Perl RE for valid RFC822 email addresses.

```
(?:(?:\r\n)?[ \t])*(?:(?:(?:[^()<>@,;:\\".\[\] \000-\031]+(?:(?:(?:\r\n)?[ \t])+|\Z|(?=[\["()<>@,;:\\".\[\]]))|"(?:[^\"\r\\]|\\.|(?:(?:\r\n)?[ \t]))*"(?:(?:
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```

http://www.ex-parrot.com/~pdw/Mail-RFC822-Address.html

http://algs4.cs.princeton.edu

5.4 REGULAR EXPRESSIONS

- *regular expressions*
- *NFAs and NFA simulation*
- *NFA construction*
- *applications and context*

http://algs4.cs.princeton.edu

5.4 Regular Expressions

- *regular expressions*
- *NFAs and NFA simulation*
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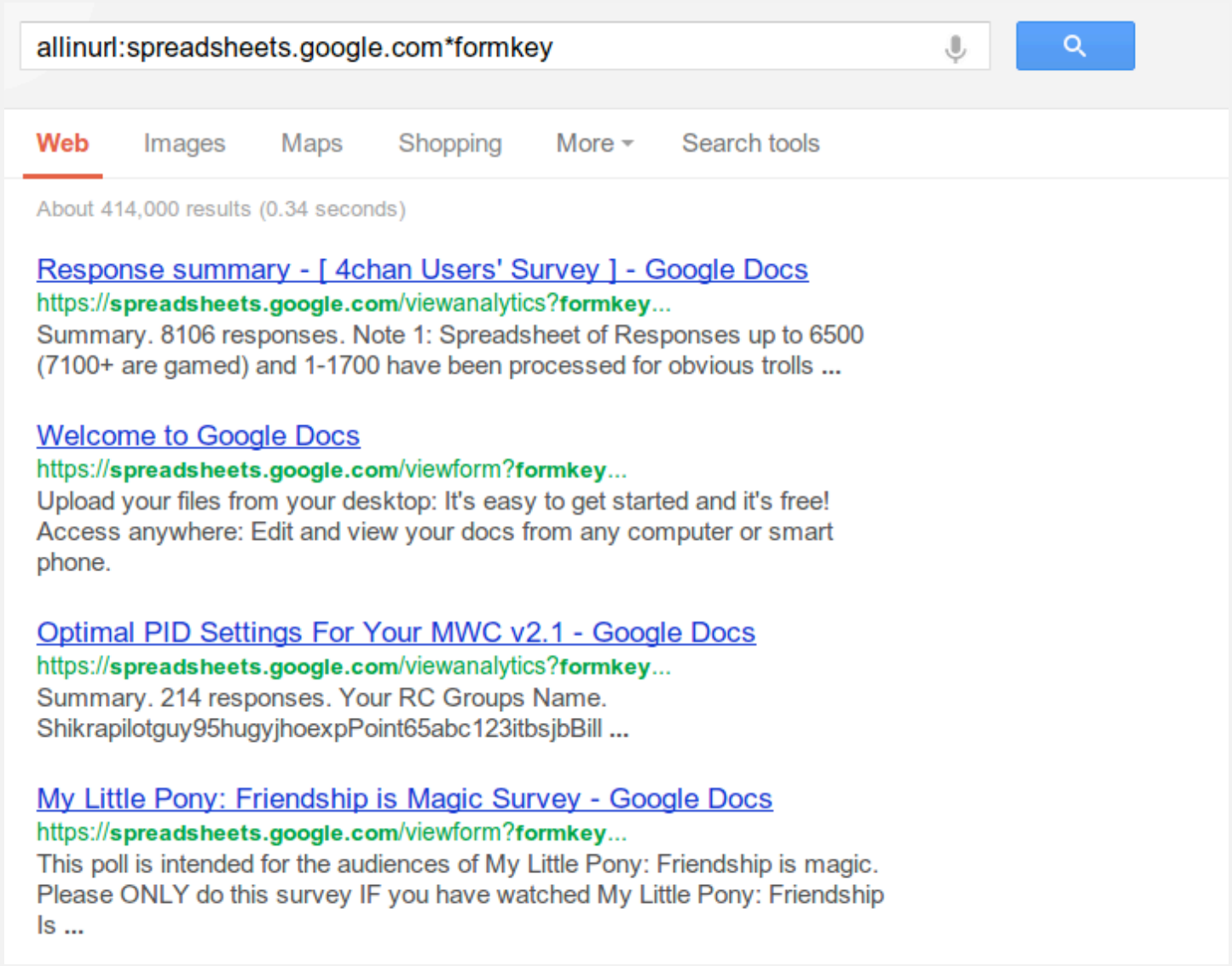

allinurl:spreadsheets.google.com*formkey
Web
Images
Maps
Shopping
More
Search tools
About 414,000 results (0.34 seconds)
Response summary - [4chan Users' Survey] - Google Docs
https://spreadsheets.google.com/viewanalytics?formkey...
Summary. 8106 responses. Note 1: Spreadsheet of Responses up to 6500 (7100+ are gamed) and 1-1700 have been processed for obvious trolls ...
Welcome to Google Docs
https://spreadsheets.google.com/viewform?formkey...
Upload your files from your desktop: It's easy to get started and it's free! Access anywhere: Edit and view your docs from any computer or smart phone.
Optimal PID Settings For Your MWC v2.1 - Google Docs
https://spreadsheets.google.com/viewanalytics?formkey...
Summary. 214 responses. Your RC Groups Name. Shikrapilotguy95hugyjhoexpPoint65abc123itbsjbBill ...
My Little Pony: Friendship is Magic Survey - Google Docs
https://spreadsheets.google.com/viewform?formkey...
This poll is intended for the audiences of My Little Pony: Friendship is magic. Please ONLY do this survey IF you have watched My Little Pony: Friendship Is ...

My Little Pony: Friendship is Magic Survey

This poll is intended for the audiences of My Little Pony: Friendship is magic.

Please ONLY do this survey IF you have watched My Little Pony: Friendship Is Magic And Please do not submit multiple surveys. Thank you

**Survey result can be found here
https://spreadsheets.google.com/viewanalytics?hl=en&formkey=dDB5dy0yTjhlMnlKdEsxRGFzWTNLUlE6MQ
* Required

What is your sex? *

- Male
- Female

What is your age (range)? *

- 5 - 11
- 12 - 14
- 15 - 17
- 18 - 24
- 25 - 30
- 31 - 40
- 41- 50
- 51 - 60
- 60 or above

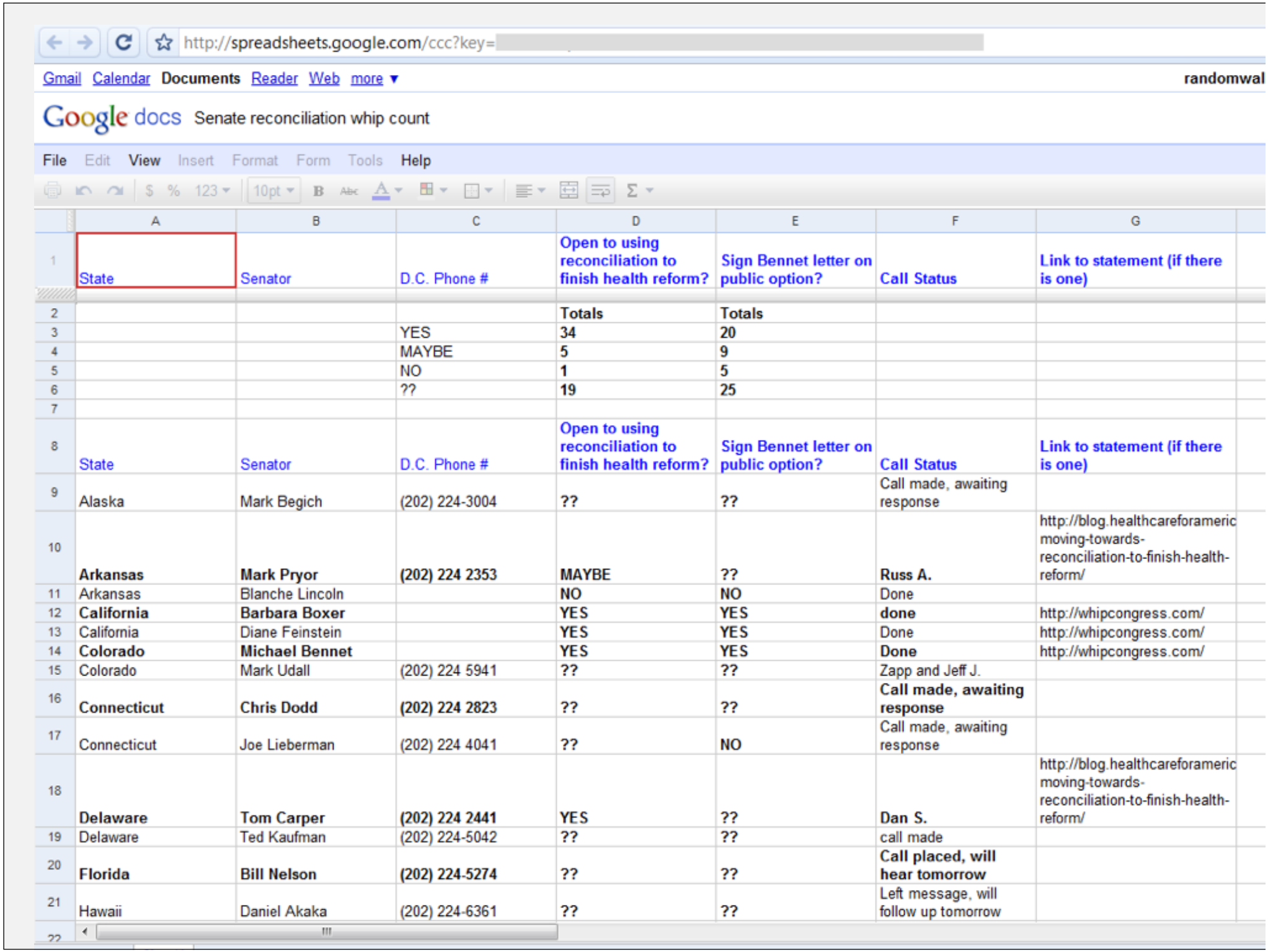
What is your exact age? (optional)

Who is your Favorite Character *

- Twilight Sparkle
- Pinkie Pie
- Fluttershy
- Applejack
- Rainbow Dash
- Rarity
- Princess Celestia
- Derpy Hooves
- Spike
- None of the above/ others
- Luna

Who is your Second Favorite Character *

- Twilight Sparkle
- Pinkie Pie
- Fluttershy



http://spreadsheets.google.com/ccc?key=

Gmail Calendar **Documents** Reader Web more ▼ **randomwal**

Google docs Senate reconciliation whip count

File Edit View Insert Format Form Tools Help

	A	B	C	D	E	F	G
1	State	Senator	D.C. Phone #	Open to using reconciliation to finish health reform?	Sign Bennet letter on public option?	Call Status	Link to statement (if there is one)
2				**Totals**	**Totals**		
3			YES	**34**	**20**		
4			MAYBE	**5**	**9**		
5			NO	**1**	**5**		
6			??	**19**	**25**		
7							
8	State	Senator	D.C. Phone #	Open to using reconciliation to finish health reform?	Sign Bennet letter on public option?	Call Status	Link to statement (if there is one)
9	Alaska	Mark Begich	(202) 224-3004	??	??	Call made, awaiting response	
10	**Arkansas**	**Mark Pryor**	**(202) 224 2353**	**MAYBE**	**??**	**Russ A.**	http://blog.healthcareforamericmoving-towards-reconciliation-to-finish-health-reform/
11	Arkansas	Blanche Lincoln		NO	NO	Done	
12	**California**	**Barbara Boxer**		**YES**	**YES**	**done**	http://whipcongress.com/
13	California	Diane Feinstein		YES	YES	Done	http://whipcongress.com/
14	**Colorado**	**Michael Bennet**		**YES**	**YES**	**Done**	http://whipcongress.com/
15	Colorado	Mark Udall	(202) 224 5941	??	??	Zapp and Jeff J.	
16	**Connecticut**	**Chris Dodd**	**(202) 224 2823**	??	??	**Call made, awaiting response**	
17	Connecticut	Joe Lieberman	(202) 224 4041	??	NO	Call made, awaiting response	
18	**Delaware**	**Tom Carper**	**(202) 224 2441**	**YES**	**??**	**Dan S.**	http://blog.healthcareforamericmoving-towards-reconciliation-to-finish-health-reform/
19	Delaware	Ted Kaufman	(202) 224-5042	??	??	call made	
20	**Florida**	**Bill Nelson**	**(202) 224-5274**	??	??	**Call placed, will hear tomorrow**	
21	Hawaii	Daniel Akaka	(202) 224-6361	??	??	Left message, will follow up tomorrow	
22							

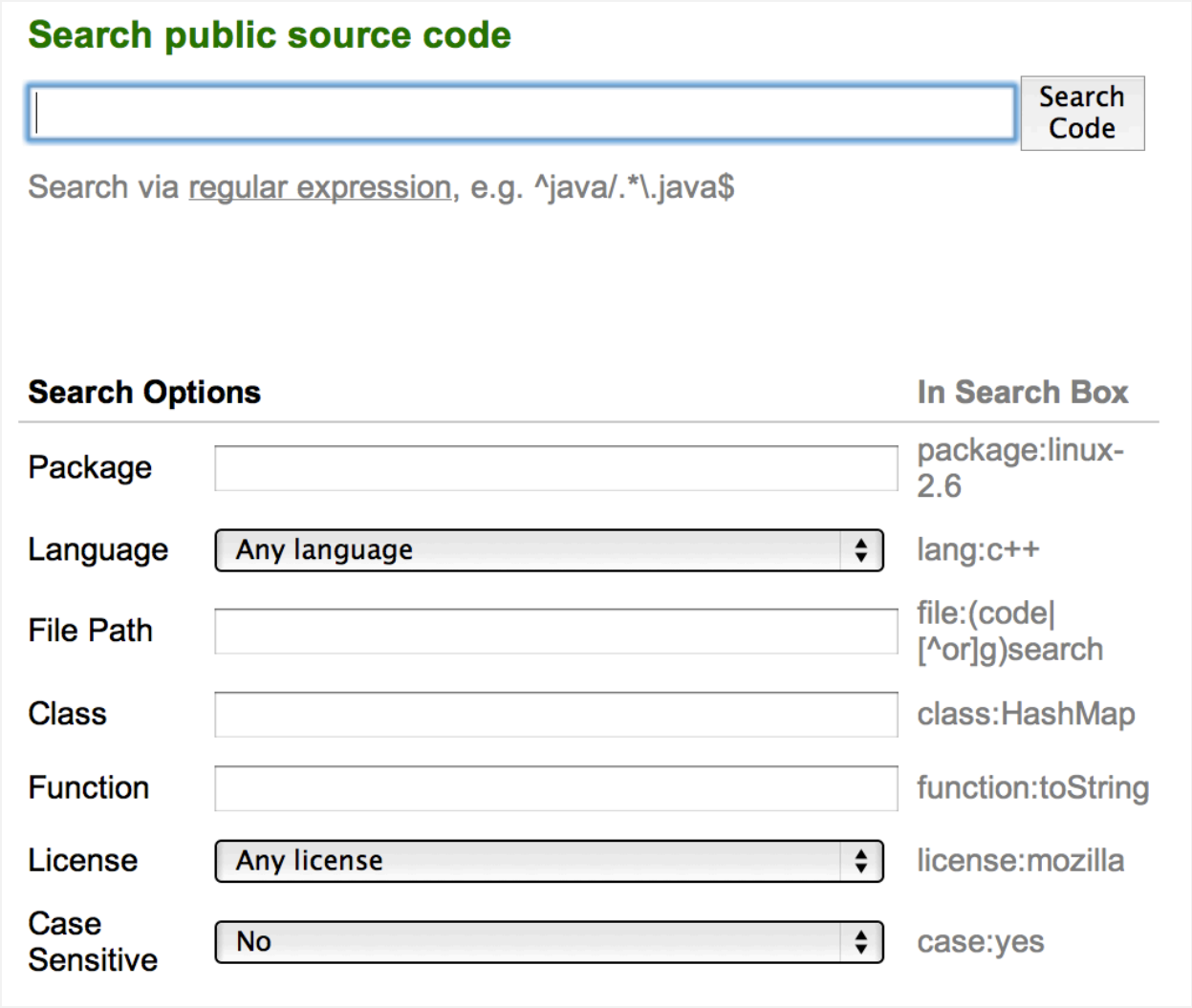
Syntax highlighting

```
/******************************************************************************
 *  Compilation:  javac NFA.java
 *  Execution:    java NFA regexp text
 *  Dependencies: Stack.java Bag.java Digraph.java DirectedDFS.java
 *
 *  % java NFA "(A*B|AC)D" AAAABD
 *  true
 *
 *  % java NFA "(A*B|AC)D" AAAAC
 *  false
 *
 ******************************************************************************/

public class NFA {

    private Digraph G;          // digraph of epsilon transitions
    private String regexp;      // regular expression
    private int M;              // number of characters in regular expression

    // Create the NFA for the given RE
    public NFA(String regexp) {
        this.regexp = regexp;
        M = regexp.length();
        Stack<Integer> ops = new Stack<Integer>();
        G = new Digraph(M+1);
```

GNU source-highlight 3.1.4

input	output
Ada	HTML
Asm	XHTML
Applescript	LATEX
Awk	MediaWiki
Bat	ODF
Bib	TEXINFO
Bison	ANSI
C/C++	DocBook
C#	
Cobol	
Caml	
Changelog	
Css	
D	
Erlang	
Flex	
Fortran	
GLSL	
Haskell	
Html	
Java	
Javalog	
Javascript	
Latex	

Google code search



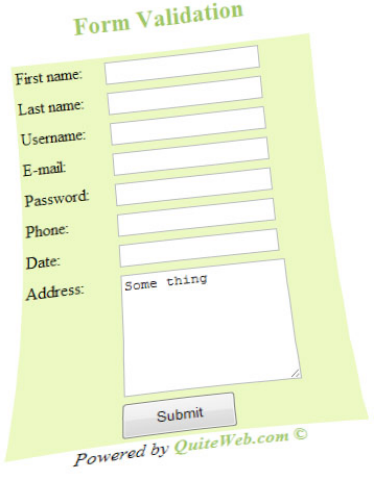
http://code.google.com/p/chromium/source/search

Pattern matching: applications

Test if a string matches some pattern.

- Scan for virus signatures.
- Process natural language.
- Specify a programming language.
- Access information in digital libraries.
- Search genome using PROSITE patterns.
- Filter text (spam, NetNanny, Carnivore, malware).
- Validate data-entry fields (dates, email, URL, credit card).

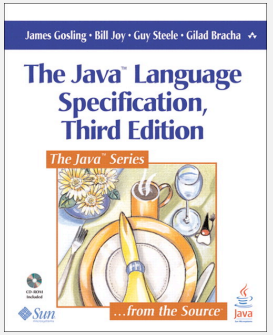
  ...



Parse text files.

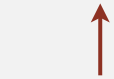
- Compile a Java program.
- Crawl and index the Web.
- Read in data stored in ad hoc input file format.
- Create Java documentation from Javadoc comments.

  ...



Regular expressions

A regular expression is a notation to specify a set of strings.



possibly infinite

operation	order	example RE	matches	does not match
concatenation	3	AABAAB	AABAAB	every other string
or	4	AA | BAAB	AA BAAB	every other string
closure	2	AB*A	AA ABBBBBBBBA	AB ABABA
parentheses	1	A(A|B)AAB	AAAAB ABAAB	every other string
		(AB)*A	A ABABABABABA	AA ABBA

Regular expression shortcuts

Additional operations are often added for convenience.

operation	example RE	matches	does not match
wildcard	`.U.U.U.`	CUMULUS JUGULUM	SUCCUBUS TUMULTUOUS
character class	`[A-Za-z][a-z]*`	word Capitalized	camelCase 4illegal
at least 1	`A(BC)+DE`	ABCDE ABCBCDE	ADE BCDE
exactly k	`[0-9]{5}-[0-9]{4}`	08540-1321 19072-5541	111111111 166-54-111

Ex. `[A-E]+` is shorthand for `(A|B|C|D|E)(A|B|C|D|E)*`

Regular expression examples

RE notation is surprisingly expressive.

regular expression	matches	does not match
`.*SPB.*` (*substring search*)	RASPBERRY CRISPBREAD	SUBSPACE SUBSPECIES
`[0-9]{3}-[0-9]{2}-[0-9]{4}` (*U. S. Social Security numbers*)	166-11-4433 166-45-1111	11-55555555 8675309
`[a-z]+@([a-z]+\.)+(edu|com)` (*simplified email addresses*)	wayne@princeton.edu rs@princeton.edu	spam@nowhere
`[$_A-Za-z][$_A-Za-z0-9]*` (*Java identifiers*)	ident3 PatternMatcher	3a ident#3

REs play a well-understood role in the theory of computation.

Regular expression examples

regular expression
(CAT|SUP*)

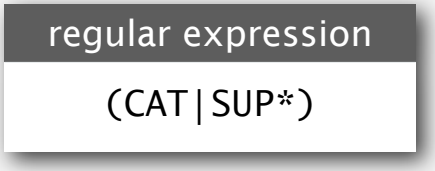
CATU	CATUP	CATSUPPP	SU

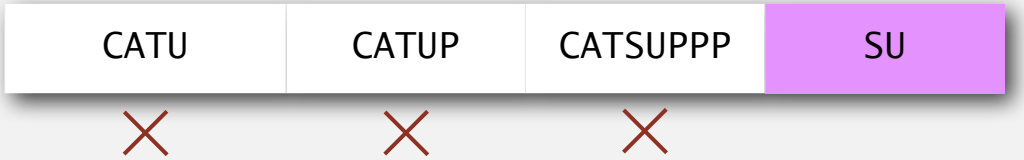
pollEv.com/jhug text to **37607**

Q: How many of the strings match the regular expression?

A. 0 [406437]
B. 1 [406438]
C. 2 [406439]
D. 3 [406446]
E. 4 [406795]

Regular expression examples





pollEv.com/jhug text to **37607**

Q: How many of the strings match the regular expression?

B. 1 [406438]

Regular expression examples

regular expression
(A|(B|C*)*)

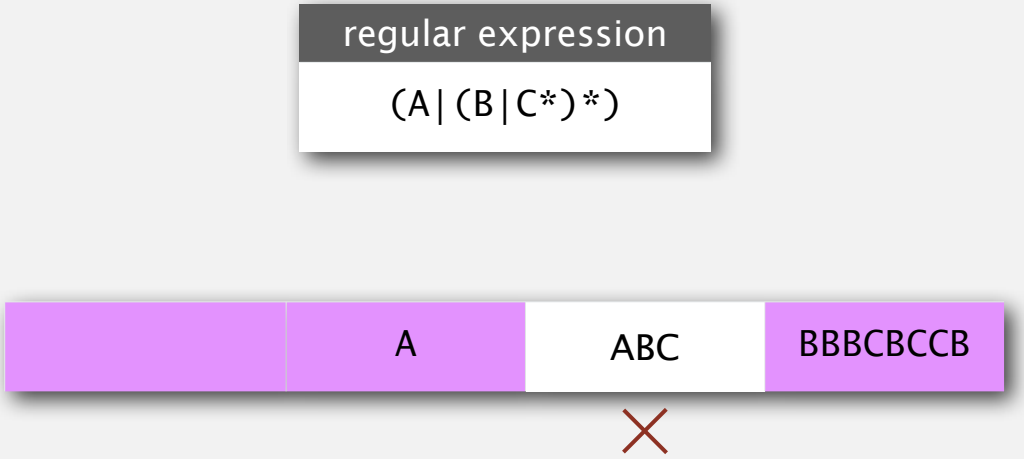
	A	ABC	BBBCBCCB

pollEv.com/jhug text to **37607**

Q: How many of the strings match the regular expression?

A. 0 [424621]
B. 1 [424623]
C. 2 [424625]
D. 3 [424765]
E. 4 [424770]

Regular expression examples



Q: How many of the strings match the regular expression?

D. 3

Can the average programmer learn to use REs?

Perl RE for valid RFC822 email addresses

```
(?:(?:\r\n)?[ \t])*(?:(?:(?:[^()<>@,;:\\".\[\] \000-\031]+(?:(?:(?:\r\n)?[ \t])+|\Z|(?=[\["()<>@,;:\\".\[\]]))|"(?:[^\"\r\\]|\\.|(?:(?:\r\n)?[ \t]))*"(?:(?:
\r\n)?[ \t])*)(?:\.(?:(?:\r\n)?[ \t])*(?:[^()<>@,;:\\".\[\] \000-\031]+(?:(?:(?:\r\n)?[ \t])+|\Z|(?=[\["()<>@,;:\\".\[\]]))|"(?:[^\"\r\\]|\\.|(?:(?:\r\n)?[
\t]))*"(?:(?:\r\n)?[ \t])*))*@(?:(?:\r\n)?[ \t])*(?:[^()<>@,;:\\".\[\] \000-\031]+(?:(?:(?:\r\n)?[ \t])+|\Z|(?=[\["()<>@,;:\\".\[\]]))|\[([^\[\]\r\\]|\\.)*\
](?:(?:\r\n)?[ \t])*)(?:\.(?:(?:\r\n)?[ \t])*(?:[^()<>@,;:\\".\[\] \000-\031]+(?:(?:(?:\r\n)?[ \t])+|\Z|(?=[\["()<>@,;:\\".\[\]]))|\[([^\[\]\r\\]|\\.)*\](?:
(?:\r\n)?[ \t])*))*|(?:[^()<>@,;:\\".\[\] \000-\031]+(?:(?:(?:\r\n)?[ \t])+|\Z|(?=[\["()<>@,;:\\".\[\]]))|"(?:[^\"\r\\]|\\.|(?:(?:\r\n)?[ \t]))*"(?:(?:\r\n)
?[ \t])*)*\<(?:(?:\r\n)?[ \t])*(?:@(?:[^()<>@,;:\\".\[\] \000-\031]+(?:(?:(?:\r\n)?[ \t])+|\Z|(?=[\["()<>@,;:\\".\[\]]))|\[([^\[\]\r\\]|\\.)*\](?:(?:\r\n)?[
 \t])*)(?:\.(?:(?:\r\n)?[ \t])*(?:[^()<>@,;:\\".\[\] \000-\031]+(?:(?:(?:\r\n)?[ \t])+|\Z|(?=[\["()<>@,;:\\".\[\]]))|\[([^\[\]\r\\]|\\.)*\](?:(?:\r\n)?[ \t]
)*))*(?:,@(?:(?:\r\n)?[ \t])*(?:[^()<>@,;:\\".\[\] \000-\031]+(?:(?:(?:\r\n)?[ \t])+|\Z|(?=[\["()<>@,;:\\".\[\]]))|\[([^\[\]\r\\]|\\.)*\](?:(?:\r\n)?[ \t])*
)(?:\.(?:(?:\r\n)?[ \t])*(?:[^()<>@,;:\\".\[\] \000-\031]+(?:(?:(?:\r\n)?[ \t])+|\Z|(?=[\["()<>@,;:\\".\[\]]))|\[([^\[\]\r\\]|\\.)*\](?:(?:\r\n)?[ \t])*))*)
*:(?:(?:\r\n)?[ \t])*)?(?:[^()<>@,;:\\".\[\] \000-\031]+(?:(?:(?:\r\n)?[ \t])+|\Z|(?=[\["()<>@,;:\\".\[\]]))|"(?:[^\"\r\\]|\\.|(?:(?:\r\n)?[ \t]))*"(?:(?:\r
\n)?[ \t])*)(?:\.(?:(?:\r\n)?[ \t])*(?:[^()<>@,;:\\".\[\] \000-\031]+(?:(?:(?:\r\n)?[ \t])+|\Z|(?=[\["()<>@,;:\\".\[\]]))|"(?:[^\"\r\\]|\\.|(?:(?:\r\n)?[ \t
]))*"(?:(?:\r\n)?[ \t])*))*@(?:(?:\r\n)?[ \t])*(?:[^()<>@,;:\\".\[\] \000-\031]+(?:(?:(?:\r\n)?[ \t])+|\Z|(?=[\["()<>@,;:\\".\[\]]))|\[([^\[\]\r\\]|\\.)*\](
?:(?:\r\n)?[ \t])*)(?:\.(?:(?:\r\n)?[ \t])*(?:[^()<>@,;:\\".\[\] \000-\031]+(?:(?:(?:\r\n)?[ \t])+|\Z|(?=[\["()<>@,;:\\".\[\]]))|\[([^\[\]\r\\]|\\.)*\](?:(?
:\r\n)?[ \t])*))*\>(?:(?:\r\n)?[ \t])*)|(?:[^()<>@,;:\\".\[\] \000-\031]+(?:(?:(?:\r\n)?[ \t])+|\Z|(?=[\["()<>@,;:\\".\[\]]))|"(?:[^\"\r\\]|\\.|(?:(?:\r\n)?
[ \t]))*"(?:(?:\r\n)?[ \t])*)*:(?:(?:\r\n)?[ \t])*(?:(?:(?:[^()<>@,;:\\".\[\] \000-\031]+(?:(?:(?:\r\n)?[ \t])+|\Z|(?=[\["()<>@,;:\\".\[\]]))|"(?:[^\"\r\\]|
\\.|(?:(?:\r\n)?[ \t]))*"(?:(?:\r\n)?[ \t])*)(?:\.(?:(?:\r\n)?[ \t])*(?:[^()<>@,;:\\".\[\] \000-\031]+(?:(?:(?:\r\n)?[ \t])+|\Z|(?=[\["()<>@,;:\\".\[\]]))|"
(?:[^\"\r\\]|\\.|(?:(?:\r\n)?[ \t]))*"(?:(?:\r\n)?[ \t])*))*@(?:(?:\r\n)?[ \t])*(?:[^()<>@,;:\\".\[\] \000-\031]+(?:(?:(?:\r\n)?[ \t])+|\Z|(?=[\["()<>@,;:\\
".\[\]]))|\[([^\[\]\r\\]|\\.)*\](?:(?:\r\n)?[ \t])*)(?:\.(?:(?:\r\n)?[ \t])*(?:[^()<>@,;:\\".\[\] \000-\031]+(?:(?:(?:\r\n)?[ \t])+|\Z|(?=[\["()<>@,;:\\".\[
\]]))|\[([^\[\]\r\\]|\\.)*\](?:(?:\r\n)?[ \t])*))*|(?:[^()<>@,;:\\".\[\] \000-\031]+(?:(?:(?:\r\n)?[ \t])+|\Z|(?=[\["()<>@,;:\\".\[\]]))|"(?:[^\"\r\\]|\\.|(?:(?:\r\n)?[ \t]))*"(?:(?:\r\n)?[ \t])*)*\<(?:(?:\r\n)?[ \t])*(?:@(?:[^()<>@,;:\\".\[\] \000-\031]+(?:(?:(?:\r\n)?[ \t])+|\Z|(?=[\["()<>@,;:\\".\[\]]))|\[([^\[\]\r\\]|\\.)*\](?:(?:\r\n)?[ \t])*)(?:\.(?:(?:\r\n)?[ \t])*(?:[^()<>@,;:\\".\[\] \000-\031]+(?:(?:(?:\r\n)?[ \t])+|\Z|(?=[\["()<>@,;:\\".\[\]]))|\[([^\[\]\r\\]|\\.)*\](?:(?:\r\n)?[ \t])*))*(?:,@(?:(?:\r\n)?[ \t])*(?:[^()<>@,;:\\".\[\] \000-\031]+(?:(?:(?:\r\n)?[ \t])+|\Z|(?=[\["()<>@,;:\\".\[\]]))|\[([^\[\]\r\\]|\\.)*\](?:(?:\r\n)?[ \t])*)(?:\.(?:(?:\r\n)?[ \t])*(?:[^()<>@,;:\\".\[\] \000-\031]+(?:(?:(?:\r\n)?[ \t])+|\Z|(?=[\["()<>@,;:\\".\[\]]))|\[([^\[\]\r\\]|\\.)*\](?:(?:\r\n)?[ \t])*))*:(?:(?:\r\n)?[ \t])*(?:(?:(?:[^()<>@,;:\\".\[\] \000-\031]+(?:(?:(?:\r\n)?[ \t])+|\Z|(?=[\["()<>@,;:\\".\[\]]))|"(?:[^\"\r\\]|\\.|(?:(?:\r\n)?[ \t]))*"(?:(?:\r\n)?[ \t])*)(?:\.(?:(?:\r\n)?[ \t])*(?:[^()<>@,;:\\".\[\] \000-\031]+(?:(?:(?:\r\n)?[ \t])+|\Z|(?=[\["()<>@,;:\\".\[\]]))|"(?:[^\"\r\\]|\\.|(?:(?:\r\n)?[ \t]))*"(?:(?:\r\n)?[ \t])*))*@(?:(?:\r\n)?[ \t])*(?:[^()<>@,;:\\".\[\] \000-\031]+(?:(?:(?:\r\n)?[ \t])+|\Z|(?=[\["()<>@,;:\\".\[\]]))|\[([^\[\]\r\\]|\\.)*\](?:(?:\r\n)?[ \t])*)(?:\.(?:(?:\r\n)?[ \t])*(?:[^()<>@,;:\\".\[\] \000-\031]+(?:(?:(?:\r\n)?[ \t])+|\Z|(?=[\["()<>@,;:\\".\[\]]))|\[([^\[\]\r\\]|\\.)*\](?:(?:\r\n)?[ \t])*))*\>(?:(?:\r\n)?[ \t])*)(?:,\s*(?:(?:[^()<>@,;:\\".\[\] \000-\031]+(?:(?:(?:\r\n)?[ \t])+|\Z|(?=[\["()<>@,;:\\
".\[\]]))|"(?:[^\"\r\\]|\\.|(?:(?:\r\n)?[ \t]))*"(?:(?:\r\n)?[ \t])*)(?:\.(?:(?:\r\n)?[ \t])*(?:[^()<>@,;:\\".\[\] \000-\031]+(?:(?:(?:\r\n)?[ \t])+|\Z|(?=[
\["()<>@,;:\\".\[\]]))|"(?:[^\"\r\\]|\\.|(?:(?:\r\n)?[ \t]))*"(?:(?:\r\n)?[ \t])*))*@(?:(?:\r\n)?[ \t])*(?:[^()<>@,;:\\".\[\] \000-\031]+(?:(?:(?:\r\n)?[ \t])+|\Z|(?=[\["()<>@,;:\\".\[\]]))|\[([^\[\]\r\\]|\\.)*\](?:(?:\r\n)?[ \t])*)(?:\.(?:(?:\r\n)?[ \t])*(?:[^()<>@,;:\\".\[\] \000-\031]+(?:(?:(?:\r\n)?[ \t])+|\Z|(?=[\["()<>@,;:\\".\[\]]))|\[([^\[\]\r\\]|\\.)*\](?:(?:\r\n)?[ \t])*))*\>(?:(?:\r\n)?[ \t])*)?;\s*)
```

http://www.ex-parrot.com/~pdw/Mail-RFC822-Address.html

Regular expression caveat

Writing a RE is like writing a program.

- Need to understand programming model.
- Can be easier to write than read.
- Can be difficult to debug.

> *" Some people, when confronted with a problem, think 'I know I'll use regular expressions.' Now they have two problems. "*
>
> *— Jamie Zawinski (flame war on alt.religion.emacs)*

Bottom line. REs are amazingly powerful and expressive,
but using them in applications can be amazingly complex and error-prone.

http://algs4.cs.princeton.edu

5.4 Regular Expressions

- *regular expressions*
- *NFAs and NFA simulation*
- *NFA construction*
- *applications and context*

Duality between REs and DFAs

RE. Concise way to describe a set of strings.

DFA. Machine to recognize whether a given string is in a given set.

See COS487 next Fall (requires COS340)

Kleene's theorem.

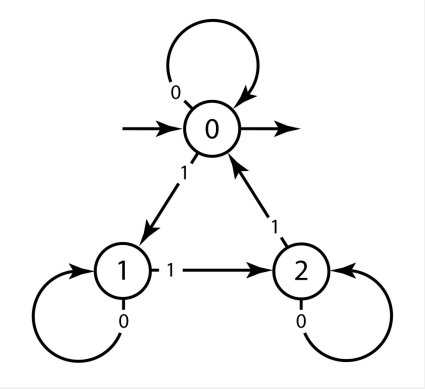
- For any DFA, there exists a RE that describes the same set of strings.
- For any RE, there exists a DFA that recognizes the same set of strings.

RE

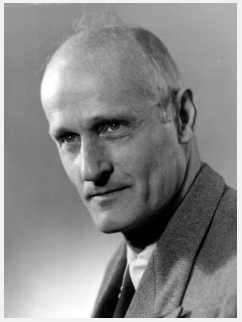
0* | (0*10*10*10*)*

number of 1's is a multiple of 3

DFA



number of 1's is a multiple of 3

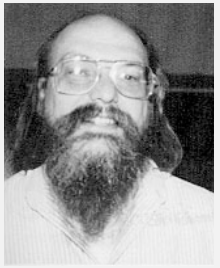


Stephen Kleene
Princeton Ph.D. 1934

Pattern matching implementation: basic plan (first attempt)

Overview is the same as for KMP.

- No backup in text input stream.
- Linear-time guarantee.

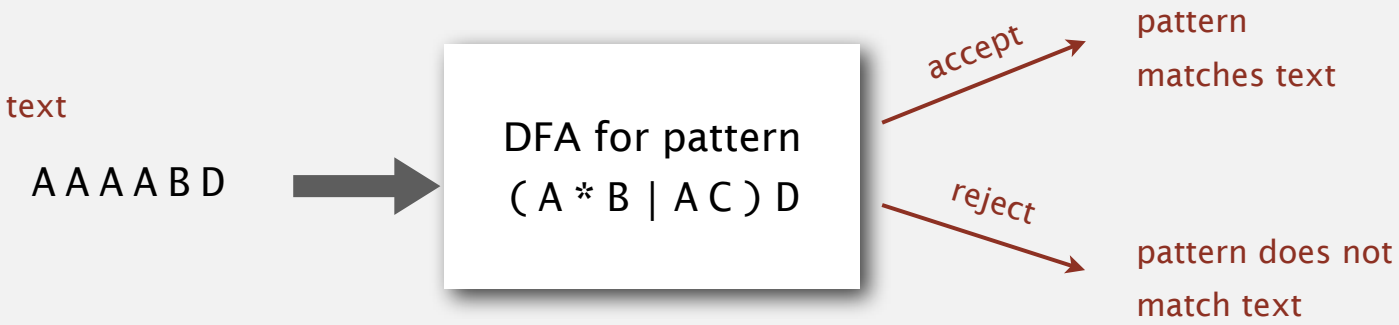


Ken Thompson
Turing Award '83

Underlying abstraction. Deterministic finite state automata (DFA).

Basic plan. [apply Kleene's theorem]

- Build DFA from RE.
- Simulate DFA with text as input.

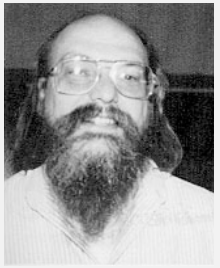


Bad news. Basic plan is infeasible (DFA may have exponential # of states).

Pattern matching implementation: basic plan (revised)

Overview is similar to KMP.

- No backup in text input stream.
- Quadratic-time guarantee (linear-time typical).

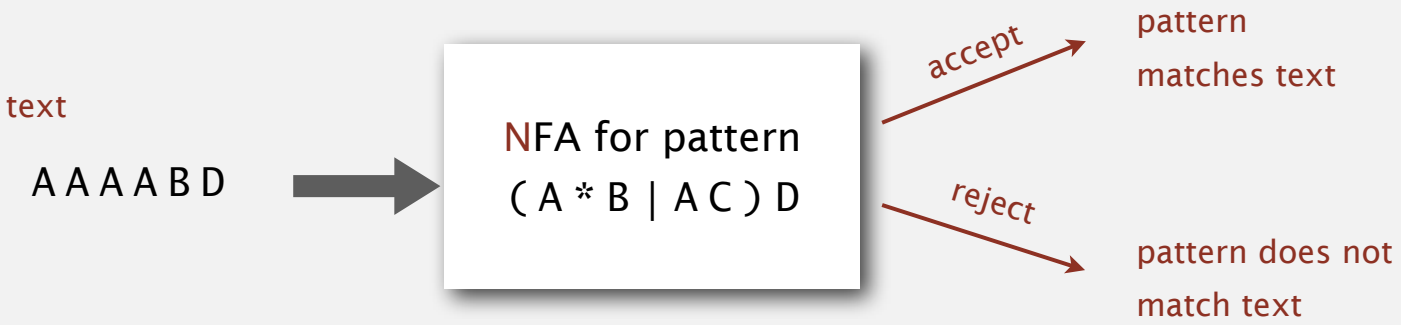


Ken Thompson
Turing Award '83

Underlying abstraction. Nondeterministic finite state automata (NFA).

Basic plan. [apply Kleene's theorem]

- Build NFA from RE.
- Simulate NFA with text as input.



Q. What is an NFA?

Nondeterministic finite-state automata

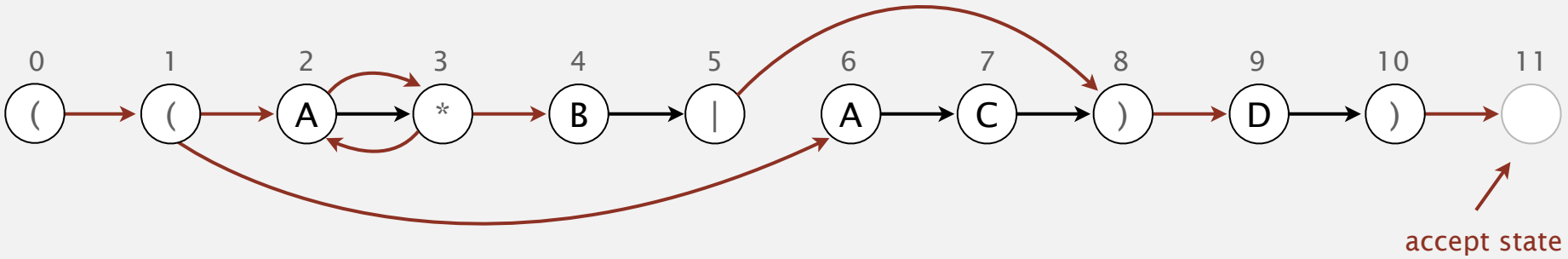
Regular-expression-matching NFA.

- RE enclosed in parentheses.
- One state per RE character (start = 0, accept = M).
- Red ε-transition (change state, but don't scan text).
- Black match transition (change state and scan to next text char).
- Accept if any sequence of transitions ends in accept state.

after scanning all text characters

Nondeterminism.

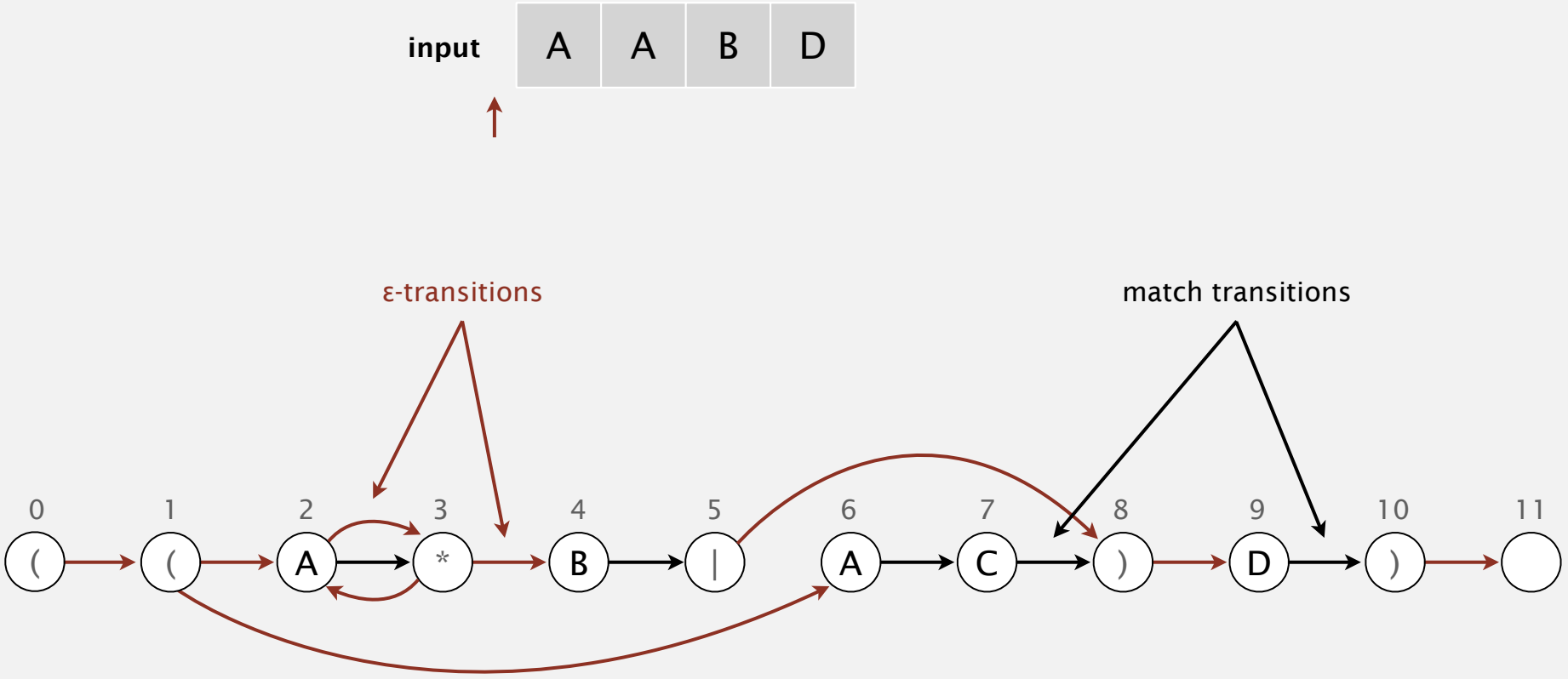
- One view: machine can guess the proper sequence of state transitions.
- Another view: sequence is a proof that the machine accepts the text.



NFA corresponding to the pattern ((A * B | A C) D)

NFA simulation demo

Goal. Check whether input matches pattern.

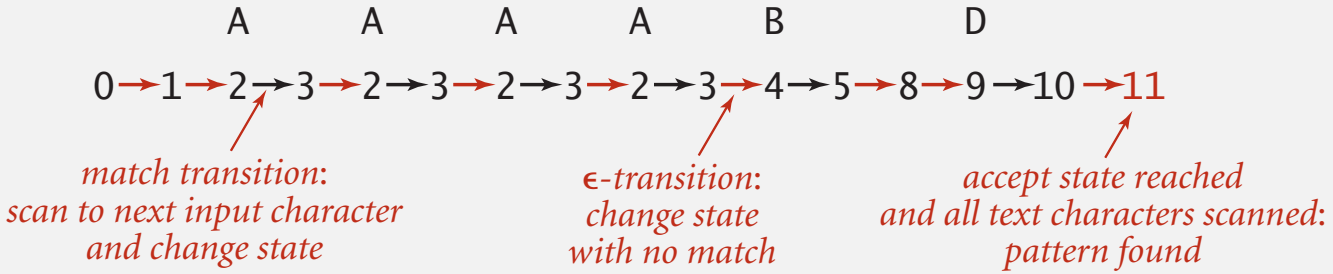


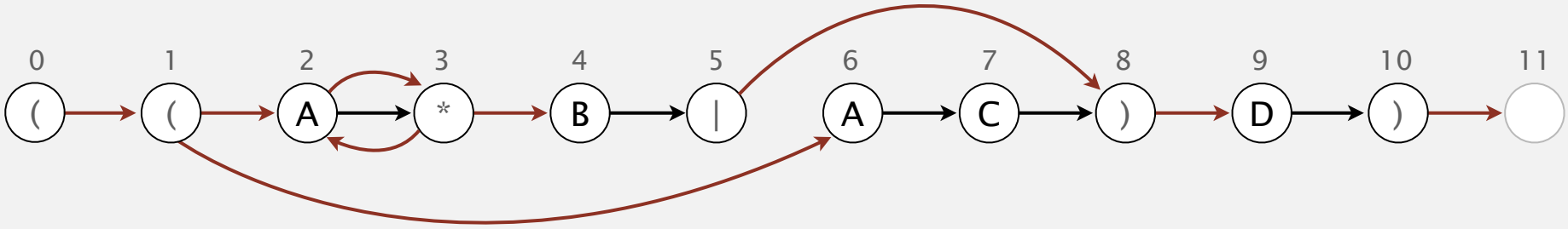
NFA corresponding to the pattern ((A * B | A C) D)

Nondeterministic finite-state automata

Q. Is A A A A B D matched by NFA?

A. Yes, because some sequence of legal transitions ends in state 11.





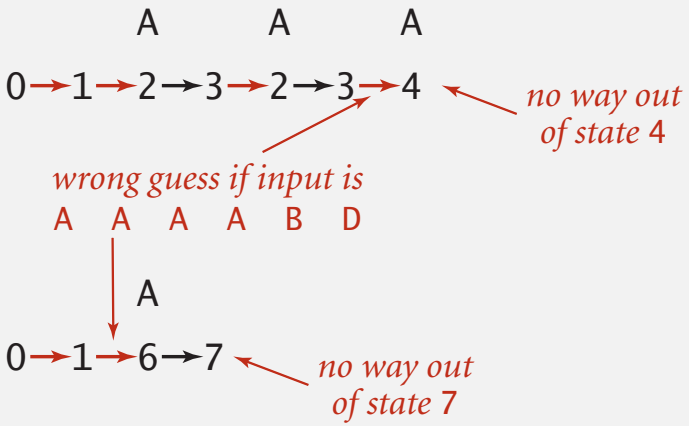
NFA corresponding to the pattern ((A * B | A C) D)

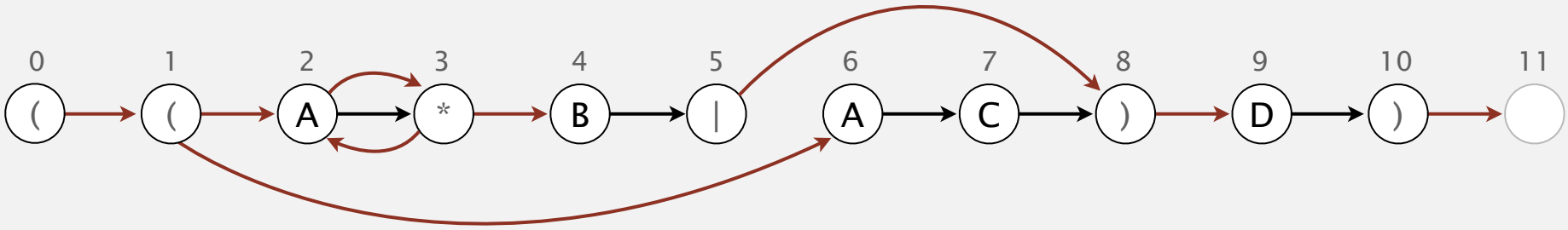
Nondeterministic finite-state automata

Q. Is A A A A B D matched by NFA?

A. Yes, because some sequence of legal transitions ends in state 11.

[even though some sequences end in wrong state or stall]





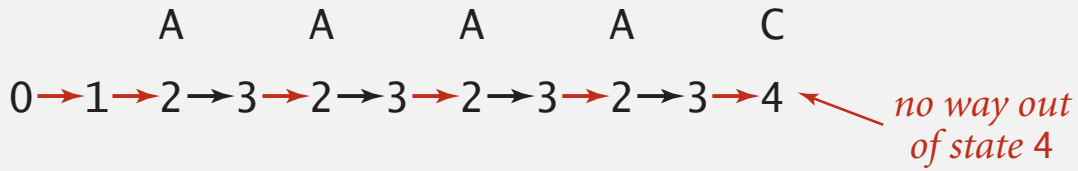
NFA corresponding to the pattern ((A * B | A C) D)

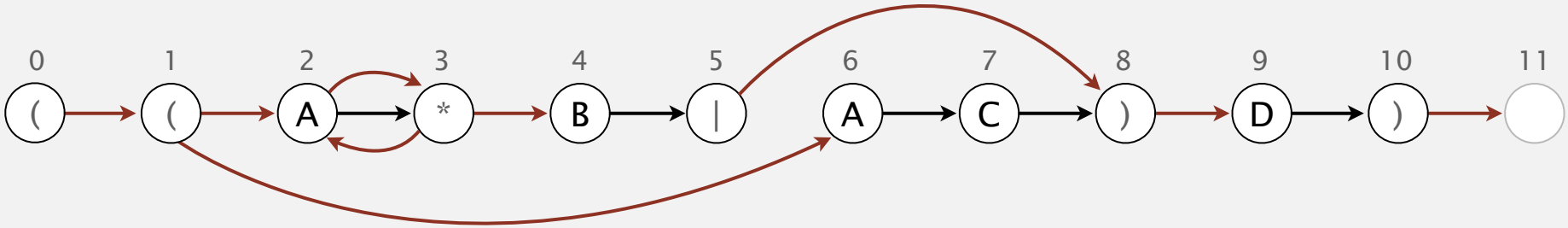
Nondeterministic finite-state automata

Q. Is A A A C matched by NFA?

A. No, because no sequence of legal transitions ends in state 11.

[but need to argue about all possible sequences]





NFA corresponding to the pattern ((A * B | A C) D)

Nondeterminism

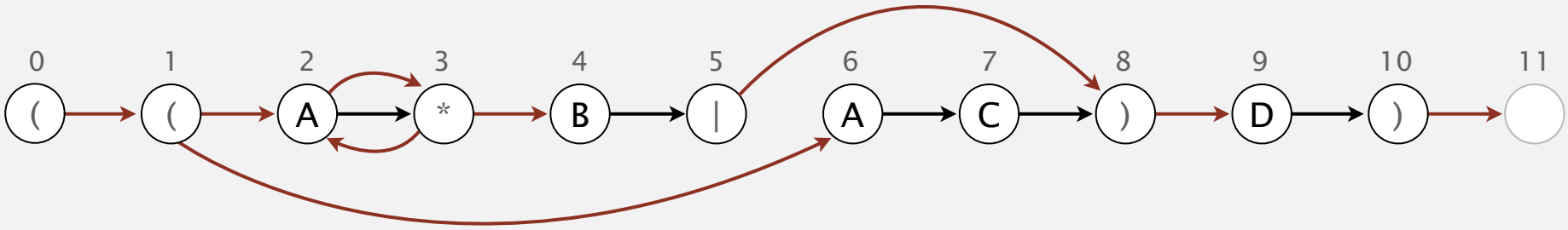
Q. How to determine whether a string is matched by an automaton?

DFA. Deterministic ⇒ easy because exactly one applicable transition.

NFA. Nondeterministic ⇒ can be several applicable transitions;
need to select the right one!

Q. How to simulate NFA?

A. Systematically consider all possible transition sequences.



NFA corresponding to the pattern ((A * B | A C) D)

NFA representation

State names. Integers from 0 to M.

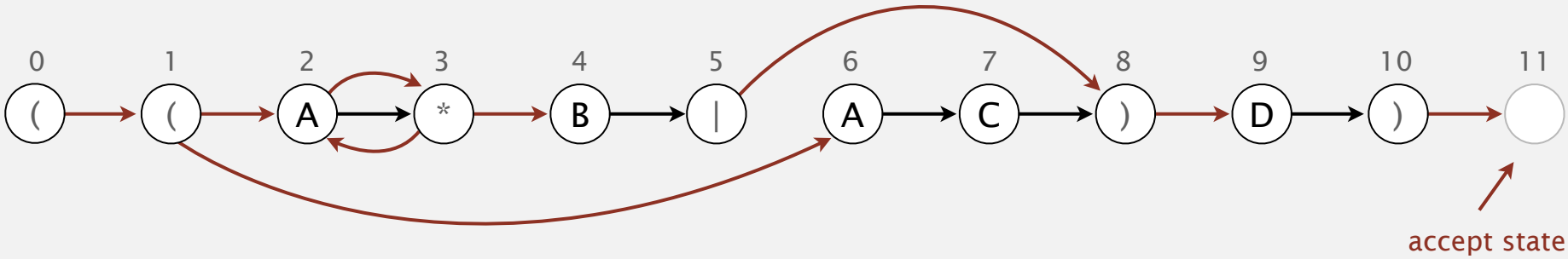
number of symbols in RE

Match-transitions. Keep regular expression in array `re[]`.

e.g. re[4] = 'B'

ε-transitions. Store in a digraph G.

0→1, 1→2, 1→6, 2→3, 3→2, 3→4, 5→8, 8→9, 10→11

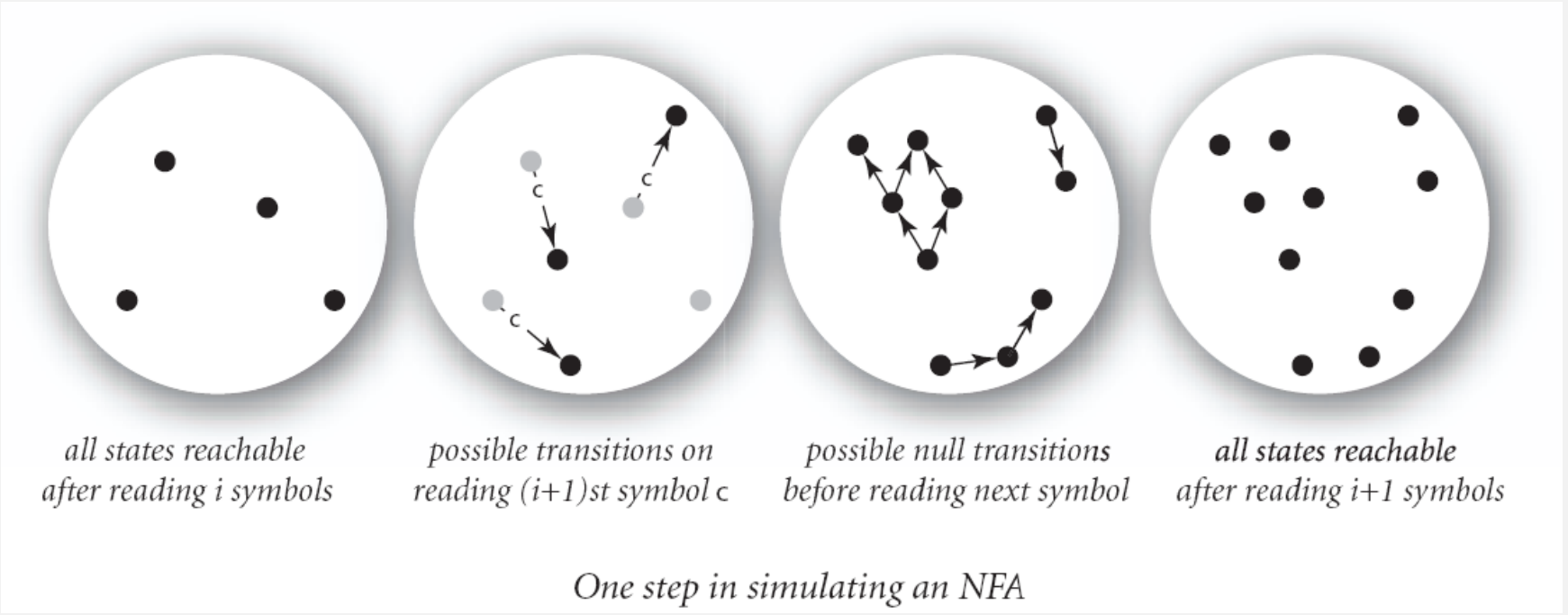


NFA corresponding to the pattern ((A * B | A C) D)

NFA simulation

Q. How to efficiently simulate an NFA?

A. Maintain set of all possible states that NFA could be in after reading in the first i text characters.



One step in simulating an NFA

Q. How to perform reachability?

Digraph reachability

Digraph reachability. Find all vertices reachable from a given source or set of vertices.

recall Section 4.2

public class DirectedDFS	
DirectedDFS(Digraph G, int s)	find vertices reachable from s
DirectedDFS(Digraph G, Iterable<Integer> s)	find vertices reachable from sources
boolean marked(int v)	is v reachable from source(s)?

Solution. Run DFS from each source, without unmarking vertices.

Performance. Runs in time proportional to $E + V$.

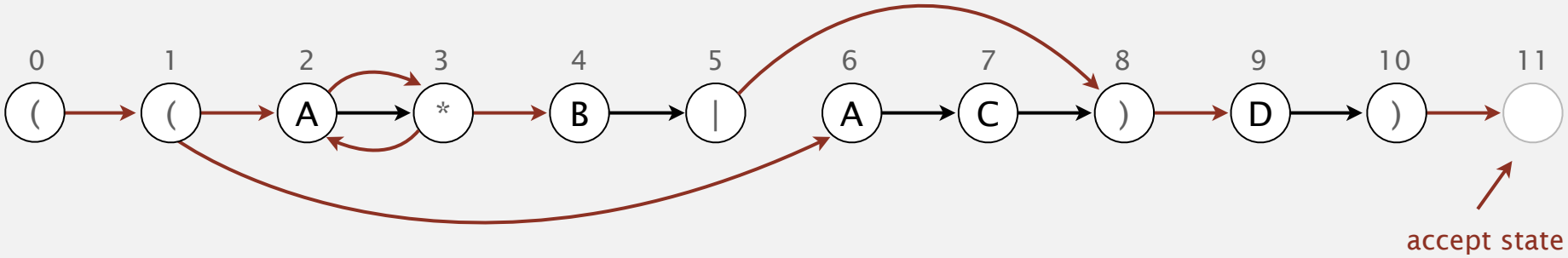
Runtime for NFA simulation

NFA simulation steps for each text character:

- Find states reachable by match transitions.
- Find states reachable by ε-transitions

Let:

- N = length of text
- M = length of pattern (also number of DFA states)
- R = alphabet size



pollEv.com/jhug text to **37607**

Q: What is the runtime to complete NFA simulation in the worst case?

A. N	[428594]	D. N + M	[428616]
B. M	[428595]	E. N + M + R	[428617]
C. NM	[428615]	F. NMR	[428634]

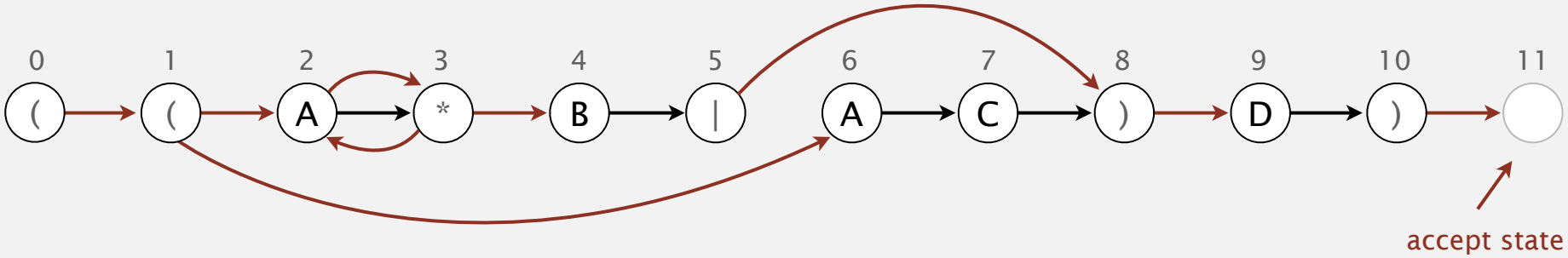
Runtime for NFA simulation

NFA simulation steps for each text character:

- Find states reachable by match transitions.
- Find states reachable by ε-transitions

Let:

- N = length of text
- M = length of pattern (also number of DFA states)
- R = alphabet size



Q: What is the runtime to complete NFA simulation in the worst case?

C. NM

Finding states reachable by match transitions: O(M)

Finding states reachable by match transitions: V + E

Number of vertices: M. Total number of epsilon edges: O(M) (stay tuned)

NFA simulation: Java implementation

```
public class NFA
{
   private char[] re;       // match transitions
   private Digraph G;       // epsilon transition digraph
   private int M;           // number of states

   public NFA(String regexp)
   {
      M  = regexp.length();
      re = regexp.toCharArray();
      G = buildEpsilonTransitionsDigraph();
   }

   public boolean recognizes(String txt)
   {  /* see next slide */  }

   public Digraph buildEpsilonTransitionDigraph()
   {  /* stay tuned */  }

}
```

stay tuned (next segment)

NFA simulation: Java implementation

```
public boolean recognizes(String txt)
{
   Bag<Integer> pc = new Bag<Integer>();
   DirectedDFS dfs = new DirectedDFS(G, 0);
   for (int v = 0; v < G.V(); v++)
      if (dfs.marked(v)) pc.add(v);

   for (int i = 0; i < txt.length(); i++)
   {
      Bag<Integer> match = new Bag<Integer>();
      for (int v : pc)
      {
         if (v == M) continue;
         if ((re[v] == txt.charAt(i)) || re[v] == '.')
            match.add(v+1);
      }

      dfs = new DirectedDFS(G, match);
      pc = new Bag<Integer>();
      for (int v = 0; v < G.V(); v++)
         if (dfs.marked(v)) pc.add(v);
   }

   for (int v : pc)
      if (v == M) return true;
   return false;
}
```

states reachable from start by ε-transitions

states reachable after scanning past `txt.charAt(i)`

follow ε-transitions

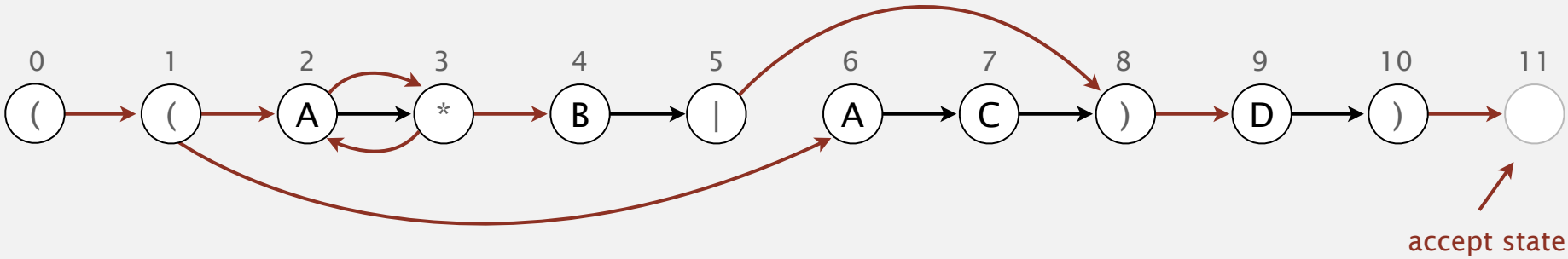
accept if can end in state M

NFA simulation: analysis

Proposition. Determining whether an N-character text is recognized by the NFA corresponding to an M-character pattern takes time proportional to $M\,N$ in the worst case.

Pf. For each of the N text characters, we iterate through a set of states of size no more than M and run DFS on the graph of ε-transitions.
[The NFA construction we will consider ensures the number of edges ≤ $3M$.]

Alternate Pf. See PollEverywhere question.



NFA corresponding to the pattern ((A * B | A C) D)

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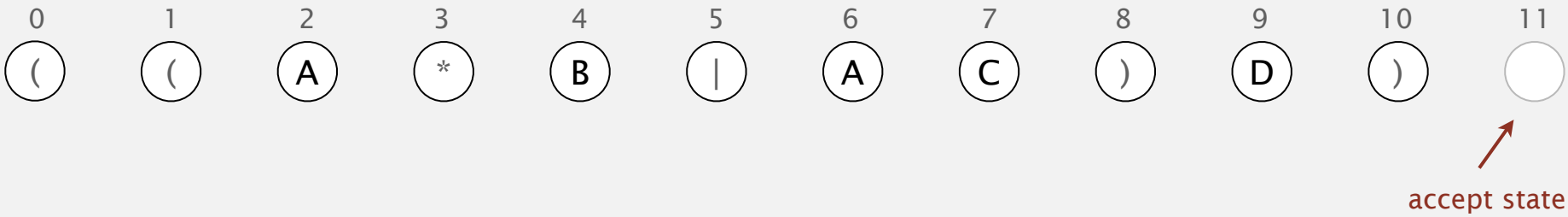
5.4 Regular Expressions

- *regular expressions*
- *NFAs and NFA simulation*
- *NFA construction*
- *applications and context*

Building an NFA corresponding to an RE

States. Include a state for each symbol in the RE, plus an accept state.



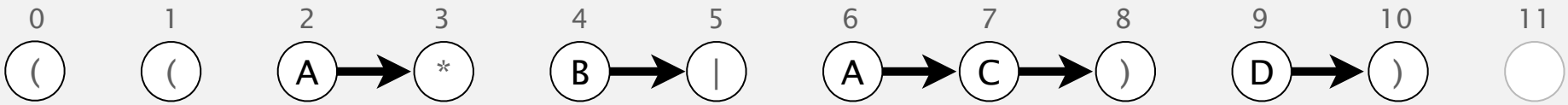
NFA corresponding to the pattern ((A * B | A C) D)

Building an NFA corresponding to an RE

Concatenation. Add match-transition edge from state corresponding to characters in the alphabet to next state.

Alphabet. `A B C D`

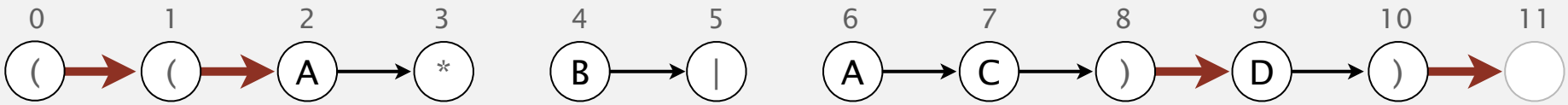
Metacharacters. `( ) . * |`



NFA corresponding to the pattern `( ( A * B | A C ) D )`

Building an NFA corresponding to an RE

Parentheses. Add ε-transition edge from parentheses to next state.

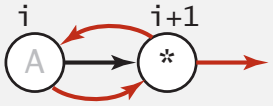


NFA corresponding to the pattern ((A * B | A C) D)

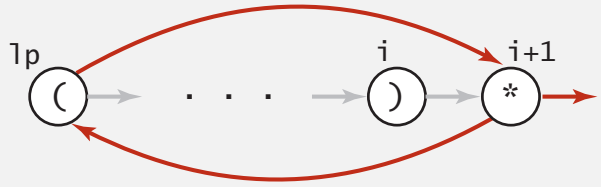
Building an NFA corresponding to an RE

Closure. Add three ε-transition edges for each * operator.

single-character closure



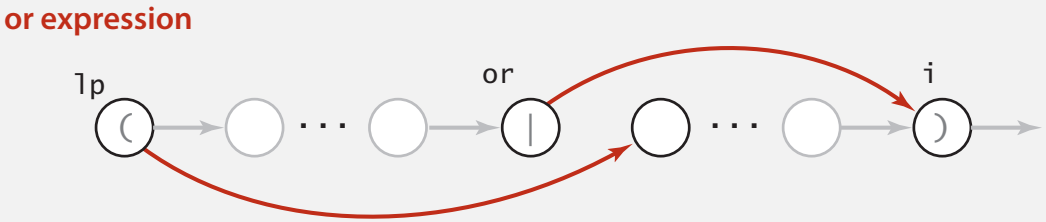
closure expression

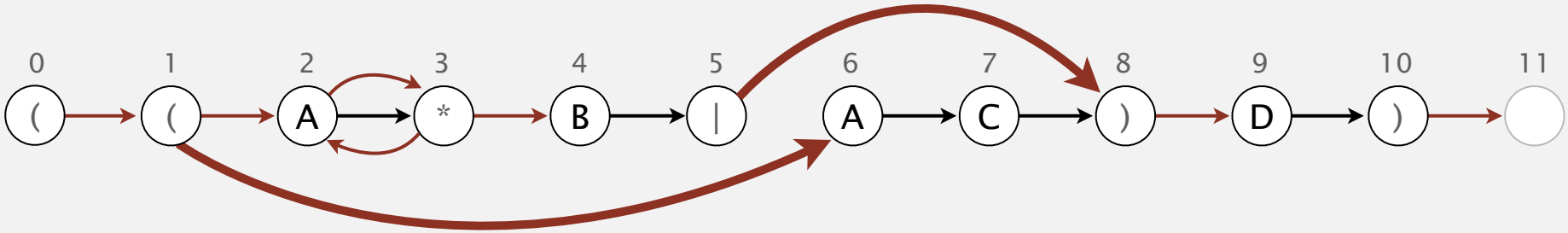


NFA corresponding to the pattern ((A * B | A C) D)

Building an NFA corresponding to an RE

Or. Add two ε-transition edges for each | operator.





NFA corresponding to the pattern ((A * B | A C) D)

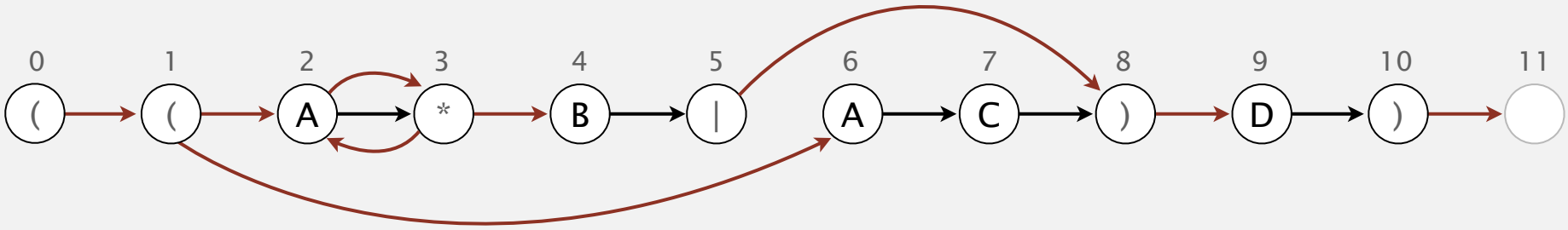
NFA construction: implementation

Goal. Write a program to build the ε-transition digraph.

Challenges. Remember left parentheses to implement closure and or; remember | to implement or.

Solution. Maintain a stack.

- (symbol: push (onto stack.
- | symbol: push | onto stack.
-) symbol: pop corresponding (and any intervening |; add ε-transition edges for closure/or.



NFA corresponding to the pattern ((A * B | A C) D)

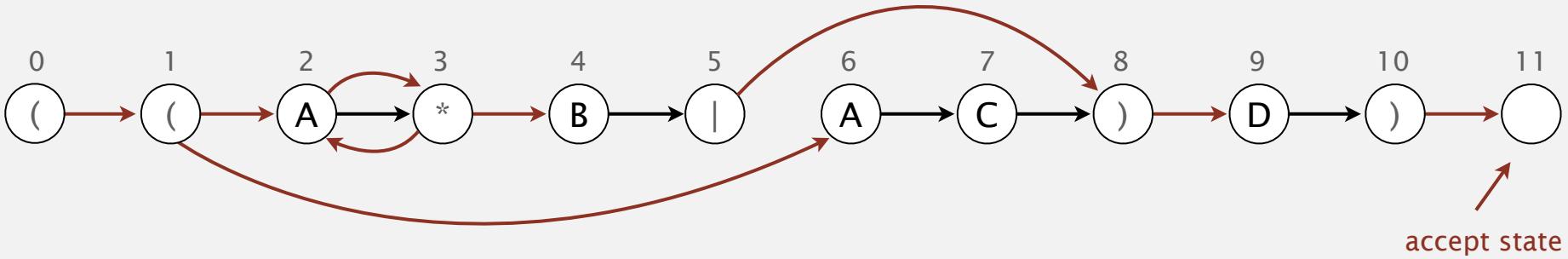
NFA construction demo

stack

((A * B | A C) D)

NFA construction demo

stack



NFA corresponding to the pattern ((A * B | A C) D)

NFA construction: Java implementation

```
private Digraph buildEpsilonTransitionDigraph() {
   Digraph G = new Digraph(M+1);
   Stack<Integer> ops = new Stack<Integer>();
   for (int i = 0; i < M; i++) {
      int lp = i;

      if (re[i] == '(' || re[i] == '|') ops.push(i);

      else if (re[i] == ')') {
         int or = ops.pop();
         if (re[or] == '|') {
            lp = ops.pop();
            G.addEdge(lp, or+1);
            G.addEdge(or, i);
         }
         else lp = or;
      }

      if (i < M-1 && re[i+1] == '*') {
         G.addEdge(lp, i+1);
         G.addEdge(i+1, lp);
      }

      if (re[i] == '(' || re[i] == '*' || re[i] == ')')
         G.addEdge(i, i+1);
   }
   return G;
}
```

left parentheses and |

or

closure

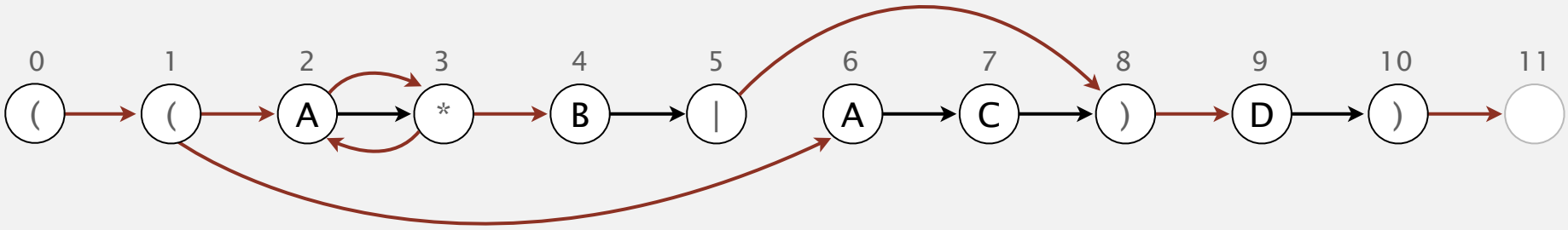
(needs 1-character lookahead)

metasymbols

NFA construction: analysis

Proposition. Building the NFA corresponding to an M-character RE takes time and space proportional to M.

Pf. For each of the M characters in the RE, we add at most three ε-transitions and execute at most two stack operations.



NFA corresponding to the pattern ((A * B | A C) D)

http://algs4.cs.princeton.edu

5.4 Regular Expressions

- *regular expressions*
- *NFAs and NFA simulation*
- *NFA construction*
- *applications and context*

Generalized regular expression print

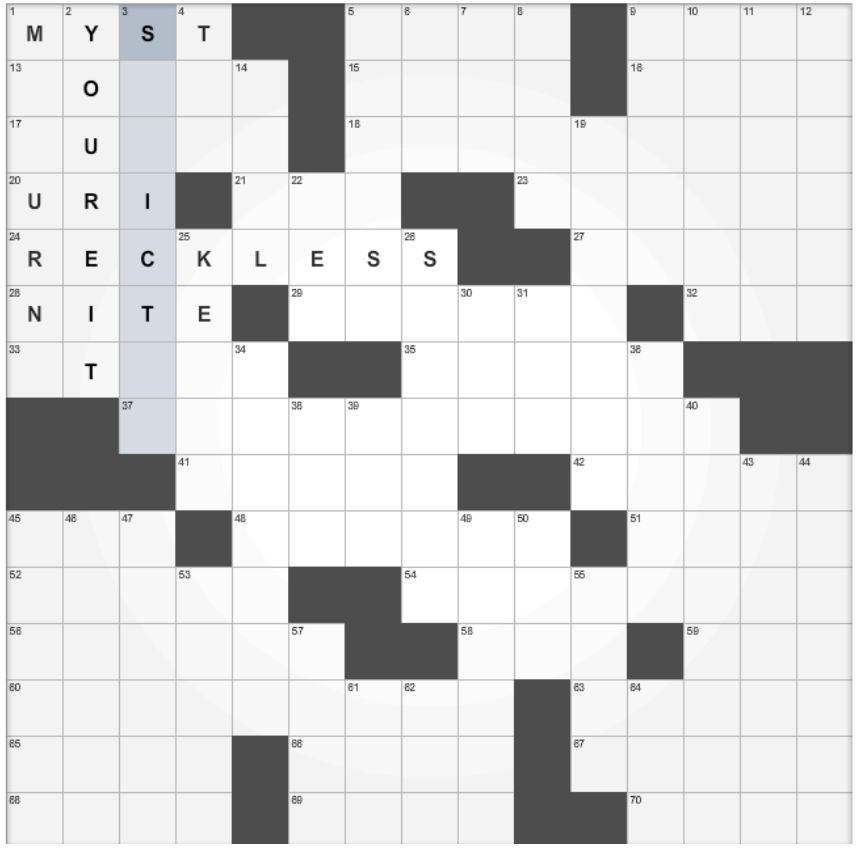
Grep. Take a RE as a command-line argument and print the lines from standard input having s **substring that is matched** by the RE.

```
public class GREP
{
   public static void main(String[] args)
   {
      String re = "(.*" + args[0] + ".*)";
      NFA nfa = new NFA(re);
      while (StdIn.hasNextLine())
      {
         String line = StdIn.readLine();
         if (nfa.recognizes(line))
            StdOut.println(line);
      }
   }
}
```

contains RE as a substring

Bottom line. Worst-case for grep (proportional to MN) is the same as for brute-force substring search.

Typical grep application: crossword puzzles



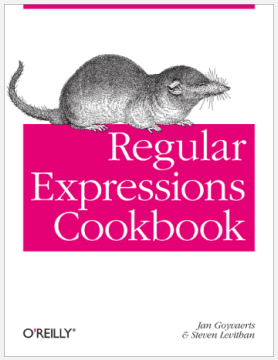

```
% more words.txt
a
aback
abacus
abalone
abandon
...

% grep "s..ict.." words.txt
constrictor
stricter
stricture
```

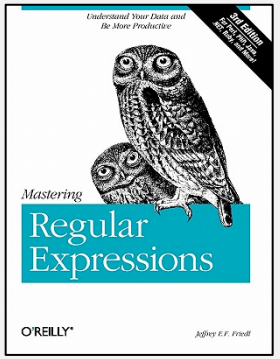
dictionary
(standard in Unix)
also on booksite

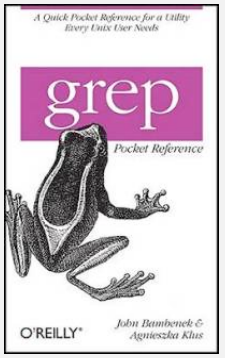
Industrial-strength grep implementation

To complete the implementation:

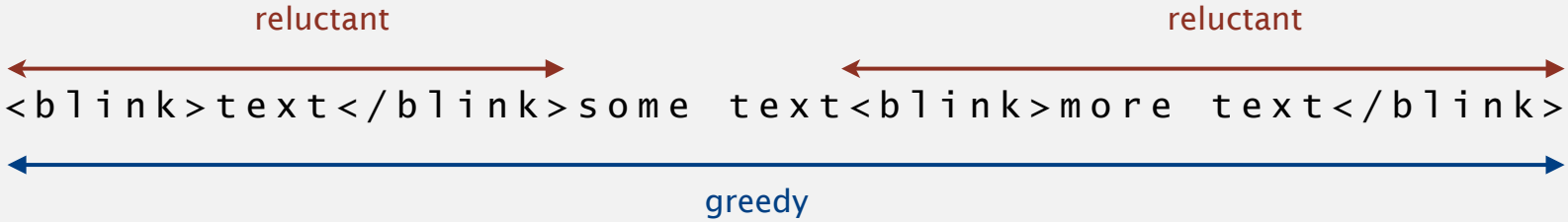
- Add character classes. [0-9][0-9]
- Handle metacharacters. a\.b
- Add capturing capabilities.
- Extend the closure operator. a+b
- Error checking and recovery. *|*|*
- Greedy vs. reluctant matching. to.*?be







Ex. Which substring(s) should be matched by the RE `<blink>.*</blink>` ?



Regular expressions in Java

Validity checking. Does the `input` match the `re`?

Java string library. Use `input.matches(re)` for basic RE matching.

```
public class Validate
{
   public static void main(String[] args)
   {
      String regexp = args[0];
      String input  = args[1];
      StdOut.println(input.matches(re));
   }
}
```

```
% java Validate "[$_A-Za-z][$_A-Za-z0-9]*" ident123
true

% java Validate "[a-z]+@([a-z]+\.)+(edu|com)" rs@cs.princeton.edu
true

% java Validate "[0-9]{3}-[0-9]{2}-[0-9]{4}" 166-11-4433
true
```

← legal Java identifier

← valid email address (simplified)

← Social Security number

Harvesting information

Goal. Print all substrings of input that match a RE.

```
% java Harvester "gcg(cgg|agg)*ctg" chromosomeX.txt
gcgcggcggcggcggcggctg
gcgctg
gcgctg
gcgcggcggcggaggcggaggcggctg
```

harvest patterns from DNA

harvest links from website

```
% java Harvester "http://(\\w+\\.)*(\\w+)" http://www.cs.princeton.edu
http://www.princeton.edu
http://www.google.com
http://www.cs.princeton.edu/news
```

Harvesting information

RE pattern matching is implemented in Java's `java.util.regexp.Pattern` and `java.util.regexp.Matcher` classes.

```
import java.util.regex.Pattern;
import java.util.regex.Matcher;

public class Harvester
{
   public static void main(String[] args)
   {
      String regexp   = args[0];
      In in           = new In(args[1]);
      String input    = in.readAll();
      Pattern pattern = Pattern.compile(regexp);
      Matcher matcher = pattern.matcher(input);
      while (matcher.find())
      {
         StdOut.println(matcher.group());
      }
   }
}
```

`compile()` creates a `Pattern` (NFA) from RE

`matcher()` creates a `Matcher` (NFA simulator) from NFA and text

`find()` looks for the next match

`group()` returns the substring most recently found by `find()`

Algorithmic complexity attacks

Warning. Typical implementations do not guarantee performance!

Unix grep, Java, Perl

```
% java Validate "(a|aa)*b" aaaaaaaaaaaaaaaaaaaaaaaaaaaaac              1.6 seconds
% java Validate "(a|aa)*b" aaaaaaaaaaaaaaaaaaaaaaaaaaaaaac             3.7 seconds
% java Validate "(a|aa)*b" aaaaaaaaaaaaaaaaaaaaaaaaaaaaaaac            9.7 seconds
% java Validate "(a|aa)*b" aaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaac          23.2 seconds
% java Validate "(a|aa)*b" aaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaac         62.2 seconds
% java Validate "(a|aa)*b" aaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaac       161.6 seconds
```

SpamAssassin regular expression.

```
% java RE "[a-z]+@[a-z]+([a-z\.]+\.)+[a-z]+" spammer@x.....................
```

- Takes exponential time on pathological email addresses.
- Troublemaker can use such addresses to DOS a mail server.

Not-so-regular expressions

Back-references.

- `\1` notation matches subexpression that was matched earlier.
- Supported by typical RE implementations, but not our NFA approach.

```
(.+)\1           // beriberi couscous
1?$|^(11+?)\1+   // 1111 111111 111111111
```

Some non-regular languages.

- Strings of the form ww for some string w: `beriberi`.
- Unary strings with a composite number of 1s: `111111`.
- Bitstrings with an equal number of 0s and 1s: `01110100`.
- Watson-Crick complemented palindromes: `atttcggaaat`.

Remark. Pattern matching with back-references is intractable.

Summary of pattern-matching algorithms

Programmer.

- Implement substring search via DFA simulation.
- Implement RE pattern matching via NFA simulation.

Theoretician.

- RE is a compact description of a set of strings.
- NFA is an abstract machine equivalent in power to RE.
- DFAs, NFAs, and REs have limitations.

You. Practical application of core computer science principles.

Example of essential paradigm in computer science.

- Build intermediate abstractions.
- Pick the right ones!
- Solve important practical problems.

Context

Abstract machines, languages, and nondeterminism.

- Basis of the theory of computation.
- Intensively studied since the 1930s.
- Basis of programming languages.

Compiler. A program that translates a program to machine code.

- KMP string ⇒ DFA.
- `grep` RE ⇒ NFA.
- `javac` Java language ⇒ Java byte code.

	KMP	grep	Java
pattern	string	RE	program
parser	unnecessary	check if legal	check if legal
compiler output	DFA	NFA	byte code
simulator	DFA simulator	NFA simulator	JVM

Regular expressions in other languages

Broadly applicable programmer's tool.

- Originated in Unix in the 1970s.
- Popularized through early tools developed by Ken Thompson.
- Many languages support extended regular expressions.
- Built into grep, awk, emacs, Perl, PHP, Python, JavaScript, ...

```
% grep 'NEWLINE' */*.java
```

print all lines containing NEWLINE which occurs in any file with a .java extension

```
% egrep '^[qwertyuiop]*[zxcvbnm]*$' words.txt | egrep '..........'
typewritten
```

Some programs produce themselves as output

*Quine.java

```
public class Quine
{
  public static void main( String[] args )
  {
    char q = 34;       // Quotation mark characte
    String[] l = {     // Array of source code
    "public class Quine",
    "{",
    "  public static void main( String[] args )",
```

Console

<terminated> Quine [Java Application] C:\Program Files\Java\jre6\bin\javaw.ex

```
public class Quine
{
  public static void main( String[] args )
  {
    char q = 34;       // Quotation mark character
    String[] l = {     // Array of source code
    "public class Quine",
    "{",
    "  public static void main( String[] args )",
```

What about programs that take themselves as input?

"Reflections on Trusting Trust" - Ken Thompson (1983 Turing lecture)