

NAME:

login id:

Precept:

## COS 126 Midterm 2 Written Exam Fall 2011

### Solutions

This test has 10 questions, weighted as indicated. The exam is closed book, except that you are allowed to use a one page cheatsheet (double-sided). No calculators or other electronic devices are permitted. Give your answers and show your work in the space provided.

*Print your name, login ID, and precept number on this page (now), and write out and sign the Honor Code pledge before turning in this paper. Note: It is a violation of the Honor Code to discuss this midterm exam question with anyone until after everyone in the class has taken the exam. You have 50 minutes to complete the test.*

*"I pledge my honor that I have not violated the Honor Code during this examination."*

---

*Signature*

1	/3
2	/8
3	/5
4	/9
5	/5
6	/5
7	/8
8	/8
9	/11
10	/8
	/70

1. **Number Systems (3 points).** The following hexadecimal numbers represent 16-bit 2's complement numbers. Put them in order from lowest (most negative) to highest (most positive).

0FFF

F000

1ABC

8888

FFFF

*lowest* 8888

F000

FFFF

0FFF

*highest* 1ABC

**2. Combinational Circuits (8 points).**

A. Complete the following truth table:

x	y	x AND y	x XOR y	x OR y
0	0	0	0	0
0	1	0	1	1
1	0	0	1	1
1	1	1	0	1

B. Mark T if the given Boolean expression is equivalent to  $(x \text{ OR } y)$ . Otherwise, mark F.

  T    $(x \text{ AND } y) \text{ OR } (x \text{ OR } y)$

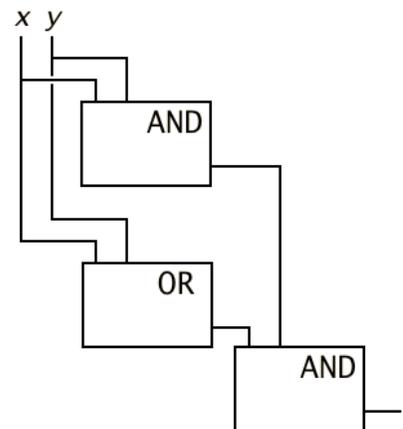
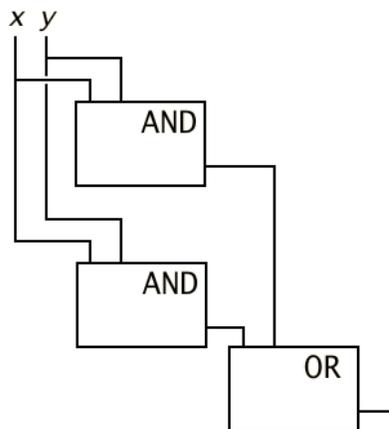
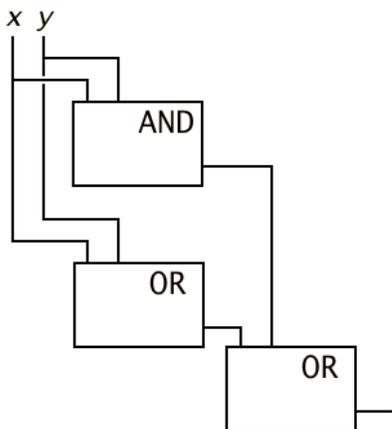
  F    $(x \text{ OR } y) \text{ AND } (x \text{ AND } y)$

  F    $(x \text{ AND } y) \text{ OR } (x \text{ AND } y)$

  T    $(x \text{ OR } y) \text{ OR } x$

B. Circle the one circuit below that computes  $(x \text{ OR } y)$ .

Leftmost



**3. Programming languages (5 points).** Consider the following five sentences.

1. We program a card game in C++ by first building a `Card` object, a `Deck` object and a `Player` object.
2. We declare instance variables to be `final` in Java.
3. We declare instance variables to be `private` in Java.
4. We use a function as an argument to another function in Python.
5. `public class ST<Key extends Comparable <Key>, Value>` implies that whatever data type we select as a `Key` will have a `compareTo()` method.

By writing a number in the blank to the left of each phrase (below), match each of the above sentences with the programming language capability with which it is best associated. Use each number once and only once.

- 2      **A.** Immutability.
- 4      **B.** Functional programming.
- 5      **C.** Interface inheritance.
- 1      **D.** Data abstraction.
- 3      **E.** Encapsulation.

**4. Regular languages (9 points).** Consider the set of binary strings with no repeating consecutive digits: the set consisting of the empty string, 0, 1, 01, 10, 010, 101, 0101, 1010, etc.

**A.** For each of the REs below, write YES in the blank at left if the regular expression describes all strings in this set and only strings in this set. Otherwise, write NO.

  NO    $(10)^* \mid (01)^*$

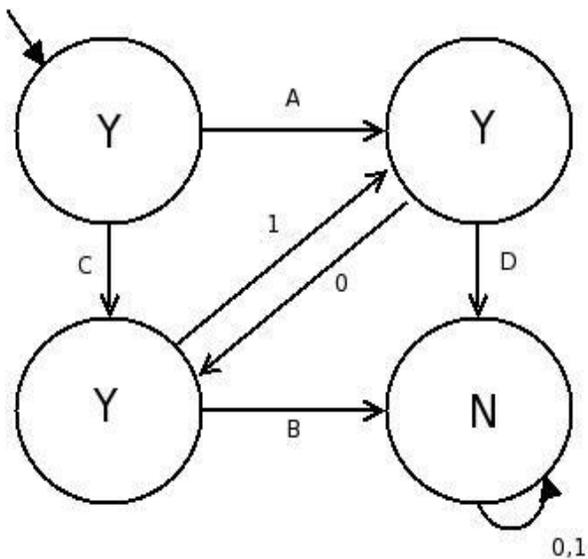
  NO    $1 \mid 0 \mid (01)^+ \mid (10)^+$

  YES    $(01)^* \mid (10)^* \mid 0(10)^* \mid 1(01)^*$

  NO    $(1 \mid 0)^* (0 \mid 1)^*$

  NO    $(1 \mid 0) \mid (01 \mid 10) \mid (01)^* \mid (10)^+$

**B.** The DFA at left below accepts the strings in the set of binary strings with no repeating consecutive digits (and only those strings) but is missing four arc labels. Provide the labels (0 or 1) for each of the arcs A, B, C, and D. Write your answers in the blanks to the left of the corresponding letters.



  1   A.

  0   B.

  0   C.

  1   D.

**5. BSTs (5 points).** Suppose that we create a BST by inserting the letters A through G into an initially empty tree. In the blank to the left of each of the following insertion orders write the height of the tree produced when keys are inserted in that order into an initially empty tree. Height is defined as the max distance from the root to any node. (e.g., A tree that has only its root and one child has height 2.) The first answer is provided for you.

A. 7 A, B, C, D, E, F, G

B. 6 B, A, C, D, G, F, E

C. 4 D, C, E, B, A, F, G

D. 3 D, B, F, A, C, E, G

E. 5 E, D, C, A, B, G, F

F. 5 C, B, D, A, E, G, F

**6. Stacks and Queues (5 points).** Consider the following Java program.

```
public class Question6
{
    public static void main(String[] args)
    {
        Stack<String> s = new Stack<String>();
        Queue<String> q = new Queue<String>();
        while (!StdIn.isEmpty())
            s.push(StdIn.readString());
        for (String str : s)
            q.enqueue(str);
        for (String str : q)
            s.push(str);
        while (!s.isEmpty())
            StdOut.print(s.pop() + " ");
    }
}
```

Which of the following is the result of running this program with

mary had a little lamb

on standard input? Assume that the stack iterator uses LIFO order and the queue iterator uses FIFO order. Circle your answer.

- A. lamb little a had mary
- B. mary had a little lamb mary had a little lamb
- C. mary had a little lamb lamb little a had mary
- D. lamb little a had mary lamb little a had mary
- E. mary had a little lamb

**7. TOY (8 points).** Consider what happens when the following TOY program is executed by pressing RUN with the program counter set to 10:

```
10: 8110   R[1] <- Mem[10]
11: 7203   R[2] <- 03
12: 1212   R[2] <- R[1] + R[2]
13: 9214   Mem[14] <- R[2]
14: 0000   Halt
15: 0000   Halt
```

A. What is the value of  $R[1]$  after the instruction at location 10 completes?

8110

B. What is the value of  $R[2]$  after the instruction at location 12 completes?

8113

C. What is the value of  $Mem[14]$  after the instruction at location 13 completes?

8113

D. What is the value of  $R[1]$  when the program halts?

9214

The program is in memory locations 10 through 15.

**8. Name game (8 points).** Match the following names with an associated phrase. Use each letter once and only once.

- |                             |         |                 |
|-----------------------------|---------|-----------------|
| <b>A.</b> Steve Cook        | ___C___ | Incompleteness  |
| <b>B.</b> Alan Turing       | ___E___ | Reductions      |
| <b>C.</b> Kurt Gödel        | ___B___ | Computability   |
| <b>D.</b> James Gosling     | ___G___ | MS Word         |
| <b>E.</b> Richard Karp      | ___A___ | NP-completeness |
| <b>F.</b> Alan Kay          | ___H___ | C++             |
| <b>G.</b> Charles Simonyi   | ___D___ | Java            |
| <b>H.</b> Bjarne Stroustrup | ___F___ | Dynabook        |

**9. Theory (11 points).** In the blanks mark each of the statements below as true (T) or false (F).

- A.   F   No RE matches a string shorter than itself.
- B.   T   Any RE without closure (\* or +) describes only finitely many strings.
- C.   F   No problem in NP can be solved in polynomial time.
- D.   T   It is possible to write a program that goes into an infinite loop if a given Java program goes into an infinite loop and terminates otherwise.
- E.   T   If P equals NP, every problem in NP is NP-complete.
- F.   F   No Turing machine can decide whether a given DFA halts on an arbitrary finite input.
- G.   T   The Church-Turing thesis cannot be proven mathematically.
- H.   T   If P equals NP, then the Traveling Salesperson Problem can be solved in polynomial time by a deterministic Turing Machine.
- I.   T   If P does not equal NP, then the Traveling Salesperson Problem is not in P.
- J.   T   Factoring is known to be in NP but has not been proven to be NP-complete.
- K.   F   The discovery of a polynomial-time algorithm for TSP would not imply a polynomial-time algorithm for factoring.

**10. Circuits (8 points).** Match each term on the left with a phrase on the right by writing a letter in each blank space. Use each letter once and only once.

- |                         |       |   |
|-------------------------|-------|---|
| A. SR flip-flop         | __H__ | holds instruction address during execution                          |
| B. multiplexor          | __G__ | performs arithmetic operations                                      |
| C. memory bit           | __A__ | two cross-coupled NOR gates   |
| D. decoder              | __F__ | holds instruction during execution                                  |
| E. control              | __B__ | selects among multiple inputs                                       |
| F. instruction register | __E__ | combinational circuit for sequencing                                |
| G. ALU                  | __D__ | sets addressed output to 1; others to 0                             |
| H. PC                   | __C__ | flip-flop with write timing control<br>and read selection mechanism |