

COS 217: Introduction to Programming Systems

Virtual Memory and Caching



PRINCETON UNIVERSITY

Agenda



Virtual Memory

Virtual vs. physical memory

Page tables

Page faults



Storage and Locality

The storage hierarchy

Spatial and temporal locality

Caching



Effective Caching

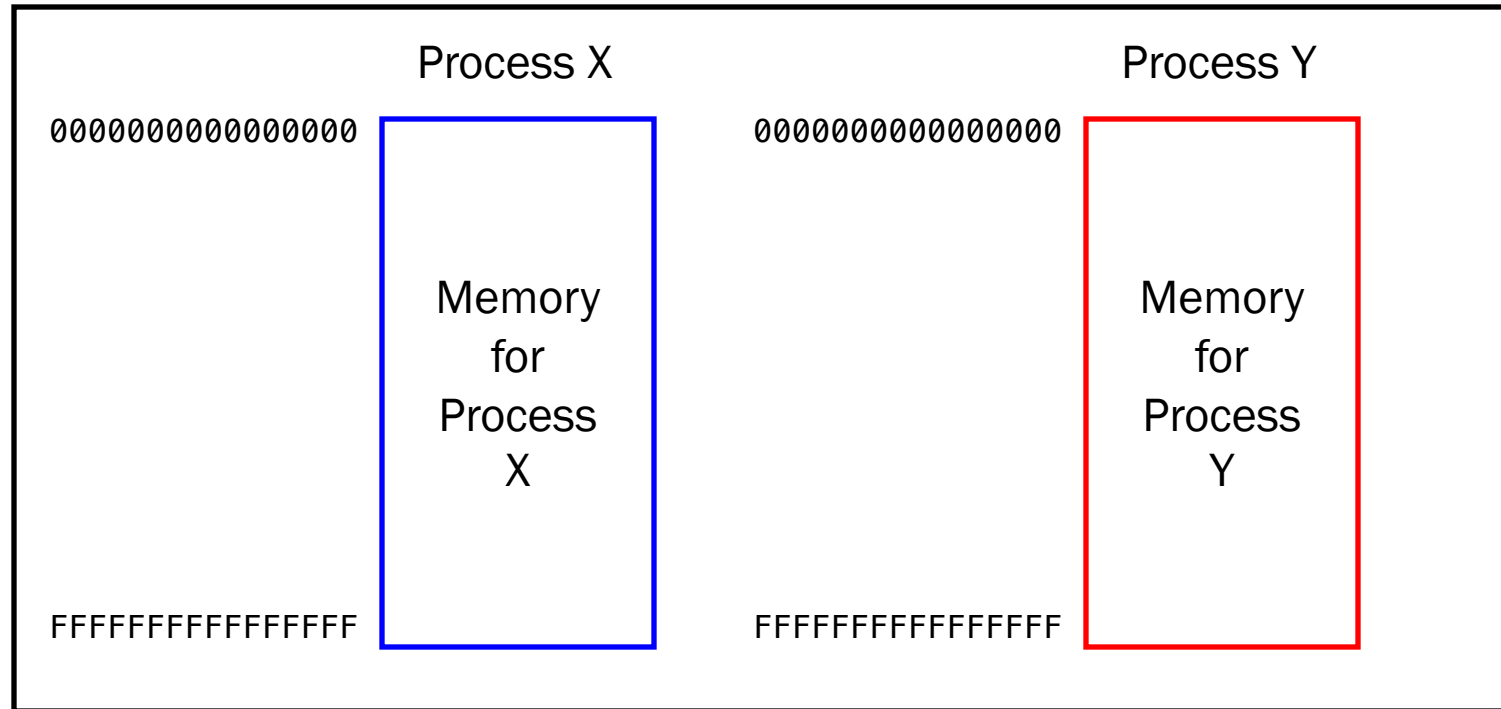
Block size

Eviction policy

Order of operations



Private Address Space: Illusion



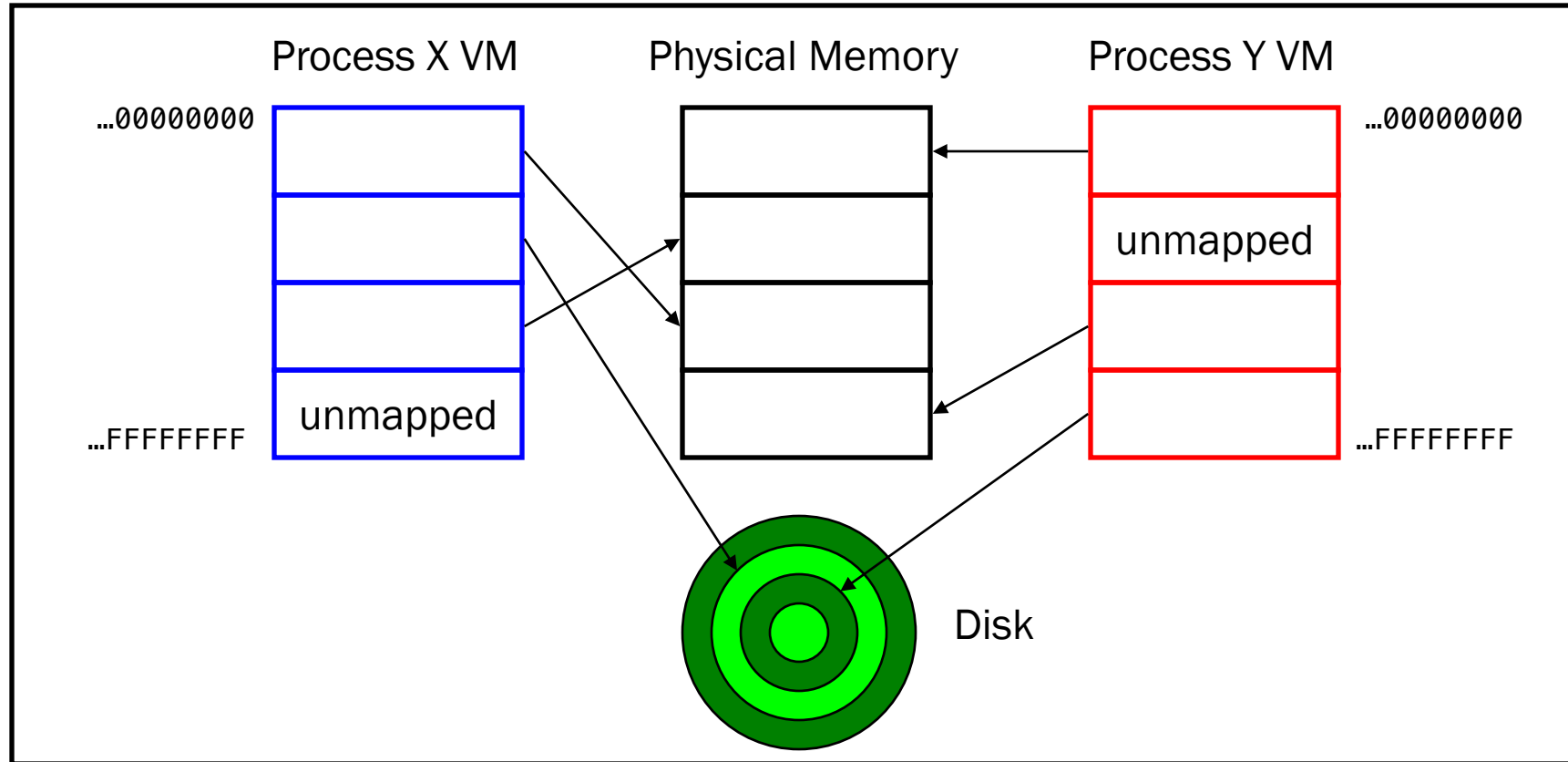
Each process sees main memory as

Huge: $2^{64} = 16$ EB (16 exabytes) of memory $\approx 10^{19}$ bytes

Uniform: contiguous memory locations from 0 to $2^{64}-1$



Private Address Space: Reality



Memory is divided into **pages**

- At any time, some pages are in physical memory, some on disk
- OS and hardware swap pages between physical memory and disk
- Multiple processes share physical memory



Virtual & Physical Addresses

Question

- How do OS and hardware implement virtual memory?

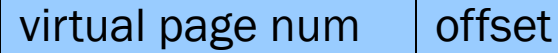
Answer (part 1)

- Distinguish between **virtual addresses** and **physical addresses**



Virtual & Physical Addresses (cont.)

Virtual address



- Identifies a location in a particular process's virtual memory
 - Independent of size of physical memory
 - Independent of other concurrent processes
- Consists of virtual page number & offset
- Used by **application programs**

Physical address



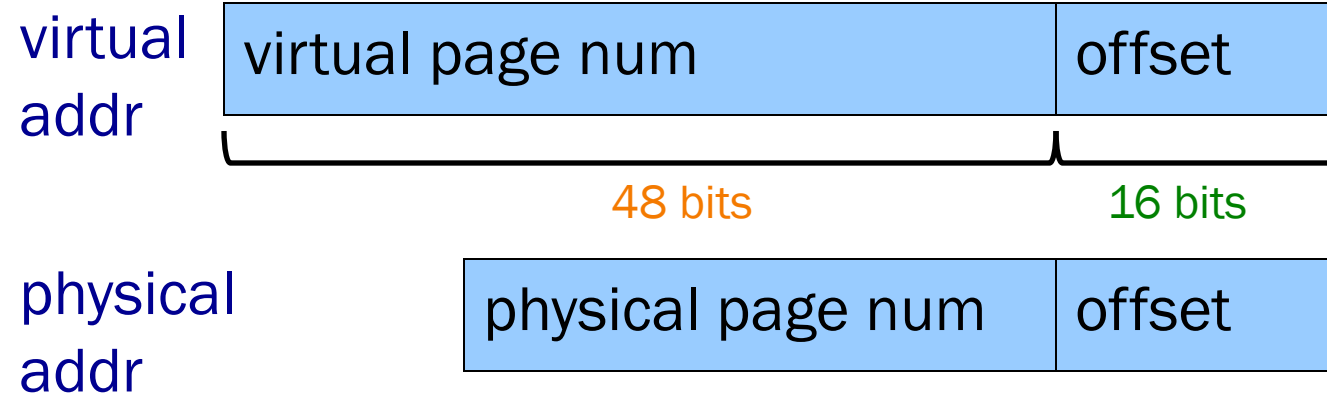
- Identifies a location in physical memory
- Consists of physical page number & offset
- Known only to **OS** and **hardware**

Note:

- Offset is same in virtual addr and corresponding physical addr



ArmLab Virtual & Physical Addresses

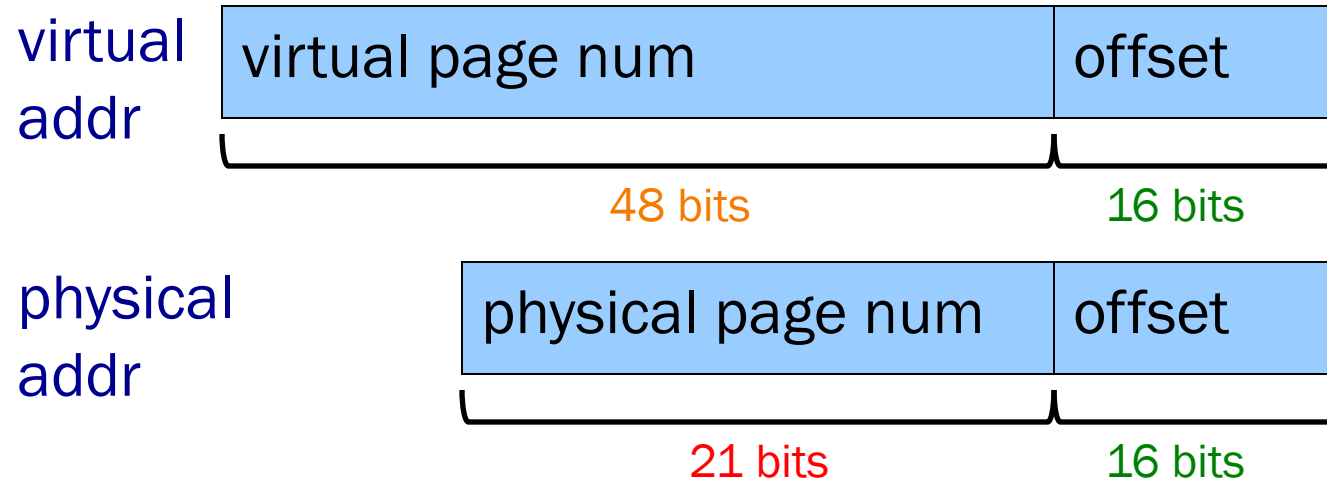


On ArmLab:

- Each virtual address consists of 64 bits
 - There are 2^{64} bytes of virtual memory (per process)
- Each offset is 16 bits
 - Each page consists of 2^{16} bytes
- Each virtual page number consists of $64 - 16 = 48$ bits
 - There are 2^{48} virtual pages



ArmLab Virtual & Physical Addresses



On ArmLab:

- Each physical address consists of 37 bits
 - There are 2^{37} (128G) bytes of physical memory (per computer)
- Each offset is 16 bits
 - Each page consists of 2^{16} bytes
- Each physical page number consists of $37 - 16 = 21$ bits
 - There are 2^{21} physical pages



Page Tables

Question

- How do OS and hardware implement virtual memory?

Answer (part 2)

- Maintain a **page table** for each process (stored in physical memory)



Page Tables (cont.)

Page Table for Process 1234

Virtual Page Num	Physical Page Num or Disk Addr
0	Physical page 5
1	(unmapped)
2	Spot X on disk
3	Physical page 8

...

...

Page table maps each in-use virtual page to:

- A physical page, or
- A spot on disk



Private Address Space Example 1

- Process executes instruction that references virtual memory
- CPU determines virtual page
- CPU checks if required virtual page is in physical memory: **yes**
- CPU does load/store from/to physical memory



Private Address Space Example 2

- Process executes instruction that references virtual memory
- CPU determines virtual page
- CPU checks if required virtual page is in physical memory: **no!**

Now what?



Page Faults

Question

- How do OS and hardware implement virtual memory?

Answer (part 3)

- Trigger a **page fault** for accesses to virtual pages that are swapped out (on disk)



Private Address Space Example 2

- Process executes instruction that references virtual memory
- CPU determines virtual page
- CPU checks if required virtual page is in physical memory: **no!**
 - CPU generates **page fault**
 - OS gains control of CPU
 - OS (potentially) evicts some page from physical memory to disk, loads required page from disk to physical memory
 - OS returns control of CPU to process – to **same instruction**
- Process executes instruction that references virtual memory
- CPU checks if required virtual page is in physical memory: **yes**
- CPU does load/store from/to physical memory

Virtual memory enables the illusion of private address spaces



VM Effects on Security and Speed



Q: What effect does virtual memory have on the security and speed of processes?

	Security	Speed
A.		
B.		
C.		
D.		

Let's start by considering security...



Consequences of Virtual Memory

Memory protection among processes

- Process's page table references only physical memory pages that the process currently owns
- Process can't accidentally/maliciously affect physical memory used by another process

Memory protection within processes

- Permission bits in page-table entries indicate whether page is read-only, etc.
- Allows CPU to prohibit
 - Writing to RODATA & TEXT sections
 - Access to protected (OS owned) virtual memory



VM Effects on Security and Speed



Q: What effect does virtual memory have on the security and speed of processes?

	Security	Speed
A.		
B.		
C.		
D.		

OK, so part of the answer is:

Security



But what about speed?



Consequences of Virtual Memory

Context switching

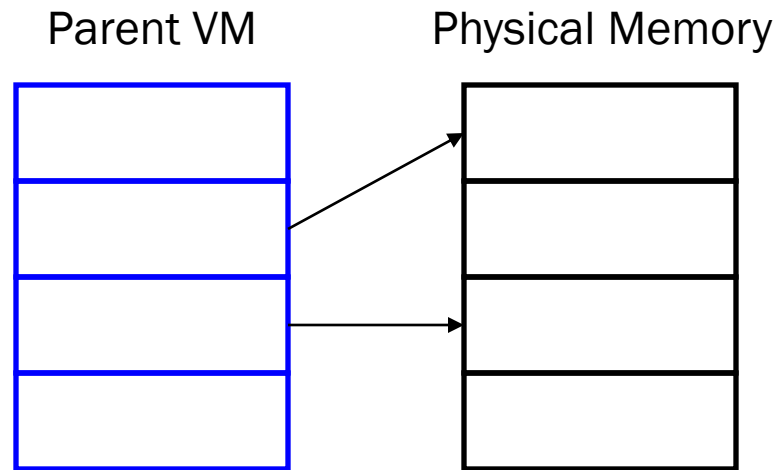
- **Illusion:** To context switch from process X to process Y, OS must save contents of registers **and memory** for process X, and restore contents of registers **and memory** for process Y
- **Reality:** To context switch from process X to process Y, OS must save contents of registers **and virtual memory** for process X, and restore contents of registers **and virtual memory** for process Y
- **Implementation:** To context switch from process X to process Y, OS must save contents of registers **and pointer to the page table** for process X, and restore contents of registers **and pointer to the page table** for process Y



Consequences of Virtual Memory

Creating new processes

- Efficient for a parent to `fork()` a new child process

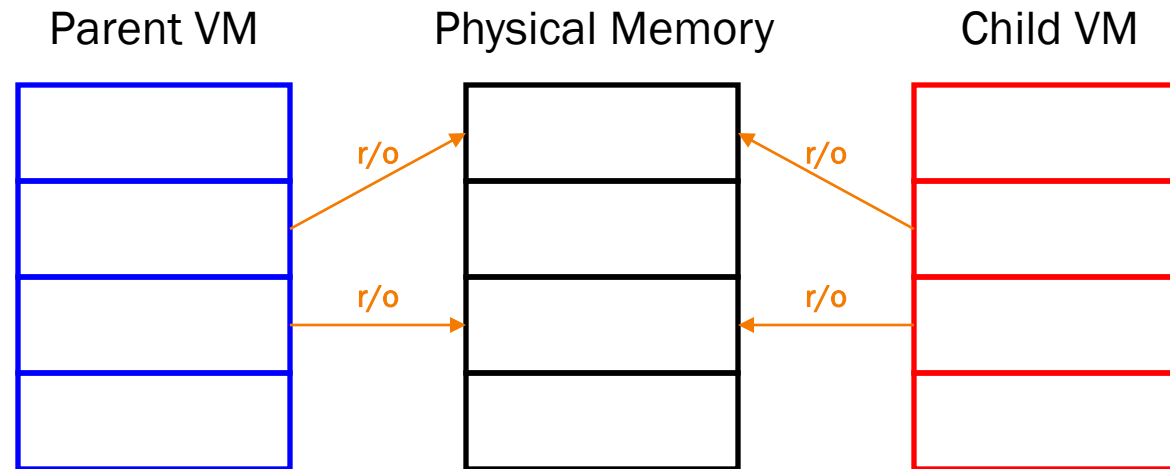




Consequences of Virtual Memory

Creating new processes

- Efficient for a parent to `fork()` a new child process
 - **Initially:** copy parent's page table to child, mark both parent and child pages **read-only**

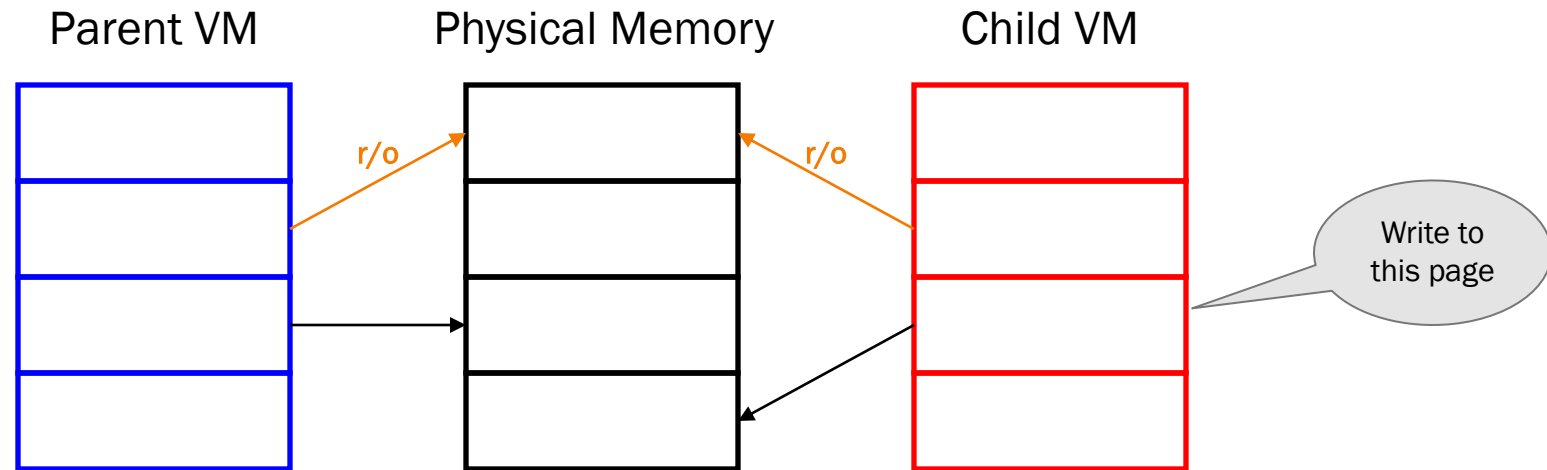




Consequences of Virtual Memory

Creating new processes

- Efficient for a parent to `fork()` a new child process
 - **Initially:** copy parent's page table to child, mark both parent and child pages read-only
 - **Incrementally:** when parent or child writes to page, page fault handler creates private copies





Consequences of Virtual Memory

Overwriting one program with another

- Easy for a process to `execvp()` another program
 - **Initially:** set page table entries to point to program pages that already exist on disk!
 - **Incrementally:** page fault handler swaps pages into memory as required



Consequences of Virtual Memory

*But if we're thinking about efficiency, isn't that all outweighed by the need to do **multiple** physical memory accesses (including page tables) for every virtual access?*

Conceptually, umm, yes. But it's not so bad in reality!



Agenda



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Page faults



Storage and Locality

The storage hierarchy

Spatial and temporal locality

Caching



Effective Caching

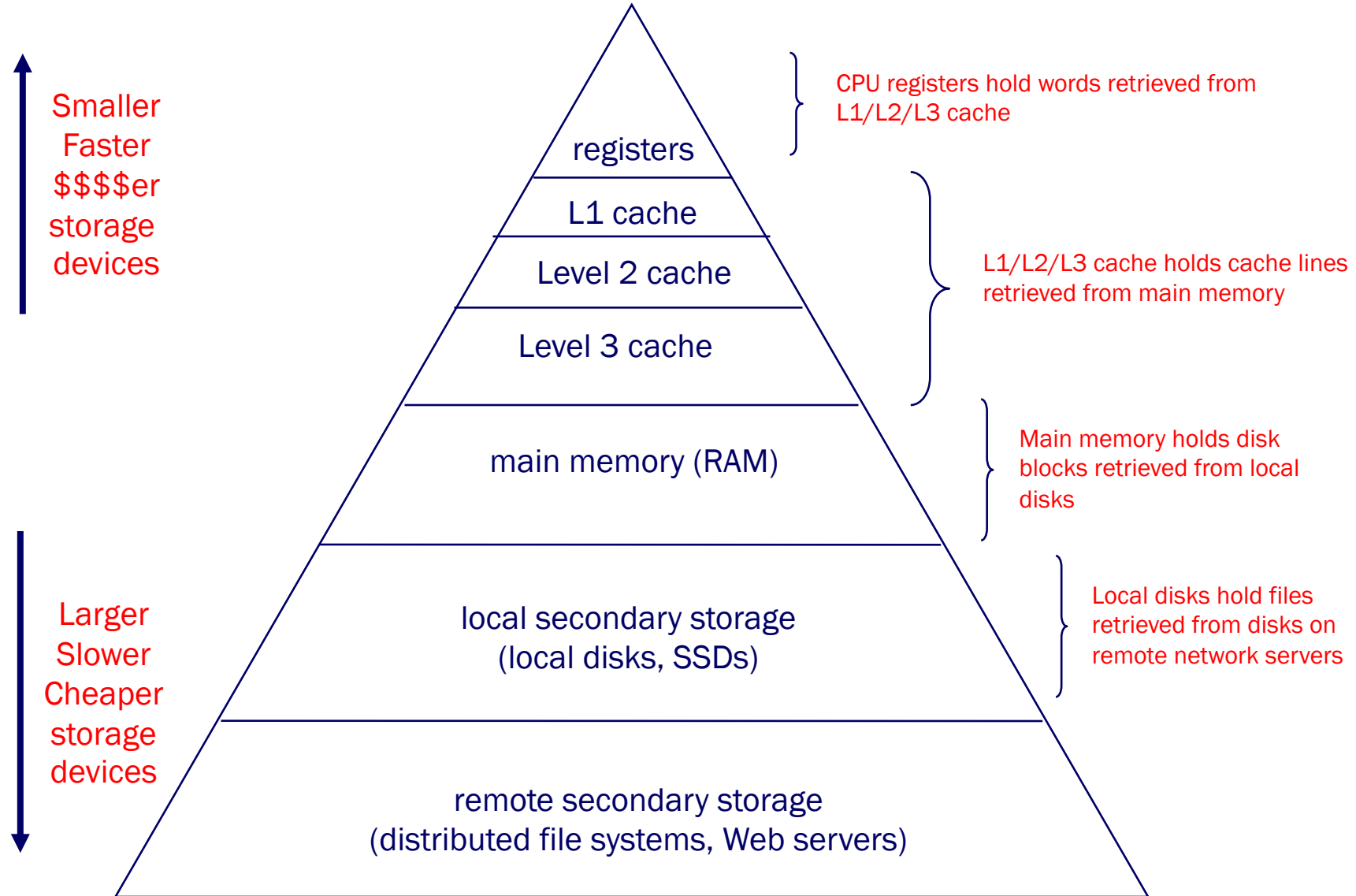
Block size

Eviction policy

Order of operations



Typical Storage Hierarchy





Typical Storage Hierarchy

Factors to consider:

- Capacity
- Latency (how long to do a read)
- Bandwidth (how many bytes/sec can be read)
 - Weakly correlated to latency: reading 1 MB from a hard disk isn't much slower than reading 1 byte
- Volatility
 - Do data persist in the absence of power?



Typical Storage Hierarchy

Registers

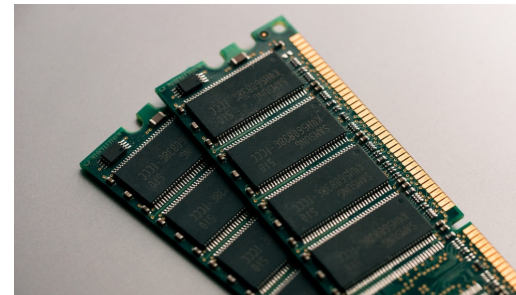
- **Latency:** 0 cycles
- **Capacity:** 8-256 registers (31 general purpose registers in AArch64)

L1/L2/L3 Cache

- **Latency:** 1 to 40 cycles
- **Capacity:** 32KB to 32MB

Main memory (RAM)

- **Latency:** ~ 50-100 cycles
 - 100 times slower than registers
- **Capacity:** GB





Typical Storage Hierarchy

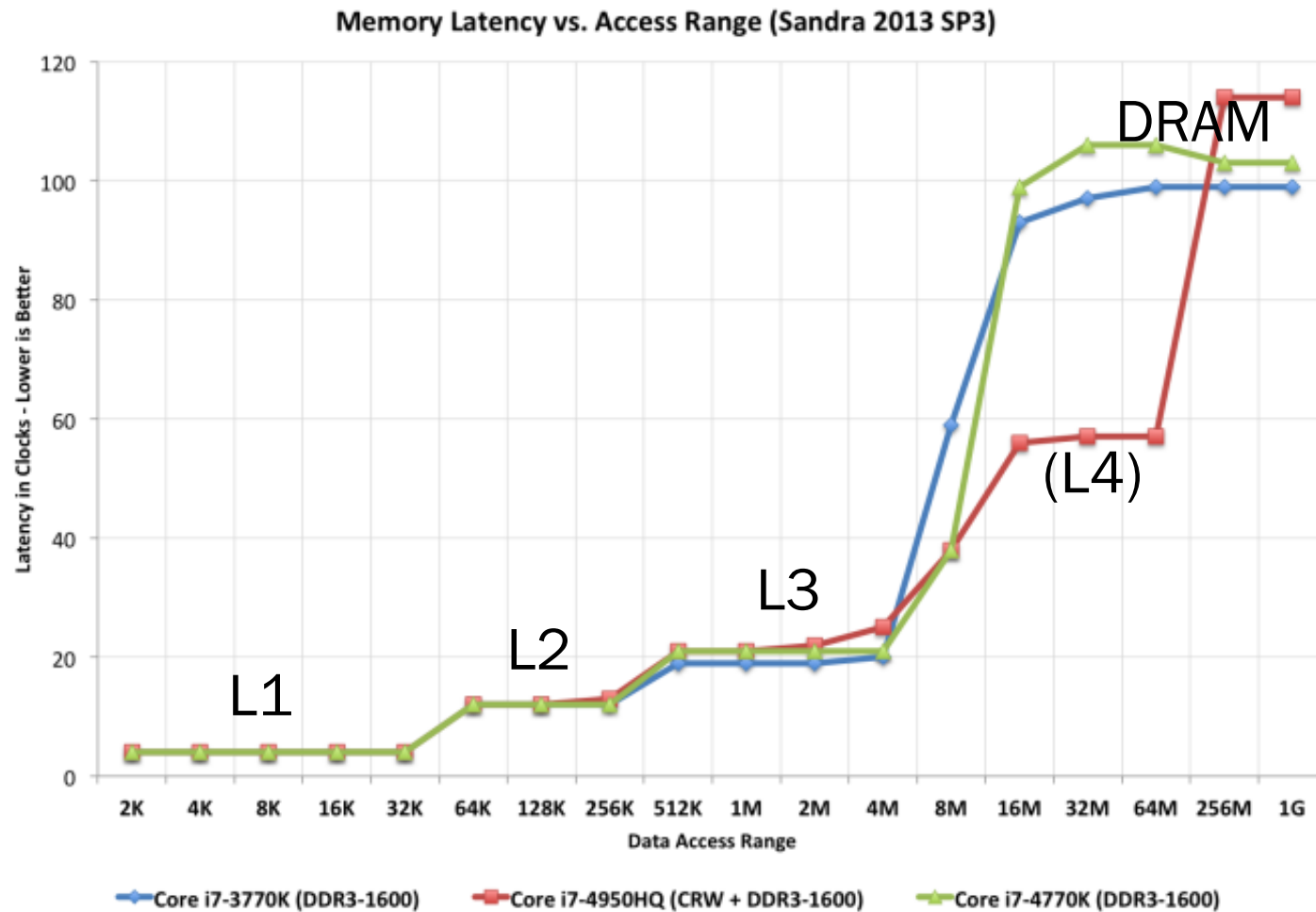
Local secondary storage: disk drives

- Solid-State Disk (SSD):
 - Flash memory (nonvolatile)
 - **Latency:** 0.1 ms (~ 300k cycles)
 - **Capacity:** 128 GB – 2 TB
- Hard Disk:
 - Spinning magnetic platters, moving heads
 - **Latency:** 10 ms (~ 30M cycles)
 - **Capacity:** 1 – 10 TB





Cache / RAM Latency



Disks



HDD



1 ms

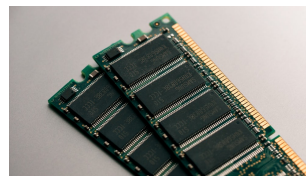
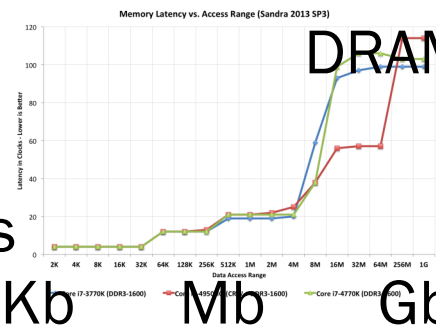
SSD



1 μ s

DRAM

1 ns



Kb

Mb

Gb

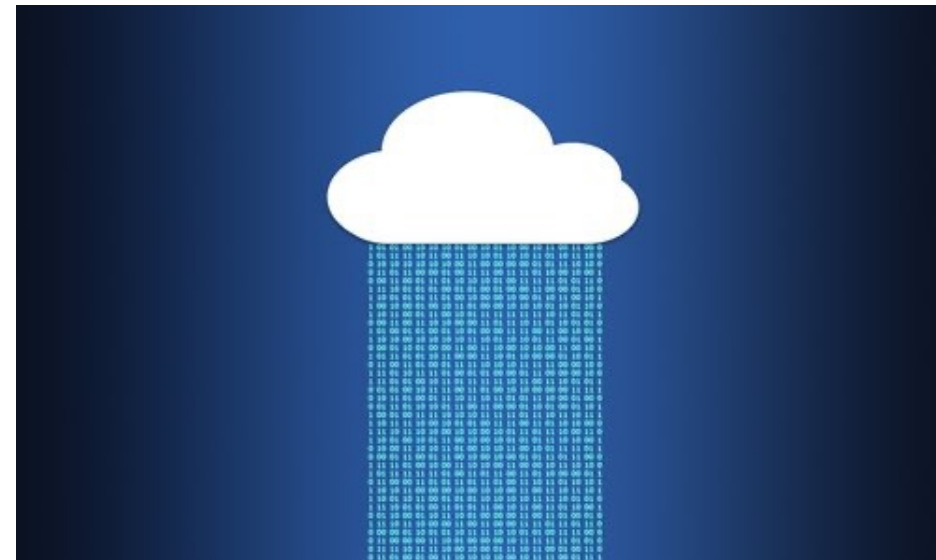
Tb



Typical Storage Hierarchy

Remote secondary storage (a.k.a. “the cloud”)

- **Latency:** tens of milliseconds
 - Limited by network bandwidth
- **Capacity:** essentially unlimited





Storage Device Speed vs. Size

Facts:

- CPU needs sub-nanosecond access to data to run instructions at full speed
- **Fast** storage (sub-nanosecond) is small (100-1000 bytes)
- **Big** storage (gigabytes) is slow (15 nanoseconds)
- **Huge** storage (terabytes) is *glacially* slow (milliseconds)

Goal:

- Need many gigabytes of memory,
- but with fast (sub-nanosecond) average access time

Solution: **locality** allows **caching**

- Most programs exhibit good **locality**
- A program that exhibits good locality will benefit from proper **caching**, which enables good **average** performance

Locality



Two kinds of **locality**

- **Temporal** locality
 - If a program references item X now,
then it probably will reference X again soon
- **Spatial** locality
 - If a program references item X now,
then it probably will reference item at address $X \pm 1$ soon

Most programs exhibit good temporal and spatial locality



Locality Example

Locality example

```
sum = 0;  
for (i = 0; i < n; i++)  
    sum += a[i];
```

Typical code
(good locality)

Temporal locality

- *Data:* Whenever the CPU accesses `sum`, it accesses `sum` again shortly thereafter
- *Instructions:* Whenever the CPU executes `sum += a[i]`, it executes `sum += a[i]` again shortly thereafter

Spatial locality

- *Data:* Whenever the CPU accesses `a[i]`, it accesses `a[i+1]` shortly thereafter
- *Instructions:* Whenever the CPU executes `sum += a[i]`, it executes `i++` shortly thereafter

Caching



Cache

- Fast access, small capacity storage device
- Acts as a staging area for a subset of the items in a slow access, large capacity storage device

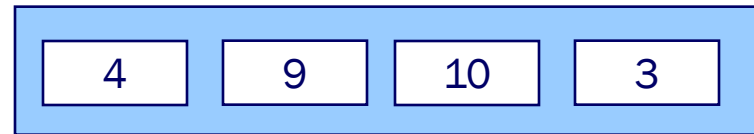
Good locality + proper caching

- ⇒ Most storage accesses can be satisfied by cache
- ⇒ Overall storage performance improved



Caching in a Storage Hierarchy

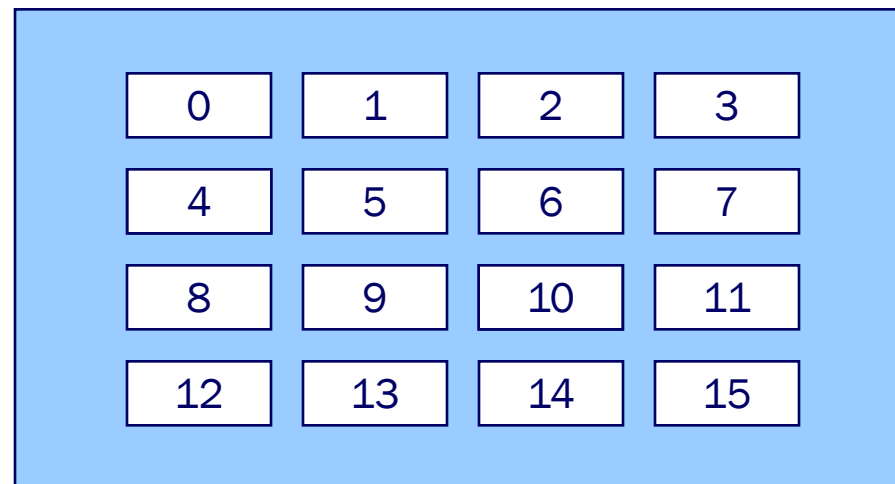
Level k:



Smaller, faster device at level k caches a subset of the blocks from level k+1

Blocks copied between levels

Level k+1:



Larger, slower device at level k+1 is partitioned into blocks



Cache Hits and Misses

Cache hit

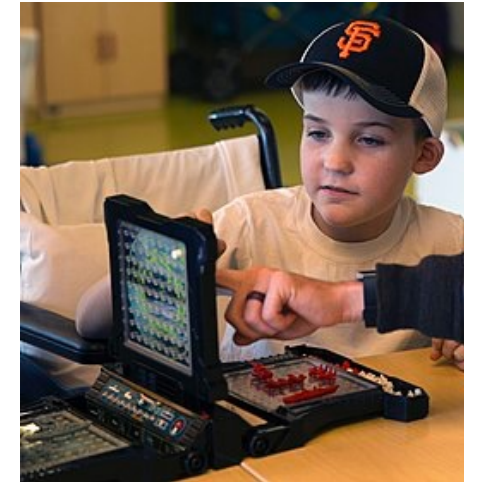
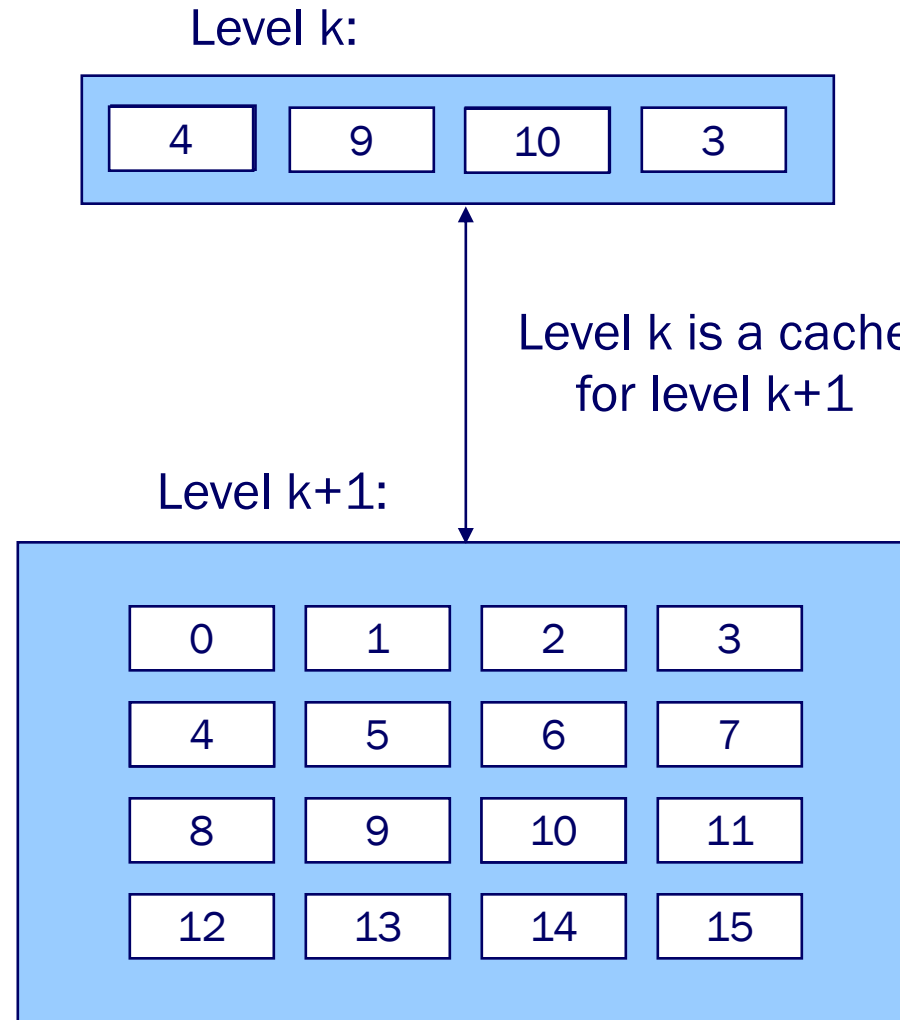
- E.g., request for block 10
- Access block 10 at level k
- Fast!

Cache miss

- E.g., request for block 8
- **Evict** some block from level k
- Load block 8 from level k+1 to level k
- Access block 8 at level k
- Slow!

Caching goal:

- Maximize cache hits
- Minimize cache misses





VM Effects on Security and Speed



Q: What effect does virtual memory have on the security and speed of processes?

	Security	Speed
A.		
B.		
C.		
D.		

So, with caching, we *finally* arrive at the answer:

Security	Speed
	no change



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Block size

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Do Exam Questions Exhibit Temporal Locality?



Here's a real question from an old exam:

For caching in a memory hierarchy,
what is the best motivation for a *larger* cache block size?

A. Temporal Locality

B. Spatial Locality

C. Both

D. Neither

B

Spatial locality makes use of subsequent data after a given read, so having more data to keep reading is a win.



Cache Block Size

Large block size:

- + do data transfer less often
- + take advantage of spatial locality
- longer time to complete data transfer
- less advantage of temporal locality

Small block size: the opposite

Typical: Lower in pyramid \Rightarrow slower data transfer \Rightarrow larger block sizes

Device	Block Size
Register	8 bytes
L1/L2/L3 cache line	128 bytes
Main memory page	4KB or 64KB
Disk block	512 bytes to 4KB
Disk transfer block	4KB (4096 bytes) to 64MB (67108864 bytes)

Cache Management



Device	Managed by:
Registers (cache of L1/L2/L3 cache and main memory)	Compiler, using complex code-analysis techniques Assembly lang programmer
L1/L2/L3 cache (cache of main memory)	Hardware, using simple algorithms
Main memory (cache of local sec storage)	Hardware and OS, using virtual memory with complex algorithms (since accessing disk is expensive)
Local secondary storage (cache of remote sec storage)	End user, by deciding which files to download



Cache Eviction Policies

Best eviction policy: “oracle”

- Always evict a block that is *never* accessed again, or...
- Always evict the block accessed the *furthest in the future*
- Impossible in the general case

Worst eviction policy

- Always evict the block that will be accessed next!
- Causes **thrashing**
- Impossible in the general case!



Cache Eviction Policies

Reasonable eviction policy: **LRU policy**

- Evict the “Least Recently Used” (LRU) block
 - With the assumption that it will not be used again (soon)
- Good for straight-line code
- (can be) bad for (large) loops
- Expensive to implement
 - Often simpler approximations are used
 - See Wikipedia “Page replacement algorithm” topic



Locality/Caching Example: Matrix Multiplication

Matrix multiplication

- Matrix = two-dimensional array
- Multiply n -by- n matrices A and B
- Store product in matrix C

Performance depends upon

- Effective use of caching (as implemented by **system**)
- Good locality (as implemented by **you**)



Locality/Caching Example: Matrix Mult

Two-dimensional arrays are stored in either **row-major** or **column-major** order

a	0	1	2
0	18	19	20
1	21	22	23
2	24	25	26

row-major		col-major	
a[0][0]	18	a[0][0]	18
a[0][1]	19	a[1][0]	21
a[0][2]	20	a[2][0]	24
a[1][0]	21	a[0][1]	19
a[1][1]	22	a[1][1]	22
a[1][2]	23	a[2][1]	25
a[2][0]	24	a[0][2]	20
a[2][1]	25	a[1][2]	23
a[2][2]	26	a[2][2]	26

C uses **row-major** order

- Access in row order \Rightarrow good spatial locality
- Access in column order \Rightarrow poor spatial locality

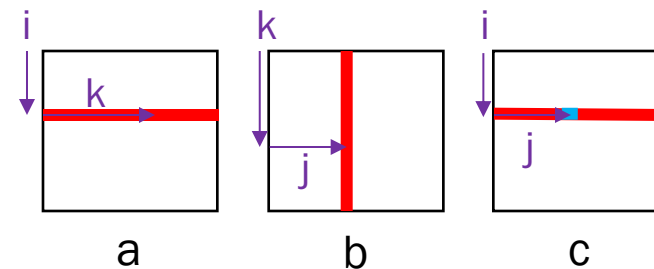


Locality/Caching Example: Matrix Mult

```
for (i=0; i<n; i++)  
  for (j=0; j<n; j++)  
    for (k=0; k<n; k++)  
      c[i][j] += a[i][k] * b[k][j];
```

Reasonable cache effects

- Good locality for A
- Bad locality for B
- Good locality for C



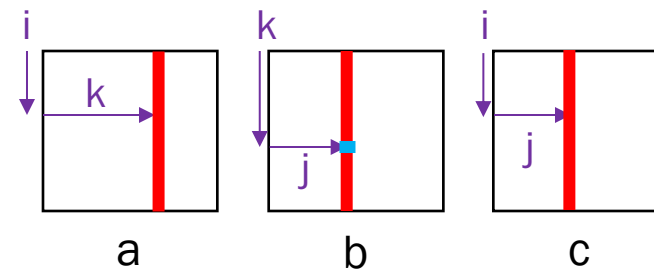


Locality/Caching Example: Matrix Mult

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```

Poor cache effects

- Bad locality for A
- Bad locality for B
- Bad locality for C



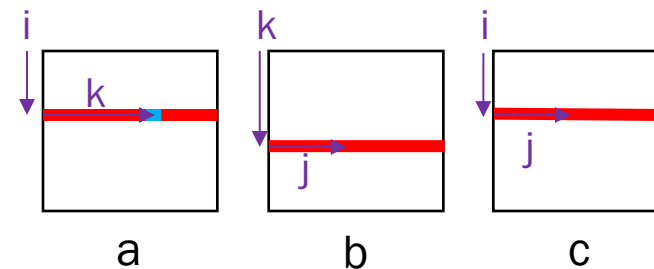


Locality/Caching Example: Matrix Mult

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      c[i][j] += a[i][k] * b[k][j];
```

Good cache effects

- Good locality for A
- Good locality for B
- Good locality for C





Another ghost of exams past ...



Suppose that C laid out arrays in column-major order instead of row-major order. What would be the *most efficient* loop ordering for matrix multiplication to maximize performance through good locality?

- A. i k j (Same as row-major)
- B. i j k
- C. j k i
- D. j i k
- E. k i j
- F. k j i

```
for (i=0; i<n; i++)  
  for (k=0; k<n; k++)  
    for (j=0; j<n; j++)  
      c[i][j] += a[i][k] * b[k][j];
```

C: j k i

Exactly what makes this bad for all three in row-major makes it ideal for column-major: a and c have good spatial b has good temporal, spatial



Next time ...

Getting started with ARM!

