

## Bitcoin and the Blockchain



COS 418: *Distributed Systems*  
Lecture 20

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## Bitcoin: 10,000 foot view

- New bitcoins are “created” every ~10 min, owned by “miner” (more on this later)
- Thereafter, just keep record of transfers
  - e.g., Alice pays Bob 1 BTC
- Basic protocol:
  - Alice signs transaction:  $\text{txn} = \text{Sign}_{\text{Alice}}(\text{BTC}, \text{PK}_{\text{Bob}})$
  - Alice shows transaction to others...

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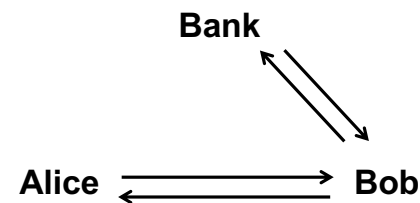
## Problem: Equivocation!

Can Alice “pay” both Bob and Charlie  
with same bitcoin ?

( Known as “double spending” )

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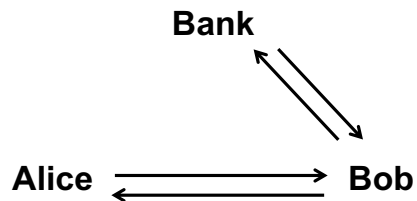
## How traditional e-cash handled problem



- When Alice pays Bob with a coin, Bob validates that coin hasn't been spend with trusted third party
- Introduced “blind signatures” and “zero-knowledge protocols” so bank can't link withdrawals and deposits

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## How traditional e-cash handled problem



- When Alice pays Bob with a coin, Bob validates that coin hasn't been spend with trusted third party

Bank maintains linearizable log of transactions

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## Problem: Equivocation!

Goal: No double-spending in decentralized environment

Approach: Make transaction log

1. public
2. append-only
3. strongly consistent

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## Bitcoin: 10,000 foot view

- Public
  - Transactions are signed:  $\text{txn} = \text{Sign}_{\text{Alice}}(\text{BTC}, \text{PK}_{\text{Bob}})$
  - All transactions are sent to all network participants
- No equivocation: Log append-only and consistent
  - All transactions part of a hash chain
  - Consensus on set/order of operations in hash chain

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## Intro to crypto in 5 minutes

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## Public-Key Cryptography

- Each party has (public key, private key)
- Alice's public key PK
  - Known by anybody
  - Bob uses PK to encrypt messages *to* Alice
  - Bob uses PK to verify signatures *from* Alice
- Alice's private/secret key: sk
  - Known only by Alice
  - Alice uses sk to decrypt ciphertexts sent to her
  - Alice uses sk to generate new signatures on messages

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## Public-Key Cryptography

- $(PK, sk) = \text{generateKey}(\text{keysize})$
- Encryption API
  - ciphertext = encrypt (message, PK)
  - message = decrypt (ciphertext, sk)
- Digital signatures API
  - Signature = sign (message, sk)
  - isValid = verify (signature, message, PK)

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## Cryptography Hash Functions I

- Take message  $m$  of arbitrary length and produces fixed-size (short) number  $H(m)$
- One-way function
  - Efficient: Easy to compute  $H(m)$
  - **Hiding property:** Hard to find an  $m$ , given  $H(m)$ 
    - Assumes "m" has sufficient entropy, not just {"heads", "tails"}
  - **Random:** Often assumes for output to "look" random

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## Cryptography Hash Functions II

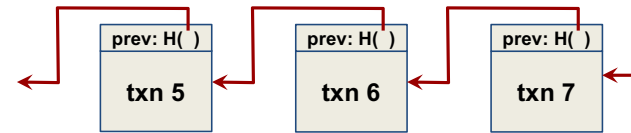
- Collisions exist: | possible inputs |  $\gg$  | possible outputs |  
... but hard to find
- Collision resistance:
  - Strong resistance: Find any  $m \neq m'$  such that  $H(m) == H(m')$
  - Weak resistance: Given  $m$ , find  $m'$  such that  $H(m) == H(m')$
  - For 160-bit hash (SHA-1)
    - Finding any collision is birthday paradox:  $2^{\{160/2\}} = 2^{80}$
    - Finding specific collision requires  $2^{160}$

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# Tamper-evident logging

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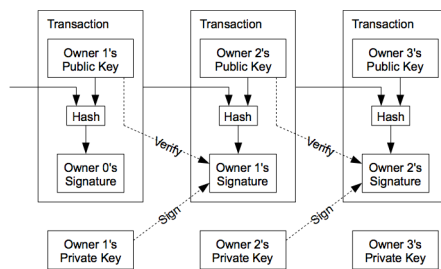
## Blockchain: Append-only hash chain



- Hash chain creates “tamper-evident” log of txns
- Security based on collision-resistance of hash function
  - Given  $m$  and  $h = \text{hash}(m)$ , difficult to find  $m'$  such that  $h = \text{hash}(m')$  and  $m \neq m'$

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## Blockchain: Append-only hash chain



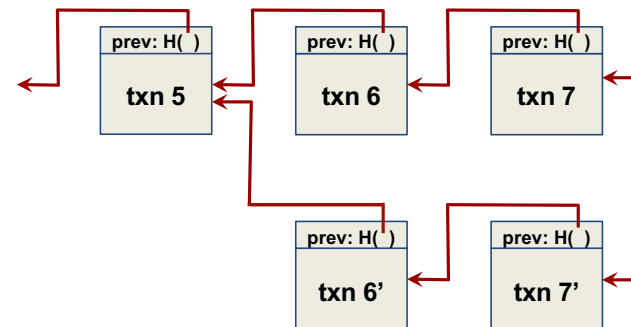
Bitcoin: A Peer-to-Peer Electronic Cash System

Satoshi Nakamoto  
satoshi@gmx.com  
www.bitcoin.org

Abstract. A purely peer-to-peer version of electronic cash would allow online payments to be sent directly from one party to another without going through a financial institution. Digital signatures provide part of the solution, but the main

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## Problem remains: forking



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## Goal: Consensus

- Recall Byzantine fault-tolerant protocols to achieve consensus of replicated log
  - Requires:  $n \geq 3f + 1$  nodes, at most  $f$  faulty
- Problem
  - Communication complexity is  $n^2$
  - Requires **strong view** of network participants

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## Consensus susceptible to Sybils

- All consensus protocols based on membership...
  - ... assume independent failures ...
  - ... which implies strong notion of identity
- “Sybil attack” (p2p literature ~2002)
  - **Idea**: one entity can create many “identities” in system
  - **Typical defense**: 1 IP address = 1 identity
  - **Problem**: IP addresses aren’t difficult / expensive to get, esp. in world of botnets & cloud services

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## Consensus based on “work”

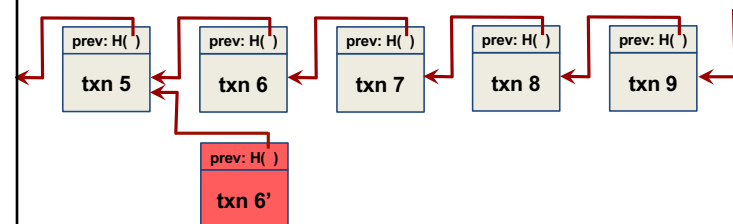
- Rather than “count” IP addresses, bitcoin “counts” the amount of CPU time / electricity that is expended

“The system is secure as long as honest nodes collectively control more CPU power than any cooperating group of attacker nodes.”  
- Satoshi Nakamoto

- Proof-of-work: Cryptographic “proof” that certain amount of CPU work was performed

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## Key idea: Chain length requires work



- Generating a new block requires “proof of work”
- “Correct” nodes accept longest chain
- Creating fork requires rate of malicious work  $\gg$  rate of correct
  - So, the older the block, the “safer” it is from being deleted

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## Use hashing to determine work!

- Recall hash functions are one-way / collision resistant
  - Given  $h$ , hard to find  $m$  such that  $h = \text{hash}(m)$
- But what about finding partial collision?
  - $m$  whose hash has most significant bit = 0?
  - $m$  whose hash has most significant bit = 00?
  - Assuming output is randomly distributed, complexity grows exponentially with # bits to match

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## Bitcoin proof of work

Find **nonce** such that

$$\text{hash}(\text{nonce} \parallel \text{prev\_hash} \parallel \text{block data}) < \text{target}$$

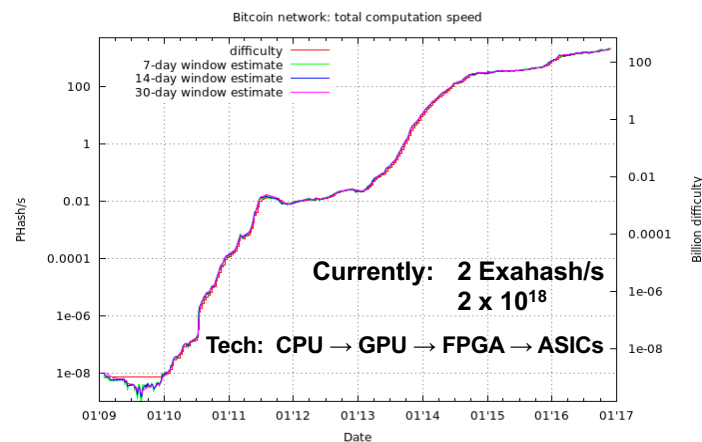
i.e., hash has certain number of leading 0's

What about changes in total system hashing rate?

- Target is recalculated every 2 weeks
- Goal: One new block every 10 minutes

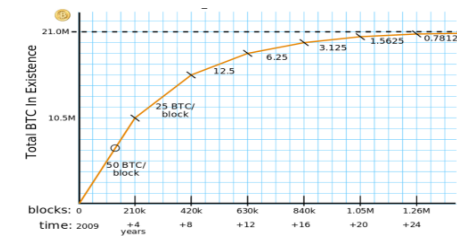
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## Historical hash rate trends of bitcoin



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## Why consume all this energy?



- Creating a new block creates bitcoin!
  - Initially 50 BTC, decreases over time, currently 12.5
  - New bitcoin assigned to party named in new block
  - Called "mining" as you search for gold/coins

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## Bitcoin is worth (LOTS OF) money!



- 12.5 BTC = \$140,000+ today

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## Incentivizing correct behavior?

- Race to find nonce and claim block reward, at which time race starts again for next block

**hash (nonce || prev\_hash || block data)**

- As solution has prev\_hash, corresponds to particular chain
- Correct behavior is to accept longest chain
  - “Length” determined by aggregate work, not # blocks
  - So miners incentivized only to work on longest chain, as otherwise solution not accepted
  - Remember blocks on other forks still “create” bitcoin, but only matters if chain in collective conscious (majority)

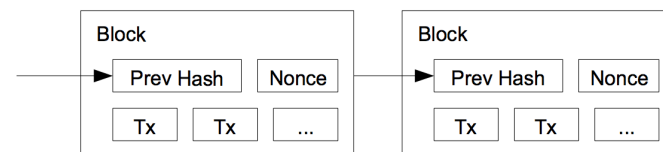
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## Form of randomized leader election

- Each time a nonce is found:
  - New leader elected for past epoch (~10 min)
  - Leader elected randomly, probability of selection proportional to leader’s % of global hashing power
  - Leader decides which transactions comprise block

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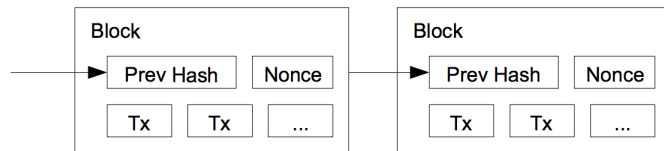
## One block = many transactions



- Each miner picks a set of transactions for block
- Builds “block header”: prevhash, version, timestamp, txns, ...
- Until hash < target OR another node wins:
  - Pick nonce for header, compute hash = SHA256(SHA256(header))

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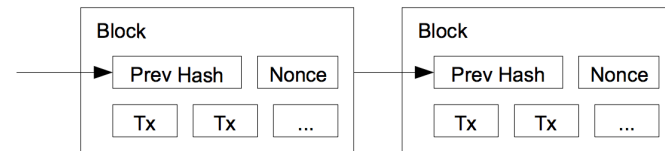
## Transactions are delayed



- At some time  $T$ , block header constructed
- Those transactions had been received  $[T - 10 \text{ min}, T]$
- Block will be generated at time  $T + 10 \text{ min}$  (on average)
- So transactions are from 10 - 20 min before block creation
- Can be much longer if “backlog” of transactions are long

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## Commitments further delayed



- When do you trust a transaction?
  - After we know it is “stable” on the hash chain
  - Recall that the longer the chain, the hard to “revert”
- Common practice: transaction “committed” when 6 blocks deep
  - i.e., Takes another ~1 hour for txn to become committed

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## Transaction format: strawman

Create 12.5 coins, credit to Alice	
Transfer 3 coins from Alice to Bob	SIGNED(Alice)
Transfer 8 coins from Bob to Carol	SIGNED(Bob)
Transfer 1 coins from Carol to Alice	SIGNED(Carol)

How do you determine if Alice has balance?  
Scan backwards to time 0 !

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## Transaction format

<b>Inputs:</b>	$\emptyset$	// Coinbase reward
<b>Outputs:</b>	25.0→PK_Alice	
<b>Inputs:</b>	$H(\text{prevtxn}, 0)$	// 25 BTC from Alice
<b>Outputs:</b>	25.0→PK_Bob	SIGNED(Alice)
<b>Inputs:</b>	$H(\text{prevtxn}, 0)$	// 25 BTC From Alice
<b>Outputs:</b>	5.0→PK_Bob, 20.0 →PK_Alice2	SIGNED(Alice)
<b>Inputs:</b>	$H(\text{prevtxn1}, 1), H(\text{prevtxn2}, 0)$	// 10+5 BTC
<b>Outputs:</b>	14.9→PK_Bob	SIGNED(Alice)

- Transaction typically has 1+ inputs, 1+ outputs
- Making change: 1<sup>st</sup> output payee, 2<sup>nd</sup> output self
- Output can appear in single later input (avoids scan back)

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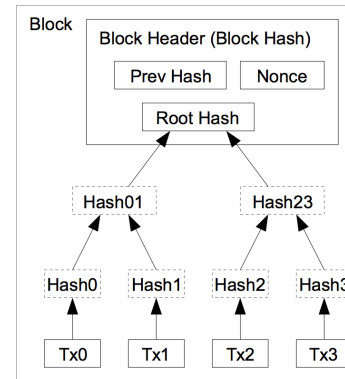
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- Unspent portion of inputs is “transaction fee” to miner
- In fact, “outputs” are stack-based scripts
- 1 Block = 1MB max

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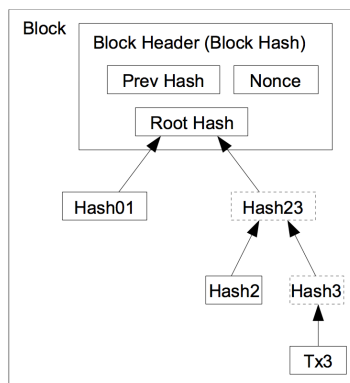
## Storage / verification efficiency



- Merkle tree
  - Binary tree of hashes
  - Root hash “binds” leaves given collision resistance
- Using a root hash
  - Block header now constant size for hashing
  - Can prune tree to reduce storage needs over time

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## Storage / verification efficiency



- Merkle tree
  - Binary tree of hashes
  - Root hash “binds” leaves given collision resistance
- Using a root hash
  - Block header now constant size for hashing
  - Can prune tree to reduce storage needs over time
    - Can prune when all txn outputs are spent
    - Now: 80GB pruned, 300GB unpruned

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## Not panacea of scale as some claim

- Scaling limitations
  - 1 block = 1 MB max
  - 1 block ~ 2000 txns
  - 1 block ~ 10 min
  - So, 3-4 txns / sec
  - Log grows linearly, joining requires full dload and verification
- Visa peak load comparison
  - Typically 2,000 txns / sec
  - Peak load in 2013: 47,000 txns / sec



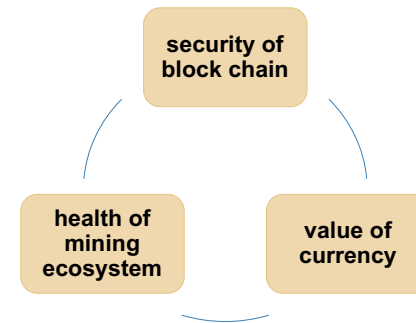
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## Summary

- Coins xfer/split between “addresses” (PK) in txns
- Blockchain: Global ordered, append-only log of txns
  - Reached through decentralized consensus
    - Each epoch, “random” node selected to batch transactions into block and append block to log
  - Nodes incentivized to perform work and act correctly
    - When “solve” block, get block rewards + txn fees
    - Reward: 12.5 BTC @ ~730 USD/BTC (11-25-16) = \$9125 / 10 min
    - Only “keep” reward if block persists on main chain

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## Bitcoin & blockchain intrinsically linked



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## Rich ecosystem: Mining pools

health of mining ecosystem

- Mining == gambling:
  - Electricity costs \$, huge payout, low probability of winning
- Development of mining pools to **amortize risk**
  - Pool computational resources, participants “paid” to mine e.g., rewards “split” as a fraction of work, etc
  - Verification? Demonstrate “easier” proofs of work to admins
  - Prevent theft? Block header (coinbase txn) given by pool

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More than just currency...

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