



# COS526: Advanced Computer Graphics



Tom Funkhouser  
Fall 2014



# Background

## Image Processing

- Basic signal processing
- Filtering, resampling, warping, ...

## Rendering

- Polygon rendering pipeline
- Basic ray tracing

## Modeling

- Basic 3D object representations
- Polygonal meshes

# Background



## Image Processing

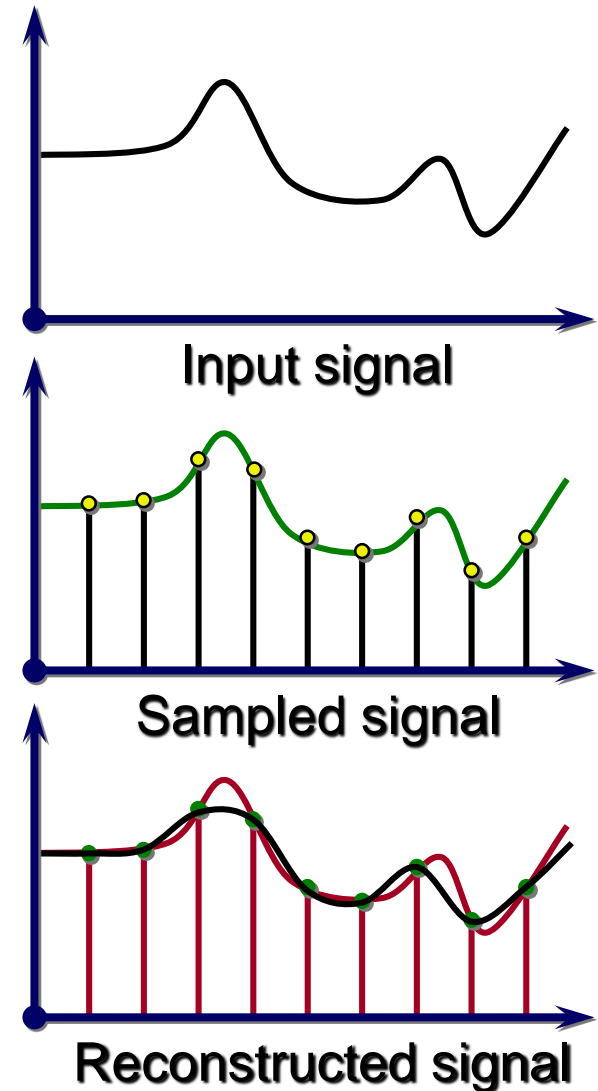
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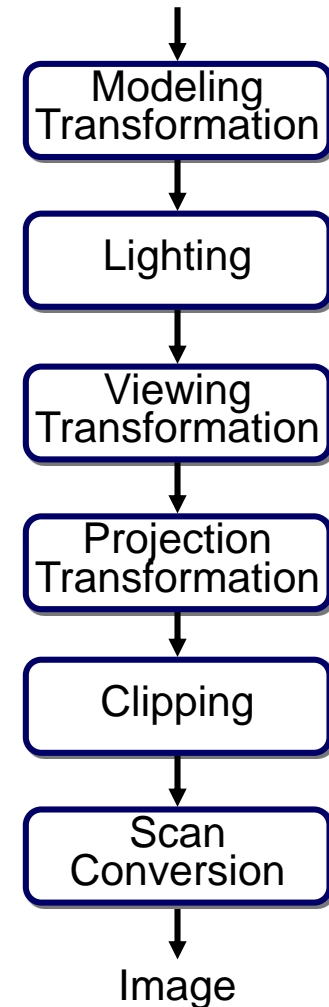
## Rendering

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## Modeling

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- Polygonal meshes

## 3D Geometric Primitives





# Background

## Image Processing

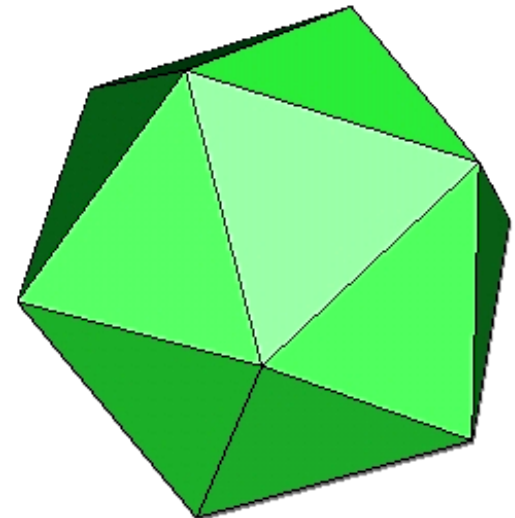
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# CS526 Syllabus



## Global illumination

- Photon mapping
- Monte Carlo path tracing

## Computational Photography

- Image composition
- Texture synthesis
- Image-based rendering

## Geometric Representations

- Multiresolution meshes
- Laplacian meshes
- Point representations

## Shape Analysis

- Feature detection
- Segmentation
- Correspondence



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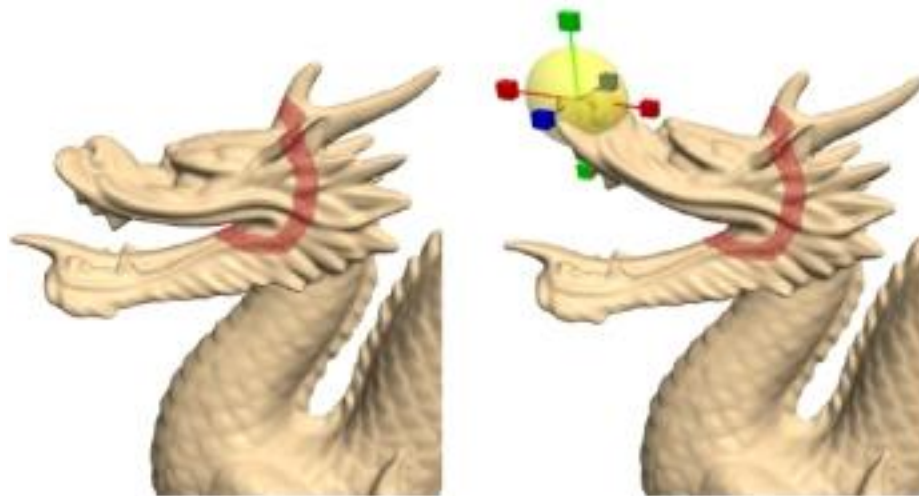
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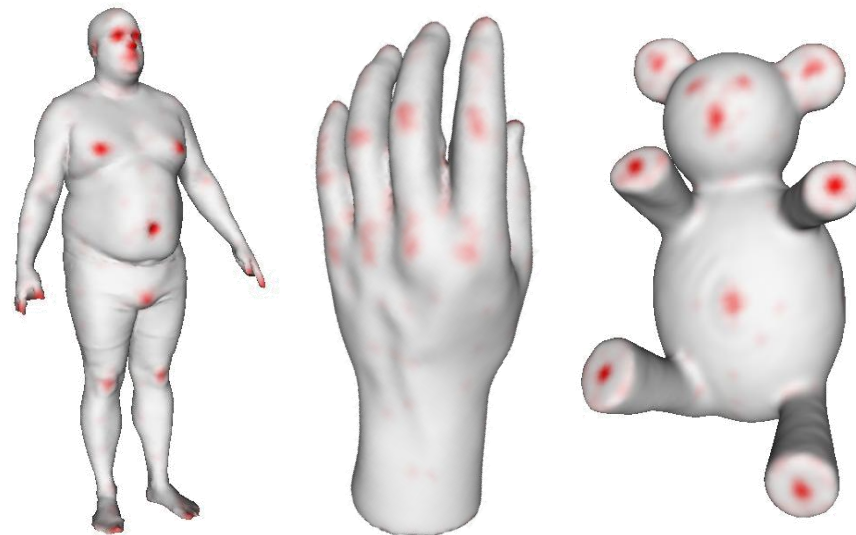
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# CS526 Syllabus



COS526: Syllabus

www.cs.princeton.edu/courses/archive/fall14/cos526/syllabus.php

## COS 526 Advanced Computer Graphics Fall 2012



[General](#) | [Syllabus](#) | [Homework](#)

### Syllabus (tentative)

Week	Lectures (click for notes)	Readings
Wed 9/10	<a href="#">Rendering Equation</a>	[ <a href="#">kajiya86</a> ] [ <a href="#">zimmerman98</a> ] [ <a href="#">greenberg97</a> ]
1 Mon 9/15	Photon Mapping	[ <a href="#">jensen96</a> ] [ <a href="#">jensen01</a> ]
Wed 9/17	Monte Carlo Path Tracing	[ <a href="#">jensen03</a> ]
2 Mon 9/22	Radiosity	[ <a href="#">cohen88</a> ]
Wed 9/24	Visibility	[ <a href="#">durand00</a> ]
Wed 9/24	Written Exercise 1 due	
3 Mon 9/29	Computational Photography	[ <a href="#">gutierrez12</a> ]
Wed 10/1	Texture Synthesis	[ <a href="#">efros99</a> ] [ <a href="#">efros01</a> ] [ <a href="#">wei09</a> ] [ <a href="#">hertzmann01</a> ] [ <a href="#">barnes09</a> ]
Sun 10/4	Programming Assignment 1 due	
4 Mon 10/6	Multiscale Images	[ <a href="#">debevec97</a> ] [ <a href="#">petschigg04</a> ] [ <a href="#">levin07</a> ]
Wed 10/8	Image Composition	[ <a href="#">kwatra03</a> ] [ <a href="#">perez03</a> ] [ <a href="#">agarwala04</a> ] [ <a href="#">hays07</a> ]
5 Mon 10/13	Point Sets	[ <a href="#">kobbelt04</a> ]
Wed 10/15	Point Set Rendering	[ <a href="#">pfister00</a> ] [ <a href="#">rusinkiewicz00</a> ]
Wed 10/15	Written Exercise 2 due	
6 Mon 10/20	Point Set Alignment	[ <a href="#">tam13</a> ] [ <a href="#">rusinkiewicz01</a> ]
Wed 10/21	Point Set Surface Reconstruction	[ <a href="#">hoppe92</a> ] [ <a href="#">kazhdan06</a> ]
Fri 10/23	Programming Assignment 2 due	
Fall break!		
7 Mon 11/3	Polygonal Meshes	[ <a href="#">botsch08</a> ] [ <a href="#">alliez08</a> ]
Wed 11/5	Laplacian Meshes	[ <a href="#">sorkine05</a> ]
8 Mon 11/10	Multiresolution Meshes	[ <a href="#">hoppe96</a> ] [ <a href="#">guskov99</a> ]
Wed 11/12	Spectral Meshes	[ <a href="#">levy09</a> ] [ <a href="#">zhang10</a> ]
Sun 11/16	Written Exercise 3 due	
9 Mon 11/17	Surface Analysis	[ <a href="#">mitra14</a> ]
Wed 11/19	Surface Segmentation	[ <a href="#">shamir08</a> ]
10 Mon 11/24	Symmetry Detection	[ <a href="#">mitra12</a> ]
Wed 11/26	Programming Assignment 3 due	
11 Mon 12/1	Surface Correspondence	[ <a href="#">hormann08</a> ] [ <a href="#">trankaick10</a> ]
Wed 12/3	Shape Collection Co-Analysis	
Wed 12/3	Final Project Proposal due	
12 Mon 12/8	Shape Collection Modeling	[ <a href="#">kim13</a> ]
Wed 12/10	Final Project Progress Talks	

# Coursework



3 Short written exercises

3 Programming assignments

Final project

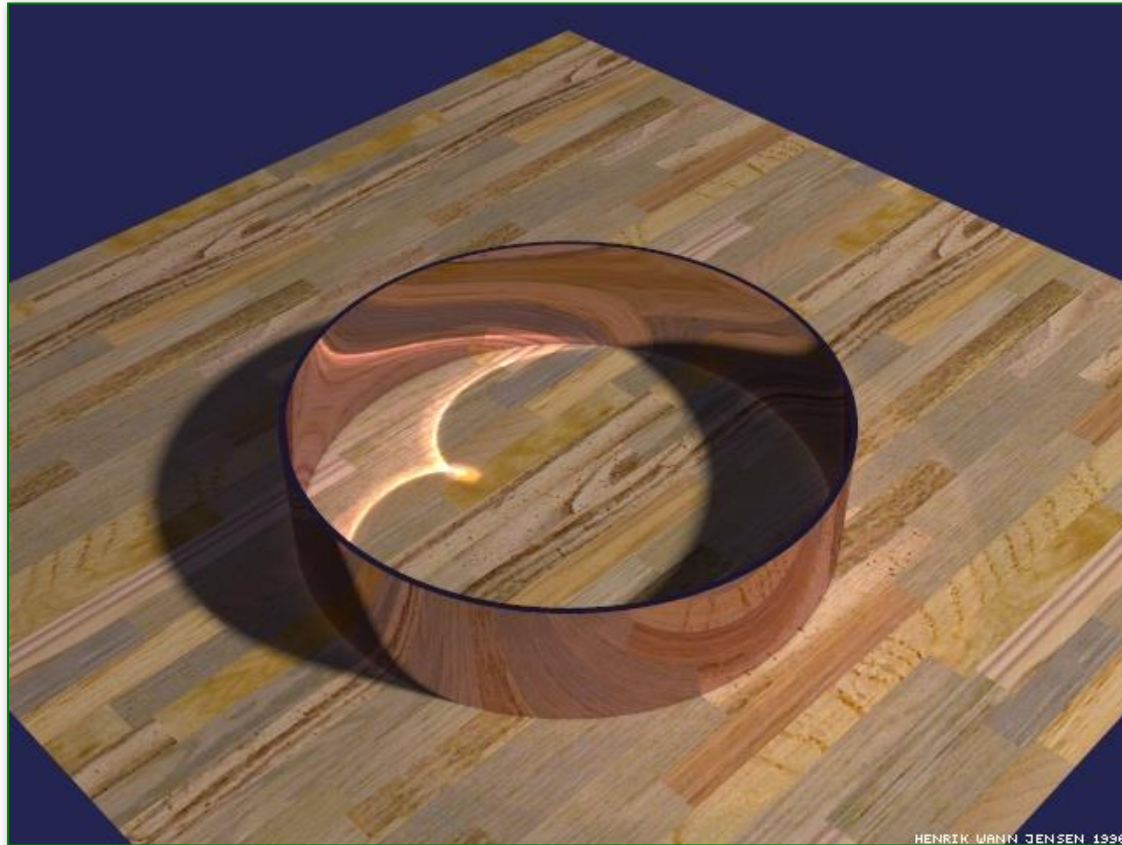


# Global Illumination

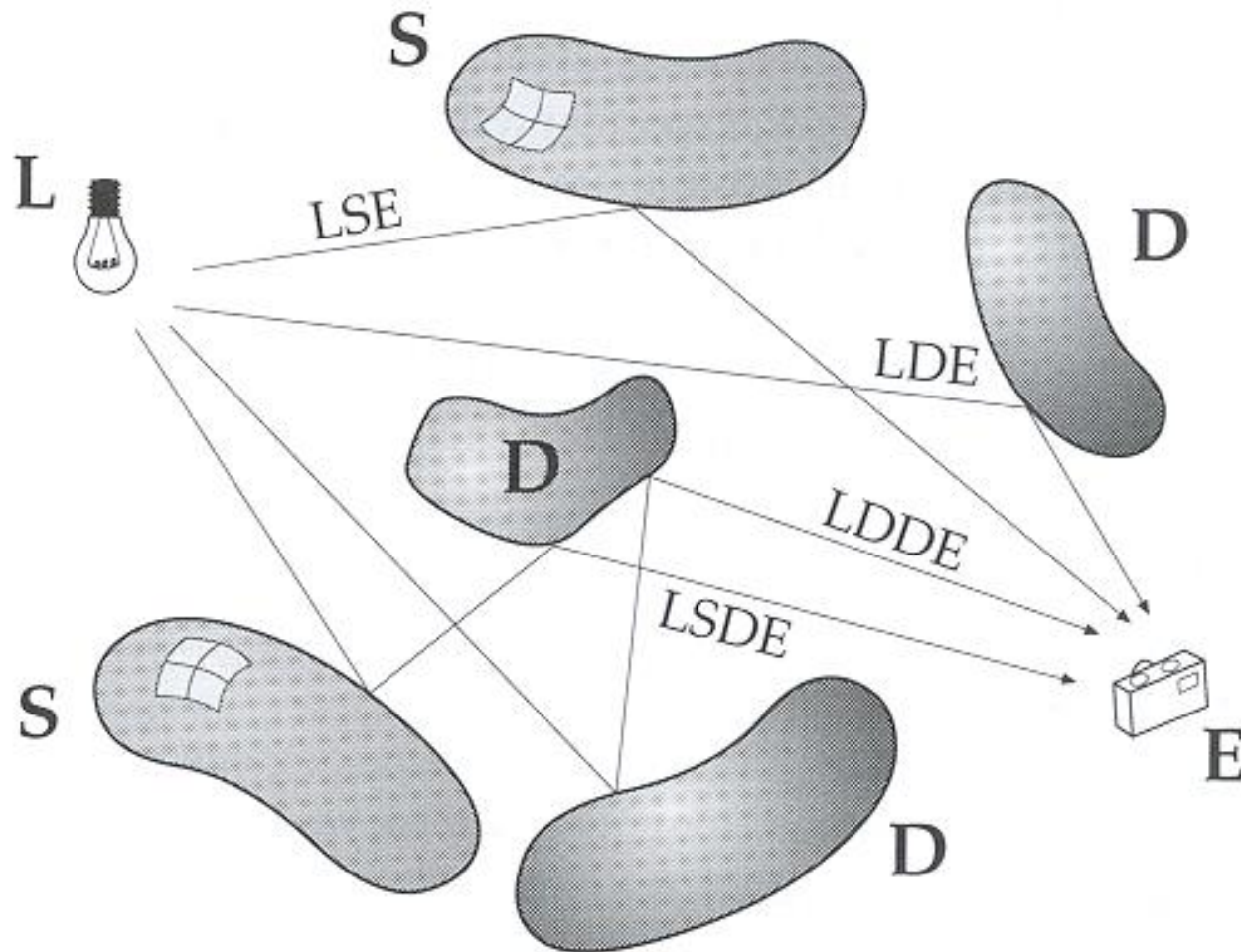
Tom Funkhouser  
Princeton University  
COS 526, Fall 2014

# Global Illumination

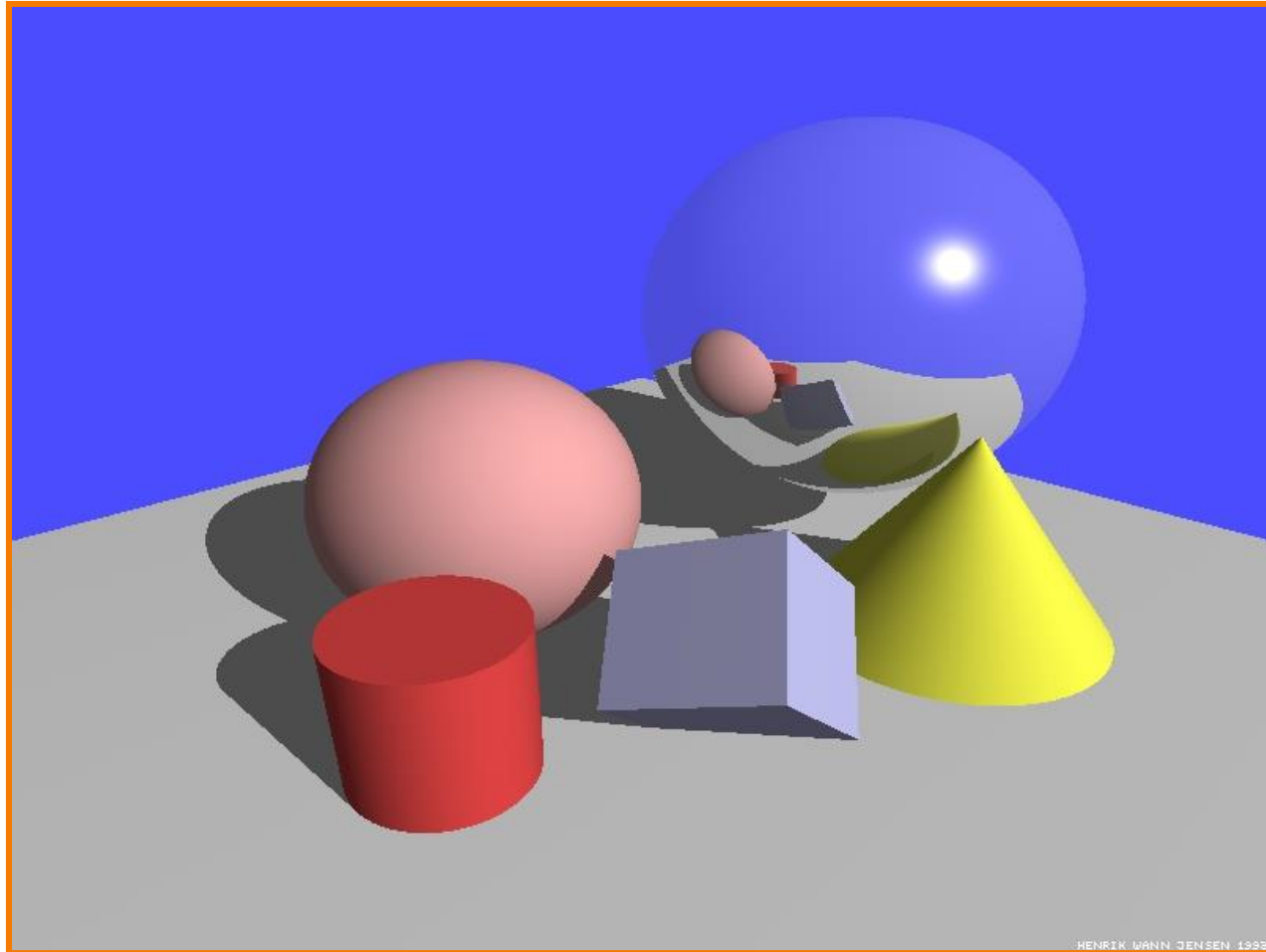
Synthesize image of a 3D scene accounting for all light transport (including indirect illumination)



# Path Types



# Path Types?



HENRIK WANN JENSEN 1998

# Path Types?





# Path Types?

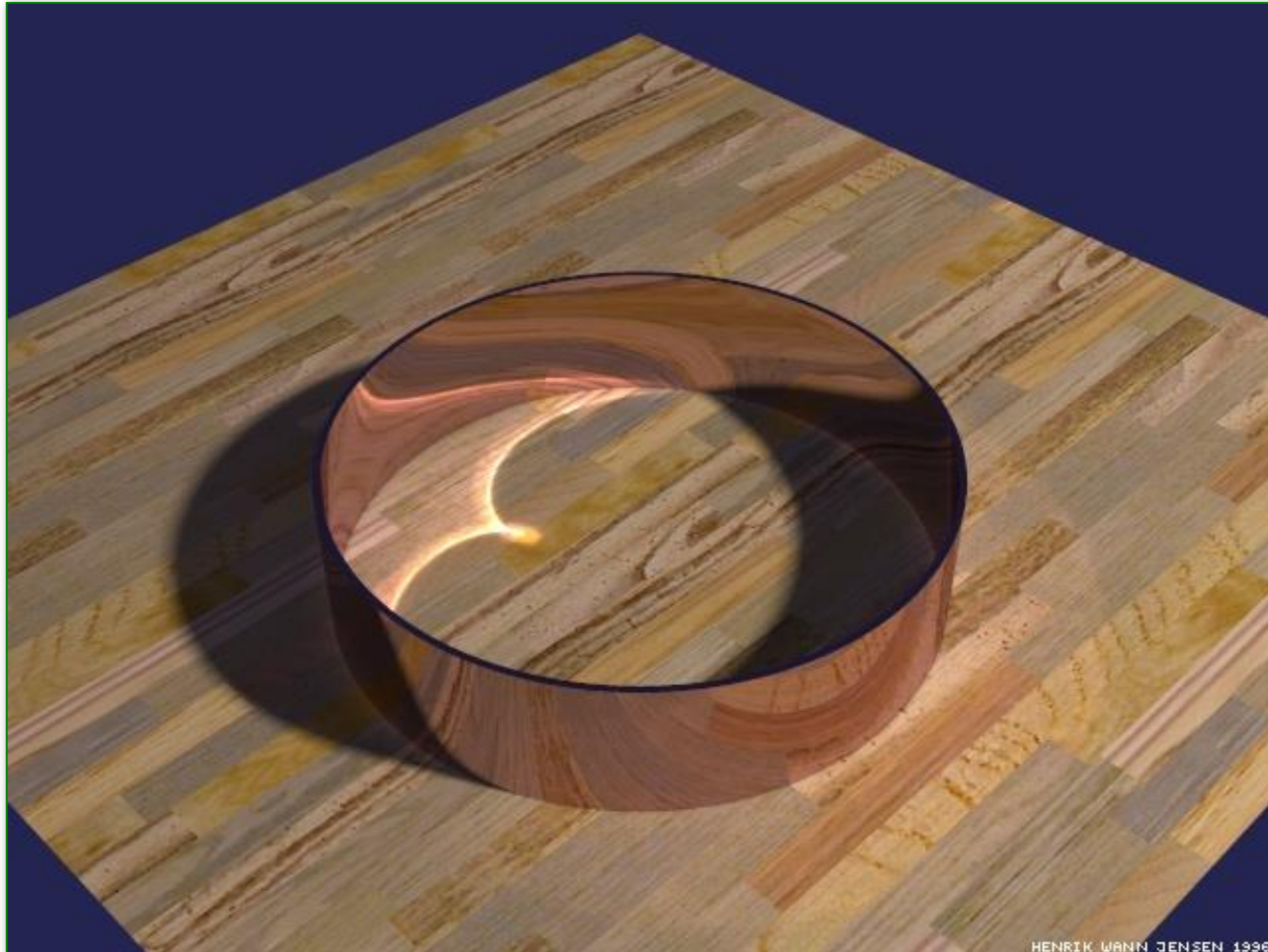


*Paul Debevec*

# Path Types?



# Path Types?



HENRIK WANN JENSEN 1996

*Henrik Wann Jensen*

# Path Types?



# Overview



## Rendering equation

- Rendering is integration

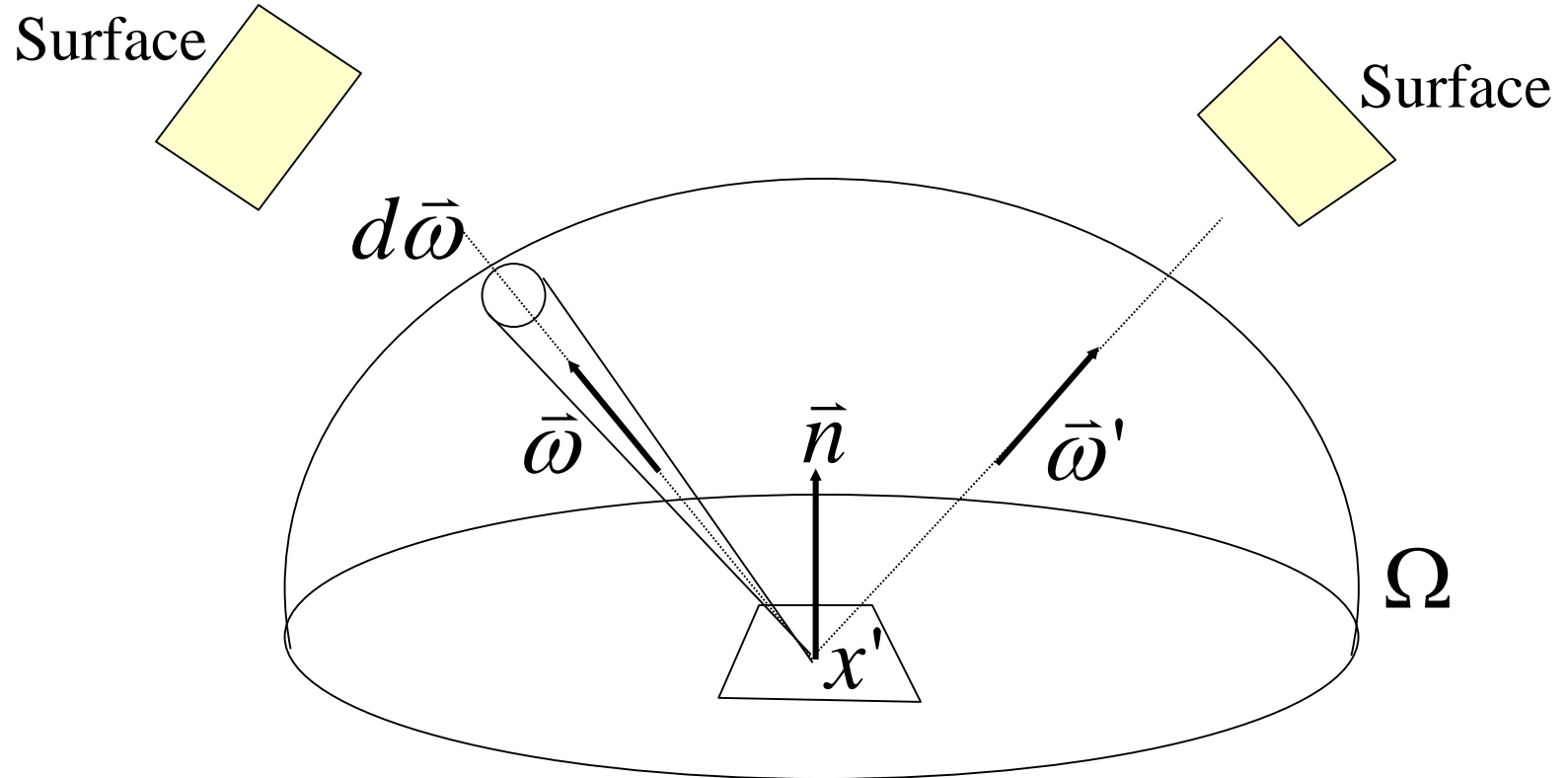
## Solution methods

- Direct illumination
- Recursive ray tracing
- Distribution ray tracing
- Path tracing
- Photon Mapping
- Radiosity
- etc.



# Rendering Equation

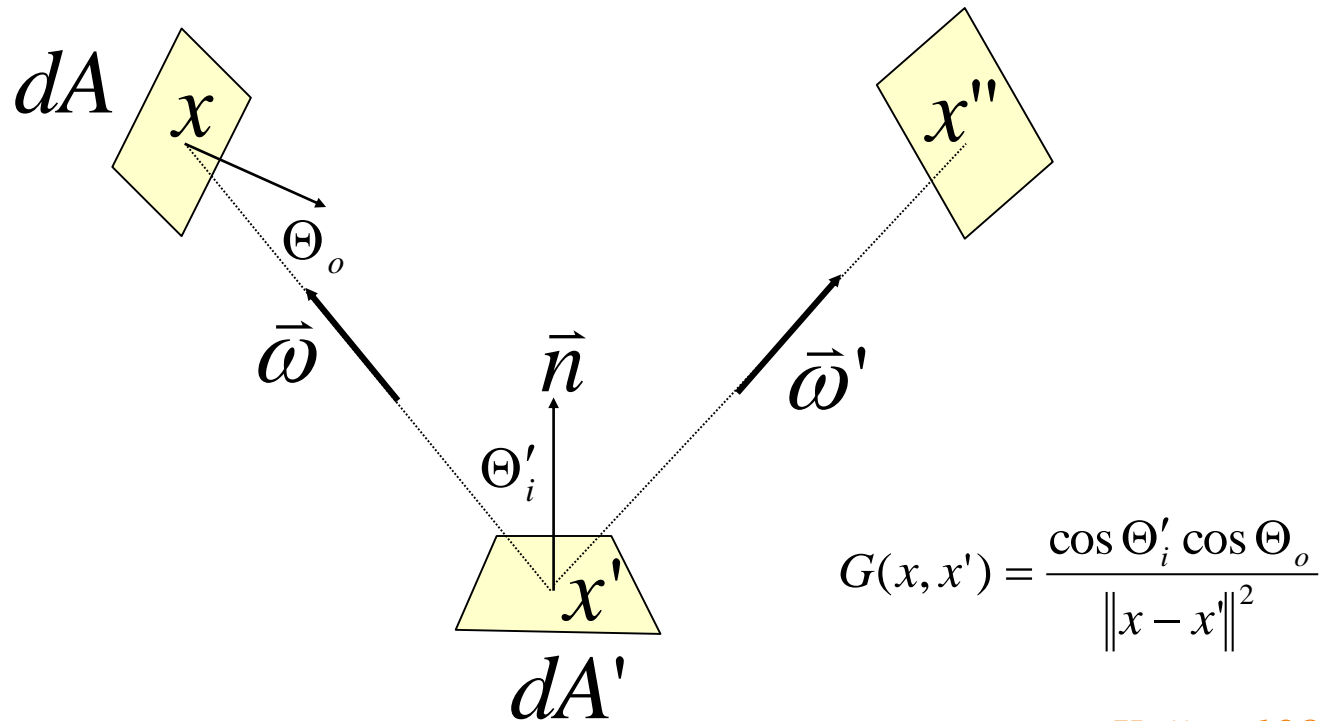
$$L_o(x', \bar{\omega}') = L_e(x', \bar{\omega}') + \int_{\Omega} f_r(x', \bar{\omega}, \bar{\omega}') L_i(x', \bar{\omega}) (\bar{\omega} \cdot \bar{n}) d\bar{\omega}$$



# Rendering Equation (2)



$$L(x' \rightarrow x'') = L_e(x' \rightarrow x'') + \int_S f_r(x \rightarrow x' \rightarrow x'') L(x \rightarrow x') V(x, x') G(x, x') dA$$



# Overview



## Rendering equation

- Rendering is integration

## ➤ Solution methods

- Direct illumination
- Recursive ray tracing
- Distribution ray tracing
- Path tracing
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- etc.



# Overview



## Rendering equation

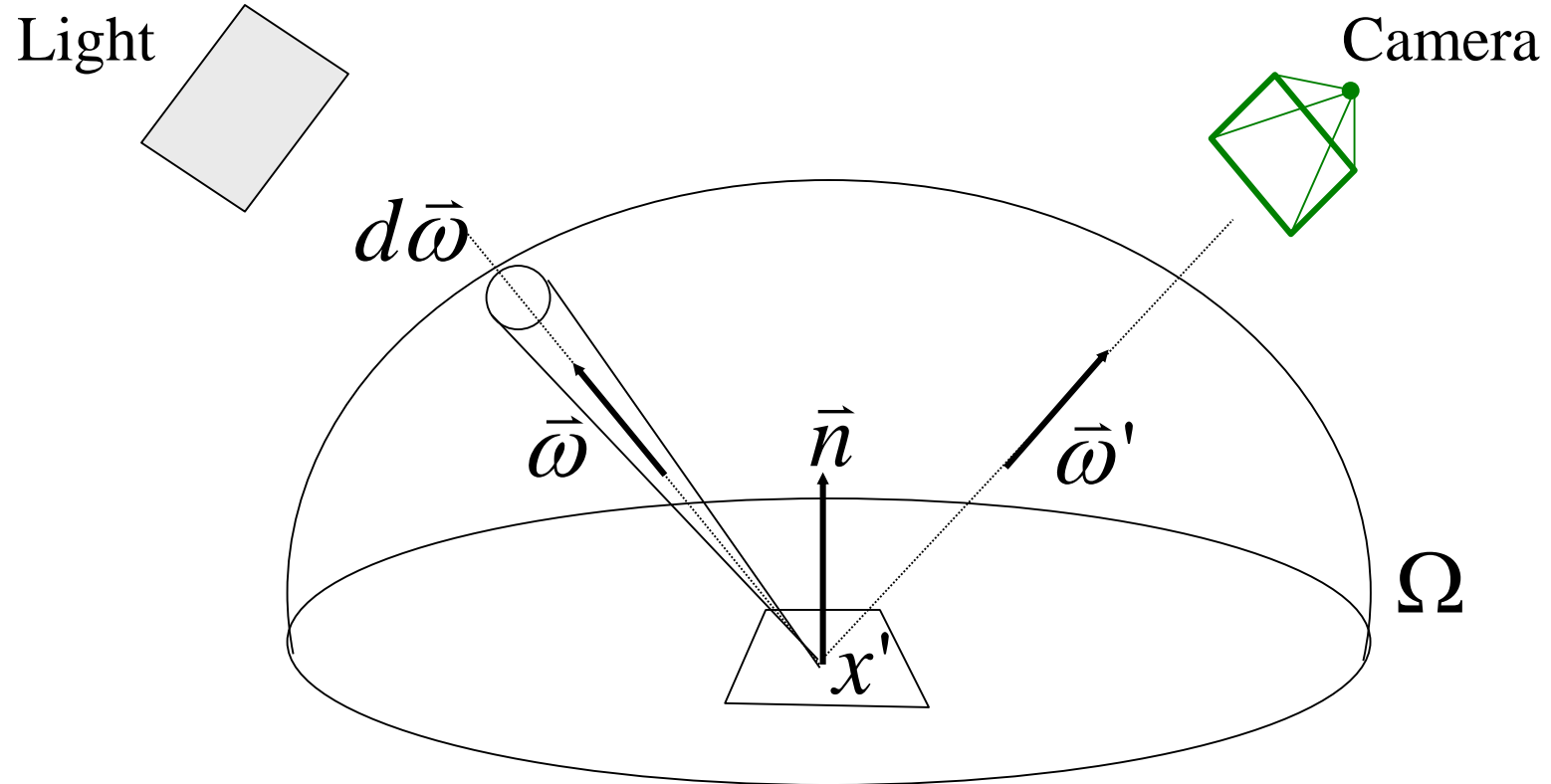
- Rendering is integration

## Solution methods

- **Direct illumination**
  - Recursive ray tracing
  - Distribution ray tracing
  - Path tracing
  - Photon Mapping
  - Radiosity
  - etc.

# Direct Illumination

$$L_o(x', \bar{\omega}') = L_e(x', \bar{\omega}') + \int_{\Omega_L} f_r(x', \bar{\omega}, \bar{\omega}') L_i(x', \bar{\omega}) (\bar{\omega} \cdot \bar{n}) d\bar{\omega}$$

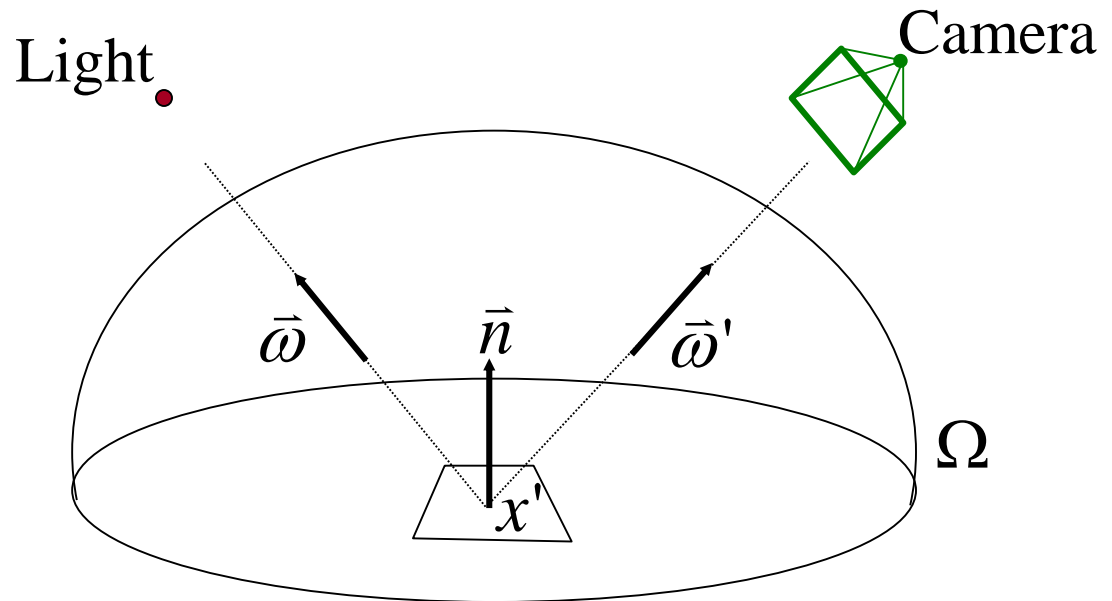


# OpenGL



$$L_o(x', \bar{\omega}') = L_e(x', \bar{\omega}') + \int_{\Omega} f_r(x', \bar{\omega}, \bar{\omega}') L_i(x', \bar{\omega}) (\bar{\omega} \cdot \bar{n}) d\bar{\omega}$$

Assume  
direct illumination  
from point lights  
and ignore visibility



$$L_o(x', \bar{\omega}') = L_e(x', \bar{\omega}') + \sum_{i=1}^{nlights} f_r(x', \bar{\omega}, \bar{\omega}') L_i(x', \bar{\omega}) (\bar{\omega} \cdot \bar{n})$$

# Overview



## Rendering equation

- Rendering is integration

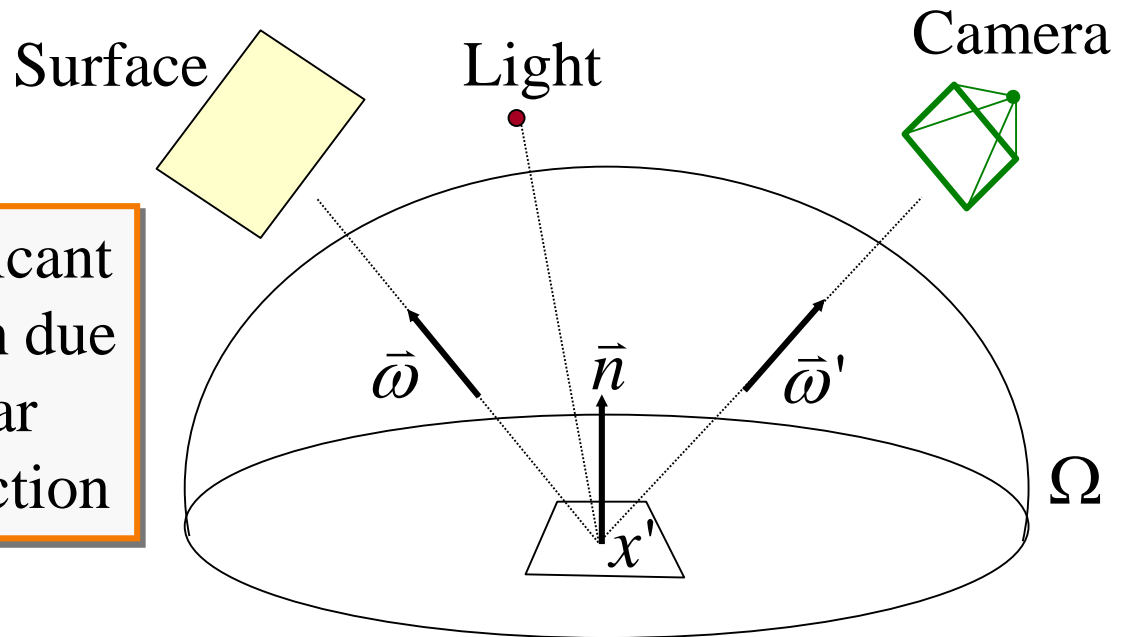
## Solution methods

- Direct illumination
- **Recursive ray tracing**
- Distribution ray tracing
- Path tracing
- Photon Mapping
- Radiosity
- etc.

# Recursive Ray Tracing

$$L_o(x', \bar{\omega}') = L_e(x', \bar{\omega}') + \int_{\Omega} f_r(x', \bar{\omega}, \bar{\omega}') L_i(x', \bar{\omega}) (\bar{\omega} \cdot \bar{n}) d\bar{\omega}$$

Assume only significant indirect illumination due to perfect specular reflection and refraction



$$L_o(x', \bar{\omega}') = L_e(x', \bar{\omega}') + \sum_{i=1}^{nlights} f_r(x', \bar{\omega}, \bar{\omega}') L_i(x', \bar{\omega}) (\bar{\omega} \cdot \bar{n}) + specular$$

# Overview



## Rendering equation

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## Solution methods

- Direct illumination
- Recursive ray tracing
- **Distribution ray tracing**
- Path tracing
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- Radiosity
- etc.

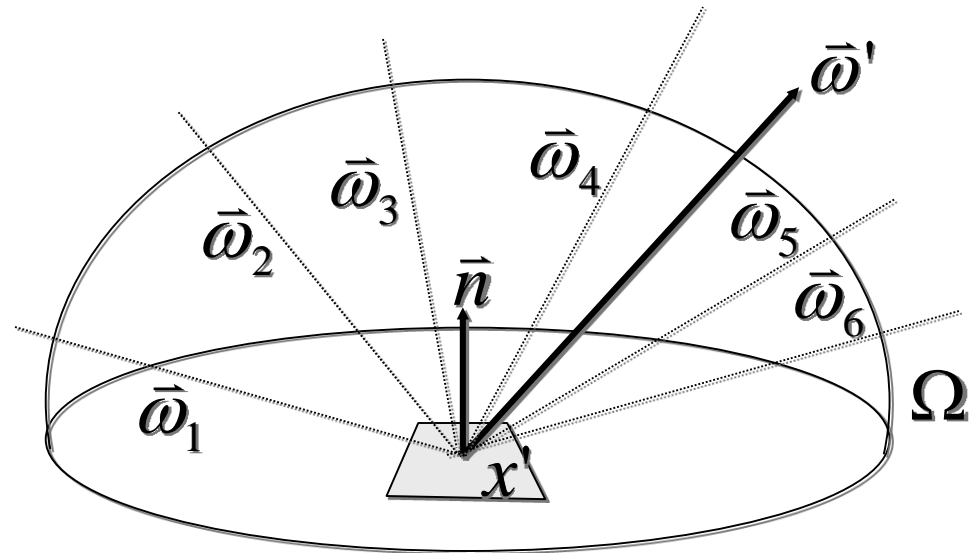
# Distribution Ray Tracing

$$L_o(x', \bar{\omega}') = L_e(x', \bar{\omega}') + \int_{\Omega} f_r(x', \bar{\omega}, \bar{\omega}') L_i(x', \bar{\omega}) (\bar{\omega} \cdot \bar{n}) d\bar{\omega}$$

Estimate integral  
for each reflection  
by random sampling

Also:

- Depth of field
- Motion blur
- etc.



# Overview



## Rendering equation

- Rendering is integration

## Solution methods

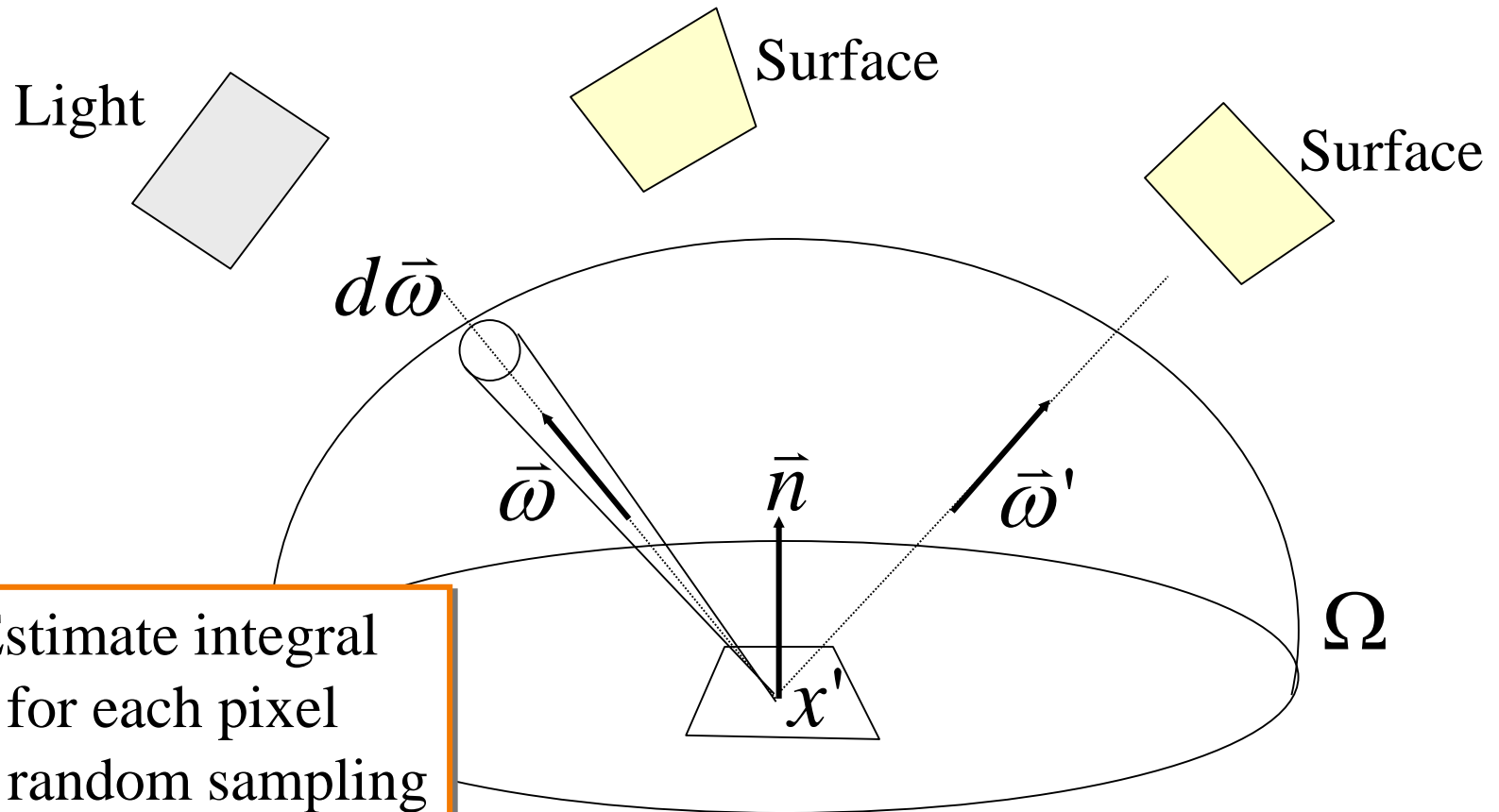
- Direct illumination
- Recursive ray tracing
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- etc.





# Path Tracing

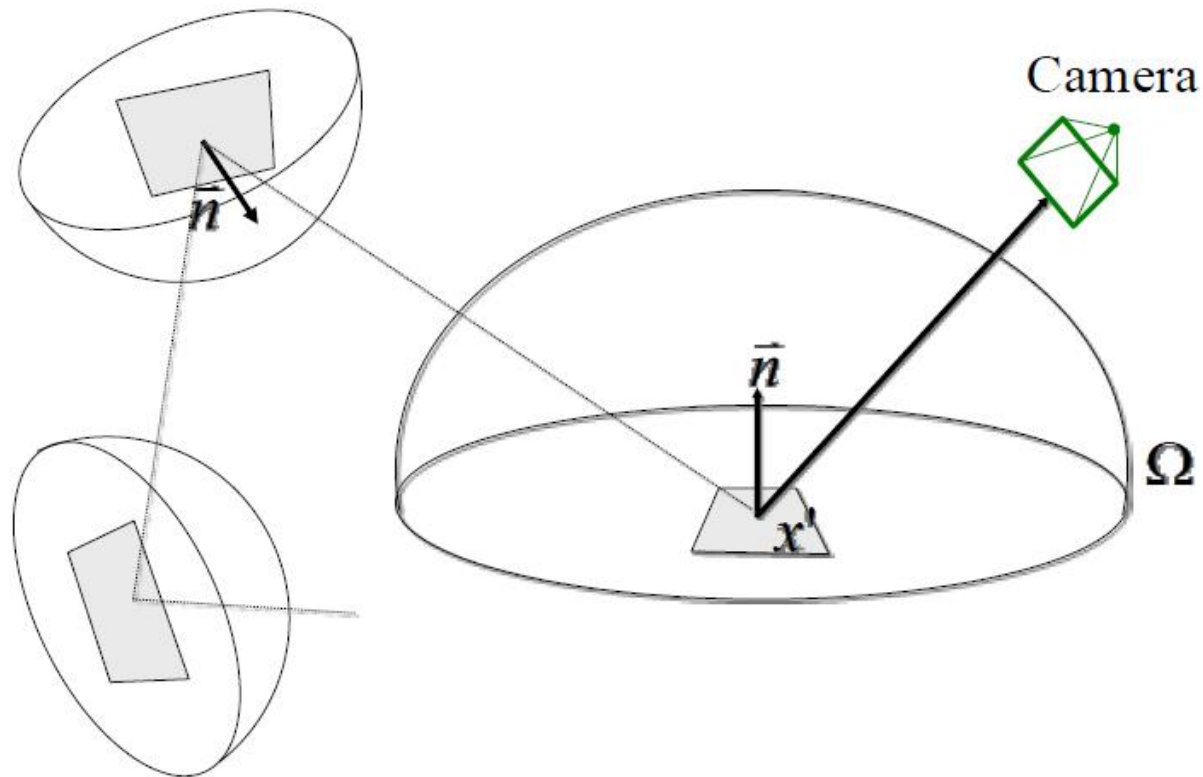
$$L_o(x', \bar{\omega}') = L_e(x', \bar{\omega}') + \int_{\Omega} f_r(x', \bar{\omega}, \bar{\omega}') L_i(x', \bar{\omega}) (\bar{\omega} \cdot \bar{n}) d\bar{\omega}$$



# Path Tracing



Estimate integral for each pixel by sampling paths from the camera



# Overview



## Rendering equation

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- Radiosity
- etc.

# Photon Mapping



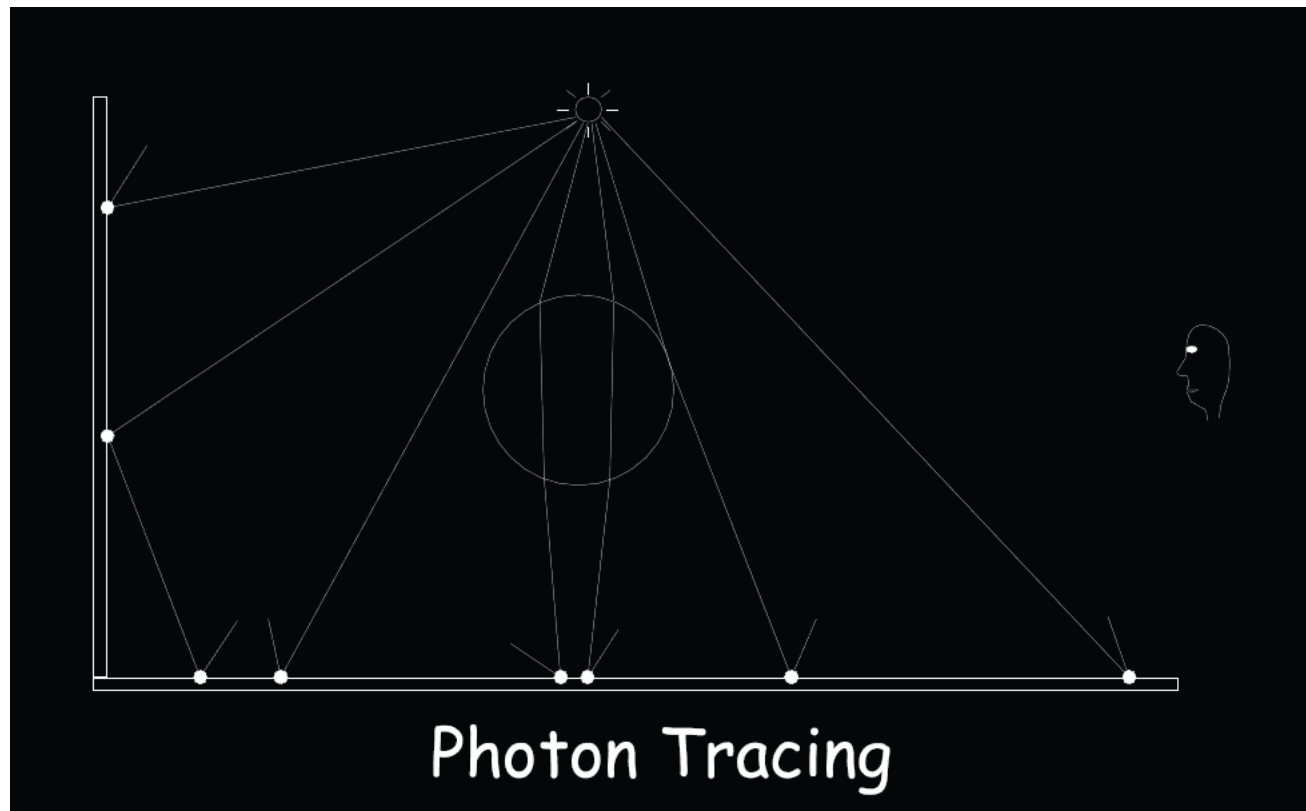
Two pass method:

1. Build photon map by tracing paths from lights
2. Render image by tracing paths from camera

# Photon Mapping

Two pass method:

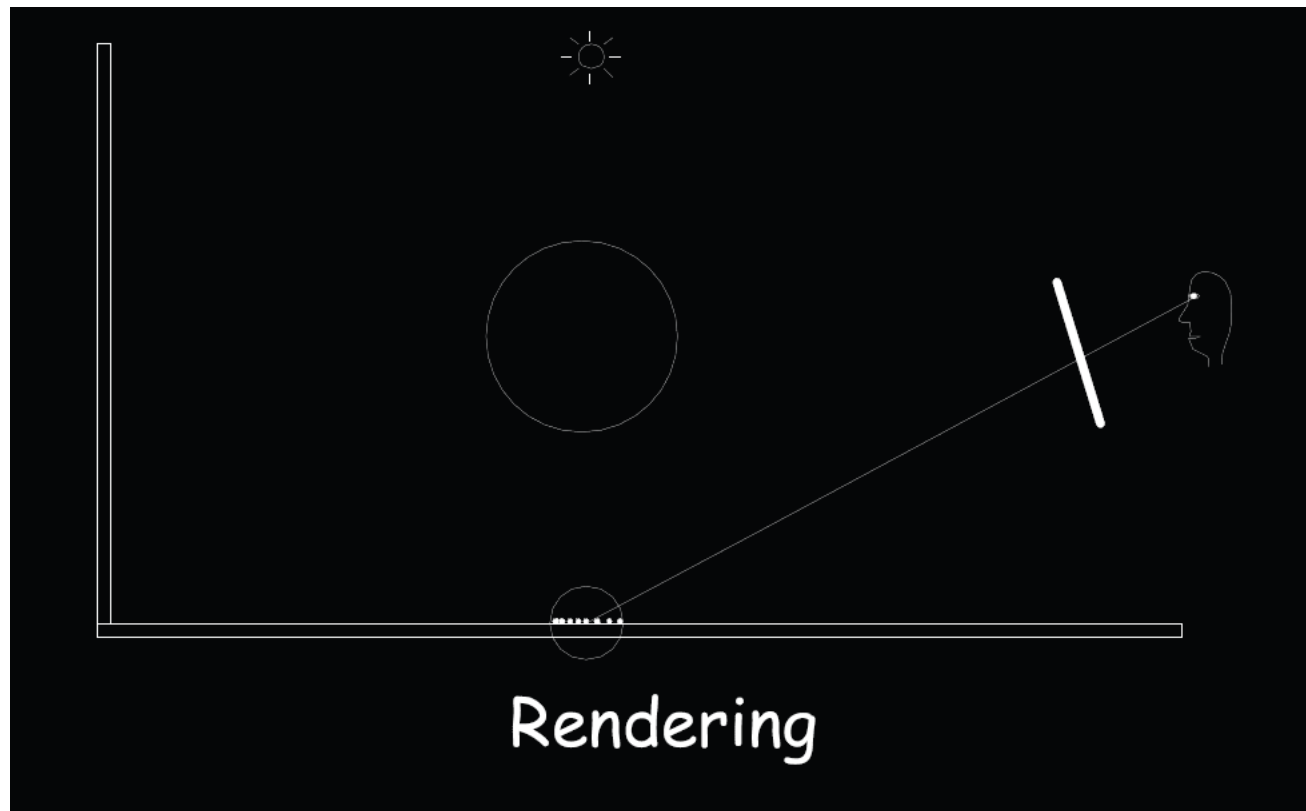
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# Photon Mapping

Two pass method:

1. Build photon map by tracing paths from lights
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- etc.

# Radiosity



Discretize surfaces into small patches



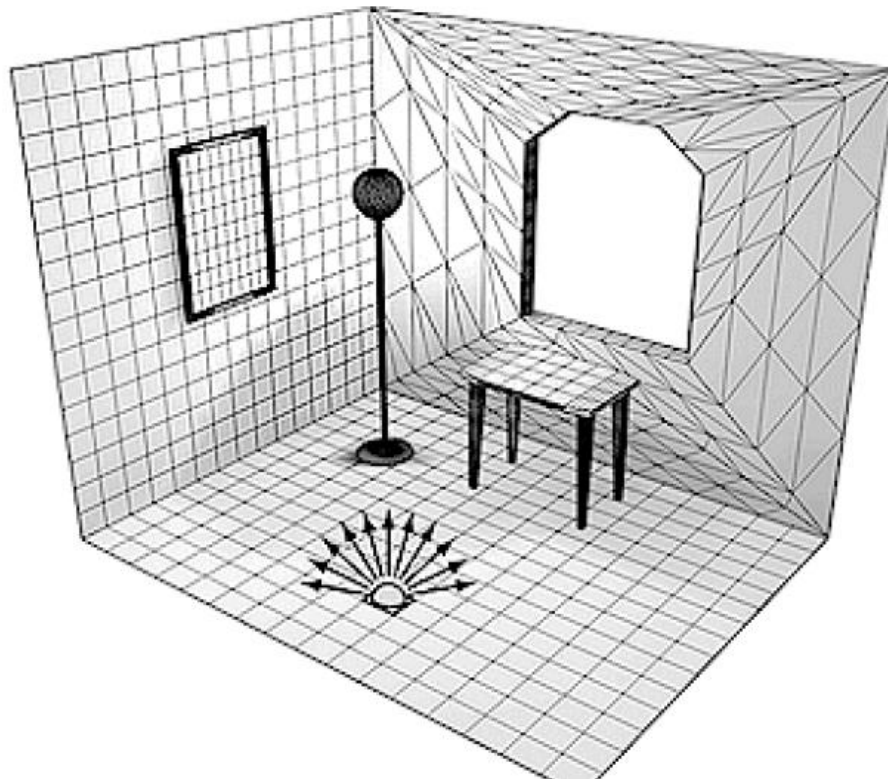
Baum



# Radiosity



Assume simple function (constant) is good approximation for radiosity (sum of all energy leaving a point) within a patch





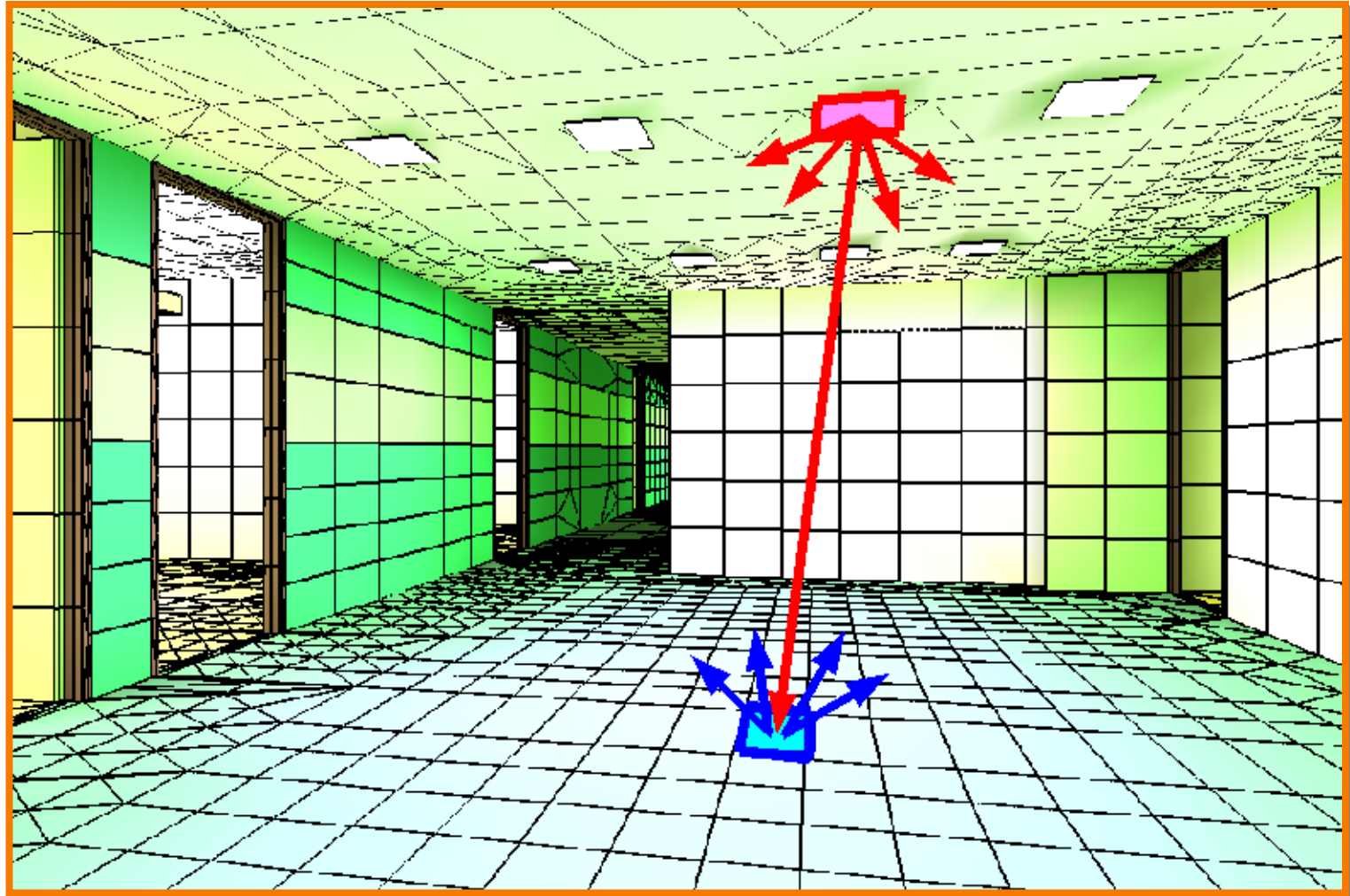
# Radiosity

Leads to sparse linear system of equations

$$B_i A_i = E_i A_i + \rho_i \sum_{j=1}^N F_{ji} B_j A_j$$

$$\begin{bmatrix} 1 - \rho_1 F_{1,1} & \cdot & \cdot & \cdot & -\rho_1 F_{1,n} \\ -\rho_2 F_{2,1} & 1 - \rho_2 F_{2,2} & \cdot & \cdot & -\rho_2 F_{2,n} \\ \cdot & \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot \\ -\rho_{n-1} F_{n-1,1} & \cdot & \cdot & \cdot & -\rho_{n-1} F_{n-1,n} \\ -\rho_n F_{n,1} & \cdot & \cdot & \cdot & 1 - \rho_n F_{n,n} \end{bmatrix} \begin{bmatrix} B_1 \\ B_2 \\ \cdot \\ \cdot \\ \cdot \\ B_n \end{bmatrix} = \begin{bmatrix} E_1 \\ E_2 \\ \cdot \\ \cdot \\ \cdot \\ E_n \end{bmatrix}$$

# Radiosity



# Overview



## Rendering equation

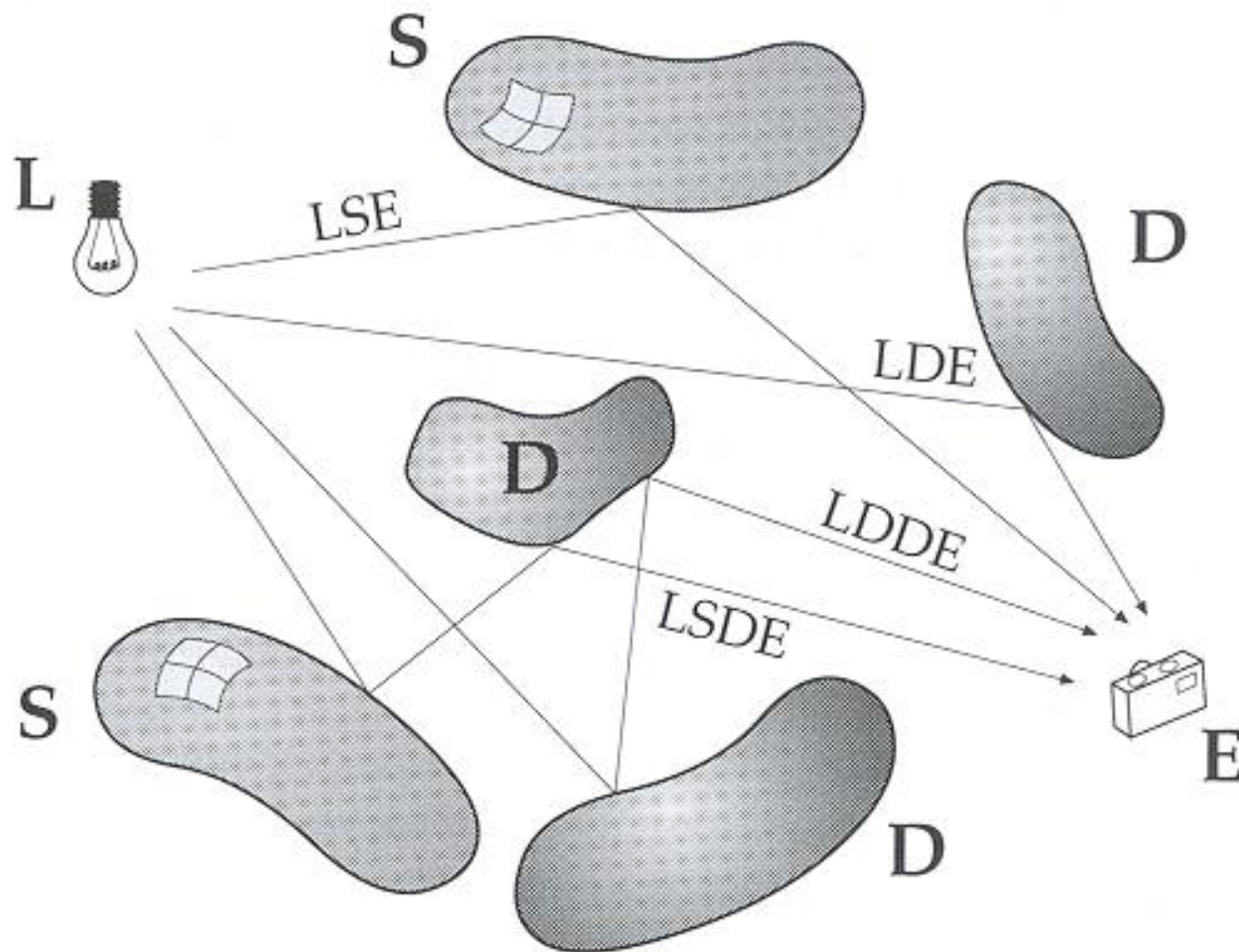
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## Solution methods

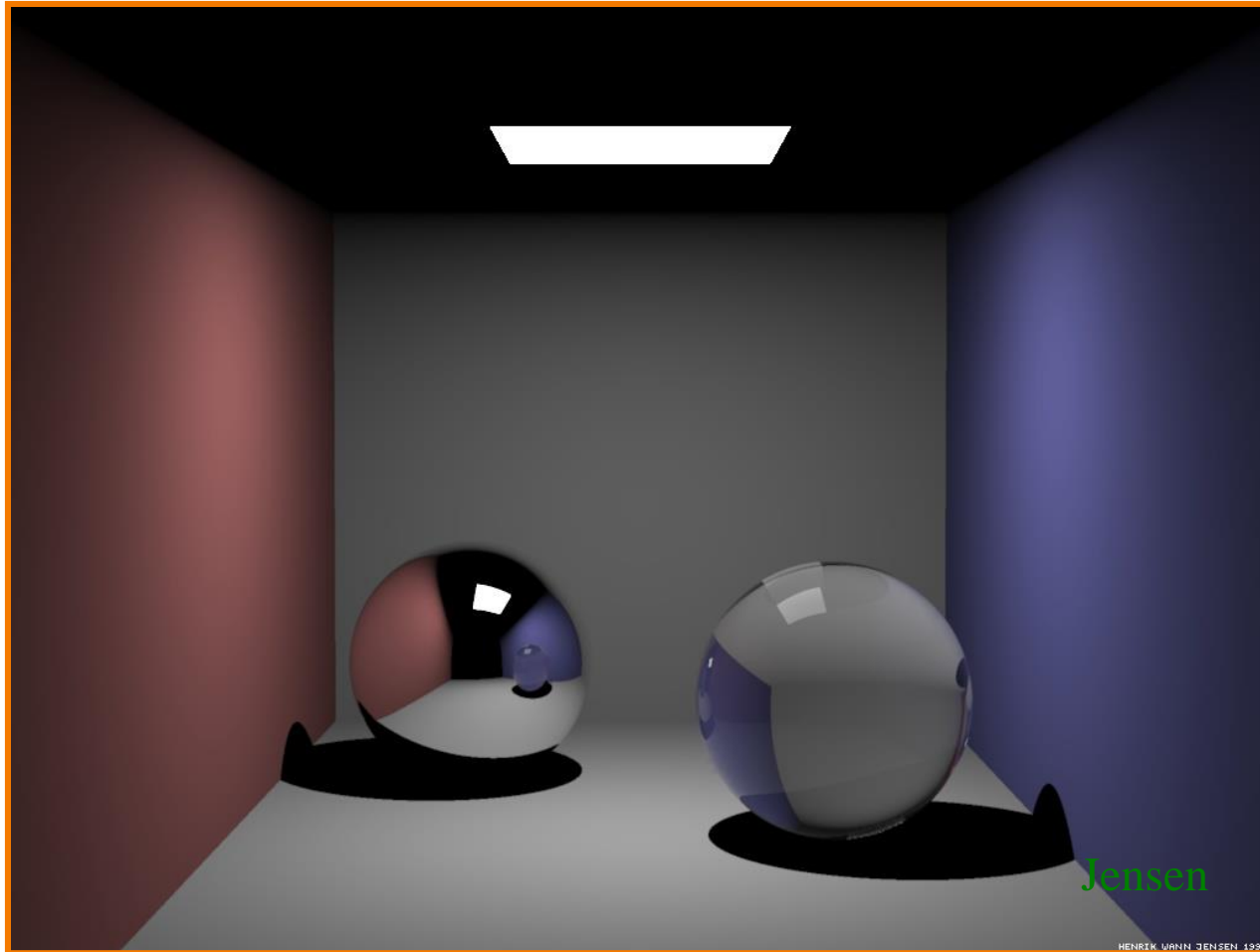
- Direct illumination
- Recursive ray tracing
- Distribution ray tracing
- Path tracing
- Photon Mapping
- Radiosity
- etc.

Which method is best?

# Path Types



# Path Types



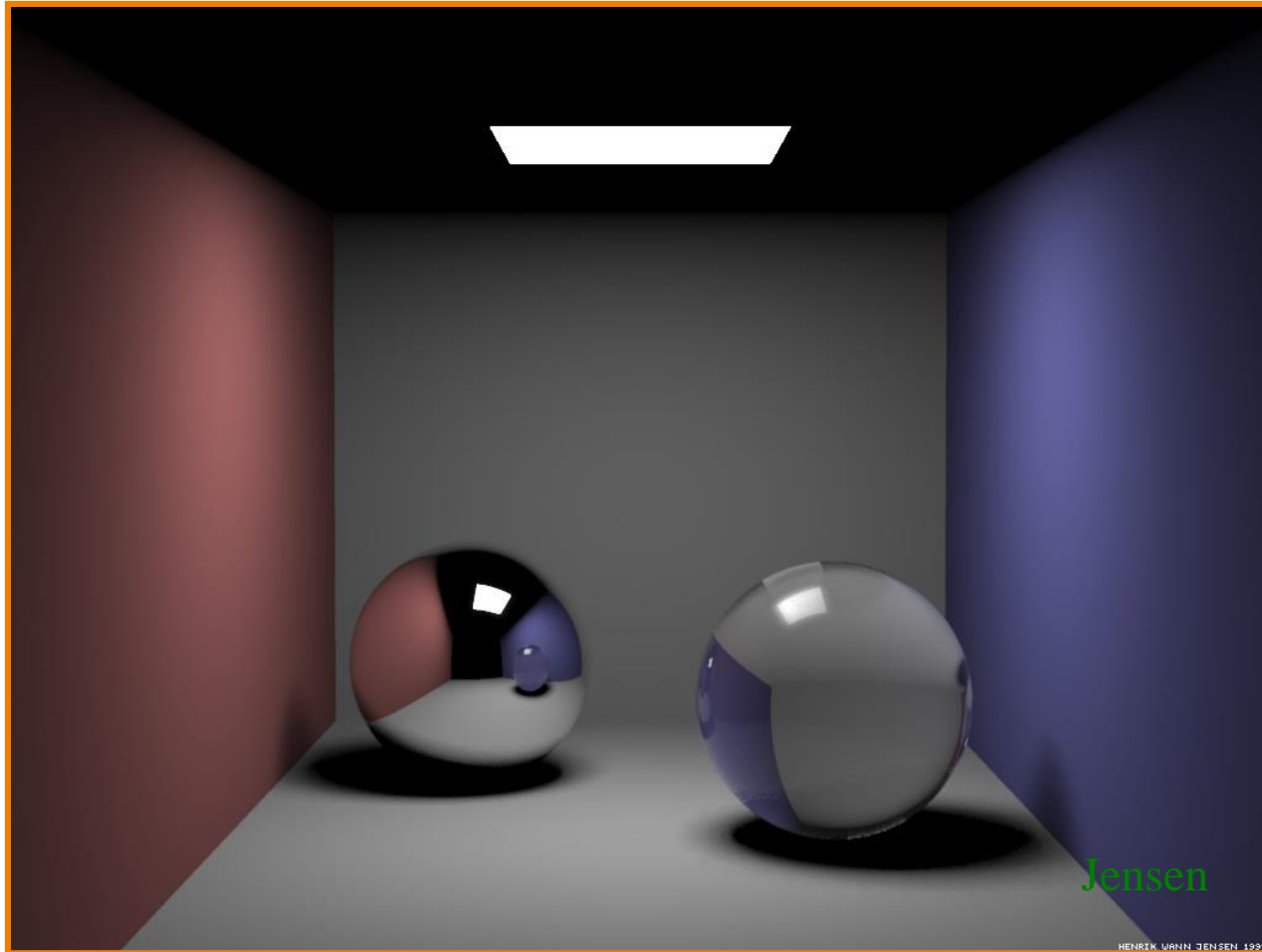
Ray tracing

HENRIK WANN JENSEN 1999

Jensen

*Henrik Wann Jensen*

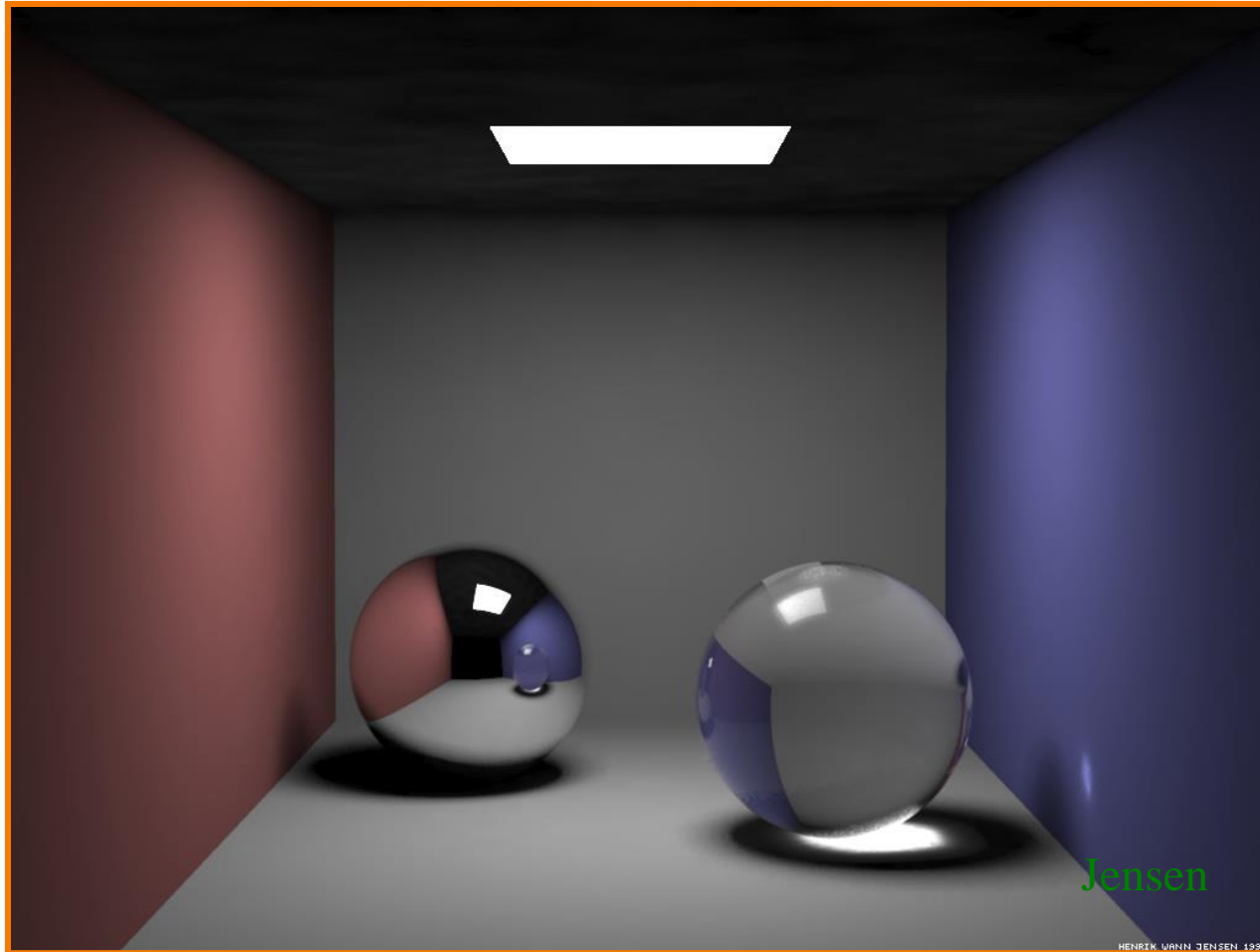
# Path Types



+ soft shadows

*Henrik Wann Jensen*

# Path Types

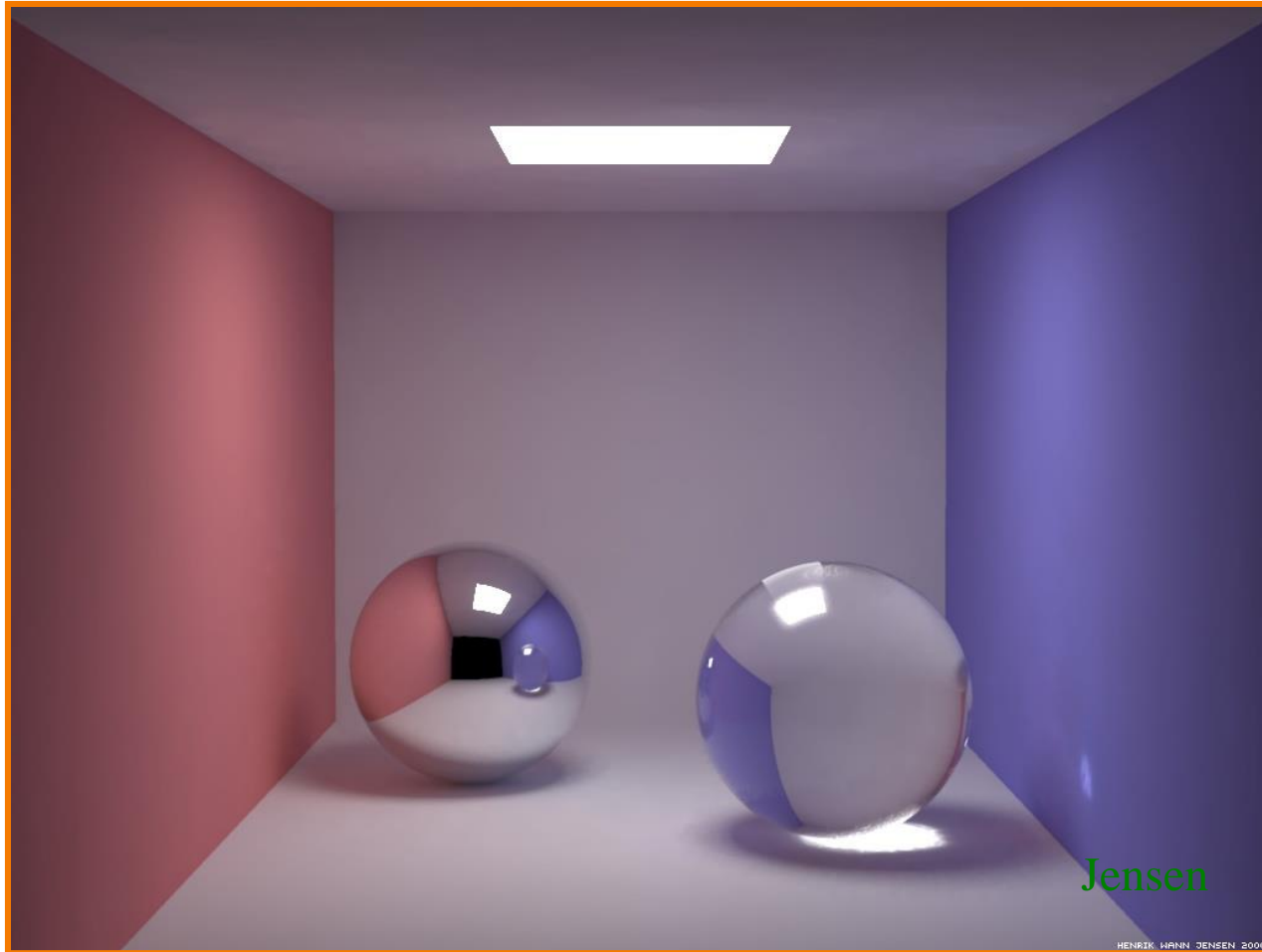


+ caustics

*Henrik Wann Jensen*



# Path Types



+ indirect diffuse illumination

*Henrik Wann Jensen*

# Summary



## Rendering equation

- Rendering is integration

Different solution methods are best for different types of scenes (depending on path types)

- Direct illumination - LDE
- Recursive ray tracing -  $LDS^*E$
- Distribution ray tracing –  $L(SD)^*E$
- Path tracing–  $L(SD)^*E$
- Photon Mapping–  $L(SD)^*E$  (biased)
- Radiosity –  $LD^*E$
- etc.