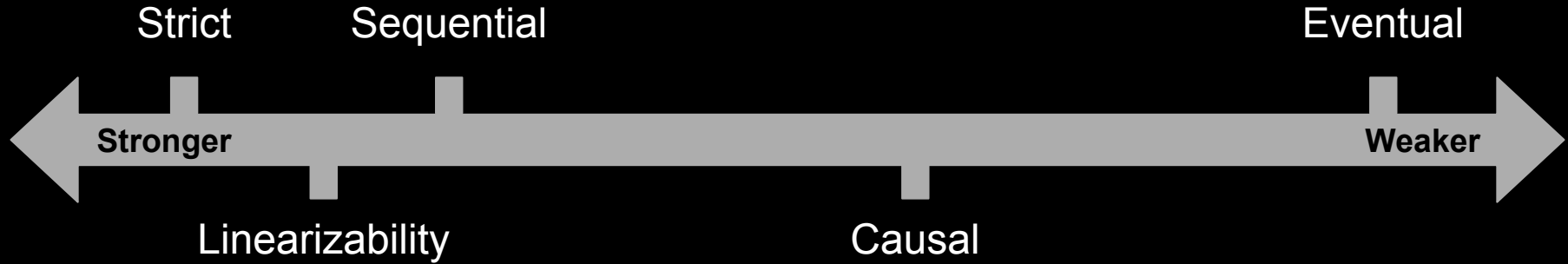


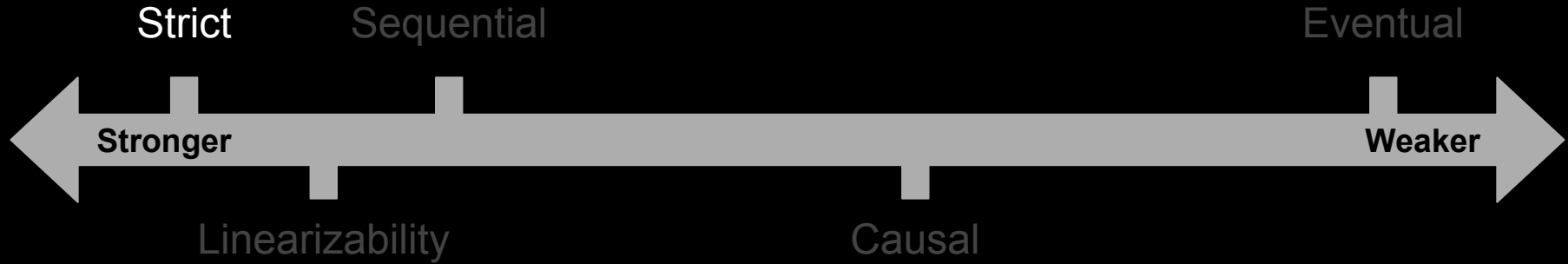
Consistency

11/17/2017

Consistency Models



Consistency Models



Strict Consistency

- **Instantaneous writes**: All writes immediately observed by all processes
- **Global clock**: Order ops across all processes as if on one machine
- Strongest consistency

○

Pros: Easily reason about correctness

Cons: Highly unavailable

Strict Consistency Example

Strict? **Yes**

P1: $W(x)b$

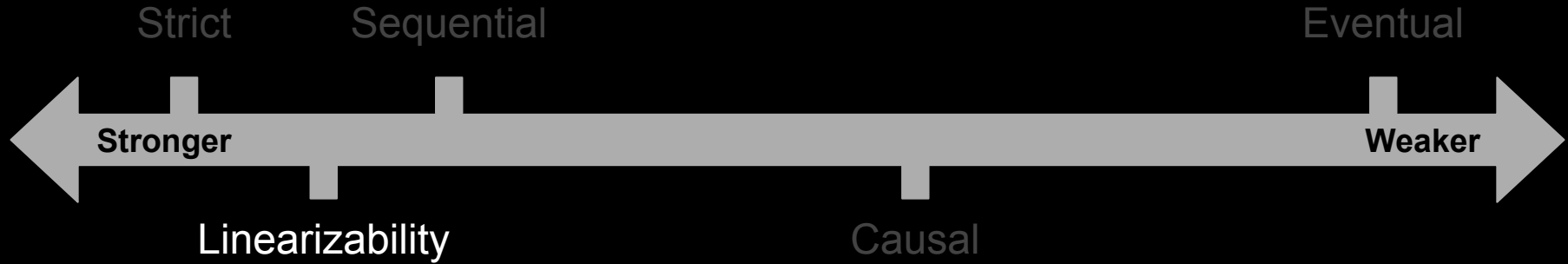
P2: $R(x)b$ $R(x)b$

Strict? **No**

P1: $W(x)b$

P2: $R(x)a$ $R(x)b$

Consistency Models



Linearizability

- **Total order**: All processes agree on the same sequence of ops
- **Global clock**: Determine sequence of ops using real time
- Difference from *strict consistency*?
 - Writes don't have to be *immediately* observed by everyone
- Properties
 - A completed write appears to all future reads
 - Once a read sees a value, all future reads must also return the same value (until new write)

Pros: Easily reason about correctness

Cons: High read and write latencies

Linearizability Example

Linearizable?

Yes

P1: W(x)a

P2: W(x)b

P3: R(x)a R(x)b

P4: R(x)a R(x)b

Linearizable?

No

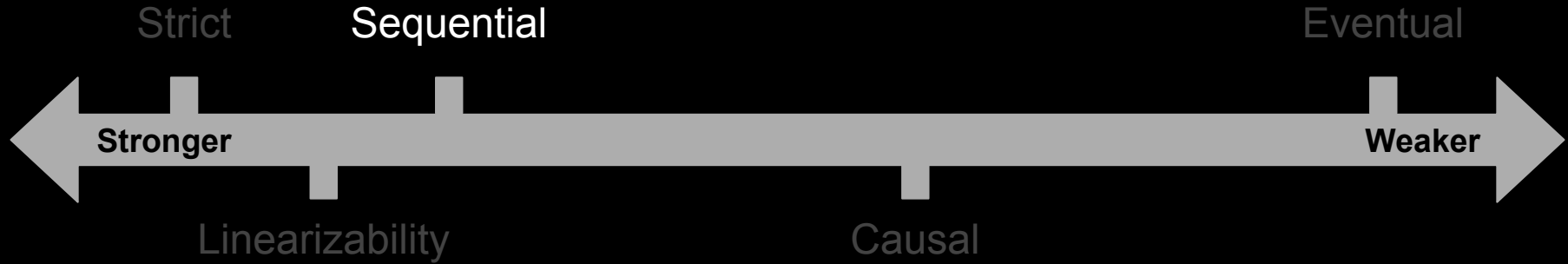
P1: W(x)a

P2: W(x)b

P3: R(x)b R(x)a

P4: R(x)b R(x)a

Consistency Models



Sequential Consistency

- **Total order**: All processes agree on the same sequence of ops
- Difference from *linearizability*?
 - Sequence of ops not determined by global clock

Pros: Easily reason about correctness, more permissive

Cons: Many possible sequential executions, non-deterministic

Sequential Consistency Example

Sequentially Consistent? **Yes**

P1: W(x)a

P2: W(x)b

P3: R(x)b R(x)a

P4: R(x)b R(x)a

Sequentially Consistent? **No**

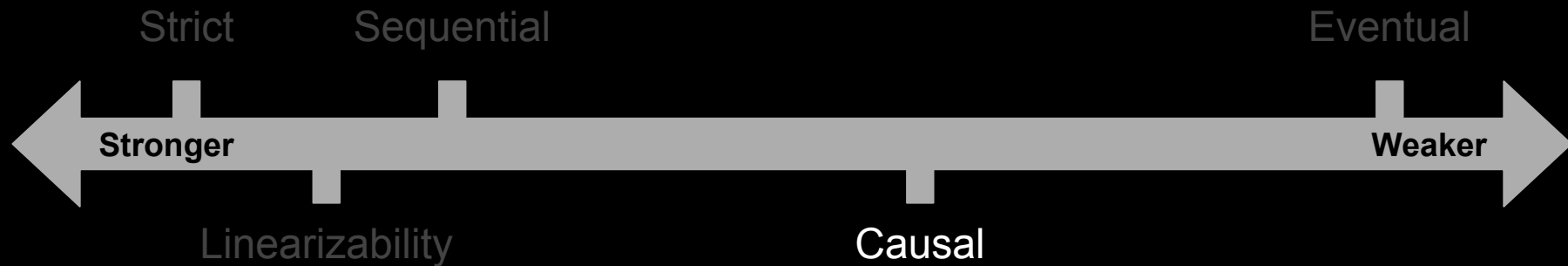
P1: W(x)a

P2: W(x)b

P3: R(x)b R(x)a

P4: R(x)a R(x)b

Consistency Models



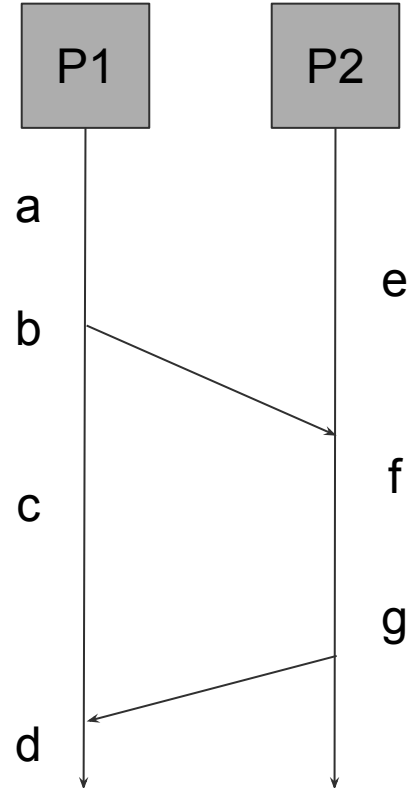
Causal Consistency

- **Partial order**: Order causally related ops the same way across all processes
- Difference from *sequential consistency*?
 - Only casually related ops need to be ordered
 - Concurrent ops may be ordered differently across different processes

Pros: Preserves causality while improving efficiency

Cons: Need to reason about concurrency

Ops	Concurrent
a,b	No
a,e	Yes
a,g	No
c,e	Yes
c,d	No
d,g	No
d,f	No
e,g	No
a,d	No



Causal Consistency Example

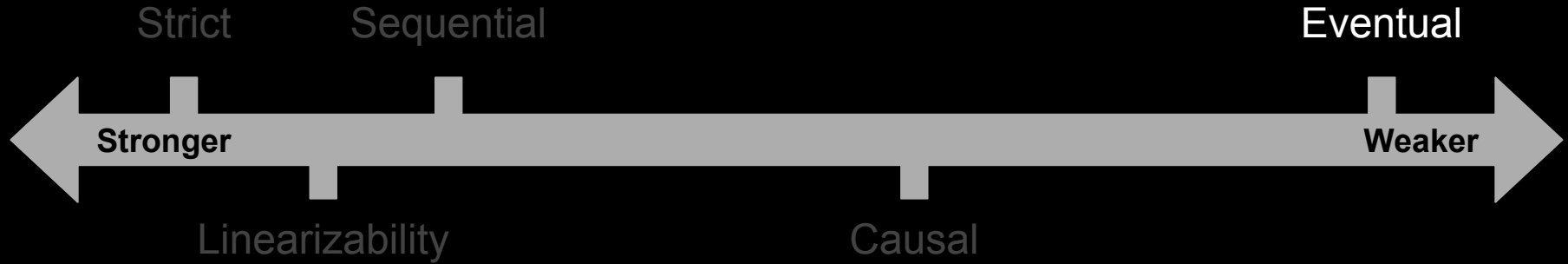
Causally Consistent? Yes

P1:	W(x)a		
P2:	W(x)b		
P3:		R(x)b	R(x)a
P4:		R(x)a	R(x)b

Causally Consistent? No

P1:	W(x)a		
P2:		R(x)a	W(x)b
P3:			R(x)b
P4:		R(x)a	R(x)b

Consistency Models



Eventual Consistency

- **Eventual convergence**: If no more writes, all replicas *eventually* agree
- Difference from *causal consistency*?
 - Does not preserve causal relationships
- Frequently used with application conflict resolution, anti-entropy

Pros: Super duper highly available

Cons: No safety guarantees, need conflict resolution

In a nutshell...

Strict consistency: all writes are immediately observed

Linearizability: Total order + real time guarantees

Sequential consistency: Total order

Causal consistency: Partial order that respects causal relationships

Eventual consistency: Eventually everyone should agree on state

Exercise 1:

P1: W(x) 1 R(y) 4

P2: R(x) 1 R(y) 4

P3: R(x) 1 W(y) 4

P4: R(x) 1 R(y) 4

Consistency Model:

Strict **Yes**

Linearizable **Yes**

Sequential **Yes**

Causal **Yes**

Eventual **Yes**

Exercise 2:

P1:	W(x) 3			W(y) 7
P2:	W(x) 1			
P3:		R(x) 1	R(x) 3	R(y) 7
P4:		R(x) 1	R(x) 3	R(y) 7
P5:		R(x) 1	R(x) 3	R(y) 7

Consistency Model:

Strict	No
Linearizable	No
Sequential	Yes
Causal	Yes
Eventual	Yes

Exercise 3:

Consistency Model:

Strict **No**

Linearizable **No**

Sequential **No**

Causal **Yes**

Eventual **No**

P1:	W(x) 3			W(y) 7
P2:	W(x) 1			
P3:		R(x) 1	R(x) 3	R(y) 7
P4:		R(x) 3	R(x) 1	R(y) 7
P5:		R(x) 1	R(x) 3	R(y) 7

Exercise 4:

P1: W(x) 1

P2: W(x) 3

P3: W(x) 7

P4: R(x) 3 R(x) 7 R(x) 1

P5: R(x) 3 R(x) 1 R(x) 7

Consistency Model:

Strict No

Linearizable No

Sequential No

Causal Yes

Eventual No

Exercise 5:

Consistency Model:

Strict	No
Linearizable	No
Sequential	No
Causal	Yes
Eventual	No

P1:	W(x)	1			
P2:	W(x)	3			
P3:	R(x)	3	W(x)	7	
P4:		R(x)	3	R(x)	7
P5:		R(x)	3	R(x)	1
				R(x)	7

Exercise 6:

Consistency Model:

Strict	No
Linearizable	No
Sequential	No
Causal	No
Eventual	No

P1:	W(x) 1				
P2:		R(x) 1	W(x) 3		
P3:				R(x) 3	W(x) 7
P4:				R(x) 3	R(x) 7
P5:				R(x) 3	R(x) 1