



Introduction to Ocaml

Speaker: Andrew Appel

COS 326

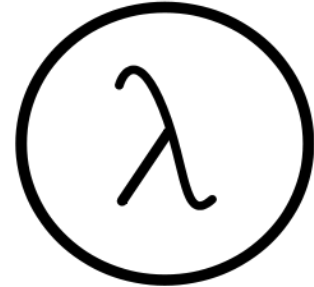
Princeton University



Why OCaml?

Small, orthogonal core based on the *lambda calculus*.

- Control is based on (recursive) functions.
- Instead of for-loops, while-loops, do-loops, iterators, etc.
 - can be defined as library functions.
- Makes it easy to define semantics



Supports *first-class, lexically scoped, higher-order* procedures

- a.k.a. first-class functions or closures or lambdas.
- **first-class**: functions are data values like any other data value
 - like numbers, they can be stored, defined anonymously, ...
- **lexically scoped**: meaning of variables determined statically.
- **higher-order**: functions as arguments and results
 - programs passed to programs; generated from programs

These features also found in Scheme, Haskell, Scala, F#, Clojure,



Why OCaml?

Statically typed: debugging and testing aid

- compiler catches many silly errors before you can run the code.
 - A type is worth a thousand tests
- Java is also strongly, statically typed.
- Scheme, Python, Javascript, etc. are all strongly, *dynamically typed* – type errors are discovered while the code is running.

Strongly typed: compiler enforces type abstraction.

- cannot cast an integer to a record, function, string, etc.
 - so we can utilize *types as capabilities*; crucial for local reasoning
- C/C++ are *weakly typed* (statically typed) languages. The compiler will happily let you do something smart (*more often stupid*).

Type inference: compiler fills in types for you



Integer Functor Ord Char
Either Monad
Bool Enum
Int [...] Ec
->
Num
Bounded
Integral () IO Sho
Maybe String Ratio Float

Installing, Running OCaml

- OCaml comes with compilers:
 - "ocamlc" – fast bytecode compiler
 - "ocamlopt" – optimizing, native code compiler
 - "ocamlbuild" – a nice wrapper that computes dependencies
- And an interactive, top-level shell:
 - useful for trying something out.
 - "ocaml" at the prompt.
 - *but use the compiler most of the time*
- And many other tools
 - e.g., debugger, dependency generator, profiler, etc.
- See the course web pages for installation pointers
 - also OCaml.org

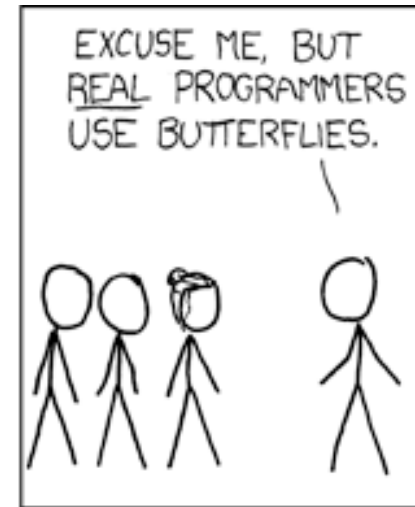
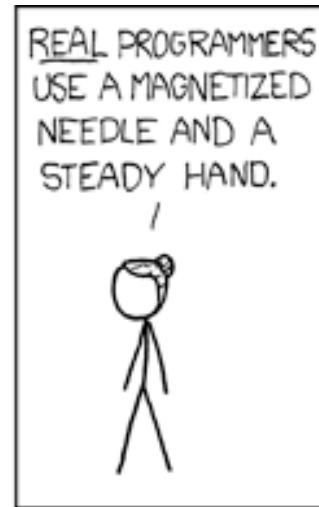
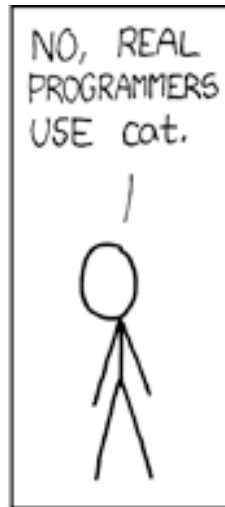
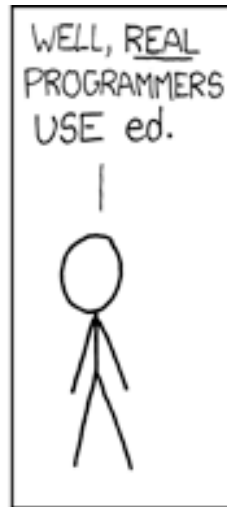
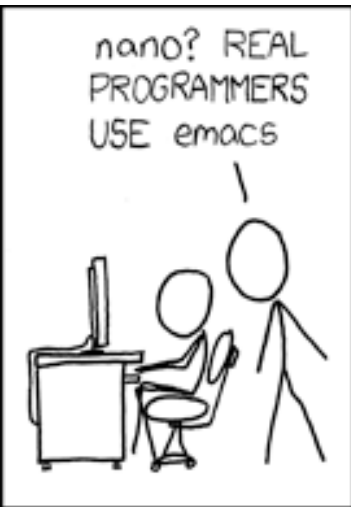


Editing OCaml Programs

- Many options: pick your own poison
 - Emacs
 - what your professors use
 - good but not great support for OCaml.
 - we like it because we're used to it
 - (extensions written in elisp – a functional language!)
 - OCaml IDE
 - integrated development environment written in OCaml.
 - haven't used it, so can't comment.
 - Eclipse
 - we've put up a link to an OCaml plugin
 - we haven't tried it but others recommend it
 - Sublime, atom
 - A lot of students seem to gravitate to this



XKCD on Editors

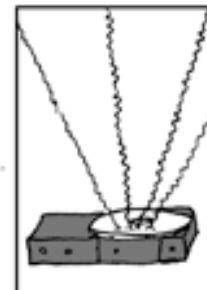
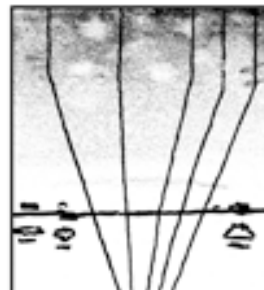


THE DISTURBANCE RIPPLES OUTWARD, CHANGING THE FLOW OF THE EDDY CURRENTS IN THE UPPER ATMOSPHERE.



THESE CAUSE MOMENTARY POCKETS OF HIGHER-PRESSURE AIR TO FORM,

WHICH ACT AS LENSES THAT DEFLECT INCOMING COSMIC RAYS, FOCUSING THEM TO STRIKE THE DRIVE PLATTER AND FLIP THE DESIRED BIT.

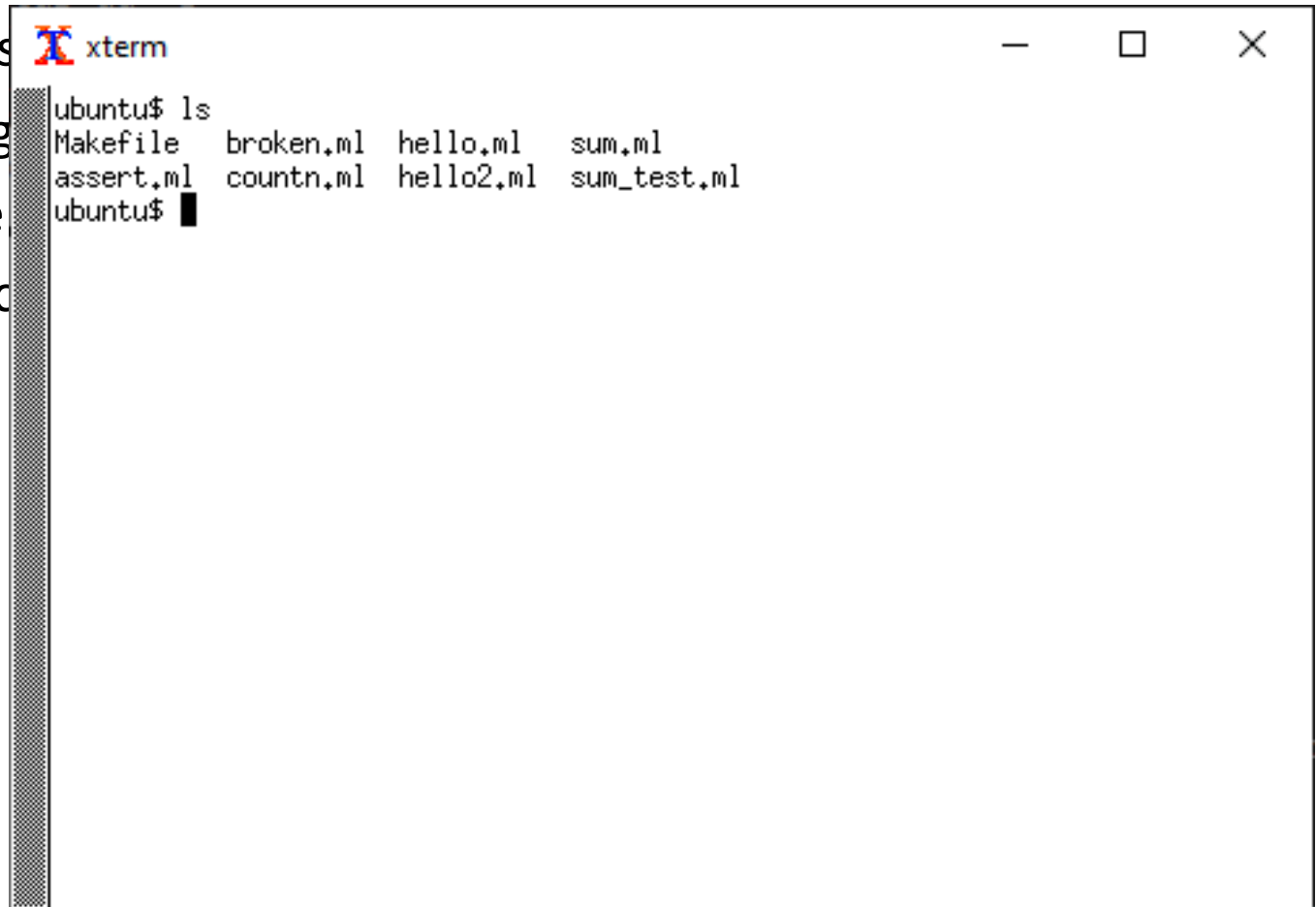


AN INTRODUCTORY EXAMPLE (OR TWO)



OCaml Compiler and Interpreter

- Demo:
 - emacs
 - ml files
 - writing
 - simple
 - ocamlc

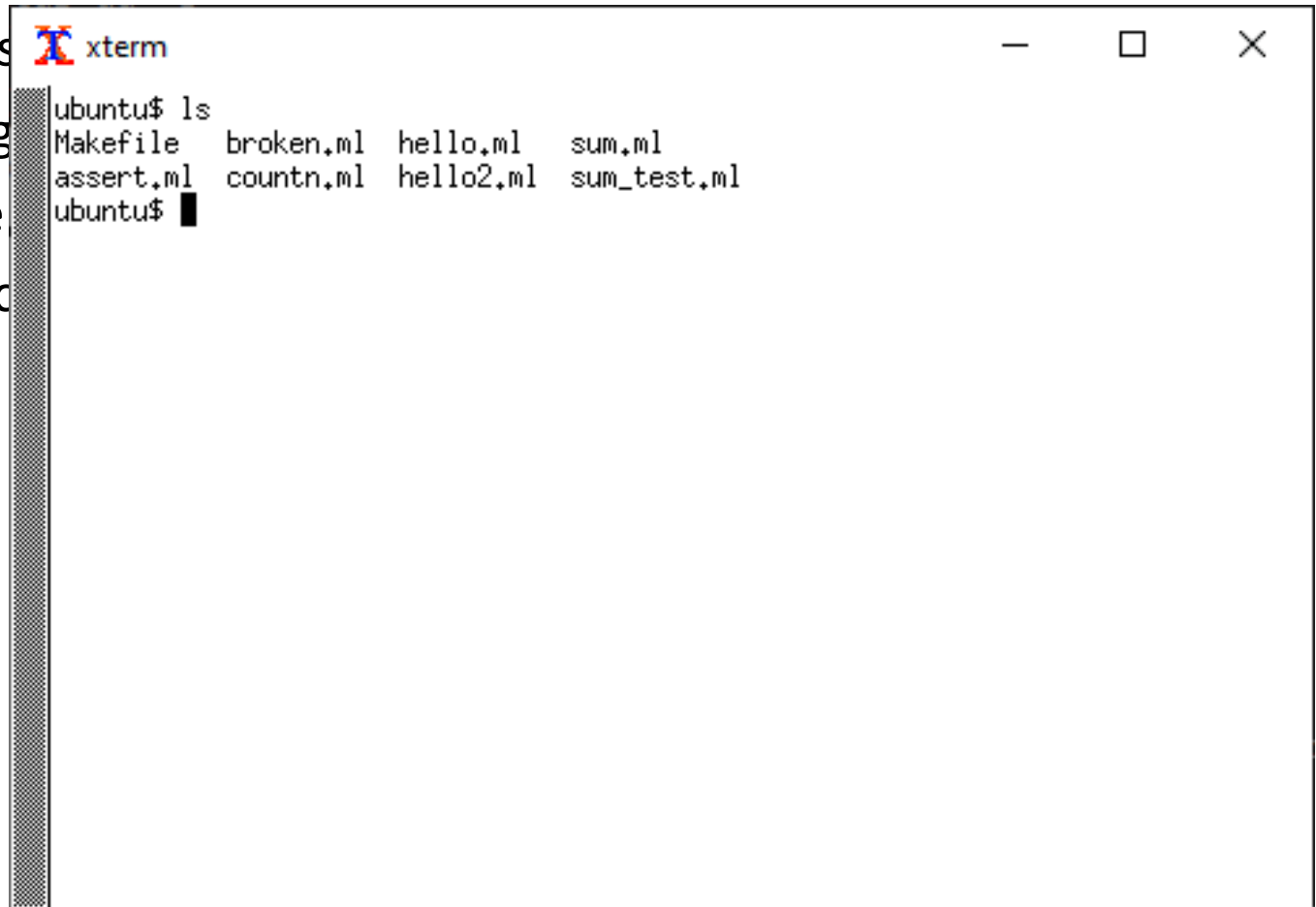


```
xterm
ubuntu$ ls
Makefile  broken.ml  hello.ml   sum.ml
assert.ml countn.ml  hello2.ml  sum_test.ml
ubuntu$
```



OCaml Compiler and Interpreter

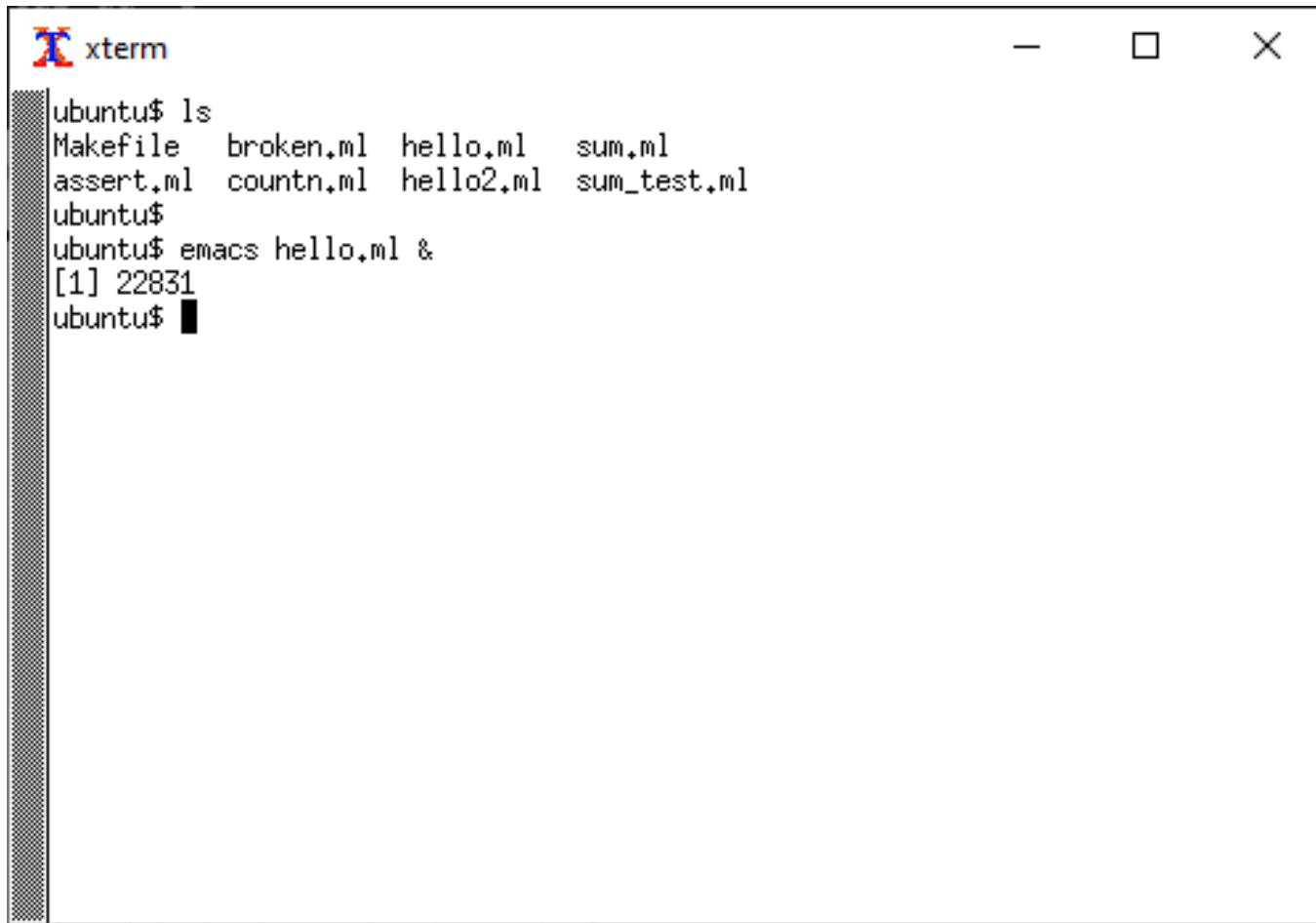
- Demo:
 - emacs
 - ml files
 - writing
 - simple
 - ocamlc



```
xterm
ubuntu$ ls
Makefile  broken.ml  hello.ml   sum.ml
assert.ml  countn.ml  hello2.ml  sum_test.ml
ubuntu$
```



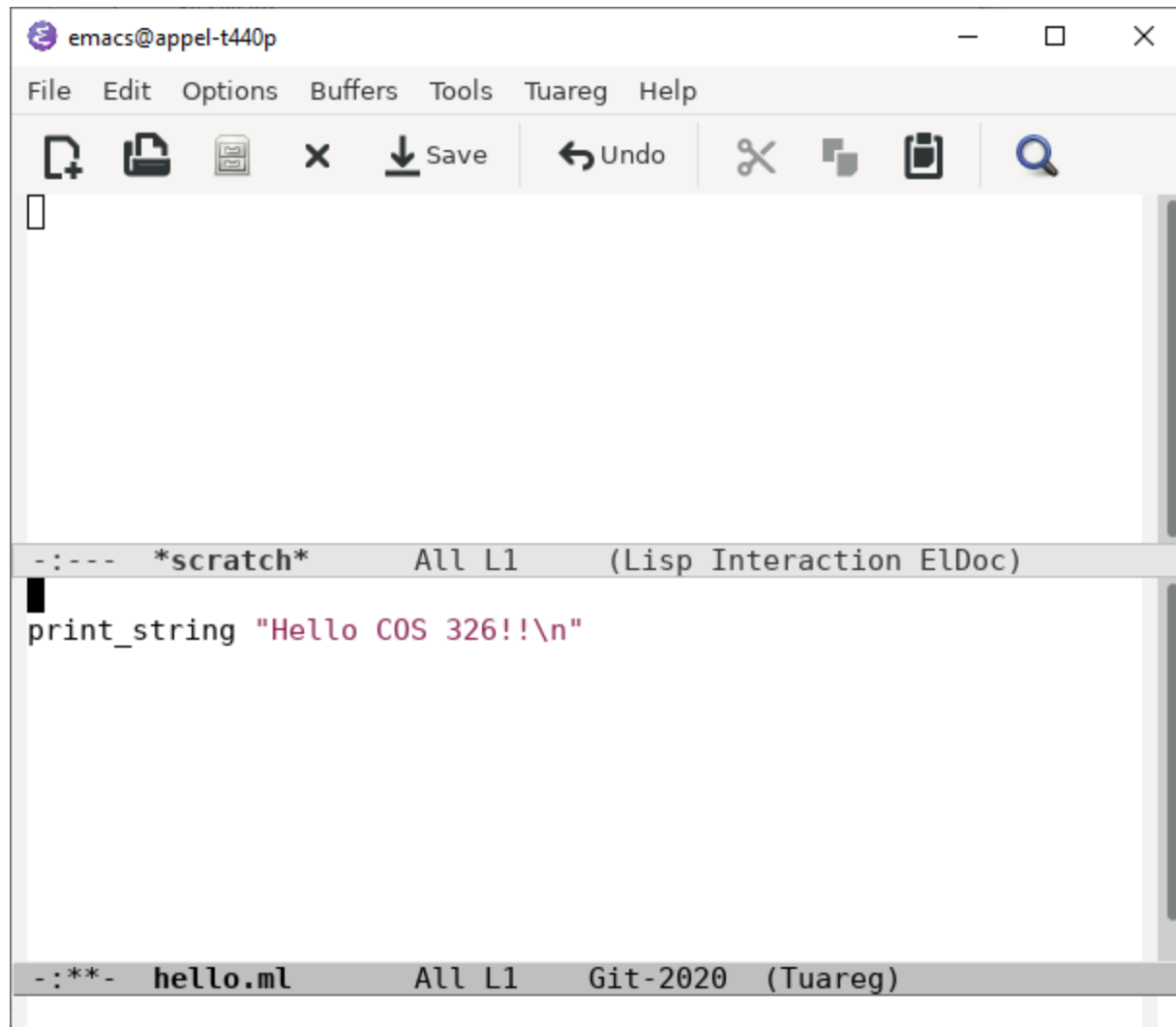
OCaml demo



```
xterm
ubuntu$ ls
Makefile  broken.ml  hello.ml  sum.ml
assert.ml  countrn.ml  hello2.ml  sum_test.ml
ubuntu$
ubuntu$ emacs hello.ml &
[1] 22831
ubuntu$ █
```



OCaml demo

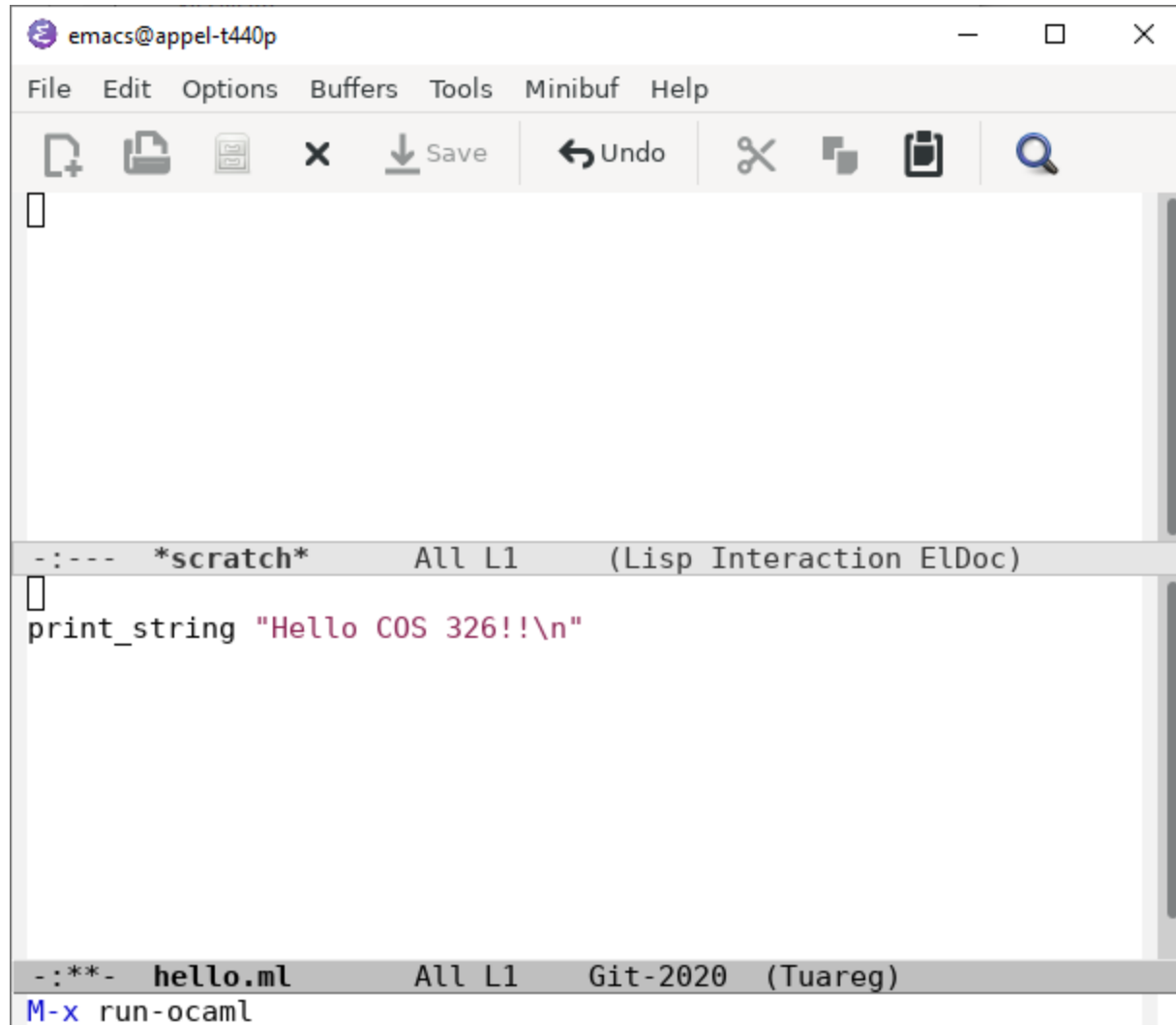


The image shows a screenshot of the Emacs text editor. The window title is "emacs@appel-t440p". The menu bar includes "File", "Edit", "Options", "Buffers", "Tools", "Tuareg", and "Help". The toolbar contains icons for opening a file, saving, undo, redo, and search. The main editing area is currently empty. At the bottom, there are two buffer tabs: "*scratch*" (All L1, (Lisp Interaction ElDoc)) and "hello.ml" (All L1, Git-2020 (Tuareg)). The "hello.ml" buffer is active and contains the OCaml code: `print_string "Hello COS 326!!\n"`.

```
emac...@appel-t440p  
File Edit Options Buffers Tools Tuareg Help  
[Icons: Open, Save, Undo, Redo, Search]  
[Empty editing area]  
-:--- *scratch* All L1 (Lisp Interaction ElDoc)  
print_string "Hello COS 326!!\n"  
-:***- hello.ml All L1 Git-2020 (Tuareg)
```



OCaml demo

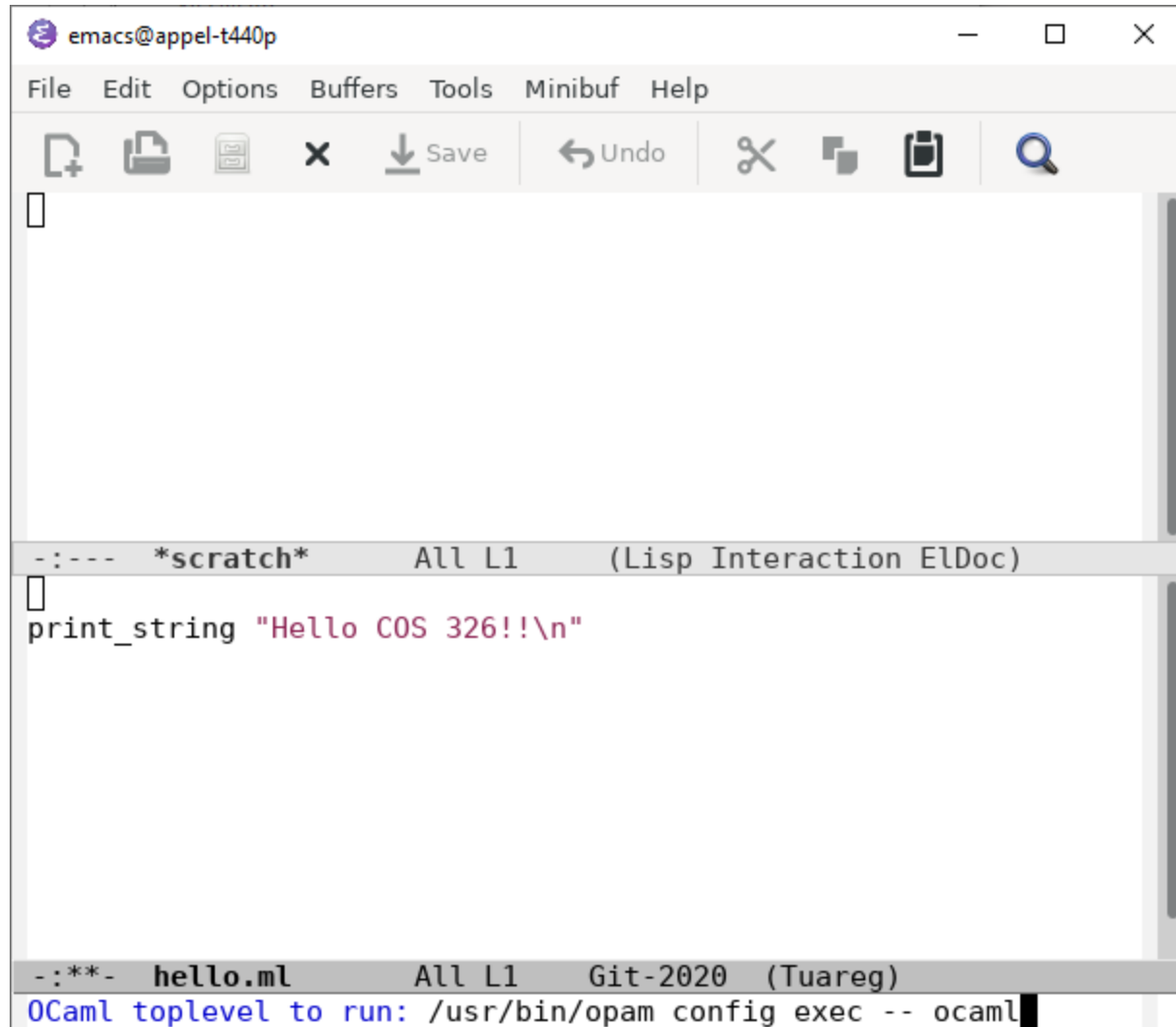


The image shows a screenshot of the Emacs text editor. The window title is "emacs@appel-t440p". The menu bar includes "File", "Edit", "Options", "Buffers", "Tools", "Minibuf", and "Help". The toolbar contains icons for opening a file, saving, undo, redo, copy, paste, and search. The main editing area is empty, with a cursor at the top left. Below the editing area, there are two buffer tabs. The top tab is titled "---- *scratch* All L1 (Lisp Interaction ElDoc)" and contains the OCaml code: `print_string "Hello COS 326!!\n"`. The bottom tab is titled ":-*- hello.ml All L1 Git-2020 (Tuareg)" and contains the command `M-x run-ocaml`.

```
emacs@appel-t440p
File Edit Options Buffers Tools Minibuf Help
[Icons: Open, Save, Undo, Redo, Copy, Paste, Search]
[]
-:--- *scratch* All L1 (Lisp Interaction ElDoc)
[]
print_string "Hello COS 326!!\n"
-:***- hello.ml All L1 Git-2020 (Tuareg)
M-x run-ocaml
```



OCaml demo

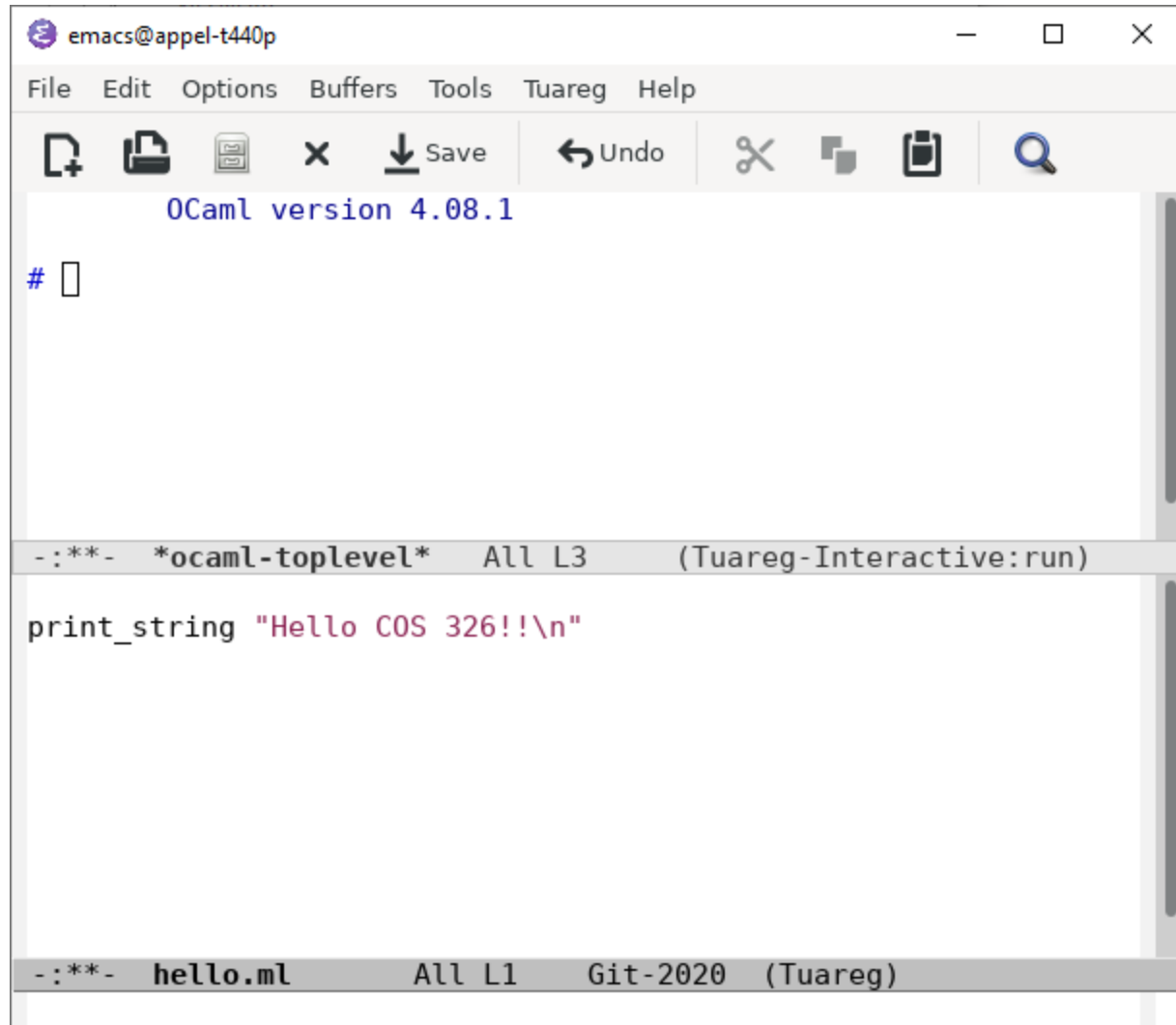


The image shows a screenshot of the Emacs text editor window. The title bar reads "emacs@appel-t440p". The menu bar includes "File", "Edit", "Options", "Buffers", "Tools", "Minibuf", and "Help". The toolbar contains icons for opening, saving, undo, redo, and search. The main editing area is empty. Below the editing area, there are two terminal-like buffers. The first buffer, titled "*scratch*", contains the OCaml code `print_string "Hello COS 326!!\n"`. The second buffer, titled "hello.ml", shows the command `OCaml toplevel to run: /usr/bin/opam config exec -- ocaml`.

```
emacs@appel-t440p
File Edit Options Buffers Tools Minibuf Help
[Icons: Open, Save, Undo, Redo, Search]
[]
-:--- *scratch* All L1 (Lisp Interaction ElDoc)
[]
print_string "Hello COS 326!!\n"
-:***- hello.ml All L1 Git-2020 (Tuareg)
OCaml toplevel to run: /usr/bin/opam config exec -- ocaml
```



OCaml demo

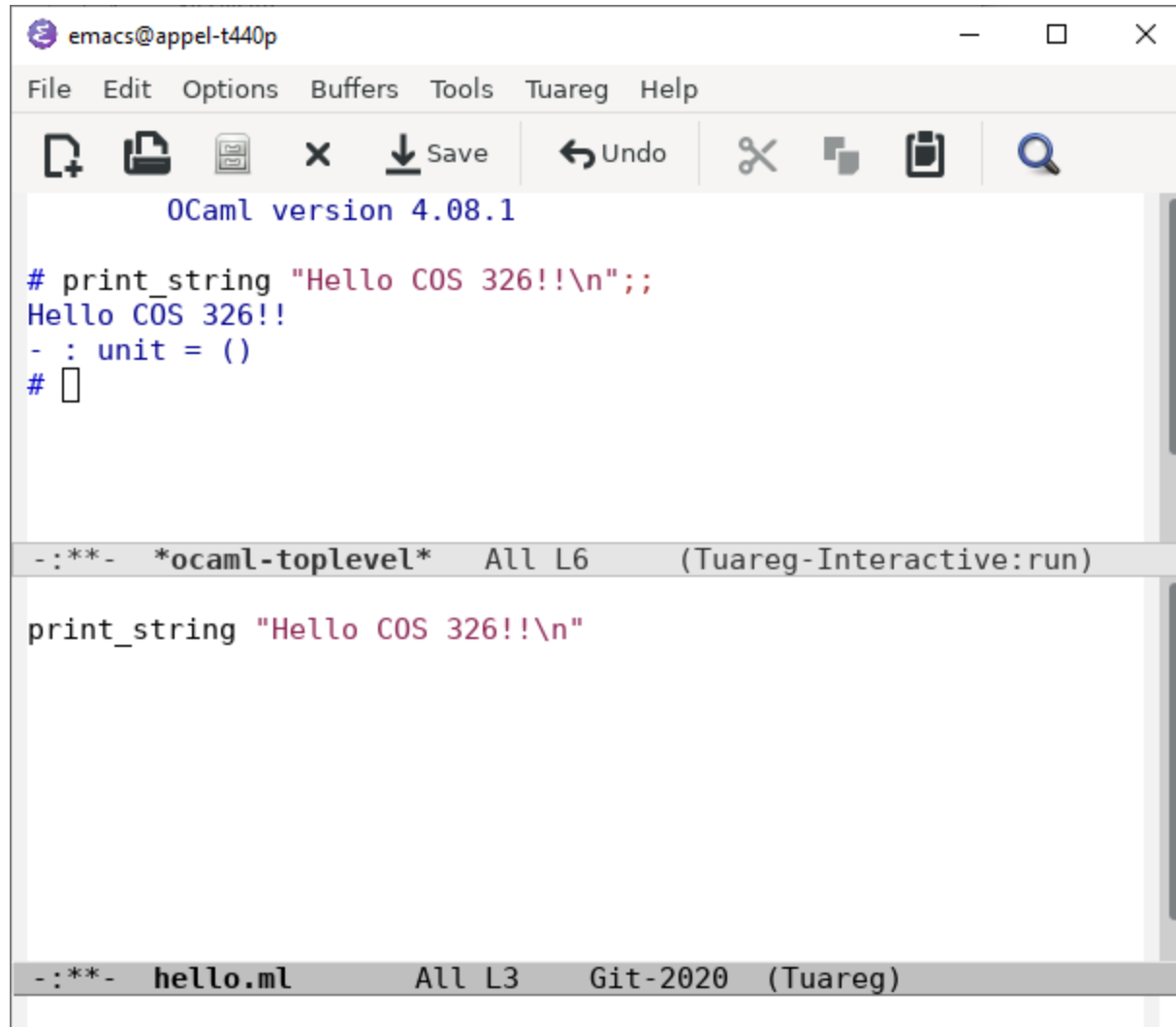


The image shows a screenshot of the Emacs text editor. The window title is "emacs@appel-t440p". The menu bar includes "File", "Edit", "Options", "Buffers", "Tools", "Tuareg", and "Help". The toolbar contains icons for opening files, saving, undo, redo, copy, paste, and search. The main text area displays "OCaml version 4.08.1" and a prompt "#". Below this, a buffer named "*ocaml-toplevel*" is active, showing the command "print_string \"Hello COS 326!!\n\"". At the bottom, another buffer named "hello.ml" is active, showing the filename and the text "All L1 Git-2020 (Tuareg)".

```
emacs@appel-t440p
File Edit Options Buffers Tools Tuareg Help
[Icons: Open, Save, Undo, Redo, Copy, Paste, Search]
OCaml version 4.08.1
# 
-:***- *ocaml-toplevel* All L3 (Tuareg-Interactive:run)
print_string "Hello COS 326!!\n"
-:***- hello.ml All L1 Git-2020 (Tuareg)
```



OCaml demo



The screenshot shows an Emacs window titled "emacs@appel-t440p". The menu bar includes "File", "Edit", "Options", "Buffers", "Tools", "Tuareg", and "Help". The toolbar contains icons for opening, saving, undo, redo, and search. The main text area displays OCaml code and its output:

```
OCaml version 4.08.1

# print_string "Hello COS 326!!\n";;
Hello COS 326!!
- : unit = ()
#
```

Below the code, a buffer titled "ocaml-toplevel" is shown, containing the command:

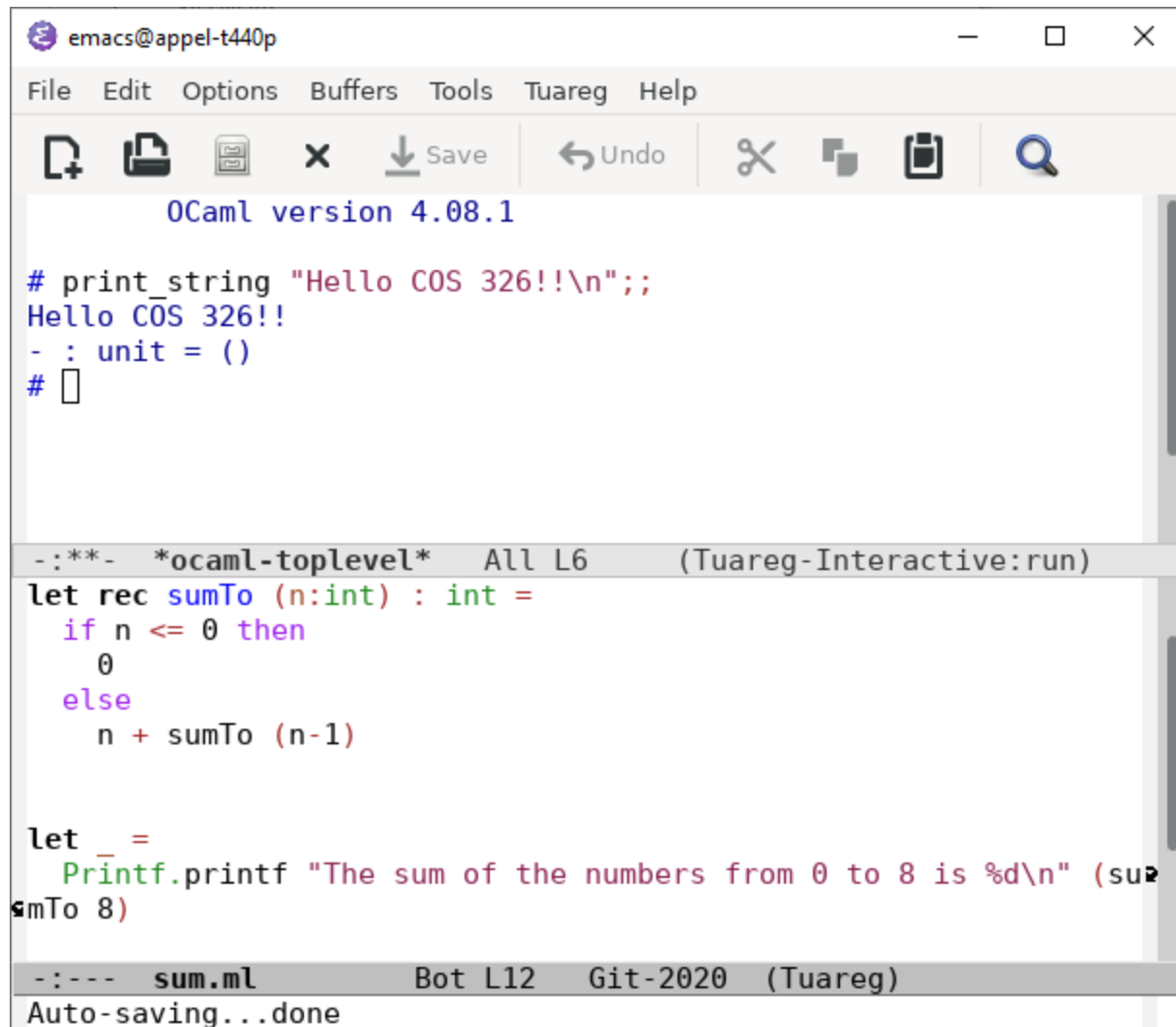
```
print_string "Hello COS 326!!\n"
```

At the bottom, another buffer titled "hello.ml" is visible, containing the code:

```
print_string "Hello COS 326!!\n"
```



OCaml demo



The screenshot shows an Emacs editor window titled "emacs@appel-t440p". The menu bar includes "File", "Edit", "Options", "Buffers", "Tools", "Tuareg", and "Help". The toolbar contains icons for opening, saving, undo, redo, and search. The main text area displays OCaml code and its execution output. The code defines a recursive function `sumTo` and uses `Printf.printf` to print the sum of numbers from 0 to 8. The output shows "Hello COS 326!!" and "The sum of the numbers from 0 to 8 is 36". The status bar at the bottom indicates the current file is `sum.ml`, the cursor is at line 12, and the buffer is `Git-2020`. A message "Auto-saving...done" is visible at the bottom.

```
OCaml version 4.08.1

# print_string "Hello COS 326!!\n";;
Hello COS 326!!
- : unit = ()
# []

-:***- *ocaml-toplevel* All L6 (Tuareg-Interactive:run)
let rec sumTo (n:int) : int =
  if n <= 0 then
    0
  else
    n + sumTo (n-1)

let _ =
  Printf.printf "The sum of the numbers from 0 to 8 is %d\n" (sumTo 8)

-:--- sum.ml Bot L12 Git-2020 (Tuareg)
Auto-saving...done
```



OCaml demo

```

emacs@appel-t440p
File Edit Options Buffers Tools Tuareg Help
Save Undo
# print_string "Hello COS 326!!\n";;
Hello COS 326!!
- : unit = ()
# let rec sumTo (n:int) : int =
  if n <= 0 then
    0
  else
    n + sumTo (n-1);;
  val sumTo : int -> int = <fun>
#
-:***- *ocaml-toplevel* Bot L12 (Tuareg-Interactive:run)
let rec sumTo (n:int) : int =
  if n <= 0 then
    0
  else
    n + sumTo (n-1)

let _ =
  Printf.printf "The sum of the numbers from 0 to 8 is %d\n" (sumTo 8)
-:--- sum.ml Bot L14 Git-2020 (Tuareg)
C-c C-e

```



OCaml demo

```

emacs@appel-t440p
File Edit Options Buffers Tools Tuareg Help
Save Undo
0
else
  n + sumTo (n-1);;
  val sumTo : int -> int = <fun>
# let _ =
  Printf.printf "The sum of the numbers from 0 to 8 is %d\n" (sumTo 8);;
The sum of the numbers from 0 to 8 is 36
- : unit = ()
#
-:***- *ocaml-toplevel* Bot L16 (Tuareg-Interactive:run)
let rec sumTo (n:int) : int =
  if n <= 0 then
    0
  else
    n + sumTo (n-1)

let _ =
  Printf.printf "The sum of the numbers from 0 to 8 is %d\n" (sumTo 8)
-:--- sum.ml Bot L16 Git-2020 (Tuareg)
C-c C-e

```

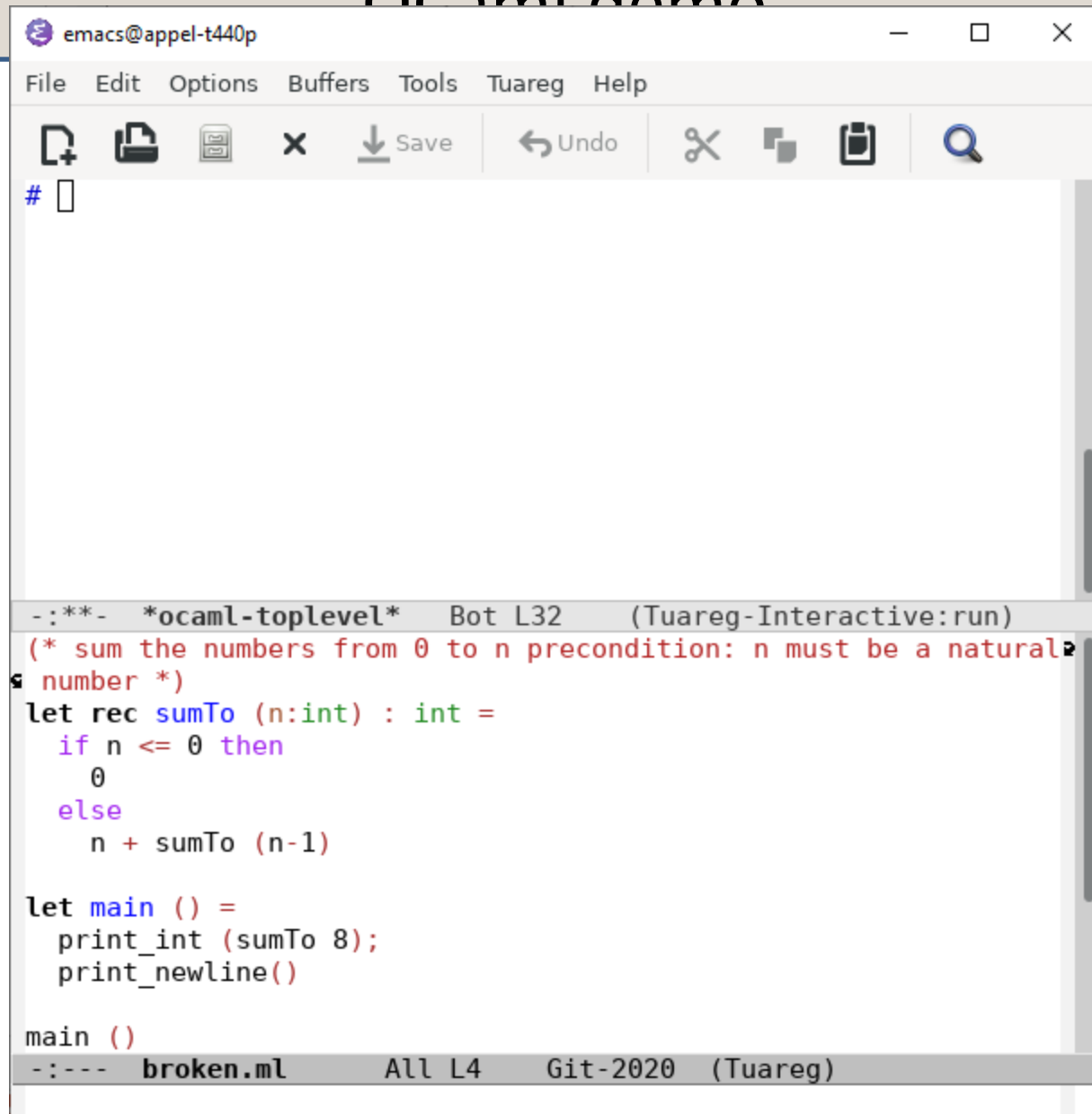


OCaml demo

```
xterm
ubuntu$ ls
Makefile  assert.ml  countn.ml  hello2.ml  sum_test.ml
a.out     broken.ml  hello.ml   sum.ml
ubuntu$
ubuntu$
ubuntu$
ubuntu$ ocamlc sum.ml
ubuntu$
ubuntu$ ls
Makefile  assert.ml  countn.ml  hello2.ml  sum.cmo  sum_test.ml
a.out     broken.ml  hello.ml   sum.cmi    sum.ml
ubuntu$
ubuntu$
ubuntu$ ./a.out
The sum of the numbers from 0 to 8 is 36
ubuntu$
```



OCaml demo



```
emacs@appel-t440p
File Edit Options Buffers Tools Tuareg Help
# 
-:***- *ocaml-toplevel* Bot L32 (Tuareg-Interactive:run)
(* sum the numbers from 0 to n precondition: n must be a natural
number *)
let rec sumTo (n:int) : int =
  if n <= 0 then
    0
  else
    n + sumTo (n-1)

let main () =
  print_int (sumTo 8);
  print_newline()

main ()
-:--- broken.ml All L4 Git-2020 (Tuareg)
```



OCaml demo

```

emacs@appel-t440p
File Edit Options Buffers Tools Tuareg Help
[Icons: Open, Save, Undo, Cut, Copy, Paste, Find]

let main () =
  print_int (sumTo 8);
  print_newline()

main ();;
                                     Line 9, characters 2-15:
9 |  print_newline()
   |  ~~~~~
Error: This function has type unit -> unit
      It is applied to too many arguments; maybe you forgot a `>
#
-:***- *ocaml-toplevel* Bot L48 (Tuareg-Interactive:run)
(* sum the numbers from 0 to n precondition: n must be a natural
number *)
let rec sumTo (n:int) : int =
  if n <= 0 then
    0
  else
    n + sumTo (n-1)

let main () =
  print_int (sumTo 8);
  print_newline()

main ()
-:--- broken.ml All L2 Git-2020 (Tuareg)

```



OCaml demo

The screenshot shows an Emacs window titled 'emacs@appel-t440p' with a menu bar (File, Edit, Options, Buffers, Tools, Tuareg, Help) and a toolbar with icons for file operations and search. The main editor area contains OCaml code for a recursive sum function and a main function. Below the code, the Tuareg interactive environment is shown, displaying the execution of the code and the resulting output.

```

else
  n + sumTo (n-1)

let main () =
  print_int (sumTo 8);
  print_newline();;

main ();;
                                val sumTo : int -> int = <fun>
val main : unit -> unit = <fun>
# 36
- : unit = ()
#
-:***- *ocaml-toplevel* Bot L81 (Tuareg-Interactive:run)
(* sum the numbers from 0 to n precondition: n must be a natural
number *)
let rec sumTo (n:int) : int =
  if n <= 0 then
    0
  else
    n + sumTo (n-1)

let main () =
  print_int (sumTo 8);
  print_newline();;

main ()
-:***- broken.ml All L10 Git-2020 (Tuareg)

```



OCaml demo

```

emacs@appel-t440p
File Edit Options Buffers Tools Tuareg Help
[Icons: Open, Save, Undo, etc.]

0
else
  n + sumTo (n-1)

let main () =
  print_int (sumTo 8);
  print_newline()

let _ = main ();;
                                     36
val sumTo : int -> int = <fun>
val main : unit -> unit = <fun>
# [

-:***- *ocaml-toplevel* Bot L124 (Tuareg-Interactive:run)
(* sum the numbers from 0 to n precondition: n must be a natural
number *)
let rec sumTo (n:int) : int =
  if n <= 0 then
    0
  else
    n + sumTo (n-1)

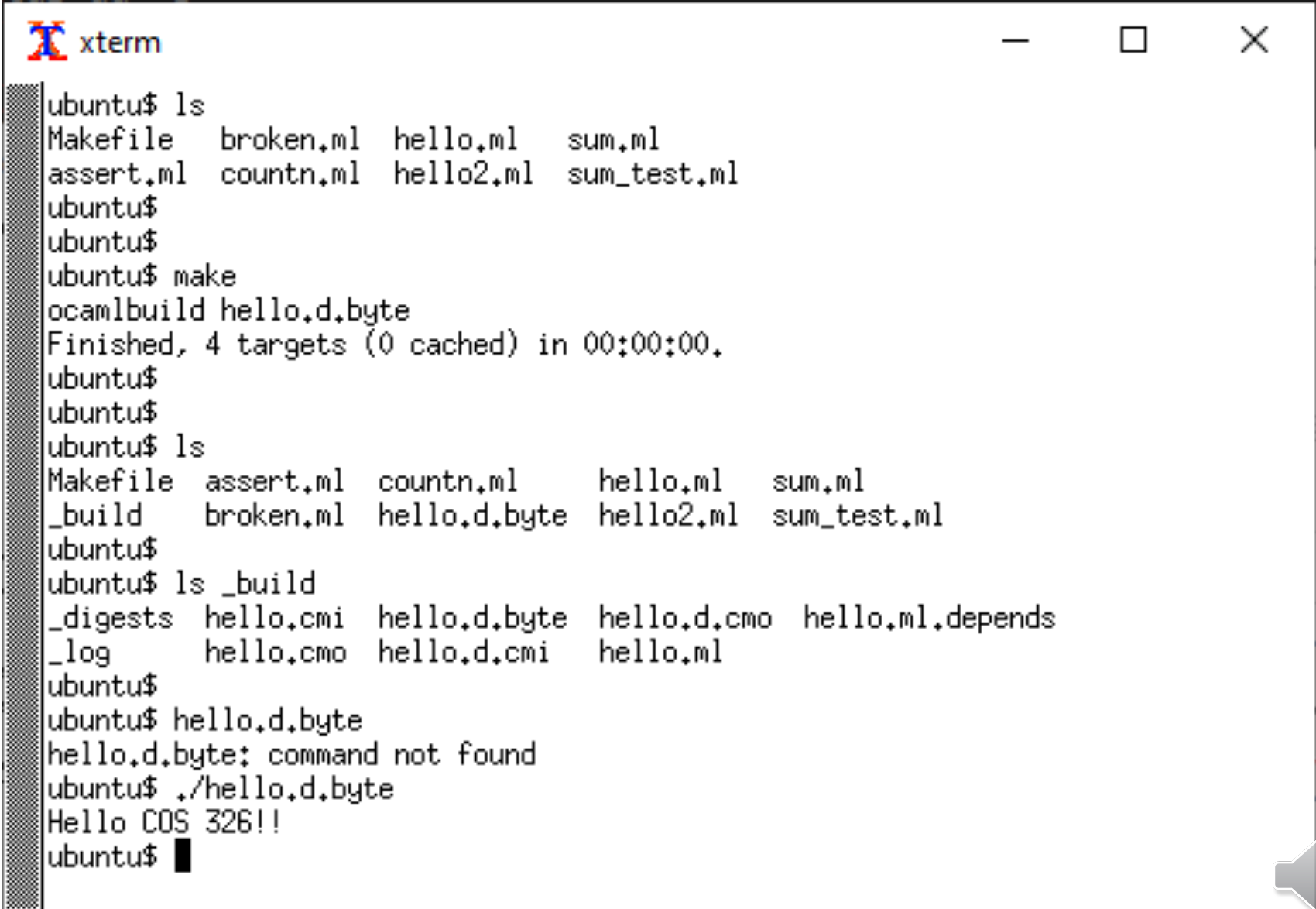
let main () =
  print_int (sumTo 8);
  print_newline()

let _ = main ()
-:***- broken.ml All L12 Git-2020 (Tuareg)

```



OCaml demo



```
xterm
ubuntu$ ls
Makefile  broken.ml  hello.ml  sum.ml
assert.ml  countrn.ml  hello2.ml  sum_test.ml
ubuntu$
ubuntu$
ubuntu$ make
ocamlbuild hello.d.byte
Finished, 4 targets (0 cached) in 00:00:00.
ubuntu$
ubuntu$
ubuntu$ ls
Makefile  assert.ml  countrn.ml  hello.ml  sum.ml
_build    broken.ml  hello.d.byte  hello2.ml  sum_test.ml
ubuntu$
ubuntu$ ls _build
_digests  hello.cmi  hello.d.byte  hello.d.cmo  hello.ml.depends
_log      hello.cmo  hello.d.cmi  hello.ml
ubuntu$
ubuntu$ hello.d.byte
hello.d.byte: command not found
ubuntu$ ./hello.d.byte
Hello COS 326!!
ubuntu$
```



A First OCaml Program

hello.ml:

```
print_string "Hello COS 326!!\n";;
```



A First OCaml Program

hello.ml:

```
print_string "Hello COS 326!!\n"
```

a function

its string argument
enclosed in "..."

a program
can be nothing
more than
just a single
expression
(but that is
uncommon)

no parens. normally call a function *f* like this:

```
f arg
```

(parens are used for grouping, precedence
only when necessary)



A First OCaml Program

hello.ml:

```
print_string "Hello COS 326!!\n"
```

compiling and running hello.ml:

```
$ ocamlbuild hello.d.byte
$ ./hello.d.byte
Hello COS 326!!
$
```

.d for debugging
(other choices .p for profiled; or none)

.byte for interpreted bytecode
(other choices .native for machine code)



A First OCaml Program

hello.ml:

```
print_string "Hello COS 326!!\n"
```

interpreting and playing with hello.ml:

```
$ ocaml  
      Objective Caml Version 3.12.0  
#
```



A First OCaml Program

hello.ml:

```
print_string "Hello COS 326!!\n"
```

interpreting and playing with hello.ml:

```
$ ocaml
      Objective Caml Version 3.12.0
# 3 + 1;;
- : int = 4
#
```



A First OCaml Program

hello.ml:

```
print_string "Hello COS 326!!\n"
```

interpreting and playing with hello.ml:

```
$ ocaml
      Objective Caml Version 3.12.0
# 3 + 1;;
- : int = 4
# #use "hello.ml";;
hello cos326!!
- : unit = ()
#
```



A First OCaml Program

hello.ml:

```
print_string "Hello COS 326!!\n"
```

interpreting and playing with hello.ml:

```
$ ocaml
      Objective Caml Version 3.12.0
# 3 + 1;;
- : int = 4
# #use "hello.ml";;
hello cos326!!
- : unit = ()
# #quit;;
$
```



A Second OCaml Program

sumTo8.ml:

```
(* sum the numbers from 0 to n
   precondition: n must be a natural number
*)
let rec sumTo (n:int) : int =
  match n with
  | 0 -> 0
  | n -> n + sumTo (n-1)

let _ =
  print_int (sumTo 8);
  print_newline()
```

a comment
(* ... *)



A Second OCaml Program

the name of the function being defined

sumTo8.ml:

```
(* sum the numbers from 0 to n
   precondition: n must be a natural number
   *)
let rec sumTo (n:int) : int =
  match n with
  | 0 -> 0
  | n -> n + sumTo (n-1)

let _ =
  print_int (sumTo 8);
  print_newline();
```

the keyword "let" begins a definition; keyword "rec" indicates recursion



A Second OCaml Program

sumTo8.ml:

```
(* sum the numbers from 0 to n
   precondition: n must be a natural number
*)
let rec sumTo (n:int) : int =
  match n with
    0 -> 0
  | n -> n + sumTo (n-1)

let _ =
  print_int (sumTo 8);
  print_newline()
```

result type int

argument
named n
with type int



A Second OCaml Program

deconstruct the value n
using pattern matching

sumTo8.ml:

```
(* sum the numbers from 0 to n
   precondition: n must be a natural number
*)
let rec sumTo (n:int) : int =
  match n with
    0 -> 0
  | n' -> n' + sumTo (n-1)

let _ =
  print_int (sumTo 8);
  print_newline()
```

data to be
deconstructed
appears
between
key words
"match" and
"with"



A Second OCaml Program

vertical bar "|" separates the alternative patterns

sumTo8.ml:

```
(* sum the numbers from 0 to n
   precondition: n must be a natural number
*)
let rec sumTo (n:int) : int =
  match n with
  | 0 -> 0
  | n -> n + sumTo (n-1)

let _ =
  print_int (sumTo 8);
  print_newline()

_
```

deconstructed data matches one of 2 cases:

(i) the data matches the pattern 0, or (ii) the data matches the variable pattern n



A Second OCaml Program

Each branch of the match statement constructs a result

sumTo8.ml:

```
(* sum the numbers from 0 to n
   precondition: n must be a natural number
*)
let rec sumTo (n:int) : int =
  match n with
    0 -> 0
  | n -> n + sumTo (n-1)

let _ =
  print_int (sumTo 8);
  print_newline()
```

construct
the result 0

construct
a result
using a
recursive
call to sumTo



A Second OCaml Program

sumTo8.ml:

```
(* sum the numbers from 0 to n
   precondition: n must be a natural number
*)
let rec sumTo (n:int) : int =
  match n with
  | 0 -> 0
  | n -> n + sumTo (n-1)

let _ =
  print_int (sumTo 8);
  print_newline()
```

print the
result of
calling
sumTo on 8

print a
new line 

OCAML BASICS: EXPRESSIONS, VALUES, SIMPLE TYPES



Terminology: Expressions, Values, Types

Expressions are computations

- $2 + 3$ is a computation

Values (a subset of the expressions) are the results of computations

- 5 is a value

Types describe collections of values and the computations that generate those values

- int is a type
- values of type int include
 - 0, 1, 2, 3, ..., max_int
 - -1, -2, ..., min_int



Some simple types, values, expressions

| <u>Type:</u> | <u>Values:</u> | <u>Expressions:</u> |
|--------------|-----------------|------------------------|
| int | -2, 0, 42 | 42 * (13 + 1) |
| float | 3.14, -1., 2e12 | (3.14 +. 12.0) *. 10e6 |
| char | 'a', 'b', '&' | int_of_char 'a' |
| string | "moo", "cow" | "moo" ^ "cow" |
| bool | true, false | if true then 3 else 4 |
| unit | () | print_int 3 |

For more primitive types and functions over them,
see the OCaml Reference Manual here:

<http://caml.inria.fr/pub/docs/manual-ocaml/libref/Pervasives.html>




Evaluation

$$42 * (13 + 1)$$



Evaluation

$$42 * (13 + 1) \text{ -->* } 588$$



Read like this: "the expression $42 * (13 + 1)$ **evaluates to** the value 588"

The "*****" is there to say that it does so in 0 or more small steps



Evaluation

42 * (13 + 1) --> * 588



Read like this: "the expression 42 * (13 + 1) **evaluates to** the value 588"

The "*" is there to say that it does so in 0 or more small steps

Here I'm telling you how to execute an OCaml expression --- ie, I'm telling you something about the *operational semantics* of OCaml

More on semantics later.



Evaluation

| | | |
|-------------------------------------|----------------------|-------------------------|
| <code>42 * (13 + 1)</code> | <code>-->*</code> | <code>588</code> |
| <code>(3.14 +. 12.0) *. 10e6</code> | <code>-->*</code> | <code>151400000.</code> |
| <code>int_of_char 'a'</code> | <code>-->*</code> | <code>97</code> |
| <code>"moo" ^ "cow"</code> | <code>-->*</code> | <code>"moocow"</code> |
| <code>if true then 3 else 4</code> | <code>-->*</code> | <code>3</code> |
| <code>print_int 3</code> | <code>-->*</code> | <code>()</code> |



Evaluation

1 + "hello" -->* ???



Evaluation

1 + "hello" -->* ???

"+" processes integers
"hello" is not an integer
evaluation is undefined!

Don't worry! This expression doesn't type check.

Aside: See this talk on Javascript:
<https://www.destroyallsoftware.com/talks/wat>



OCAML BASICS: CORE EXPRESSION SYNTAX



Core Expression Syntax

The simplest OCaml expressions e are:

- values *numbers, strings, bools, ...*
- id *variables (x, foo, ...)*
- e_1 op e_2 *operators (x+3, ...)*
- id e_1 e_2 ... e_n *function call (foo 3 42)*
- **let** id = e_1 **in** e_2 *local variable decl.*
- **if** e_1 **then** e_2 **else** e_3 *a conditional*
- (e) *a parenthesized expression*
- (e : t) *an expression with its type*



A note on parentheses

In most languages, arguments are parenthesized & separated by commas:

`f(x, y, z)` `sum(3, 4, 5)`

In OCaml, we don't write the parentheses or the commas:

`f x y z` `sum 3 4 5`

But we do have to worry about *grouping*. For example,

`f x y z` same as: `((f x) y) z`
 not the same as: `f x (y z)`

The first one passes three arguments to `f` (`x`, `y`, and `z`)

The second passes two arguments to `f` (`x`, and the result of applying the function `y` to `z`.)



OCAML BASICS: TYPE CHECKING



Type Checking

Every value has a type and so does every expression

This is a concept that is familiar from Java but it becomes more important when programming in a functional language

We write ($e : t$) to say that *expression e has type t*. eg:

2 : int

"hello" : string

2 + 2 : int

"I say " ^ "hello" : string



Type Checking Rules

There are a set of **simple rules** that govern type checking

- programs that do not follow the rules will not type check and O’Caml will refuse to compile them for you (the nerve!)
- at first you may find this to be a pain ...

But types are a great thing:

- help us *think* about *how to construct* our programs
- help us *find stupid programming errors*
- help us track down errors quickly when we *edit our code*
- allow us to *enforce powerful invariants* about data structures



Type Checking Rules

Example rules:

- (1) `0 : int` (and similarly for any other integer constant `n`)
- (2) `"abc" : string` (and similarly for any other string constant `"..."`)



Type Checking Rules

Example rules:

- (1) $0 : \text{int}$ (and similarly for any other integer constant n)
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- (3) if $e1 : \text{int}$ and $e2 : \text{int}$
then $e1 + e2 : \text{int}$
- (4) if $e1 : \text{int}$ and $e2 : \text{int}$
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- (5) if $e1 : \text{string}$ and $e2 : \text{string}$
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- (6) if $e : \text{int}$
then $\text{string_of_int } e : \text{string}$



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Using the rules:

$2 : \text{int}$ and $3 : \text{int}$. (By rule 1)



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Using the rules:

$2 : \text{int}$ and $3 : \text{int}$. (By rule 1)
Therefore, $(2 + 3) : \text{int}$ (By rule 3)



Type Checking Rules

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Using the rules:

$2 : \text{int}$ and $3 : \text{int}$. (By rule 1)
 Therefore, $(2 + 3) : \text{int}$ (By rule 3)
 $5 : \text{int}$ (By rule 1)



Type Checking Rules

Example rules:

(1) $0 : \text{int}$ (and similarly for any other integer constant n)

(2) $"\text{abc}" : \text{string}$ (and similarly for any other string constant s)

(3) if $e_1 : \text{int}$ and $e_2 : \text{int}$
then $e_1 + e_2 : \text{int}$

(5) if $e_1 : \text{string}$ and $e_2 : \text{string}$
then $e_1 \wedge e_2 : \text{string}$

FYI: This is a *formal proof*
that the expression is well-
typed!

Using the rules:

$2 : \text{int}$ and $3 : \text{int}$. (By rule 1)

Therefore, $(2 + 3) : \text{int}$ (By rule 3)

$5 : \text{int}$ (By rule 1)

Therefore, $(2 + 3) * 5 : \text{int}$ (By rule 4 and our previous work)



Type Checking Rules

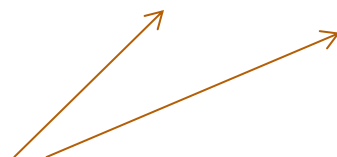
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then $\text{string_of_int } e : \text{string}$

Another perspective:

rule (4) for typing expressions
says I can put any expression
with type int in place of the $????$

$???? * ???? : \text{int}$




Type Checking Rules

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then `string_of_int e : string`

Another perspective:

rule (4) for typing expressions
says I can put any expression
with type `int` in place of the `????`

`7 * ???? : int`



Type Checking Rules

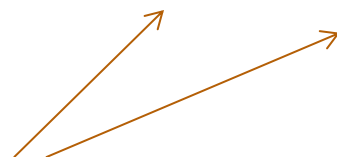
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Another perspective:

rule (4) for typing expressions
says I can put any expression
with type `int` in place of the `????`

$7 * (\text{add_one } 17) : \text{int}$




Type Checking Rules

You can always start up the OCaml interpreter to find out a type of a simple expression:

```
$ ocaml
      Objective Caml Version 3.12.0
#
```



Type Checking Rules

You can always start up the OCaml interpreter to find out a type of a simple expression:

```
$ ocaml
      Objective Caml Version 3.12.0
# 3 + 1;;
```

use ";;"
to end
a phrase
in the
top level

(";" can also end a top-level phrase in a file, but I'm going to avoid using it there because then some of you will confuse it with a ";" ...)



Type Checking Rules

You can always start up the OCaml interpreter to find out a type of a simple expression:

```
$ ocaml
      Objective Caml Version 3.12.0
# 3 + 1;;
- : int = 4
#
```

press
return
and you
find out
the type
and the
value



Type Checking Rules

You can always start up the OCaml interpreter to find out a type of a simple expression:

```
$ ocaml
      Objective Caml Version 3.12.0
# 3 + 1;;
- : int = 4
# "hello " ^ "world";;
- : string = "hello world"
#
```

press
return
and you
find out
the type
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value



Type Checking Rules

You can always start up the OCaml interpreter to find out a type of a simple expression:

```
$ ocaml
      Objective Caml Version 3.12.0
# 3 + 1;;
- : int = 4
# "hello " ^ "world";;
- : string = "hello world"
# #quit;;
$
```



Type Checking Rules

Example rules:

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then `string_of_int e : string`

Violating the rules:

| | |
|-------------------------------|-----------------------------------|
| <code>"hello" : string</code> | (By rule 2) |
| <code>1 : int</code> | (By rule 1) |
| <code>1 + "hello" : ??</code> | (NO TYPE! Rule 3 does not apply!) |



Type Checking Rules

Violating the rules:

```
# "hello" + 1;;
```

```
Error: This expression has type string but an  
expression was expected of type int
```

The type error message tells you the type that was **expected** and the type that it **inferred** for your subexpression

By the way, this was one of the nonsensical expressions that did not evaluate to a value

It is a **good thing** that this expression does not type check!

"Well typed programs do not go wrong"

Robin Milner, 1978



Type Checking Rules

Violating the rules:

```
# "hello" + 1;;
```

```
Error: This expression has type string but an  
expression was expected of type int
```

A possible fix:

```
# "hello" ^ (string_of_int 1);;  
- : string = "hello1"
```

One of the keys to becoming a good ML programmer is to understand type error messages.



Type Checking Rules

What about this expression:

```
# 3 / 0 ;;  
Exception: Division_by_zero.
```

Why doesn't the ML type checker do us the favor of telling us the expression will raise an exception?



Type Checking Rules

What about this expression:

```
# 3 / 0 ;;  
Exception: Division_by_zero.
```

Why doesn't the ML type checker do us the favor of telling us the expression will raise an exception?

- In general, detecting a divide-by-zero error requires we know that the divisor evaluates to 0.
- In general, deciding whether the divisor evaluates to 0 requires solving the halting problem:

```
# 3 / (run_turing_machine(); 0);;
```

There are type systems that will rule out divide-by-zero errors, but they require programmers supply proofs to the type checker



Isn't that cheating?

"Well typed programs do not go wrong"

Robin Milner, 1978

(3 / 0) is well typed. Does it "go wrong?" Answer: No.

"Go wrong" is a technical term meaning, "have no defined semantics." Raising an exception is perfectly well defined semantics, which we can reason about, which we can handle in ML with an exception handler.

So, it's not cheating.

(Discussion: why do we make this distinction, anyway?)



Type Soundness

"Well typed programs do not go wrong"

Programming languages with this property have *sound* type systems. They are called *safe* languages.

Safe languages are generally *immune* to buffer overrun vulnerabilities, uninitialized pointer vulnerabilities, etc., etc.
(but not immune to all bugs!)

Safe languages: ML, Java, Python, ...

Unsafe languages: C, C++, Pascal



**OVERALL SUMMARY:
A SHORT INTRODUCTION TO
FUNCTIONAL PROGRAMMING**



OCaml

OCaml is a *functional* programming language

- express control flow and iteration by defining *functions*

OCaml is a *typed* programming language

- the *type* of an expression *correctly predicts* the kind of *value* the expression will generate when it is executed
- types help us *understand* and *write* our programs
- the type system is *sound*; the language is *safe*

