## Introduction to

## Motivation

Thomas Funkhouser
Large repositories of 3D data are becoming available


Computer Graphics


Medicine


Cultural Heritage


Molecular Biology


Computer Vision

## Lecture Outline

Introduction
Applications
Problems

- Feature detection


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Introduction
Applications $\longleftarrow$
Problems

- Feature detection


## Applications

Examples:

- Computer graphics
- Geometric modeling
- Archaeology
- Urban planning
- Paleontology
- Molecular bio


## Applications

Examples:
$>$ Computer graphics

- Geometric modeling
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- Medicine
- Art



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Reconstructing Frescoes from Thera (Weyrich, Brown, Rusinkiewicz, et al.)

## Applications

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## Shape Analysis Problems

Examples:

- Feature detection
- Segmentation
- Labeling
- Registration
- Matching
- Recognition
- Classification
- Clustering
- Retrieval


## Shape Analysis Problems

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## Shape Analysis Problems

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"How can we compute a measure of geometric similarity?"



## Shape Analysis Problems

Examples:

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Query


Classes
"How can we determine the class of a 3D model?"

## Shape Analysis Problems

Examples:

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- Classification

$>$ Clustering

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## Features

## Point Features

Applications:

- Maintaining shape features as process mesh
- Matching shape features as align meshes
- Reasoning about part decomposition
- Visualization
- etc.

Point Features杯

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## Point Feature Detection

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## Goals:

- Invariant to transformations
- Robust to small surface deviations (holes, noise, etc.)
- Common across different surfaces in same class
- Semantic?


Point Feature Detection
Algorithmic methods to detect feature points?


## Point Feature Detection

Multiscale methods
Many methods consider scale-space persistence


Zou08


How should we ask people which points are salient?

## Point Feature Detection

 뭇Some relevant properties Average geodesic distance Gauss curvature
Differences of curvature Shape diameter function etc.


Feature Point Study
Ask people on the Amazon Mechanical Turk


## Key question

How should we ask people which points are salient?

- "Please select salient points"


## Key question

## Key question

How should we ask people which points are salient?

- "Please select salient points"
- Please select a pattern of points from which another person can recognize the object's class by viewing only those points

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## Key question



How should we ask people which points are salient?

- "Please select salient points"


## Schelling approach



We asked people to:

- Please select points that you think other people will select

Based on the "focal point" theory of [Schelling60]

- A solution that people tend to use in the absence of communication, because it seems natural, special or relevant to them person can recognize the object's class by viewing only those points



## Schelling Feature Points

Schelling feature points


## Schelling Feature Points

Schelling feature point distributions


Relation with geometric properties?

## Local properties

- Curvatures
- Mesh Saliency
- HKS at small t

Global properties

- HKS at large t
- SDF [Shapira 08]
- Symmetry
- Segment Center
- AGD
- Etc.


## Relation with geometric properties?

## Local properties

- Curvatures
- Mesh Saliency
- HKS at small t Global properties
- HKS at large t
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Relation with geometric properties?


## Relation with geometric properties?



Relation with geometric properties?



## Principal Curvatures



The curvature at a point varies between some minimum and maximum－these are the principal curvatures $\kappa_{1}$ and $\kappa_{2}$
They occur in the principal directions $d_{1}$ and $d_{2}$ which are perpendicular to each other


## Gaussian and Mean Curvature

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Gauss Curvature

$$
K=\kappa_{1} \kappa_{2}
$$



Mean Curvature
$\mathrm{H}=1 / 2\left(\kappa_{1}+\kappa_{2}\right)$

Principal Curvatures $\stackrel{\text { 踶 }}{5}$


Minimum Curvature
$\kappa_{1}$


Maximum Curvature $\kappa_{2}$

## What Does Curvature Tell Us？

Planar points：
－Zero Gaussian curvature and zero mean curvature
－Tangent plane intersects surface at infinity points

## What Does Curvature Tell Us？

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Parabolic points：
－Zero Gaussian curvature，non－zero mean curvature
－Tangent plane intersects surface along 1 curves


## What Does Curvature Tell Us？

## Elliptical points：

－Positive Gaussian curvature
－Convex／concave depending on sign of mean curvature
－Tangent plane intersects surface at 1 point


## What Does Curvature Tell Us?

Hyperbolic points:

- Negative Gaussian curvature
- Tangent plane intersects surface along 2 curves



## What Does Curvature Tell Us?

Mesh Saliency:

- Motivated by models of perceptual salience
- Difference between mean curvature blurred with $\sigma$ and blurred with $2 \sigma$


Principal Component Analysis (PCA)

## Principal Component Analysis (PCA)

Tensor voting

- Extract points $\left\{q_{i}\right\}$ in neighborhood
- Compute covariance matrix M
- Analyze eigenvalues and eigenvectors of M (via SVD)
- Eigenvectors are Principal Axes

$$
\mathbf{M}=\frac{1}{n} \sum_{i=1}^{n}\left[\begin{array}{ccc}
q_{i}^{x} q_{i}^{x} & q_{i}^{x} q_{i}^{y} & q_{i}^{x} q_{i}^{z} \\
q_{i}^{y} q_{i}^{x} & q_{i}^{y} q_{i}^{y} & q_{i}^{y} q_{i}^{z} \\
q_{i}^{z} q_{i}^{x} & q_{i}^{z} q_{i}^{y} & q_{i}^{z} q_{i}^{z}
\end{array}\right]
$$

Covariance Matrix

## $\mathbf{M}=\mathbf{U S U}^{t}$



Eigenvalues \& Eigenvectors

Principal Component Analysis (PCA)
Tensor voting

- Extract points $\left\{q_{i}\right\}$ in neighborhood
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Covariance Matrix


Eigenvalues \& Eigenvectors

Principal Component Analysis (PCA)
Eigenvectors are
"Principal Axes of Inertia"
Eigenvalues are variances of the point distribution in those directions


What Does PCA Tell Us？
Provides estimate of normal direction
－Eigenvector（principal axis）associated with smallest eigenvalue


## What Does PCA Tell Us？

Helps us construct a
local coordinate frame
for every point
－Map $\hat{e}_{1}$ to X axis
－Map $\hat{e}_{2}$ to Y axis
－Map $\hat{e}_{3}$ to Z axis


## What Does PCA Tell Us？

Helps differentiate nearly plane－like， from stick－like， from sphere－like， etc．


## What Does PCA Tell Us？ <br> 装

Helps differentiate nearly plane－like， from stick－like， from sphere－like， etc．



[^0]:    "How can we learn classes of 3D models automatically?"

