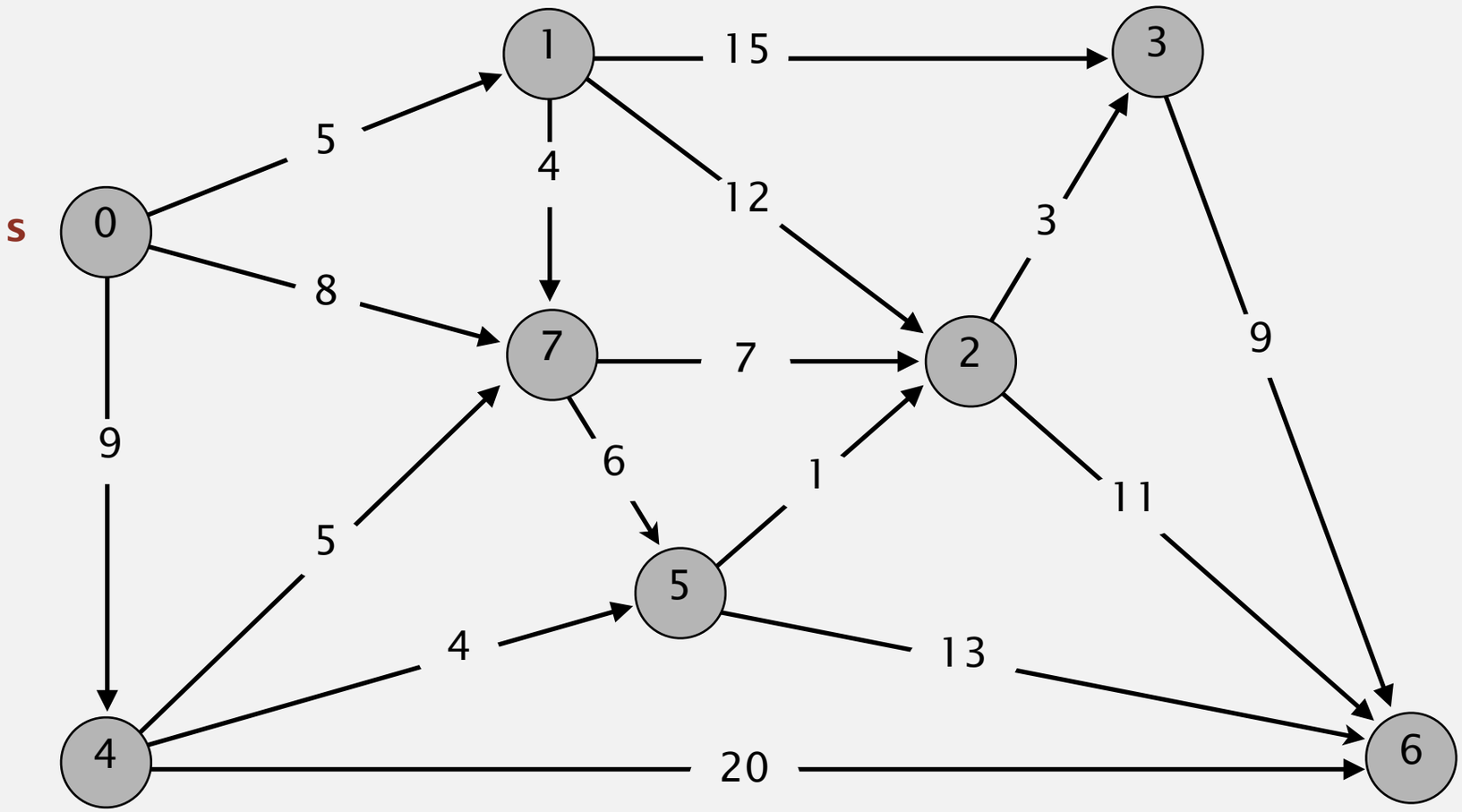
http://algs4.cs.princeton.edu

ACYCLIC SHORTEST PATHS DEMO

Last updated on 11/16/17 6:19 PM

Acyclic shortest paths demo

- Consider vertices in topological order.
- Relax all edges adjacent from that vertex.



an edge-weighted DAG

```
0→1    5.0
0→4    9.0
0→7    8.0
1→2   12.0
1→3   15.0
1→7    4.0
2→3    3.0
2→6   11.0
3→6    9.0
4→5    4.0
4→6   20.0
4→7    5.0
5→2    1.0
5→6   13.0
7→5    6.0
7→2    7.0
```

Acyclic shortest paths demo

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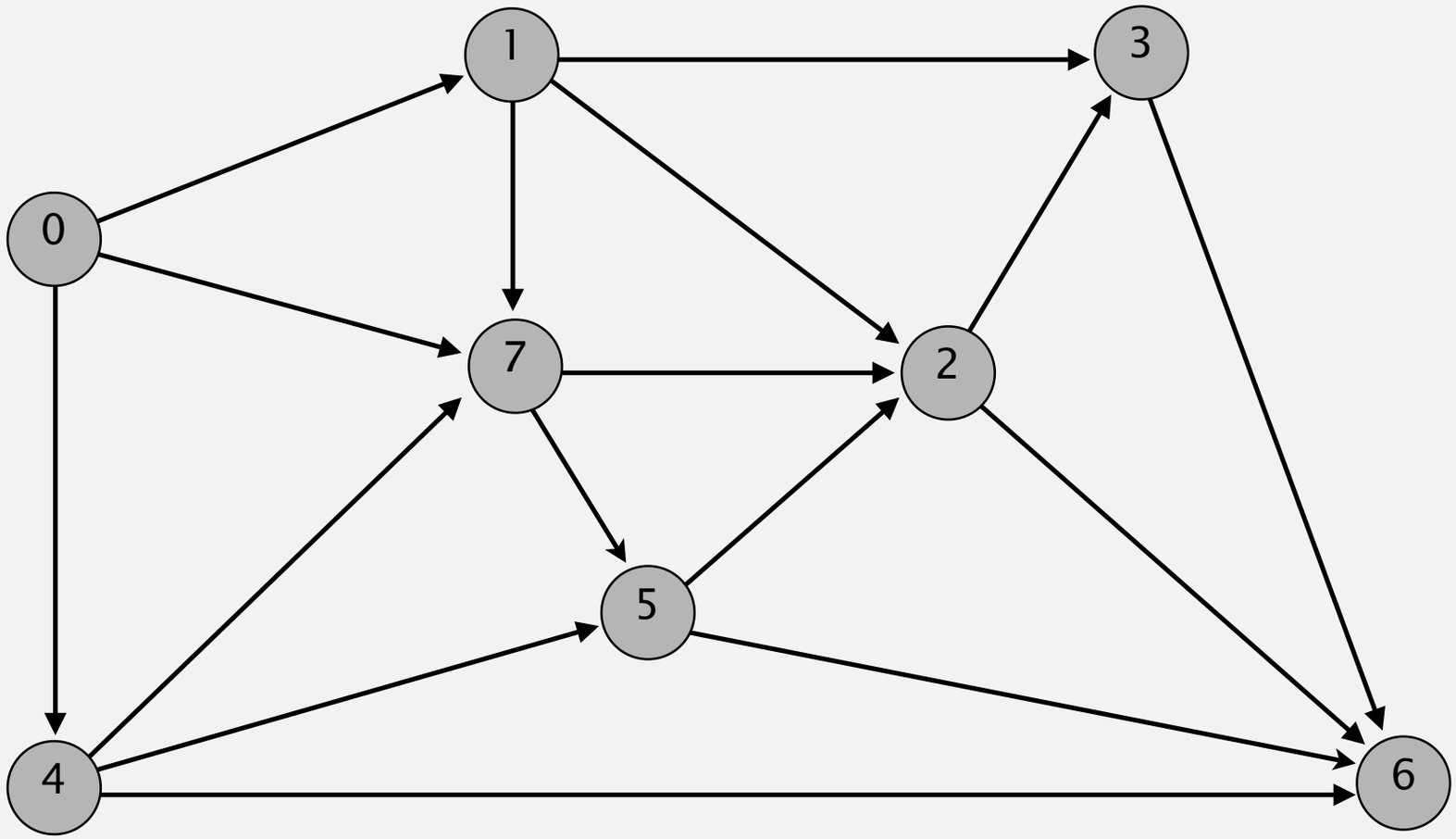
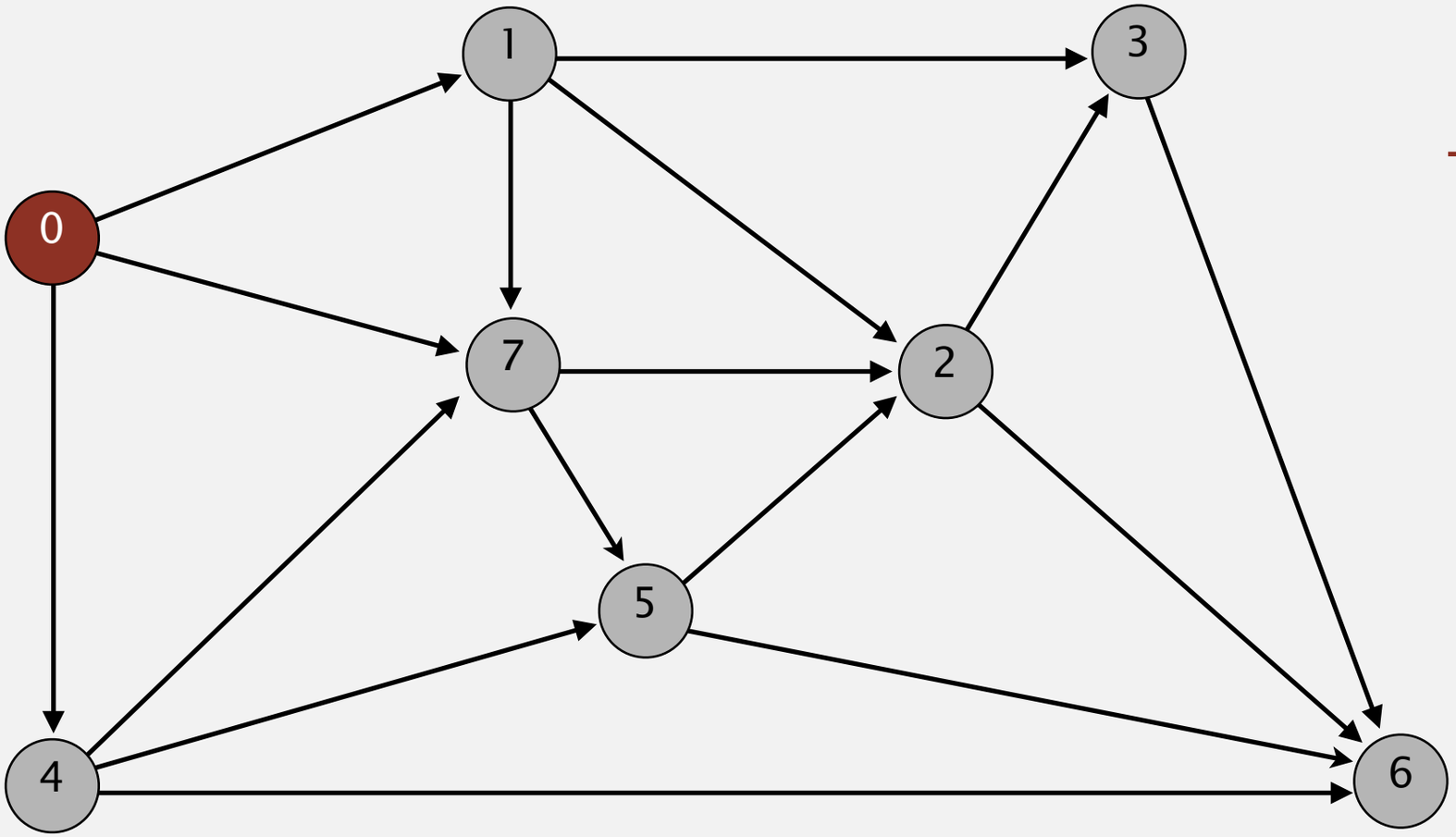


topological order: 0 1 4 7 5 2 3 6

Acyclic shortest paths demo

- Consider vertices in topological order.
- Relax all edges adjacent from that vertex.



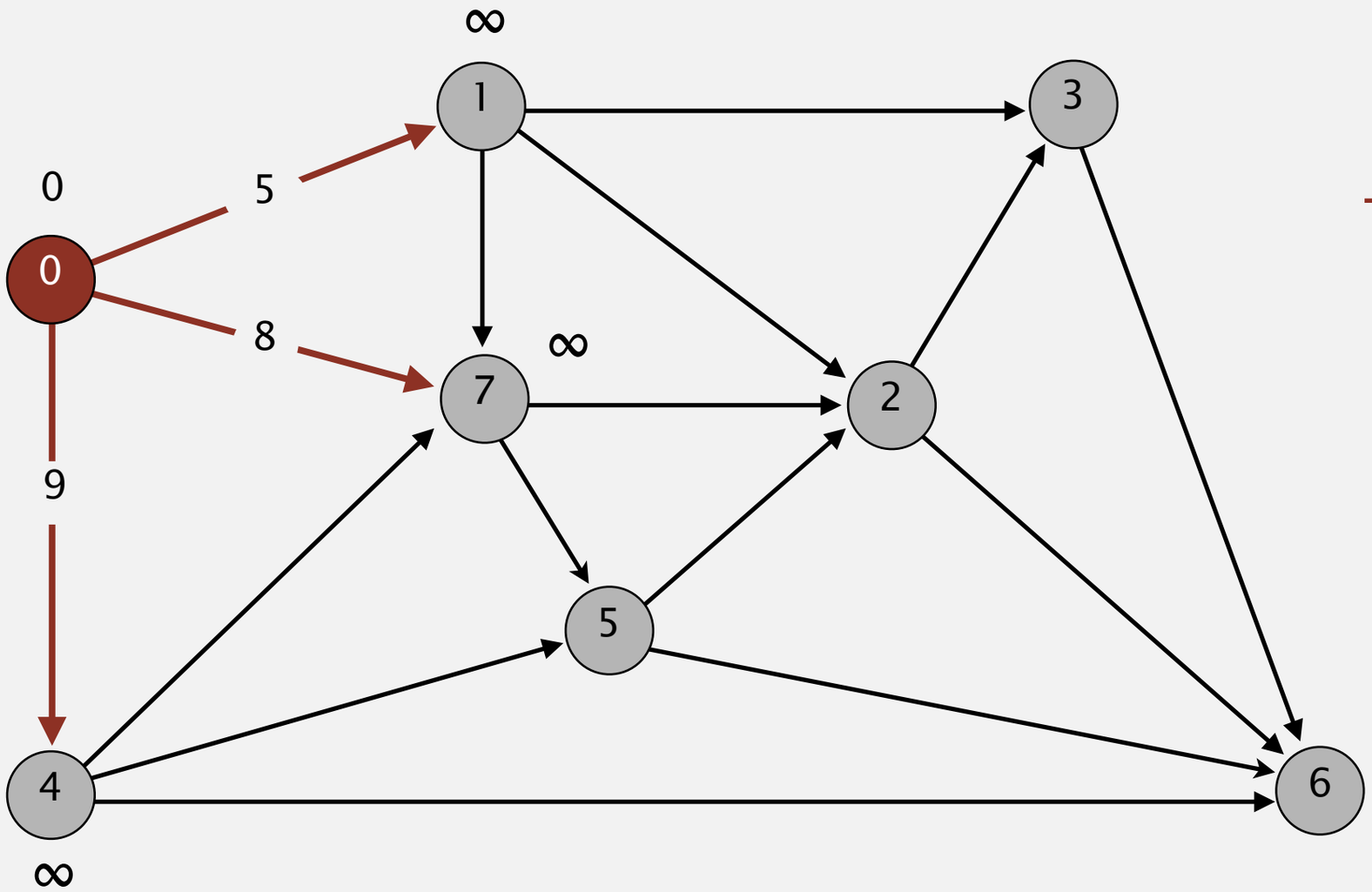
0 1 4 7 5 2 3 6

v	distTo[]	edgeTo[]
0	0.0	-
1		
2		
3		
4		
5		
6		
7		

choose vertex 0

Acyclic shortest paths demo

- Consider vertices in topological order.
- Relax all edges adjacent from that vertex.



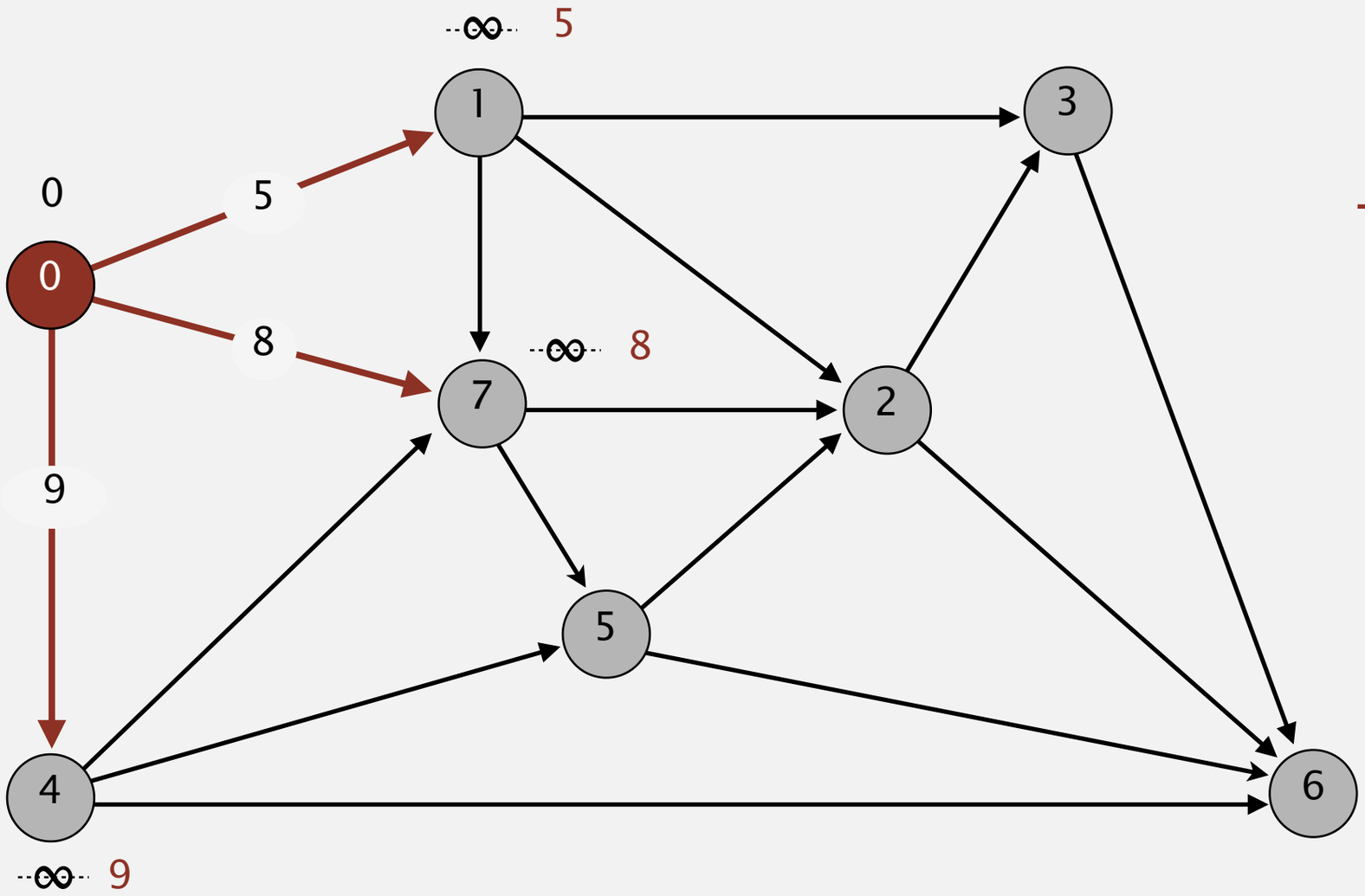
v	distTo[]	edgeTo[]
0	0.0	-
1		
2		
3		
4		
5		
6		
7		

0 1 4 7 5 2 3 6

relax all edges adjacent from 0

Acyclic shortest paths demo

- Consider vertices in topological order.
- Relax all edges adjacent from that vertex.

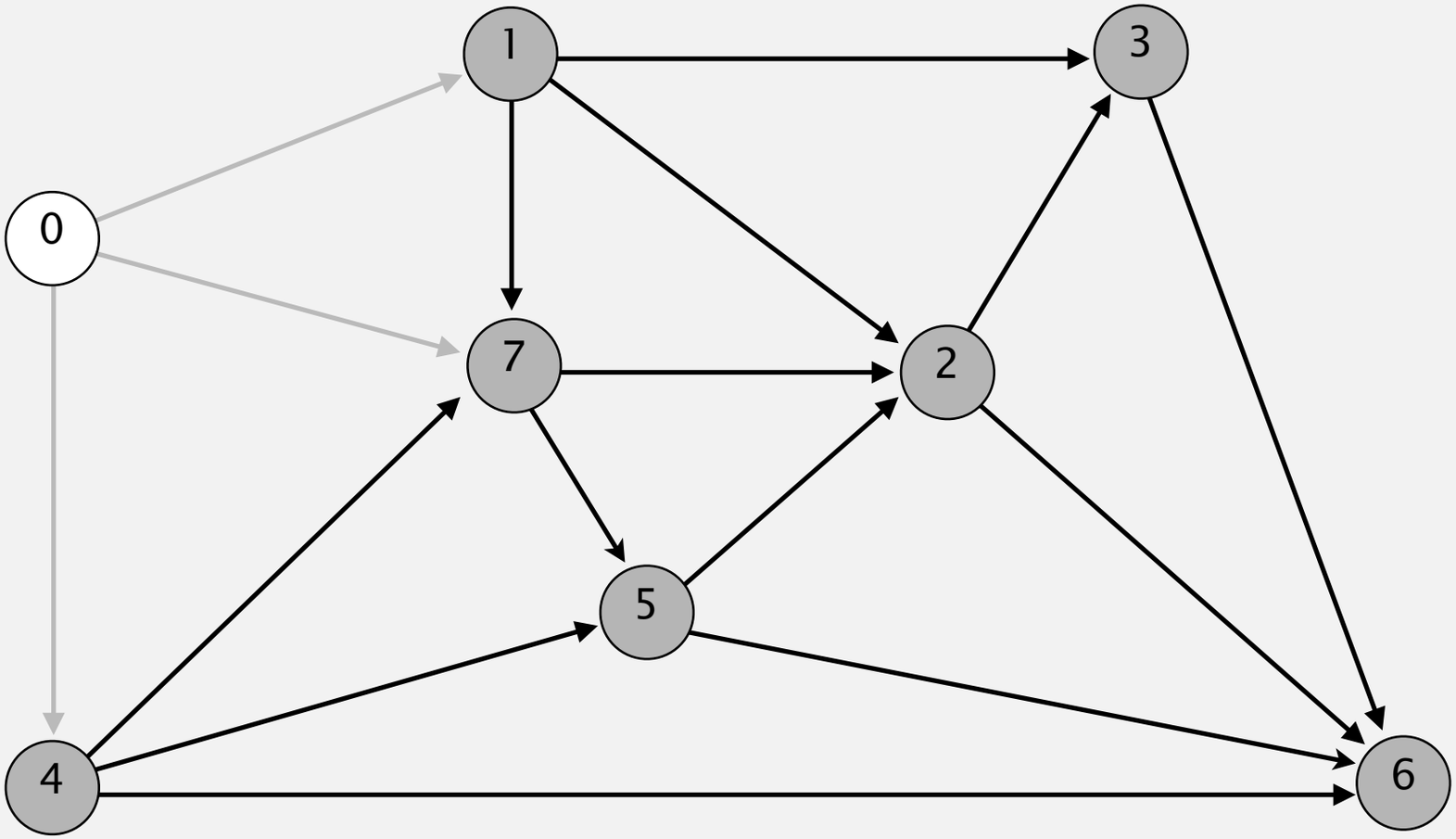


	v	distTo[]	edgeTo[]
→	0	0.0	-
	1	5.0	0→1
	2		
	3		
	4	9.0	0→4
	5		
	6		
	7	8.0	0→7

relax all edges adjacent from 0

Acyclic shortest paths demo

- Consider vertices in topological order.
- Relax all edges adjacent from that vertex.

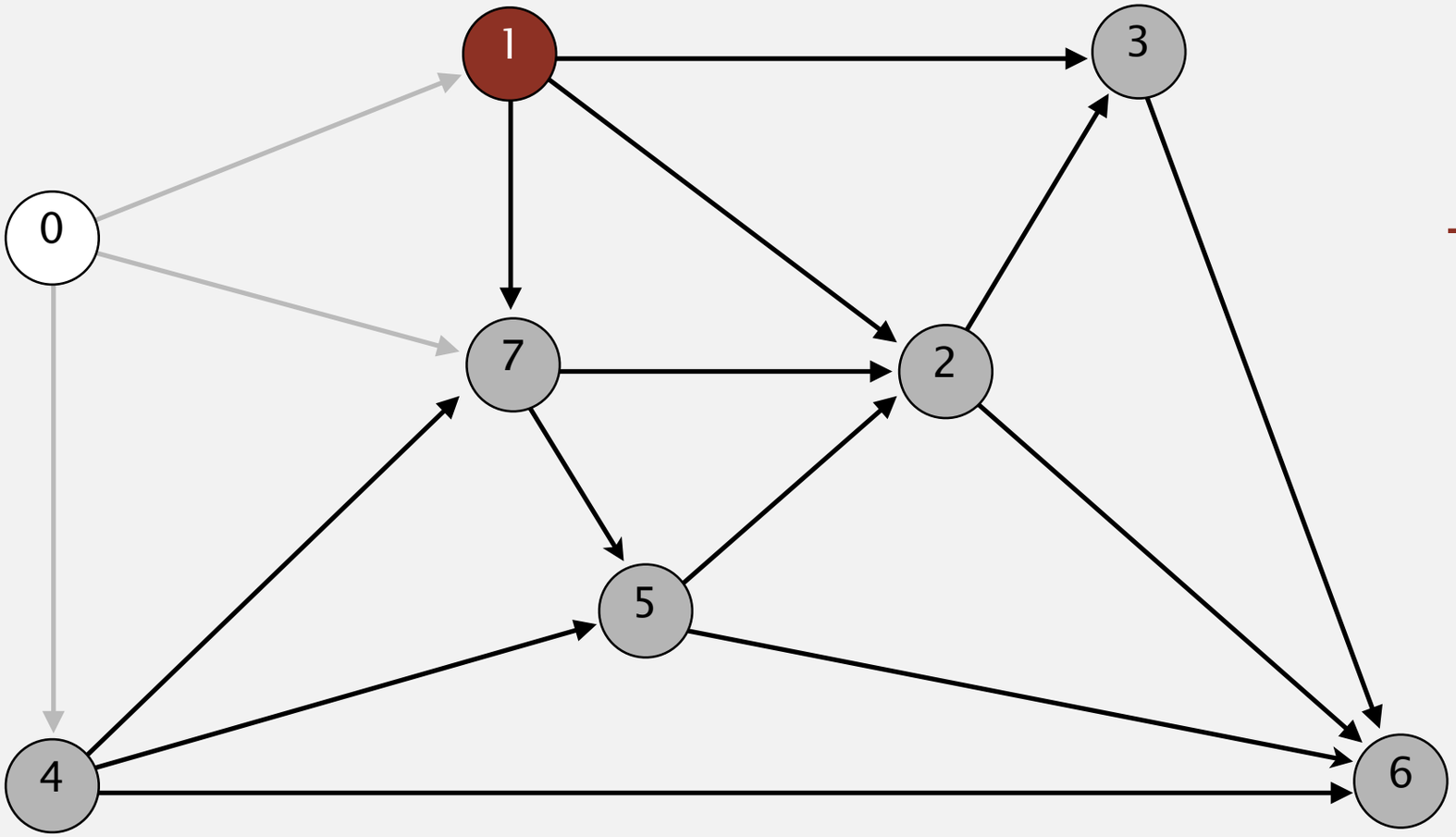


0 1 4 7 5 2 3 6

v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2		
3		
4	9.0	0→4
5		
6		
7	8.0	0→7

Acyclic shortest paths demo

- Consider vertices in topological order.
- Relax all edges adjacent from that vertex.



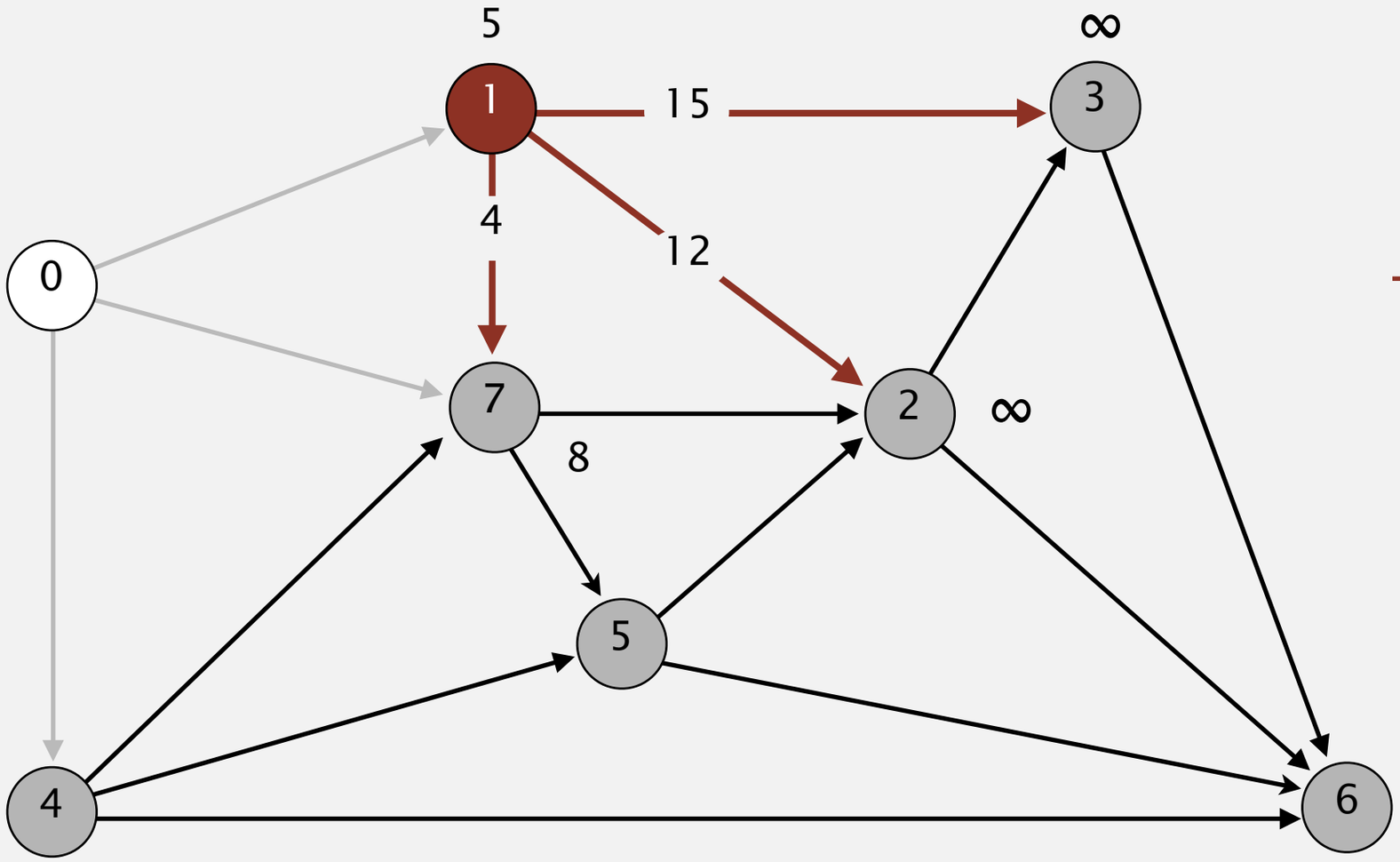
0 **1** 4 7 5 2 3 6

v	distTo[]	edgeTo[]
0	0.0	-
→ 1	5.0	0→1
2		
3		
4	9.0	0→4
5		
6		
7	8.0	0→7

choose vertex 1

Acyclic shortest paths demo

- Consider vertices in topological order.
- Relax all edges adjacent from that vertex.



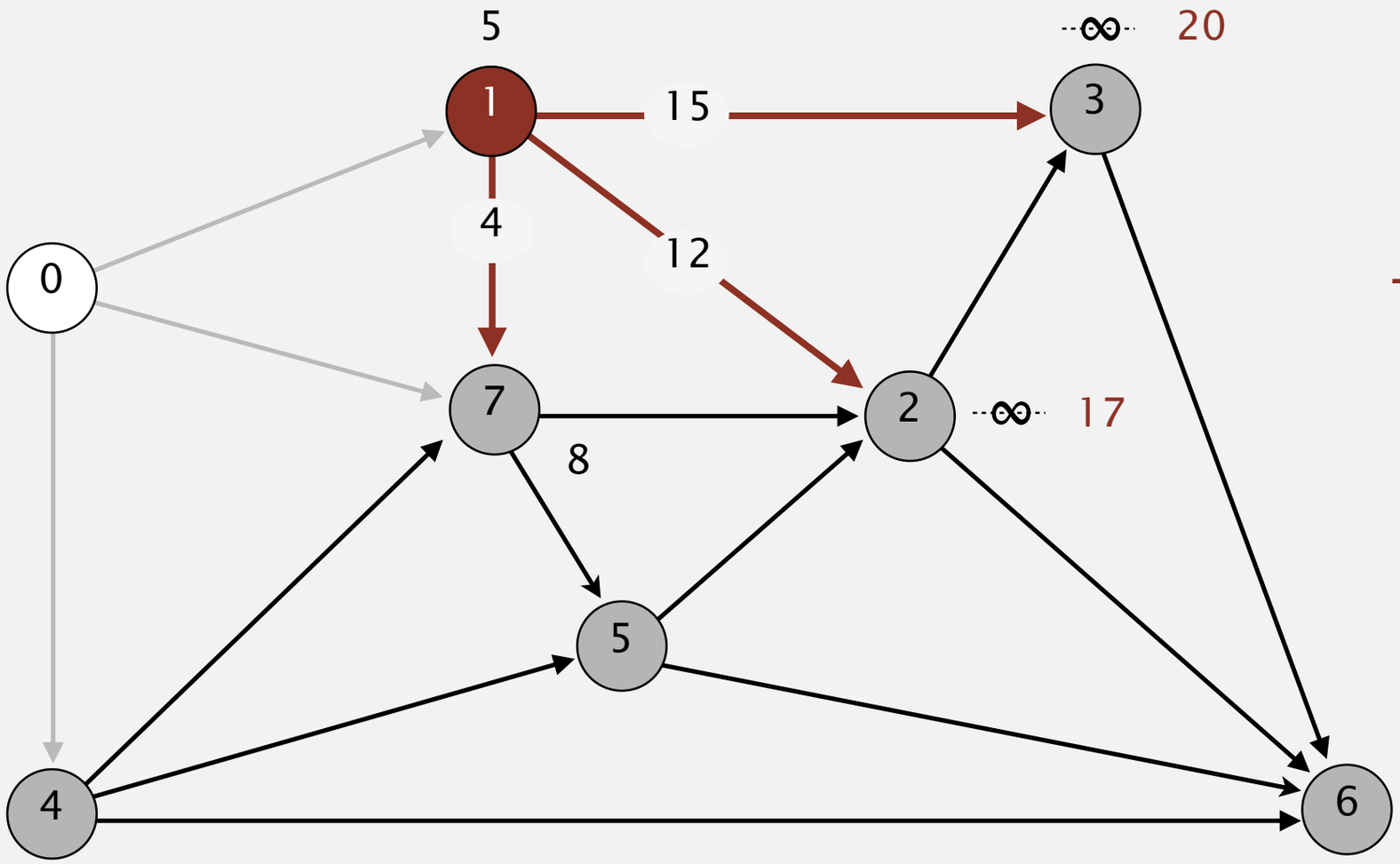
0 **1** 4 7 5 2 3 6

v	distTo[]	edgeTo[]
0	0.0	-
→ 1	5.0	0→1
2		
3		
4	9.0	0→4
5		
6		
7	8.0	0→7

relax all edges adjacent from 1

Acyclic shortest paths demo

- Consider vertices in topological order.
- Relax all edges adjacent from that vertex.



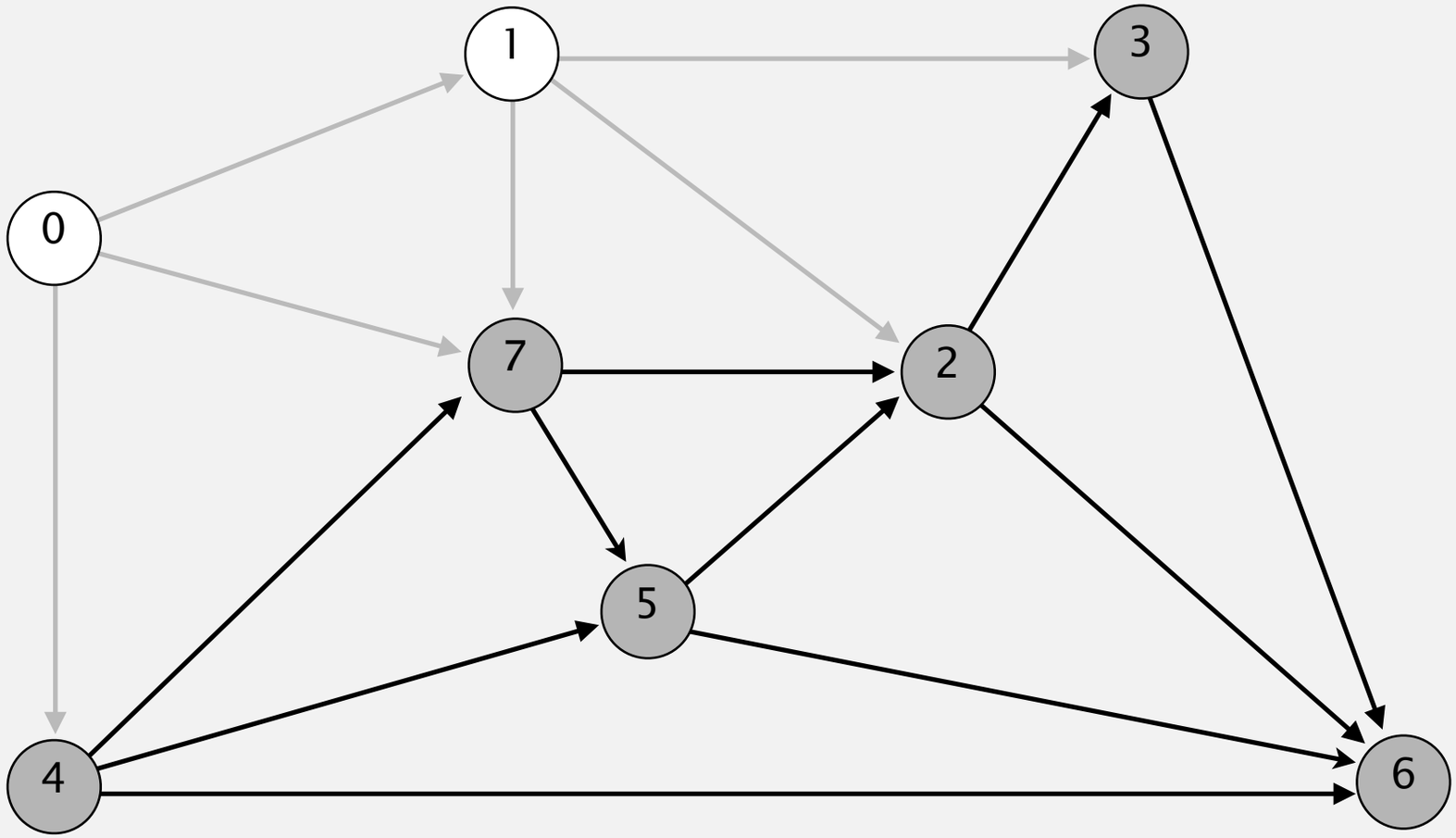
0 1 4 7 5 2 3 6

v	distTo[]	edgeTo[]
0	0.0	-
→ 1	5.0	0→1
2	17.0	1→2
3	20.0	1→3
4	9.0	0→4
5		
6		
7	8.0 ✔	0→7

relax all edges adjacent from 1

Acyclic shortest paths demo

- Consider vertices in topological order.
- Relax all edges adjacent from that vertex.

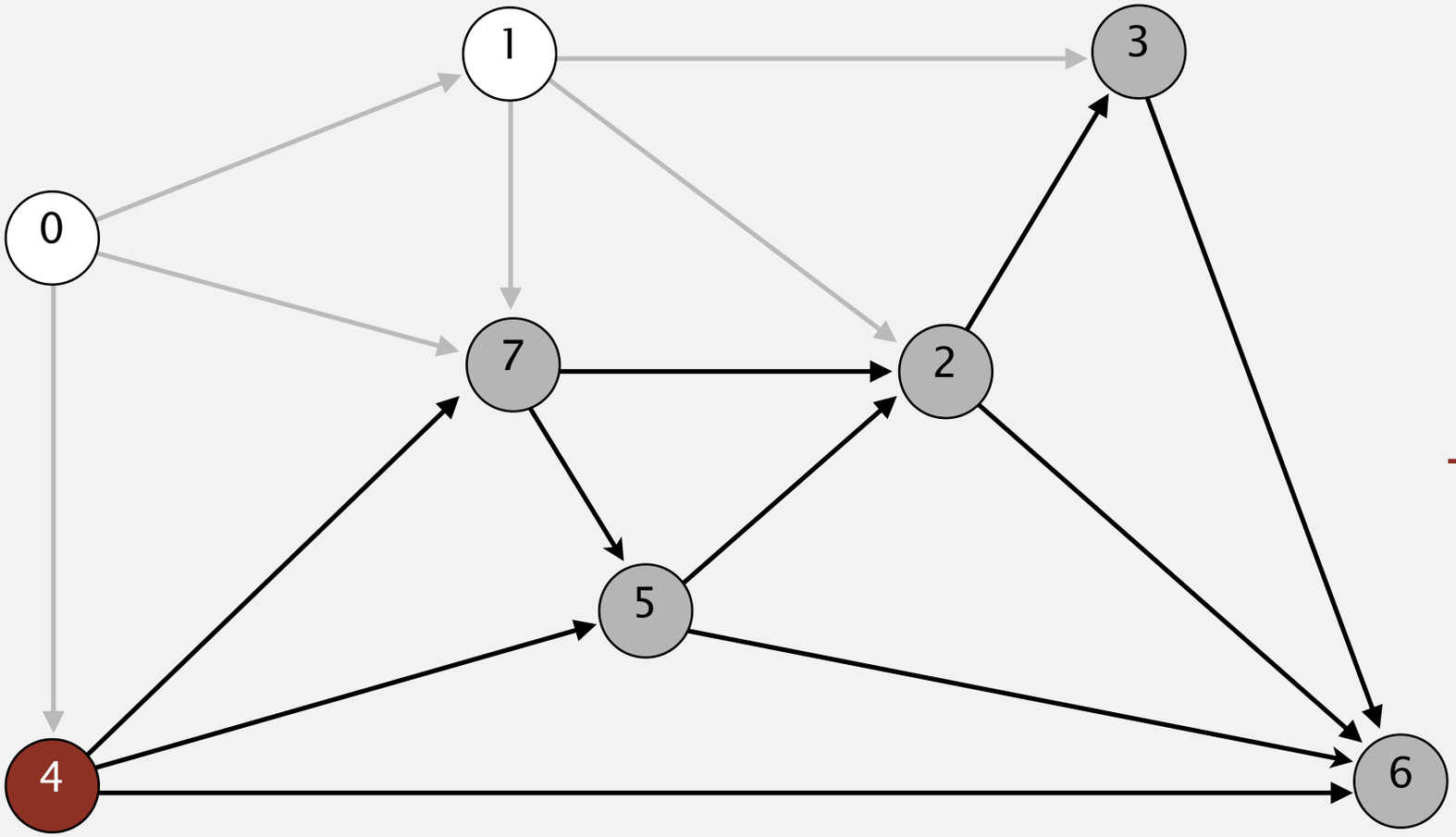


0 1 4 7 5 2 3 6

v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	17.0	1→2
3	20.0	1→3
4	9.0	0→4
5		
6		
7	8.0	0→7

Acyclic shortest paths demo

- Consider vertices in topological order.
- Relax all edges adjacent from that vertex.



0 1 4 7 5 2 3 6

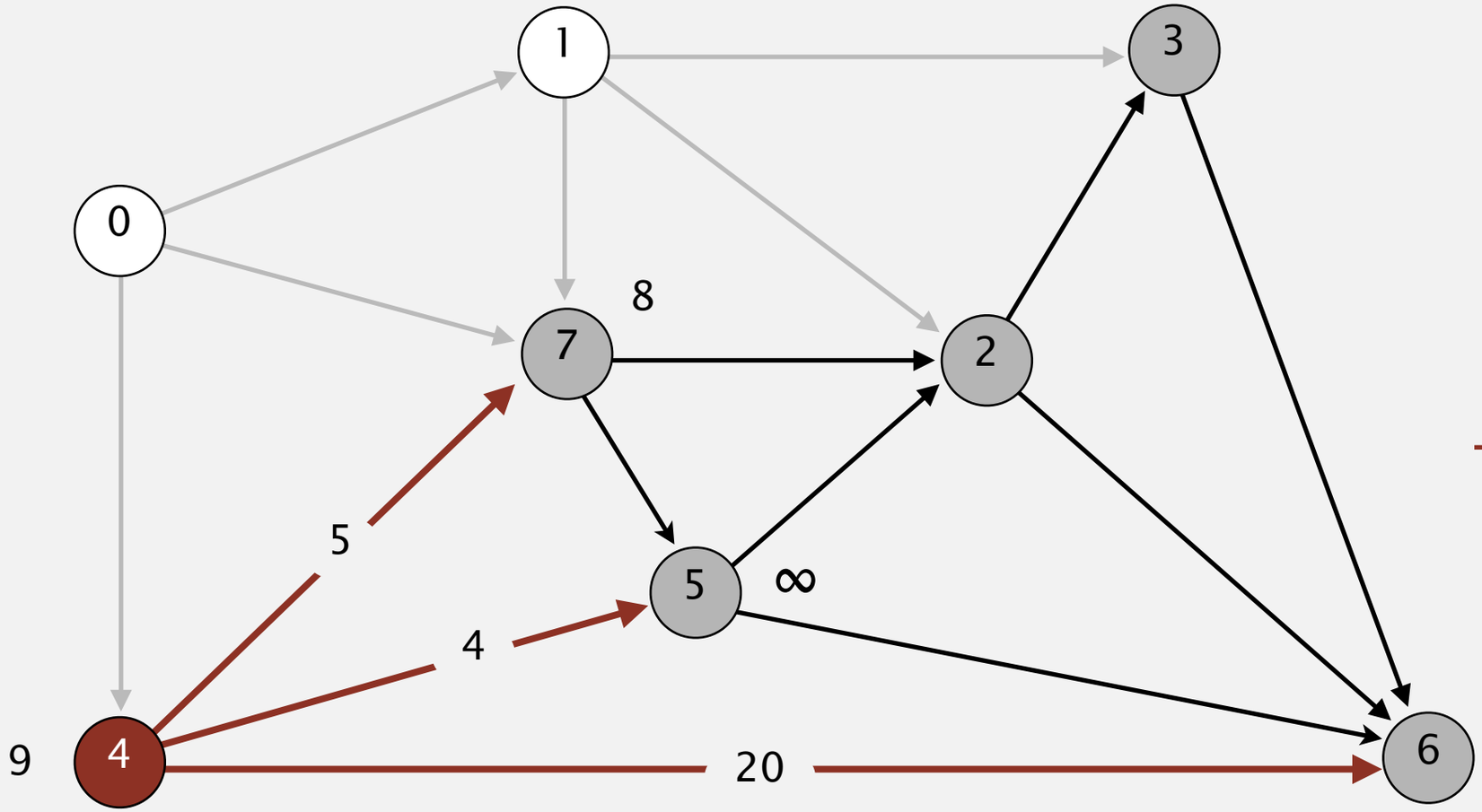
	v	distTo[]	edgeTo[]
	0	0.0	-
	1	5.0	0→1
	2	17.0	1→2
	3	20.0	1→3
→	4	9.0	0→4
	5		
	6		
	7	8.0	0→7

select vertex 4

(Dijkstra would have selected vertex 7)

Acyclic shortest paths demo

- Consider vertices in topological order.
- Relax all edges adjacent from that vertex.



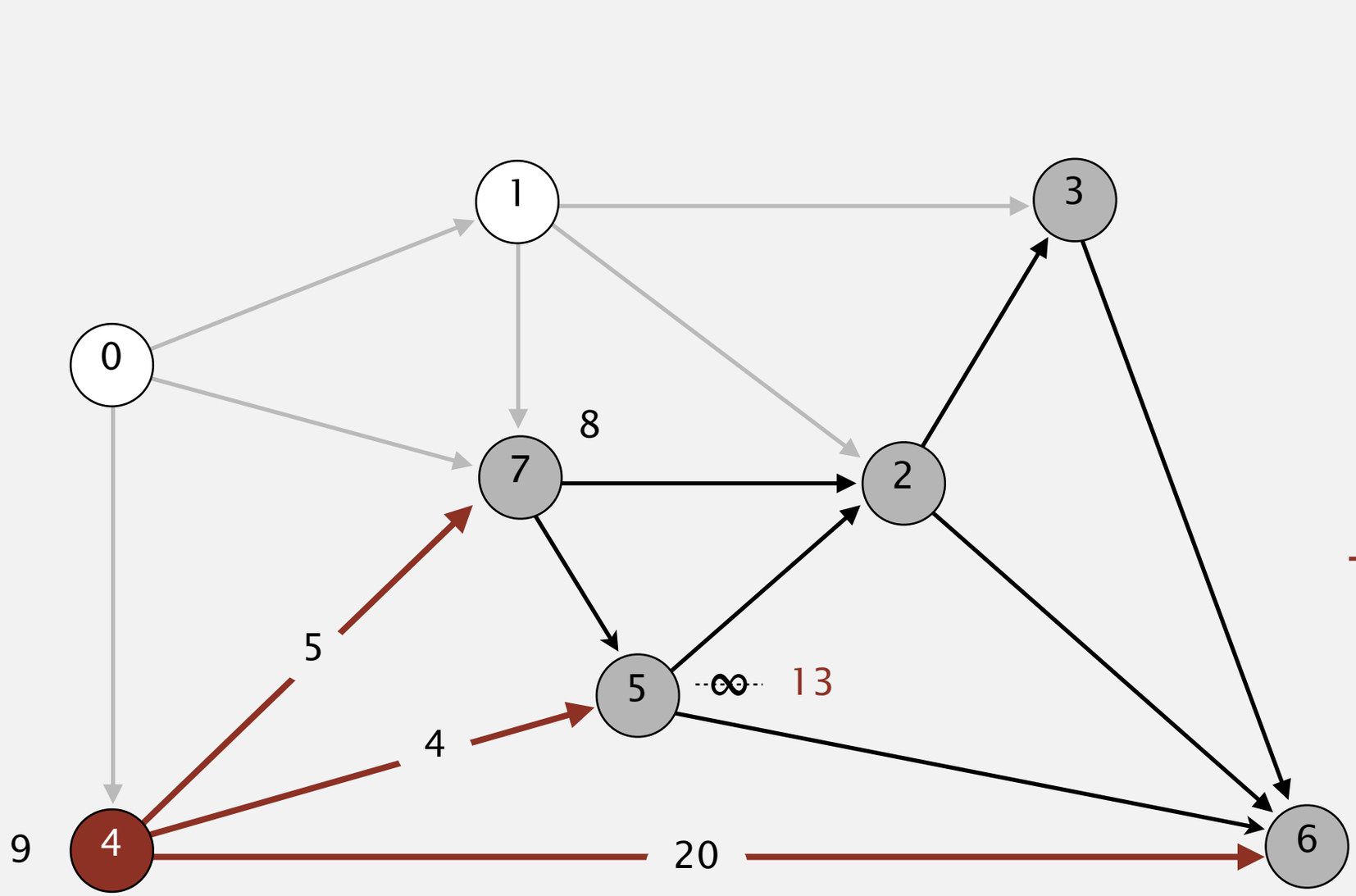
0 1 4 7 5 2 3 6

v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	17.0	1→2
3	20.0	1→3
→ 4	9.0	0→4
5		
6		
7	8.0	0→7

relax all edges adjacent from 4

Acyclic shortest paths demo

- Consider vertices in topological order.
- Relax all edges adjacent from that vertex.



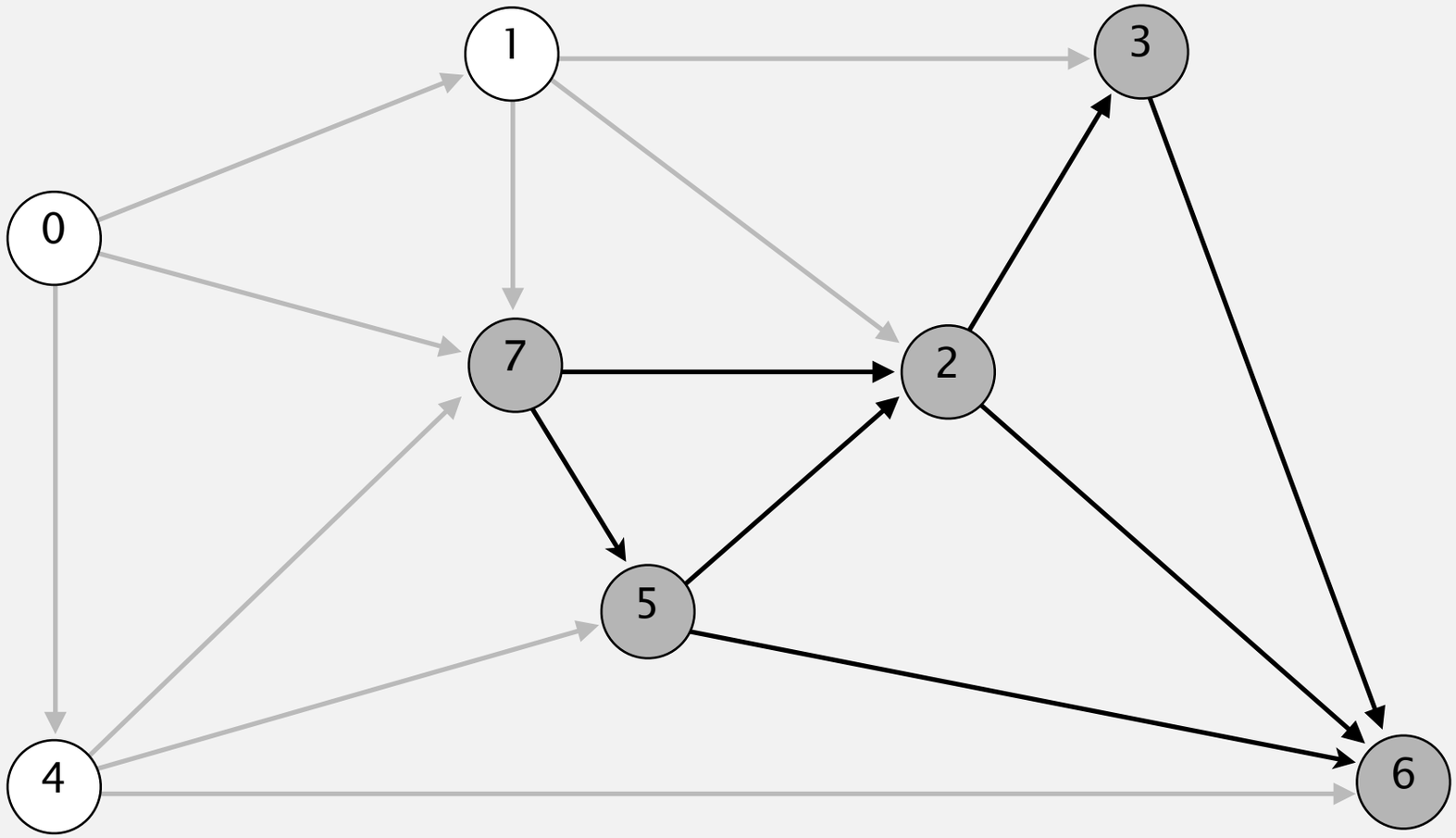
0 1 4 7 5 2 3 6

v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	17.0	1→2
3	20.0	1→3
→ 4	9.0	0→4
5	13.0	4→5
6	29.0	4→6
7	8.0 ✔	0→7

relax all edges adjacent from 4

Acyclic shortest paths demo

- Consider vertices in topological order.
- Relax all edges adjacent from that vertex.

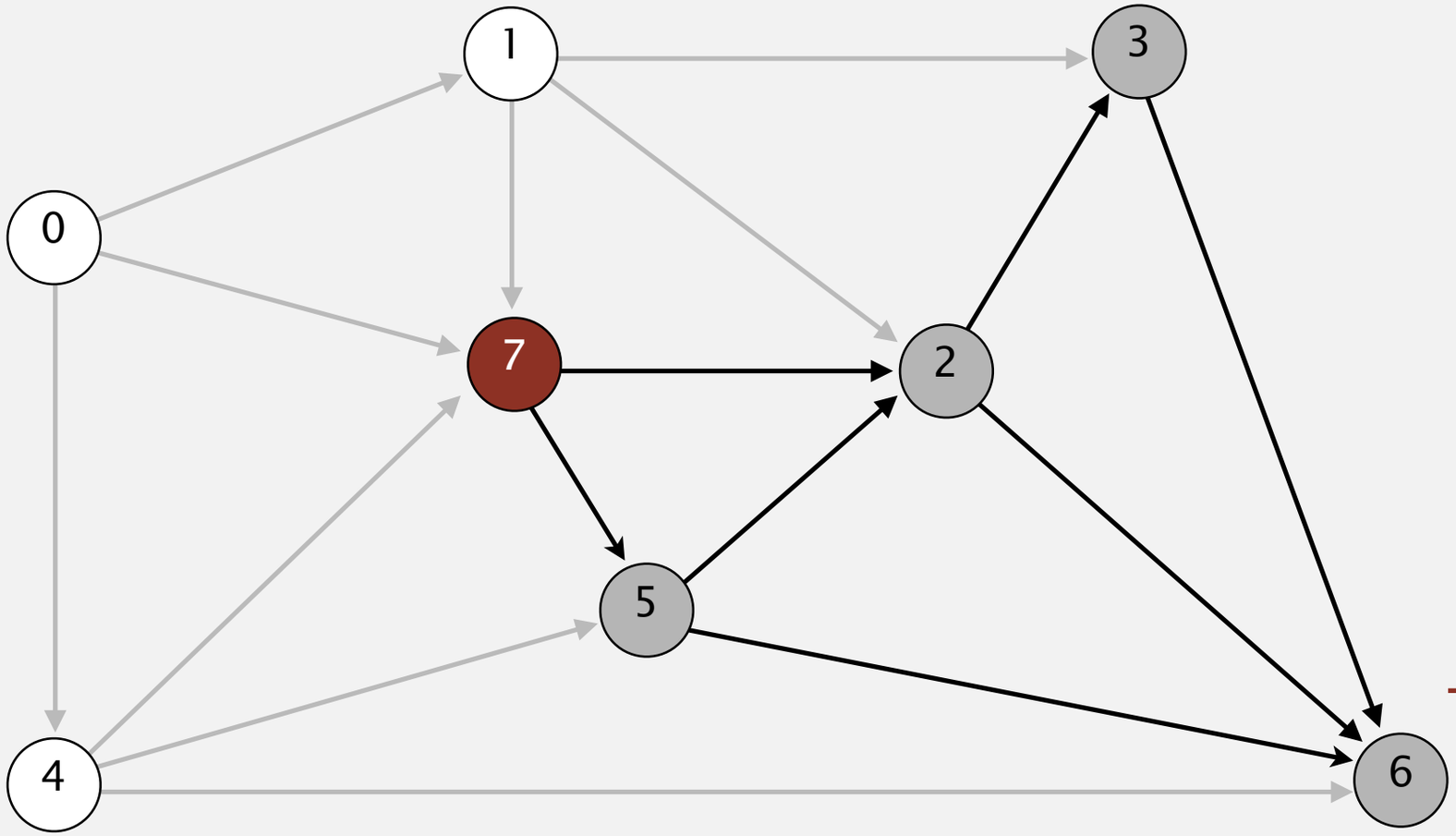


0 1 4 7 5 2 3 6

v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	17.0	1→2
3	20.0	1→3
4	9.0	0→4
5	13.0	4→5
6	29.0	4→6
7	8.0	0→7

Acyclic shortest paths demo

- Consider vertices in topological order.
- Relax all edges adjacent from that vertex.



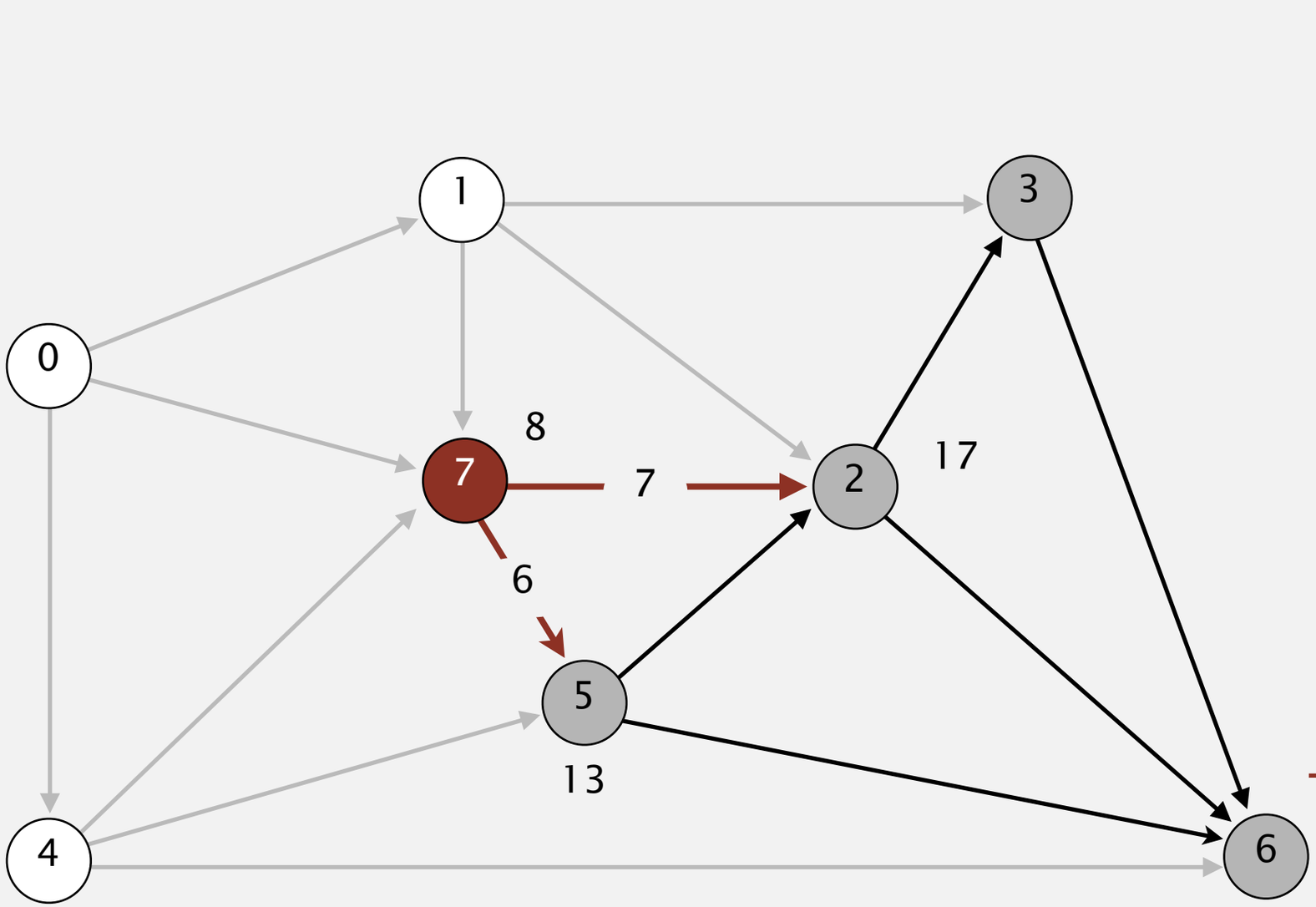
0 1 4 7 5 2 3 6

v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	17.0	1→2
3	20.0	1→3
4	9.0	0→4
5	13.0	4→5
6	29.0	4→6
→ 7	8.0	0→7

choose vertex 7

Acyclic shortest paths demo

- Consider vertices in topological order.
- Relax all edges adjacent from that vertex.



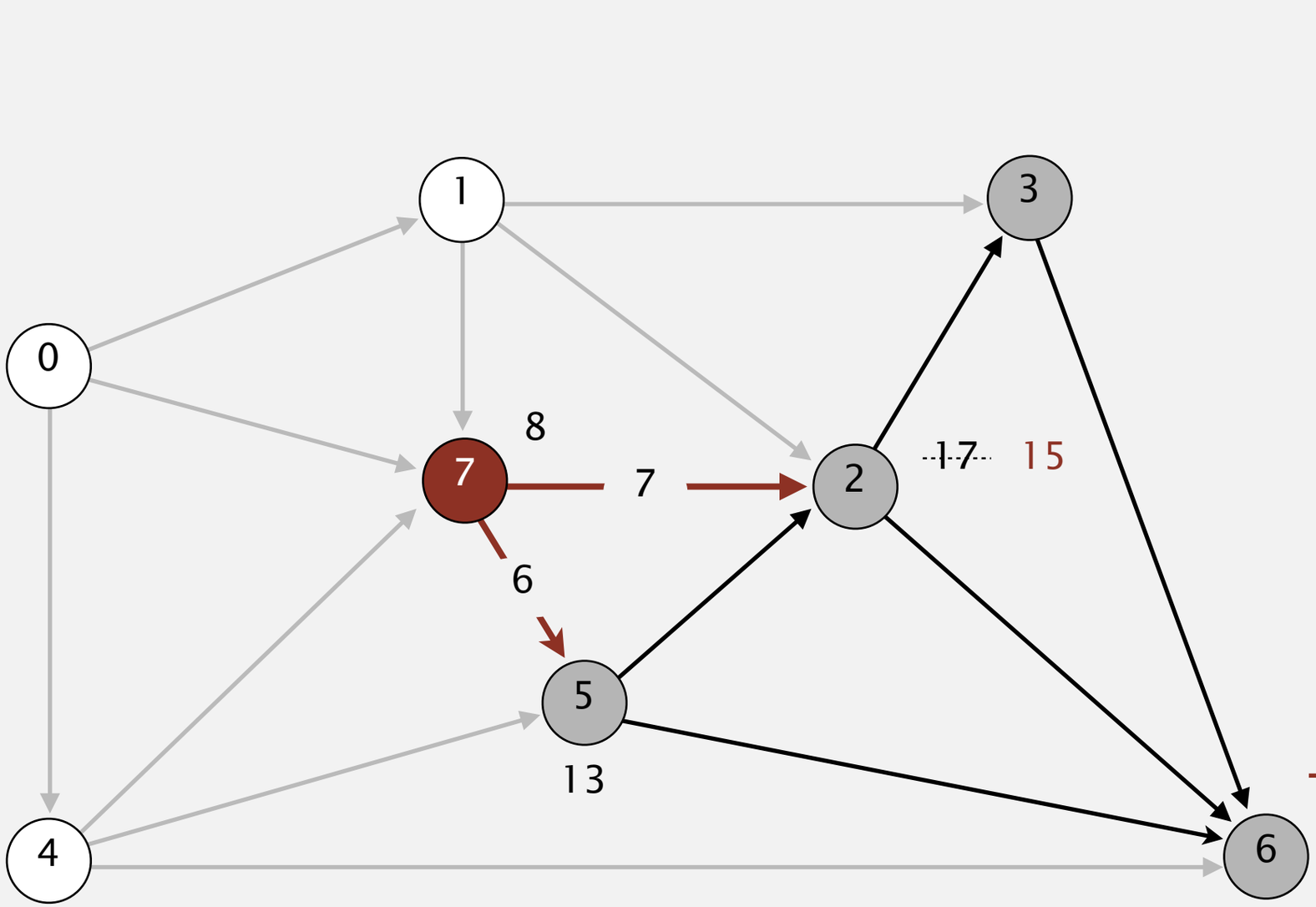
0 1 4 7 5 2 3 6

v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	17.0	1→2
3	20.0	1→3
4	9.0	0→4
5	13.0	4→5
6	29.0	4→6
→ 7	8.0	0→7

relax all edges adjacent from 7

Acyclic shortest paths demo

- Consider vertices in topological order.
- Relax all edges adjacent from that vertex.



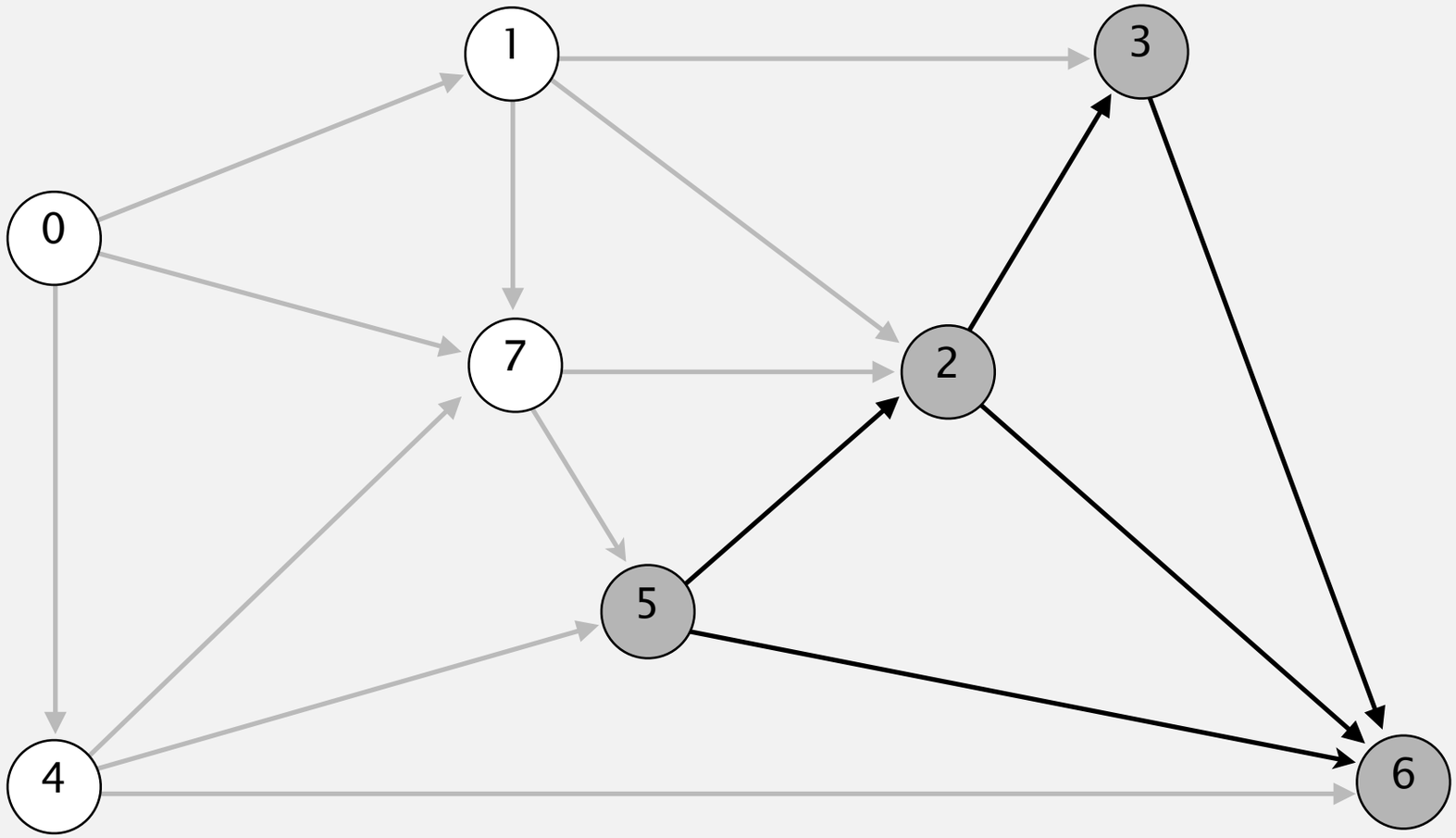
0 1 4 7 5 2 3 6

v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	15.0	7→2
3	20.0	1→3
4	9.0	0→4
5	13.0 ✔	4→5
6	29.0	4→6
→ 7	8.0	0→7

relax all edges adjacent from 7

Acyclic shortest paths demo

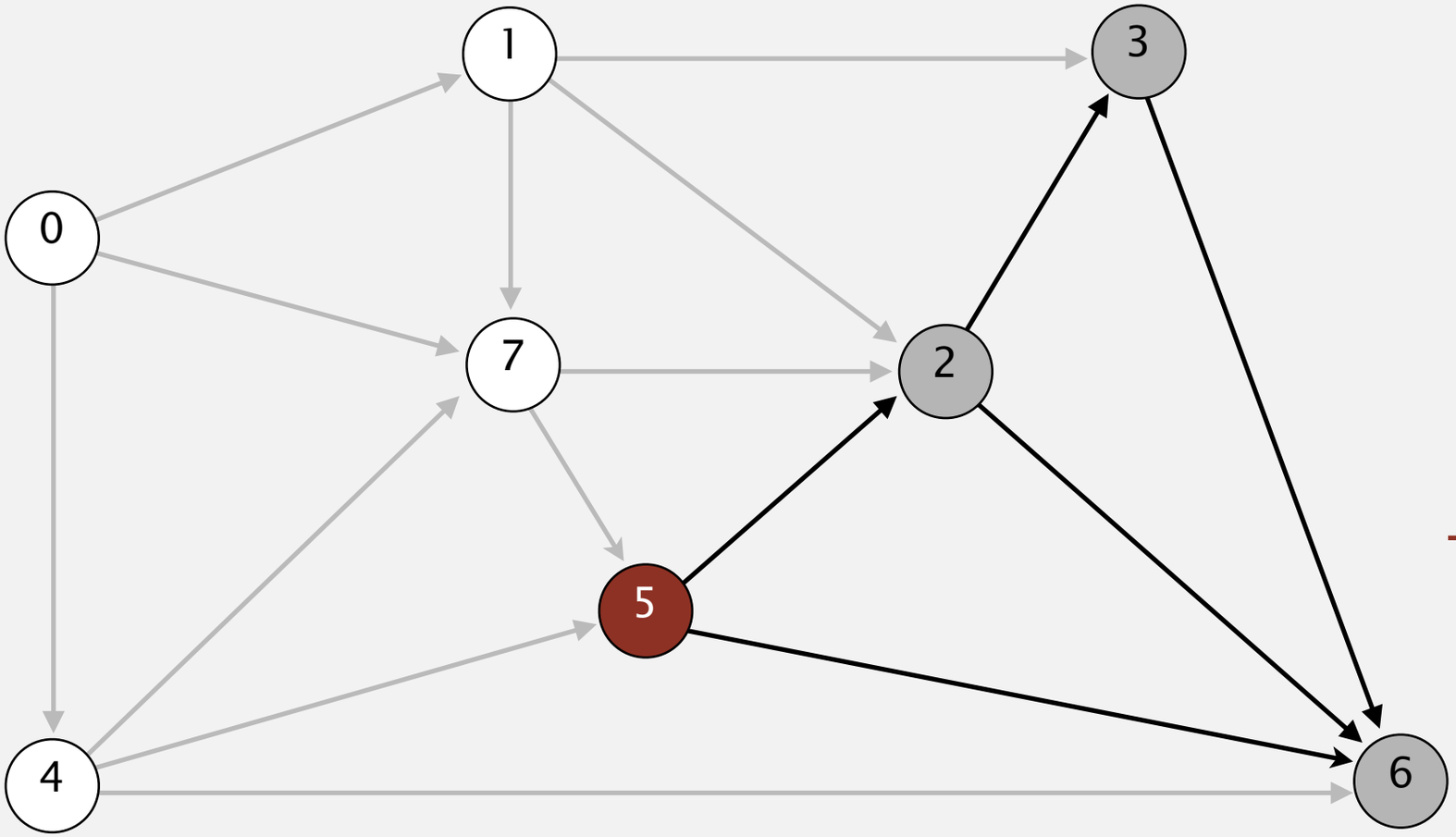
- Consider vertices in topological order.
- Relax all edges adjacent from that vertex.



v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	15.0	7→2
3	20.0	1→3
4	9.0	0→4
5	13.0	4→5
6	29.0	4→6
7	8.0	0→7

Acyclic shortest paths demo

- Consider vertices in topological order.
- Relax all edges adjacent from that vertex.



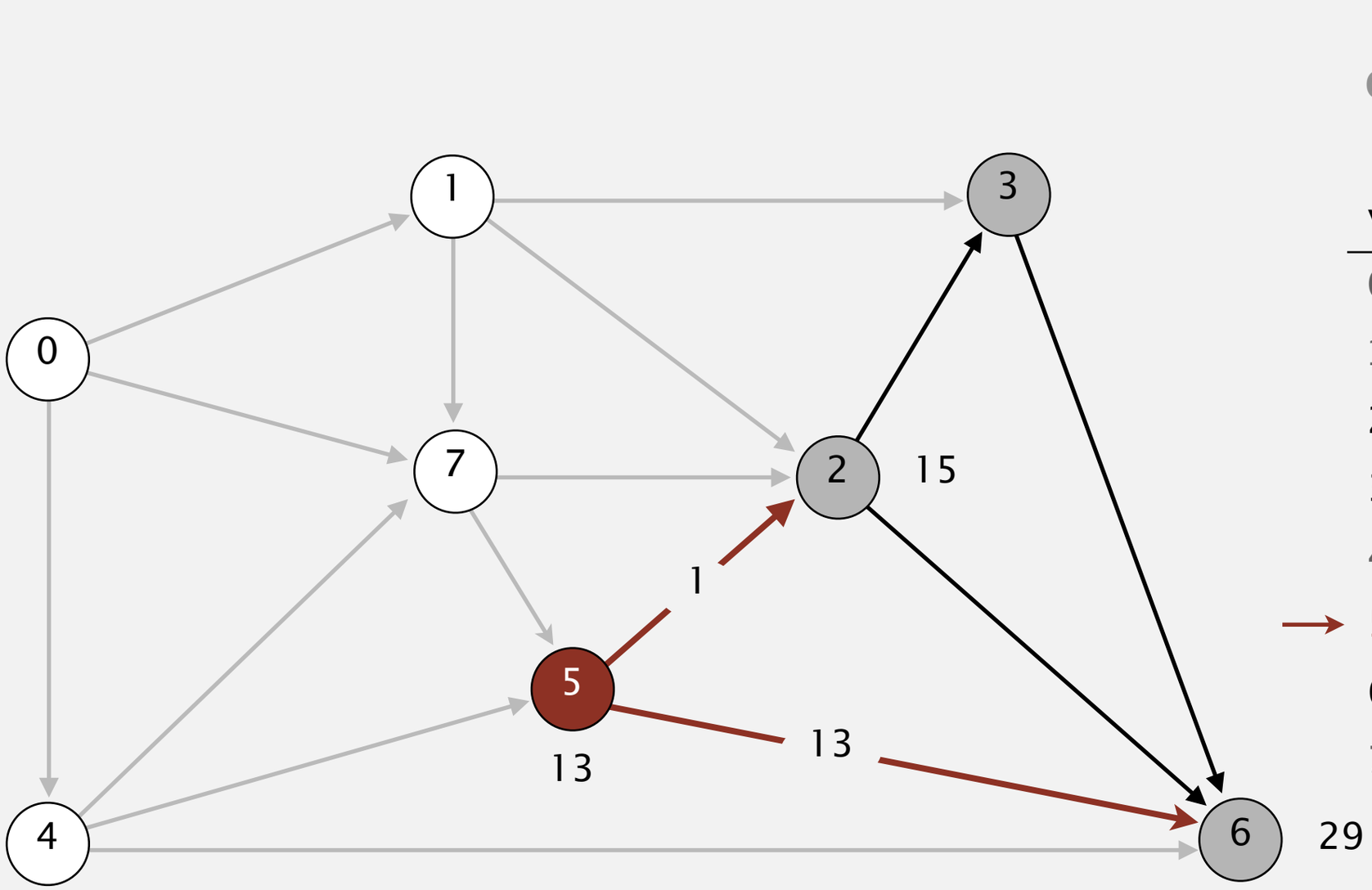
0 1 4 7 **5** 2 3 6

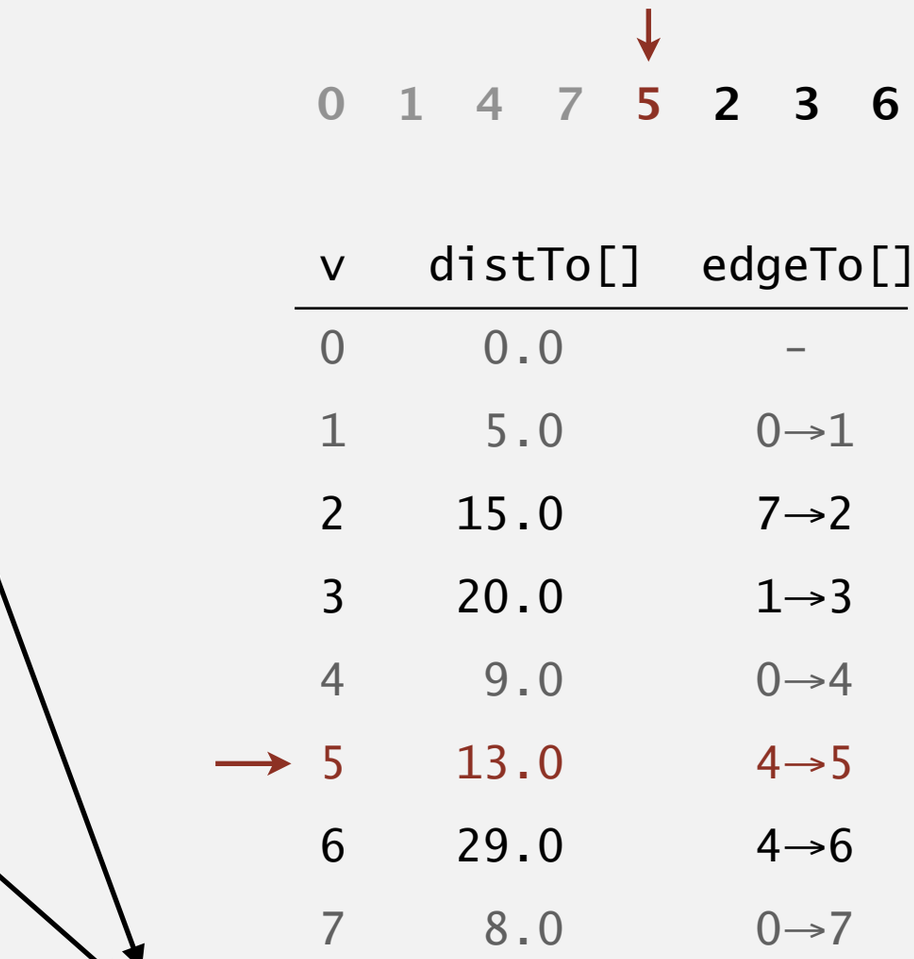
v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	15.0	7→2
3	20.0	1→3
4	9.0	0→4
→ 5	13.0	4→5
6	29.0	4→6
7	8.0	0→7

select vertex 5

Acyclic shortest paths demo

- Consider vertices in topological order.
- Relax all edges adjacent from that vertex.



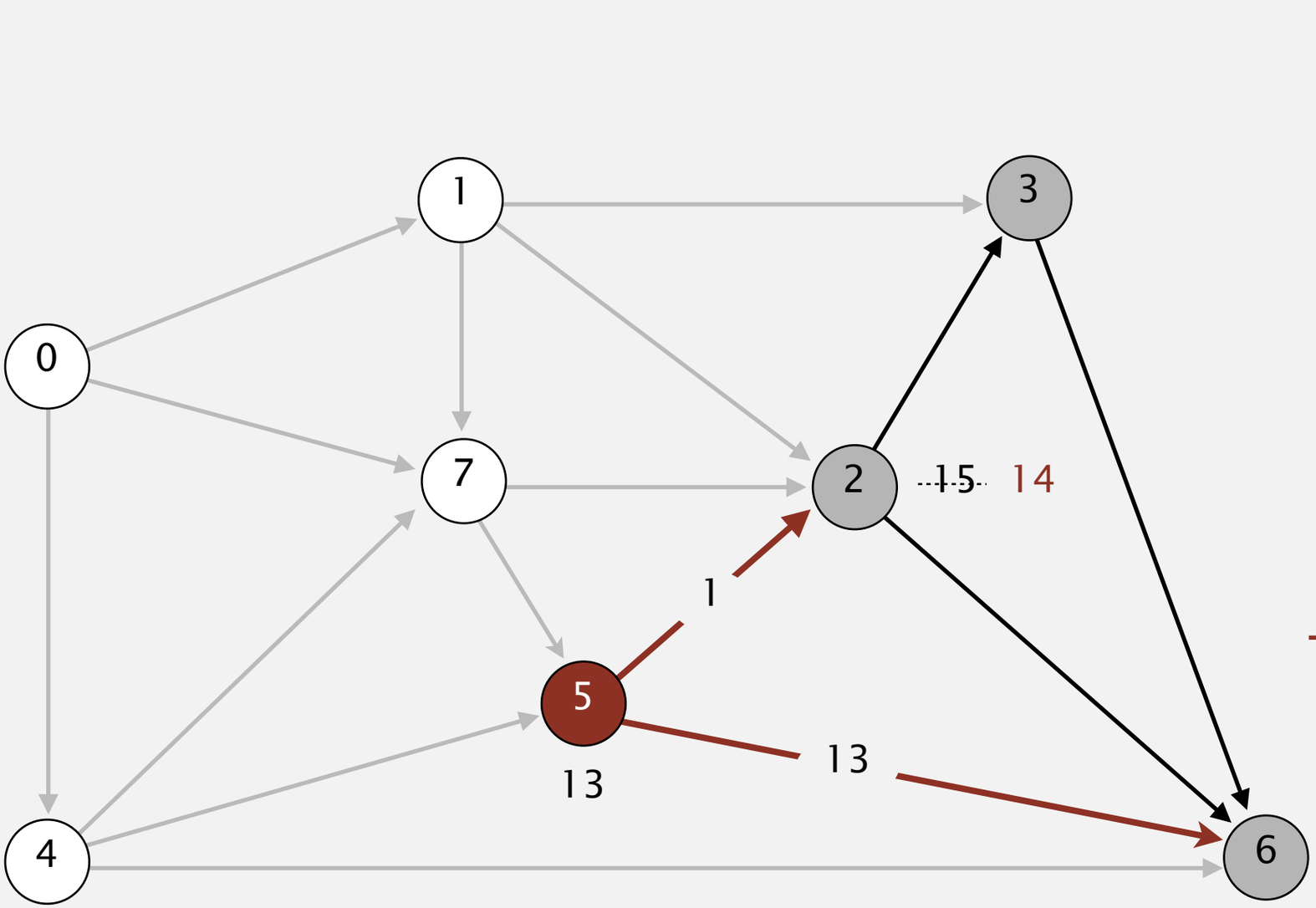


	v	distTo[]	edgeTo[]
	0	0.0	-
	1	5.0	0→1
	2	15.0	7→2
	3	20.0	1→3
	4	9.0	0→4
→	5	13.0	4→5
	6	29.0	4→6
	7	8.0	0→7

relax all edges adjacent from 5

Acyclic shortest paths demo

- Consider vertices in topological order.
- Relax all edges adjacent from that vertex.



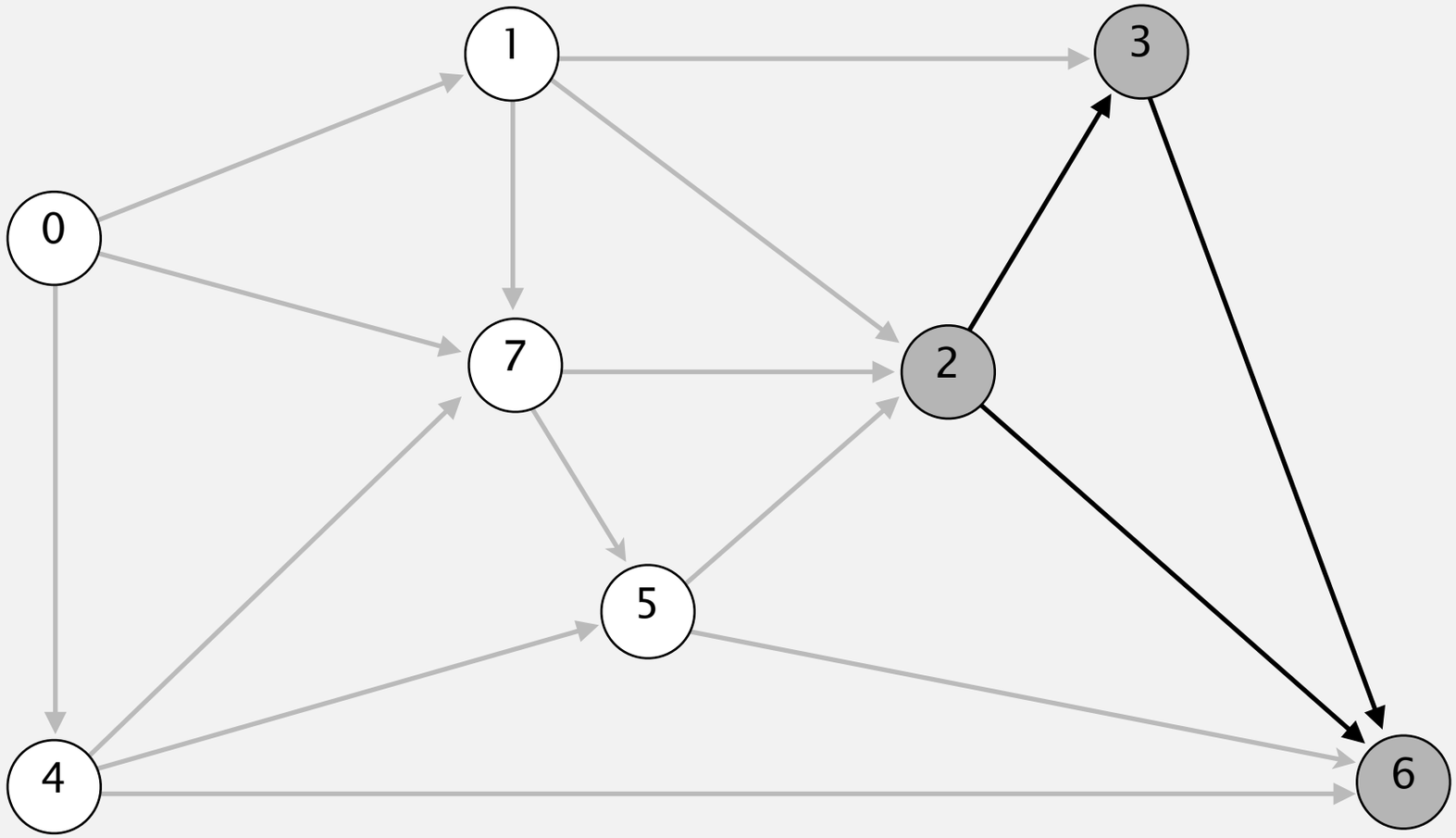
0 1 4 7 5 2 3 6

v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	14.0	5→2
3	20.0	1→3
4	9.0	0→4
→ 5	13.0	4→5
6	26.0	5→6
7	8.0	0→7

relax all edges adjacent from 5

Acyclic shortest paths demo

- Consider vertices in topological order.
- Relax all edges adjacent from that vertex.

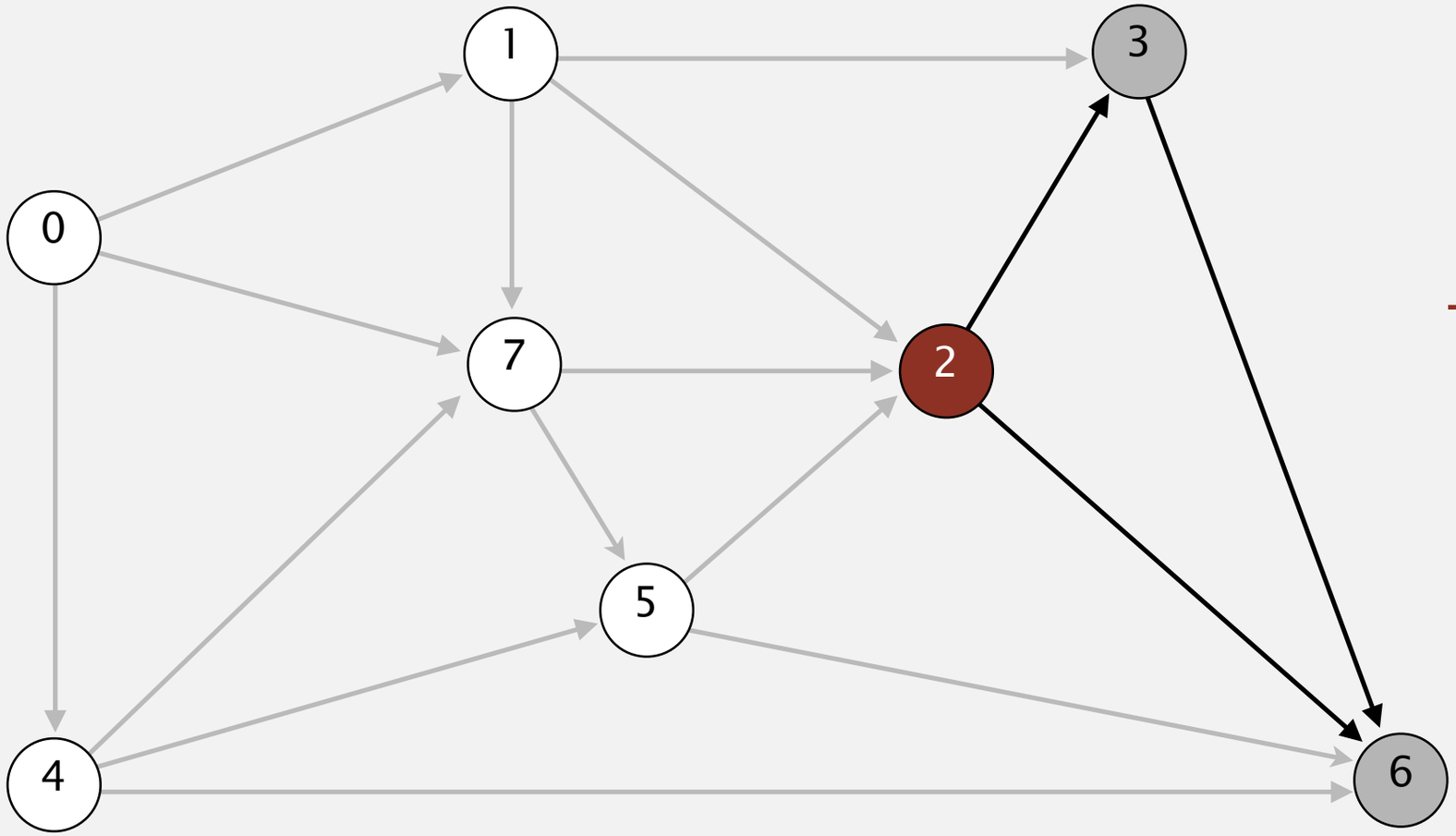


0 1 4 7 5 2 3 6

v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	14.0	5→2
3	20.0	1→3
4	9.0	0→4
5	13.0	4→5
6	26.0	5→6
7	8.0	0→7

Acyclic shortest paths demo

- Consider vertices in topological order.
- Relax all edges adjacent from that vertex.



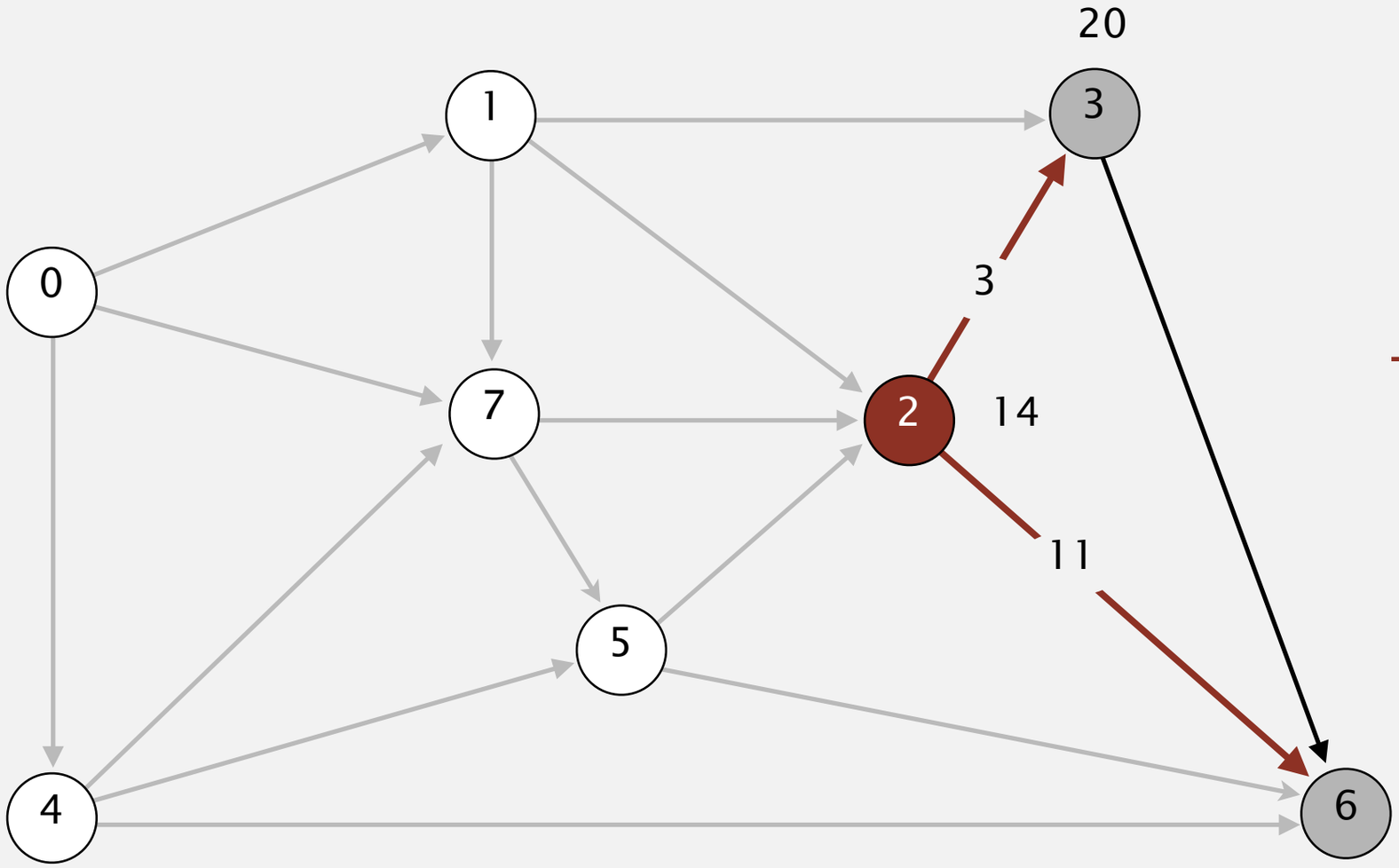
0 1 4 7 5 2 3 6

v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
→ 2	14.0	5→2
3	20.0	1→3
4	9.0	0→4
5	13.0	4→5
6	26.0	5→6
7	8.0	0→7

select vertex 2

Acyclic shortest paths demo

- Consider vertices in topological order.
- Relax all edges adjacent from that vertex.



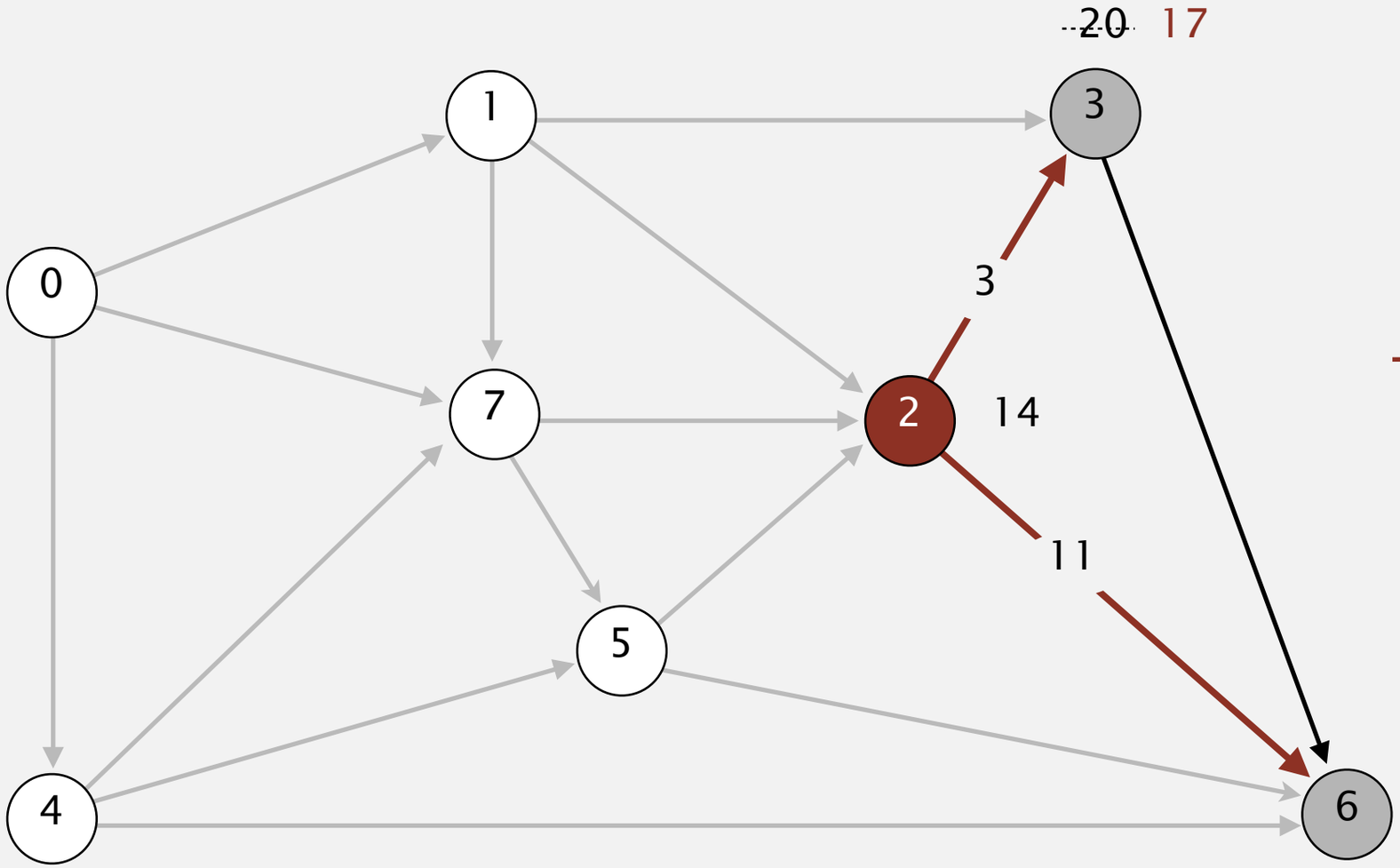
0 1 4 7 5 2 3 6

v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
→ 2	14.0	5→2
3	20.0	1→3
4	9.0	0→4
5	13.0	4→5
6	26.0	5→6
7	8.0	0→7

relax all edges adjacent from 2

Acyclic shortest paths demo

- Consider vertices in topological order.
- Relax all edges adjacent from that vertex.



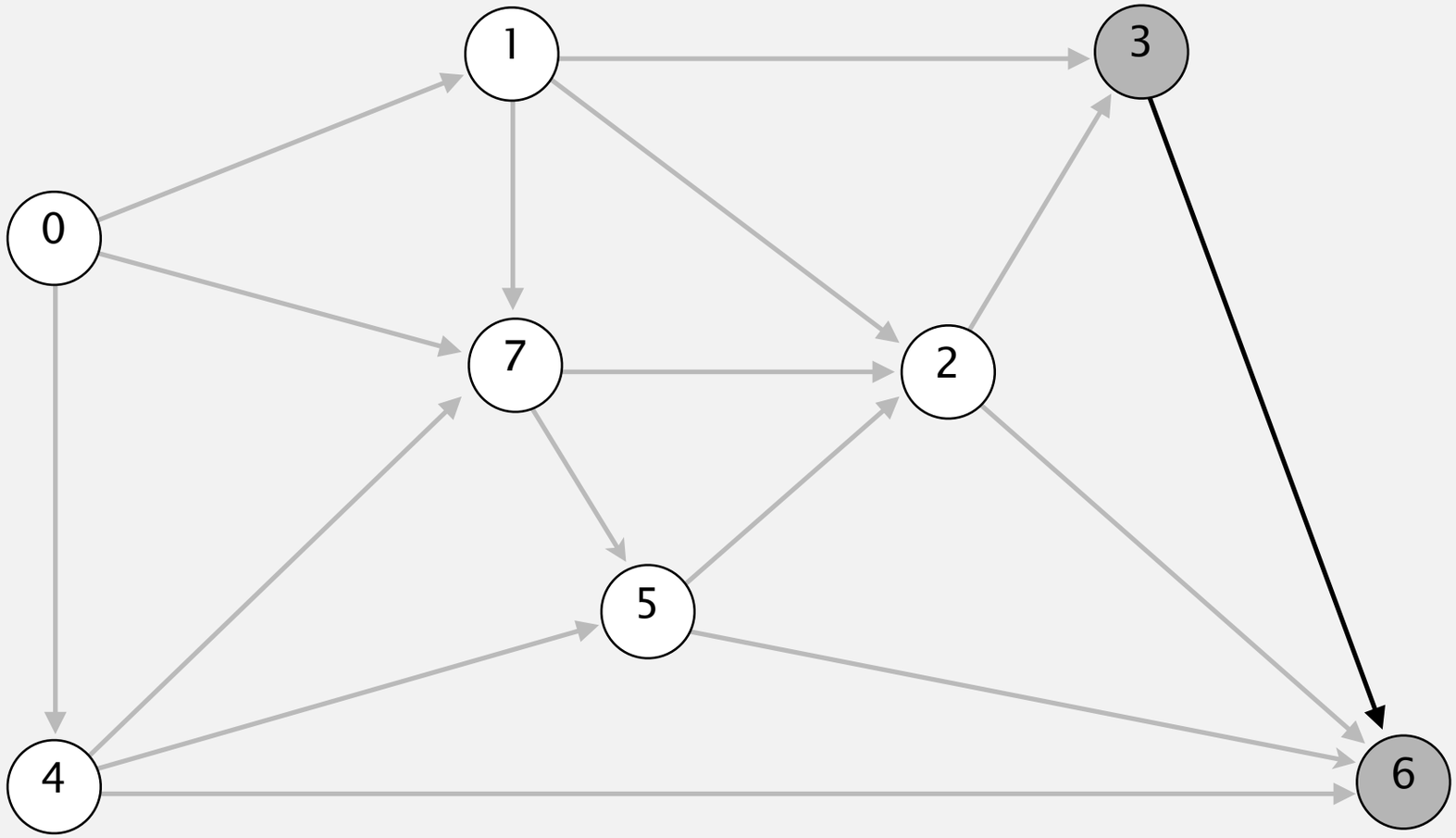
0 1 4 7 5 2 3 6

v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
→ 2	14.0	5→2
3	17.0	2→3
4	9.0	0→4
5	13.0	4→5
6	25.0	2→6
7	8.0	0→7

relax all edges adjacent from 2

Acyclic shortest paths demo

- Consider vertices in topological order.
- Relax all edges adjacent from that vertex.

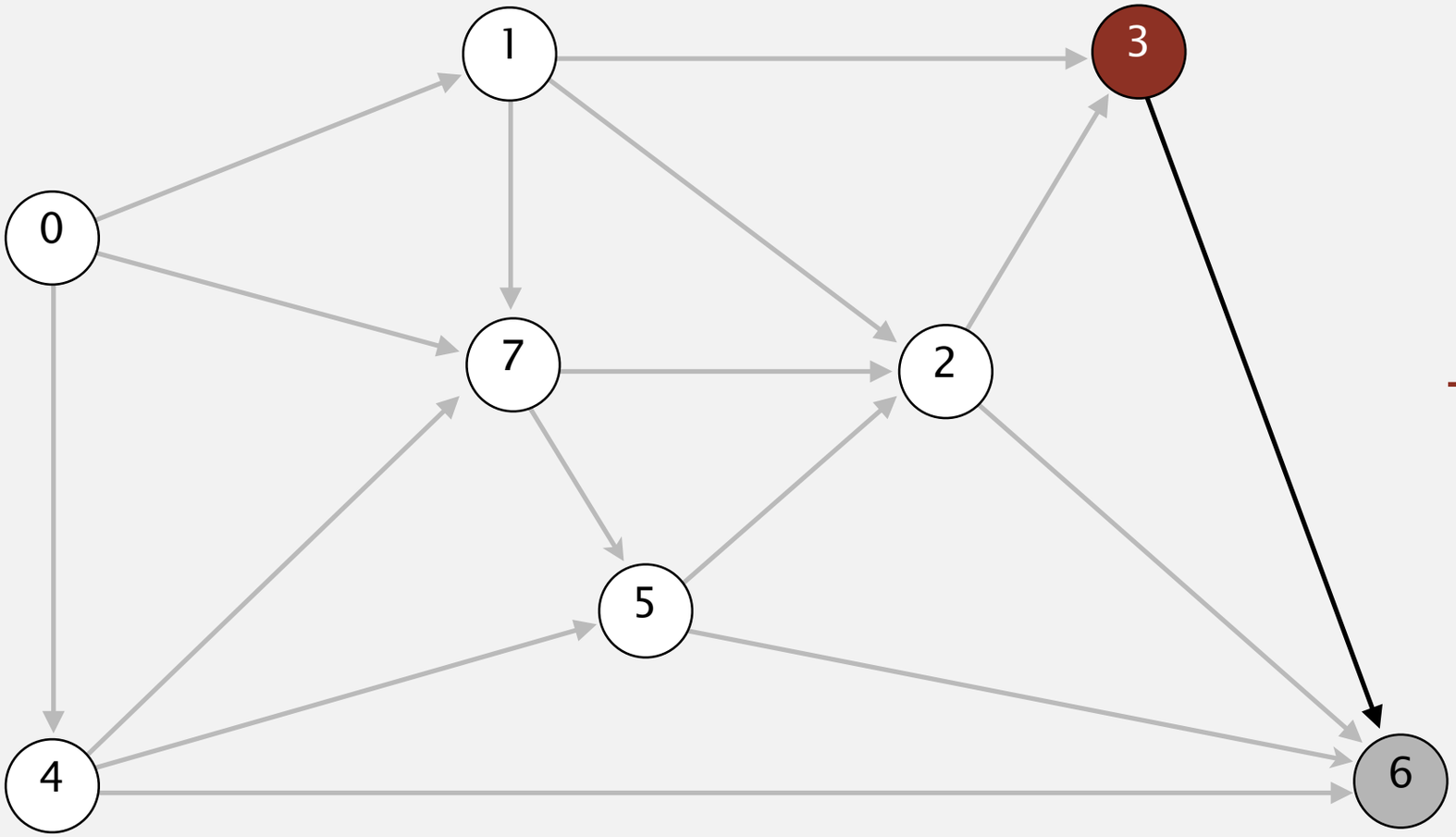


0 1 4 7 5 2 **3** **6**

v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	14.0	5→2
3	**17.0**	**2→3**
4	9.0	0→4
5	13.0	4→5
6	**25.0**	**2→6**
7	8.0	0→7

Acyclic shortest paths demo

- Consider vertices in topological order.
- Relax all edges adjacent from that vertex.



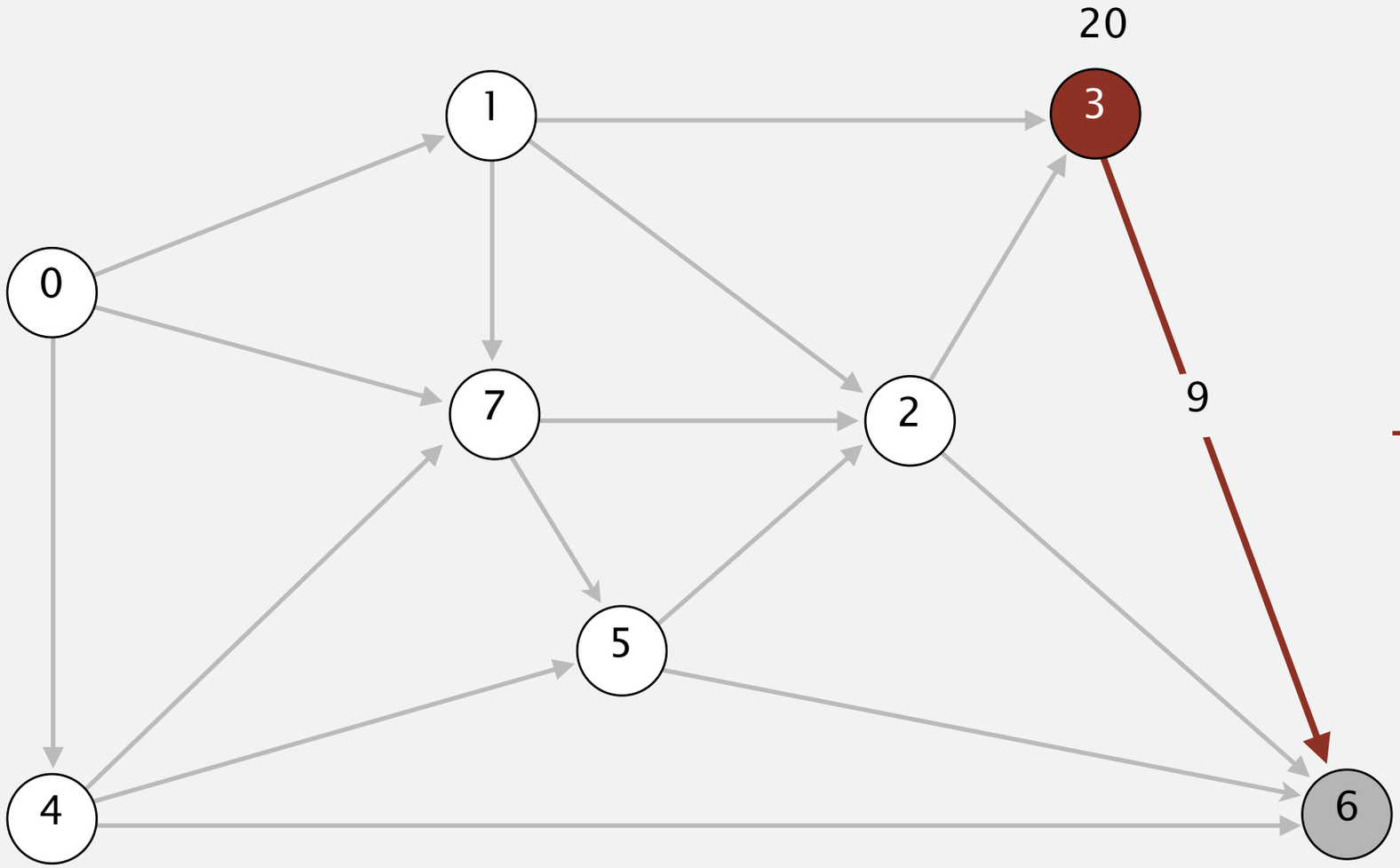
0 1 4 7 5 2 3 6

v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	14.0	5→2
→ 3	17.0	2→3
4	9.0	0→4
5	13.0	4→5
6	25.0	2→6
7	8.0	0→7

select vertex 3

Acyclic shortest paths demo

- Consider vertices in topological order.
- Relax all edges adjacent from that vertex.



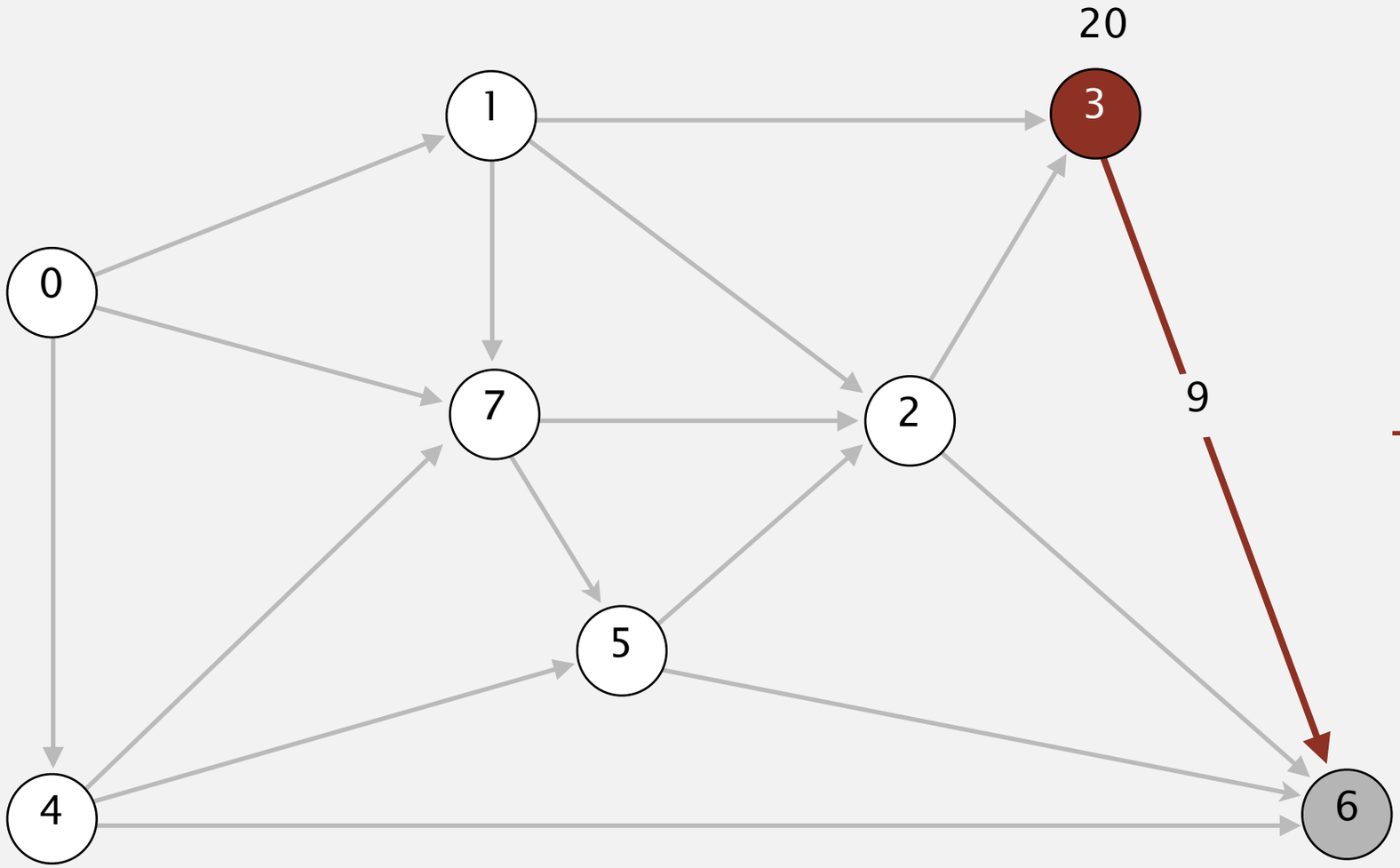
0 1 4 7 5 2 3 6

v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	14.0	5→2
→ 3	17.0	2→3
4	9.0	0→4
5	13.0	4→5
6	25.0	2→6
7	8.0	0→7

relax all edges adjacent from 3

Acyclic shortest paths demo

- Consider vertices in topological order.
- Relax all edges adjacent from that vertex.



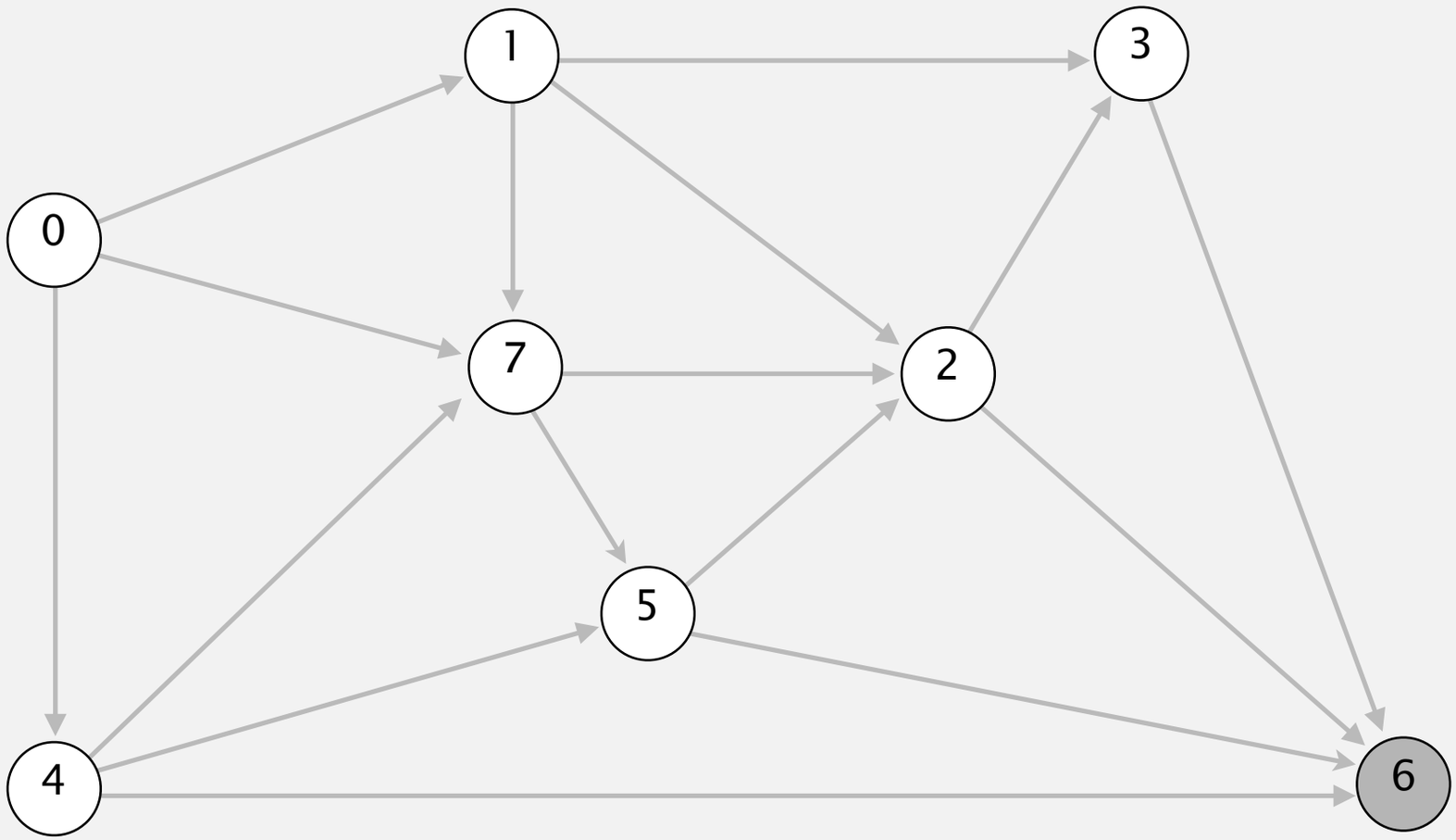
0 1 4 7 5 2 3 6

v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	14.0	5→2
→ 3	17.0	2→3
4	9.0	0→4
5	13.0	4→5
6	25.0 ✔	2→6
7	8.0	0→7

relax all edges adjacent from 3

Acyclic shortest paths demo

- Consider vertices in topological order.
- Relax all edges adjacent from that vertex.

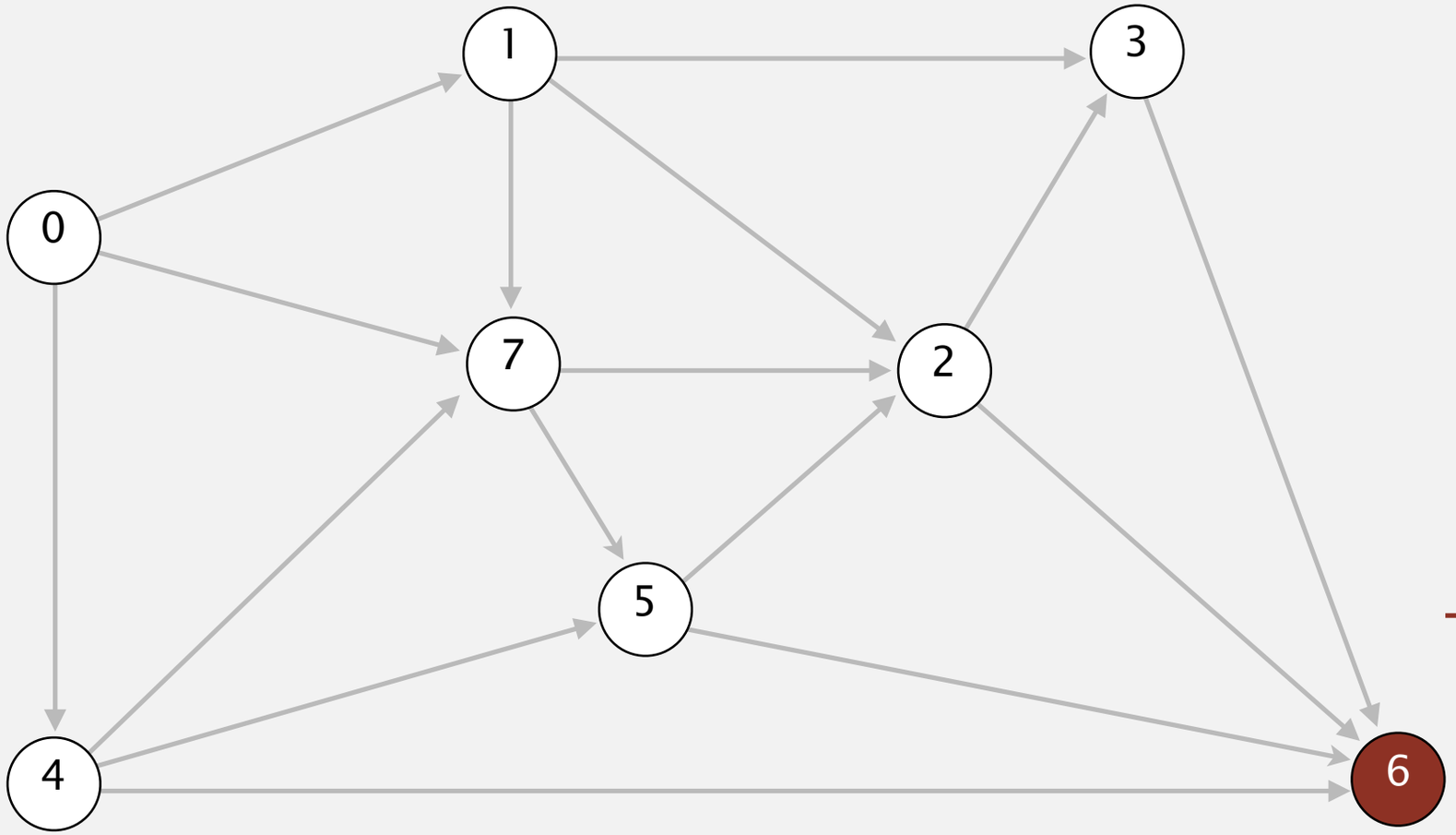


0 1 4 7 5 2 3 **6**

v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	14.0	5→2
3	17.0	2→3
4	9.0	0→4
5	13.0	4→5
6	**25.0**	**2→6**
7	8.0	0→7

Acyclic shortest paths demo

- Consider vertices in topological order.
- Relax all edges adjacent from that vertex.



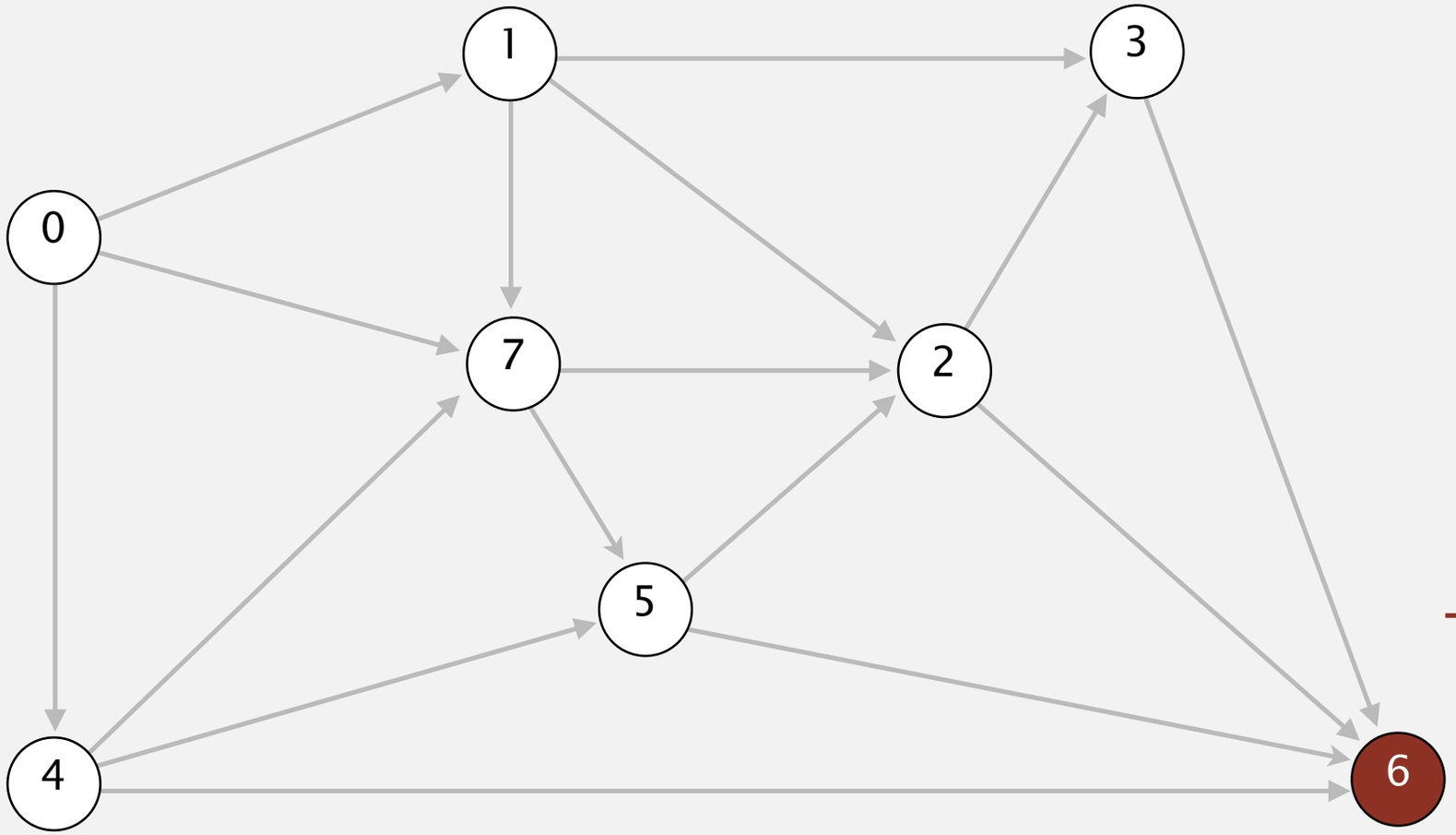
0 1 4 7 5 2 3 6

v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	14.0	5→2
3	17.0	2→3
4	9.0	0→4
5	13.0	4→5
→ 6	25.0	2→6
7	8.0	0→7

select vertex 6

Acyclic shortest paths demo

- Consider vertices in topological order.
- Relax all edges adjacent from that vertex.



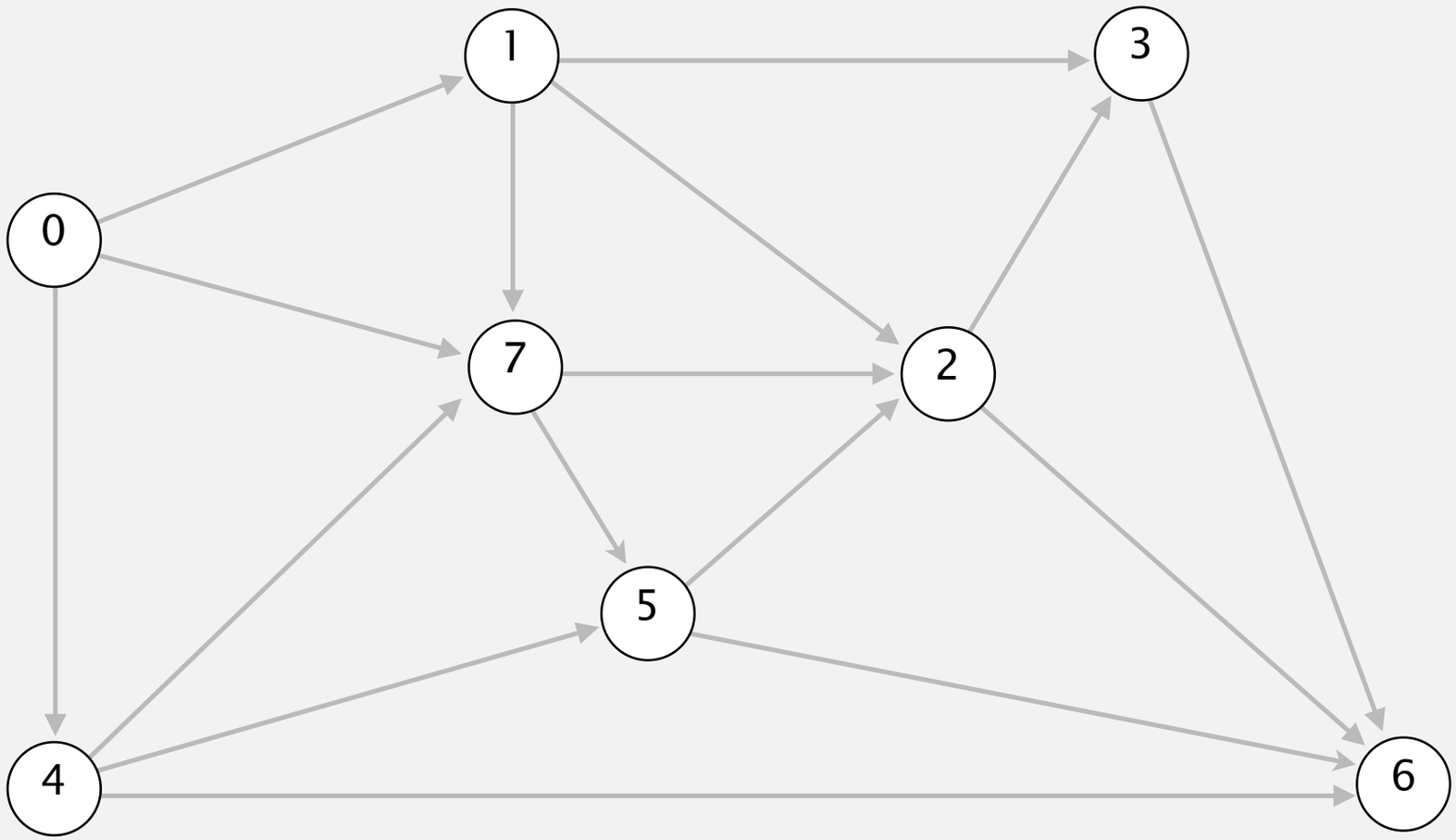
0 1 4 7 5 2 3 6

v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	14.0	5→2
3	17.0	2→3
4	9.0	0→4
5	13.0	4→5
→ 6	25.0	2→6
7	8.0	0→7

relax all edges adjacent from 6

Acyclic shortest paths demo

- Consider vertices in topological order.
- Relax all edges adjacent from that vertex.



0 1 4 7 5 2 3 6

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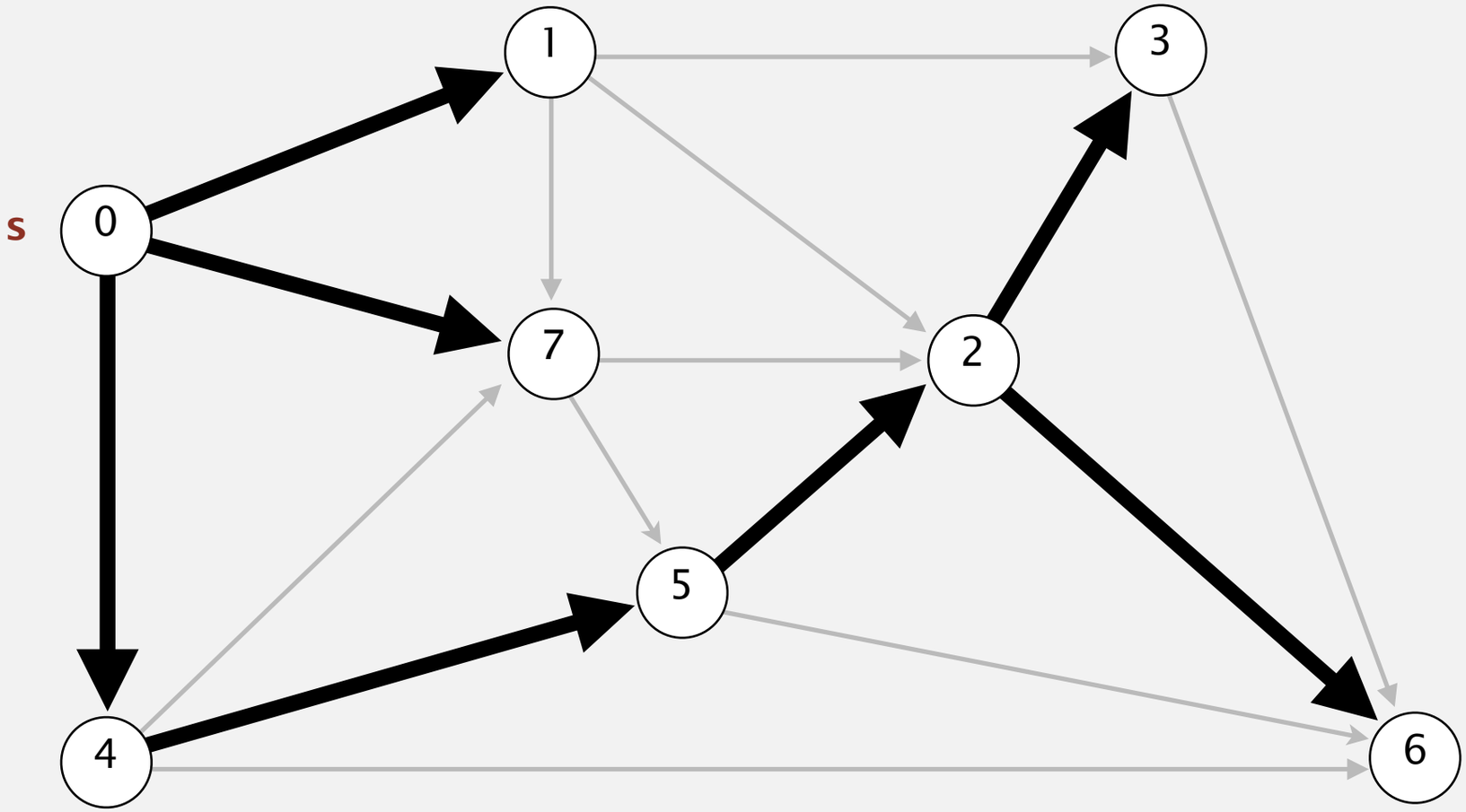

0 1 4 7 5 2 3 6

v	distTo[]	edgeTo[]
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3	17.0	2→3
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5	13.0	4→5
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7	8.0	0→7

shortest-paths tree from vertex s