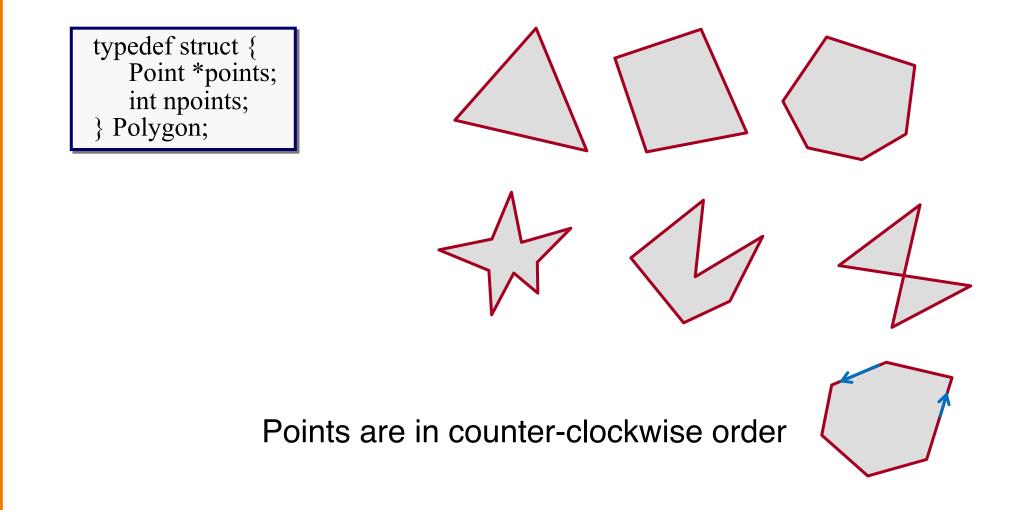
N is the plane "normal"
 » Unit-length vector
 » Perpendicular to plane



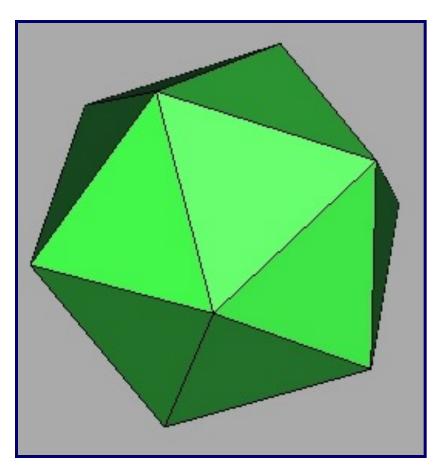
3D Polygon



• Set of points "inside" a sequence of coplanar points

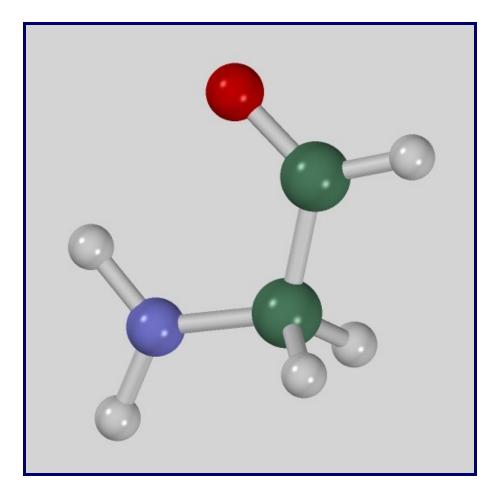






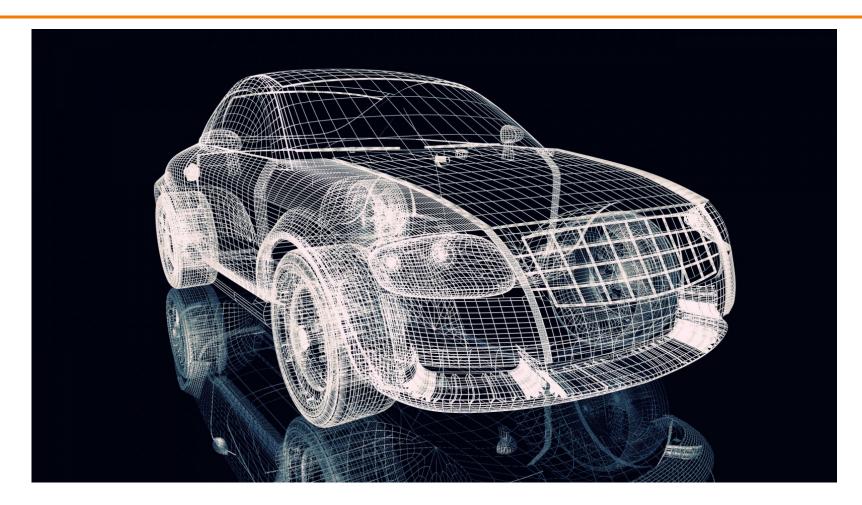
How can this object be represented in a computer?





How about this one?

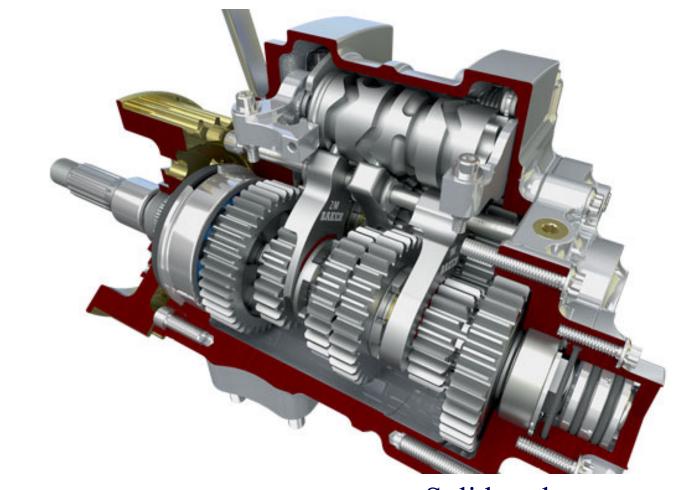




Wallpapersonly.net







How about this one?

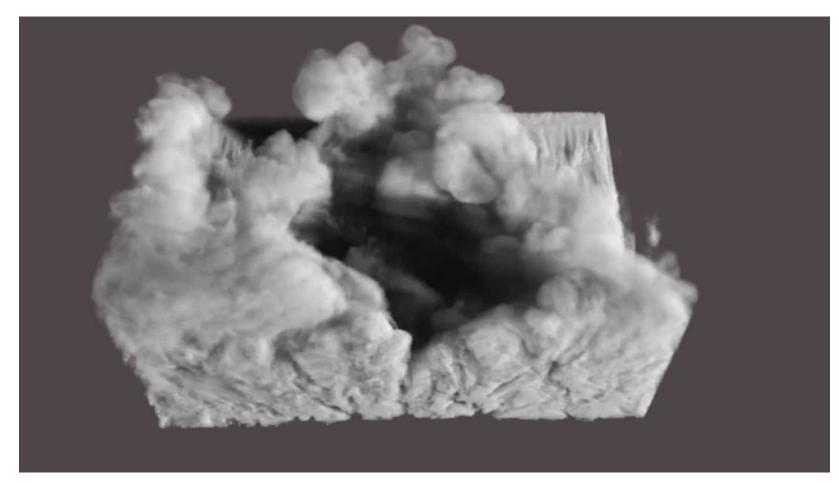
Solidworks





The visible human





This one?

FumeFx

- Points
 - Range image
 - Point cloud
- Surfaces
 - Polygonal mesh
 - Subdivision
 - Parametric
 - Implicit

- Solids
 - \circ Voxels
 - BSP tree
 - CSG
 - Sweep
- High-level structures
 - Scene graph
 - Application specific

Equivalence of Representations



- Thesis:
 - Each representation has enough expressive power to model the shape of any geometric object
 - It is possible to perform all geometric operations with any representation
- Analogous to Turing-equivalence
 - Computers and programming languages are Turing-equivalent, but each has its benefits...

Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
- Manipulation
- Animation

→ Data structures determine algorithms

Efficiency for different tasks

- Acquisition
 - » Range Scanning
- Rendering
- Analysis
- Manipulation
- Animation











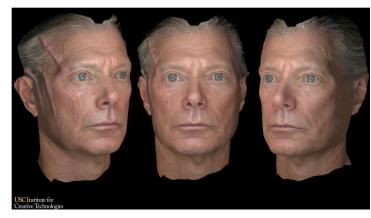
DGP course notes, Technion

Efficiency for different tasks

- Acquisition
 - » Computer Vision
- Rendering
- Analysis
- Manipulation
- Animation



Indiana University

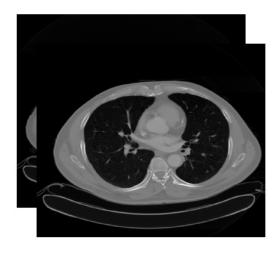




Efficiency for different tasks

- Acquisition
 - » Tomography
- Rendering
- Analysis
- Manipulation
- Animation







DGP course notes, Technion

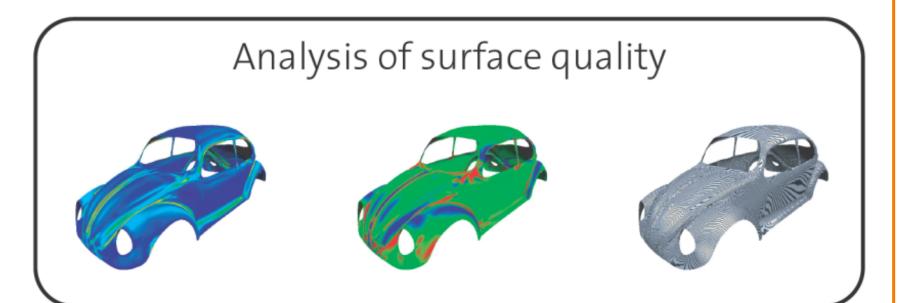
Efficiency for different tasks

- Acquisition
- Rendering
 Intersection
- Analysis
- Manipulation
- Animation



Efficiency for different tasks

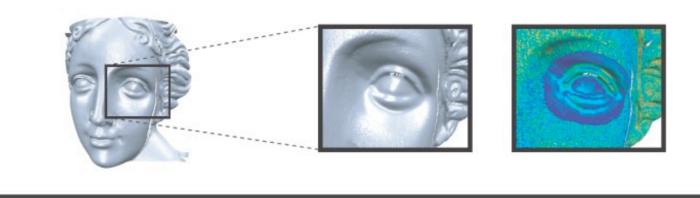
- Acquisition
- Rendering
- Analysis
 - » Curvature,
 smoothness
- Manipulation
- Animation



Efficiency for different tasks

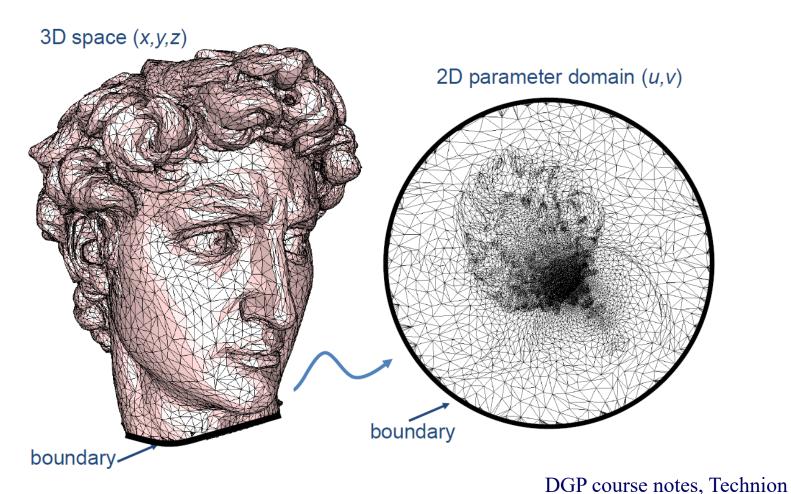
- Acquisition
- Rendering
- Analysis
 - » Fairing
- Manipulation
- Animation

Surface smoothing for noise removal



Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
 - » Parametrization
- Manipulation
- Animation

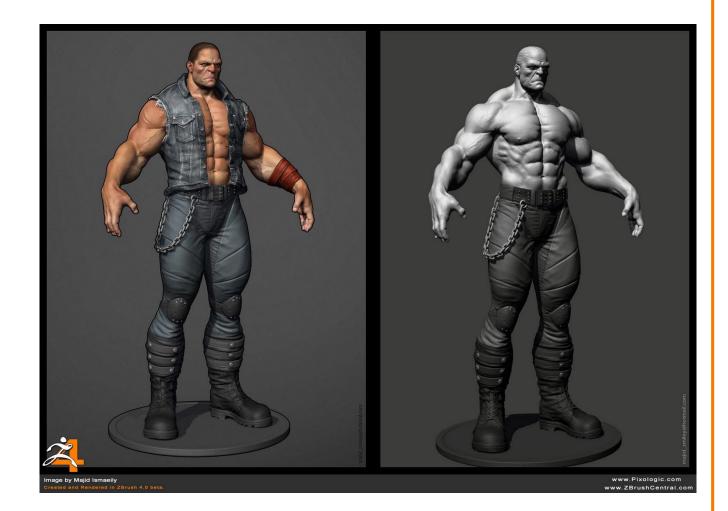




Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
 - » Texture mapping
- Manipulation
- Animation

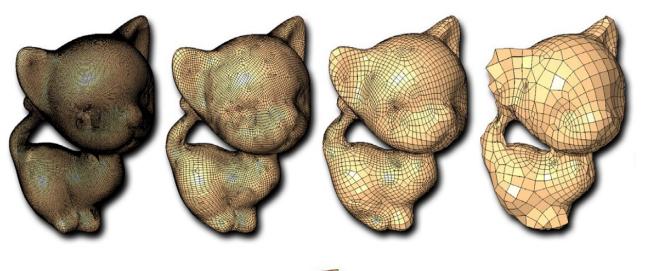


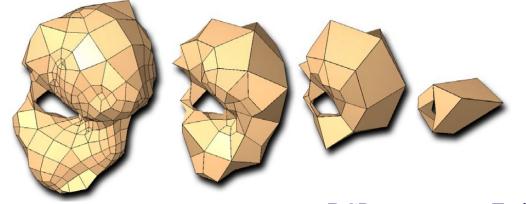


DGP course notes, Technion

Efficiency for different tasks

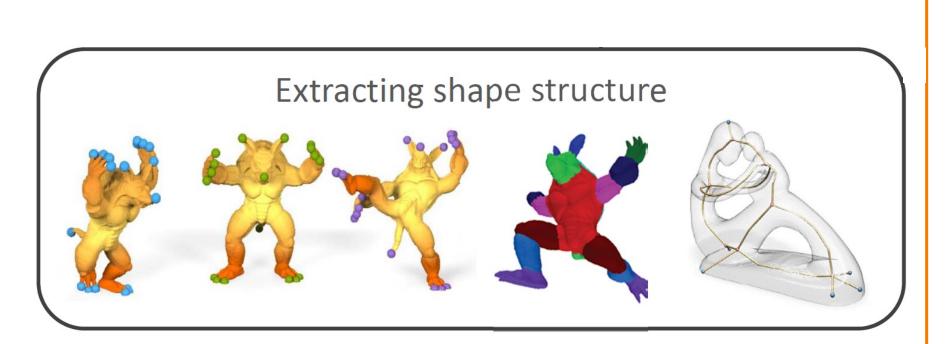
- Acquisition
- Rendering
- Analysis
 - » Reduction
- Manipulation
- Animation





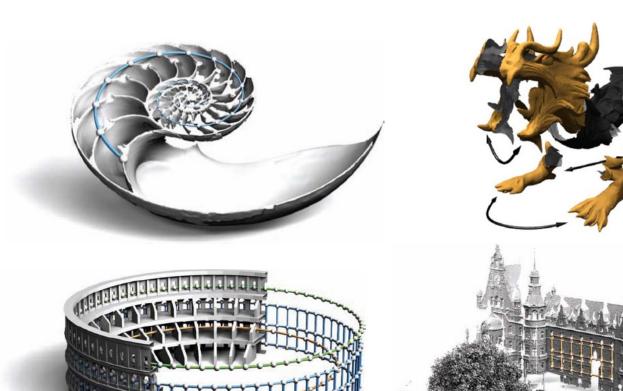
Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
 - » Structure
- Manipulation
- Animation



Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
 - » Symmetry detection
- Manipulation
- Animation





Efficiency for different tasks

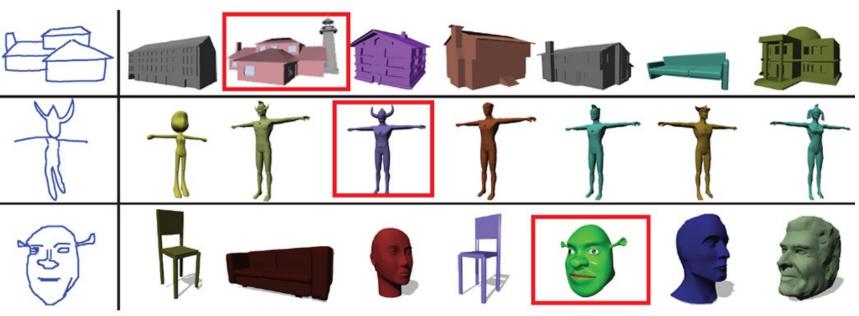
- Acquisition
- Rendering
- Analysis
 - » Correspondence
- Manipulation
- Animation





Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
 - » Shape retrieval
- Manipulation
- Animation



Shao et al. 2011

Efficiency for different tasks

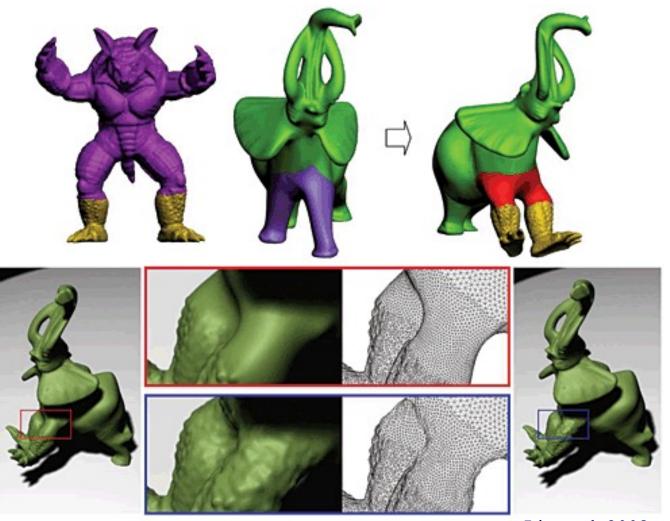
- Acquisition
- Rendering
- Analysis
 - » Segmentation
- Manipulation
- Animation





Efficiency for different tasks

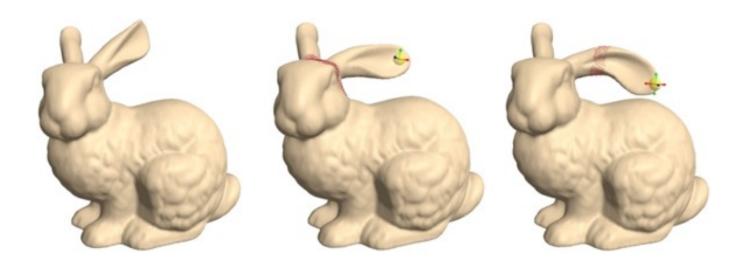
- Acquisition
- Rendering
- Analysis
 - » Composition
- Manipulation
- Animation



Lin et al. 2008

Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
- Manipulation» Deformation
- Animation

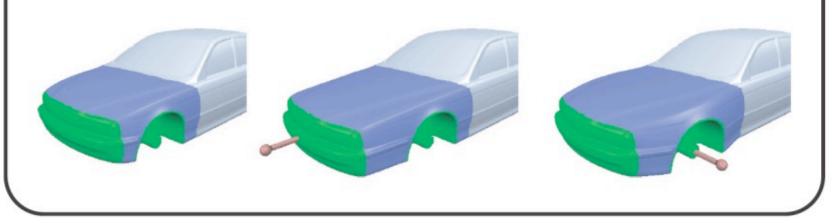


IGL

Efficiency for different tasks

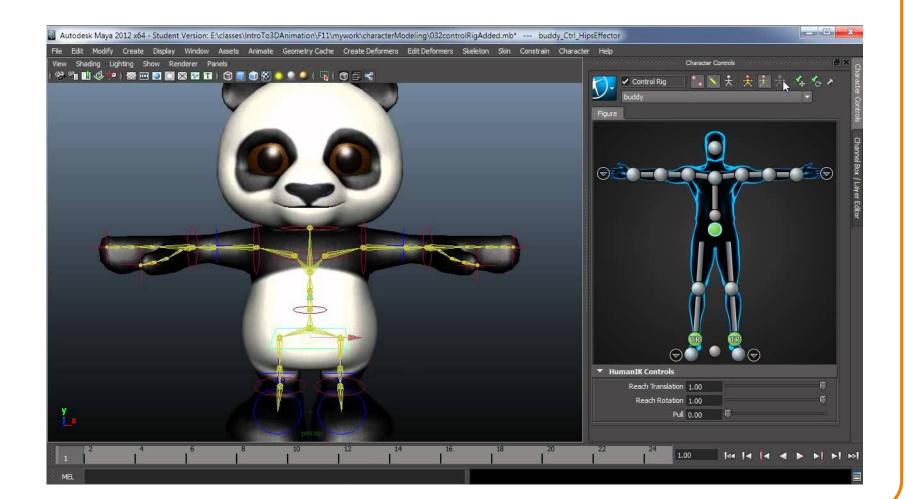
- Acquisition
- Rendering
- Analysis
- Manipulation» Deformation
- Animation

Freeform and multiresolution modeling



Efficiency for different tasks

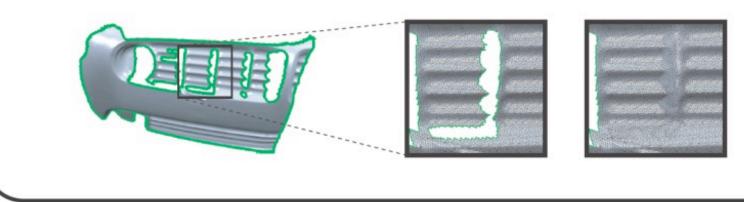
- Acquisition
- Rendering
- Analysis
- Manipulation» Control
- Animation



Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
- Manipulation
 - » Healing
- Animation

Removal of topological and geometrical errors

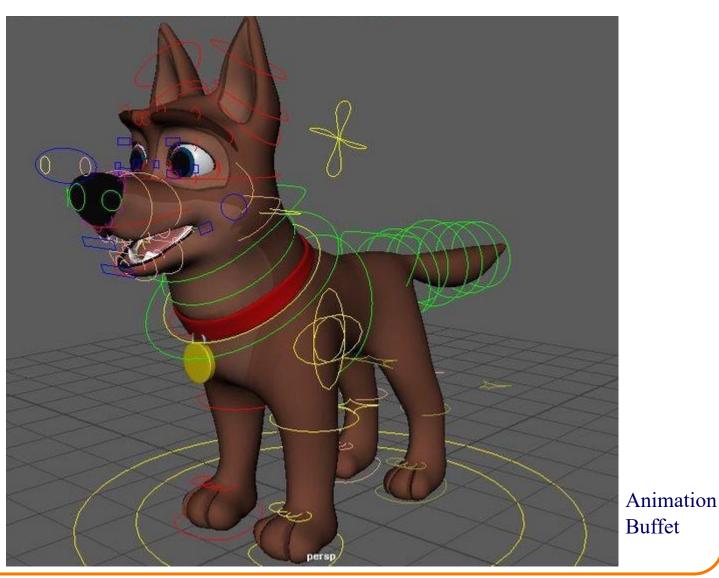






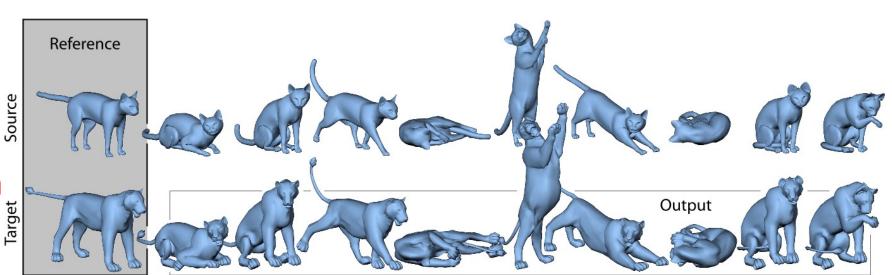
Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
- Manipulation
- Animation
 - » Rigging



Efficiency for different tasks

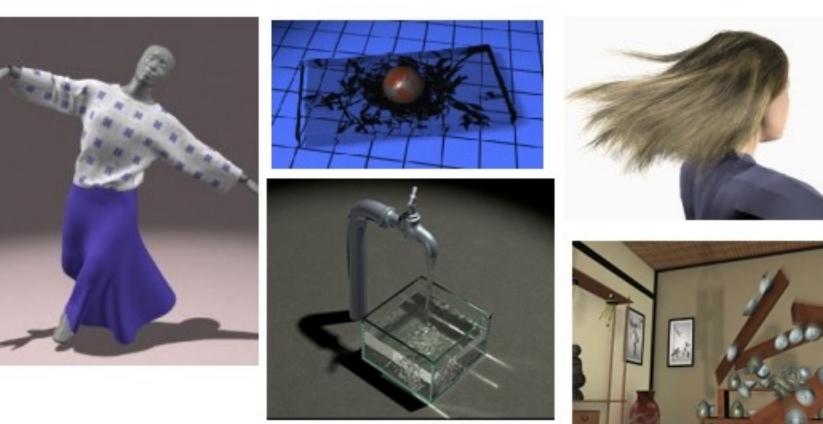
- Acquisition
- Rendering
- Analysis
- Manipulation
- Animation
 - » Deformation transfer



Sumner et al. 2004

Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
- Manipulation
- Animation
 - » Simulation



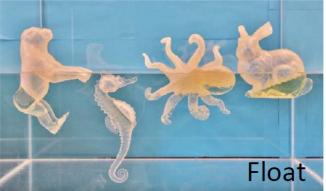
Physically Based Modelling course notes, USC

Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
- Manipulation
- Animation
 - » Fabrication







3D Object Representations

- Points
 - Range image
 - Point cloud
- Surfaces
 - Polygonal mesh
 - Subdivision
 - Parametric
 - Implicit

- Solids
 - \circ Voxels
 - BSP tree
 - CSG
 - Sweep
- High-level structures
 - Scene graph
 - Application specific

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Range Image



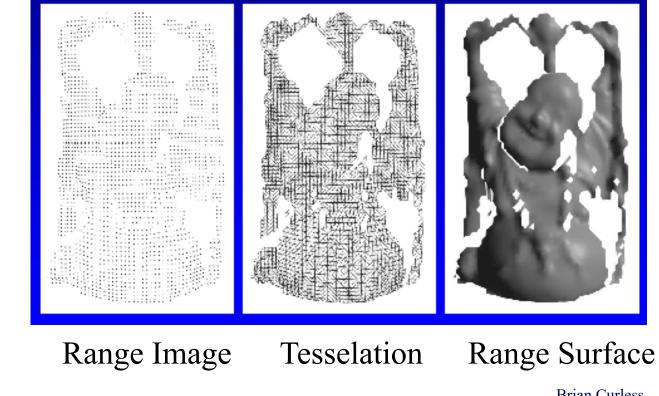
Set of 3D points mapping to pixels of depth image Can be acquired from range scanner



Cyberware



Stanford



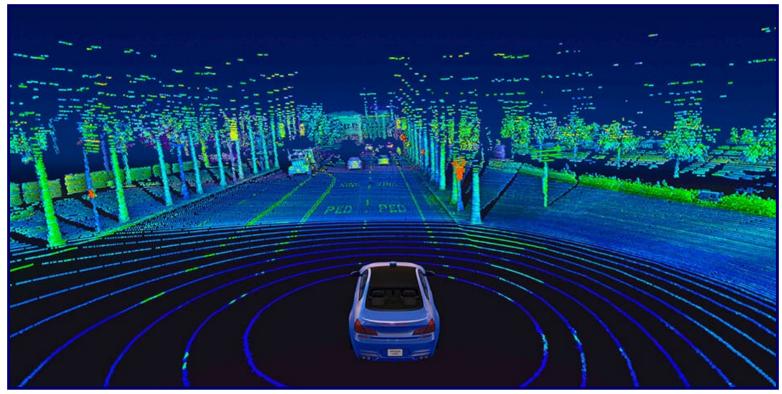
Brian Curless SIGGRAPH 99 Course #4 Notes

Point Cloud



Unstructured set of 3D point samples

• Acquired from range finder, computer vision, etc



Velodyne Lidar Scan

3D Object Representations

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 - Implicit

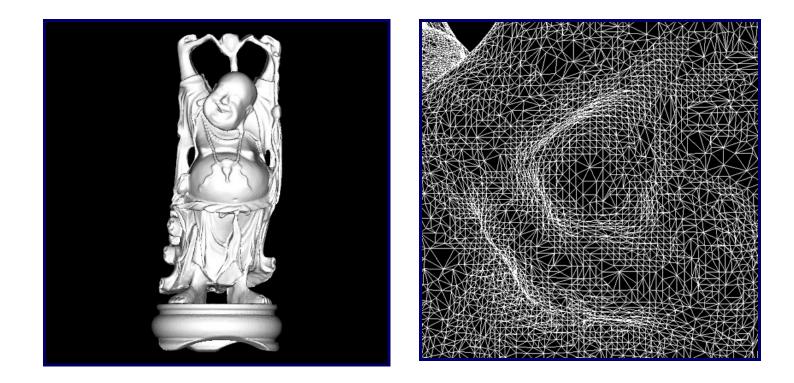
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Polygonal Mesh



Connected set of polygons (often triangles)

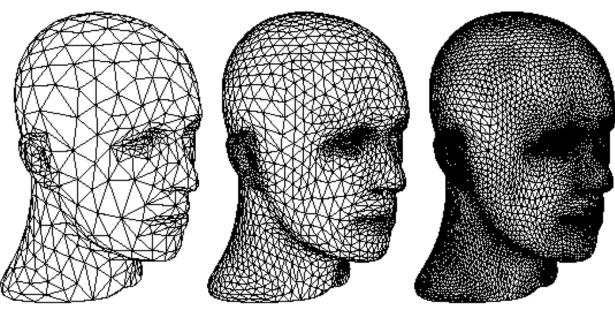


Stanford Graphics Laboratory

Subdivision Surface

Coarse mesh & subdivision rule

• Smooth surface is limit of sequence of refinements



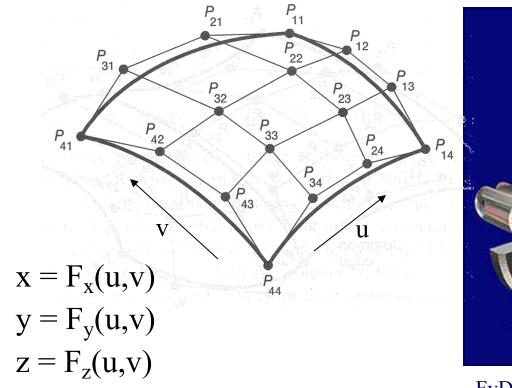
Zorin & Schroeder SIGGRAPH 99 Course Notes



Parametric Surface

Tensor-product spline patches

- Each patch is parametric function
- Careful constraints to maintain continuity



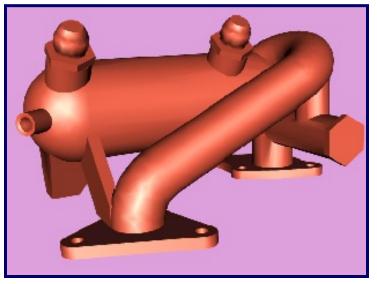




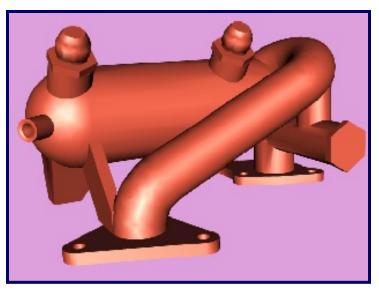
Implicit Surface



Set of all points satisfying: F(x,y,z) = 0



Polygonal Model



Implicit Model

Bill Lorensen SIGGRAPH 99 Course #4 Notes

3D Object Representations

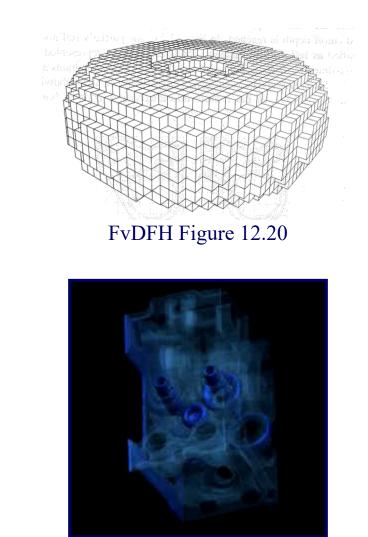
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Voxel grid

Uniform volumetric grid of samples:

- Occupancy (object vs. empty space)
- Density
- Color
- Other function (speed, temperature, etc.)
- Often acquired via simulation or from CAT, MRI, etc.





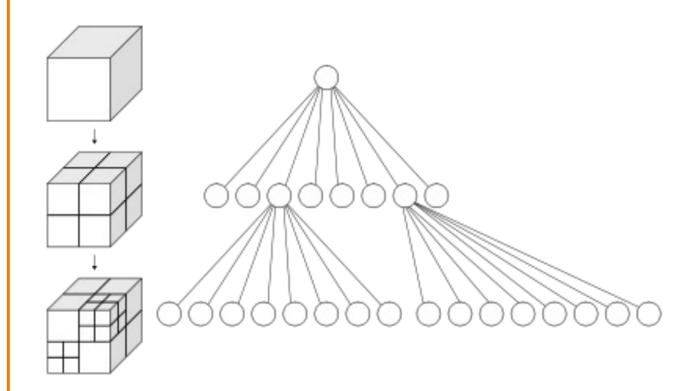


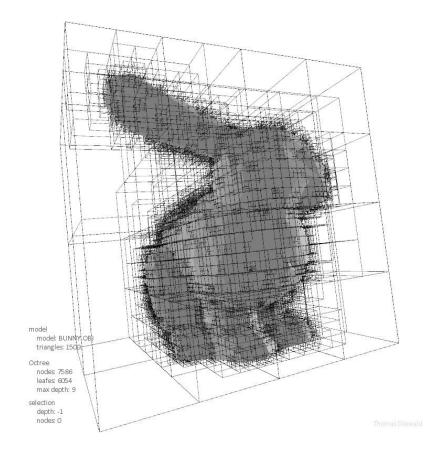
Octree



The adaptive version of the voxel grid

- Significantly more space efficient
- Makes operations more cumbersome





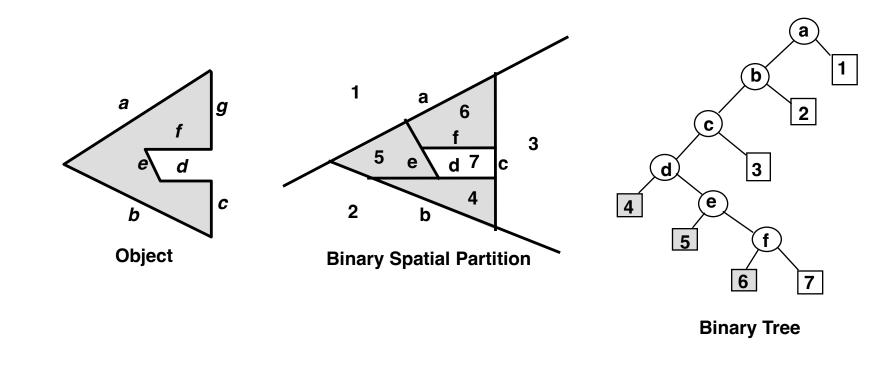
Thomas Diewald

BSP Tree



Hierarchical Binary Space Partition with solid/empty cells labeled

Constructed from polygonal representations

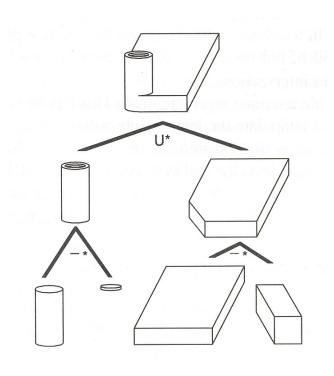


Naylor

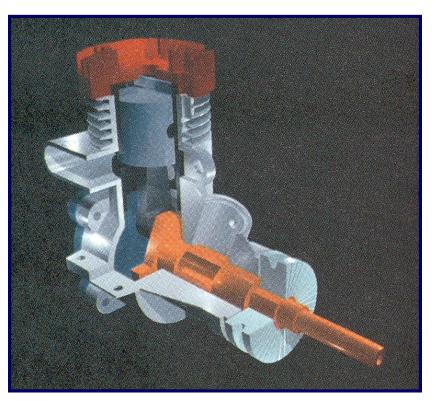
CSG



Constructive Solid Geometry: set operations (union, difference, intersection) applied to simple shapes



FvDFH Figure 12.27

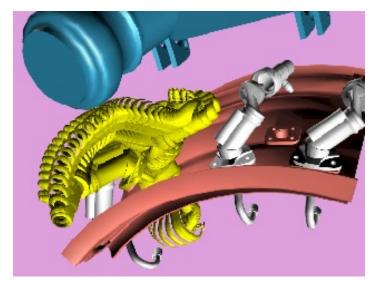


H&B Figure 9.9

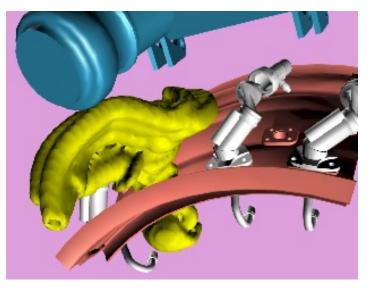




Solid swept by curve along trajectory



Removal Path



Sweep Model

Bill Lorensen SIGGRAPH 99 Course #4 Notes

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Scene Graph



Union of objects at leaf nodes



Bell Laboratories

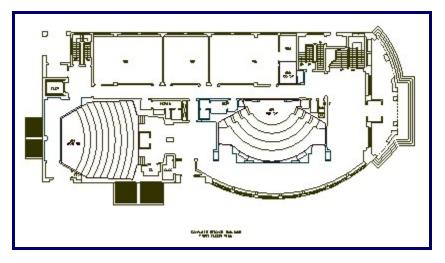


avalon.viewpoint.com

Application Specific

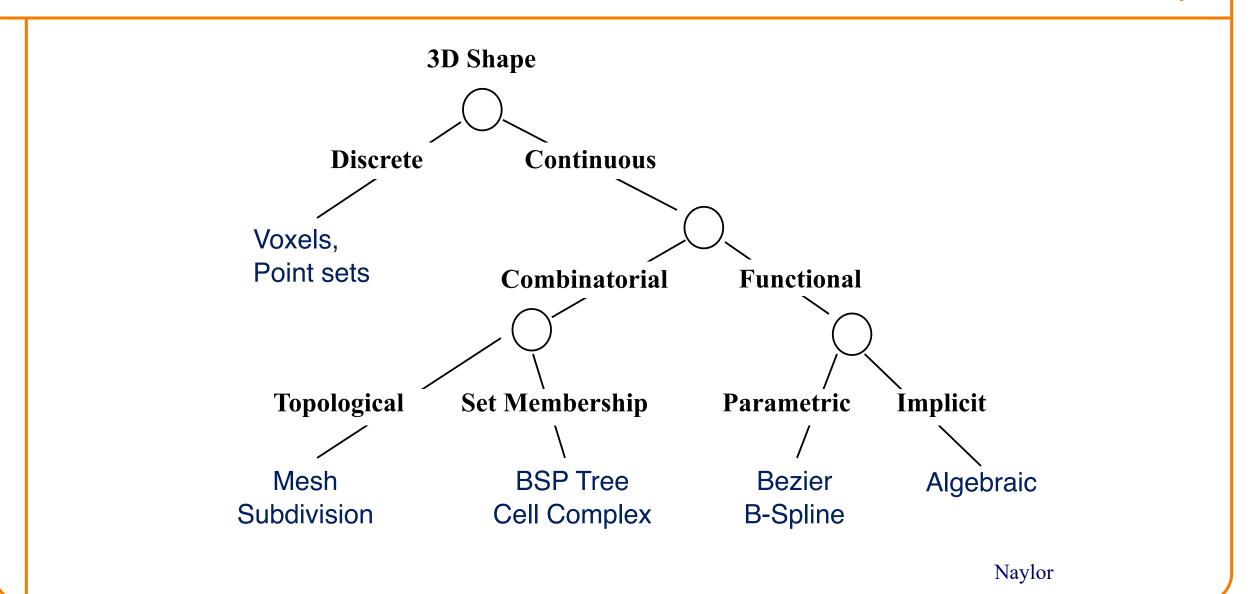


Apo A-1 (Theoretical Biophysics Group, University of Illinois at Urbana-Champaign)



Architectural Floorplan (CS Building, Princeton University)

Taxonomy of 3D Representations



Equivalence of Representations



- Thesis:
 - Each representation has enough expressive power to model the shape of any geometric object
 - It is possible to perform all geometric operations with any representation
- Analogous to Turing-equivalence
 - Computers and programming languages are Turing-equivalent, but each has its benefits...

Computational Differences

- Efficiency
 - Representational complexity (e.g. surface vs. volume)
 - $\circ~$ Computational complexity (e.g. $O(n^2)~vs~O(n^3)$)
 - Space/time trade-offs (e.g. tree data structures)
 - Numerical accuracy/stability (e.g. degree of polynomial)
- Simplicity
 - Ease of acquisition
 - Hardware acceleration
 - Software creation and maintenance
- Usability
 - Designer interface vs. computational engine

Upcoming Lectures

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