

# COS 126 – Atomic Theory of Matter

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# Goal of the Assignment

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- Calculate Avogadro's number
  - Using Einstein's equations
  - Using fluorescent imaging
- Input data
  - Sequence of images
  - Each image is a rectangle of pixels
  - Each pixel is either light or dark
- Output
  - Estimate of Avogadro's number



# Assignment: Four Programs

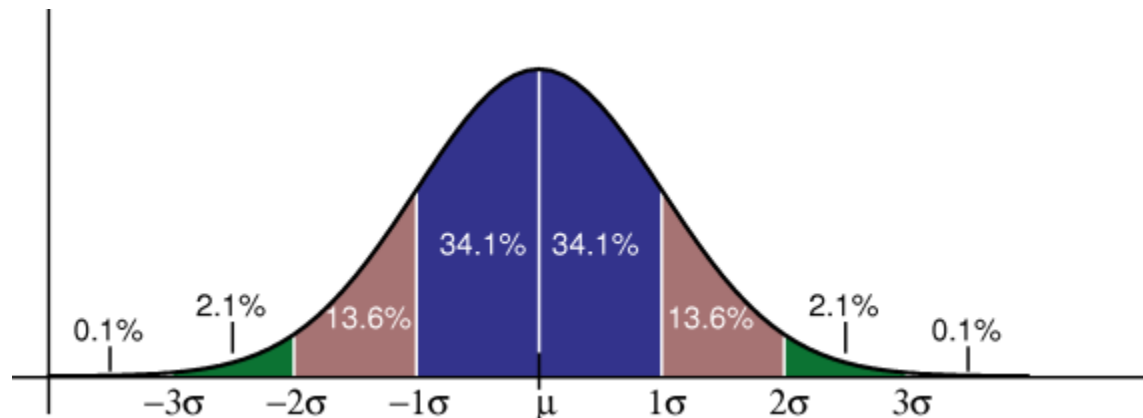
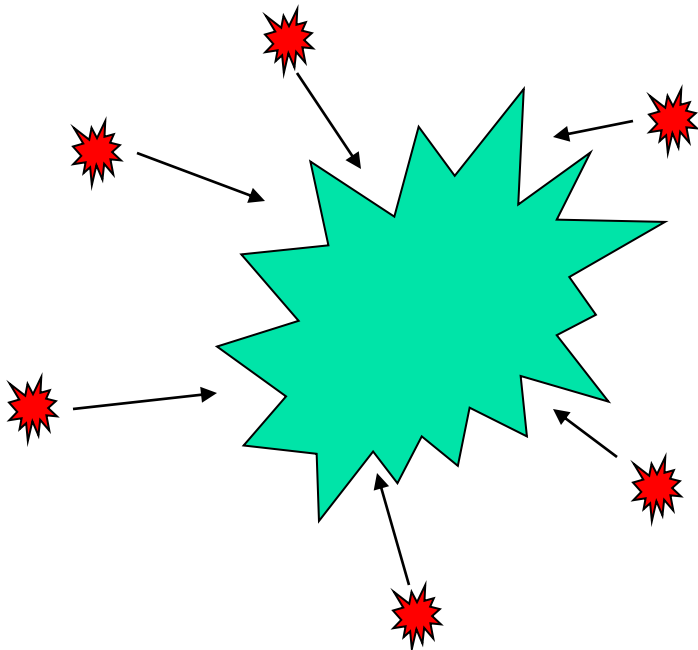
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- Blob data type
  - Maximal set of connected light pixels
- BlobFinder
  - Find *all* blobs in a JPEG image
  - List all the *big* blobs (aka beads)
- BeadTracker
  - Track beads from one image to the next
- Avogadro
  - Data analysis to estimate Avogadro's number from the motion of beads

# Atomic Theory Overview

## ■ Brownian Motion

- Random collision of molecules
- Displacement over time fits a Gaussian distribution





# Atomic Theory Overview

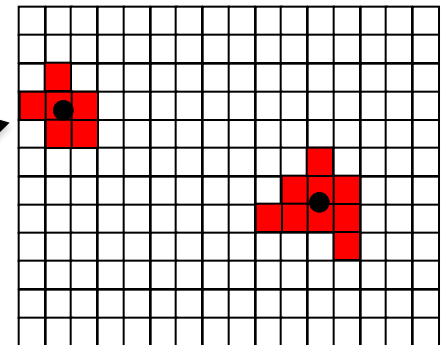
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- Avogadro's Number
  - Number of atoms needed to equal substance's atomic mass in grams
    - $N_A$  atoms of Carbon-12 = 12 grams
  - Can calculate from Brownian Motion
    - Variance of Gaussian distribution is a function of resistance in water, number of molecules

# Blob.java

- API for representing particles (blobs) in water
  - `public Blob()`
  - `public void add(int i, int j)`
  - `public int mass() // number of pixels`
  - `public double distanceTo(Blob b) // from center (average)`
  - `public String toString()`
- Only need *three* values to efficiently store
  - Do *not* store the positions of every pixel in the blob

Center of mass,  
and # of pixels





# Blob Challenges

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- Format numbers in a nice way
  - `String.format("%2d (%8.4f, %8.4f)", mass, cx, cy);`
  - (Use same format in `System.out.printf()`)
  - E.g., `"%6.3f"` -> `_2.354`
  - E.g., `"%10.4e"` -> `1.2535e-23`
- Thoroughly test
  - Create a simple `main()`



# BlobFinder.java

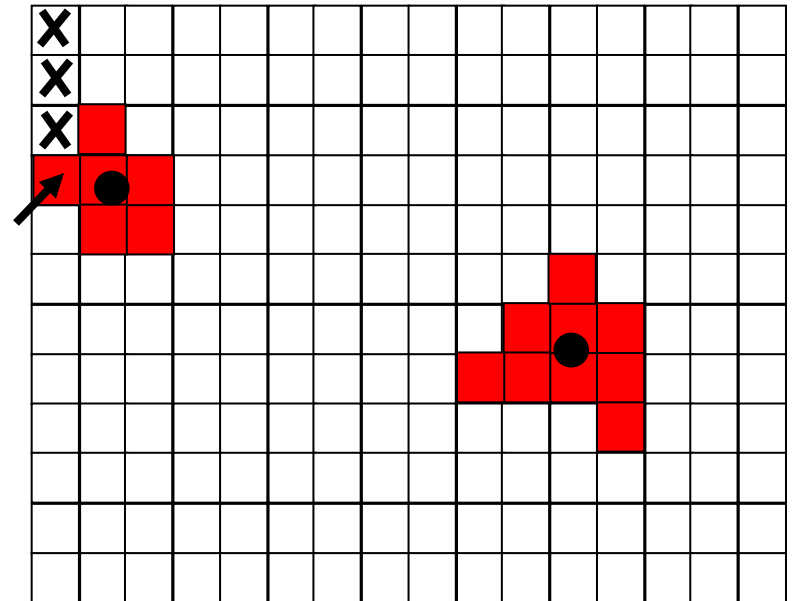
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- Locate all blobs in a given image
  - And identify large blobs (called beads)
- API
  - `public BlobFinder(Picture picture, double threshold)`
    - Calculate luminance (see `Luminance.java`, 3.1)
      - Include pixels with a luminance  $\geq$  threshold
    - Find blobs with DFS (see `Percolation.java`, 2.4)
      - The hard part, next slide...
  - `public Blob[] getBeads(int minSize)`
    - Returns all beads with at least `minSize` pixels
    - Array must be of size equal to number of beads



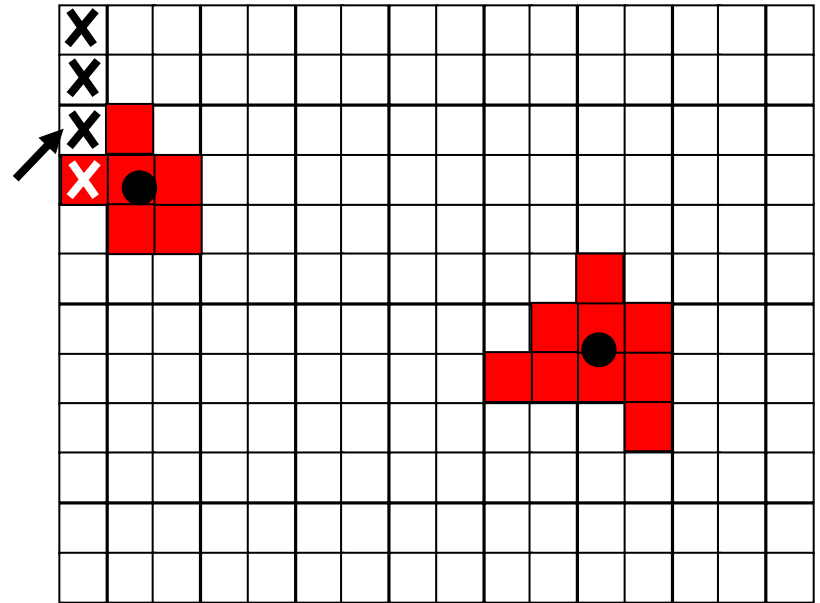
# BlobFinder - Depth First Search

- Use boolean[][] array to mark visited
- Traverse image pixel by pixel
  - Dark pixel
    - Mark as visited, continue
  - Light pixel
    - Create new blob, call DFS
- DFS algorithm
  - Base case: simply return if
    - Pixel out-of-bounds
    - Pixel has been visited
    - Pixel is dark (and mark as visited)
  - Add pixel to current blob, mark as visited
  - Recursively visit up, down, left, and right neighbors



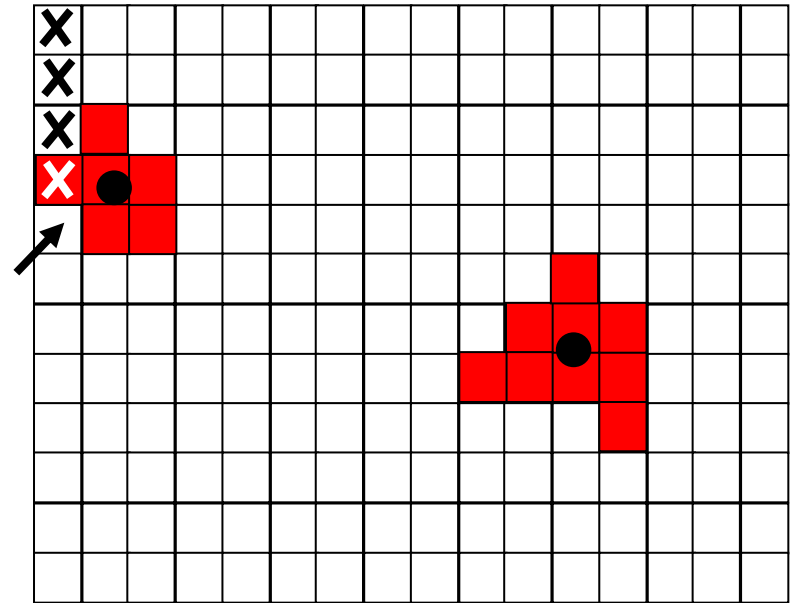
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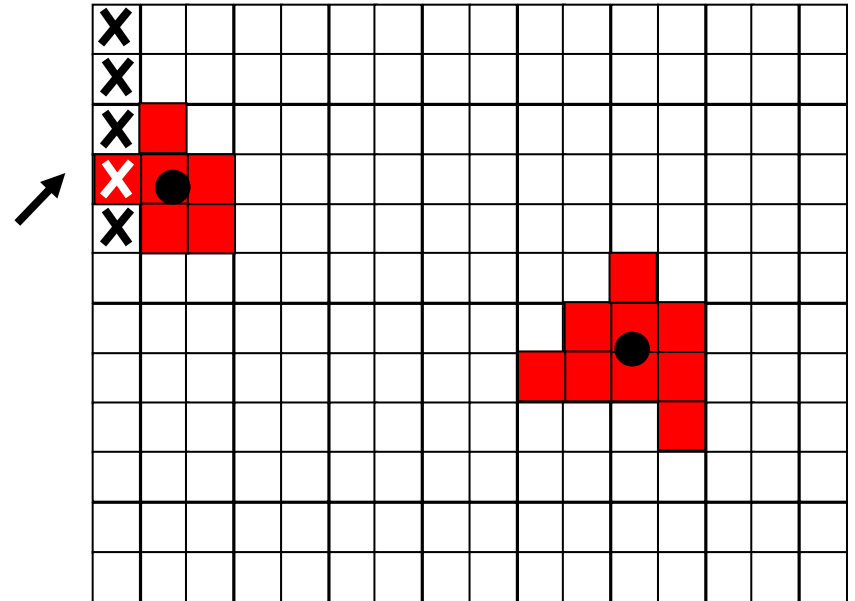
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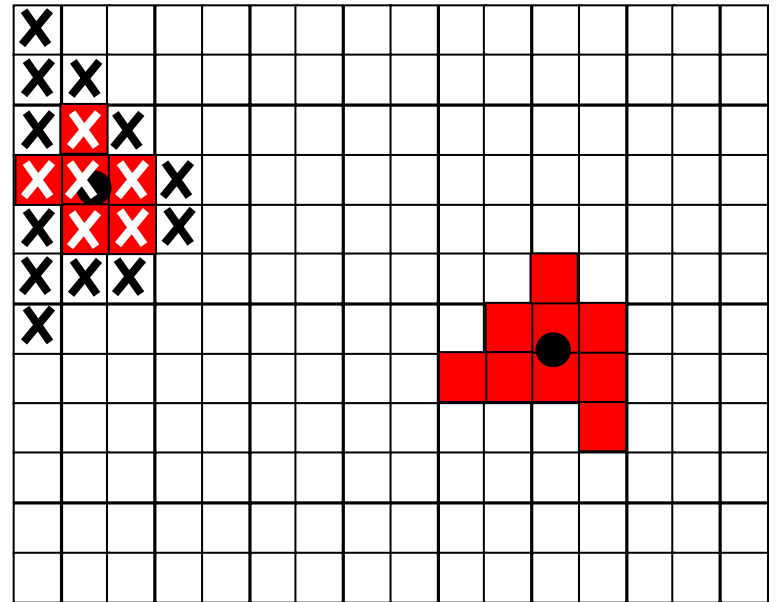
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# BlobFinder Challenges

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- Data structure for the collection of blobs
  - Store them any way you like
  - But be aware of memory use and timing



# BlobFinder Challenges

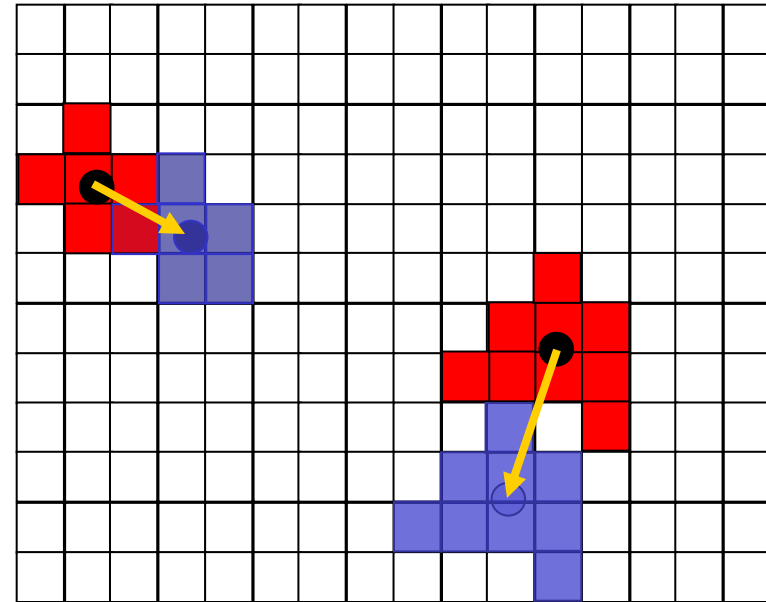
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- Data structure for the collection of blobs
  - Store them any way you like
  - But be aware of memory use and timing
- Array of blobs?
  - But how big should the array be?
- Linked list of blobs?
  - Memory efficient, but harder to implement
  - Avoid traversing whole list to add a blob!
- Anything else?
  - Submit your (extra) object classes if not in 4.3



# BeadTracker.java

- Track beads between successive images
- Single main function
  - Take in a series of images
  - Output distance traversed by all beads for each time-step
    - For each bead found at time  $t+1$ , find closest bead at time  $t$  and calculate distance
      - Not the other way around!
      - Don't include if distance  $> 25$  pixels (new bead)





# BeadTracker Challenges

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- Reading multiple input files
  - `java BeadTracker run_1/*.jpg`
  - Expands files in alphabetical order
  - End up as `args[0]`, `args[1]`, ...
- Avoiding running out of memory
  - How?
- Recompiling
  - Recompile if Blob or BlobFinder change



# BeadTracker Challenges

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- Reading multiple input files
  - `java BeadTracker run_1/*.jpg`
  - Expands files in alphabetical order
  - End up as `args[0]`, `args[1]`, ...
- Avoiding running out of memory
  - Do *not* open all picture files at same time
  - Only two need to be open at a time
- Recompiling
  - Recompile if `Blob` or `BlobFinder` change



# Avogadro.java

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- Analyze Brownian motion of all calculated displacements
  - Lots of crazy formulas, all given, pretty straightforward
  - Be careful about units in the math, convert pixels to meters, etc.
- Can test without the other parts working
  - We provide sample input files
  - Can work on it while waiting for help



# Conclusion: Final Tips

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- Avoiding subtle bugs in BlobFinder
  - Double check what happens at corner cases (e.g. at boundary pixels, or when luminance == tau, or mass == cutoff)
- Common errors in BlobFinder
  - NullPointerException
  - StackOverflowError (e.g., if no base case)
  - No output (need to add prints)
- Look at checklist Q&A



# Conclusion: Final Tips

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- Testing with a main()
  - BlobFinder, BeadTracker, and Avogadro
  - Must have a main() that can handle I/O described in Testing section of checklist
- Timing analysis
  - Look at feedback from earlier assignments
  - BeadTracker is time sink, so analyze that
- How can you run 100 frames?