
Lecture 8: Control

COS / ELE 375

Computer Architecture and Organization

Princeton University
Fall 2015

Prof. David August

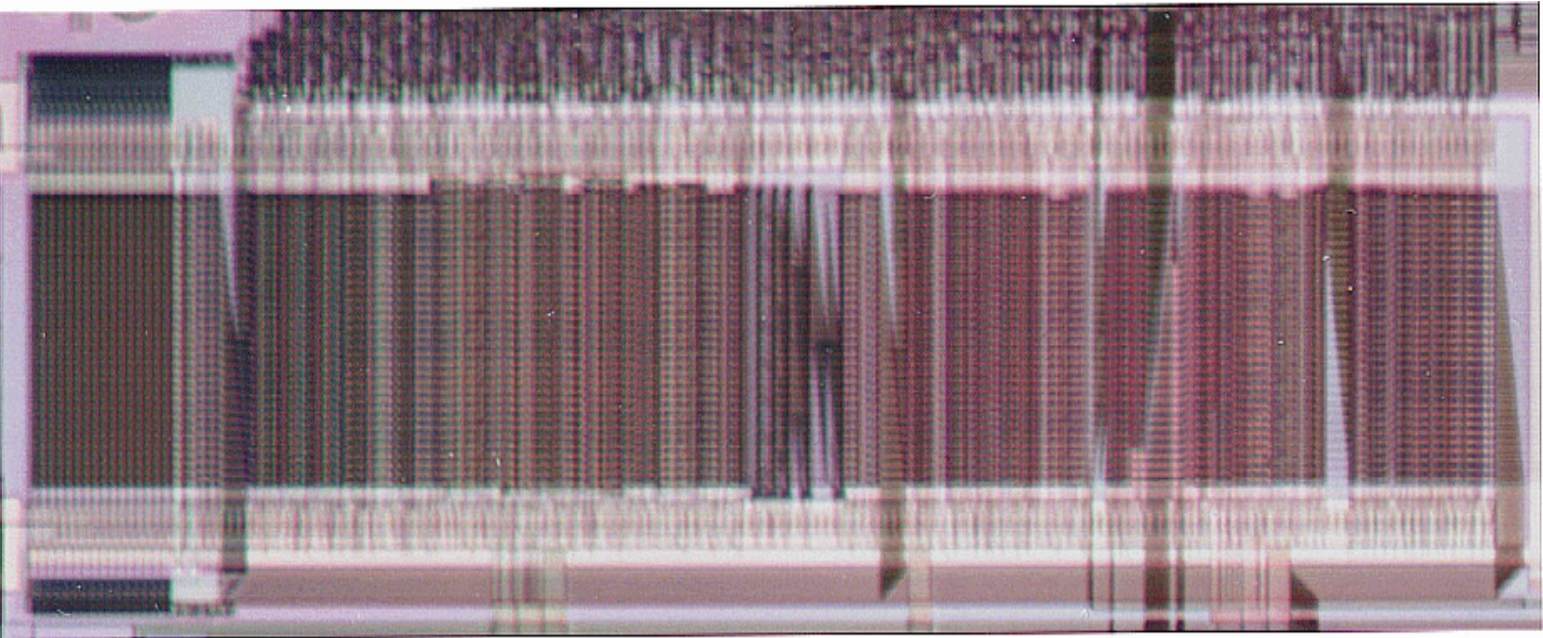
Datapath and Control

Datapath

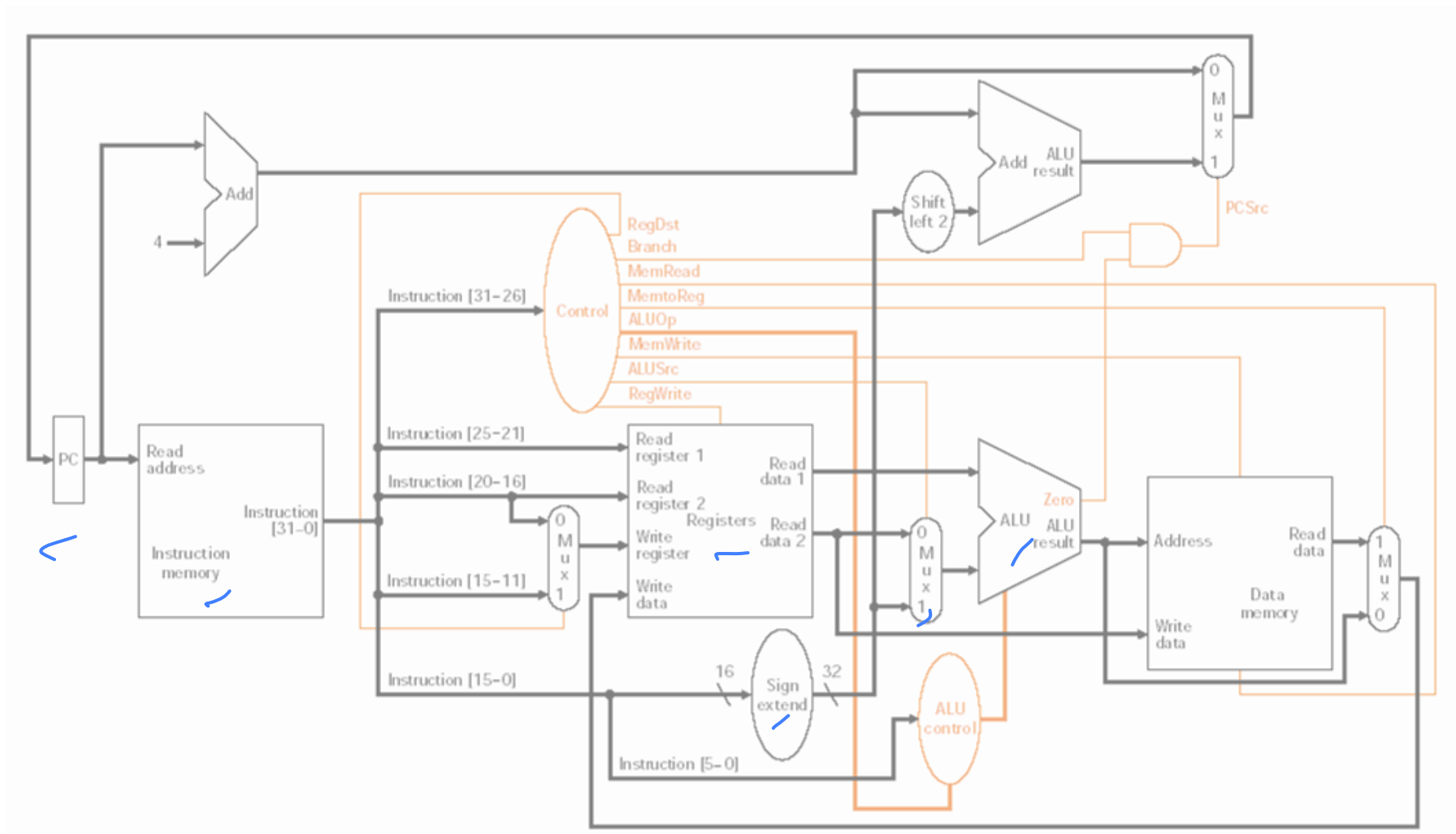
The collection of state elements, computation elements, and interconnections that together provide a conduit for the flow and transformation of data in the processor during execution. - DIA

Control

The component of the processor that commands the datapath, memory, and I/O devices according to the instructions of the program. – P&H

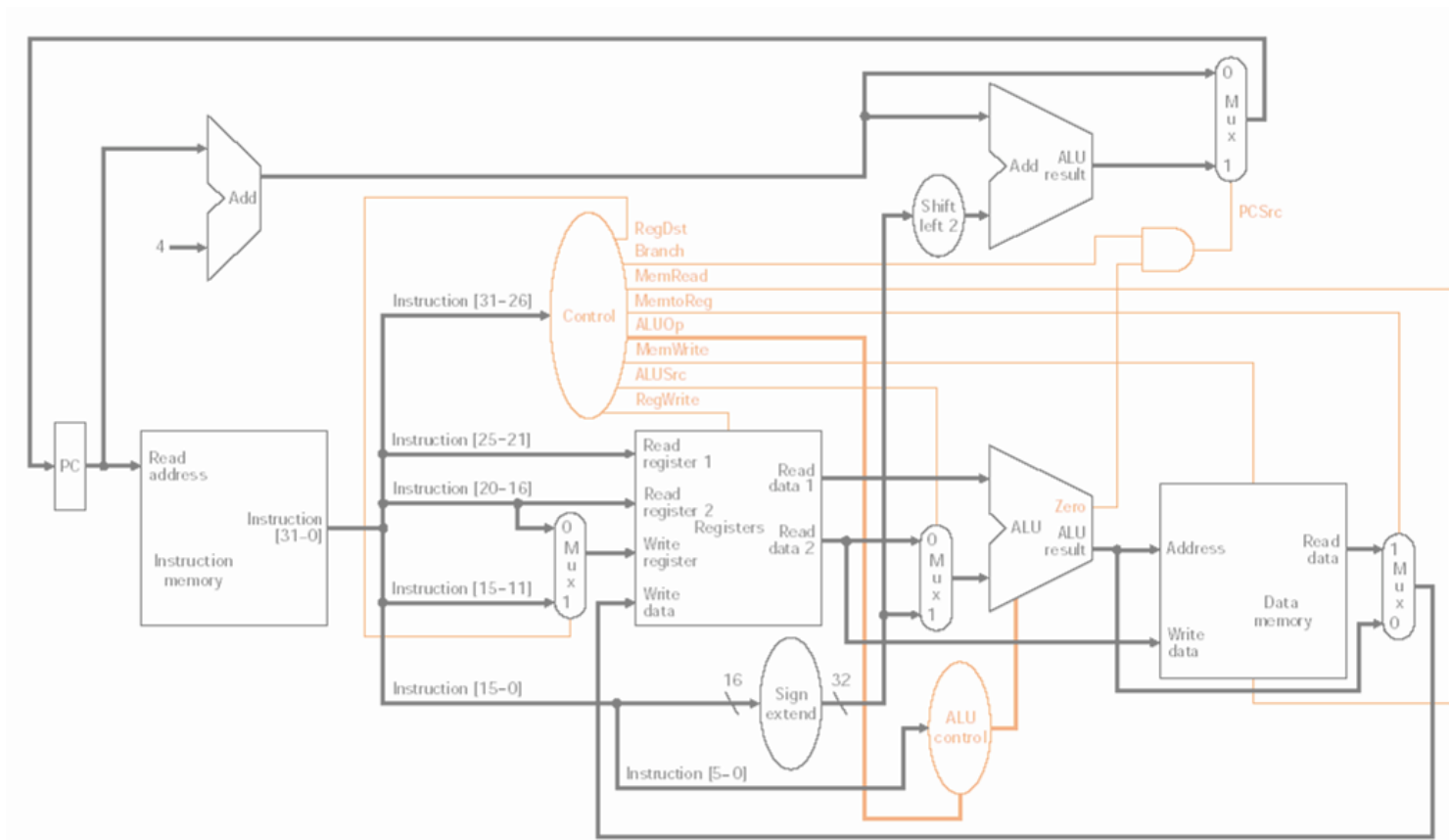


Datapath with Control



Datapath with Control

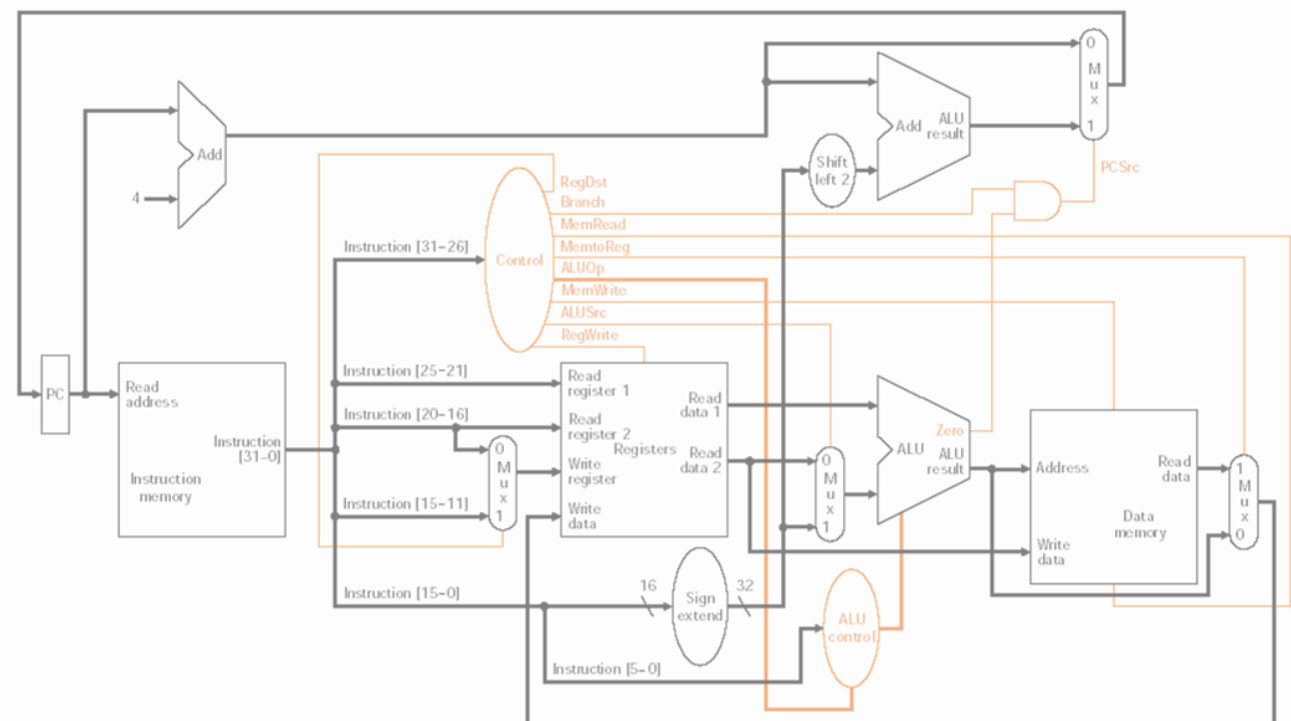
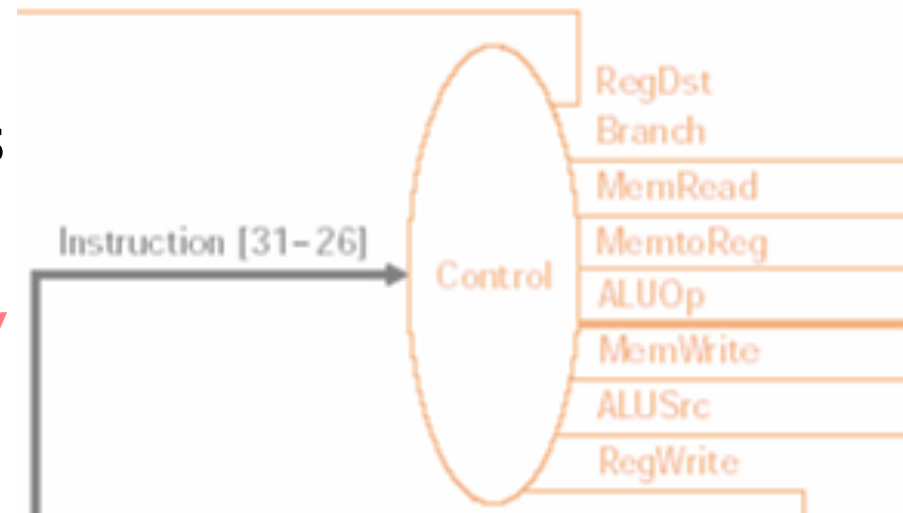
- Memory reference: `lw`, `sw`
- Arithmetic/logical: `add`, `sub`, `and`, `or`, `slt`
- Control flow: `beq`, `j` (see book)



The Control Unit

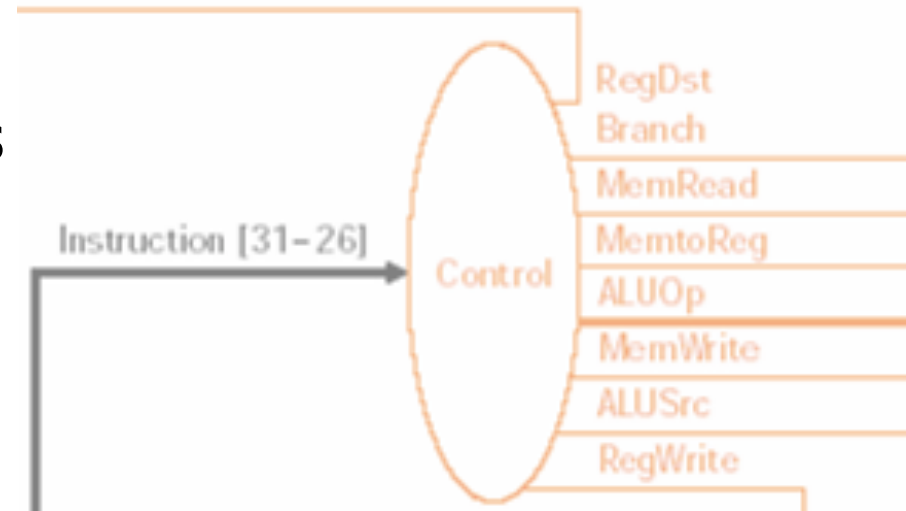
- Generates Control Signals

RegDst, Branch, MemRead, MemtoReg, ALUOp, MemWrite, ALUSrc, RegWrite



The Control Unit

- Generates Control Signals
- Uses Op Field [31-26]

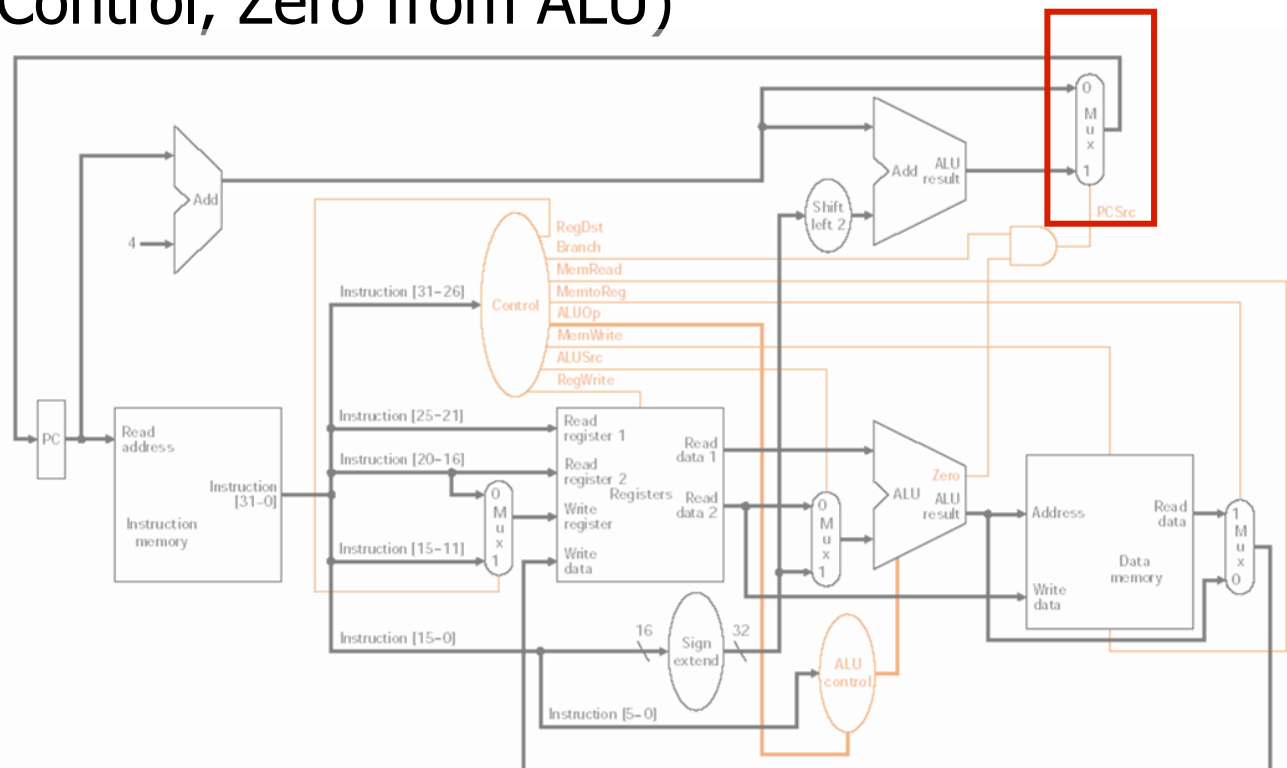
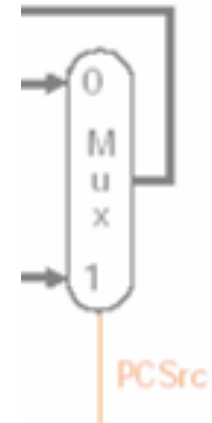


	6 bits	5 bits	5 bits	5 bits	5 bits	6 bits
R:	op	rs	rt	rd	shamt	funct
I:	op	rs	rt	address / immediate		
J:	op	target address				

Control Signals

PCSrc

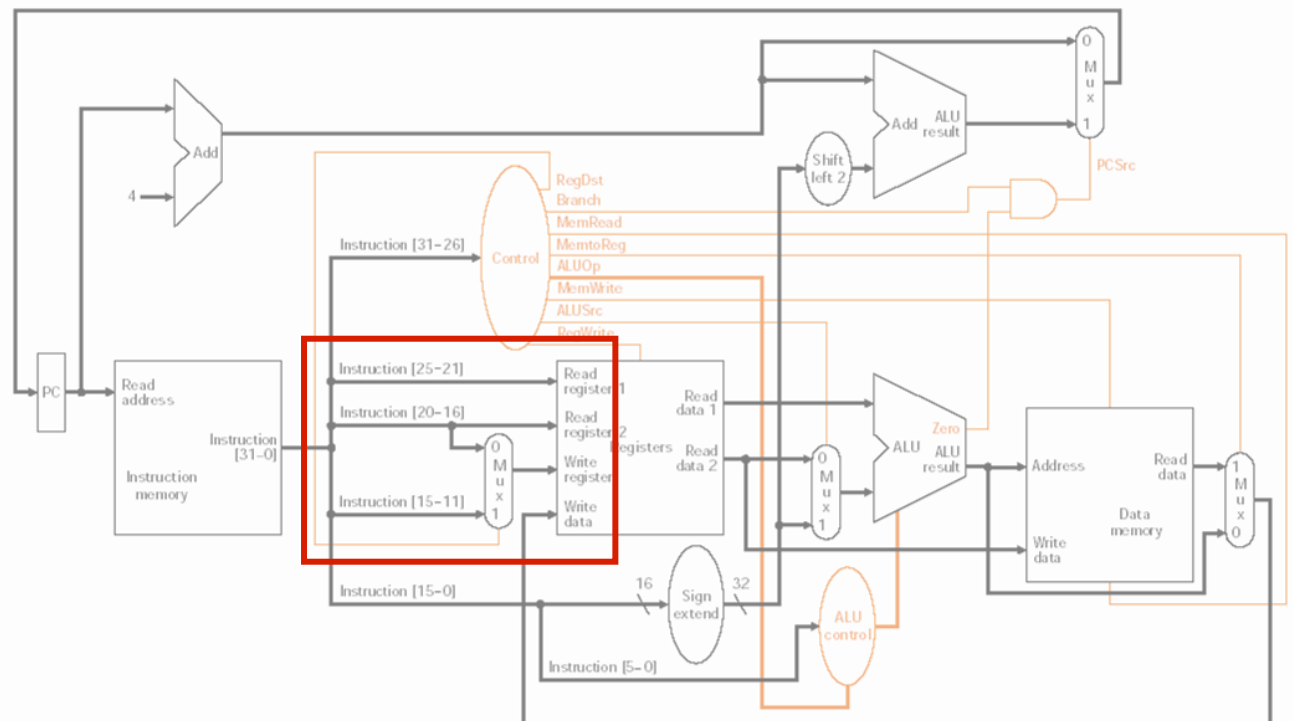
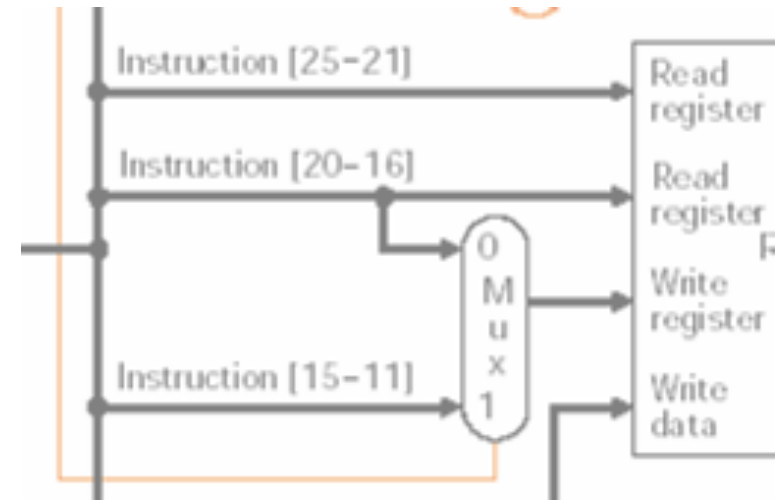
- True: $PC = \text{SignExt}(\text{Imm}_{16}) \ll 2 + PC + 4$
- False: $PC = PC + 4$
- $\text{PCSrc} = \text{Branch} \ \& \ \text{Zero}$
(Branch from Control, Zero from ALU)



Control Signals

RegDst

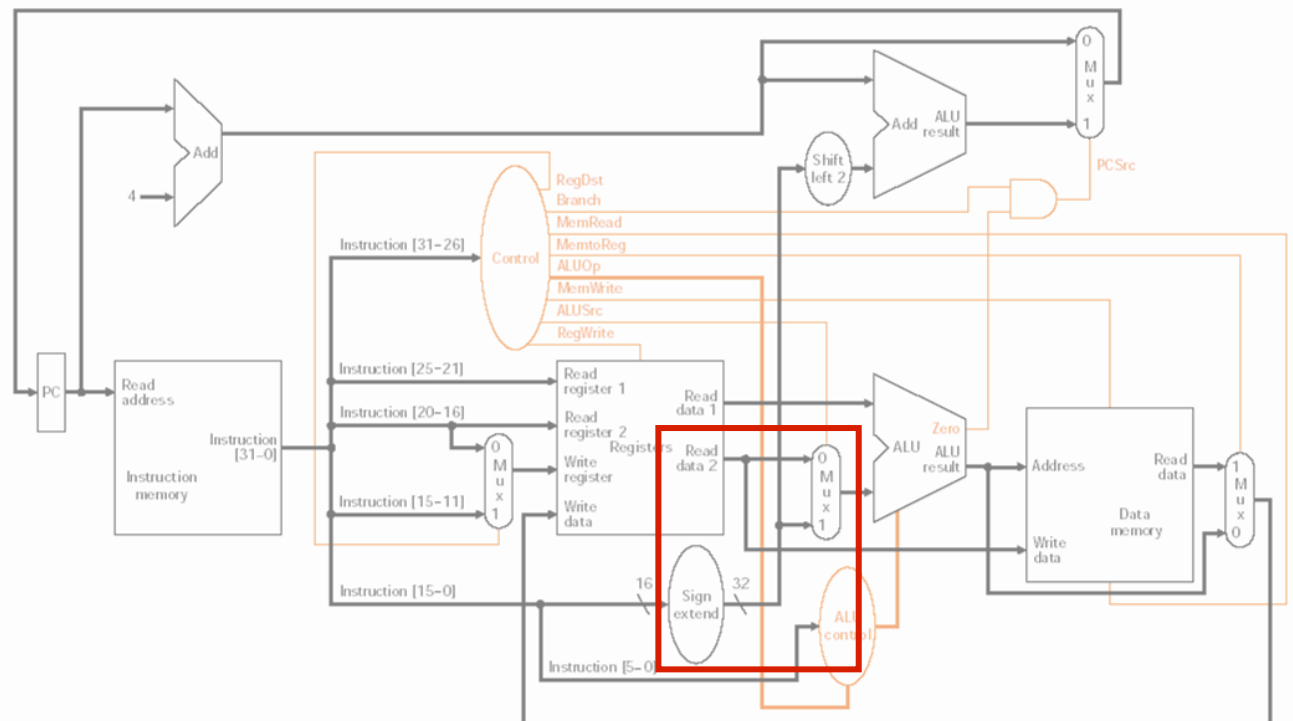
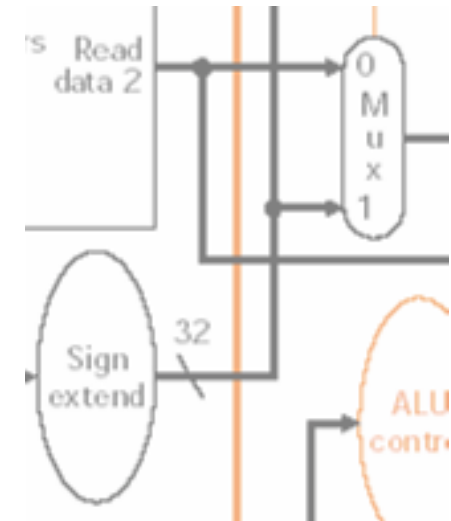
- True: WriteReg = Inst[15-11]
- False: WriteReg = Inst[20-16]



Control Signals

ALUSrc

- True: $\text{SignExt}(\text{Imm}_{16})$
- False: RegisterData2



ALUControl

-
- Diagram illustrating the ALU control logic. The instruction bits [5-0] are fed into the ALU control unit, which outputs control signals to the ALU. The ALU performs operations like Add and Sub based on these control signals and produces an ALU result and a Zero flag.

The diagram illustrates the internal components and data flow of a MIPS processor. Key elements include:

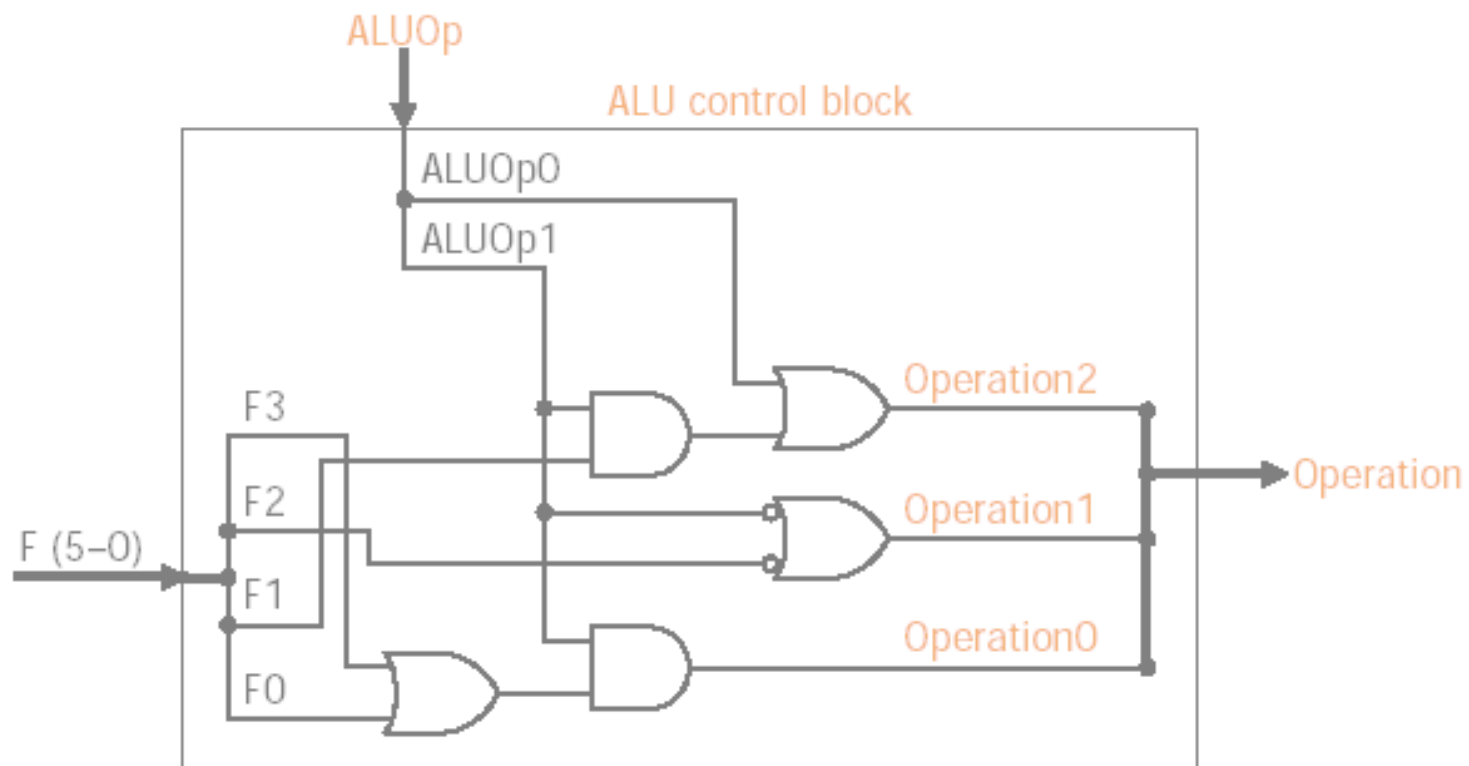
- Instruction Fields:** The instruction is divided into segments: [31-0], [31-26], [25-21], [20-16], [15-11], and [5-0].
- Control Unit:** Receives the [31-26] instruction bits and outputs control signals: RegDst, Branch, MemRead, MemtoReg, ALUOp, MemWrite, ALUSrc, and RegWrite.
- Registers:** A set of registers that store data. They receive write data from the ALU and output read data 1 and read data 2 based on register indices from the instruction.
- ALU (Arithmetic Logic Unit):** Performs operations on data from registers or immediate values. It includes a Zero flag output. The ALU control is determined by the ALUOp field.
- Shifters:** A 'Shift left 2' unit is used to calculate the PCSrc (Program Counter Source).
- Multiplexers (Mux):** Used to select between different data sources (e.g., register data, ALU result, immediate values) for the ALU and the PCSrc.
- Memory:** Data memory that receives addresses and write data, and outputs read data based on the address.
- Sign Extension:** A unit that extends the 16-bit immediate value from the instruction to 32 bits.

ALUControl

ALUOp		Funct field						Operation	
ALUOp1	ALUOp0	F5	F4	F3	F2	F1	F0		
0	0	X	X	X	X	X	X	010	lw/sw
X	1	X	X	X	X	X	X	110	
1	X	X	X	0	0	0	0	010	R-Type
1	X	X	X	0	0	1	0	110	
1	X	X	X	0	1	0	0	000	
1	X	X	X	0	1	0	1	001	
1	X	X	X	1	0	1	0	111	

ALUControl	Function
000	AND
001	OR
010	add
110	subtract
111	set on less than

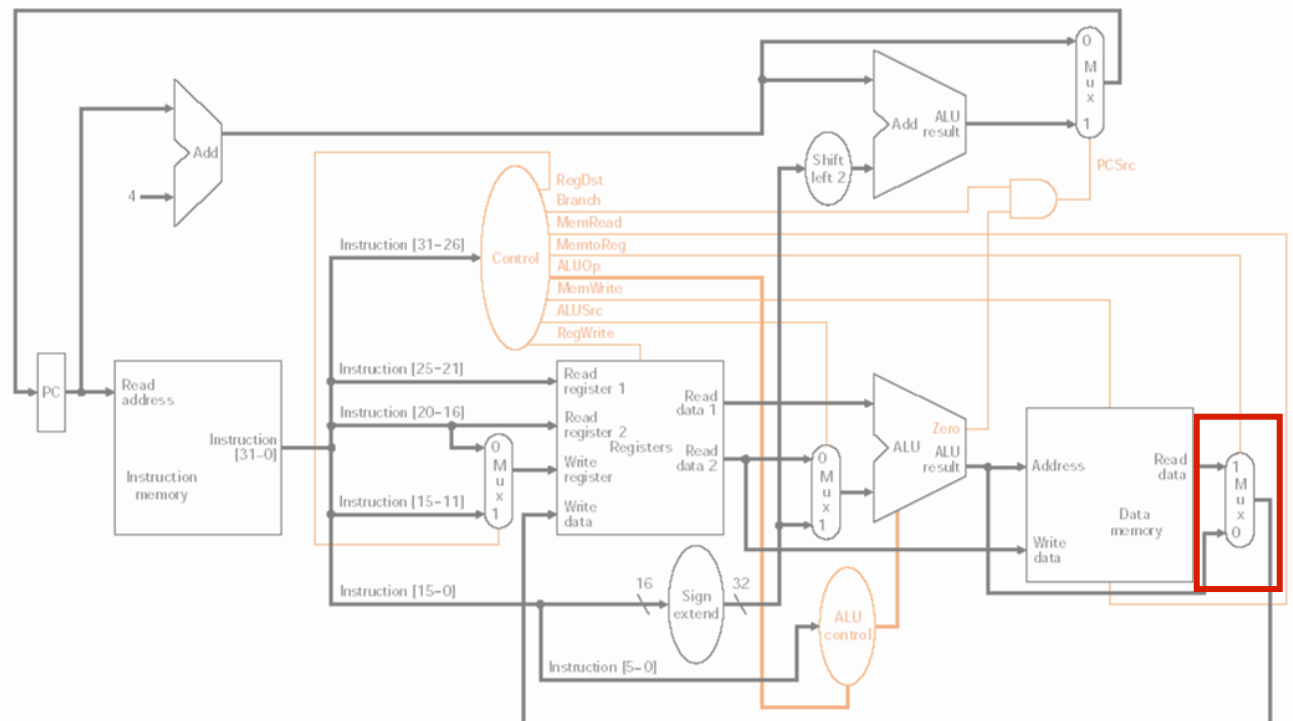
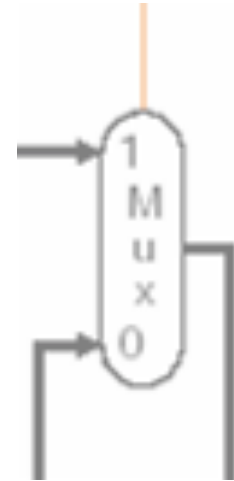
ALU Control Combinational Implementation



Control Signals

MemtoReg

- True: RegisterWriteData = MemReadData
- False: RegisterWriteData = ALUResult

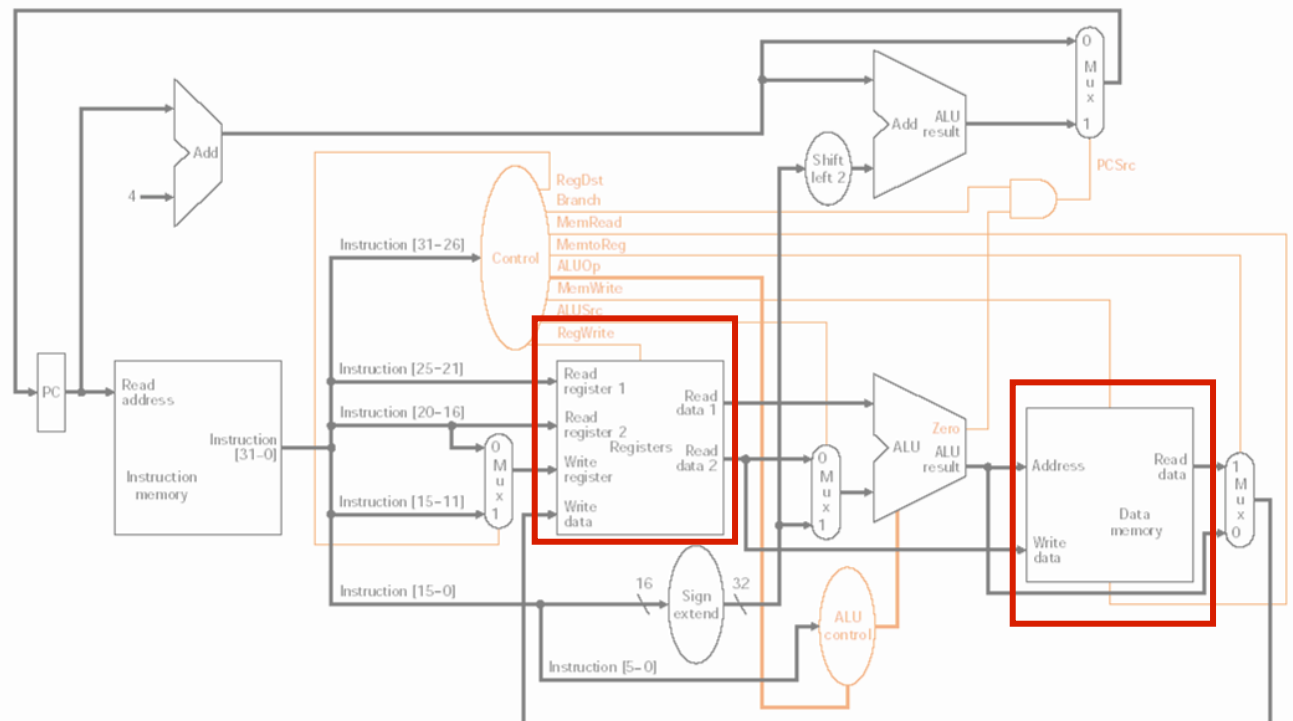
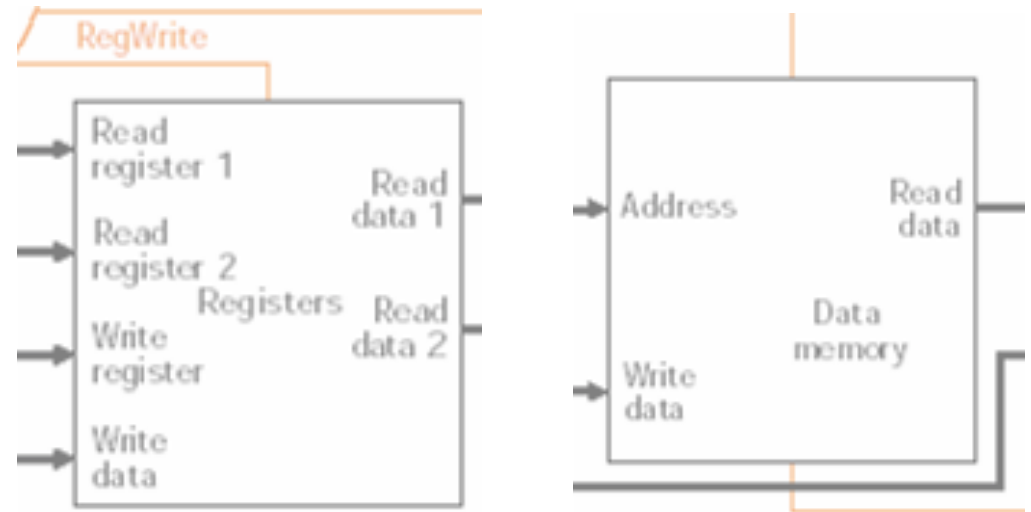


Control Signals

MemRead

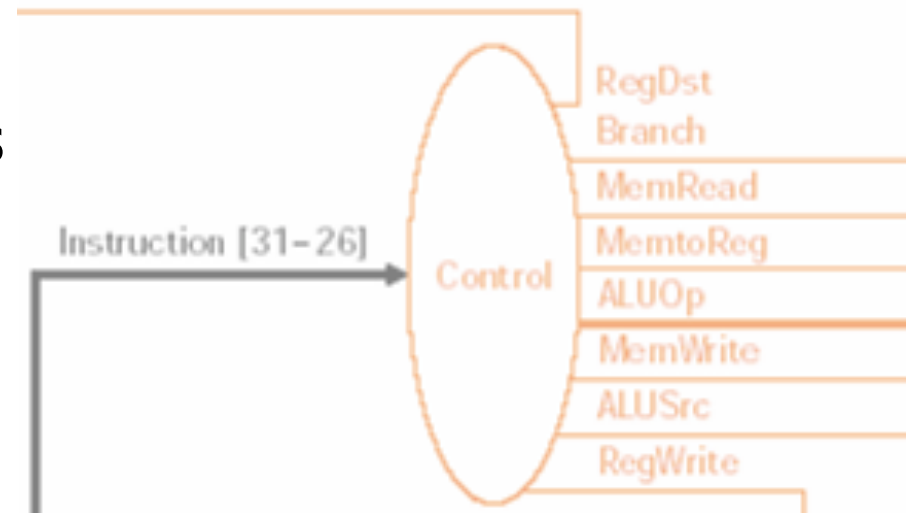
MemWrite

RegWrite



The Control Unit

- Generates Control Signals
- Uses Op Field [31-26]

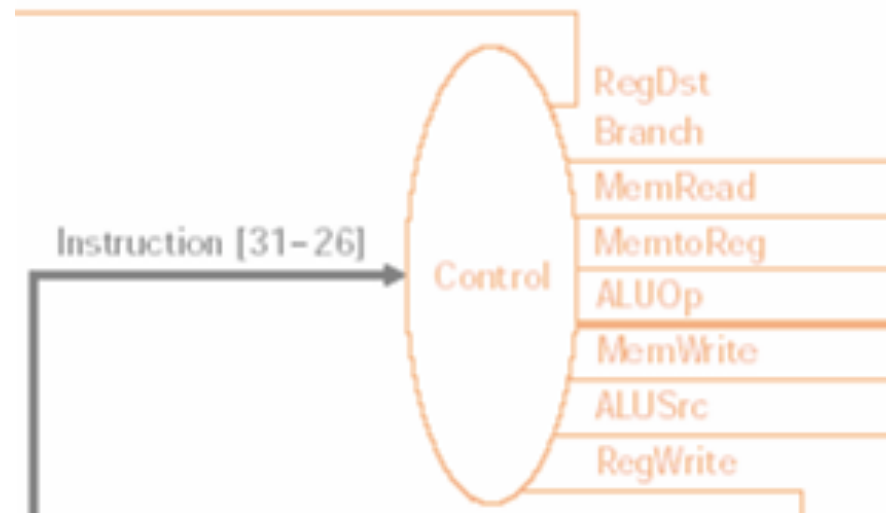


	6 bits	5 bits	5 bits	5 bits	5 bits	6 bits
R:	op	rs	rt	rd	shamt	funct
I:	op	rs	rt	address / immediate		
J:	op	target address				

Control Design: Inputs

Opcode	op5	op4	op3	op2	op1	op0	Value
R-Format	0	0	0	0	0	0	0 ₁₀
lw	1	0	0	0	1	1	35 ₁₀
sw	1	0	1	0	1	1	43 ₁₀
beq	0	0	0	1	0	0	4 ₁₀

Where were these values chosen?



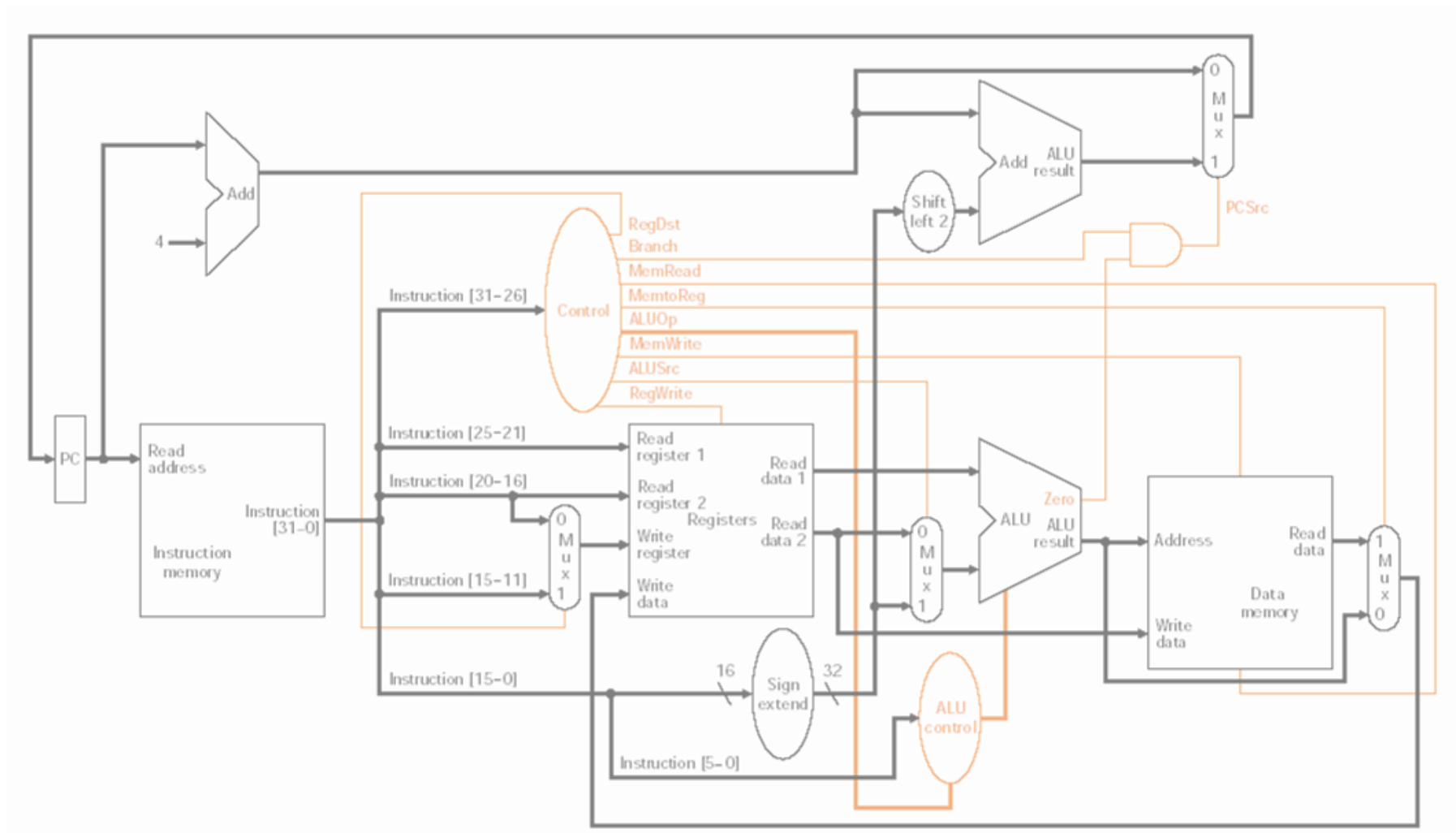
Control Design: Outputs

Signal	R-Format	lw	sw	beq
RegDst				
ALUSrc				
MemtoReg				
RegWrite				
MemRead				
MemWrite				
Branch				
ALUOp1				
ALUOp2				

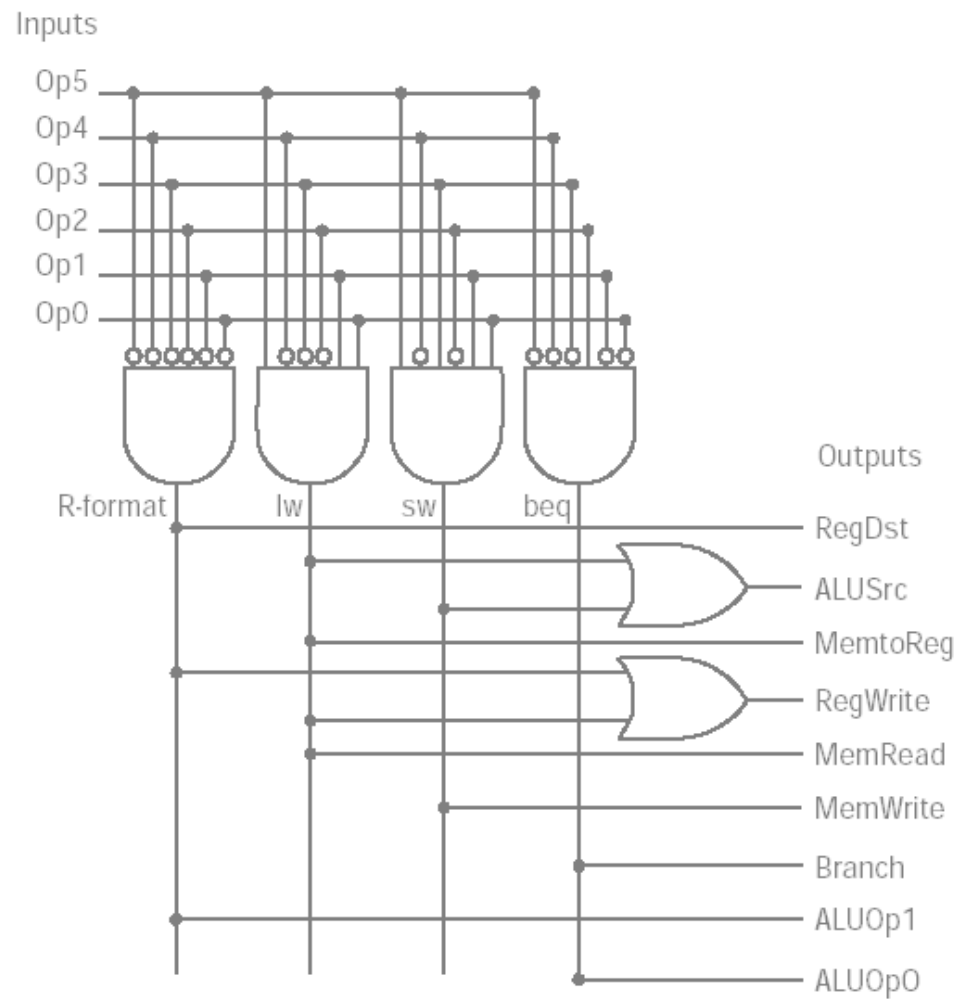


You fill it out with: 0, 1, X (don't care) - check with book

Datapath with Control

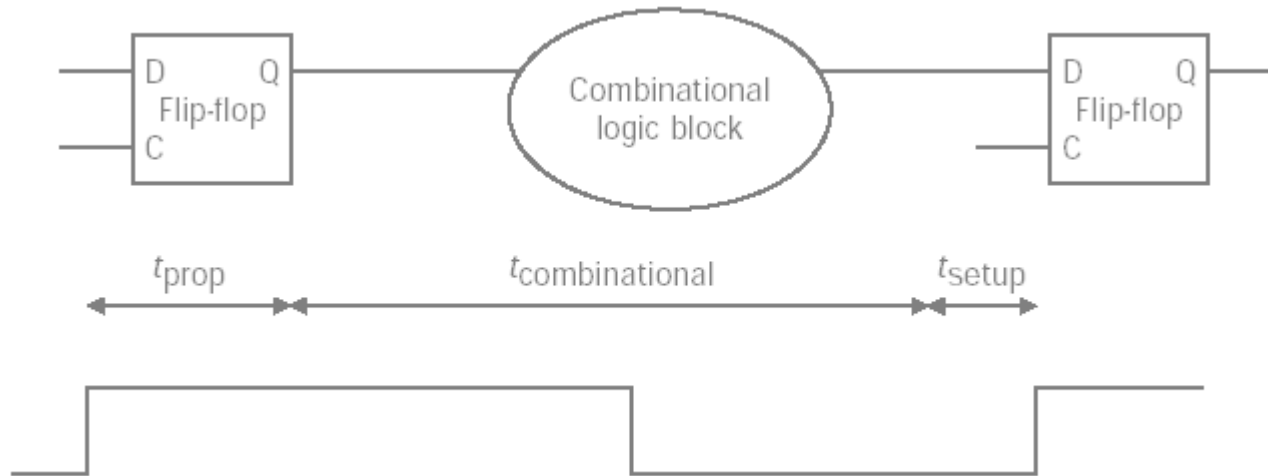


Combinational Implementation





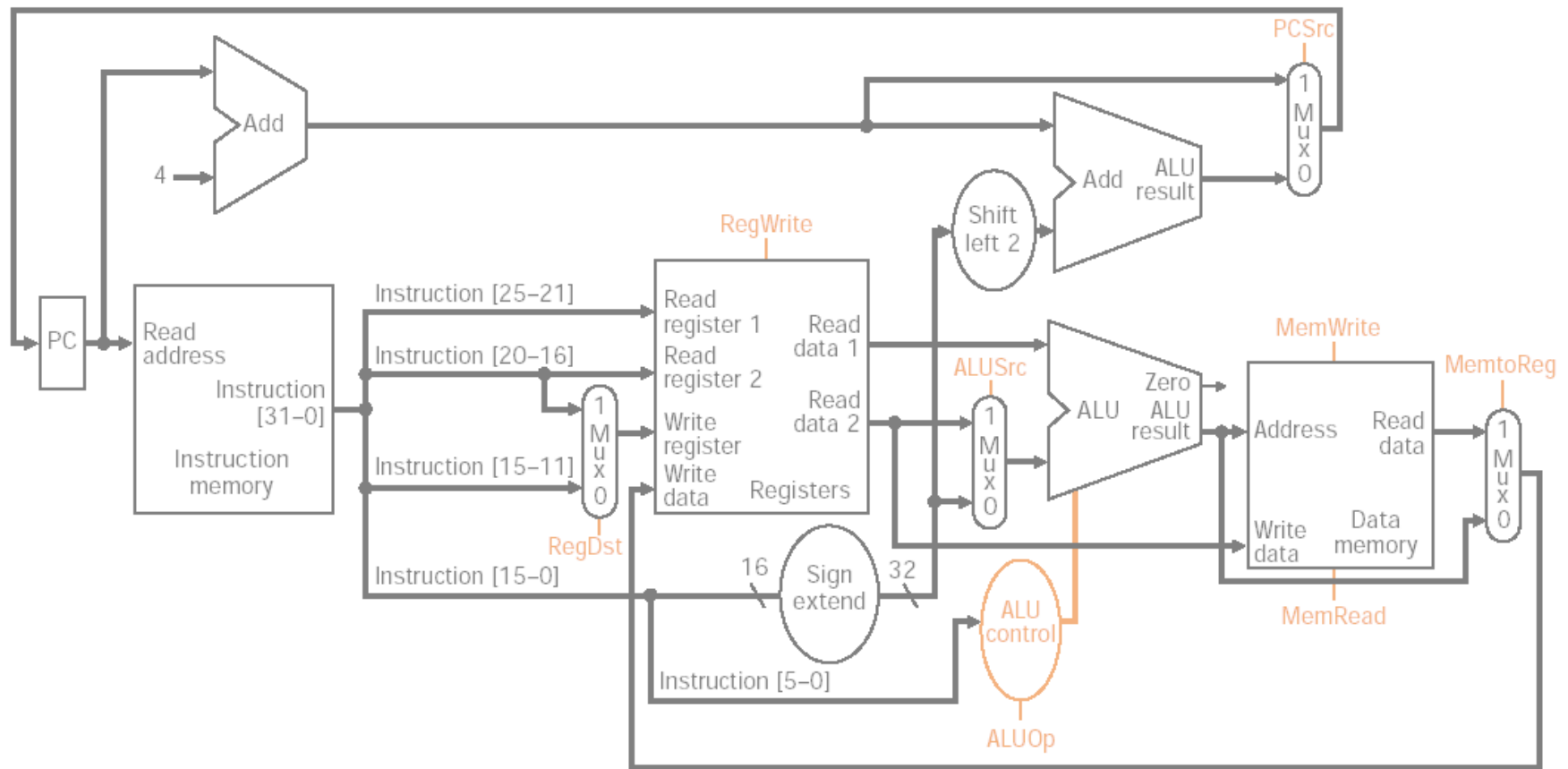
Single Cycle Implementation



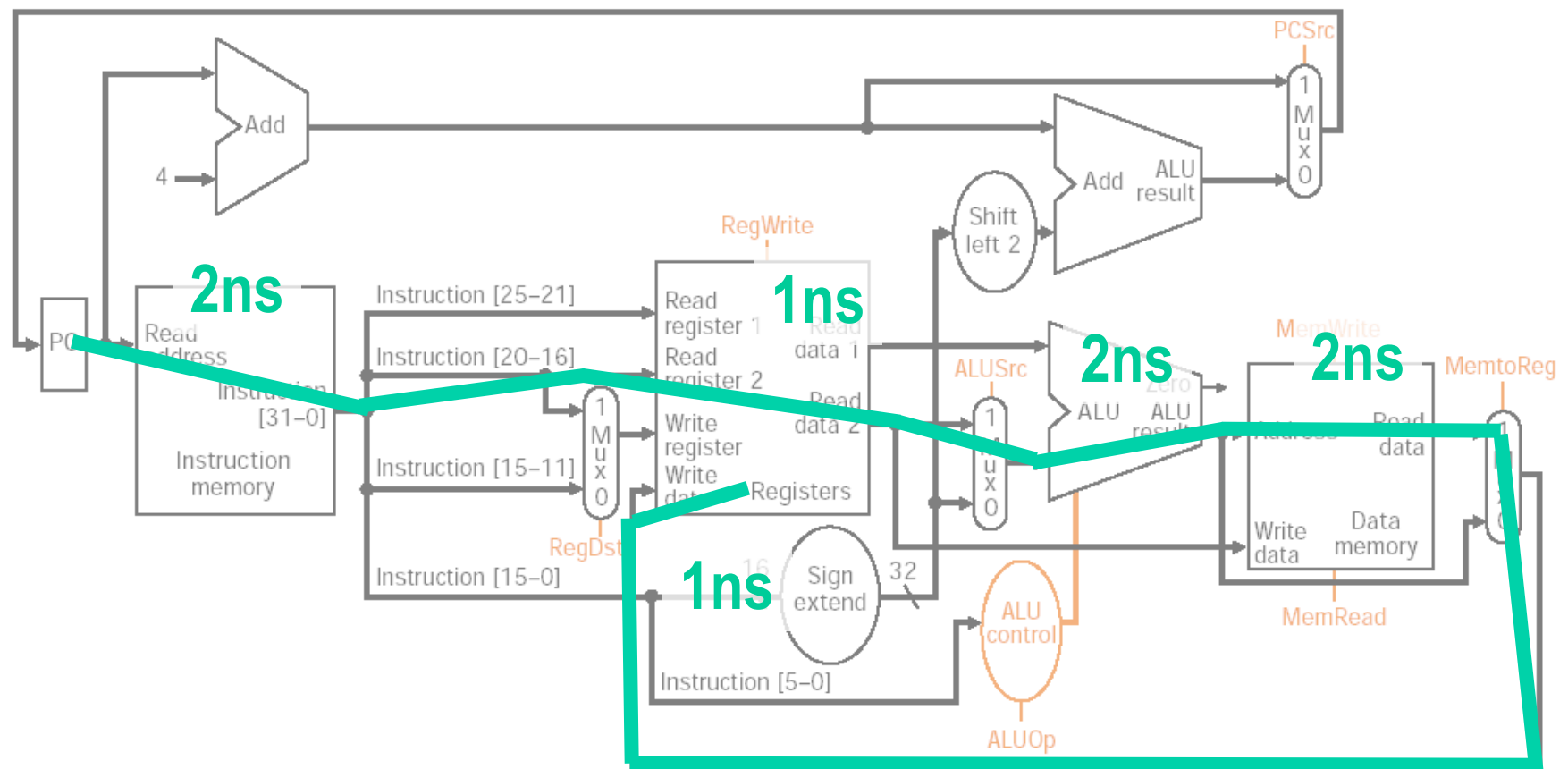
- All of the logic is combinational
- We wait for everything to settle down
 - ALU might not produce “right answer” right away
 - Use write signals along with clock to determine when to write
- Cycle time determined by length of the longest path

Single Cycle Implementation

Calculate cycle time assuming negligible delays except:
memory (2ns), ALU/adders (2ns), register file access (1ns)



Single Cycle Implementation



Load Word is longest running instruction

(prove to yourself by computing time for sw, br, R-type)

memory (2ns), ALU/adders (2ns), register file access (1ns)

$$2ns + 1ns + 2ns + 2ns + 1ns = 8ns$$

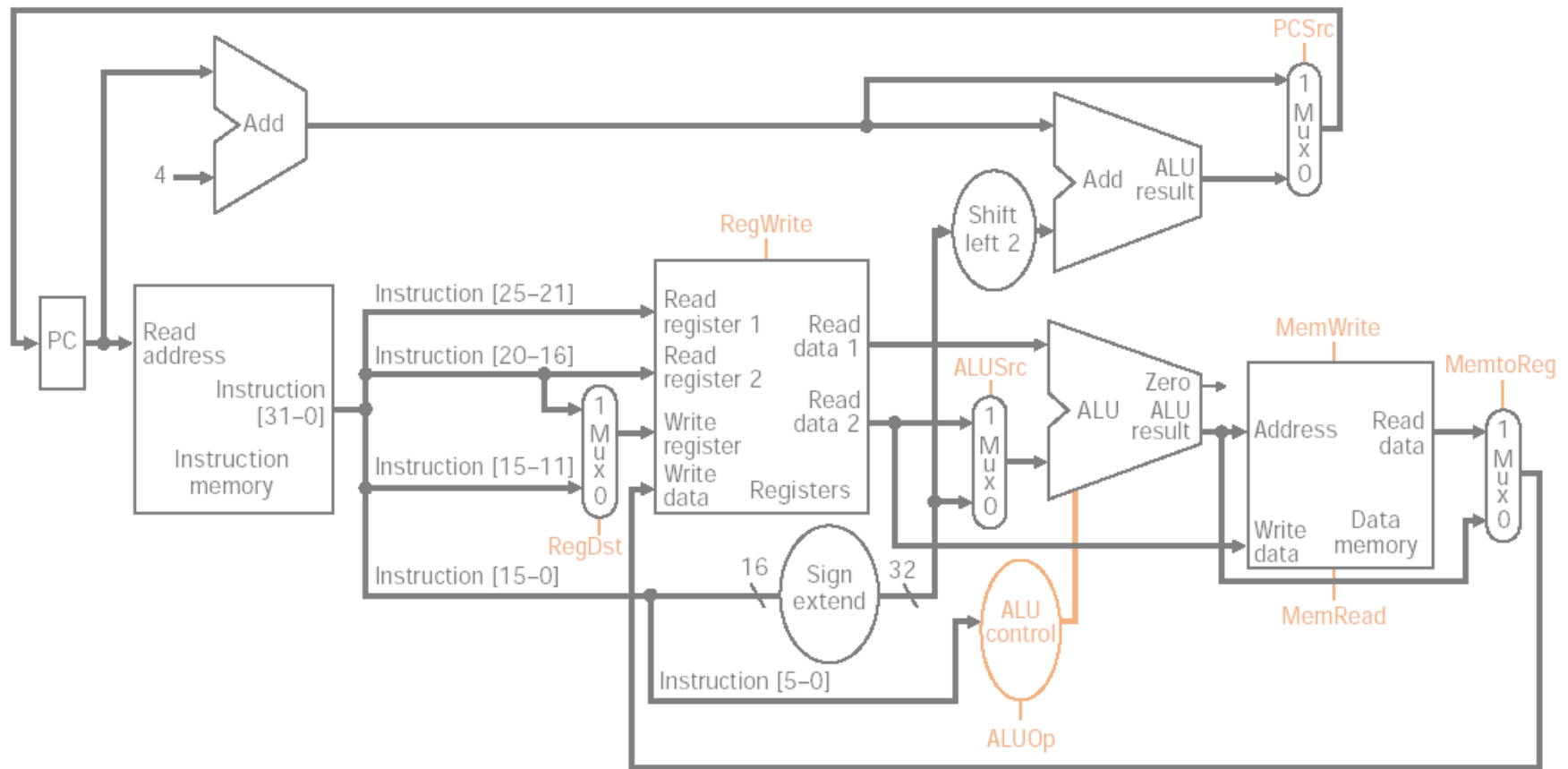
Magic Moment!

At this point, you should be able to design a computer!

1. Analyze instruction set for datapath requirements
2. Select set of datapath components
3. Assemble datapath meeting the requirements
4. Analyze implementation of each instruction to determine setting of control signals
5. Assemble the control logic
6. Set clock rate

What's Wrong with Single Cycle?

Calculate cycle time assuming negligible delays except:
memory (2ns), ALU/adders (2ns), register file access (1ns)



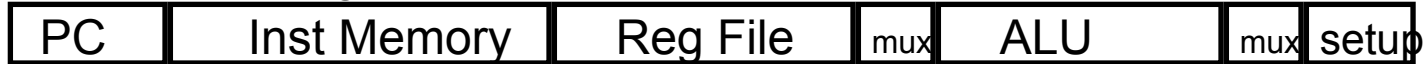
What's Wrong with Single Cycle?

memory (2ns), ALU/adders (2ns), register file access (1ns)

Inst.	Inst. Mem	Reg. Read	ALU	Data Mem	Reg. Write	Total
ALU	2	1	2		1	6
lw	2	1	2	2	1	8
sw	2	1	2	2		7
br	2	1	2			5

What's Wrong with Single Cycle?

Arithmetic & Logical



Load



← Critical Path →

Store



Branch



- Long Cycle Time
- All instructions take as much time as the slowest
- Real memory is not so nice as our idealized memory
(cannot always get the job done in fixed amount of time)

How Bad?

- Assume: 100 instructions executed
 - 25% of instructions are loads (8ns),
 - 10% of instructions are stores (7ns),
 - 45% of instructions are adds (6ns), and
 - 20% of instructions are branches (5ns).

- Single-cycle execution:

$$100 * 8\text{ns} = 800 \text{ ns}$$

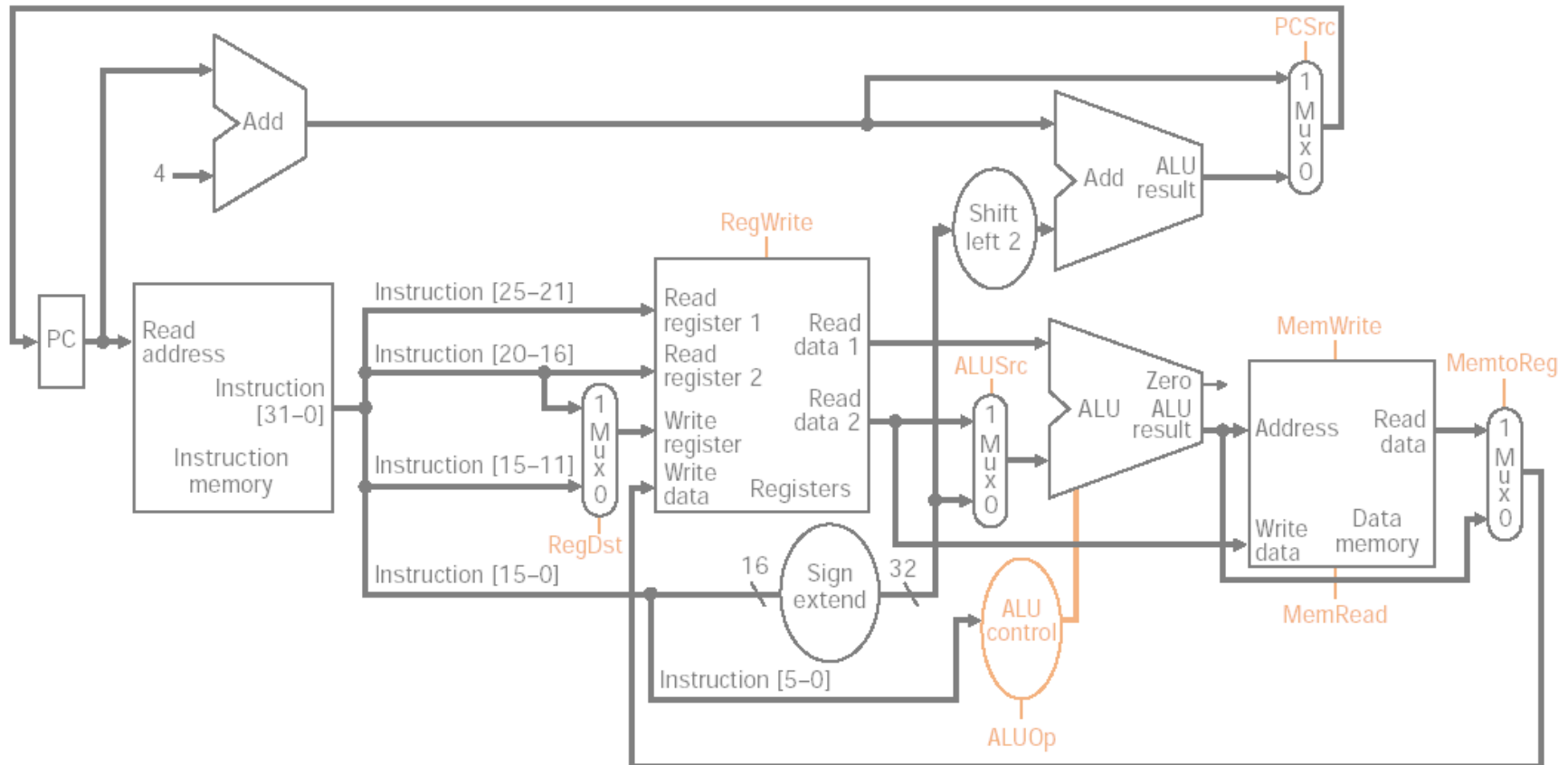
- Optimal execution:

$$25*8\text{ns} + 10*7\text{ns} + 45*6\text{ns} + 20*5\text{ns} = 640 \text{ ns}$$

$$\text{Speedup} = 800/640 = 1.25$$

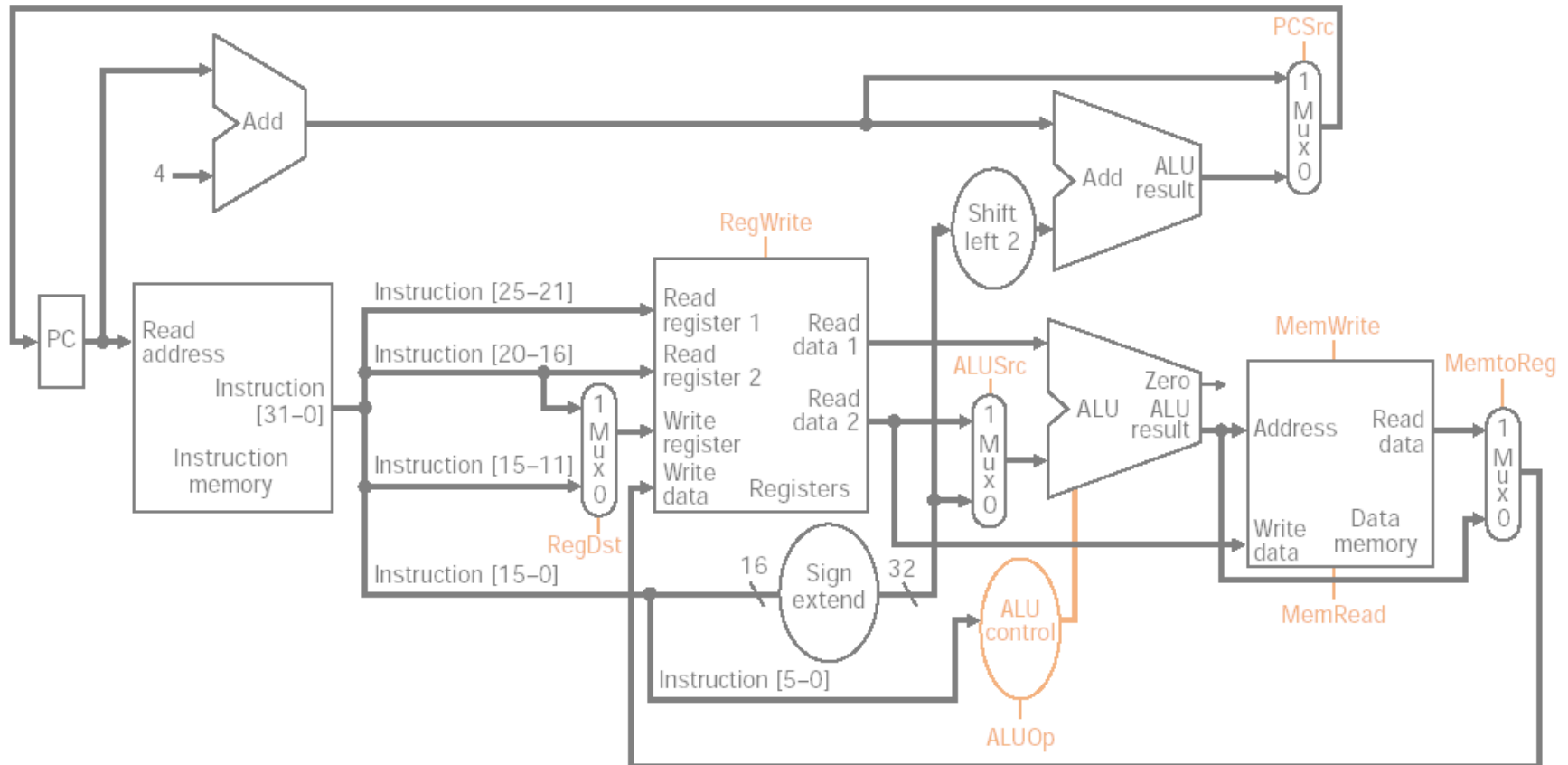
Other Problems

- Instruction and Data Memory are the same
- Some units hold value long after job is complete
 - Could reuse ALU for example
 - Underutilized resources (wasteful of area/power)



Other Problems

- What about floating point or other VERY LONG instructions?

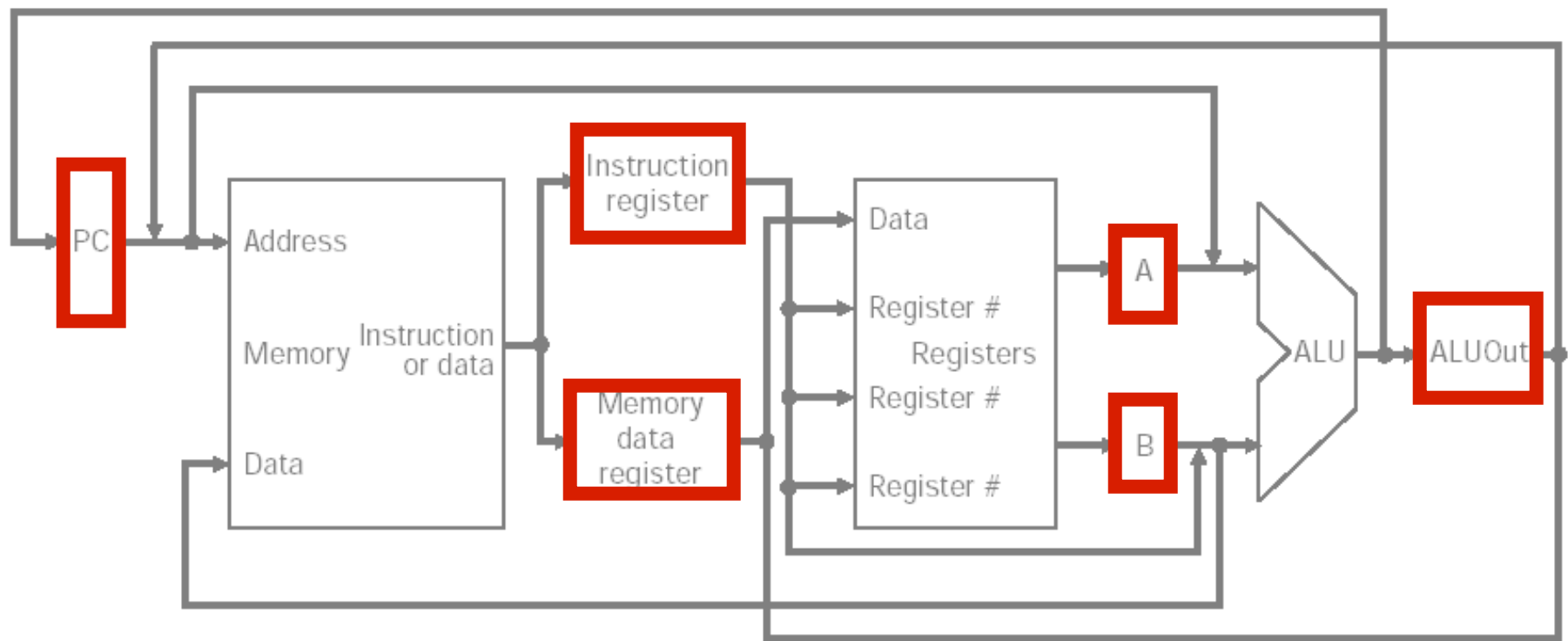




Multicycle Approach

- Break up the instructions into steps, one per cycle
 - balance the amount of work to be done
 - restrict each cycle to use only one major functional unit
- At the end of a cycle
 - store values for use in later cycles (easiest thing to do)
 - introduce additional “internal” registers to hold values between cycles

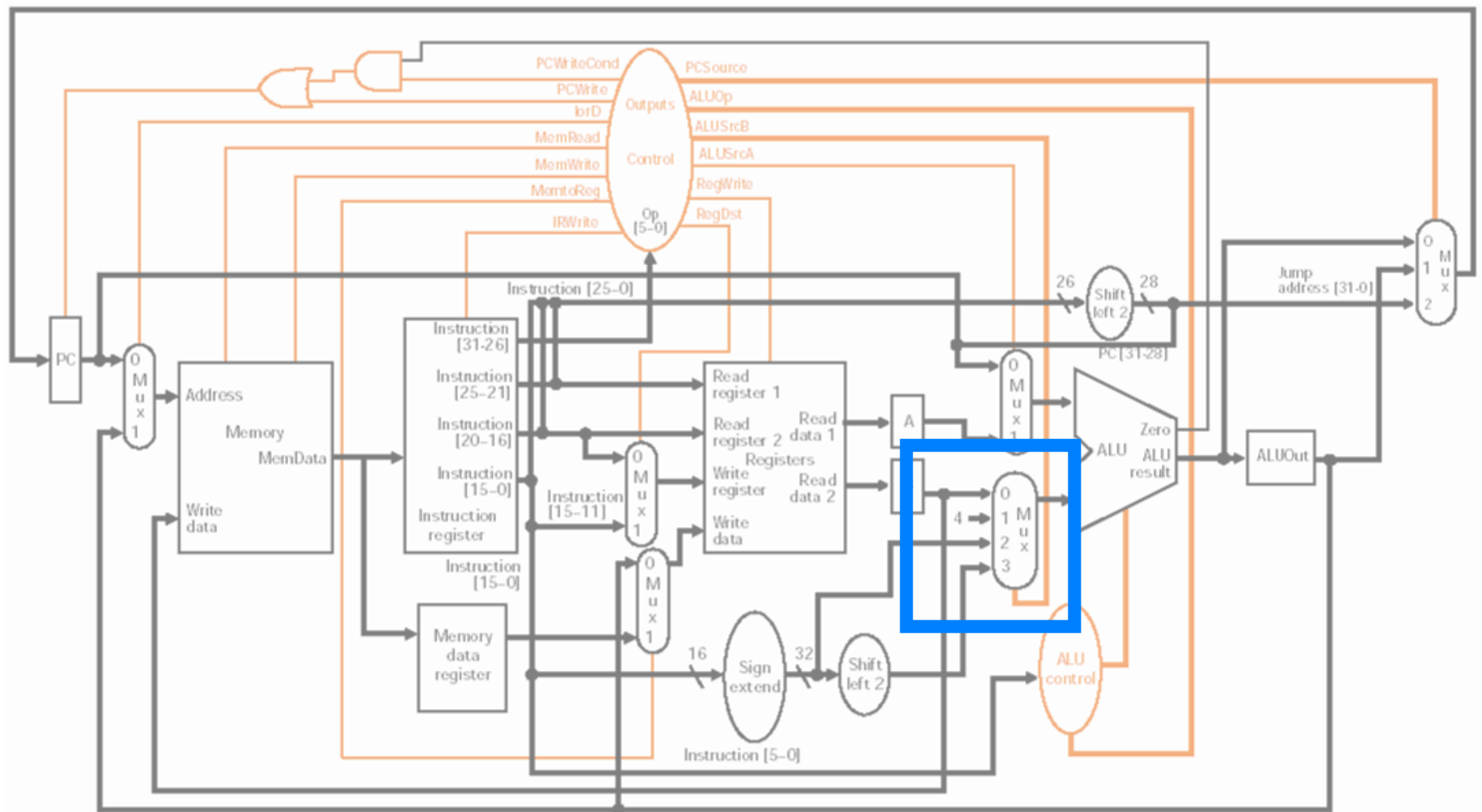
Multicycle Approach



Architectural vs. Microarchitectural State?
Register File?

Multicycle Control

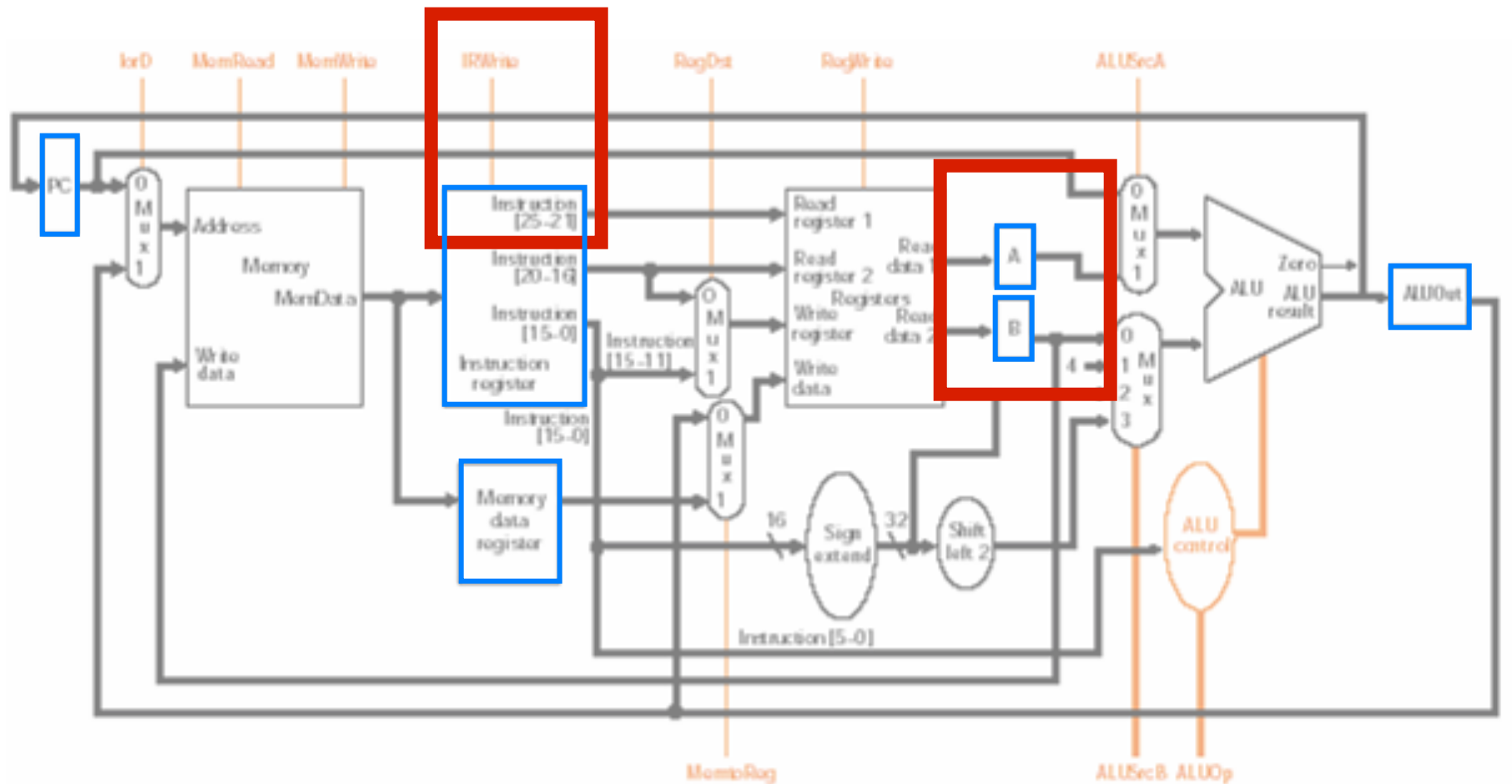
More Mux Magic



Multicycle Control

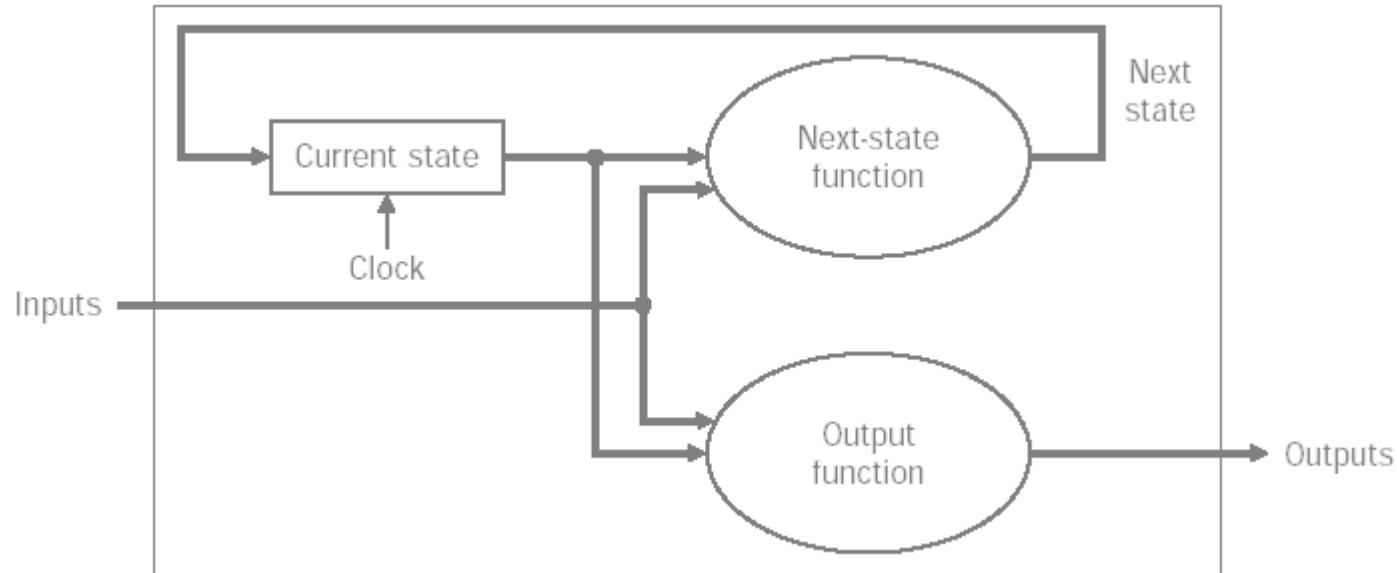
- Reuse datapath components
 - ALU used to compute address and to increment PC
 - Memory used for instruction and data
- Control signals not determined solely by instruction
 - What should the ALU do for a “subtract” instruction?

Multicycle Control



Use Finite State Machine For Control

- Set of states
- Next state function (determined by current state and the input)
- Output function (determined by current state and possibly input)



- We'll use a Moore machine (output based only on current state)
- To derive FSM, need steps of the instruction!



Five Execution Steps

1. Instruction Fetch
2. Instruction Decode and Register Fetch
3. Execution, Memory Address Computation, or Branch Completion
4. Memory Access or R-type instruction completion
5. Write-Back Step

INSTRUCTIONS TAKE FROM 3 - 5 STEPS/CYCLES!

Step 1: Instruction Fetch

- Use PC to get instruction and put it in the Instruction Register.
- Increment the PC by 4 and put result back in the PC.
- Can be described succinctly using RTL "Register-Transfer Language"

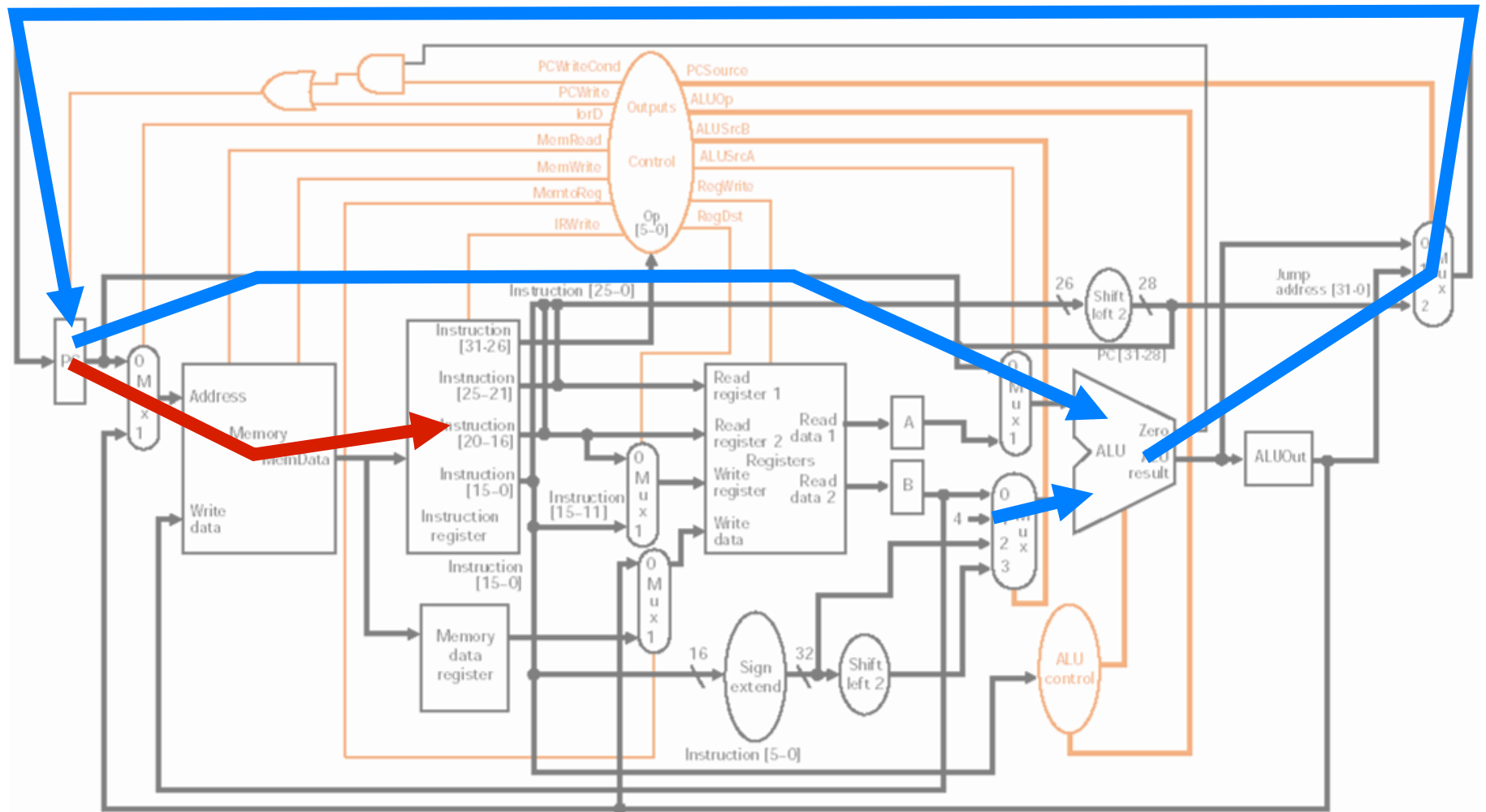
`IR = Memory[PC];`

`PC = PC + 4;`

*Can we figure out the values of the control signals?
ALU? IR?*

What is the advantage of updating the PC now?

Step 1: Instruction Fetch



IR = Memory[PC];

PC = PC + 4;

Step 2:

Instruction Decode & Register Fetch

- Read registers rs and rt in case we need them
- Compute the branch address in case the instruction is a branch
- RTL:

`A = Reg[IR[25-21]];`

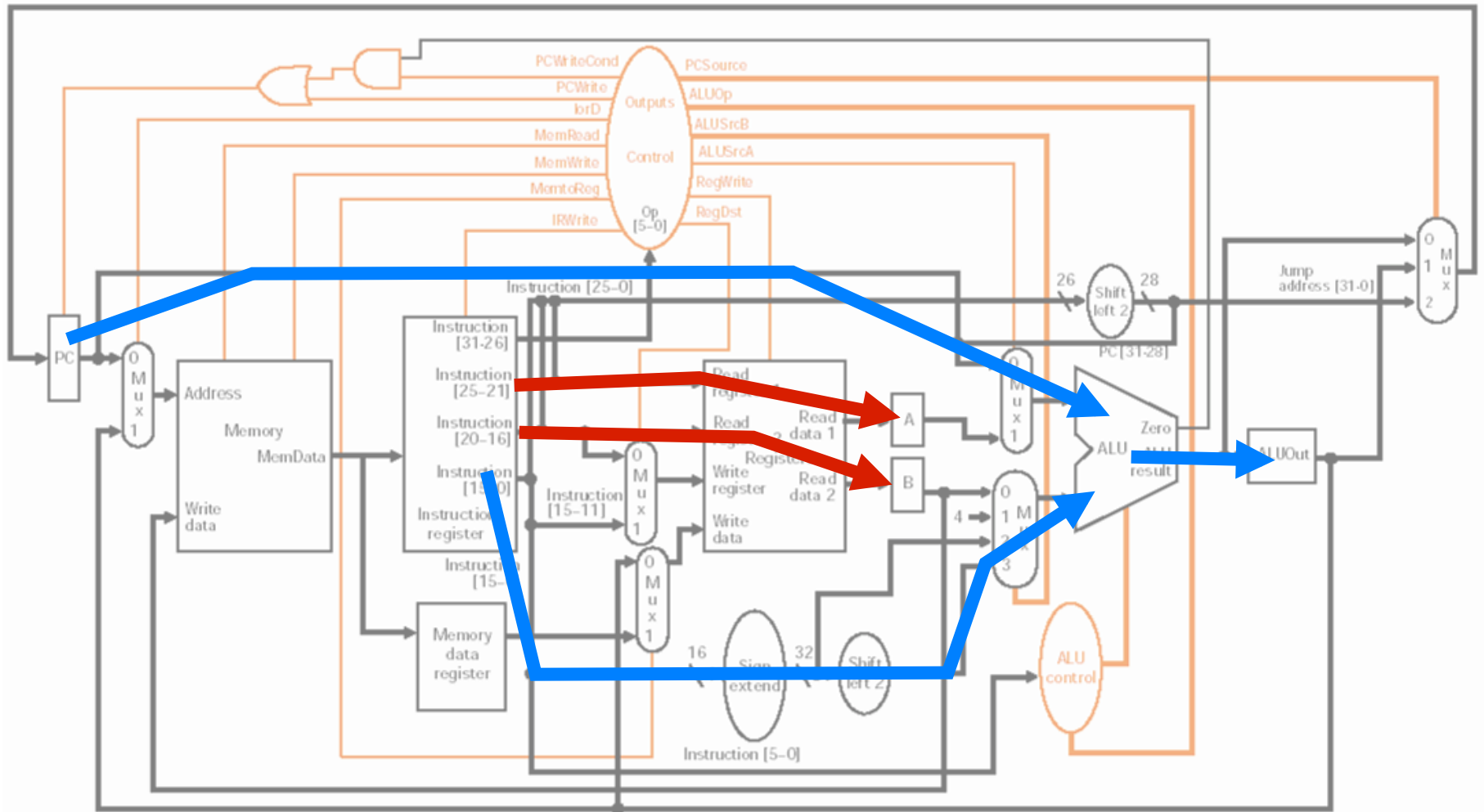
`B = Reg[IR[20-16]];`

`ALUOut = PC + (SgnExt(IR[15-0]) << 2);`

*Note: Again, no control lines based on the instruction type
(busy "decoding" it in control logic)*

Reg? ALU? What if not branch instruction?

Step 2:



A = Reg[IR[25-21]];

B = Reg[IR[20-16]];

ALUOut = PC + (SgnExt(IR[15-0]) << 2);

Step 3: (Instruction Dependent)

ALU performs a function based on instruction type:

- Memory Reference:

$$\text{ALUOut} = A + \text{sign-extend}(\text{IR}[15-0]);$$

- R-type:

$$\text{ALUOut} = A \text{ op } B;$$

- Branch:

$$\text{if } (A == B) \text{ PC} = \text{ALUOut};$$

ALU Utilization rate to step 3?

Step 4: (R-type or memory-access)

- Loads and stores access memory

`MDR = Memory[ALUOut];`

or

`Memory[ALUOut] = B;`

- R-type instructions finish

`Reg[IR[15-11]] = ALUOut;`

Writes takes place at the end of the cycle on the edge

Step 5:

Write-Back

`Reg[IR[20-16]] = MDR;`

What about all the other instructions?

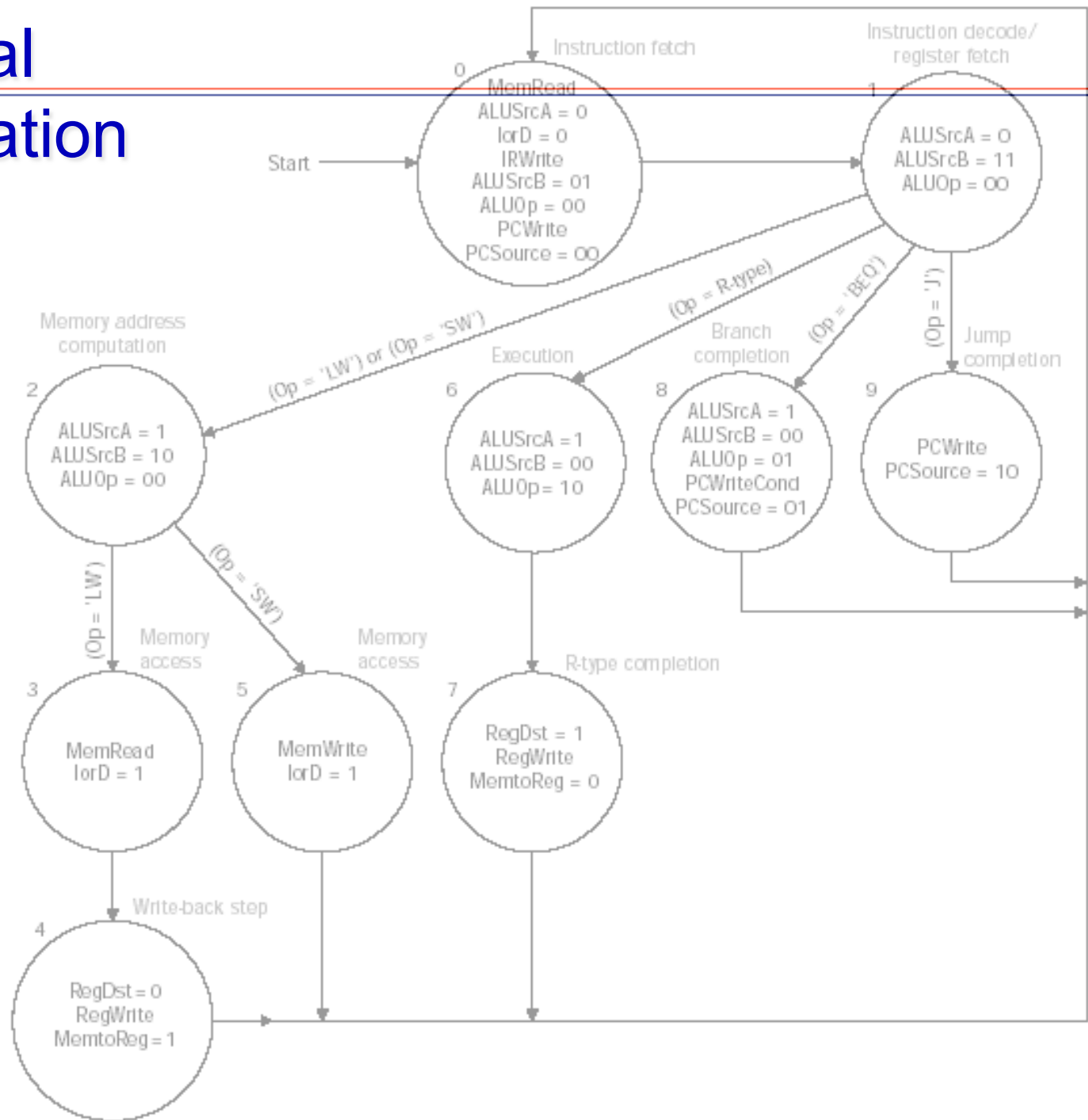
Summary Of Steps

Step name	Action for R-type instructions	Action for memory-reference instructions	Action for branches	Action for jumps
Instruction fetch	$IR = \text{Memory}[PC]$ $PC = PC + 4$			
Instruction decode/register fetch	$A = \text{Reg } [IR[25-21]]$ $B = \text{Reg } [IR[20-16]]$ $ALUOut = PC + (\text{sign-extend } (IR[15-0]) \ll 2)$			
Execution, address computation, branch/ jump completion	$ALUOut = A \text{ op } B$	$ALUOut = A + \text{sign-extend } (IR[15-0])$	if $(A == B)$ then $PC = ALUOut$	$PC = PC[31-28] \parallel (IR[25-0] \ll 2)$
Memory access or R-type completion	$\text{Reg } [IR[15-11]] = ALUOut$	Load: $MDR = \text{Memory}[ALUOut]$ or Store: $\text{Memory } [ALUOut] = B$		
Memory read completion		Load: $\text{Reg}[IR[20-16]] = MDR$		

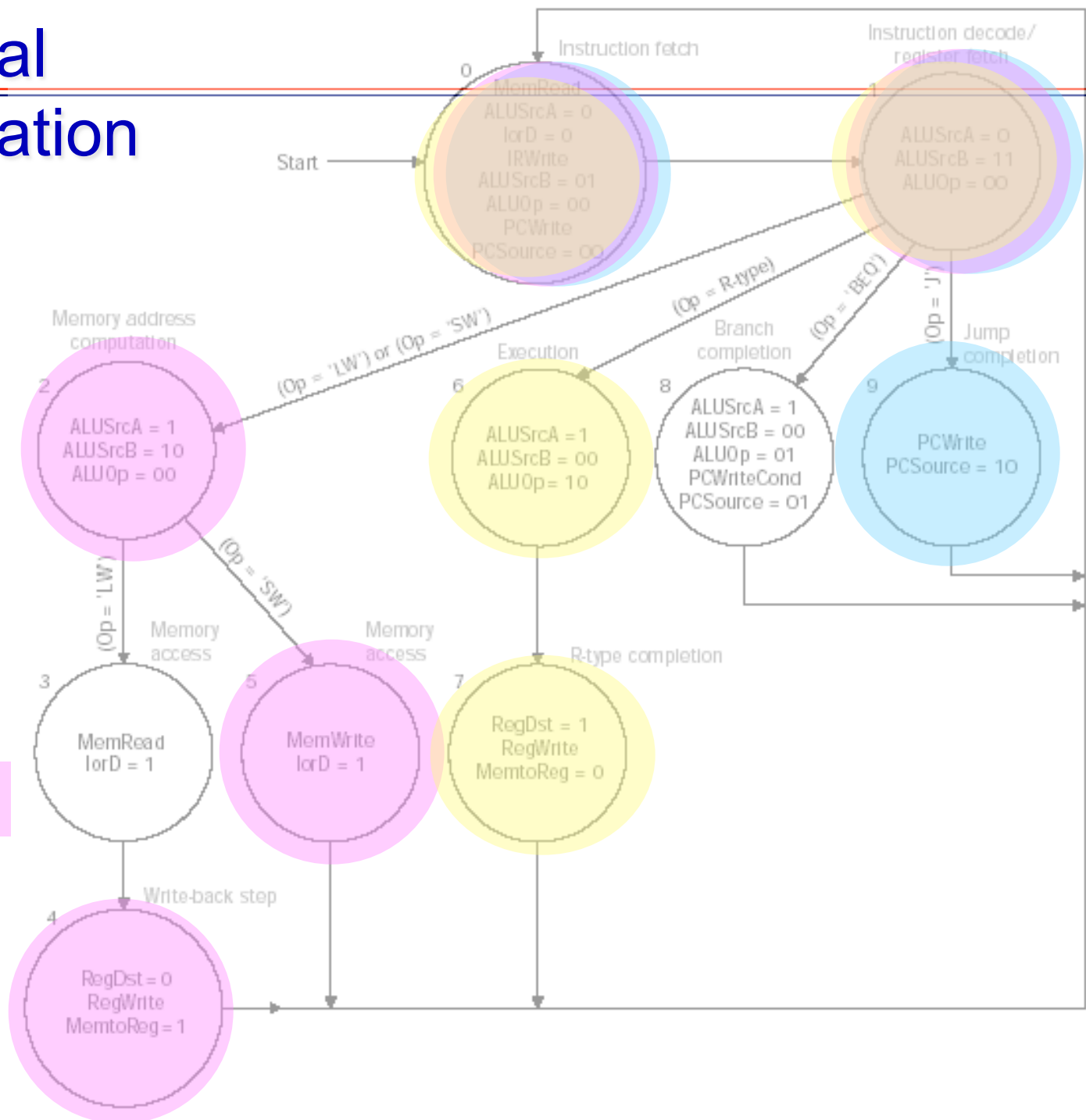
Implementing the Control

- Values of control signals are dependent upon:
 1. instruction is being executed
 2. step is being performed
- Using steps, specify a finite state machine
 - specify the finite state machine graphically, or
 - use “microprogramming” (more on this next time)
- Implementation can be derived from specification

Graphical Specification of FSM



Specification of FSM



Add r1, r2, r3

sw r1, 100(r2)

jr r31

Performance Evaluation

- What is the average CPI?
 - state diagram gives CPI for each instruction type
 - workload gives frequency of each type

Type	CPI_i for type	Frequency	$CPI_i \times freq_i$
Arith/Logic	4	40%	1.6
Load	5	30%	1.5
Store	4	10%	0.4
branch	3	20%	0.6
Average CPI: 4.1			

Single/Multi-Cycle Summary

$$CPU\ time = \frac{Instructions}{Program} \times \frac{Cycles}{Instruction} \times \frac{Seconds}{Cycle}$$

Single Cycle Datapath:

- CPI = 1!!
- Long cycle time ☹️
(critical path based)

Multiple Cycle Datapath:

- Short cycle time!!
- CPI = 3-5 ☹️

Can we achieve a CPI of 1 (on average)
with a clock cycle time
similar to the multiple cycle datapath?