

PART II: ALGORITHMS, MACHINES, and THEORY

17. A Computing Machine

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17. A Computing Machine

- Overview
- Data types
- Instructions
- Operating the machine
- Machine language programming

CS.17.A.MachineI.Overview

A TOY computing machine

TOY is an imaginary machine similar to:

- Ancient computers.
- Today's smartphone processors.
- Countless other devices designed and built over the past 50 years.

| LOAD | | | .00 | К | 5 | ΓEP | | R | UN |) | | | | ON/ | OF | 3 |
|------|---|---|-----|---|---|-----|---|----------|----|----|-----|---|---|-----|-----|----|
| ADDR | 8 | 3 | 3 | 3 | 3 | 3 | 3 | <u>}</u> | A | co | DMF | | | IAC | HIN | JE |
| DATA | 8 | 8 | 8 | 8 | 8 | 8 | 8 | 0 | 8 | 8 | 8 | 0 | 8 | 8 | 8 | 8 |



Smartphone processor, 2010s



PDP-8, 1970s

Reasons to study TOY

Prepare to learn about computer architecture

- How does your computer's processor work?
- What are its basic components?
- How do they interact?

Learn about machine-language programming.

- How do Java programs relate to your computer?
- Key to understanding Java references.
- Intellectual challenge of a new programming regime.
- Still necessary in some modern applications.

multimedia, computer games, embedded devices, scientific computing,...

Learn fundamental abstractions that have informed processor design for decades.



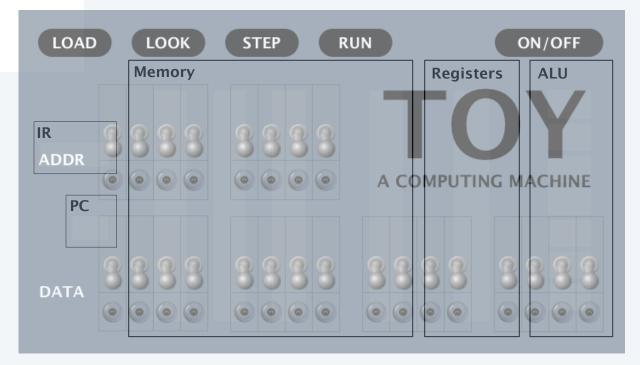
Bits and words

| | binary | hex |
|--|--------|-----|
| <i>Everything</i> in TOY is encoded with a sequence of <i>bits</i> (value 0 or 1). | 0000 | 0 |
| • Why? Easy to represent two states (on and off) in real world. | 0001 | 1 |
| • Bits are organized in 16-bit sequences called <i>words</i> . | 0010 | 2 |
| | 0011 | 3 |
| $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | 0100 | 4 |
| | 0101 | 5 |
| 88855885588558555 | 0110 | 6 |
| | 0111 | 7 |
| | 1000 | 8 |
| More convenient for humans: <i>hexadecimal notation</i> (base 16) | 1001 | 9 |
| • 4 hex digits in each word. | 1010 | Α |
| Convert to and from binary 4 bits at a time. | 1011 | В |
| convert to and nom smary i bits at a time. | 1100 | С |
| 0 0 0 1 1 0 0 0 1 1 0 0 1 1 1 | 1101 | D |
| | 1110 | Е |
| | 1111 | F |

Inside the box

Components of TOY machine

- Memory
- Registers
- Arithmetic and logic unit (ALU)
- Program counter (PC)
- Instruction register (IR)



Memory

Holds data and instructions

- 256 words
- 16 bits in each word
- Connected to registers
- Words are *addressable*

Use *hexadecimal* for addresses

- Number words from 00 to FF
- Think in hexadecimal
- Use array notation

• Example: M[2A] = CO24

| Mer | nory | | | | | | |
|------------|-----------------|----|-----------------|------------|---------|-----------|-----------------|
| 00 | 0000 | 10 | 8 A O 1 | 20 | 7101 | F0 | F 0 F 0 |
| 01 | FFFE | 11 | 8 B O 2 | 21 | 8 A F F | F1 | 0505 |
| 02 | 000D | 12 | 1 C A B | 22 | 7680 | F2 | 000D |
| 03 | 0003 | 13 | 9 C O 3 | 23 | 7 B O O | F3 | 1 0 0 0 |
| 04 | $0 \ 0 \ 0 \ 1$ | 14 | $0 \ 0 \ 0 \ 1$ | 24 | C A 2 B | F4 | $0\ 1\ 0\ 1$ |
| 05 | 0000 | 15 | $0 \ 0 \ 1 \ 0$ | 25 | 8 C F F | F 5 | 0 0 1 0 |
| 06 | 0000 | 16 | 0 1 0 0 | 26 | 156B | F6 | $0 \ 0 \ 0 \ 1$ |
| 07 | 0000 | 17 | 1 0 0 0 | 27 | BC05 | F7 | 0 0 1 0 |
| 08 | 0000 | 18 | 0 1 0 0 | 28 | 2 A A 1 | F8 | 0 1 0 0 |
| 09 | 0000 | 19 | $0 \ 0 \ 1 \ 0$ | 29 | 2 B B 1 | F9 | 1 0 0 0 |
| 0A | 0000 | 1A | $0 \ 0 \ 0 \ 1$ | 2 A | C 0 2 4 | FA | $0 \ 1 \ 0 \ 0$ |
| 0 B | 0000 | 1B | $0 \ 0 \ 1 \ 0$ | 2B | 0000 | FB | $0 \ 0 \ 1 \ 0$ |
| 0C | 0000 | 1C | $0\ 1\ 0\ 0$ | 2C | 0000 | FC | $0 \ 0 \ 0 \ 1$ |
| 0 D | 0000 | 1D | 1 0 0 0 | 2D | 0000 | FD | $0 \ 0 \ 1 \ 0$ |
| 0 E | 0000 | 1E | $0\ 1\ 0\ 0$ | 2 E | 0000 | FE | $0\ 1\ 0\ 0$ |
| 0F | 0000 | 1F | $0 \ 0 \ 1 \ 0$ | 2 F | 0000 | FF | $0 \ 1 \ 0 \ 0$ |

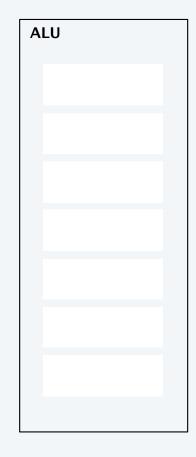
Table of 256 words *completely specifies* contents of memory.

Arithmetic and logic unit (ALU)

ALU

- TOY's computational engine
- A *calculator*, not a computer
- Hardware that implements *all* data-type operations
- How? Stay tuned for computer architecture lectures





Registers

| Registers | Registers |
|--|------------------------------|
| • 16 words, addressable in hex from 0 to F (use names R[0] through R[F]) | R[0] 0 0 0 0 |
| Scratch space for calculations and data movement. | R[1] 0001 R[2] FFFE |
| Connected to memory and ALU | R[2] FFFE R[3] 1 C A B |
| By convention, R[0] is always 0. | R[4] 0001 |
| In our code, we often also keep 0001 in R[1]. | R[5] 0 0 0 0 |
| | R[6] F A C E R[7] 0 0 0 0 |
| Q. Why not just connect memory directly to ALU? | R[8] F 0 0 1 |
| | R[9] 0 0 0 0 |
| A. Too many different memory names (addresses). | R[A] 0 0 0 5 |
| | R[B] 0 0 0 8 R[C] 0 0 0 D |
| Q. Why not just connect memory locations to one another? | R[D] 0 0 0 0 |
| | R[E] 0 0 0 0 |
| A. Too many different connections. | R[F] 0 0 0 0 |
| | |

Table of 16 words *completely specifies* contents of registers.

Program counter and instruction register

TOY operates by executing a sequence of instructions.

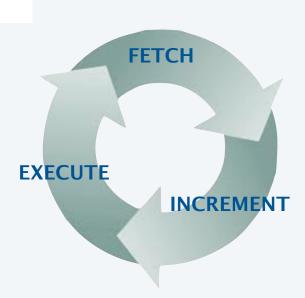
Critical abstractions in making this happen

- Program Counter (PC). Memory address of next instruction.
- Instruction Register (IR). Instruction being executed.

PCIR101 C A B

Fetch-increment-execute cycle

- Fetch: Get instruction from memory into IR.
- Increment: Update PC to point to *next* instruction.
- Execute: Move data to or from memory, change PC, or perform calculations, as specified by IR.



The state of the machine

Contents of memory, registers, and PC at a particular time

- Provide a record of what a program has done.
- Completely determines what the machine will do.

ALU and IR hold intermediate states of computation

| | Memory | Registers | S | ALU |
|----|--------|-----------|---|-----|
| | | | | |
| IR | | | | |
| | | | | |
| | | | | |
| PC | | | | |
| | | | | |
| | | | | |
| | | | | |
| | | | | |
| | | | | |

Image sources

http://pixabay.com/en/man-flashlight-helmet-detective-308611/
http://en.wikipedia.org/wiki/Marchant_calculator#/media/File:Marchant_-_Odhner_clone_1950.png
http://en.wikipedia.org/wiki/Marchant_calculator#/media/File:SCM_Marchant_calculator.jpg
http://commons.wikimedia.org/wiki/File:Calculator_casio.jpg
http://commons.wikimedia.org/wiki/File:Abacus_5.jpg

CS.17.A.MachineI.Overview

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CS.17.B.MachineI.Types

TOY data type

A data type is a set of values and a set of operations on those values.

TOY's data type is 16-bit two's complement integers.

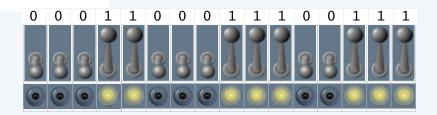
Two kinds of operations

- Arithmetic.
- Bitwise.

All other types of data must be implemented with *software*

- 32-bit and 64-bit integers.
- 32-bit and 64-bit floating point values.
- Characters and strings.
- ...

All values are represented in 16-bit words.





TOY data type (original design): Unsigned integers

Values. 0 to $2^{16}-1$, encoded in binary (or, equivalently, hex).

| | | | 15 | 14 | 13 | 12 | 11 | 10 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | 0 |
|---|------------------|---------------|-----|----|-----------------|------------------------|------|-----|------|-----|-----|-----|------|---|---|-----|-----|-----|
| | Example. 637510. | binary | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 1 | 1 | 1 | 0 | 0 | 1 | 1 | 1 |
| | | | | | | 2 ¹² | +211 | | | | +27 | +26 | +25 | | | +22 | +21 | +20 |
| | | hex | | | 1 | | | ł | 8 | | | | E | | | 7 | 7 | |
| | | | | | 16 ³ | | | | × 16 | 2 | | | × 16 | 5 | | | 7 | |
| | | | | 40 | 96 | | | + 2 | 048 | | | + 2 | 224 | | | + | 7 | |
| Orecretica | | E vere | | 10 | F7 | | 100 | 7 | 21 | | | | | | | | | |
| Operation | 5. | Exam | pie | 10 | E/ | + . | LÕE | / = | - 3 | LCE | | | | | | | | |
| Add.Subtract | | | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 1 | 1 | 1 | 0 | 0 | 1 | 1 | 1 |
| • Test if C | | + | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 1 | 1 | 1 | 0 | 0 | 1 | 1 | 1 |
| - restric | · · | 1 | | • | | _ | _ | | | | | _ | _ | | | - | | |
| | | = | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 1 | 1 | 1 | 0 | 0 | 1 | 1 | 1 | 0 |

Warning. TOY ignores overflow.

TOY data type (better design): two's complement

| Values. -2^{15} to $2^{15}-1$, encoded in <i>16-bit</i> | two's complemen | nt. | decimal | hex | binary |
|--|-------------------------|------|---------|-----------------|---|
| | | | +32,767 | 7 F F F | 011111111111111 |
| Operations. | | | +32,766 | 7FFE | 011111111111110 |
| • Add. | | | +32,765 | 7FFD | 011111111111101 |
| • Subtract. | | | | | |
| • Test if positive, negative, or 0. | | | +3 | 0003 | 00000000000011 |
| | | +2 | 0002 | 000000000000010 | |
| 16 bit two's complement | | | +1 | 0001 | 000000000000001 |
| 16-bit binary representation of x for pos | | | 0 | 0000 | 000000000000000000000000000000000000000 |
| • 16-bit binary representation of $2^{16} - \mathbf{x} ^{16}$ | | | -1 | FFFF | 1111111111111111 |
| | for negative x. | | -2 | FFFE | 1111111111111110 |
| Useful properties | | | -3 | FFFD | 1111111111111101 |
| • Leading bit (bit 15) signifies sign. | | | | | |
| 000000000000000000000000000000000000 | | | -32,766 | 8002 | 100000000000010 |
| Add/subtract is <i>the same</i> as for unsigne | | | -32,767 | 8001 | 100000000000001 |
| - Audy subtract is the sume as for unsigne | zu. | | -32,768 | 8000 | 1000000000000000 |
| slight annovance: o | one extra negative valu | ue / | | | |

slight annoyance: one extra negative value ?

Two's complement: conversion

To convert from decimal to two's complement

- If greater than +32,767 or less than -32,768 report error.
- Convert to 16-bit binary.
- If not negative, done.
- If negative, *flip all bits and add 1*.

To convert from two's complement to decimal

- If sign bit is 1, *flip all bits and add 1* and output minus sign.
- Convert to decimal.

To add/subtract

- Use same rules as for unsigned binary.
- (Still) ignore overflow.

Examples

| +1310 | 000000000001101 | 000D |
|------------|-----------------|------|
| -13_{10} | 111111111110011 | FFF3 |
| +25610 | 00000010000000 | 0100 |
| -25610 | 111111100000000 | FF00 |

Examples

| 0001 | 0000000000000001 | 110 |
|------|--------------------|--------|
| FFFF | 111111111111111111 | -110 |
| FF0D | 1111111100001101 | -24310 |
| 00F3 | 000000011110011 | +24310 |

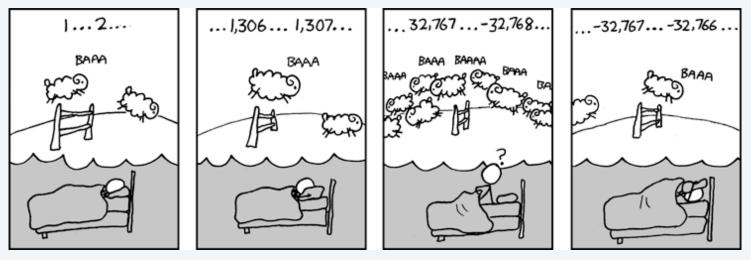
Example

| -25610 | 111111100000000 | FF00 |
|----------|-------------------|-------|
| +1310 | +000000000001011 | +000D |
| = -24310 | =1111111100001101 | =FF0D |

17

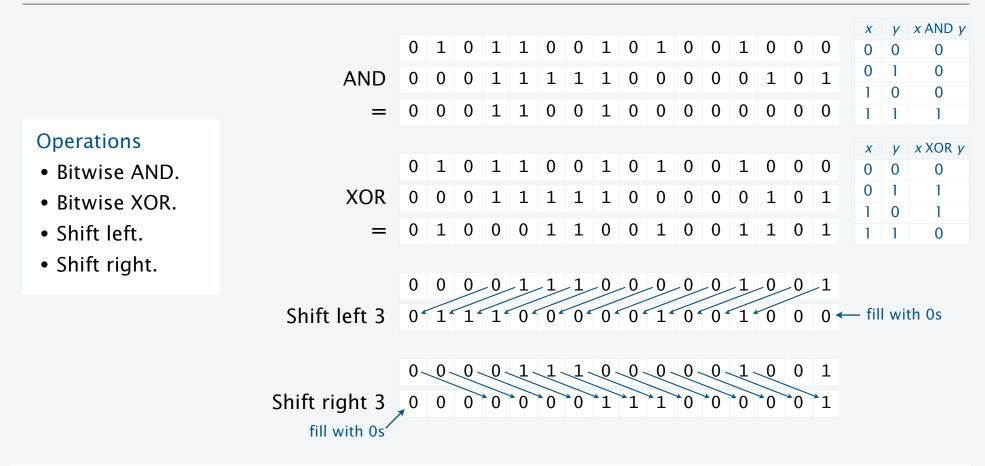
Overflow in two's complement

| $32,767_{10} = 2^{15} - 1$ | 0111111111111111 | 7FFF | | | |
|------------------------------|---|--------|----------------------------|-----|-------------------------------|
| +1 | + 000000000000001 | + 0001 | | | |
| largest (positive) number | = 1000000000000000000000000000000000000 | = 8000 | $= -2^{15} = -32,768_{10}$ | ←── | smallest (negative) number |



http://xkcd.com/571/

TOY data type: Bitwise operations



Special note: Shift left/right operations also implement multiply/divide by powers of 2 for integers.

shift right fills with 1s if leading bit is 1

Image sources

http://pixabay.com/en/network-media-binary-computer-65923/ https://xkcd.com/571/

CS.17.B.MachineI.Types

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CS.17.C.MachineI.Instructions

TOY instructions

ANY 16-bit (4 hex digit) value defines a TOY instruction.

First hex digit specifies which instruction.

Each instruction changes machine state in a well-defined way.

| category | opcodes | implements | changes |
|--------------------|-----------|---|----------------------|
| operations | 123456 | data-type operations | registers |
| data movement | 789AB | data moves between registers and memory | registers, memory |
| flow of control | 0 C D E F | conditionals, loops, and functions | PC |

| opcode | instruction |
|--------|--------------------|
| 0 | halt |
| 1 | add |
| 2 | subtract |
| 3 | bitwise and |
| 4 | bitwise xor |
| 5 | shift left |
| 6 | shift right |
| 7 | load address |
| 8 | load |
| 9 | store |
| Α | load indirect |
| В | store indirect |
| С | branch if zero |
| D | branch if positive |
| Е | jump register |
| F | jump and link |

Encoding instructions

ANY 16-bit (4 hex digit) value defines a TOY instruction.

Two different instruction formats

• Type RR: Opcode and 3 registers.

| 15 | 14 | 13 | 12 | 11 | 10 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | 0 |
|----|----------------------|----|----------|----|----|---|----------|---|---|---|---|---|---|---|---|
| | | | | | | | | | | | | | | | |
| | opcode destination d | | source s | | | | source t | | | | | | | | |

• Type A: Opcode, 1 register, and 1 memory address.

| 15 | 14 | 13 | 12 | 11 | 10 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | 0 |
|----|----------------------|----|----|---------------------|----|---|---|---|---|---|---|---|---|---|---|
| | | | | | | | | | | | | | | | |
| | opcode destination d | | | <i>address</i> addr | | | | | | | | | | | |

Examples

| 1CAB | Add $R[A]$ to $R[B]$ and put result in $R[C]$. |
|------|---|
| 8A15 | Load into R[A] data from M[15]. |

| opcode | | instruction |
|--------|----|--------------------|
| 0 | RR | halt |
| 1 | RR | add |
| 2 | RR | subtract |
| 3 | RR | bitwise and |
| 4 | RR | bitwise xor |
| 5 | RR | shift left |
| 6 | RR | shift right |
| 7 | Α | load address |
| 8 | Α | load |
| 9 | А | store |
| Α | RR | load indirect |
| В | RR | store indirect |
| С | А | branch if zero |
| D | А | branch if positive |
| E | RR | jump register |
| F | А | jump and link |

A TOY program

Add two integers

- Load operands from memory into registers.
- Add the registers.
- Put result in memory.

| | Load | into | R[A] | data | from | M[15] | |
|--|------|------|------|------|------|-------|--|
|--|------|------|------|------|------|-------|--|

Load into R[B] data from M[16]

Add R[A] and R[B] and put result into R[C]

Store R[C] into M[17]

Halt

Q. How can you tell whether a word is an instruction?

A. If the PC has its address, it *is* an instruction!

| | Memory |
|------|---|
| PC | ,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,, |
| 10 → | 10 8 A 1 5 |
| 11 | 11 8 B 1 6 |
| 12 | 12 1 C A B |
| 13 | 13 9 C 1 7 |
| 14 | 14 0 0 0 0 |
| | 15 0 0 0 8 |
| | 16 0 0 5 |
| | 17 000D |
| | |
| | Registers |
| | |
| | A 0008 |
| | B 0005 |
| | C 000D |
| | |

R[A] ← M[15]

- R[B] ← M[16]
- $R[C] \leftarrow R[A] + R[B]$

M[17] ← R[C]

halt

Same program with different data

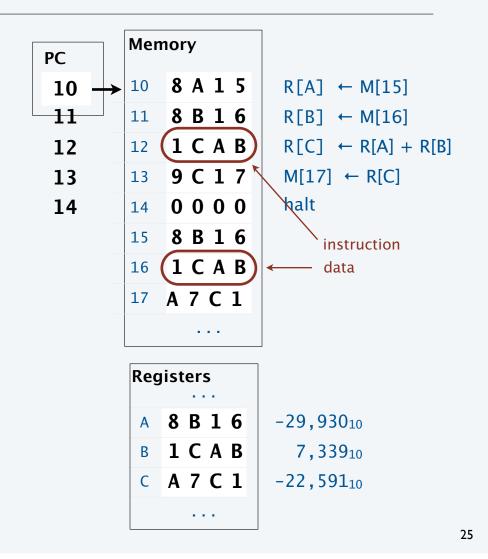
Add two integers

- Load operands from memory into registers.
- Add the registers.
- Put result in memory.

| Load into R[A] data from M[15] |
|--|
| Load into R[B] data from M[16] |
| Add R[A] and R[B] and put result into R[C] |
| Store R[C] into M[17] |
| Halt |

Q. How can you tell whether a word is data?

A. If it is added to another word, it *is* data !





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CS.17.D.MachineI.Operating

Outside the box

User interface

- Switches.
- Lights.
- Control Buttons.

First step: Turn on the machine!



Loading a program into memory

- Set 8 memory address switches.
- Set 16 data switches to instruction encoding.
- Press LOAD to load instruction from switches into addressed memory word.



- Set 8 memory address switches.
- Set 16 data switches to instruction encoding.
- Press LOAD to load instruction from switches into addressed memory word.



- Set 8 memory address switches.
- Set 16 data switches to instruction encoding.
- Press LOAD to load instruction from switches into addressed memory word.



- Set 8 memory address switches.
- Set 16 data switches to instruction encoding.
- Press LOAD to load instruction from switches into addressed memory word.



- Set 8 memory address switches.
- Set 16 data switches to instruction encoding.
- Press LOAD to load instruction from switches into addressed memory word.



Looking at what's in the memory

To double check that you loaded the data correctly

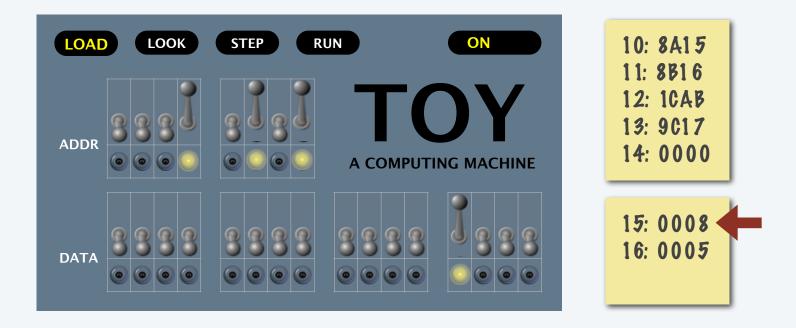
- Set 8 memory address switches.
- Press LOOK to examine the addressed memory word.



Loading data into memory

To load data, use the *same* procedure as for instructions

- Set 8 memory address switches.
- Set 16 data switches to *data* encoding.
- Press LOAD to load *data* from switches into addressed memory word.



Loading data into memory

To load data, use the *same* procedure as for instructions

- Set 8 memory address switches.
- Set 16 data switches to *data* encoding.
- Press LOAD to load *data* from switches into addressed memory word.



Running a program

To run a program, set the address switches to the address of first instruction and press RUN.

[data lights may flash, but all (and RUN light) go off when HALT instruction is reached]

To see the output, set the address switches to the address of expected result and press LOOK.

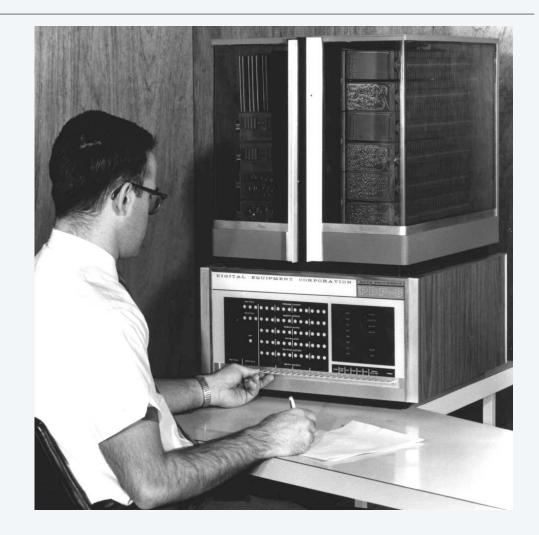


To run the program again, enter different data and press RUN again.

Switches and lights

Q. Did people really program this way?

A. Yes!





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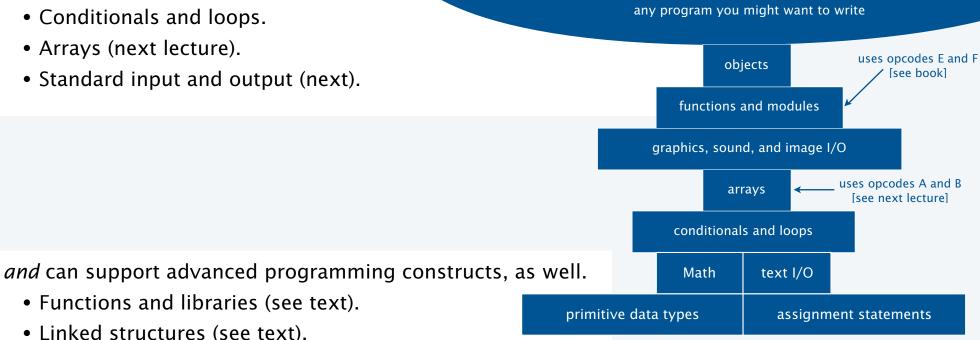
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CS.17.E.MachineI.Programming

Machine language programming

TOY instructions support the same basic programming constructs as Java.

- Primitive data types.
- Assignment statements.
- Conditionals and loops.
- Arrays (next lecture).
- Standard input and output (next).



Conditionals and loops

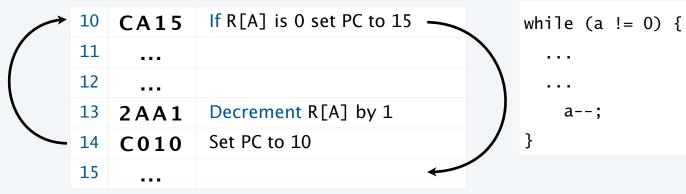
To control the flow of instruction execution

- Test a register's value.
- Change the PC, depending on the value.

Example: Absolute value of R[A]

| 10 | DA12 | If R[A] > 0 set PC to 12 (skip 11) |
|----|---------|--|
| 11 | 2 A 0 A | Subtract R[A] from 0 (R[0]) and put result into R[A] |
| 12 | | |

Example: Typical while loop (assumes R[1] is 0001)



| opcode | instruction |
|--------|--------------------|
| С | branch if zero |
| D | branch if positive |

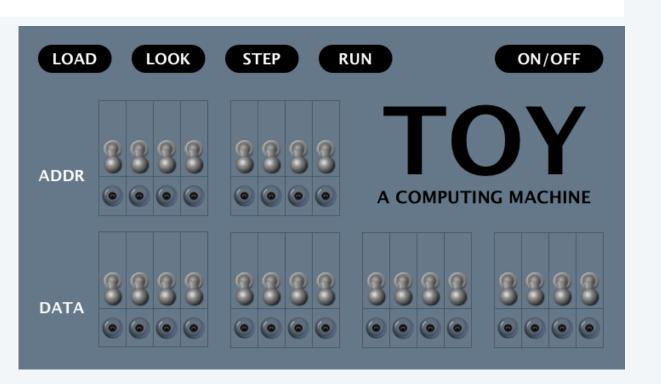


To infinity and beyond!

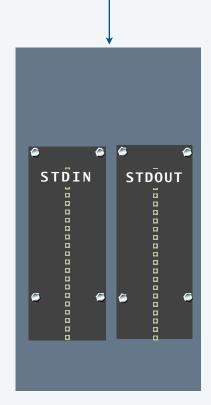
Standard input and output

An immediate problem

- We're not going to be able to address real-world problems with just switches and lights for I/O!
- One solution: Paper tape.







Standard input and output

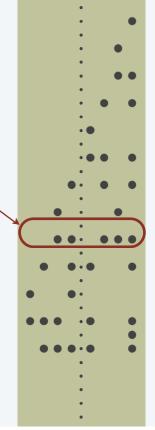
Punched paper tape

- Encode 16-bit words in two 8-bit rows.
- To write a word, punch a hole for each 1.
- To *read* a word, shine a light behind the tape and sense the holes.



TOY mechanism

- Connect hardware to memory location FF.
- To write the contents of a register to stdout, store to FF.
- To *read* from stdin into a register, *load* from FF.



| | Register trace | Α | 1 | 1 | 2 | 3 | 5 | 8 | 13 | 21 | 34 | 55 | 89 |
|---------------------------------|------------------|------|-----|----|-----------------|------|-----|------|-----|-----|----|----|-----|
| | | В | 1 | 2 | 3 | 5 | 8 | 13 | 21 | 34 | 55 | 89 | 144 |
| | | С | 2 | 3 | 3 | 5 | 8 | 13 | 21 | 34 | 55 | 89 | 144 |
| | D [1] 1 | 9 | А | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | 0 |
| $PC \rightarrow 40 7 1 0 1$ | R[1] = 1 | | | | | | | | | | | | |
| 41 7 A O 1 | R[A] = 1 | | | | a = | = 1; | | | | | | | |
| 42 7 B 0 1 | R[B] = 1 | | | | b = | = 1; | | | | | | | |
| 43 8 9 4 C | R[9] = M[4C] | | | | i = | = N; | | | | | | | |
| 44 C 9 4 B | if $(R[9] == 0)$ |) PC | = 4 | 4B | wh ⁻ | ile | (i | != | 0) | { | | | |
| 45 9 A F F | write R[A] to s | tdou | t | | 0 | StdC | ut. | pri | nt(| a); | | | |
| 46 1 C A B | R[C] = R[A] + | R[B |] | | C | 2 = | a + | ⊦b; | | | | | |
| 47 1 A B O | R[A] = R[B] | | | | ā | a = | b; | | | | | | |
| 48 1 B C 0 | R[B] = R[C] | | | | k |) = | c; | | | | | | |
| 49 2 9 9 1 | R[9] = R[9] - | 1 | | | _ | i = | i - | - 1; | | | | | |
| 4A C 0 4 4 | PC = 44 | | | | } | | | | | | | | |
| 4B 0 0 0 0 | halt | | | | | | | | | | | | |
| 4C 000A | | | | | | | | | | | | | |
| | | | | | | | | | | | | | |

Flow of control and standard output example: Fibonacci numbers

TOY reference card

| opcode | operation | format | pseudo-code |
|--------|-----------------|--------|----------------------------|
| 0 | halt | — | halt |
| 1 | add | RR | R[d] = R[s] + R[t] |
| 2 | subtract | RR | R[d] = R[s] - R[t] |
| 3 | bitwise and | RR | R[d] = R[s] & R[t] |
| 4 | bitwise xor | RR | $R[d] = R[s] \wedge R[t]$ |
| 5 | shift left | RR | $R[d] = R[s] \iff R[t]$ |
| 6 | shift right | RR | R[d] = R[s] >> R[t] |
| 7 | load addr | А | R[d] = addr |
| 8 | load | А | R[d] = M[addr] |
| 9 | store | А | M[addr] = R[d] |
| Α | load indirect | RR | R[d] = M[R[t]] |
| В | store indirect | RR | M[R[t]] = R[d] |
| С | branch zero | А | if $(R[d] == 0) PC = addr$ |
| D | branch positive | А | if $(R[d] > 0)$ PC = addr |
| E | jump register | RR | PC = R[d] |
| F | jump and link | А | R[d] = PC + 1; PC = addr |

Format RR

| 15 | 14 | 13 | 12 | 11 | 10 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | 0 |
|----------|----|----|----------------------|----|----|---|--------------|-------|---|----------|---|---|---|---|---|
| | | | | | | | | | | | | | | | |
| opcode | | | <i>destination</i> d | | | 9 | soui | rce s | S | source t | | | | | |
| Format A | | | | | | | | | | | | | | | |
| 15 | 14 | 13 | 12 | 11 | 10 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | 0 |
| | | | | | | | | | | | | | | | |
| opcode | | | <i>destination</i> d | | | | address ADDR | | | | | | | | |

ZEROR[0] is always 0.STANDARD INPUTLoad from FF.

STANDARD OUTPUT Store to FF.

Pop quiz 1 on TOY

Q. What is the interpretation of

1A75 as a TOY instruction?

1A75 as a two's complement integer value?

OFFF as a TOY instruction?

0FFF as a two's complement integer value?

8888 as a TOY instruction?

8888 as a two's complement integer value? (Answer in base 16).

Pop quiz 2 on TOY

Q. How does one flip all the bits in a TOY register ?

Pop quiz 3 on TOY

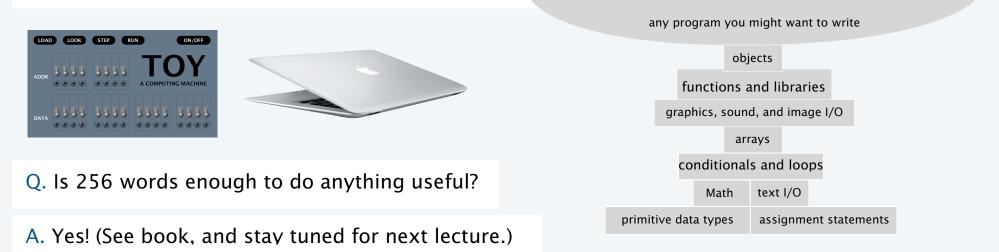
Q. What does the following TOY program leave in R[2]?

107 C O A
$$R[C] = 10_{10}$$
117 I O I $R[1] = 1$ 127 2 O I $R[2] = 1$ 13I 2 2 2 2 $R[2] = R[2] + R[2]$ 142 C C I $R[C] = R[C] - 1$ 15D C I 3 $HALT$

TOY vs. your laptop

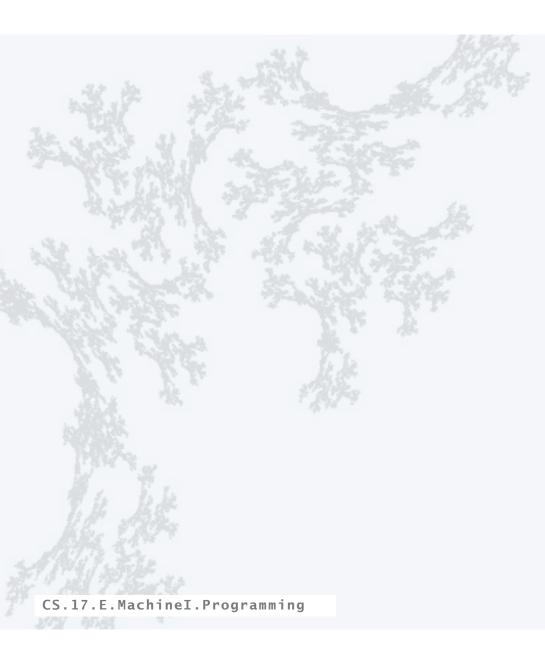
Two different computing machines

- Both implement basic data types, conditionals, loops, and other low-level constructs.
- Both can have arrays, functions, and other high-level constructs.
- Both have infinite input and output streams.



A. Yes! It is a Turing Machine, with a read/write I/O device (see theory lectures).

OK, we definitely want a faster version with more memory when we can afford it...





PART II: ALGORITHMS, MACHINES, and THEORY

17. A Computing Machine