# Data Structures and Data Types

# 4.3 Stacks and Queues



#### Collections

LIFO = "last in first out"

FIFO = "first in first out"

# Fundamental data types.

- Set of operations (add, remove, test if empty) on generic data.
- Intent is clear when we insert.
- · Which item do we remove?

#### Stack. (this lecture)

• Remove the item most recently added.

• Ex: cafeteria trays, Web surfing.

#### Queue. (see text)

• Remove the item least recently added.

• Ex: Registrar's line.

#### Symbol Table. (next lecture)

- Remove item with a given key.
- Ex: Phone book

#### Data types

- Set of values.
- Set of operations on those values.
- Some are built in to Java: int, double, char,...
- Most are not: Complex, Picture, Charge, Stack, Queue, Graph,...



#### Data structures.

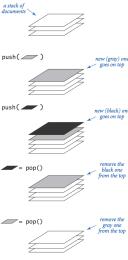
- Represent data.
- Represent relationships among data.
- Some are built in to Java: arrays, string, . . .
- Most are not: linked list, circular list, tree, sparse array, graph, . . .



# Design challenge for every data type: What data structure to use?

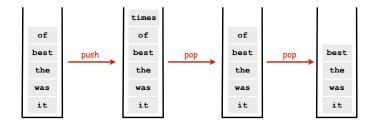
- Requirement 1: Space usage.
- Requirement 2: Time usage for data-type methods

# Pushdown Stacks



#### Stack API

# public class \*StackOfStrings \*StackOfStrings() create an empty stack boolean isEmpty() is the stack empty? void push(String item) push a string onto the stack String pop() pop the stack



# Stack Client Example 2: Test Client

```
public static void main(String[] args)
   StackOfStrings stack = new StackOfStrings();
   while (!StdIn.isEmpty())
      String item = StdIn.readString();
      if (item.compareTo("-") != 0)
          stack.push(item);
          System.out.print(stack.pop());
   System.out.println();
                            % more test.txt
                            to be or not to - be - - that - - - is
                            % java StackOfStrings < test.txt</pre>
                            to be not that or be
   to
   not
             — stack contents just before first pop() operation
   or
   be
   to
```

# Stack Client Example 1: Reverse

```
public class Reverse
  public static void main(String[] args)
      StackOfStrings stack = new StackOfStrings();
      while (!StdIn.isEmpty())
          stack.push(StdIn.readString());
      while (!stack.isEmpty())
          StdOut.print(stack.pop());
      StdOut.println();
}
                                   % more tiny.txt
                                   it was the best of times
                                   % java Reverse tiny.txt
   times
                                   times of best the was it
     of
    best
                 stack contents when
                   StdIn is empty
    the
    was
     it
```

# Stack Client Example 3: Balanced Parentheses

```
(((a+b)*d)+(e*f))
(
)
(
)
)
(
)
)
push
push
pop
push
pop
```

# Stack Client Example 3: Balanced Parentheses

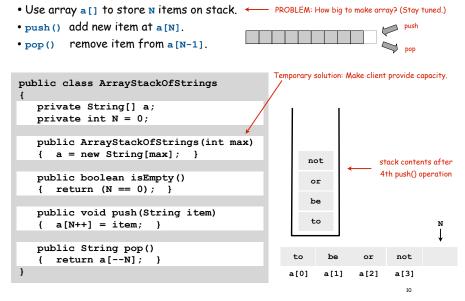
```
public class Balanced
   public static void main(String[] args)
     StackOfStrings stack = new StackOfStrings();
     while (!StdIn.isEmpty())
        String item = StdIn.readString();
        if (item.compareTo("(") == 0)
           stack.push(item);
        if (item.compareTo(")") == 0)
           if (stack.isEmpty())
           { StdOut.println("Not balanced"); return; }
           stack.pop();
     if (!stack.isEmpty()) StdOut.println("Not balanced");
                           StdOut.println("Balanced");
     else
                               % java Balanced
                               (((a+b)*d)+(e*f))
                               Balanced
                               % java Balanced
                               ((a+b)*d)+(e*f))
                               Not balanced
```

# Array Stack: Trace

	StdIn	StdOut	N	a[]				
				0	1	2	3	4
			0					
push	to		1	to				
	be		2	to	be			
	or		3	to	be	or		
	not		4	to	be	or	not	
	to		5	to	be	or	not	to
pop	-	to	4	to	be	or	not	to
	be		5	to	be	or	not	be
	-	be	4	to	be	or	not	be
	-	not	3	to	be	or	not	be
	that		4	to	be	or	that	be
	-	that	3	to	be	or	that	be
	-	or	2	to	be	or	that	be
	-	be	1	to	be	or	that	be
	is		2	to	is	or	not	to

# Stack: Array Implementation





TEQ on Stacks

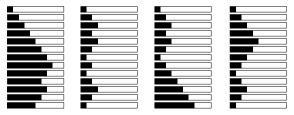
Q. Can we always insert pop commands (-) to make strings come out sorted?

Running time. Push and pop take constant time.

Memory. Proportional to client-supplied capacity, not number of items. X

#### Problem.

- API does not call for capacity (never good to change API)
- Client might have multiple stacks
- Client might not know what capacity to use (depends on its client)



Challenge. Stack implementation where space use is not fixed ahead of time.

ioi fixed unedd of finie.

Sequential vs. Linked Data Structures

Sequential data structure. Put object one next to another.

- TOY: consecutive memory cells.
- Java: array of objects.

Linked data structure. Include in each object a link to the another one.

- TOY: link is memory address of next object.
- Java: link is reference to next object.

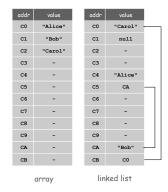
#### Key distinctions. \_\_get i<sup>th</sup> elemen

- Array: arbitrary access, fixed size.
- Linked list: sequential access, variable size.

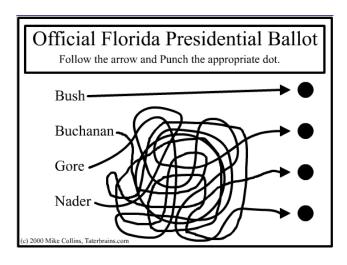
qet next element

#### Linked structures.

- Not intuitive, overlooked by naive programmers
- Flexible, widely used method for organizing data

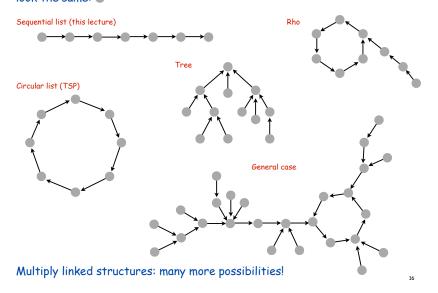


# Linked Lists



Singly-linked data structures

From the point of view of a particular object, all of these structures look the same:  $\longrightarrow$ 



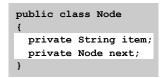
# Building a Linked List

#### Linked list.

- Simplest linked structure.
- A recursive data structure.
- A item plus a pointer to another linked list (or empty list).
- Unwind recursion: linked list is a sequence of items.

# Node data type.

- A reference to a String.
- A reference to another Node.

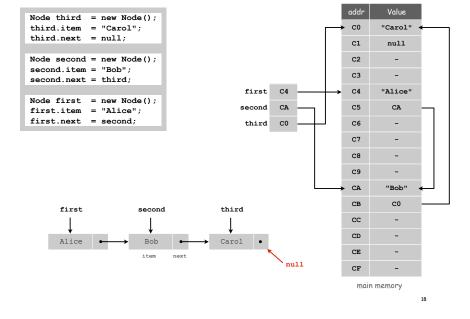


Confusing point:

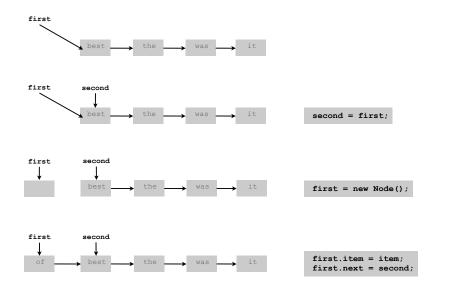
Purpose of data **structure** is to represent data in a data **type** but, we also use data **types** to implement data **structures** 



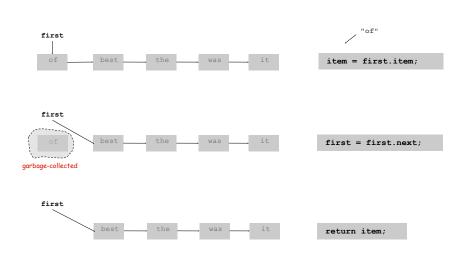
17



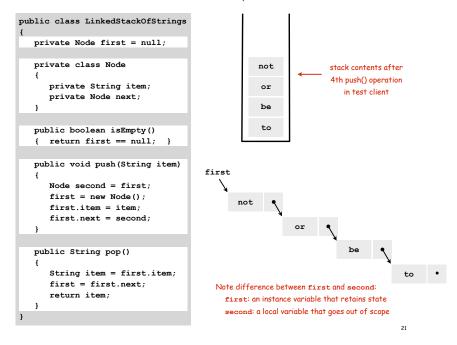
# Stack Push: Linked List Implementation



# Stack Pop: Linked List Implementation



# Stack: Linked List Implementation

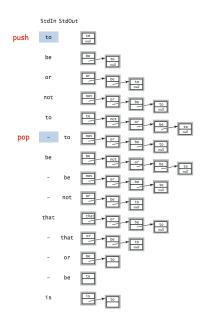


#### Linked-List Stack: Performance

Running time. Push and pop take constant time.  $\checkmark$ 

Memory. Always proportional to number of items in stack.  $\checkmark$ 

#### Linked List Stack: Trace



Stack Data Structures: Tradeoffs

22

Two data structures to implement the Stack data type.

#### Array.

- Every push/pop operation take constant time.
- But... must fix maximum capacity of stack ahead of time.

#### Linked list.

- Every push/pop operation takes constant time.
- But... uses extra space and time to deal with references.

Client can evaluate performance tradeoffs to choose among implementations (implicitly choosing among underlying data structures)

# What does the following code do?

```
Node list = null;
while (!StdIn.isEmpty())
{
   Node old = list;
   list = new Node();
   list.item = StdIn.readString();
   list.next = old;
}
for (Node t = list; t != null; t = t.next)
   StdOut.println(t.item);
...
```

# What does the following code do?

```
Node list = new Node();
list.item = StdIn.readString();
Node last = list;
while (!StdIn.isEmpty())
{
   last.next = new Node();
   last = last.next;
   last.item = StdIn.readString();
}
```

# Parameterized Data Types

# Parameterized Data Types

We implemented: StackOfStrings.

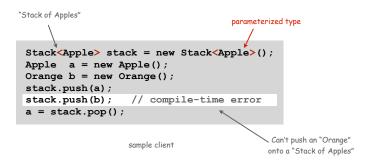
We also want: StackOfMemoryBlocks, StackOfURLs, StackOfInts, ...

Strawman. Implement a separate stack class for each type.

- Rewriting code is tedious and error-prone.
- Maintaining cut-and-pasted code is tedious and error-prone.

#### Generics

Generics. Parameterize stack by a single type.



# Autoboxing

Generic stack implementation. Only permits reference types.

#### Wrapper type.

- Each primitive type has a wrapper reference type.
- Ex: Integer is wrapper type for int.
- Wrapper type has larger set of operations than primitive type.
- Values of wrapper type are objects.

Autoboxing. Automatic cast from primitive type to wrapper type. Autounboxing. Automatic cast from wrapper type to primitive type.

```
Stack<Integer> stack = new Stack<Integer>();
stack.push(17);
                       // Autobox
                                     (int -> Integer)
int a = stack.pop();
                     // Auto-unbox (Integer -> int)
```

# Generic Stack: Linked List Implementation

String stack (for reference)

```
public class LinkedStackOfStrings
  private Node first = null;
  private class Node
     private String item;
     private Node next;
  public boolean isEmpty()
   { return first == null; }
  public void push (String item)
     Node second = first;
     first = new Node();
     first.item = item;
      first.next = second;
  public String pop()
     String item = first.item;
     first = first.next;
     return item:
```

```
public class Stack<Item>
   private Node first = null
   private class Node
                                     arameterized
                                     type name
      private Item item;
                                     chosen by
      private Node next;
                                     programmer
   public boolean isEmpty()
   { return first == null,
  public void push (Item item)
      Node second = first;
      first = new Node();
      first.item = item;
      first.next = second;
  public Item pop()
      Item item = first.item;
      first = first.next;
      return item;
```

# Stack Applications

#### Real world applications.

- Parsing in a compiler.
- Java virtual machine.
- Undo in a word processor.
- Back button in a Web browser.
- PostScript language for printers.
- Implementing function calls in a compiler.

# Stack Client 4: Arithmetic Expression Evaluation

Goal. Evaluate infix expressions.

value stack operator stack

```
( 1 + ( ( 2 + 3 ) * ( 4 * 5 ) ) ) ^{\uparrow}_{\text{operand}}
```

### Two stack algorithm. [E. W. Dijkstra]

- Value: push onto the value stack.
- Operator: push onto the operator stack.
- Left parens: ignore.
- Right parens: pop operator and two values; push the result of applying that operator to those values onto the operand stack.

33

#### Correctness

Why correct? When algorithm encounters an operator surrounded by two values within parentheses, it leaves the result on the value stack.

```
(1+((2+3)*(4*5)))
```

So it's as if the original input were:

Repeating the argument:

Extensions. More ops, precedence order, associativity, whitespace.

```
1 + (2 - 3 - 4) * 5 * sqrt(6*6 + 7*7)
```

# Arithmetic Expression Evaluation

```
public class Evaluate
   public static void main(String[] args)
      Stack<String> ops = new Stack<String>();
     Stack<Double> vals = new Stack<Double>();
      while (!StdIn.isEmpty())
        String s = StdIn.readString();
                 (s.equals("("))
        else if (s.equals("+"))
                                    ops.push(s);
        else if (s.equals("*"))
                                    ops.push(s);
        else if (s.equals(")"))
           String op = ops.pop();
                    (op.equals("+"))
              vals.push(vals.pop() + vals.pop());
           else if (op.equals("*"))
               vals.push(vals.pop() * vals.pop());
        else vals.push(Double.parseDouble(s));
      StdOut.println(vals.pop());
                                    % java Evaluate
                                    (1+((2+3)*(4*5)))
                                    101.0
```

#### Postfix

Observation 1. Remarkably, the 2-stack algorithm computes the same value if the operator occurs after the two values.

```
(1((23+)(45*)*)+)
```

Observation 2. Now all of the parentheses are redundant!

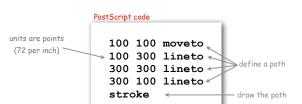
```
1 2 3 + 4 5 * * +
```

Bottom line. Postfix or "reverse Polish" notation.

# Real-World Stack Application: PostScript

#### PostScript (Warnock-Geschke, 1980s). A turtle with a stack.

- postfix program code
- add commands to drive virtual graphics machine
- add loops, conditionals, functions, types



# Simple virtual machine, but not a toy.

- · Easy to specify published page.
- Easy to implement on various specific printers
- Revolutionized world of publishing.
- Virtually all printed material is PostScript.



20

Context/Definitions/Summary

TOY is our proxy for a real machine

#### Interpreter.

- Takes a program as input
- Does what that program would do.
- Simulates a virtual machine.



#### Compiler.

- Takes a program as input
- Produces a program as output.
- Produces code for a (real) machine.



# Data Type and Virtual Machine are the same thing!

- Set of values = machine state.
- Operations on values = machine operations.

#### Virtual machines you have used

- LFSR
- Stack
   TOY
- PostScript
- Java Virtual Machine (another stack machine)

#### Data Structure.

- Represent data and relationships among data in a data type.
- array, linked list, compound, multiple links per node

36

TOY code