### **Consistency examples**



#### COS 418: Distributed Systems Precept 5

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# Plan

• Midterm poll

• Consistency examples

# Fill out this poll: http://tinyurl.com/zdeq4lr

# Linearizability

# Strong consistency = linearizability

- Linearizability (Herlihy and Wang 1991)
  - 1. All servers execute all ops in *some* identical sequential order
  - 2. Global ordering preserves each client's own local ordering
  - 3. Global ordering preserves real-time guarantee
    - All ops receive global time-stamp using a sync'd clock
    - If  $ts_{op1}(x) < ts_{op2}(y)$ , OP1(x) precedes OP2(y) in sequence
- Once write completes, all later reads (by wall-clock start time) should return value of that write or value of later write.
- Once read returns particular value, all later reads should return that value or value of later write.

### Sequential Consistency

### Is that valid?

| P1: W(x)a |       |       | W(x)c |       |       |
|-----------|-------|-------|-------|-------|-------|
| P2:       | R(x)a | W(x)b |       |       |       |
| P3:       | R(x)a |       |       | R(x)c | R(x)b |
| P4:       | R(x)a |       |       | R(x)b | R(x)c |

#### No. Why?

Ordering of the Write operations needs to be preserved

### Causal Consistency



| Operations | Concurrent? |
|------------|-------------|
| a, b       |             |
| b, f       |             |
| c, f       |             |
| e, f       |             |
| e, g       |             |
| a, c       |             |
| a, e       |             |





| Operations | Concurrent? |
|------------|-------------|
| a, b       | Ν           |
| b, f       |             |
| c, f       |             |
| e, f       |             |
| e, g       |             |
| a, c       |             |
| a, e       |             |





| Operations | Concurrent? |
|------------|-------------|
| a, b       | Ν           |
| b, f       | Y           |
| c, f       |             |
| e, f       |             |
| e, g       |             |
| a, c       |             |
| a, e       |             |





| Operations | Concurrent? |
|------------|-------------|
| a, b       | Ν           |
| b, f       | Υ           |
| c, f       | Υ           |
| e, f       |             |
| e, g       |             |
| a, c       |             |
| a, e       |             |





| Operations | Concurrent? |
|------------|-------------|
| a, b       | Ν           |
| b, f       | Y           |
| c, f       | Y           |
| e, f       | Y           |
| e, g       |             |
| a, c       |             |
| a, e       |             |





| Operations | Concurrent? |
|------------|-------------|
| a, b       | Ν           |
| b, f       | Υ           |
| c, f       | Y           |
| e, f       | Y           |
| e, g       | Ν           |
| a, c       |             |
| a, e       |             |





| Operations | Concurrent? |
|------------|-------------|
| a, b       | N           |
| b, f       | Y           |
| c, f       | Y           |
| e, f       | Y           |
| e, g       | Ν           |
| a, c       | Y           |
| a, e       |             |





| Operations | Concurrent? |
|------------|-------------|
| a, b       | Ν           |
| b, f       | Υ           |
| c, f       | Υ           |
| e, f       | Y           |
| e, g       | Ν           |
| a, c       | Y           |
| a, e       | Ν           |



### Is that valid?

| P1: V | √(x)a |       | W(x)c |       |       |
|-------|-------|-------|-------|-------|-------|
| P2:   | R(x)a | W(x)b |       |       |       |
| P3:   | R(x)a |       |       | R(x)c | R(x)b |
| P4:   | R(x)a |       |       | R(x)b | R(x)c |

### Is that valid?

| P1: W(x)a |       |       | W(x)c |       |       |  |
|-----------|-------|-------|-------|-------|-------|--|
| P2:       | R(x)a | W(x)b |       |       |       |  |
| P3:       | R(x)a |       |       | R(x)c | R(x)b |  |
| P4:       | R(x)a |       |       | R(x)b | R(x)c |  |

Valid under causal consistency

**Why?** W(x)b and W(x)c are concurrent

So all processes don't (need to) see them in same order

P3 and P4 read the values 'a' and 'b' in order as potentially causally related. No 'causality' for 'c'.

### What causal dependencies do we have?

Direction of time ----->
P1 : w1[x] = 1
P2 : w2[x] = 2
P3 : r3[x] = 2
P4 : r4[x] = 1

### What causal dependencies do we have?

Execution causally consistent:

- r3[x] is causally dependent on w2[x]
- r4[x] is causally dependent on w1[x]

# Designing a stock market

• What kind of consistency would you use to implement an electronic stock market?

# Example: Designing a stock market

- What kind of consistency would you use to implement an electronic stock market?
- Causal Consistency:
  - Reactions to changes in stock values should be consistent.
  - Changes in stocks that are independent can be seen in different orders.

### Further examples

# Simplifications



- In the following example, simplified read, write and reduced system complexity (no replicas).
- Assignment as write, print as read.
- Intended to demonstrate how linearizability, sequential consistency are violated.
- More realistic view, as above.

### Example

Client 1 Client 2  $X_1 = X_1 + 1$  $A = X_2$  $B = Y_2$  $Y_1 = Y_1 + 1$ If (A > B)print(A) else ...

**M** 

### Example: Linearizable



#### Example: Not Linearizable, sequentially consistent



#### Example: Not Linearizable nor sequentially consistent



### **Eventual Consistency**

# **Eventual consistency**

#### Eventual consistency

- Writes are eventually applied in total order
- Reads might not see most recent writes in total order
- Why do people like eventual consistency?
  - Fast read/write of local copy (no primary, no Paxos)
  - Disconnected operation

# Replication with eventual consistency



The diagram illustrates that although replicas are always available to read, some replicas may be inconsistent with the latest write on the originating node, at a particular moment in time. In the diagram, Node A is the originating node and nodes B and C are the replicas.

## Bayou



















### Bayou uses a primary to commit a total order

- Why is it important to make log stable?
  - Stable writes can be committed
  - Stable portion of the log can be truncated
- Problem: If *any* node is offline, the stable portion of all logs stops growing
- Bayou's solution:
  - A designated primary defines a total commit order
  - Primary assigns CSNs (commit-seq-no)
  - Any write with a known CSN is stable
  - All stable writes are ordered before tentative writes





## Assignment 3 Due November 21

# Monday's topic Concurrency Control, Locking and Recovery