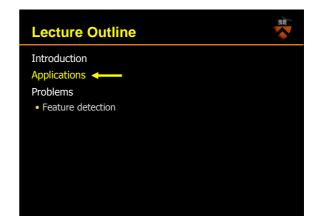


Lecture Outline

Introduction Applications Problems • Feature detection



Applications

Examples:

- Computer graphics
- Geometric modeling
- Archaeology
- Urban planning
- Paleontology
- Molecular bio
- Medicine
- Art

Applications

Examples:

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- > Computer graphics
- Geometric modeling
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Applications

Examples:

- Computer graphics
- ➤ Geometric modeling
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Applications

Examples:

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- Geometric modeling
- > Archaeology
- Urban planning
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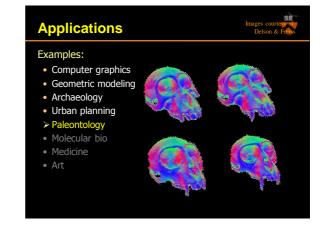
Reconstructing Frescoes from Thera (Weyrich, Brown, Rusinkiewicz, et al.)

Applications

Examples:

- Computer graphics
- Geometric modeling
- Archaeology
- > Urban planning• Paleontology
- Molecular bio
- Medicine

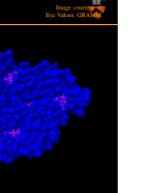




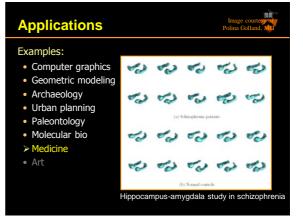
Applications

Examples:

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Applications

Examples:

- Computer graphics
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- ≻ Art

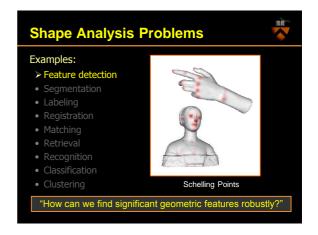


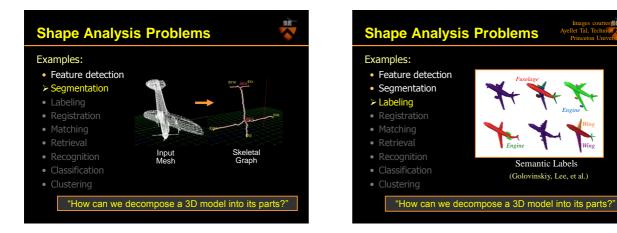
Lecture Outline

Shape Analysis Problems

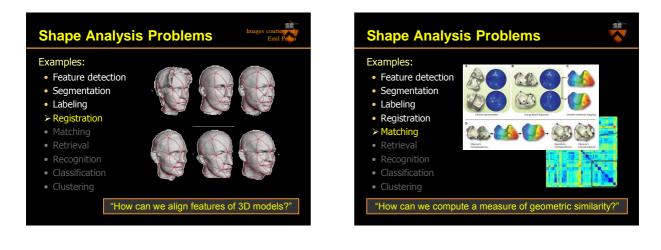
Examples:

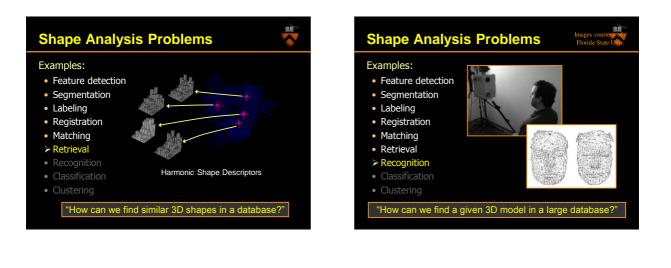
- Feature detection
- Segmentation
- Labeling
- Registration
- Matching
- Recognition
- Classification
- Clustering
- Retrieval

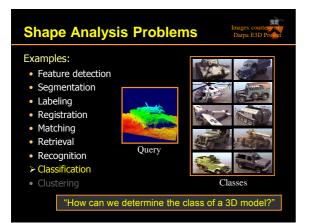


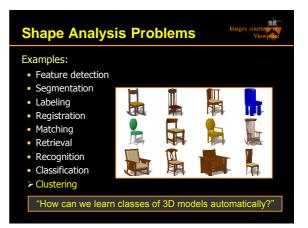


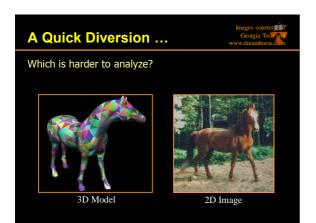
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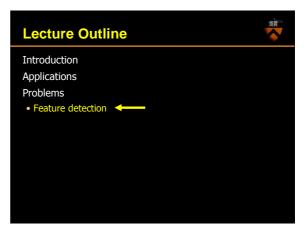


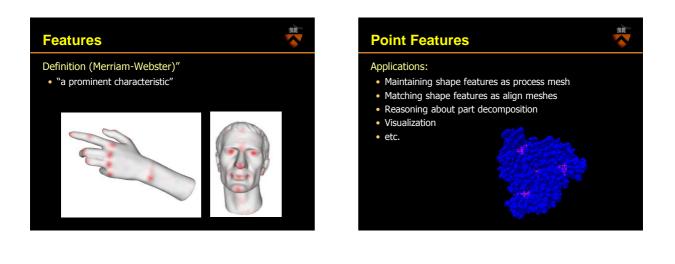










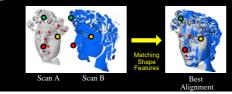


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Point Features

Applications:

- Maintaining shape features as process mesh
- > Matching shape features as align meshes
- Reasoning about part decomposition
- Visualization
- etc.



Point Feature Detection

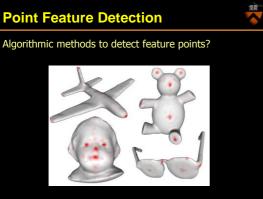
Goals:

- Invariant to transformations
- Robust to small surface deviations (holes, noise, etc.)
- Common across different surfaces in same class
- Semantic?



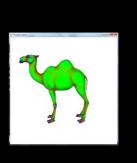
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Point Feature Detection



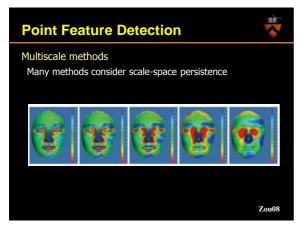
Point Feature Detection

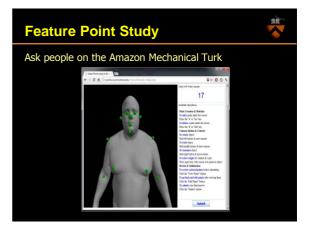
Some relevant properties Average geodesic distance Gauss curvature Differences of curvature Shape diameter function etc.



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Key question

How should we ask people which points are salient?

Key question

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How should we ask people which points are salient?

• "Please select salient points"

Key question

How should we ask people which points are salient?

- "Please select salient points"
- Please select a pattern of points from which another person can recognize the object's class by viewing only those points

Key question

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How should we ask people which points are salient?

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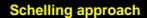
- "Please select salient points"
- Please select a pattern of points from which another person can recognize the object's class by viewing only those points



Key question

How should we ask people which points are salient?

- "Please select salient points"
- Please select a pattern of points from which another person can recognize the object's class by viewing only those points

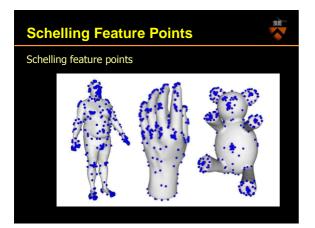


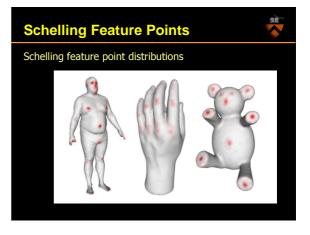
We asked people to:

• Please select points that you think other people will select

Based on the "focal point" theory of [Schelling60]

• A solution that people tend to use in the absence of communication, because it seems natural, special or relevant to them





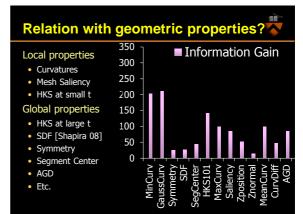
Relation with geometric properties?

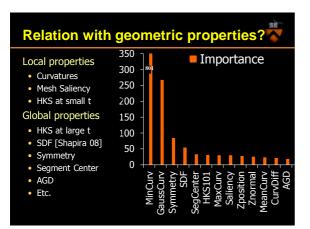
Local properties

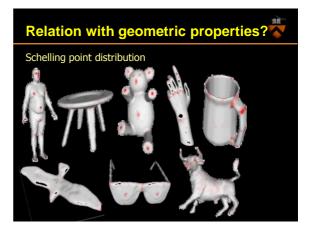
- Curvatures
- Mesh Saliency
- HKS at small t

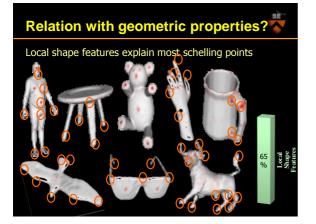
Global properties

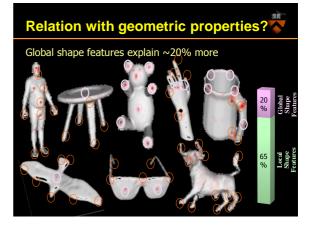
- HKS at large t
- SDF [Shapira 08]
- SymmetrySegment Center
- Segment CenteAGD
- AGL
- Etc.

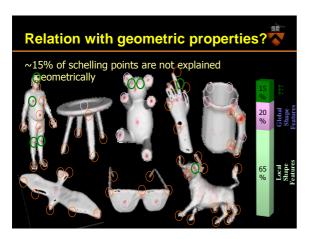


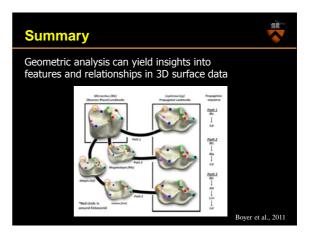




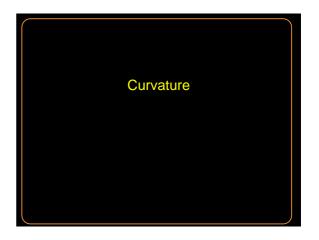


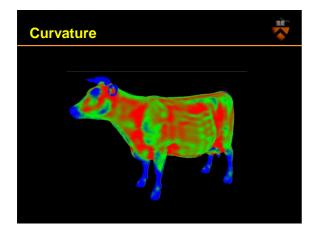


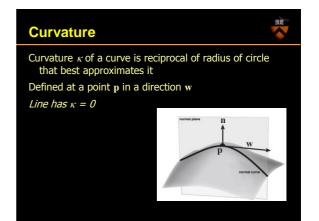






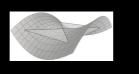




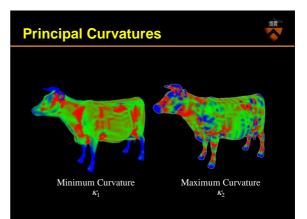


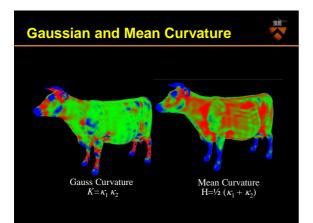
Principal Curvatures

- The curvature at a point varies between some minimum and maximum these are the *principal curvatures* κ_1 and κ_2
- They occur in the *principal directions* d_1 and d_2 which are perpendicular to each other



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What Does Curvature Tell Us?

Planar points:

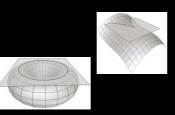
- Zero Gaussian curvature and zero mean curvature
- Tangent plane intersects surface at infinity points

What Does Curvature Tell Us?

Parabolic points:

- Zero Gaussian curvature, non-zero mean curvature
- Tangent plane intersects surface along 1 curves





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What Does Curvature Tell Us?

Elliptical points:

- Positive Gaussian curvature
- Convex/concave depending on sign of mean curvature
- Tangent plane intersects surface at 1 point

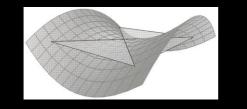


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What Does Curvature Tell Us?

Hyperbolic points:

- Negative Gaussian curvature
- Tangent plane intersects surface along 2 curves



What Does Curvature Tell Us?

Mesh Saliency:

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- Motivated by models of perceptual salience
- Difference between mean curvature blurred with σ and blurred with 2σ



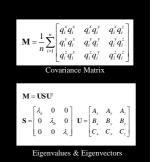
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Principal Component Analysis (PCA)

Principal Component Analysis (PCA)

Tensor voting

- Extract points {q_i} in neighborhood
- Compute covariance
 matrix M
- Analyze eigenvalues and eigenvectors of M (via SVD)
- Eigenvectors are Principal Axes



Principal Component Analysis (PCA)

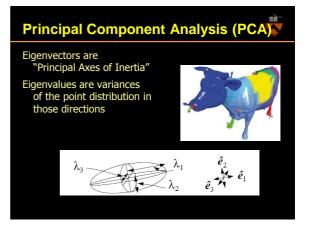
Tensor voting

- Extract points {q_i} in neighborhood
- Compute covariance matrix M
- Analyze eigenvalues and eigenvectors of M (via SVD)



$\mathbf{M} = \mathbf{U}\mathbf{S}\mathbf{U}^{\mathsf{T}}$ $\mathbf{S} = \begin{bmatrix} \lambda_a & 0 & 0\\ 0 & \lambda_b & 0\\ 0 & 0 & \lambda_c \end{bmatrix} \mathbf{U} = \begin{bmatrix} A_a & A_b & A_c \\ B_a & B_b & B_c \\ C_a & C_b & C_c \end{bmatrix}$



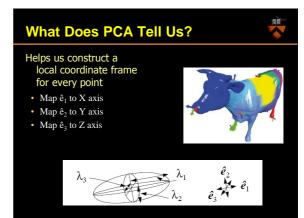


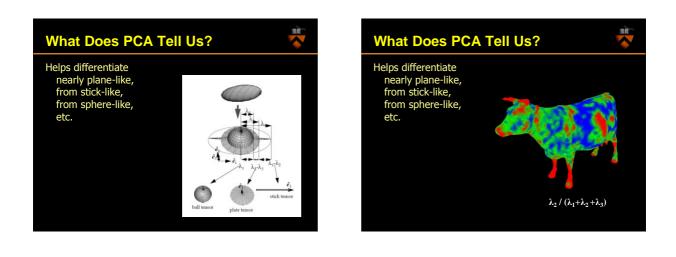
What Does PCA Tell Us?

Provides estimate of normal direction

• Eigenvector (principal axis) associated with smallest eigenvalue







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