

# Is Polleverywhere working?

---



Text a **CODE** to **37607**



Submit responses at **PollEv.com/jhug**

Yes

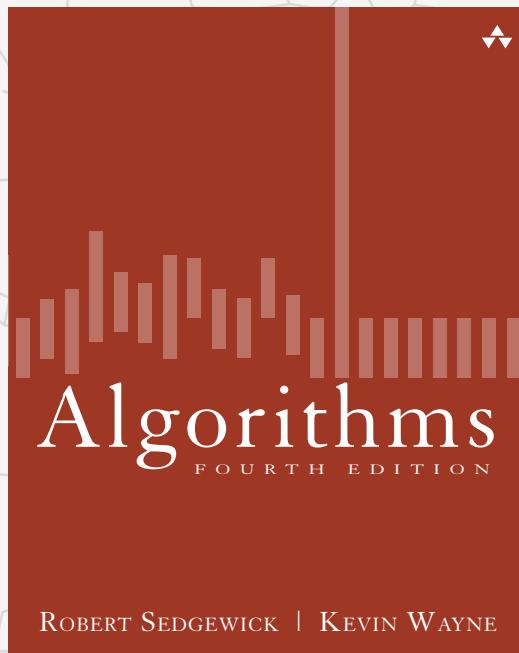
**729760**

No

**729761**



**729762**



## 1.3 BAGS, QUEUES, AND STACKS

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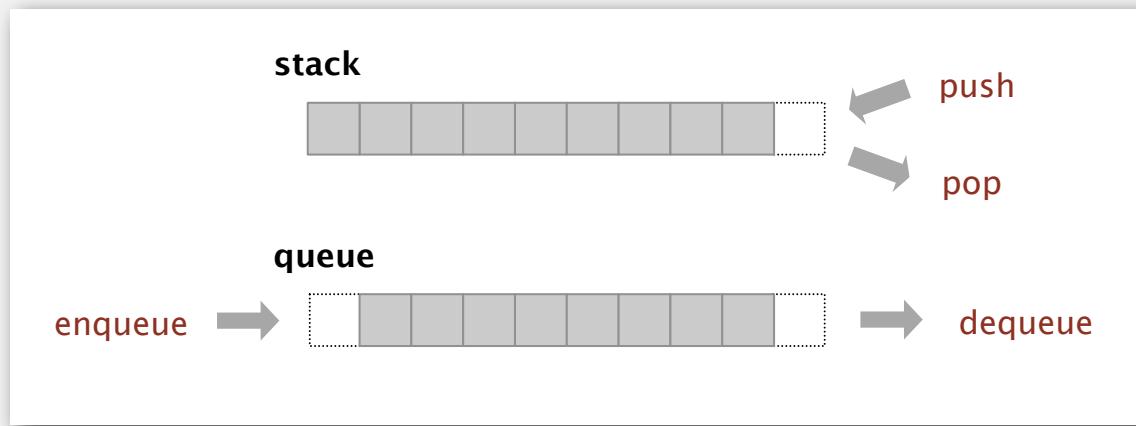
- ▶ *stacks*
- ▶ *resizing arrays*
- ▶ *queues*
- ▶ *generics*
- ▶ *iterators*
- ▶ *applications*

# Stacks and queues

---

## Fundamental data types.

- Collections of objects.
- Operations: **insert**, **remove**, **iterate**, test if empty.
- Intent is clear when we insert.
- Which item do we remove?



**Stack.** Examine the item most recently added. ← LIFO = "last in first out"

**Queue.** Examine the item least recently added. ← FIFO = "first in first out"

# Client, implementation, interface

---

Separate interface and implementation.

Ex: stack, queue, bag, priority queue, symbol table, union-find, ....

Benefits.

- Client can't know details of implementation ⇒ client has many implementation from which to choose.
- Implementation can't know details of client needs ⇒ many clients can re-use the same implementation.
- Design: creates modular, reusable libraries.
- Performance: use optimized implementation where it matters.

**Client:** program using operations defined in interface.

**Implementation:** actual code implementing operations.

**Interface:** description of data type, basic operations.

# Algorithms

ROBERT SEDGEWICK | KEVIN WAYNE

<http://algs4.cs.princeton.edu>

## 1.3 BAGS, QUEUES, AND STACKS

---

- ▶ *stacks*
- ▶ *resizing arrays*
- ▶ *queues*
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- ▶ *applications*

# Stack API

---

Warmup API. Stack of strings data type.

```
public class StackOfStrings
```

```
    StackOfStrings()
```

*create an empty stack*

```
    void push(String item)
```

*insert a new string onto stack*

```
    String pop()
```

*remove and return the string  
most recently added*

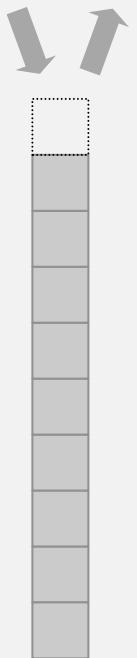
```
    boolean isEmpty()
```

*is the stack empty?*

```
    int size()
```

*number of strings on the stack*

push    pop



Warmup client. Reverse sequence of strings from standard input.

## Stack test client

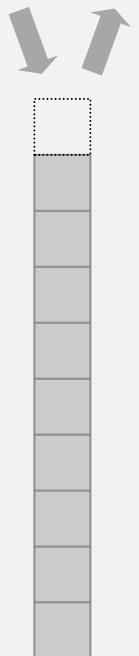
---

Read strings from standard input.

- If string equals "-", pop string from stack and print.
- Otherwise, push string onto stack.

push    pop

```
public static void main(String[] args)
{
    StackOfStrings stack = new StackOfStrings();
    while (!StdIn.isEmpty())
    {
        String s = StdIn.readString();
        if (s.equals("-")) StdOut.print(stack.pop());
        else             stack.push(s);
    }
}
```



```
% more tobe.txt
to be or not to - be - - that - - - is
```

```
% java StackOfStrings < tobe.txt
to be not that or be
```

Q: Which of the following inputs to the stack test client does NOT produce the output 5 4 3 2 1

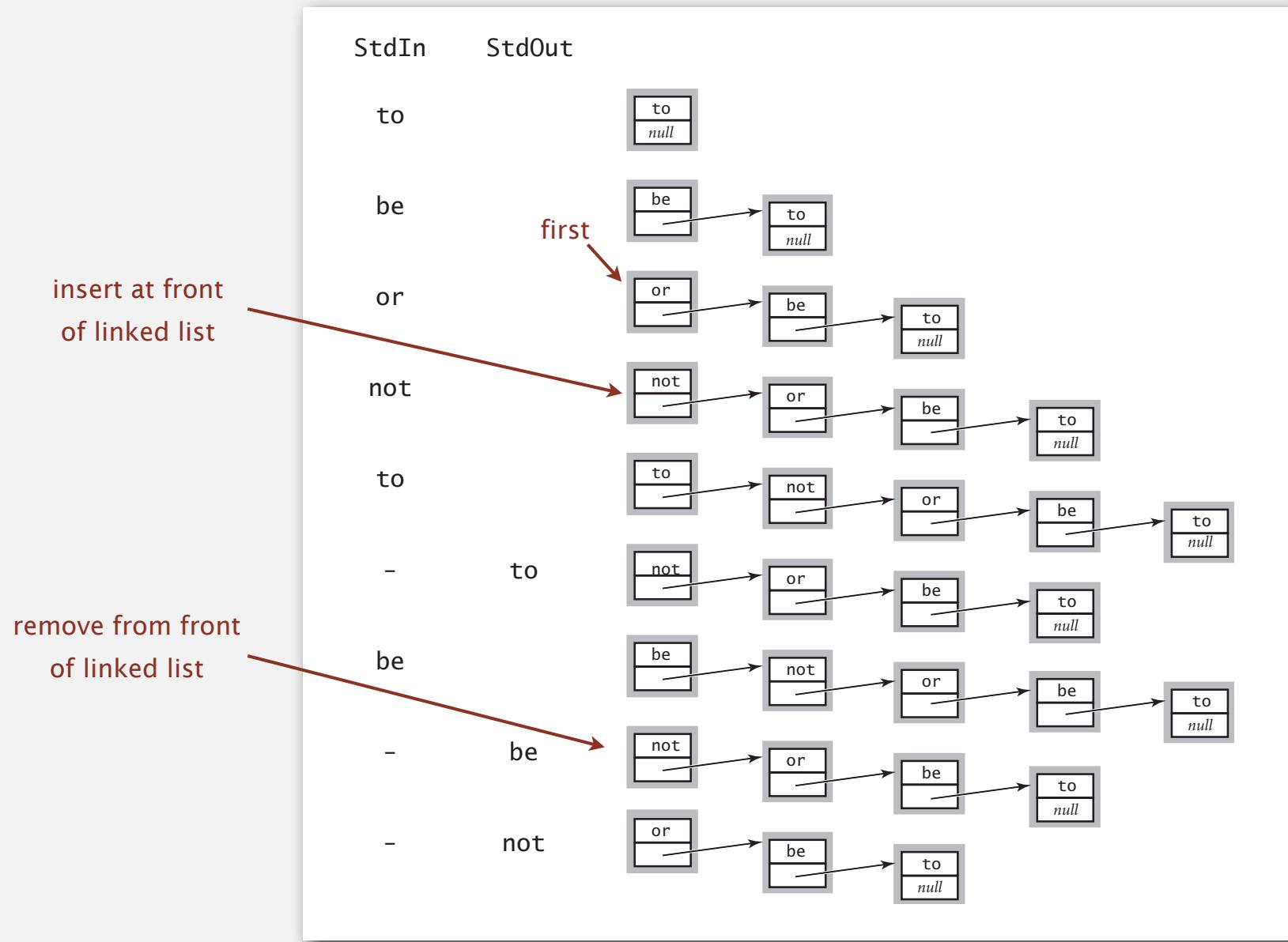
- A. 1 2 3 4 5 - - - - [740669]
- B. 1 2 5 - 3 4 - - - [740670]
- C. 5 - 1 2 3 - 4 - - - [740671]
- D. 5 - 4 - 3 - 2 - 1 - [740672]

```
public static void main(String[] args)
{
    StackOfStrings stack = new StackOfStrings();
    while (!StdIn.isEmpty())
    {
        String s = StdIn.readString();
        if (s.equals("-")) StdOut.print(stack.pop());
        else stack.push(s);
    }
}
```

```
% more tobe.txt
to be or not to - be - - that - - - is
% java StackOfStrings < tobe.txt
to be not that or be
```

# Stack: linked-list representation

Maintain pointer to first node in a linked list; insert/remove from front.



# Stack pop: linked-list implementation

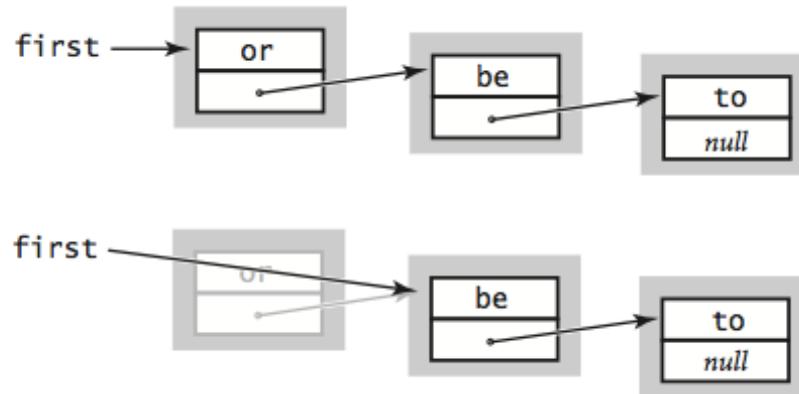
```
inner class  
private class Node  
{  
    String item;  
    Node next;  
}
```

```
public String pop() {
```

**save item to return**

```
    String item = first.item;
```

**delete first node**



```
    first = first.next;
```

**return saved item**

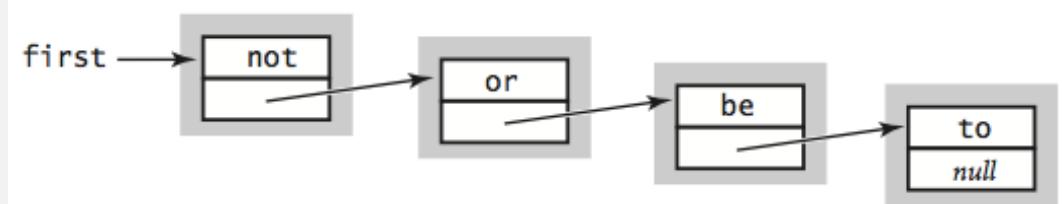
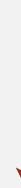
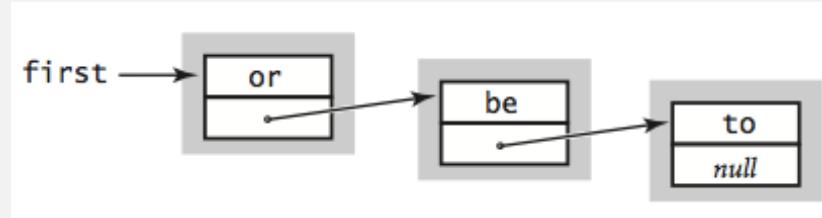
```
    return item;
```

```
}
```

# Stack push: linked-list implementation

inner class

```
private class Node  
{  
    String item;  
    Node next;  
}
```



```
public void push(String item) {  
    Node oldFirst = first;  
    first = new Node();  
    first.next = oldFirst;  
    first.item = item;  
}
```

# Stack: linked-list implementation in Java

```
public class LinkedStackOfStrings
{
    private Node first = null;

    private class Node
    {
        String item;
        Node next;
    }

    public boolean isEmpty()
    { return first == null; }

    public void push(String item)
    {
        Node oldfirst = first;
        first = new Node();
        first.item = item;
        first.next = oldfirst;
    }

    public String pop()
    {
        String item = first.item;
        first = first.next;
        return item;
    }
}
```

private inner class  
(access modifiers don't matter)

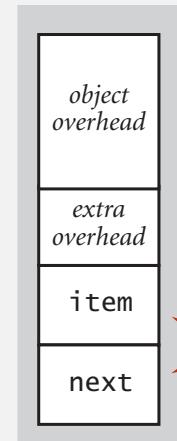
# Stack: linked-list implementation performance

---

Proposition. Every operation takes constant time in the worst case.

Proposition. A stack with  $N$  items uses  $\sim 40N$  bytes.

```
public class LinkedStackOfStrings
{
    private Node first = null;
    inner class
    private class Node
    {
        String item;
        Node next;
    }
}
```



16 bytes (object overhead)

8 bytes (inner class extra overhead)

8 bytes (reference to String)

8 bytes (reference to Node)

---

40 bytes per stack node

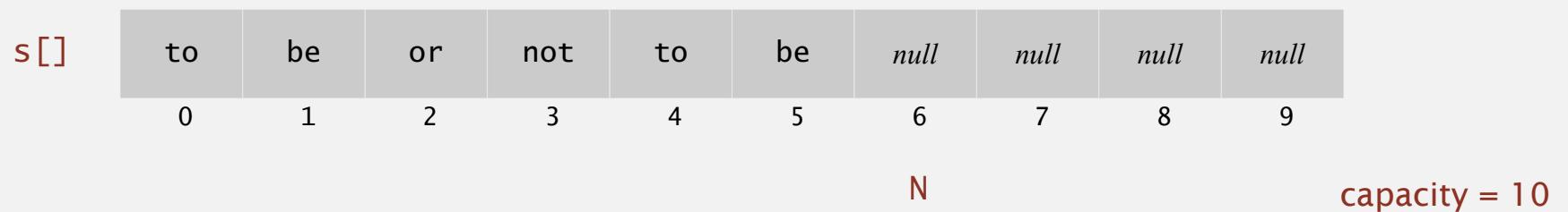
Remark. This accounts for the memory for the stack  
(but not the memory for strings themselves, which the client owns).

# Stack: array implementation

---

## Array implementation of a stack.

- Use array  $s[]$  to store  $N$  items on stack.
- $\text{push}()$ : add new item at  $s[N]$ .
- $\text{pop}()$ : remove item from  $s[N-1]$ .



Defect. Stack overflows when  $N$  exceeds capacity. [stay tuned]

# Stack: array implementation

```
public class FixedCapacityStackOfStrings
{
    private String[] s;
    private int N = 0; //# items on stack

    public FixedCapacityStackOfStrings(int capacity) {
        s = new String[capacity];
    }

    public boolean isEmpty() {
        return N == 0;
    }

    public void push(String item) {
        s[N++] = item; //some consider this bad style
    }

    public String pop() {
        N--;
        String item = s[N]; //these two lines
        s[N] = null; //prevent loitering
        return item; //so do something similar
    }
}
```

a cheat  
(stay tuned)

# Stack considerations

---

## Overflow and underflow.

- Underflow: might want to throw exception if pop from an empty stack.
- Overflow: use resizing array for array implementation. [stay tuned]

Null items. We allow null items to be inserted.

Loitering. Holding a reference to an object when it is no longer needed.

```
public String pop()
{   return s[--N]; }
```

loitering

```
public String pop()
{
    String item = s[--N];
    s[N] = null;
    return item;
}
```

this version avoids "loitering":  
garbage collector can reclaim memory  
only if no outstanding references

# Algorithms

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## 1.3 BAGS, QUEUES, AND STACKS

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- ▶ *stacks*
- ▶ *resizing arrays*
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## Stack: resizing-array implementation

---

**Problem.** Requiring client to provide capacity does not implement API!

**Q.** How to grow and shrink array?

**First try.**

- `push()`: increase size of array `s[]` by 1.
- `pop()`: decrease size of array `s[]` by 1.

**Too expensive.**

- Need to copy all items to a new array.
- Inserting first  $N$  items takes time proportional to  $1 + 2 + \dots + N \sim N^2 / 2$ .

  
infeasible for large  $N$

**Challenge.** Ensure that array resizing happens infrequently.

# Stack: resizing-array implementation

Q. How to grow array?

A. If array is full, create a new array of **twice** the size, and copy items.

```
public ResizingArrayStackOfStrings()
{   s = new String[1]; }

public void push(String item)
{
    if (N == s.length) resize(2 * s.length);
    s[N++] = item;
}

private void resize(int capacity)
{
    String[] copy = new String[capacity];
    for (int i = 0; i < N; i++)
        copy[i] = s[i];
    s = copy;
}
```

"repeated doubling"

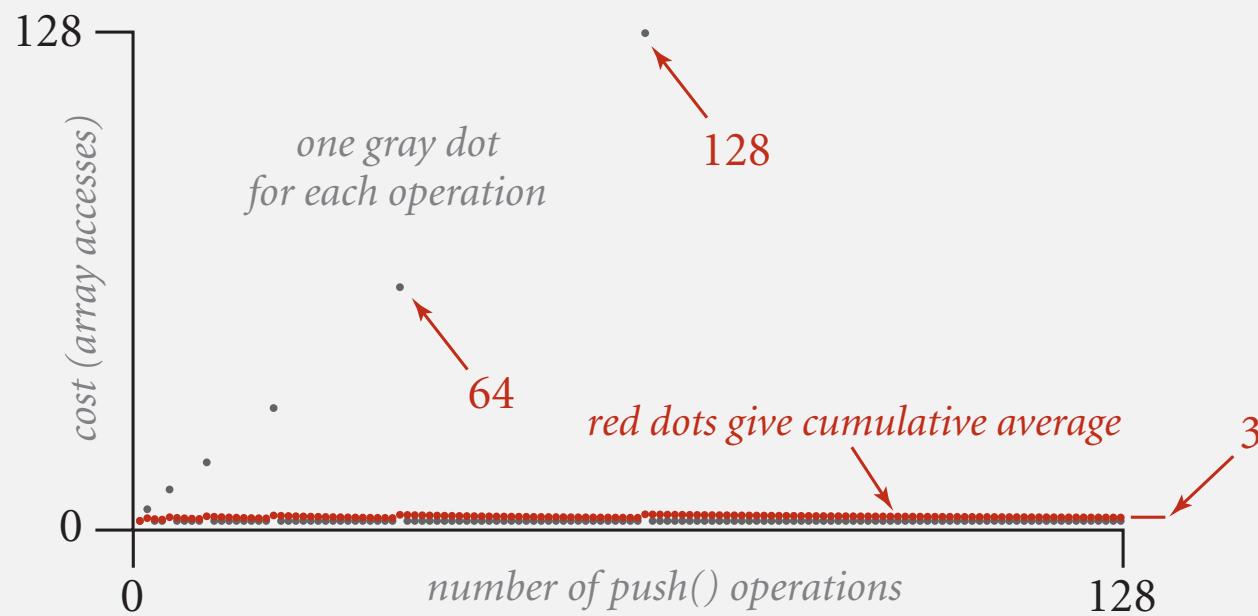
see next slide

Consequence. Inserting first  $N$  items takes time proportional to  $N$  (not  $N^2$ ).

# Stack: amortized cost of adding to a stack

Cost of inserting first  $N$  items.  $N + (2 + 4 + 8 + \dots + N) \sim 3N.$

↑  
1 array access  
per push                    ↑  
k array accesses to double to size k  
(ignoring cost to create new array)



# Stack: resizing-array implementation

---

Q. How to shrink array?

First try.

- `push()`: double size of array `s[]` when array is full.
- `pop()`: halve size of array `s[]` when array is **one-half full**.

Too expensive in worst case.

- Consider push-pop-push-pop-... sequence when array is full.
- Each operation takes time proportional to  $N$ .

$N = 5$	to	be	or	not	to	null	null	null
---------	----	----	----	-----	----	------	------	------

$N = 4$	to	be	or	not				
---------	----	----	----	-----	--	--	--	--

$N = 5$	to	be	or	not	to	null	null	null
---------	----	----	----	-----	----	------	------	------

$N = 4$	to	be	or	not				
---------	----	----	----	-----	--	--	--	--

# Stack: resizing-array implementation

---

Q. How to shrink array?

Efficient solution.

- `push()`: double size of array `s[]` when array is full.
- `pop()`: halve size of array `s[]` when array is **one-quarter full**.

```
public String pop()
{
    String item = s[--N];
    s[N] = null;
    if (N > 0 && N == s.length/4) resize(s.length/2);
    return item;
}
```

Invariant. Array is between 25% and 100% full.

# Stack: resizing-array implementation trace

push()	pop()	N	a.length	0	1	2	3	4	5	6	7	a[]
		0	1	null								
to		1	1	to								
be		2	2	to	be							
or		3	4	to	be	or						
not		4	4	to	be	or	not					
to		5	8	to	be	or	not	to				
-	to	4	8	to	be	or	not	null				
be		5	8	to	be	or	not	be				
-	be	4	8	to	be	or	not	null				
-	not	3	8	to	be	or	null	null				
that		4	8	to	be	or	that	null				
-	that	3	8	to	be	or	null	null				
-	or	2	4	to	be	null	null					
-	be	1	2	to	null							
is		2		to	is							

Trace of array resizing during a sequence of push() and pop() operations

## Stack resizing-array implementation: performance

Amortized analysis. Starting from an empty data structure, average running time per operation over a worst-case sequence of operations.

Proposition. Starting from an empty stack, any sequence of  $M$  push and pop operations takes time proportional to  $M$ .

	best	worst	amortized
construct	1	1	1
push	1	$N$	1
pop	1	$N$	1
size	1	1	1

order of growth of running time  
for resizing stack with  $N$  items

doubling and  
halving operations

## Stack resizing-array implementation: memory

Invariant. Array is between 25% and 100% full.

```
public class ResizingArrayStackOfStrings
{
    private String[] s;
    private int N = 0;
    ...
}
```

8 bytes (reference to array)  
24 bytes (array overhead)  
8 bytes × array size  
4 bytes (int)  
4 bytes (padding)

pollEv.com/jhug

text to 37607

Q: If the array is completely full, how many bytes does the stack use to store N strings? Give your answer in Tilde notation.

- |                       |                             |
|-----------------------|-----------------------------|
| A. ~N bytes [740928]  | D. ~16N bytes [740931]      |
| B. ~4N bytes [740929] | E. ~32N bytes [740932]      |
| C. ~8N bytes [740930] | F. ~16N + 40 bytes [740933] |

Do not count the memory used to store the actual strings, only count the references.

## Stack resizing-array implementation: memory

Invariant. Array is between 25% and 100% full.

```
public class ResizingArrayStackOfStrings
{
    private String[] s;
    private int N = 0;
    ...
}
```

8 bytes (reference to array)  
24 bytes (array overhead)  
8 bytes x array size  
4 bytes (int)  
4 bytes (padding)

pollEv.com/jhug

text to 37607

Q: If  $N$  is the number of strings in the stack, how much memory does a `ResizingArrayStackOfStrings` use in the **worst** case as a function of  $N$ ? Give your answer in Tilde notation.

- |                             |                                   |
|-----------------------------|-----------------------------------|
| A. $\sim N$ bytes [740966]  | D. $\sim 16N$ bytes [740969]      |
| B. $\sim 4N$ bytes [740967] | E. $\sim 32N$ bytes [740970]      |
| C. $\sim 8N$ bytes [740968] | F. $\sim 16N + 40$ bytes [740971] |

As before, don't count the memory of the actual strings, just references.

## Stack resizing-array implementation: memory usage

**Proposition.** Uses between  $\sim 8N$  and  $\sim 32N$  bytes to represent a stack with  $N$  items.

- $\sim 8N$  when full.
- $\sim 32N$  when one-quarter full.

```
public class ResizingArrayStackOfStrings
{
    private String[] s;
    private int N = 0;
    ...
}
```

8 bytes (reference to array)  
24 bytes (array overhead)  
8 bytes × array size  
4 bytes (int)  
4 bytes (padding)

**Invariant.** Array is between 25% and 100% full.

**Remark.** This accounts for the memory for the stack (but not the memory for strings themselves, which the client owns).

# Stack implementations: resizing array vs. linked list

---

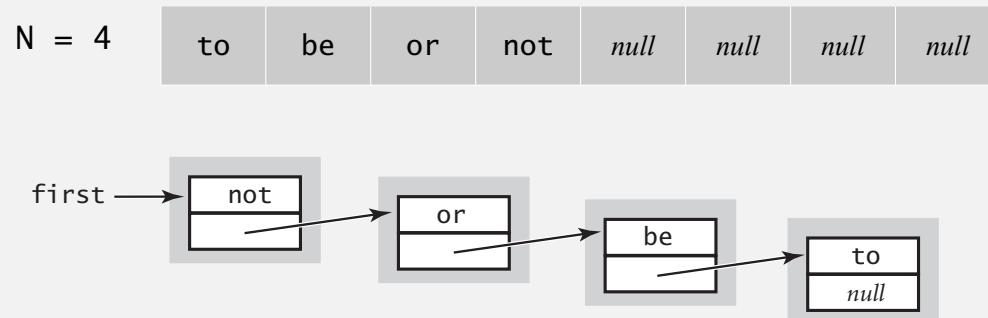
**Tradeoffs.** Can implement a stack with either resizing array or linked list; client can use interchangeably. Which one is better?

## Linked-list implementation.

- Every operation takes constant time in the **worst case**.
- Uses extra time and space to deal with the links.

## Resizing-array implementation.

- Every operation takes constant **amortized** time.
- Less wasted space.



# Algorithms

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## 1.3 BAGS, QUEUES, AND STACKS

---

- ▶ *stacks*
- ▶ *resizing arrays*
- ▶ *queues*
- ▶ *generics*
- ▶ *iterators*
- ▶ *applications*

# Queue API

```
public class QueueOfStrings
```

```
    QueueOfStrings()
```

*create an empty queue*

```
    void enqueue(String item)
```

*insert a new string onto queue*

```
    String dequeue()
```

*remove and return the string  
least recently added*

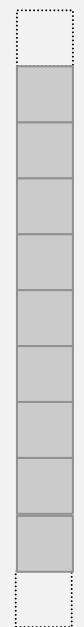
```
    boolean isEmpty()
```

*is the queue empty?*

```
    int size()
```

*number of strings on the queue*

enqueue

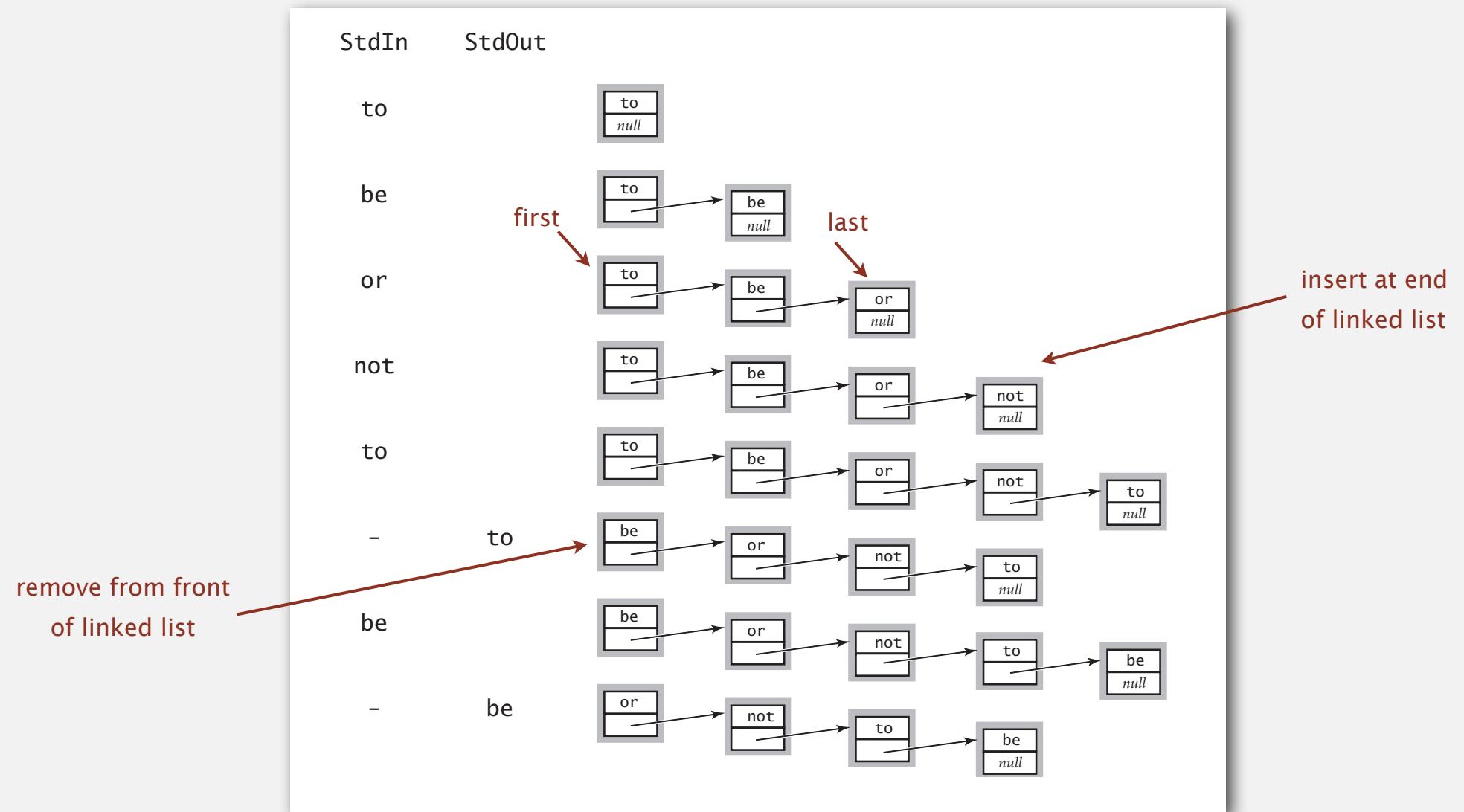


dequeue



# Queue: linked-list representation

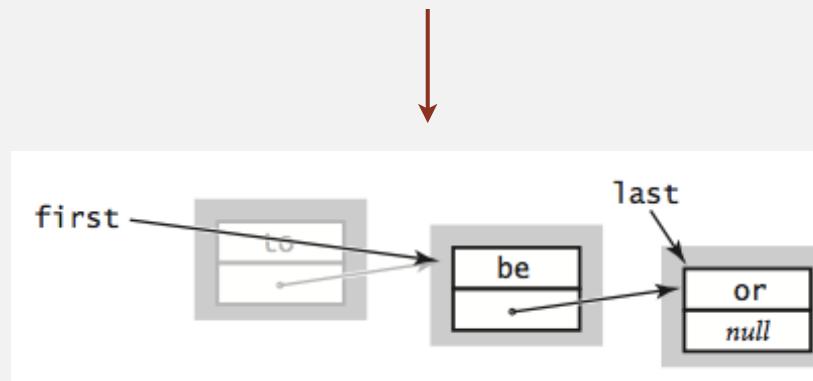
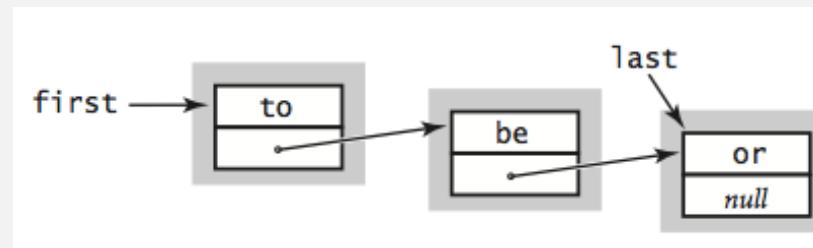
Maintain pointer to first and last nodes in a linked list;  
insert/remove from opposite ends.



# Queue dequeue: linked-list implementation

inner class

```
private class Node  
{  
    String item;  
    Node next;  
}
```

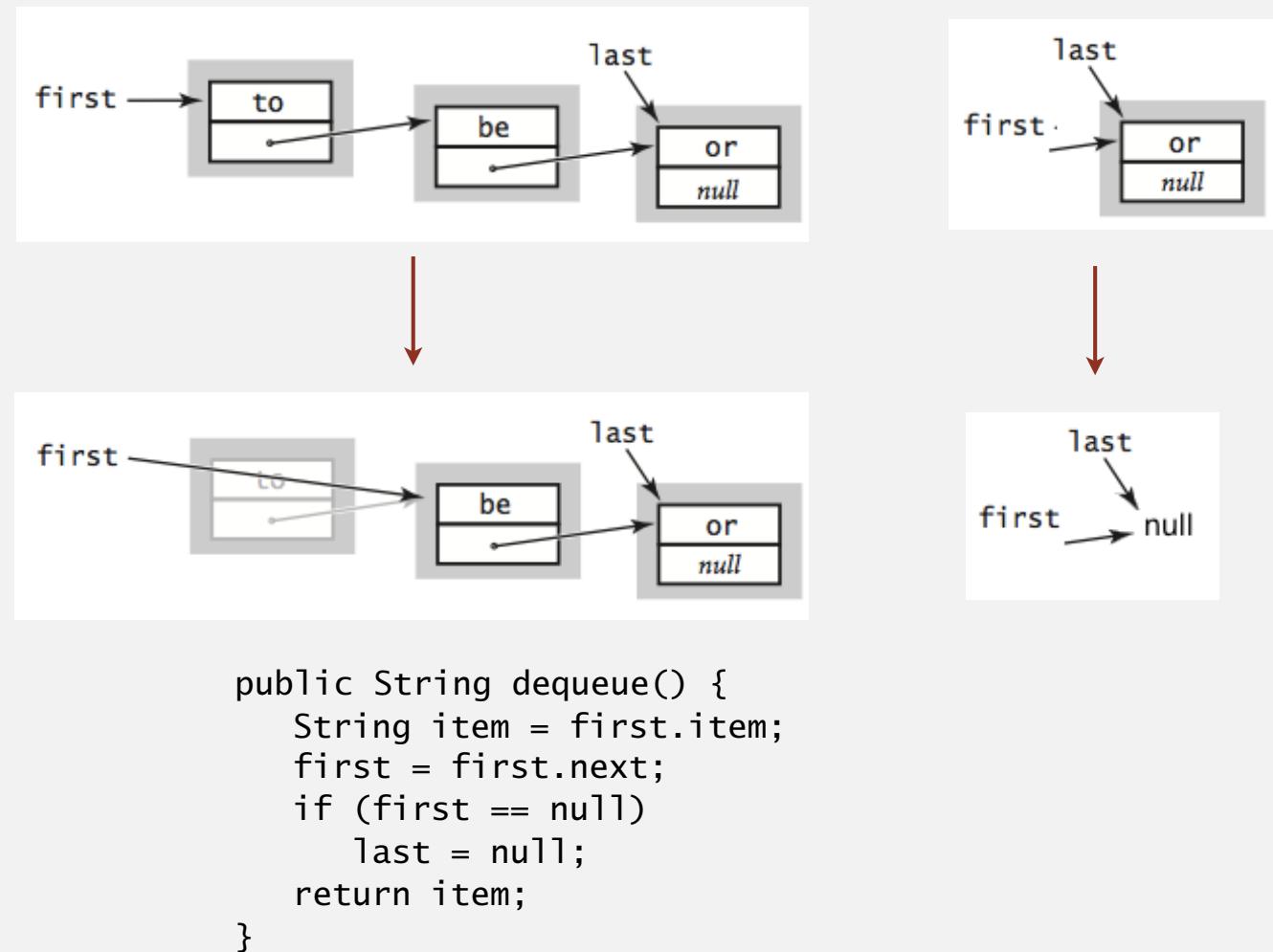


```
public String dequeue() {  
    String item = first.item;  
    first = first.next;  
    return item;  
}
```

# Queue dequeue: linked-list implementation

inner class

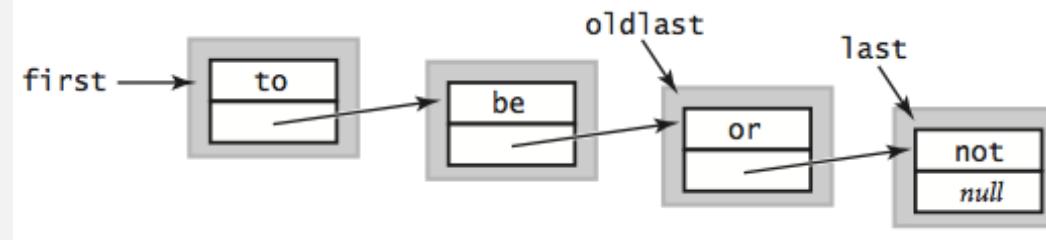
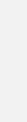
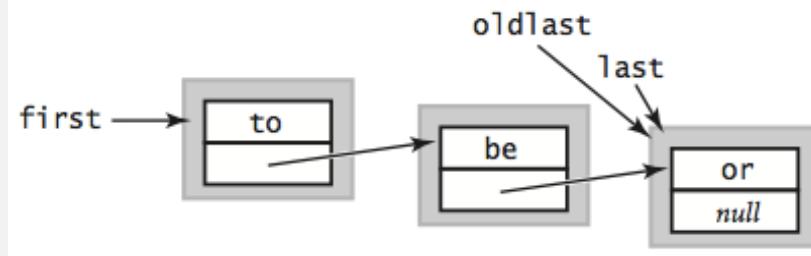
```
private class Node  
{  
    String item;  
    Node next;  
}
```



# Queue enqueue: linked-list implementation

inner class

```
private class Node  
{  
    String item;  
    Node next;  
}
```

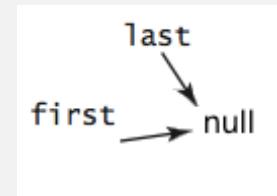
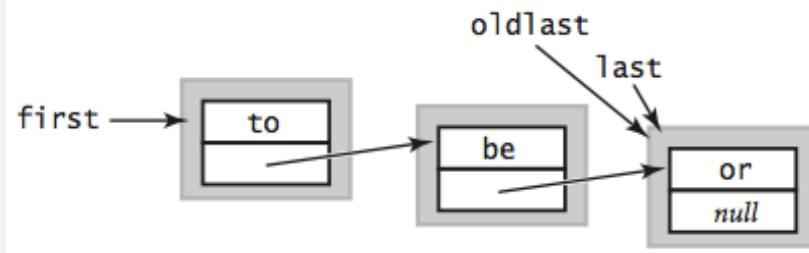


```
public void enqueue(String item) {  
    Node oldLast = last;  
    last = new Node();  
    last.item = item;  
    oldLast.next = last;  
}
```

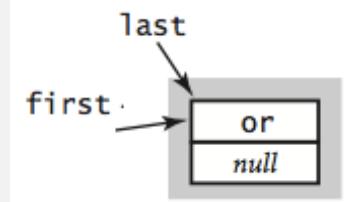
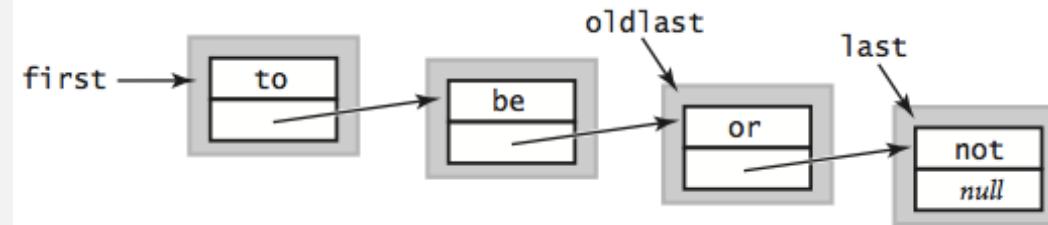
# Queue enqueue: linked-list implementation

inner class

```
private class Node  
{  
    String item;  
    Node next;  
}
```



```
public void enqueue(String item) {  
    Node oldLast = last;  
    last = new Node();  
    last.item = item;  
    if (first == null)  
        first = last;  
    else //to avoid null pointer  
        oldLast.next = last;  
}
```



# Queue: linked-list implementation in Java

```
public class LinkedQueueOfStrings
{
    private Node first, last;

    private class Node
    { /* same as in LinkedStackOfStrings */ }

    public boolean isEmpty()
    { return first == null; }

    public void enqueue(String item)
    {
        Node oldlast = last;
        last = new Node();
        last.item = item;
        last.next = null;
        if (isEmpty()) first = last;
        else          oldlast.next = last;
    }

    public String dequeue()
    {
        String item = first.item;
        first      = first.next;
        if (isEmpty()) last = null;
        return item;
    }
}
```

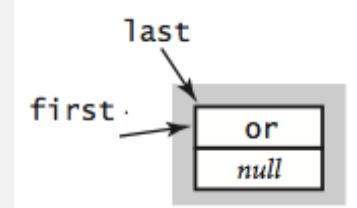
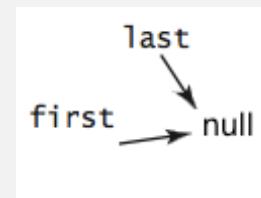
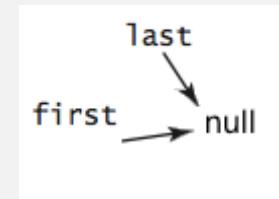
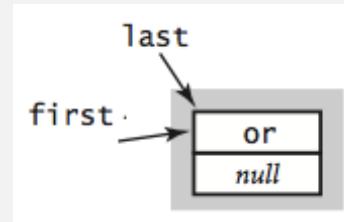
special cases for  
empty queue

# Sentinel nodes

---

## Annoying Cases.

- Enqueueing on an empty list.
- Dequeueing to an empty list.



## Solutions

- Write special case code.
- Create a node that can never be removed (sentinel node).
  - Always first in line.
  - Never gets to leave the line.
  - The queue is considered empty if sentinel is the only item.

# Sentinel nodes

---

## Annoying Cases.

- Going to/from to empty list.

## Solutions

- Use an if statement.
- Never allow an empty list.
  - Create a single dummy node.
  - Null pointer if dequeue on empty list.
- Never allow a null pointer.
  - Create two dummy nodes.
  - Have back dummy node point backwards.
  - “dummy node” returned if dequeue on empty list.

```
public class LinkedQueueOfStrings
{
    private Node sentinel, last;

    public LinkedQueueOfStrings {
        sentinel = new Node();
        sentinel.item = "dummy node";
        last = sentinel;
    }

    public boolean isEmpty()
    { return sentinel == last; }

    public void enqueue(String item)
    {
        Node oldLast = last;
        last = new Node();
        last.item = item;
        oldLast.next = last;
    }

    public String dequeue()
    {
        String item = sentinel.next.item;
        sentinel.next = sentinel.next.next;
        return item;
    }
}
```

# Queue: resizing array implementation

---

## Array implementation of a queue.

- Use array `q[]` to store items in queue.
- `enqueue()`: add new item at `q[tail]`.
- `dequeue()`: remove item from `q[head]`.
- Update head and tail modulo the capacity.
- Add resizing array.



Q. How to resize?

# Algorithms

ROBERT SEDGEWICK | KEVIN WAYNE

<http://algs4.cs.princeton.edu>

## 1.3 BAGS, QUEUES, AND STACKS

---

- ▶ *stacks*
- ▶ *resizing arrays*
- ▶ *queues*
- ▶ *generics*
- ▶ *iterators*
- ▶ *applications*

# Parameterized stack

---

We implemented: StackOfStrings.

We also want: StackOfURLs, StackOfInts, StackOfVans, ....

Attempt 1. Implement a separate stack class for each type.

- Rewriting code is tedious and error-prone.
- Maintaining cut-and-pasted code is tedious and error-prone.

@#\$\*! most reasonable approach until Java 1.5.



# Parameterized stack

We implemented: StackOfStrings.

We also want: StackOfURLs, StackOfInts, StackOfVans, ....

Attempt 2. Implement a stack with items of type Object.

- Casting is required in client.
- Casting is error-prone: run-time error if types mismatch.

```
StackOfObjects s = new StackOfObjects();
Apple a = new Apple();
Orange b = new Orange();
s.push(a);
s.push(b);
a = (Apple) (s.pop());
```

run-time error



## Parameterized stack

---

We implemented: StackOfStrings.

We also want: StackOfURLs, StackOfInts, StackOfVans, ....

Attempt 3. Java generics.

- Avoid casting in client.
- Discover type mismatch errors at compile-time instead of run-time.

```
Stack<Apple> s = new Stack<Apple>();
Apple a = new Apple();
Orange b = new Orange();
s.push(a);
s.push(b);
a = s.pop();
```

type parameter

compile-time error

Guiding principles. Welcome compile-time errors; avoid run-time errors.

# Generic stack: linked-list implementation

```
public class LinkedStackOfStrings
{
    private Node first = null;

    private class Node
    {
        String item;
        Node next;
    }

    public boolean isEmpty()
    {   return first == null;   }

    public void push(String item)
    {
        Node oldfirst = first;
        first = new Node();
        first.item = item;
        first.next = oldfirst;
    }

    public String pop()
    {
        String item = first.item;
        first = first.next;
        return item;
    }
}
```

```
public class Stack<Item>
{
    private Node first = null;

    private class Node
    {
        Item item;
        Node next;
    }

    public boolean isEmpty()
    {   return first == null;   }

    public void push(Item item)
    {
        Node oldfirst = first;
        first = new Node();
        first.item = item;
        first.next = oldfirst;
    }

    public Item pop()
    {
        Item item = first.item;
        first = first.next;
        return item;
    }
}
```

generic type name

# Generic stack: array implementation

```
public class FixedCapacityStackOfStrings
{
    private String[] s;
    private int N = 0;

    public ..StackOfStrings(int capacity)
    {   s = new String[capacity];   }

    public boolean isEmpty()
    {   return N == 0;   }

    public void push(String item)
    {   s[N++] = item;   }

    public String pop()
    {   return s[--N];   }
}
```

the way it should be

```
public class FixedCapacityStack<Item>
{
    private Item[] s;
    private int N = 0;

    public FixedCapacityStack(int capacity)
    {   s = new Item[capacity];   }

    public boolean isEmpty()
    {   return N == 0;   }

    public void push(Item item)
    {   s[N++] = item;   }

    public Item pop()
    {   return s[--N];   }
}
```

@#\$\*! generic array creation not allowed in Java

# Generic stack: array implementation

```
public class FixedCapacityStackOfStrings
{
    private String[] s;
    private int N = 0;

    public ..StackOfStrings(int capacity)
    {   s = new String[capacity];   }

    public boolean isEmpty()
    {   return N == 0;   }

    public void push(String item)
    {   s[N++] = item;   }

    public String pop()
    {   return s[--N];   }
}
```

the way it is

```
public class FixedCapacityStack<Item>
{
    private Item[] s;
    private int N = 0;

    public FixedCapacityStack(int capacity)
    {   s = (Item[]) new Object[capacity];   }

    public boolean isEmpty()
    {   return N == 0;   }

    public void push(Item item)
    {   s[N++] = item;   }

    public Item pop()
    {   return s[--N];   }
}
```

the ugly cast

## Unchecked cast

---

```
% javac FixedCapacityStack.java
```

Note: FixedCapacityStack.java uses unchecked or unsafe operations.

Note: Recompile with -Xlint:unchecked for details.

```
% javac -Xlint:unchecked FixedCapacityStack.java
```

FixedCapacityStack.java:26: warning: [unchecked] unchecked cast

found : java.lang.Object[]

required: Item[]

```
    a = (Item[]) new Object[capacity];
```

  ^

1 warning

# Generic data types: autoboxing

---

Q. What to do about primitive types?

Wrapper type.

- Each primitive type has a **wrapper** object type.
- Ex: Integer is wrapper type for int.

Autoboxing. Automatic cast between a primitive type and its wrapper.

```
Stack<Integer> s = new Stack<Integer>();
s.push(17);           // s.push(Integer.valueOf(17));
int a = s.pop();     // int a = s.pop().intValue();
```

Bottom line. Client code can use generic stack for **any** type of data.

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## 1.3 BAGS, QUEUES, AND STACKS

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- ▶ *stacks*
- ▶ *resizing arrays*
- ▶ *queues*
- ▶ *generics*
- ▶ *iterators*
- ▶ *applications*

## Iteration

---

**Question.** How would you print out the contents of the stack without destroying it?

```
public class StackOfStrings
{
    public boolean isEmpty()
    public void push()
    public String pop()
}
```

```
public void printStackOfStrings(StackOfStrings sos) {
}
```

## Iteration

---

**Question.** How would you print out the contents of the stack without destroying it?

```
public class StackOfStrings
{
    public boolean isEmpty()
    public void push()
    public String pop()
}
```

```
public void printStackOfStrings(StackOfStrings sos) {
    StackOfStrings sos2;
    while (sos.isEmpty() == false) {
        String s = sos.pop();
        StdOut.println(s);
        sos2.push(s);
    }
    while (sos2.isEmpty() == false) {
        String s = sos2.pop();
        sos.push(s);
    }
}
```

## Iteration

---

**Question.** How would you print out the contents of the stack without destroying it?

```
public class StackOfStrings
{
    public boolean isEmpty()
    public void push()
    public String pop()
}
```

**Alternate Approach.** Extend the API to support iteration.

```
public class StackOfStrings
{
    public boolean isEmpty()
    public void push()
    public String pop()
    public int startIterating()
    public String getNextString()
    public boolean hasNextString()
}
```

```
StackOfStrings sos = ...;
sos.startIterating();
while (sos.hasNextString())
    System.out.println(
        sos.getNextString());
```

API above doesn't allow nested iteration!

## Iteration

---

**Question.** How would you print out the contents of the stack without destroying it?

```
public class StackOfStrings
{
    public boolean isEmpty()
    public void push()
    public String pop()
}
```

**Java Approach.** Extend the API to support iteration using Iterable interface.

```
public class StackOfStrings
{
    public boolean isEmpty()
    public void push()
    public String pop()
    public Iterator<String> iterator()
}
```

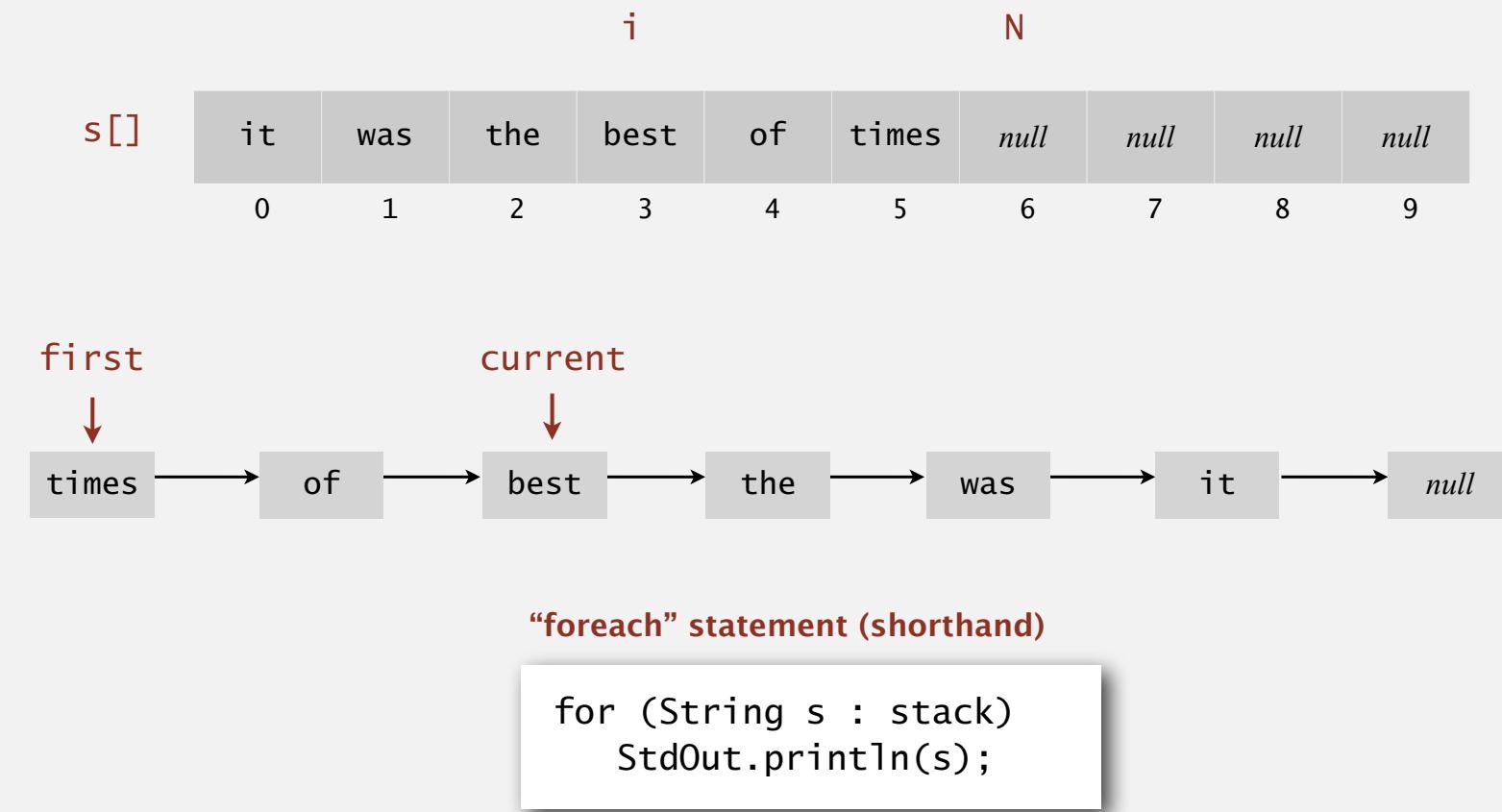
**“foreach” statement (shorthand)**

```
for (String s : stack)
    StdOut.println(s);
```

## Iteration

---

**Design challenge.** Support iteration over stack items by client, without revealing the internal representation of the stack.



**Java solution.** Make stack implement the `java.lang.Iterable` interface.

# Iterators

Q. What is an **Iterable** ?

A. Has a method called `iterator()` that returns an **Iterator**.

**Iterable interface**

```
public interface Iterable<Item>
{
    Iterator<Item> iterator();
}
```

Q. What is an **Iterator** ?

A. Has methods `hasNext()`, `next()` (and `remove()`).

**Iterator interface**

```
public interface Iterator<Item>
{
    boolean hasNext();
    Item next();
    void remove(); ← optional; use
                           at your own risk
}
```

Q. Why make data structures **Iterable** ?

A. Java supports elegant client code.

**“foreach” statement (shorthand)**

```
for (String s : stack)
    StdOut.println(s);
```

**equivalent code (longhand)**

```
Iterator<String> i = stack.iterator();
while (i.hasNext())
{
    String s = i.next();
    StdOut.println(s);
}
```

# Stack iterator: linked-list implementation

```
import java.util.Iterator;

public class Stack<Item> implements Iterable<Item>
{
    ...

    public Iterator<Item> iterator() { return new ListIterator(); }

    private class ListIterator implements Iterator<Item>
    {
        private Node current;

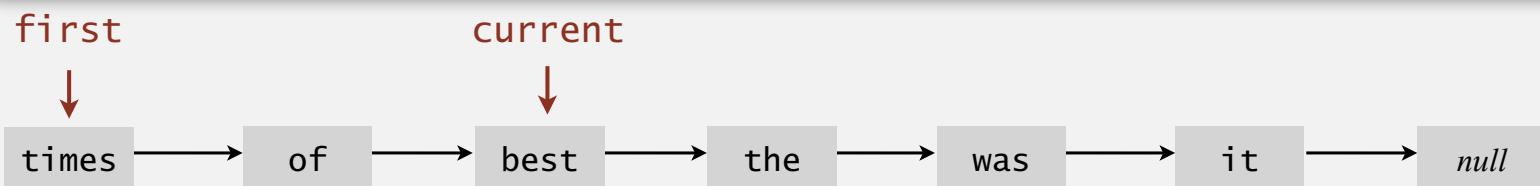
        public ListIterator() { current = first; }

        public boolean hasNext() { return current != null; }

        public void remove() { /* not supported */ }

        public Item next()
        {
            Item item = current.item;
            current = current.next;
            return item;
        }
    }
}
```

throw UnsupportedOperationException  
throw NoSuchElementException  
if no more items in iteration



## Stack iterator: array implementation

```
import java.util.Iterator;

public class Stack<Item> implements Iterable<Item>
{
    ...

    public Iterator<Item> iterator()
    { return new ReverseArrayIterator(); }

    private class ReverseArrayIterator implements Iterator<Item>
    {
        private int i;

        public ReverseArrayIterator()
        public boolean hasNext()
        public void remove()      { /* not supported */ }
        public Item next()
    }
}
```



# Algorithms

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## 1.3 BAGS, QUEUES, AND STACKS

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- ▶ *iterators*
- ▶ *applications*

# Java collections library

List interface. `java.util.List` is API for an sequence of items.

<code>public interface List&lt;Item&gt; implements Iterable&lt;Item&gt;</code>	
<code>    List()</code>	<i>create an empty list</i>
<code>    boolean isEmpty()</code>	<i>is the list empty?</i>
<code>    int size()</code>	<i>number of items</i>
<code>    void add(Item item)</code>	<i>append item to the end</i>
<code>    Item get(int index)</code>	<i>return item at given index</i>
<code>    Item remove(int index)</code>	<i>return and delete item at given index</i>
<code>    boolean contains(Item item)</code>	<i>does the list contain the given item?</i>
<code>    Iterator&lt;Item&gt; iterator()</code>	<i>iterator over all items in the list</i>
<code>    ...</code>	

Implementations. `java.util.ArrayList` uses resizing array;

`java.util.LinkedList` uses linked list.

caveat: only some  
operations are efficient

# Java collections library

---

## `java.util.Stack`.

- Supports `push()`, `pop()`, and `iteration`.
- Extends `java.util.Vector`, which implements `java.util.List` interface from previous slide, including `get()` and `remove()`.
- Bloated and poorly-designed API (why?)

### **Java 1.3 bug report (June 27, 2001)**

The iterator method on `java.util.Stack` iterates through a Stack from the bottom up. One would think that it should iterate as if it were popping off the top of the Stack.

### **status (closed, will not fix)**

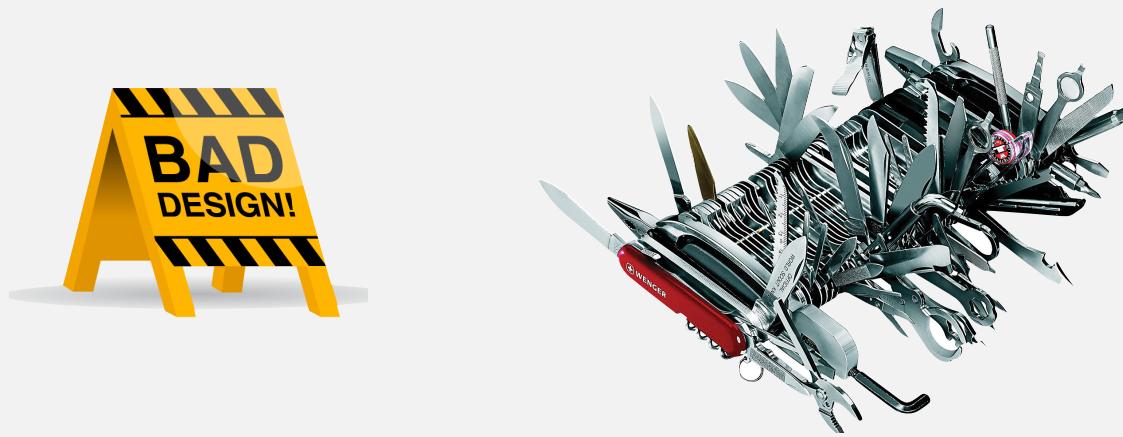
It was an incorrect design decision to have `Stack` extend `Vector` ("is-a" rather than "has-a"). We sympathize with the submitter but cannot fix this because of compatibility.

## Java collections library

---

### `java.util.Stack`.

- Supports push(), pop(), and iteration.
- Extends `java.util.Vector`, which implements `java.util.List` interface from previous slide, including get() and remove().
- Bloated and poorly-designed API (why?)



`java.util.Queue`. An interface, not an implementation of a queue.

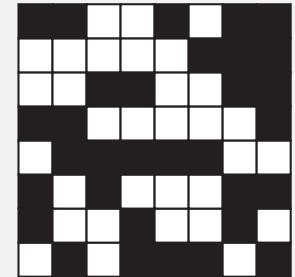
**Best practices.** Use our implementations of Stack, Queue, and Bag.

## War story (from Assignment 1)

---

Generate random open sites in an  $N$ -by- $N$  percolation system.

- Jenny: pick  $(i, j)$  at random; if already open, repeat.  
Takes  $\sim c_1 N^2$  seconds.
- Kenny: create a `java.util.ArrayList` of  $N^2$  closed sites.  
Pick an index at random and delete.  
Takes  $\sim c_2 N^4$  seconds.



Why is my program so slow?



Kenny

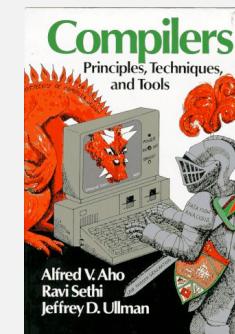
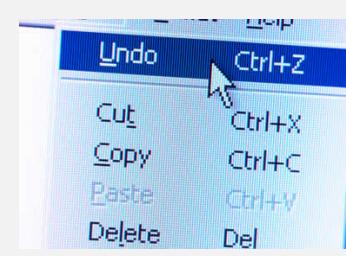
Lesson. Don't use a library until you understand its API!

This course. Can't use a library until we've implemented it in class.

# Stack applications

---

- Parsing in a compiler.
- Java virtual machine.
- Undo in a word processor.
- Back button in a Web browser.
- PostScript language for printers.
- Implementing function calls in a compiler.
- ...



# Function calls

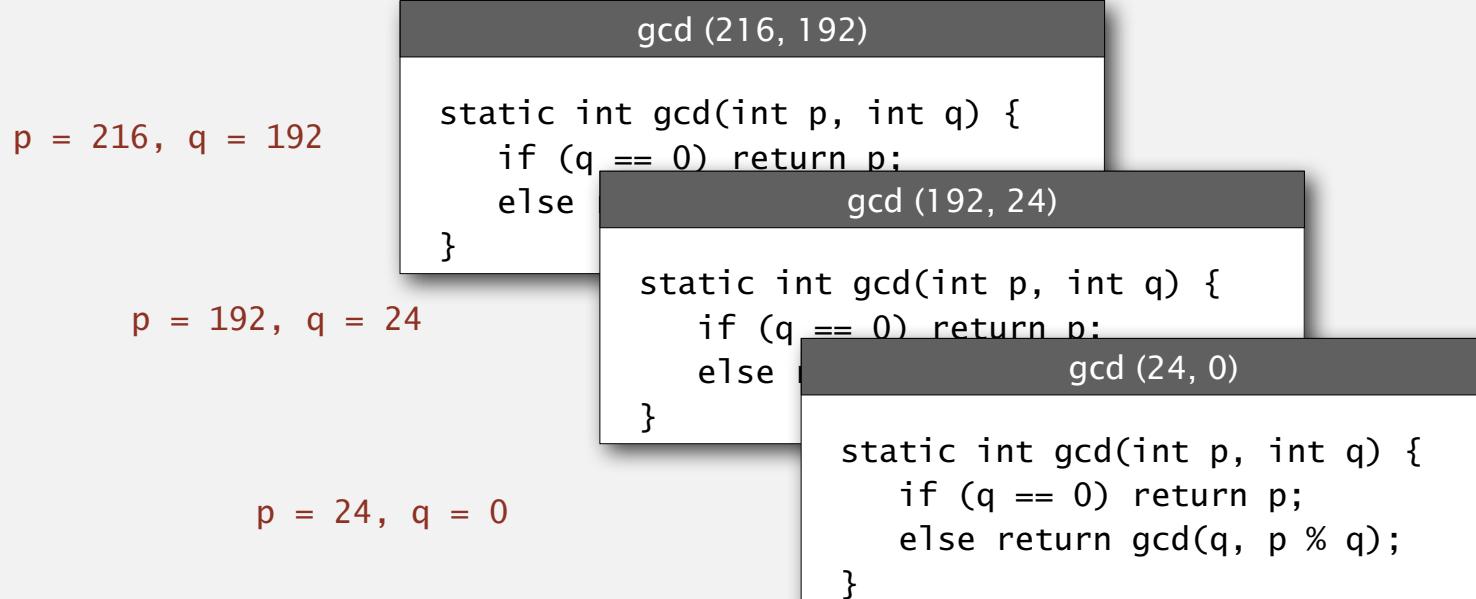
---

How a compiler implements a function.

- Function call: **push** local environment and return address.
- Return: **pop** return address and local environment.

**Recursive function.** Function that calls itself.

**Note.** Can always use an explicit stack to remove recursion.



# Assignment 2

---

## Implementation of two data types

- Randomized queue.
- Deque (double-ended queue).

## Important choice to be made

- Linked list vs. resizing array.
- Think carefully about whether your choice allows you to obey timing constraints!

## Extra credit

- Complete the checkout line simulator.
- Report anything interesting you discover.
- OK to do alone, even if you had a partner.
- Tiny amount of extra credit (1 point).
- No support in office hours.
- OK to ask questions on Piazza or to me directly by email.